

Showing Connections between Investment and City Growth

Merging statistical and clustering approaches to study growth

Springboard DSI Capstone Project
Final Report by Fernando Meira
July, 2017

ABSTRACT

The debate on measuring growth and comparing different countries and cities is vast. For a long time in sciences, different ways of doing it have been developed. As the times pass, the globalization and the fast-growing world shows that measuring growth is getting more complex each year. This complexity is due to more features that should be taken into consideration and methods that would embrace this multidimensionality in a more natural way. This study is an attempt on tackling the multidimensionality using the I-Distance method and clustering to check the extent to which investment is relevant for city growth and explore the subtleties of development within the province of São Paulo, Brazil.

1. INTRODUCTION

In this section, we are going to cover the foundations of this study. First we are going to frame the actual debate on how to measure growth and development in countries, which also encompasses the measurement of related cities within the same country. Second, we are going to introduce the main method used for this project, called I-Distance, explaining the method workflow and its particularities. Finally, we are going to discuss the relevance of this study in the context of Brazil and thereby identifying the specific client for this project, for whom recommendations are suggested at the end of this document.

1.1 The challenges associated with measuring growth

What methodologies to use to measure growth is a topic that is amply debated in Economics and Social Sciences. Most of the approaches used in this type of studies, during many years, have been focused on just economic aspects. The most used parameter for these has been the GDP (Gross Domestic Product), which is a monetary account for all the wealth generated in a country. Although this measure can be used to rank countries by their wealth, it has been very poor to capture socio-economic gaps within the subjects of study.

A first attempt for a 'multidimensional' approach started with the creation of the HDI (Human Development Index), by the The World Bank in 1990. This index consists of grouping 3

major indicators: education, income and longevity. Given its simplicity, this index was very popular during a long period but, according to many researchers, it has been criticized because of the large correlation among the indicators and its small number. This oversimplification raised the concern that this index would not capture nuances of the country's development when looking to different countries, and as consequence, different scenarios.

As a response to the concerns raised above, some other versions of the index have been created in order to try to fix these issues, and to try to get more accurate modelling of growth. The most relevant include the following. CDI (Calibrated Human Development Index) which is very similar to HDI but it gives more weight to life expectancy than to education. Another similar is the resource–infrastructure–environment (RIE) index, which attempts to capture structural concerns that are relevant to the characterization of development, including ICT infrastructure variables. Other variables could be added such as internet access and similar indicators associated with technology use.

This is na indication that the world nowadays is getting multidimensional really fast and the addition of different features to growth models is going to get more usual than ever. Because of that, approaches that could deal with this multidimensionality in a more natural way, should be of enormous importance within this study field.

1.2 The I-Distance Method

Considering all the discussion above, the focus for this study was the choice of a multidimensional method that could capture the interaction of different variables on growth, giving the opportunity to check the relative relevance of each of them. The I-Distance method used in this present study was introduced by Milenkovic and other in [1].

The main idea of this method is to use hyperplanes, composed by a given group of chosen variables, to then compare growth between countries (and in our case, cities) by using the distance between different planes. Entities of interest would be represented by the values of choosen variables, through the hyperplane representation, and they would be compared to a unique hyperplane referred to by the authors as the “reference entity”. This reference entity could represent different types of benchmarks that would serve as a baseline for the comparison among the entities. The reference entity could be, for example, the hyperplane computed with the values that can be summarized by using minimum, mean or maximum values.

Given the selected features $X^T = (X_1, X_2, \dots, X_k)$ the I-distance between $e_r^T = (X_{1r}, X_{2r}, \dots, X_{kr})$ and $e_s^T = (X_{1s}, X_{2s}, \dots, X_{ks})$, defined as follows:

$$D(r, s) = \sum_{i=1}^k \frac{|d_i(r, s)|}{\sigma_i} \prod_{j=1}^{i-1} (1 - r_{ji.12\dots j-1})$$

where $d_i(r, s)$ is the distance between the values of variable X_i for e_r and e_s e.g. the discriminate effect,

$$d(r, s) = x_{ir} - x_{is}, i \in \{1, \dots, k\}.$$

σ_i the standard deviation of X_i , and $r_{ji.12 \dots j-1}$ is a partial coefficient of the correlation between X_i and X_j , ($j < i$).

The I-Distance between the observations and the reference would be given by the discriminate effect divided by the standard deviation of that variable, multiplied by 1 minus the correlation between those variables (which would imply in the “pure” effect of that variable).

In some sets, negative correlation effects and negative partial correlation effects could occur, mainly in scenarios with reduced number of variables, it would be interesting the use of the I-Distance squared, which is given by:

$$D^2(r, s) = \sum_{i=1}^k \frac{d_i^2(r, s)}{\sigma_i^2} \prod_{j=1}^{i-1} (1 - r_{ji.12 \dots j-1}^2)$$

There is a second important part of the I-Distance method, which is one of the main points for this project: the possibility of measure the relevance of each variable for the index calculation.

After the calculation of the I-distance, the correlation effect of each variable with the I-distance is calculated. This correlation should be interpreted as the relevance of that variable for the distance index: the bigger the correlation, the most representative that feature is.

Then, after the rank is computed, we choose the smallest correlation value that is not significant. This variable will be excluded from the model, and the calculation (the distance index and the following correlation between features and distance) will be computed again. This process should be repeated until just significant variables remains. By the end, a rank of the most relevant features should remain, indicating only the variables that are relevant for measuring growth for that set.

1.3 K-Means clustering

The K-Means is in summary a method to classify data into K different clusters, where the value of K is defined *a priori*. K initial centroids are set far as possible from each other and the data points are distributed to each nearest centroid.

After this first arrangement, each cluster has its centroids recalibrated to assume the very barycenter of that centroid, and these K centers are relocated and the data points distributed

again. This process is done until no more move by the centroids are done, and the clustering is given by last iteration.

When considering the K-Means method in the context of this project, the main approach is to use the clustering method, in addition with the I-Distance ranking values, to look for patterns in growth behaving within the province of São Paulo. This should assume the form of different groups of cities that should share some similarities when considering growth as a whole and would allow as to make some comparisons, not just in individual level of characteristics, but in a group level too.

1.4 Measuring growth of cities

All of the methods discussed above were conceptualized using countries as the entities to be compared. The concern in considering all of the important aspects related to the development of nations so they can be compared by using a common metric.

This elementary question is possible because, as we know, each country has it's own particularities, and it's own data that describe its situation. This is very similar when we move to the issue of discussing the growth of cities within the same country. It is very common, mainly in medium-size to big countries (like the case of Brazil), to select two cities that belongs to the same province but have very different situation with respect to culture, economic growth, healthcare, etc.

So, in our case, once we have all the data that describe these particularities, it is reasonable to extend this methods used for countries growth, to model growth of cities within the same country.

1.5 The relevance of the study and the client

Currently, Brazil seems to be drowning in corruption scandals at various levels. One of the main concerns is the management of public resources and the effect of what is promised and what is built on these promises.

One of the main questions that this study aims to answer is the relevance of investment variables (public and private) in the growth of the cities of the São Paulo province, which might also offer some insights into aspects related to corruption.

The main client for this study is the Office of the Public Governor of the province which could, using the results from this project, measure the relevance of the investment as a policy for growth and balance the distribution of this incentive. We could say that the population of the cities and the province could be an additional stakeholder, who could use the results of this project as an argument for requesting a fairer distribution of resources.

2. DATA SET

2.1 Data Presentation

The data set used for this study was merged from two sources:

Investment (public and private) values by year:

<http://dados.gov.br/dataset>

The rest of the features (demographics, social, economic, etc.):

<http://www.imp.seade.gov.br/>

The data ranged from the years 2000 to 2016 for all the 645 cities of the province of São Paulo, Brazil. The features of choice were based on the main pillars of growth that are: education, economics, demographics, and social. The complete list of features follows:

Group	Indicator	Source
Demographic Indicators	Population density	IMP Seade - São Paulo
	Electric energy consumption in Mwh	IMP Seade - São Paulo
	Number of people	IMP Seade - São Paulo
	Number of people living on urban areas	IMP Seade - São Paulo
	Number of people living in rural areas	IMP Seade - São Paulo
	Olding Index (%)	IMP Seade - São Paulo
	Proportion of urban population (%)	IMP Seade - São Paulo
Economic Indicators	GDP per capital (R\$)	IMP Seade - São Paulo
	GDP growth (last year - current year) (%)	IMP Seade - São Paulo
	Value Invested by private companies (Million R\$)	Dados Gov
	Value Invested by public government (R\$)	Dados Gov
	Exportation Values (U\$ FOB)	IMP Seade - São Paulo
	Importation (U\$ FOB)	IMP Seade - São Paulo
	Total Value Added in thousands R\$	IMP Seade - São Paulo
	Total Value Added by agriculture in thousands R\$	IMP Seade - São Paulo
	Total Value Added by industry in thousands R\$	IMP Seade - São Paulo
	Total Value Added by services in thousands R\$	IMP Seade - São Paulo
	Total Revenue by Taxes	IMP Seade - São Paulo
	Number of jobs generated	IMP Seade - São Paulo
	Mean jobs income	IMP Seade - São Paulo
Education Indicators	Number of enrolls in undergraduation	IMP Seade - São Paulo
	Number of enrolls in primary school	IMP Seade - São Paulo
	Number of enrolls for the fundamental school	IMP Seade - São Paulo
Social Indicators	Number of policial records by 1000 habitants	IMP Seade - São Paulo
	Human Development Index	IMP Seade - São Paulo
	Total number of hospital rooms	IMP Seade - São Paulo
	Mean number of hospital rooms per habitant	IMP Seade - São Paulo

2.2 Data Exploration

The following descriptions and outcomes are available in the Jupiter notebook, available in this capstone project's repository.

2.2.1 Reading the data

The data set was available on a csv file called SPcities2.csv. All the manipulation and wrangling was done using Pandas.

2.2.1 Cleaning the data

The main question when exploring the data was to setup the best scenario to apply the I-Distance method. This scenario would be the year with the most data available, so the distance could be more accurate concerning all the features.

The focus for this analysis was on the three main variables for the study: GDP per capita, public and private investment.

When looking to GDP per capita missing values we could see:

```
year
2000    0.0
2001    0.0
2002   645.0
2003   644.0
2004   645.0
2005   645.0
2006   645.0
2007   645.0
2008   645.0
2009   645.0
2010   645.0
2011   645.0
2012   645.0
2013   645.0
2014   645.0
2015    0.0
Name: gdp_per, dtype: float64
```

Figure 1: Number of entries for GDP per capita variable, per year

Here we could conclude that 2000, 2001 and 2015 were years that should not be used to this analysis, once there were no entries for any one of them.

Going a little deeper and trying to see the year with the best combination for the three variables mentioned above, we could see a clear choice as the plot below shows:

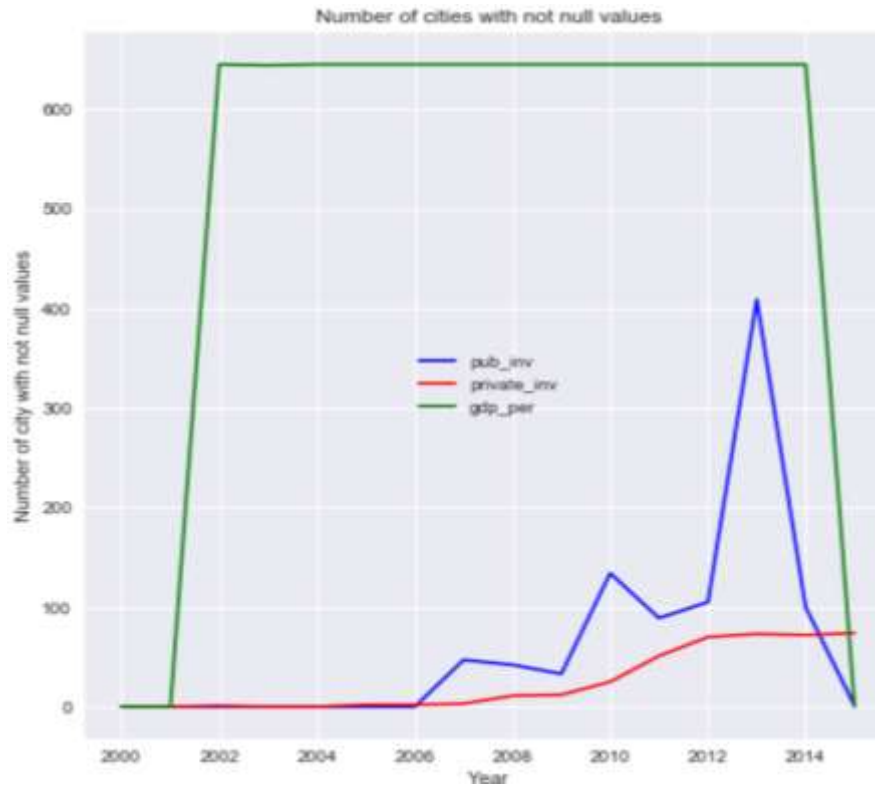


Figure 2: Number of entries for the 3 main features, by year

Looking at this plot the scenario is set. For GDP per capita we can choose from 2001 to 2014, as we seen above. But for investment, our best chance is located in 2013, once that private investment is in its top level, and public investment reaches its peak too.

Since year of 2013 is a clear choice, our final check would be in the values availability for the other features in the data set.

city	645
year	645
gdp_per	645
gdp_growth	645
private_inv	73
pub_inv	409
export	354
import	377
violence	645
HDI	0
educ_superior	0
primary_enrolls	645
density_pop	645
value_add	645
agriculture_add	644
industry_add	645
services_add	645
eletricity	645
tax_revenue	0
hosp_rooms	358
hosp_rooms_per	358
jobs	645
jobs_revenue	645
population	645
urban_pop	645
rural_pop	615
olding	645
urbing	645
fundamental	645
dtype: int64	

Figure 3: Data entries for all the features in the year of 2013

When looking to the Figure 3 we could see that 3 features need to be dropped: HDI, educ_superior and tax_revenue, once that anyone of them have values. For the other variables, we can see that there are plenty of values to maintain them, even the private investment that, besides of the fact that it has a small amount of values, it is a crucial variable to the project,

After this cleaning and dropping the 3 features above, the data set was ready for further analysis.

3. RESULTS

3.1 Defining the Reference Entity

As defined above, the reference entity is the foundation for the calculation of the I-Distance index. Among the many possibilities for this element, in this project the focus was entirely on the indicator GDP per capita. This was the case because the GDP per capita, besides of the fact that is a very used parameter in another growth studies, it resumes a decent part of wealth distribution because of its 'normalization' by the number of habitants.

Another important fact was that, for this project, the reference entity was chosen to be a real city, which could assume a more real point of comparison than taking the mean or median of all indicators. Following this thought, the city of Itapirapuã Paulista was chosen because it

has the smallest number for GDP per capita among all the cities in the studied period. This implies that cities with great values of I-Distance will reflect, by the definition of this metric, cities far from the reference and as consequence, cities with more growth.

As result, the reference entity vector would assume this form:

Indicator	Value
city	Itapirapuã Paulista
year	2013
gdp_per	6956,9
gdp_growth	0,098175775
private_inv	NaN
pub_inv	917044,27
export	NaN
import	NaN
violence	12
HDI	NaN
educ_superior	NaN
primary_enrolls	102,25
density_pop	9,73
value_add	26929,78
agriculture_add	3766,22
industry_add	1356,65
services_add	21806,9
eletricity	2302
tax_revenue	NaN
hosp_rooms	NaN
hosp_rooms_per	NaN
jobs	521
jobs_revenue	1266,38
population	3954
urban_pop	1959
rural_pop	1995
olding	42,32
urbing	49,54
fundamental	64

Table 1: Values of the reference for each indicator

3.2 Choosing between two versions of the I-Distance method

As defined above, the I-Distance method was the main tool for this analysis. Recall there are two ways of using the I-Distance method: the squared version, and the not squared one.

The not squared version is clearly more sensitive, to big differences in variable values and small number of data (or features), which could affect the final results. To check for the

difference in the results, the two versions were applied and the ‘sensitivity’ of the not squared method is clear as seen in the table below:

Method	Number of iterations	Number of excluded features	Features that remained
<i>Not Squared</i>	20	20	gdp_growth; gdp_per; density_pop; urbing
<i>Squared</i>	7	7	violence; jobs; services_add; valued_add; urban_pop; population; hosp_rooms; fundamental; pub_inv; electricity; industry_add; rural_pop; import; export; density_pop; jobs_revenue; gdp_per

Table 2: Number of iterations and excluded features for the I-Distance calculation

As we can see, the not squared version eliminated big part of the features that, in the squared version, remained. This is taken as a negative point for this model, once that the main interest of the study is to check for the features that contribute more to growth and how they contribute to it. In addition to this, for the rank of the features of the not squared version, we can see:

	feature	p-value	r
1	gdp_growth	2.519221e-61	0.588352
2	gdp_per	1.639504e-08	0.220019
3	density_pop	3.476726e-02	-0.083140
4	urbing	7.199990e-05	-0.155650

Figure 4: Rank of features relevance for the not squared I-Distance

Since the ‘r’ column reflects the correlation of that feature with the I-Distance calculation (as defined in the introduction section), hence the contribution of that variable, for “density_pop” and “urbing” features we have a negative ‘r’, which makes the interpretation difficult, once that these variables are still significant. It is important to say here that, the p-value in this context represents the probability of finding the value on the table above if in fact the value of ‘r’ were 0.

Then we can conclude here that we should focus more on the squared version.

3.3 The results of the squared I-Distance method

As mentioned before, for this version of the method, 7 iterations were needed and the following variables were excluded as non-significant, in this order: olding, agriculture_add, gdp_growth, hosp_rooms_per, primary_enrolls, private_inv and urbing.

Taking the first look at the features, we can see the rank of relevance as follows:

	feature	p-value	r
1	violence	0.000000e+00	0.990580
2	jobs	0.000000e+00	0.989353
3	services_add	0.000000e+00	0.985795
4	value_add	0.000000e+00	0.982313
5	urban_pop	0.000000e+00	0.978691
6	population	0.000000e+00	0.978607
7	hosp_rooms	0.000000e+00	0.976214
8	fundamental	0.000000e+00	0.972127
9	pub_inv	0.000000e+00	0.951517
10	electricity	8.198462e-314	0.944806
11	industry_add	4.002641e-288	0.933264
12	rural_pop	4.962174e-113	0.740399
13	import	1.767463e-86	0.673588
14	export	3.427779e-85	0.669827
15	density_pop	8.103492e-13	0.276907
16	jobs_revenue	3.553167e-05	0.162043
17	gdp_per	1.193716e-02	0.098937

Figure 5: Rank of features relevance for the squared I-Distance

One of the most interesting points that we are seeking in this project is to check the relevance of investment variables in the calculations. As we can see, the private investment was dropped in the sixth iteration. This implies that, for this scenario, the private investment was not important for the growth of the cities. On the other hand, the public investment figured as a relevant feature, located in the middle of the rank. Another interesting result concerning the features, is that, although we have a lot of economic features in the top of the rank (jobs, service_add, value_add) the top feature was the violence indicator. This is a very interesting finding, given that violence is one of the main weak points of the public management in many cities of all the country.

For the rank of cities we have:

	I-Distance	city
1	5420.100823	São Paulo
2	253.370130	São Sebastião
3	150.584562	São José dos Campos
4	142.742285	Ilha Comprida
5	120.551111	São Bernardo do Campo
6	114.357130	Diadema
7	112.603475	Santos
8	112.293461	Louveira
9	104.851029	Taboão da Serra
10	102.321066	Barueri
11	100.644117	Osasco
12	91.586236	São Caetano do Sul
13	87.955723	Guarulhos
14	85.668883	Campinas
15	78.343459	Carapicuíba
16	58.143407	Paulínia
17	43.994971	Alumínio
18	41.225816	Jundiaí
19	40.666734	Sorocaba
20	39.531636	Mauá
21	36.173007	Santo André
22	35.980659	Jaguariúna
23	34.704392	Piracicaba
24	33.638510	Cajamar
25	32.175117	Cubatão

Figure 6: Rank of cities for the squared I-Distance (best positioned cities)

For the cities, we can see that a very good reality check for the index is that the city of São Paulo is on the top of the rank. São Paulo is a very big city, it has a lot of global companies installed, it is a crucial point for the financial industry of the country, and it is clearly an outlier in the province. Other cities that are natural candidates to be placed in the best positions of the rank are there, like: Campinas, São José dos Campos, Santos, Guarulhos and Osasco. These cities are relative big, well positioned in the logistics scheme for industries and core technology development centers within the province and even within the country. Other cities of the province that are not that relevant when looking to common parameters like São Sebastião, Ilha Comprida and Louveira, are big surprises here and should be a very interesting start point when looking through the implications of their position and the parameters they have.

3.4 Merging the I-Distance method with clustering

When looking for growth contributors and ranking cities, one of the most common questions would be if there are patterns or related groups of cities that would make sense geographically, economically or even demographically.

To tackle this point, the purpose here was to use clustering methods (K-means) to combine the index explored above and look for patterns within the province.

The number of centroids (K) was chosen using the Elbow method. The number chosen was 5, and this choice is clear when looking the following plot:

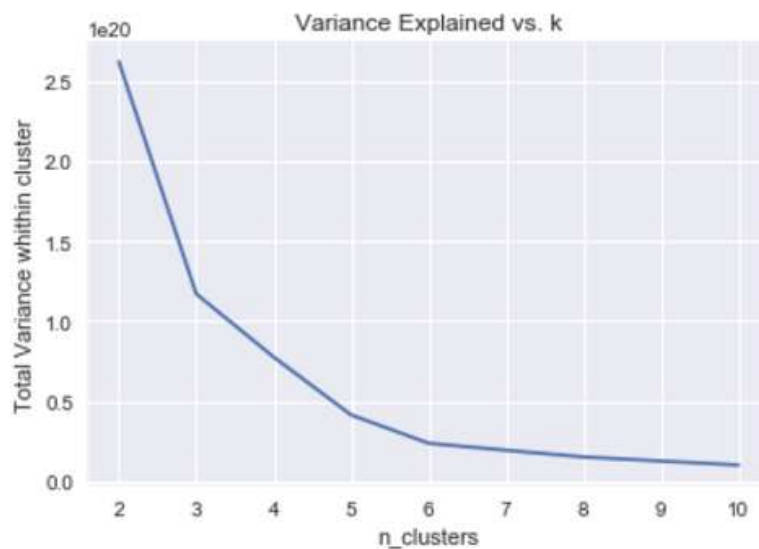


Figure 7: Variance explained versus the number of centroids chosen

With the optimal number of centroids chosen, the clusters are shown in the following figure:

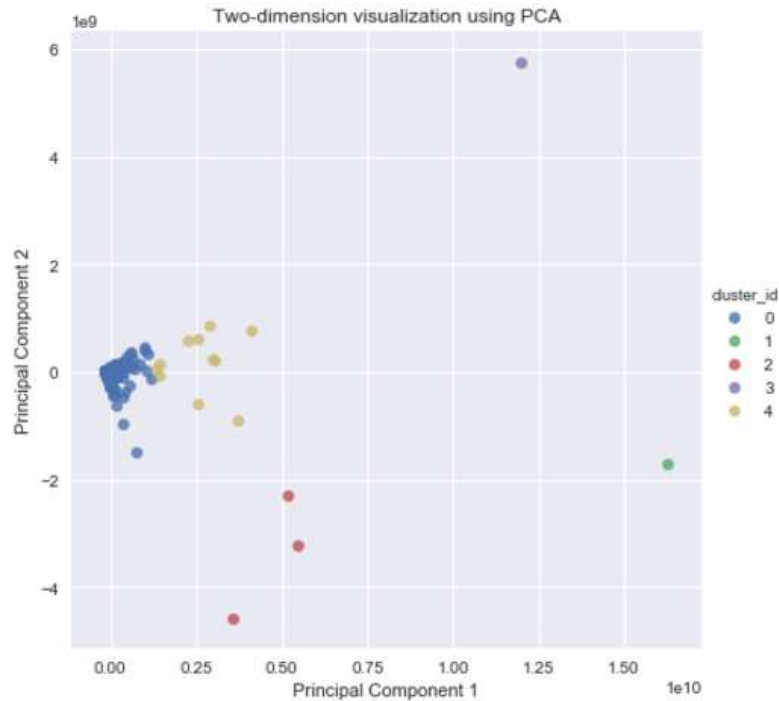


Figure 8: The distribution of the clusters using all the features

For the visualization of the Figure 8 to be possible in a two-dimension plot, a Principal Component Analysis (PCA) was performed. In a brief explanation, PCA is an algorithm to reduce the dimensionality of a data set. The main idea is reduce dimension using variables that are correlated (heavily or lightly), transforming the correlated variables in new set of variables (called principal components) and preserving the variation of the data as maximum as possible. For the Figure 8, a PCA, consisting of 2 principal components, was computed, reducing the dimension of the dataset to 2 and making possible the two-dimension visualization of the data.

Looking to the figure above it's clear why the number of 5 cluster is the optimal solution. There are clearly 5 different groups and the calculations for most representative cities for the centroids shows:

Cluster_id	Most representative city	I-Distance Squared Rank
0	Porto Feliz	228
1	São Paulo	1
2	Taubaté	29
3	São Sebastião	2
4	São José dos Campos	3

Table 3: Cluster most representative cities

The 'one-city' clusters are represented by São Paulo (for cluster 1) and São Sebastião (cluster 3). This seems to be natural for the case of the city of São Paulo, that is a clear outlier. When looking to the case of the cluster represented by the city of São Sebastião, this is not so clear, considering that it is a medium city, located in the coast of the province and far from the port infrastructure that is in the south part of the coast. However, these two cities are ranked as the best two cities when considering the index, even with a big edge separating them. This implies that, in spite of the territory size or infrastructure, the complete set of feature should be considered, and even more, this single fact helps corroborating the assumption that growth must take into account multiple metrics.

	Cluster	I-Distance	city
4	0	142.742285	Ilha Comprida
6	0	114.357130	Diadema
8	0	112.293481	Louveira
9	0	104.851029	Taboão da Serra
11	0	100.644117	Osasco
12	0	91.586236	São Caetano do Sul
15	0	78.343459	Carapicuíba
17	0	43.994971	Aluminio
20	0	39.531636	Mauá
22	0	35.980859	Jaguariúna
24	0	33.638510	Cajamar
228	0	1.809157	Porto Feliz

Figure 9: Rank of cities for the squared I-Distance (best positioned cities) for cluster 0 with cluster centroid in highlight

	Cluster	I-Distance	city
1	1	5420.100823	São Paulo

Figure 10: Rank of cities for the squared I-Distance (best positioned cities) for cluster 1 with cluster centroid in highlight

	Cluster	I-Distance	city
3	2	150.584562	São José dos Campos
5	2	120.551111	São Bernardo do Campo
7	2	112.603475	Santos

Figure 11: Rank of cities for the squared I-Distance (best positioned cities) for cluster 2 with cluster centroid in highlight

	Cluster	I-Distance	city
2	3	253.37013	São Sebastião

Figure 12: Rank of cities for the squared I-Distance (best positioned cities) for cluster 3 with cluster centroid in highlight

	Cluster	I-Distance	city
10	4	102.321066	Barueri
13	4	87.955723	Guarulhos
14	4	85.668883	Campinas
16	4	58.143407	Paulínia
18	4	41.225816	Jundiaí
19	4	40.666734	Sorocaba
21	4	36.173007	Santo André
23	4	34.704392	Piracicaba
29	4	26.810150	Taubaté
36	4	19.950008	Sumaré
41	4	15.174380	Indaiatuba

Figure 13: Rank of cities for the squared I-Distance (best positioned cities) for cluster 4 with cluster centroid in highlight

On the other hand, when looking to the question on whether investment (in this case the public, that was the only that remained in the model) is relevant to the growth of this cities, we can have very interesting insights grouping the cities with the cluster labels and comparing these as different groups.

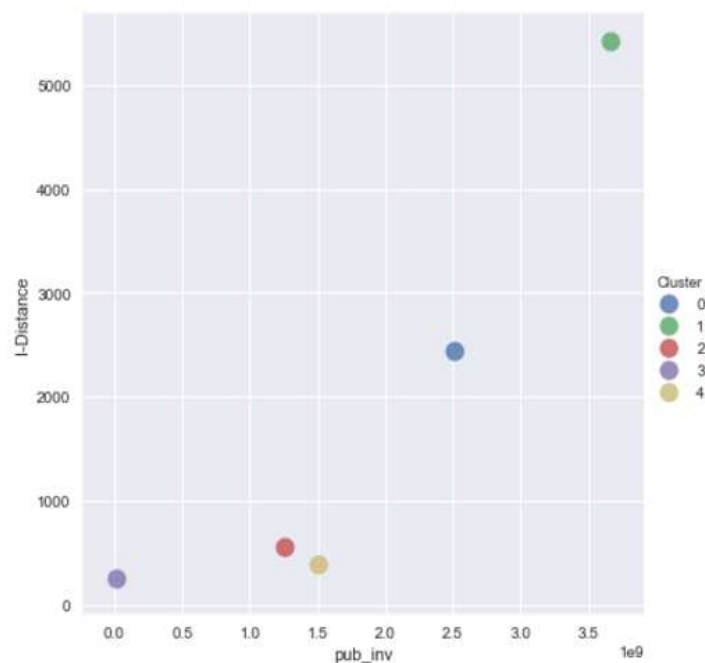


Figure 10: Scatter plot of the sum of I-Distance and public investment by cluster

In spite of the fact that cluster 0 groups the largest number of cities, there is a clear visual relationship where, the clusters with more absolute value of investment have better index. However, we should admit that, when using the mean or median (as shown in Figure 10), to normalize this distribution effect, the relationship is way subtler.

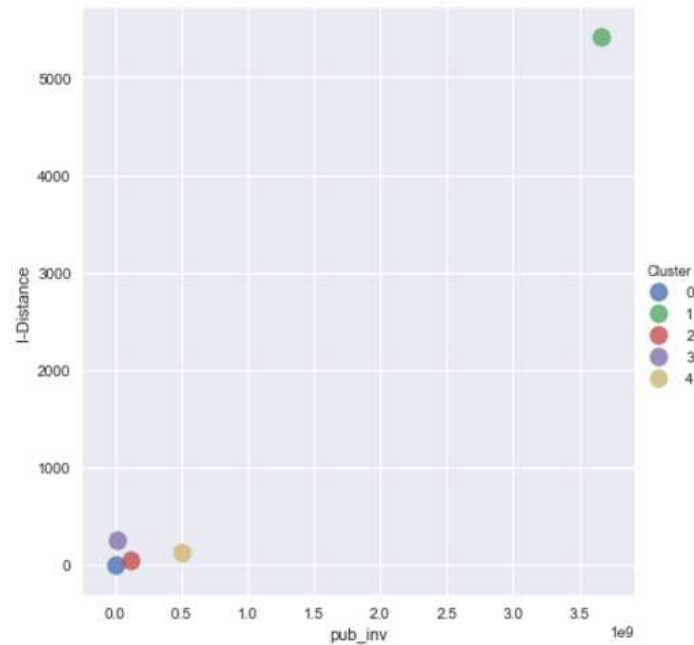


Figure 11: Scatter plot of the mean of I-Distance and public investment by cluster

4. CONCLUSION

This project explored the question of the extent on which investment is relevant to city growth, and as consequence, how growth differs from city to city (or group of cities).

Using the I-Distance as a unifying metric, it seems that private investment was not relevant in any of the scenarios we explored. However, public investment is shown to be relatively important. Moreover, when looking at the clusterings, public investment seems to be one good approach to differentiate city growth, when considering different types of cities within the province (according to the features used in this project).

The models we built using the concept of I-Distance, and its combination with clustering were relatively good, positioning cities with theoretical growth in expected places and also showing cities that are not on the radar of many public agents, but should be studied at a deeper level.

5. FUTURE WORK

Possible points for further development include the following.

- Take a deeper look at features other than investment that are relevant to the clusters found.

- A deeper study of the high positioned cities that were not expected and check which attributes made them go higher than others.
- Add more features related to technology, such as internet access.
- Look to more recent years that should have more entries for the private investment feature, to confirm if it is not relevant as found in this study.

6. RECOMMENDATIONS FOR THE CLIENT

As part of the recommendations for the client, we would like to highlight the following:

- Better management on public investment funding, since it seems to have relative relevance for cities growth.
- Look for benchmarks outside the most known cities, considering different features in the analysis.
- Take a closer look at violence indicators, since it was classified as the most important features on the subset studied.

6. CONSULTED REFERENCES

[1] N. Milenkovic, et alia: "A multivariate approach in measuring socio-economic development of MENA countries". In Economic Modeling 38 (2014) 604-608. Available from <http://www.sciencedirect.com/science/journal/02649993/38>

[2] J. Bang, et alia: "New Tools for Predicting Economic Growth Using Machine Learning: A Guide for Theory and Policy".. Available from: https://www.researchgate.net/publication/291827961_New_Tools_for_Predicting_Economic_Growth_Using_Machine_Learning_A_Guide_for_Theory_and_Policy

[3] N. Adriansson, et alia: "Forecasting GDP Growth, or How Can Random Forests Improve Predictions in Economics? ". Available from: <https://pdfs.semanticscholar.org/d402/473ba628b67bcd0d3a8cf39799ae6efbdc66.pdf>

