## INTEGRAIS TRIGONOMÉTRICAS

## Sabemos que:

- [ sen x ] ' = cos x
  [ cos x ] ' = sen x
  [ tg x ] ' = sec² x
  [ cotg x] ' = cossec² x
- [  $\sec x$  ] ' =  $\sec x \cdot \tan x$
- $[ cossec x ]' = cossec x \cdot tg x$

## Assim,

- $\bullet \quad \int \operatorname{sen} x \, dx = -\cos x + k$
- $\bullet \quad \int \cos x \, dx = \sin x + k$
- $\bullet \quad \int \sec^2 x \, dx = tg \, x + k$
- $\bullet \quad \int \operatorname{cossec}^2 x \, dx = -\cot g \, x + k$
- $\int \sec x \cdot \tan x \, dx = \sec x + k$
- $\int \operatorname{cossec} x \cdot \operatorname{cotg} x \ dx = -\operatorname{cossec} x + k$

## I – INTEGRAÇÃO POR SUBSTITUÇÃO

a) 
$$\int \frac{2x}{x^2+1} dx$$

$$R: \ln(x^2+1)+c$$

b) 
$$\int \cos(2x)dx$$

$$R: \frac{1}{2}\operatorname{sen}(2x) + c$$

c) 
$$\int \sqrt{1+y^2} \, 2y dy$$

$$R: \frac{2}{3}(1+y^2)^{\frac{3}{2}}+c$$

d) 
$$\int x^2 \operatorname{sen}(x^3) dx$$

$$R:-\frac{1}{3}\cos(x^3)+c$$

e) 
$$\int \frac{(\ln x)^2}{x} dx$$

$$R: \frac{(\ln x)^3}{3} + c$$

f) 
$$\int x(2x^2+3)^{10}dx$$

$$R: \frac{1}{44} (2x^2 + 3)^{11} + c$$

$$g) \int \frac{x}{\left(x^2 + 5\right)^3} dx$$

$$R: -\frac{1}{4}(x^2 + 5)^{-2} + c$$