Module IV - Basic Analysis

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Loading data from multiple sources

- Local network data files
- Connecting to a database
- Building directly from the Internet

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Brief review of Python dictionaries

- ▶ Why is the dict so useful?
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- Degree, Closeness, Betweeness Eigenvector
- Calculating degree distribution
- ▶ Plotting statistics using matplotlib
- Calculating cliques, clustering and transitivity

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Basic visualization

- Review of NetworkX's plotting algorithms
- Adding analysis to visualization

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Let's try!

- ▶ We will load the edge list of Hartford drug users network
- ▶ Specify that the network be a directed graph, and the nodes be integers
- ▶ Use info() to check that data has been loaded correctly

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It's time to fire up your console and load Python!

Starting NetworkX and loading data

```
>>> from networkx import *
>>> hartford=read_edgelist("../../data/hartford_drug.txt",create_using=DiGraph(),nodetype=int)
>>> info(hartford)
```

Name:

Type: DiGraph
Number of nodes: 212
Number of edges: 337
Average in degree: 1.5896
Average out degree: 1.5896

Local network data

Loading the Hartford drug users network

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What did we just do?

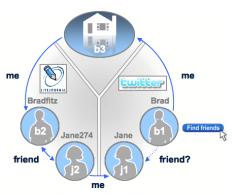
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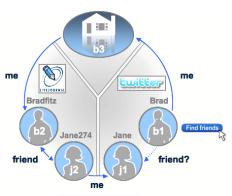
Some formats may have more or less options, always check the documentations!

Building a network from a database

As data sets become larger and persistently changing, it may make more sense to store them in a database rather than a single file

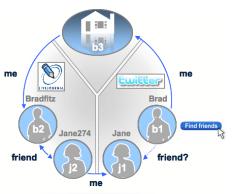
 As we have seen, Python provides binding to many modern database frameworks



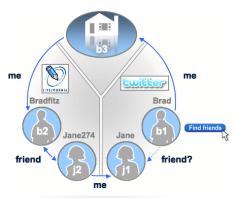


Perhaps the most powerful aspect of NetworkX is its ability to work in Python to generate networks from live-streaming data

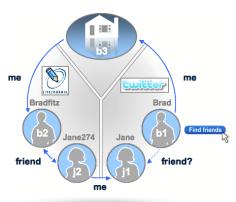
 In Python, use NetworkX, cjson and a other standard scientific libraries to parse Google's SocialGraph data



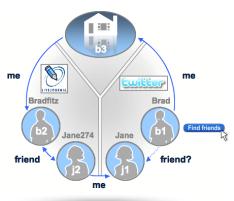
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 - Seed: imichaeldotorg.livejournal.com
 - k = 3



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 - Seed: imichaeldotorg.livejournal.comk = 3
- ► Note the low value of k

The code, part 1

Loading the libraries and setting things up

```
from cjson import *
from untlib import *
from networkx import *
from scipy import array,unique
...
if __name__ == "__main__":
seed_url='(http://imichaeldotorg.livejournal.com"
sg=get_sg(seed_url)
net_newnodes=create_egonet(sg)
info(net)
```

Get the JSON from SocialGraph

```
def get_sg(seed_url):
    sgapi_url="http://socialgraph.apis.google.com/lookup?q="+seed_url+"&edo=l&edi=l&fme=l&pretty=0"
    try:
        furl=urlopen(sgapi_url)
        fr=furl.read()
        furl.close()
        return fr
    except lOError:
        print "Could not connect to website"
        print sgapi_url
        return
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    net,newnodes=create_egonet(sg)
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```

```
Name: ['http://imichaeldotorg.livejournal.com/']
Type: DiGraph
Number of nodes: 5
Number of edges: 5
Average in degree: 1.0
Average out degree: 1.0
```

Get the JSON from SocialGraph

```
def get_sg(seed_url):
    sgapi_url="http://socialgraph.apis.google.com/lookup?q="+seed_url+"&edo=1&edi=1&fme=1&pretty=0"
    try:
        furl=urlopen(sgapi_url)
        fr=furl.read()
        furl.close()
        return fr
    except IOError:
        print "Could not connect to website"
        print sgapi_url
    return
```

Build egonet and snowball

Creating the egonet

```
def create_egonet(s):
    try:
        raw=decode(s)
        G=DiGraph()
        pendants=[]
        n=raw['nodes']
        nk=n.kevs()
        G.name=str(nk)
        pendants=[]
        for a in range(0.len(nk)):
            for b in range(0,len(nk)):
                if al=h·
                    G.add_edge(nk[a],nk[b])
        for k in nk:
            ego=n[k]
            ego out=ego['nodes referenced']
            for o in ego_out:
                 G.add_edge(k,o)
                pendants.append(o)
            ego_in=ego['nodes_referenced_by']
            for i in ego_in:
                G.add_edge(i,k)
                pendants.append(i)
        pendants=array(pendants,dtype=str)
        pendants.flatten()
        pendants=unique(pendants)
        return G, pendants
    except DecodeError:
    except KeyError:
```

Rolling the snowball

```
def snowball_round(G, seeds, myspace=False):
    t0=time()
    if myspace:
        seeds=get_myspace_url(seeds)
    sb data=∏
    for s in range(0,len(seeds)):
        s_sg=get_sg(seeds[s])
        new_ego,pen=create_egonet(s_sg)
        for p in pen:
                sb_data.append(p)
        if s<1:
            sb_net=compose(G,new_ego)
        else:
            sb_net=compose(new_ego,sb_net)
        del new_ego
        if s==round(len(seeds)*0.2):
            sb_net.name='20% complete'
            sb net.info()
            print 'AT: '+strftime('%m/%d/%Y, %H:%M:%S', gmtime())
            print ''
    # More time keeping, probably a MUCH better way to do this
    sb data=arrav(sb data)
    sb data.flatten()
    sb data=unique(sb data)
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    return sb net.sb data
```

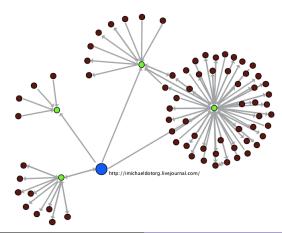
Step	Nodes	Edges	Mean Degree	Density
Seed	5	5	2.0	0.25
k=2	75	115	3.0	0.02
k = 3	4,938	8,659	3.5	3.6(10 ⁻⁴)

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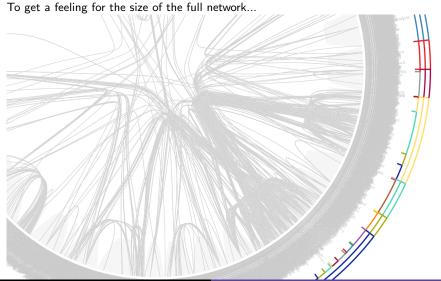
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- Our seed is abnormally isolated, with only four neighbors
- Large jump after first snowball
 Massive structural leap at k = 3
- http://imichaeldotorg.livejournal.com/

The full network



Python Dictionaries

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Now, try creating a dict of your own

Using dictionaries for network analysis

From the documentation...

networkx.closeness_centrality

closeness_centrality(G, v=None, weighted_edges=False)
Compute closeness centrality for nodes.

Closeness centrality at a node is 1/average distance to all other nodes.

Parameters: G : graph

A networkx graph

v : node, optional

Return only the value for node v.

weighted_edges : bool, optional

Consider the edge weights in determining the shortest paths. If False, all edge weights are considered equal.

Returns: nodes : dictionary

Dictionary of nodes with closeness centrality as the value.

NetworkX's metric's make extensive use of the dict type

▶ In this case the key→value mapping is of the form: {node_label: metric}

Let's look at an example:

```
>>> in_cen=in_degree_centrality(hartford)
>>> in_cen
{1: 0.014218009478672987, 2: 0.018957345971563982,...
...
90: 0.0047393364928909956, 293: 0.0}
```

In-degree centrality of Hartford data

We can see that node #90 has in-degree centrality 0.0047

▶ But we can do so much more!

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For our first analysis in NetworkX, we will do some basic network manipulation, then run multiple measures to find highest centrality nodes

 First, we will need to convert to an undirected network, and extract the main component

Find main component & symmetrize

- # Many of the centrality metrics require undirected graphs, so we will symmetrize
 >>> hartford ud=hartford.to undirected()
- # The network also has many small components, but for
- # this analysis we are interested in the largest
- >>> hartford_mc=hartford_main=connected_component_subgraphs(hartford_ud)[0]

Next, we will calculate multiple measures

- # Betweenness centrality
- >>> bet_cen=betweenness_centrality(hartford_mc)
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To find the most central actors we will use Python's list comprehension technique to do basic data manipulation on our centrality dictionaries

```
Function for finding most central actor
```

```
def highest_centrality(cent_dict):
    """Returns node key with largest value from
    NX centrality dict""
    # Create ordered tuple of centrality data
    cent_items=cent_dict.items()
    # List comprehension!
    cent_items=[(b,a) for (a,b) in cent_items]
    # Sort in descending order
    cent_items.sort()
    cent_items.reverse()
    return cent_items[0][1]
```

Now, just ask for the answer

Finding Most central actors

```
>>> print("Actor "+str(highest_centrality(bet_cen))+" has the highest Betweenness centrality")
Actor 82 has the highest Betweenness centrality
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List comprehension

- Given a dict: d={1: 0.15, 2: 0.67} $d.items() \rightarrow [(1,0.15),(2,0.67)]$
- b d=[(b,a) for (a,b in d)] → [(0.15,1),(0.67,2)]

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Finding Most central actors

>>> print("Actor "+str(highest_centrality(bet_cen))+" has the highest Betweenness centrality") Actor 82 has the highest Betweenness centrality

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```

List comprehension

- Figure 3 dict: d={1: 0.15, 2: 0.67}
- ▶ d.items() \rightarrow [(1,0.15),(2,0.67)]
- ▶ $d=[(b,a) \text{ for } (a,b \text{ in } d)] \rightarrow [(0.15,1),(0.67,2)]$

Here, we use list comprehension in order to use Python's built-in sort and reverse list functions

Now, just ask for the answer

Finding Most central actors

>>> print("Actor "+str(highest_centrality(bet_cen))+" has the highest Betweenness centrality")
Actor 82 has the highest Betweenness centrality

To find the most central actors we will use Python's list comprehension technique to do basic data manipulation on our centrality dictionaries

Function for finding most central actor

```
def highest_centrality(cent_dict):
    """Returns node key with largest value from
    NX centrality dict"""
    # Create ordered tuple of centrality data
    cent items=cent dict.items()
    # List comprehension!
    cent_items=[(b,a) for (a,b) in cent_items]
    # Sort in descending order
    cent items.sort()
    cent items.reverse()
    return cent items[0][1]
```

List comprehension

- ▶ Given a dict: d={1: 0.15, 2: 0.67}
- b d.items() → \(\(\begin{aligned}
 \) (1.0.15),(2.0.67)\(\begin{aligned}
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Calculating basic community structure

Often in network analysis we are interested in estimating the cohesiveness of a network, or the communities that exists within the structure

Cliques

 Maximal cliques are the largest complete subgraph containing a given point. There are several algorithms for finding cliques, including Bron Kerbosch (1973), Tomita, Tanaka and Takahashi (2006), Cazals and Karande (2008)

Clustering

For each node find the fraction of possible triangles that exist, $c_v = \frac{2T(v)}{deg(v)(deg(v)-1)}$, where T(v) is the number of triangles through node v.

Transitivity

▶ The fraction of all possible triangles which are in fact triangles. Or, $Trans = 3\left(\frac{T}{t}\right)$, where T = # of possible triangles and t = # of actual triads

We will use clustering coefficients to identify community structure in the Hartford drug network

```
# Calculate clustering coefficients of each node (return as dict)
clus=clustering(hartford_mc,with_labels=True)
# Get counts of nodes membership for each clustering coefficient, and clean up
unique_clus=list(unique(clus.values()))
clus_counts=zip(map(lambda c: clus.values().count(c),unique_clus),unique_clus)
clus_counts.sort()
clus_counts.reverse()
# Create a subgraph from nodes with most frequent clustering coefficient
mode_clus_sg=subgraph(hartford_mc,[(a) for (a,b) in clus.items() if b==clus_counts[0][1]])
```

Calculating clustering coefficients

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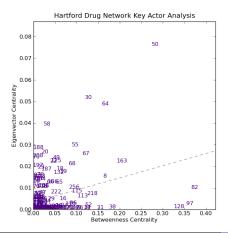


Recall Python's scientific computing trinity: NumPy, SciPy and matplotlib

► While NumPy and SciPy do most of the behind the scenes work, you will interact with matplotlib frequently for when doing network analysis

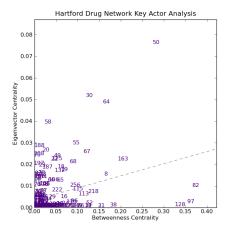
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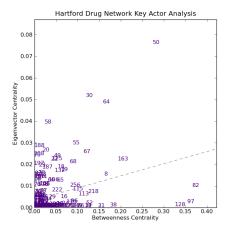
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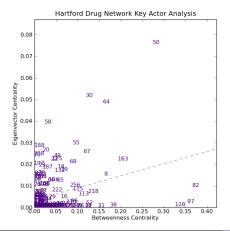


We will need to create a function that takes two centrality dict and generates this plot

1. Create a matplotlib figure

Recall Python's scientific computing trinity: NumPy, SciPy and matplotlib

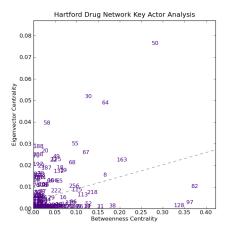
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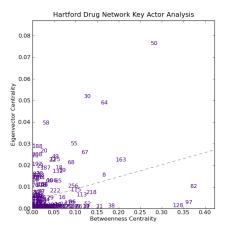
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- 1. Create a matplotlib figure
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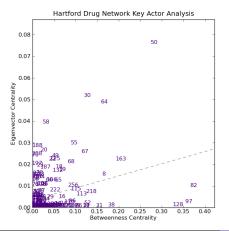
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- 1. Create a matplotlib figure
- 2. Plot each node label as a point
- 3. Add a "best fit" line
- 4. Add axis and title labels
- 5. Save figure as a PNG file

```
def centrality_scatter(met_dict1,met_dict2,path="",ylab="",xlab="",title="",reg=False):
    # Create figure and drawing axis
    fig=P.figure(figsize=(7,7))
    axi=fig.add_subplot(111)
# Create items so actors can be sorted properly
    met_items1=met_dict1.items()
    met_items2=met_dict2.items()
    met_items2.sort()
    ## Create items actors can be sorted properly
    met_items2=met_dict2.items()
    met_items2=met_dict2.items()
    met_items2.sort()
    ## Grab data
    xdata=[(b) for (a,b) in met_items1]
    ydata=[(b) for (a,b) in met_items2]
# Add each actor to the plot by ID
for p in xrange(len(met_items1)):
    ax1.text(x=xdata[p],y=ydata[p],s=str(met_items1[p][0]),color="indigo")
```

The centrality_scatter function, part one

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Create a canvas to draw on

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    xdata=[(b) for (a,b) in met_items2]
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- Create a canvas to draw on
- manipulate and store centrality data

- Create a canvas to draw on
- manipulate and store centrality data
- ▶ Add points to plot as node labels

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def centrality_scatter(met_dict1,met_dict2,path="",ylab="",xlab="",title="",reg=False):
    # If adding a best fit line, we will use NumPv to calculate the points.
    if reg:
        # Function returns y-intercept and slope. So, we create a function to
        # draw LOBF from this data
        slope, vint=polyfit(xdata, ydata, 1)
        xline=P.xticks()[0]
        vline=map(lambda x: slope*x+vint.xline)
        # Add line
        ax1.plot(xline,yline,ls='--',color='grey')
    # Set new x- and y-axis limits to data
    P.xlim((0.0,max(xdata)+(.15*max(xdata)))) # Give a little buffer
    P.ylim((0.0,max(ydata)+(.15*max(ydata))))
    # Add labels
    ax1.set_title(title)
    ax1.set_xlabel(xlab)
    ax1.set_vlabel(vlab)
    # Save figure
    P.savefig(path,dpi=100)
```

Creating a key actor plot in matplotlib

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- Add a best fit line
- Resize figure to fit data

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    # Save figure
    P.savefig(path,dpi=100)
```

- Add a best fit line
- ► Resize figure to fit data
- Add labels, and save the figure as a PNG file

As powerful as NetworkX and the complementing scientific computing packages in Python are, it may often be useful or necessary to output your data for additional analysis

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 NetworkX can write out network data in as many formats as it can read them, and the process is equally straightforward

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Next, we will review how to save data in different formats and export metrics to a CSV file using the Hartford drug net data

```
NX syntax for loading a file

>>> write_format(G, "path/to/file.txt", ....options...)

↑ ↑ ↑

NX function, net variable File to be written Nodes/edge data, etc.
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The syntax for exporting network data follows exactly the syntax for loading it

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Let's try!

- Output the Hartford drug net data as an adjacency list
- Add metric data to each node of the network
- Output new network in Pajek format with node attributes

Saving network data and adding node attributes

As shown, this is a simple one line operation

Output Hartford drug net data as an adjacency list

```
write_adjlist(hartford_mc,"../../data/hartford_mc_adj.txt")
```

Next, we will add the Eigenvector centrality of each node to the graph object

Adding node attributes

```
def add_metric(G,met_dict):
    """Adds metric data to G from a dictionary keyed by node labels"""
    if(G.nodes().sort()==met_dict.keys().sort()):
        for i in met_dict.keys():
            G.add_node(i,metric=met_dict[i])
        return G
    else:
        raise ValueError("Node labels do not match")
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Quick error checking

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- Quick error checking
- Add node attribute as "metric"

Python has powerful built-in tools for reading and writing standard data formats

 One of the most useful, and frequently used, is the CSV library and the DictWriter

```
import csv
def csv_exporter(data_dict,path):
    """Takes a dict of centralities keved by column headers and exports
    data as a CSV file"""
    # Create column header list
    col headers=["Actor"]
    col headers.extend(data dict.kevs())
    # Create CSV writer and write column headers
    writer=csv.DictWriter(open(path."w").fieldnames=col headers)
    writer.writerow(dict((h,h) for h in col headers))
    # Write each row of data
    for j in data_dict[col_headers[1]].keys():
        # Create a new dict for each row
        row=dict.fromkeys(col_headers)
        row["Actor"]=j
        for k in data dict.kevs():
            row[k]=data dict[k][i]
        writer.writerow(row)
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        row=dict.fromkeys(col_headers)
        row["Actor"]=j
        for k in data dict.kevs():
            row[k]=data dict[k][i]
        writer.writerow(row)
```

Python has powerful built-in tools for reading and writing standard data formats

 One of the most useful, and frequently used, is the CSV library and the DictWriter

```
import csv
def csv_exporter(data_dict,path):
    """Takes a dict of centralities keved by column headers and exports
    data as a CSV file"""
    # Create column header list
    col headers=["Actor"]
    col headers.extend(data dict.kevs())
    # Create CSV writer and write column headers
    writer=csv.DictWriter(open(path."w").fieldnames=col headers)
    writer.writerow(dict((h,h) for h in col headers))
    # Write each row of data
    for j in data_dict[col_headers[1]].keys():
        # Create a new dict for each row
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```

The results of CSV export

We can now open the CSV file in our favorite spreadsheet program

- Perform traditional data exploration
- ► Load into other analytics platforms for additional analysis (e.g., R)
- Store for latter use

\Q	A	В	C	D
_		_	_	_
1	Actor	Closeness	Betweeness	Eigenvector
2	1	0.12467532	0.0072576	0.00025176
3	2	0.12475634	0.01767427	0.00025964
4	3	0.12565445	0.05687441	0.00023185
5	4	0.10223642	0.03108639	1.44E-05
6	5	0.1443609	0	0.00313152
7	6	0.09943035	0.01041667	1.49E-07
8	7	0.11340815	0.04362093	6.78E-05
9	8	0.20512821	0.16354003	0.01471888
10	9	0.11267606	0.00741624	0.0001101
11	10	0.13983977	0.05258239	0.00095456
12	11	0.1703638	0.01250999	0.0032333
13	13	0.13892909	0	1.79E-05
14	14	0.17219731	0.11848775	0.00029737
15	15	0.13521127	0.00079897	2.11E-05
16	16	0.15907208	0.06203647	0.00432838