



Pilhas e Filas

PrepTech Google

Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

150. Evaluate Reverse Polish Notation

Medium Topics Companies

You are given an array of strings `tokens` that represents an arithmetic expression in a [Reverse Polish Notation](#).

Evaluate the expression. Return *an integer that represents the value of the expression*.

Note that:

- The valid operators are `+`, `-`, `*`, and `/`.
- Each operand may be an integer or another expression.
- The division between two integers always **truncates toward zero**.
- There will not be any division by zero.
- The input represents a valid arithmetic expression in a reverse polish notation.
- The answer and all the intermediate calculations can be represented in a **32-bit** integer.

Example 1:

```
Input: tokens = ["2", "1", "+", "3", "*"]
Output: 9
Explanation: ((2 + 1) * 3) = 9
```

Example 2:

```
Input: tokens = ["4", "13", "5", "/", "+"]
Output: 6
Explanation: (4 + (13 / 5)) = 6
```

Example 3:

```
Input: tokens = ["10", "6", "9", "3", "+", "-11", "*", "/", "*", "17", "+", "5", "+"]
Output: 22
Explanation: ((10 * (6 / ((9 + 3) * -11))) + 17) + 5
= ((10 * (6 / (12 * -11))) + 17) + 5
= ((10 * (6 / -132)) + 17) + 5
= ((10 * 0) + 17) + 5
= (0 + 17) + 5
= 17 + 5
= 22
```

Constraints:

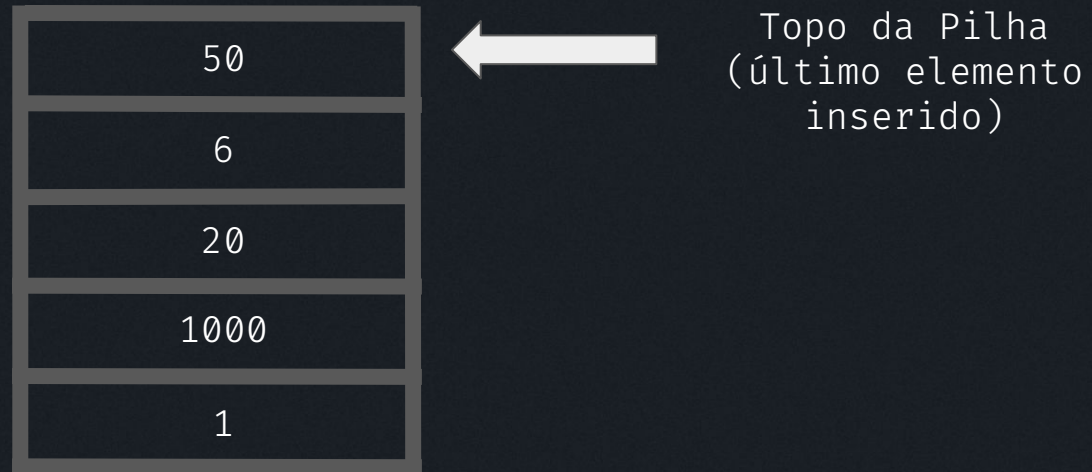
- `1 <= tokens.length <= 104`
- `tokens[i]` is either an operator: `+`, `-`, `*`, or `/`, or an integer in the range `[-200, 200]`.

Como resolver esse problema?



Pilhas

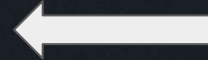
Uma pilha é uma estrutura de dados linear que segue o princípio LIFO (**Last In, First Out**), onde o último elemento inserido é o primeiro a ser removido.



Pilhas

Operações básicas:

- **push**: adiciona um elemento ao topo da pilha
- **pop**: remove o elemento do topo da pilha
- **top/peek**: acessa o elemento do topo da pilha sem removê-lo



Topo da Pilha
(último elemento
inserido)

Pilhas

Implementação

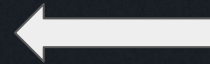
```
class Stack:  
    def __init__(self): # constructor  
  
    def push(self, item):  
  
    def pop(self):  
  
    def top(self):
```

Pilhas

Push - Adicionando elementos na pilha

Elementos sempre são adicionados ao topo da pilha. Dizemos que elementos são “empilhados”

```
stack.push(120)
```



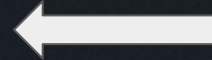
Topo da Pilha

Pilhas

Push - Adicionando elementos na pilha

Elementos sempre são adicionados ao topo da pilha. Dizemos que elementos são “empilhados”

```
stack.push(120)
```



Topo da Pilha

Pilhas

Pop - Removendo elementos da pilha

Elementos sempre são retirados do topo da pilha. Dizemos que elementos são “desempilhados”

```
stack.pop() # retorna 120
```



Pilhas

Pop - Removendo elementos da pilha

Elementos sempre são retirados do topo da pilha. Dizemos que elementos são “desempilhados”

```
stack.pop() # retorna 120
```



Pilhas

Top - Acessando o último elemento inserido

A função `top` (algumas implementações chamam essa operação de `peek`) acessa o último elemento inserido na pilha, sem removê-lo

```
stack.top() # retorna 50
```



Pilhas

Implementação

```
class Stack:
    def __init__(self): # constructor
        self.items = []

    def push(self, item):
        self.items.append(item)

    def pop(self):
        if not self.is_empty():
            return self.items.pop()
        return None

    def top(self):
        if not self.is_empty():
            return self.items[-1]
        return None

    def is_empty(self):
        return len(self.items) == 0
```

Pilhas

Implementação

**Todas essas
operações
possuem
complexidade
 $O(1)$ de tempo**

```
class Stack:
    def __init__(self): # constructor
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Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

150. Evaluate Reverse Polish Notation

Medium Topics Companies

You are given an array of strings `tokens` that represents an arithmetic expression in a [Reverse Polish Notation](#).

Evaluate the expression. Return *an integer that represents the value of the expression*.

Note that:

- The valid operators are `+`, `-`, `*`, and `/`.
- Each operand may be an integer or another expression.
- The division between two integers always **truncates toward zero**.
- There will not be any division by zero.
- The input represents a valid arithmetic expression in a reverse polish notation.
- The answer and all the intermediate calculations can be represented in a **32-bit** integer.

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```
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```

Example 3:

```
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```

Constraints:

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Como resolver esse problema
utilizando pilha?



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```
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Output: 22
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= ((10 * 0) + 17) + 5
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= 17 + 5
= 22
```

Constraints:

- `1 <= tokens.length <= 104`
- `tokens[i]` is either an operator: `+`, `-`, `*`, or `/`, or an integer in the range `[-200, 200]`.

Estratégia: percorrer o array de tokens empilhando os **operandos**.

Quando encontrar um **operador**, retira os dois últimos operandos da pilha e realiza a operação, empilhando o resultado.

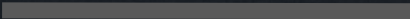
Como a entrada é garantida ser uma expressão válida, ao final das operações a pilha conterá um único valor, que é a avaliação da expressão de entrada.



Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2","1","+","3","*"]
```



Evaluate Reverse Polish Notation

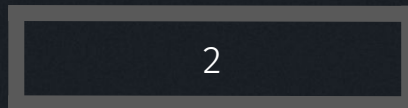
<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "2" é um **operando**, então empilhamos

```
stack.push(2)
```



Evaluate Reverse Polish Notation

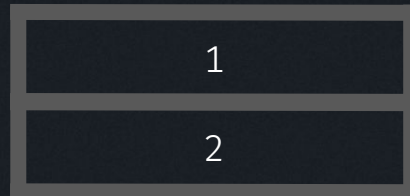
<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "1" é um **operando**, então empilhamos

```
stack.push(1)
```



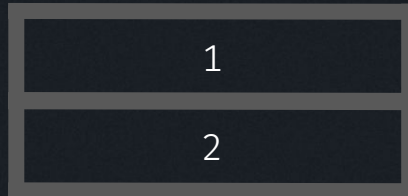
Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "+" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de soma, empilhando o resultado



Evaluate Reverse Polish Notation

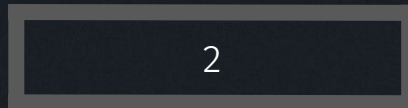
<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "+" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de soma, empilhando o resultado

```
a = stack.pop() # 1
```



Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "+" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de soma, empilhando o resultado

```
a = stack.pop() # 1
```

```
b = stack.pop() # 2
```


Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "+" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de soma, empilhando o resultado

```
a = stack.pop() # 1
```

```
b = stack.pop() # 2
```

```
result = b + a # 3
```

```
stack.push (result)
```

3

Evaluate Reverse Polish Notation

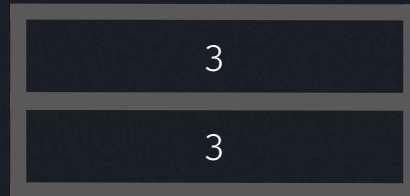
<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "3" é um **operando**, então empilhamos

```
stack.push(3)
```



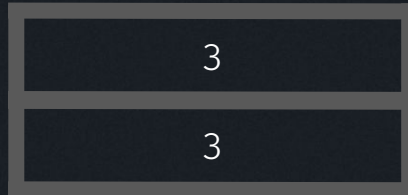
Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "*" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de multiplicação, empilhando o resultado



Evaluate Reverse Polish Notation

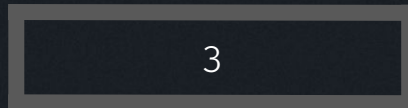
<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



token "*" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de multiplicação, empilhando o resultado

```
a = stack.pop() # 3
```



Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

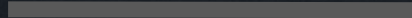
```
tokens = ["2", "1", "+", "3", "*"]
```



token "*" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de multiplicação, empilhando o resultado

```
a = stack.pop() # 3
```

```
b = stack.pop() # 3
```



Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



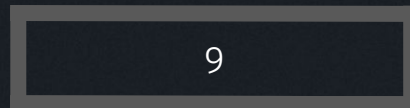
token "*" é um **operador**, então desempilhamos os últimos 2 operandos e realizamos a operação de multiplicação, empilhando o resultado

```
a = stack.pop() # 3
```

```
b = stack.pop() # 3
```

```
result = b * a # 9
```

```
stack.push (result)
```



Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2","1","+","3","*"]
```



Terminamos de percorrer o array `tokens`, a avaliação da expressão é o valor no topo da pilha

9

Evaluate Reverse Polish Notation

<https://leetcode.com/problems/evaluate-reverse-polish-notation/>

```
tokens = ["2", "1", "+", "3", "*"]
```



Terminamos de percorrer o array `tokens`, a avaliação da expressão é o valor no topo da pilha

```
return stack.pop() # 9
```


Remove All Adjacent Duplicates In String

<https://leetcode.com/problems/remove-all-adjacent-duplicates-in-string/description/>

1047. Remove All Adjacent Duplicates In String

Easy

Topics

Companies

Hint

You are given a string `s` consisting of lowercase English letters. A **duplicate removal** consists of choosing two **adjacent** and **equal** letters and removing them.

We repeatedly make **duplicate removals** on `s` until we no longer can.

Return the final string after all such duplicate removals have been made. It can be proven that the answer is **unique**.

Example 1:

Input: `s = "abbaca"`

Output: `"ca"`

Explanation:

For example, in "abbaca" we could remove "bb" since the letters are adjacent and equal, and this is the only possible move. The result of this move is that the string is "aaca", of which only "aa" is possible, so the final string is "ca".

Example 2:

Input: `s = "azxxzy"`

Output: `"ay"`

Constraints:

- `1 <= s.length <= 105`
- `s` consists of lowercase English letters.

Remove All Adjacent Duplicates In String

<https://leetcode.com/problems/remove-all-adjacent-duplicates-in-string/description/>

Solução usando pilha: precisamos iterar caracter a caracter da string de entrada, verificando se o caracter atual é igual ao que está no topo, se for igual, descartar e remover o topo da pilha.

Após passar por todos os caracteres da entrada, a string formada pelos caracteres da pilha, será a string resultante.

Remove All Adjacent Duplicates In String

<https://leetcode.com/problems/remove-all-adjacent-duplicates-in-string/description/>

C++ Solution:

```
string removeDuplicates(string s) {
    string output;
    for (const char& c: s) {
        if (output.empty()) {
            output.push_back(c);
            continue;
        }

        if (output.back() == c) {
            output.pop_back();
        }
        else {
            output.push_back(c);
        }
    }




    return output;
}
```

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

2073. Time Needed to Buy Tickets

Solved 

Easy  Topics  Companies  Hint

There are n people in a line queuing to buy tickets, where the 0^{th} person is at the **front** of the line and the $(n - 1)^{\text{th}}$ person is at the **back** of the line.

You are given a **0-indexed** integer array `tickets` of length n where the number of tickets that the i^{th} person would like to buy is `tickets[i]`.

Each person takes **exactly 1 second** to buy a ticket. A person can only buy **1 ticket at a time** and has to go back to **the end** of the line (which happens **instantaneously**) in order to buy more tickets. If a person does not have any tickets left to buy, the person will **leave** the line.

Return the **time taken** for the person at position k (**0-indexed**) to finish buying tickets.

Example 1:

Input: `tickets = [2,3,2]`, `k = 2`

Output: 6

Explanation:

- In the first pass, everyone in the line buys a ticket and the line becomes `[1, 2, 1]`.
 - In the second pass, everyone in the line buys a ticket and the line becomes `[0, 1, 0]`.
- The person at position 2 has successfully bought 2 tickets and it took $3 + 3 = 6$ seconds.

Example 2:

Input: `tickets = [5,1,1,1]`, `k = 0`

Output: 8

Explanation:

- In the first pass, everyone in the line buys a ticket and the line becomes `[4, 0, 0, 0]`.
 - In the next 4 passes, only the person in position 0 is buying tickets.
- The person at position 0 has successfully bought 5 tickets and it took $4 + 1 + 1 + 1 + 1 = 8$ seconds.

Como resolver esse problema?

Filas

Uma fila é uma estrutura de dados linear que segue o princípio FIFO (**First In, First Out**), onde o primeiro elemento inserido é o primeiro a ser removido. Ou seja, elementos são removidos na mesma ordem de inserção.



↑
Início da
fila

↑
Final da
fila

Filas

Operações básicas:

- **enqueue**: adiciona um elemento ao final da fila
- **dequeue**: remove o elemento do início da fila
- **front/peek**: acessa o elemento do início da fila sem removê-lo



Início da
fila



Final da
fila

Filas

Implementação

```
class Queue:
    def __init__(self): # constructor

    def enqueue(self, item):

    def dequeue(self):

    def front(self):

    def is_empty(self):
```

Filas

Enqueue - Adicionando elementos na fila

Elementos sempre são adicionados ao final da fila. Dizemos que elementos são “enfileirados”

```
queue.enqueue(120)
```



Início da
fila



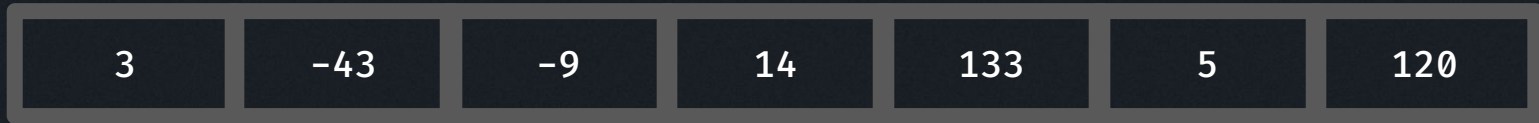
Final da
fila

Filas

Enqueue - Adicionando elementos na fila

Elementos sempre são adicionados ao final da fila. Dizemos que elementos são “enfileirados”

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queue.enqueue(120)
```



Início da
fila



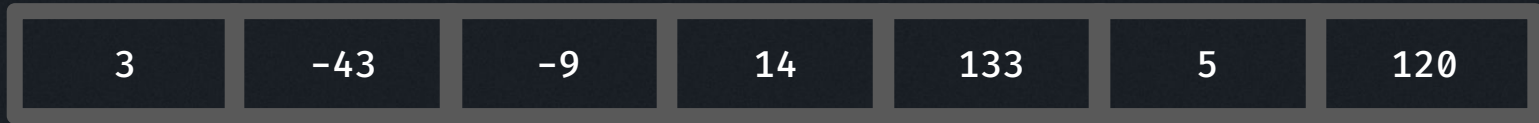
Final da
fila

Filas

Dequeue- Removendo elementos da fila

Elementos sempre são removidos do início da fila. Dizemos que elementos são “desenfileirados”

```
queue.dequeue() # 3
```



Início da
fila



Final da
fila

Filas

Dequeue- Removendo elementos da fila

Elementos sempre são removidos do início da fila. Dizemos que elementos são “desenfileirados”

```
queue.dequeue() # 3
```



Início da
fila



Final da
fila

Filas

Front - Acessando o elemento do início da fila

A função `front` (algumas implementações chamam essa função é `peek`) acessa o elemento do início da fila, sem removê-lo.

```
queue.front() # -43
```



Início da
fila



Final da
fila

Filas

Implementação com array

```
class Queue:
    def __init__(self):
        self.items = []

    def enqueue(self, item):
        self.items.append(item)

    def dequeue(self):
        if not self.is_empty():
            return self.items.pop(0)
        return None

    def front(self):
        if not self.is_empty():
            return self.items[0]
        return None

    def is_empty(self):
        return len(self.items) == 0
```

Filas

Implementação com array

**Qual é a
complexidade
dessa
implementação?**

```
class Queue:
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        return None

    def is_empty(self):
        return len(self.items) == 0
```

Filas

Implementação com array

**Adicionar um
elemento ao
final do array:
 $O(1)$**

```
class Queue:
    def __init__(self):
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```

Filas

Implementação com array

**Verificar se o
array está
vazio: $O(1)$**

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class Queue:
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        return None
```

```
def is_empty(self):
    return len(self.items) == 0
```


Filas

Implementação com array

**Retornar o primeiro
elemento do array:
 $O(1)$**

```
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    def __init__(self):
        self.items = []

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        self.items.append(item)

    def dequeue(self):
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        if not self.is_empty():
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        return None

    def is_empty(self):
        return len(self.items) == 0
```

Filas

Implementação com array

**Remover do
início do array:
 $O(N)$**

```
class Queue:
    def __init__(self):
        self.items = []

    def enqueue(self, item):
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    def dequeue(self):
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        return None

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        return None

    def is_empty(self):
        return len(self.items) == 0
```

Filas

Implementação com lista encadeada

```
class Node:
    def __init__(self, data=None): # constructor
        self.data = data
        self.next = None

class Queue:
    def __init__(self): # constructor
        self.front = None
        self.rear = None

    def is_empty(self):

    def enqueue(self, item):

    def dequeue(self):

    def front(self):
```

Filas

Implementação com lista encadeada

Quando a fila estiver vazia, `self.front` e `self.rear` são iguais a `None`

```
def is_empty(self):  
    return self.front == None
```


Filas

Implementação com lista encadeada

Para inserir na fila, temos 2 casos:

- **fila vazia:** criamos um novo nó e atualizamos a referência do início (**front**) e final da fila (**rear**)
- **fila não-vazia:** criamos um novo nó e atualizamos apenas referência do final da fila (**rear**)

```
def enqueue(self, item):  
    new_node = Node(item)  
    if self.rear is None:  
        self.front = self.rear = new_node  
    else:  
        self.rear.next = new_node  
        self.rear = new_node
```

Filas

Implementação com lista encadeada

Para retirar do início da fila, basta atualizar a referência de início da fila para o próximo elemento. Caso a fila tenha apenas 1 elemento, devemos também atualizar a referência do final da fila.

```
def dequeue(self):  
    if self.is_empty():  
        return None  
    temp = self.front  
    self.front = temp.next  
    if self.front is None:  
        self.rear = None  
    return temp.data
```

Filas

Implementação com lista encadeada

Para acessar o início da fila basta retornar o conteúdo da referência `front`.

```
def front(self):  
    if self.is_empty():  
        return None  
    return self.front.data
```

Filas

Implementação com lista encadeada



Todas as operações de uma fila implementadas usando lista encadeada tem complexidade $O(1)$ de tempo.

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

2073. Time Needed to Buy Tickets

Solved 

Easy  Topics  Companies  Hint

There are n people in a line queuing to buy tickets, where the 0^{th} person is at the **front** of the line and the $(n - 1)^{\text{th}}$ person is at the **back** of the line.

You are given a **0-indexed** integer array `tickets` of length n where the number of tickets that the i^{th} person would like to buy is `tickets[i]`.

Each person takes **exactly 1 second** to buy a ticket. A person can only buy **1 ticket at a time** and has to go back to **the end** of the line (which happens **instantaneously**) in order to buy more tickets. If a person does not have any tickets left to buy, the person will **leave** the line.

Return the **time taken** for the person at position k (**0-indexed**) to finish buying tickets.

Example 1:

Input: `tickets = [2,3,2]`, `k = 2`

Output: 6

Explanation:

- In the first pass, everyone in the line buys a ticket and the line becomes `[1, 2, 1]`.
 - In the second pass, everyone in the line buys a ticket and the line becomes `[0, 1, 0]`.
- The person at position 2 has successfully bought 2 tickets and it took $3 + 3 = 6$ seconds.

Example 2:

Input: `tickets = [5,1,1,1]`, `k = 0`

Output: 8

Explanation:

- In the first pass, everyone in the line buys a ticket and the line becomes `[4, 0, 0, 0]`.
 - In the next 4 passes, only the person in position 0 is buying tickets.
- The person at position 0 has successfully bought 5 tickets and it took $4 + 1 + 1 + 1 + 1 = 8$ seconds.

Como resolver esse problema
utilizando fila?

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

2073. Time Needed to Buy Tickets

Solved 

Easy  Topics  Companies  Hint

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Input: `tickets = [5,1,1,1]`, `k = 0`

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- In the next 4 passes, only the person in position 0 is buying tickets.
- The person at position 0 has successfully bought 5 tickets and it took $4 + 1 + 1 + 1 + 1 = 8$ seconds.

Estratégia: criar uma fila em que os elementos armazenam o **índice** e a quantidade de **tickets** restantes para comprar.

Enquanto o elemento de índice **k** ainda tiver tickets restantes para comprar, retiramos o primeiro elemento da fila, decrementamos a quantidade de tickets restantes para comprar, e colocamos de volta no final da fila caso necessário.

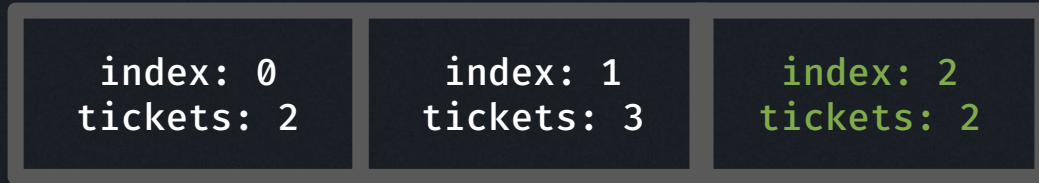
A cada iteração do loop, somamos 1 unidade de tempo.

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 0
```



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 1
```

index: 0
tickets: 2

Retiramos o primeiro
elemento da fila e
incrementamos o valor de
time

index: 1
tickets: 3

index: 2
tickets: 2



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 1
```

index: 0
tickets: 1

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0

index: 1
tickets: 3

index: 2
tickets: 2



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 1
```

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 2
```

index: 1
tickets: 3

Retiramos o primeiro
elemento da fila e
incrementamos o valor de
time

index: 2
tickets: 2

index: 0
tickets: 1



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 2
```

index: 1
tickets: 2

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0

index: 2
tickets: 2

index: 0
tickets: 1



Início da
fila



Final da
fila

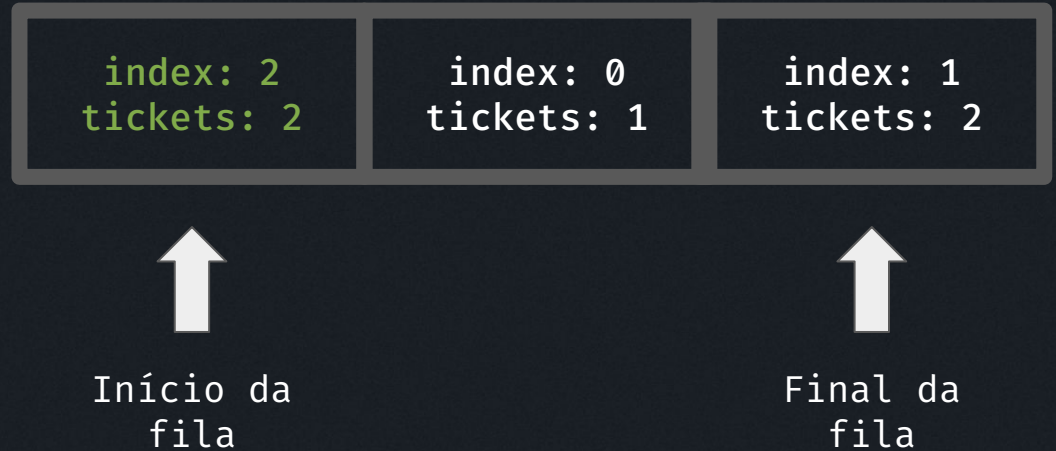
Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 2
```

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 3
```

index: 2
tickets: 2

Retiramos o primeiro elemento da fila e incrementamos o valor de **time**

index: 0
tickets: 1

index: 1
tickets: 2



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

index: 2
tickets: 1

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0

```
time = 3
```

index: 0
tickets: 1

index: 1
tickets: 2



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 3
```

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 4
```

index: 0
tickets: 1

Retiramos o primeiro
elemento da fila e
incrementamos o valor de
time

index: 1
tickets: 2

index: 2
tickets: 1



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 4
```

index: 0
tickets: 0

Decrementamos o valor de `tickets`. Como `tickets == 0` não colocamos de volta na fila

index: 1
tickets: 2

index: 2
tickets: 1



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 4
```

Decrementamos o valor de `tickets`. Como `tickets == 0` não colocamos de volta na fila



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 5
```

index: 1
tickets: 2

Retiramos o primeiro
elemento da fila e
incrementamos o valor de
time

index: 2
tickets: 1



Final da
fila



Início da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 5
```

index: 1
tickets: 1

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0

index: 2
tickets: 1



Final da
fila



Início da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 5
```

Decrementamos o valor de `tickets` e colocamos de volta na fila se for maior que 0



Início da
fila



Final da
fila

Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 6
```

index: 2
tickets: 1

Retiramos o primeiro
elemento da fila e
incrementamos o valor de
time

index: 1
tickets: 1



Final da
fila



Início da
fila



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
tickets = [2,3,2]  
k = 2
```

```
time = 6
```

```
index: 2  
tickets: 0
```

Decrementamos o valor de `tickets`. Agora `tickets == 0` e `index == k`. Chegamos ao fim e retornamos o valor de `time`.

```
index: 1  
tickets: 1
```



Final da
fila



Início da
fila



Time Needed to Buy Tickets

<https://leetcode.com/problems/time-needed-to-buy-tickets/>

```
int TimeRequiredToBuy(int[] tickets, int k) {
    int time = 0;

    var queue = new Queue<Entry> ();
    for (int i = 0; i < tickets.Length; i++) {
        var entry = new Entry();
        entry.id = i;
        entry.tickets = tickets[i];

        queue.Enqueue(entry);
    }

    bool finished = false;
    while (!finished) {
        time++;
        var entry = queue.Dequeue();
        entry.tickets--;
        if (entry.tickets == 0 && entry.id == k) {
            finished = true;
            continue;
        }
        if (entry.tickets > 0) queue.Enqueue(entry);
    }

    return time;
}
```

```
class Entry {
    public int id;

    public int tickets;
}
```


Number of Students Unable to Eat Lunch

<https://leetcode.com/problems/number-of-students-unable-to-eat-lunch/>

1700. Number of Students Unable to Eat Lunch

Solved 

Easy  Topics  Companies  Hint

The school cafeteria offers circular and square sandwiches at lunch break, referred to by numbers `0` and `1` respectively. All students stand in a queue. Each student either prefers square or circular sandwiches.

The number of sandwiches in the cafeteria is equal to the number of students. The sandwiches are placed in a **stack**. At each step:

- If the student at the front of the queue **prefers** the sandwich on the top of the stack, they will **take it** and leave the queue.
- Otherwise, they will **leave it** and go to the queue's end.

This continues until none of the queue students want to take the top sandwich and are thus unable to eat.

You are given two integer arrays `students` and `sandwiches` where `sandwiches[i]` is the type of the i^{th} sandwich in the stack ($i = 0$ is the top of the stack) and `students[j]` is the preference of the j^{th} student in the initial queue ($j = 0$ is the front of the queue). Return *the number of students that are unable to eat*.

Example 1:

Input: `students = [1,1,0,0]`, `sandwiches = [0,1,0,1]`

Output: `0`

Explanation:

- Front student leaves the top sandwich and returns to the end of the line making `students = [1,0,0,1]`.
- Front student leaves the top sandwich and returns to the end of the line making `students = [0,0,1,1]`.
- Front student takes the top sandwich and leaves the line making `students = [0,1,1]` and `sandwiches = [1,0,1]`.
- Front student leaves the top sandwich and returns to the end of the line making `students = [1,1,0]`.
- Front student takes the top sandwich and leaves the line making `students = [1,0]` and `sandwiches = [0,1]`.
- Front student leaves the top sandwich and returns to the end of the line making `students = [0,1]`.
- Front student takes the top sandwich and leaves the line making `students = [1]` and `sandwiches = [1]`.
- Front student takes the top sandwich and leaves the line making `students = []` and `sandwiches = []`.

Hence all students are able to eat.

Example 2:

Input: `students = [1,1,1,0,0,1]`, `sandwiches = [1,0,0,0,1,1]`

Output: `3`

Constraints:

- `1 <= students.length, sandwiches.length <= 100`
- `students.length == sandwiches.length`
- `sandwiches[i]` is `0` or `1`.
- `students[i]` is `0` or `1`.

Number of Students Unable to Eat Lunch

<https://leetcode.com/problems/number-of-students-unable-to-eat-lunch/>

Estratégia: O array `students` é uma fila (início na posição `0`) enquanto o array `sandwiches` é uma pilha (topo na posição `0`).

Podemos fazer uma simulação da execução: retira o elemento do início da fila e compara com o elemento no topo da pilha. Se forem iguais, faz um `pop` na pilha. Se forem diferentes, coloca o elemento no final da fila. Fazemos isso enquanto a fila e pilha não estiverem vazias.

Além disso, temos que contar quantas vezes tiramos um elemento da fila e colocamos de volta em sequência. Se esse número for igual ao tamanho da fila, significa que todo mundo saiu e entrou de novo na fila, ou seja, nenhum elemento da fila é igual ao topo da pilha. Nesse caso paramos o algoritmo e retornamos como resposta o número de elementos da fila.

Number of Students Unable to Eat Lunch

<https://leetcode.com/problems/number-of-students-unable-to-eat-lunch/>

```
public int CountStudents(int[] students, int[] sandwiches) {
    var queue = new Queue<int>(students);
    var stack = new Stack<int>(sandwiches.Reverse());

    var rotationCount = 0;
    do {
        var preference = queue.Dequeue();

        if (preference == stack.Peek()) {
            rotationCount = 0;
            stack.Pop();
        }
        else {
            rotationCount++;
            queue.Enqueue(preference);
        }
    } while (rotationCount < queue.Count && stack.Count > 0 && queue.Count > 0);

    return queue.Count;
}
```

Obrigado