

# Chapter 6: Expressions

CMSC 124, 1<sup>st</sup> Semester, AY 2009-10



# Chapter 6: Expressions

## Definition

### Expressions

- Fundamental means of specifying computations in a programming language.

### Kinds of Expressions

1. Literals
2. Aggregates
3. Function Calls
4. Conditional Expressions
5. Constants and Variables



# Chapter 6: Expressions

## Literals and Aggregates

### Literals

- Simplest kind of expression.
- Basic element of all other expressions.
- Fixed value of some type.

**Eg:** Literals in C

100

5.25

'c'

### Aggregates

- Construct an aggregate value from its component values.

**Eg:** Aggregates in ML

{ y = 2009, m = "Sep", d = 26 }

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## Function Calls

### Function Calls

- Basically do computation on arguments passed to the function and produce a result.
- All explicit f'n call has this form:  
**f(actual parameters)**
- An operator may be thought of as denoting a function.
- Given the expression
$$a + b * c - d$$
It is equivalent to
$$* (+ (a, b), - (c, d))$$

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## Conditional Expressions

### Conditional Expressions

- Allow several sub-expressions to be included in the expression but only one of these is chosen to be evaluated.
- Should not be confused with conditional commands.

➤ **Eg:** In ML (Con Expr)  
`val even :=  
 if n mod 2 = 0 then  
 true  
 else false`

➤ **Eg:** In Pascal (Con Cmd)  
`if n mod 2 = 0 then  
 even := true  
else  
 even := false;`

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## Constants and Variables

**Consider this:** In Pascal, the constant and variable declaration.

```
const a = 5.25;  
var b: real;
```

In the expression: **52.35 + a \* b**



Replaced by 5.25

The diagram illustrates the evaluation of the expression **52.35 + a \* b**. It shows two arrows pointing to the variables **a** and **b** in the expression. The arrow pointing to **a** is labeled "Replaced by 5.25". The arrow pointing to **b** is labeled "Replaced by the value of b".

Replaced by the value of b

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## Syntax for Expressions

### 1. Prefix Notation

- The operator symbol is placed ahead of the operands in left-to-right order.

`operator (operand1, operand2)`

- **Eg:**

`+( *(a,b) , -(c,d) )`

- Also, the notation used for most monadic operations.

- Negatives: `-a`
- Function calls: `power(b,n)`



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## Prefix Notation: Other Forms

### Cambridge Polish

- Variant of prefix notation.
- Used in LISP, Scheme.
- **Syntax:**  
`(orator orand1 orand2)`
- **Eg:**  
`(+ (* a b) (- c d) )`

### Polish

- Another variant of prefix notation.
- Does not use parentheses.
- **Syntax:**  
`orator orand1 orand2`
- **Eg:**  
`+ * a b - c d`



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## Syntax for Expressions

### 2. Postfix Notation

- The opposite of prefix.
- The operator symbol follows that of the operands.

`(orand1, orand2) orator`  
`orand1 orand2 orator`

- **Eg:**  
`((a,b) *, (c,d) -) +`  
`a b * c d - +`

- It is used extensively as the execution time representation of expressions.
- Since most PL's operate on stacks, eval of expressions becomes very easy.



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## Syntax for Expressions

### 3. Infix Notation

- Suitable for binary operations.
- The operator is placed between the two operands.
- **Eg:**  
 $(a * b) + (c - d)$

- The notation of mathematics, thus, supported by most PL's.



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## Infix Notation: Disadvantages

### 1. It cannot be used for monadic operations.

- **Solution:** Combine with either prefix or postfix to handle all kinds of expressions.



### 2. It is inherently ambiguous.

- **Consider this:**

$$a - b / c$$

The above expression can be interpreted as:

$$(a - b) / c$$

$$a - (b / c)$$

- **Solution:** Implement implicit control rules to dictate how expressions are to be evaluated.

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## Operator Precedence

- The value of an expression is dependent on the order of evaluation of operators involved in the expression.
- **5 + 2 \* 3** will give us:
  - 21, if addition is done first.
  - 11, if multiplication is done first.



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## Operator Precedence

- **In mathematics**, there is the concept of associating operators with priorities.
  - **“Hierarchy of evaluation”**
- This concept of hierarchy has been adopted by PL designers.
- But, remember, each PL have their own operator precedence rules.



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## Operator Precedence Rules in C

From high priority to low priority the order for all C operators is:

( ) [ ] -> .  
! - \* & sizeof cast ++ --  
*(these are right->left associativity)*  
\* / %  
+ -  
< <= >= >  
== !=  
&  
& & |  
&&  
||  
?: *(right->left associativity)*  
= += -= *(right->left associativity)*  
, (comma)

**Highest**



**Lowest**

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## Operator Associativity

- When 2 adjacent occurrence of operators with the same level of precedence is found, as to which operator evaluated first is answered by **associativity rules**.



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## Operator Associativity

### 1. Left-to-Right Evaluation

- Prevalent in FORTRAN, C, Pascal, C++, ADA
- **Eg:**  $10 - 5 + 4 = 9$

### 2. Right-to-Left Evaluation

- In FORTRAN, the evaluation of **\*\*** (power) is from right to left.
- **Eg:**  $3 ** 2 ** 2 = 81$





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## Operator Associativity

### 3. Non-Associativity

- **Eg:** In ADA, it is illegal to have an expression like:

$3 ** 2 ** 2$

- It is illegal to write an expression having these operators side by side in the expression.
- The only way to have this type of computation is through the use of parentheses.

$3 ** (2 ** 2) \text{ or } (3 ** 2) ** 2$

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## Parentheses

- Precedence and associativity rules can be overridden using parentheses.
- **Eg 1:**  $10 * 2 + 5 \Rightarrow 10 * (2 + 5)$   
The above example forces addition to be done first.
- **Eg 2 (In Pascal):**  $2 ** 3 ** 2$  OR  $2 ** (3 ** 2)$   
Pascal, by default, employs left-to-right eval.  
The above example forces a right-to-left eval.
- **In APL,** uniform associativity rule applies to all operators.  
Programmer may use parentheses.

# QUIZ

Get ¼: Consider the following operator precedence and associativity rules in C

( ) [ ] -> .  
! - \* & sizeof cast ++ -- (*right->left assoc*)  
\* / %  
+ -  
< <= >= >  
== !=  
&  
& & |  
&&  
||  
?: (*right->left associativity*)  
= += -= (*right->left associativity*)  
, (comma)

Highest

Lowest

Use parentheses to observe the operator precedence and associativity rules in C:

1.  $a < b \ \&\& \ c * d < e$
2.  $a = b = c / d + e$

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## Implementing Expressions

1. Generate the machine code directly.
2. Build the expression tree.
3. Transform the expression from its present notation to either prefix or postfix notations.



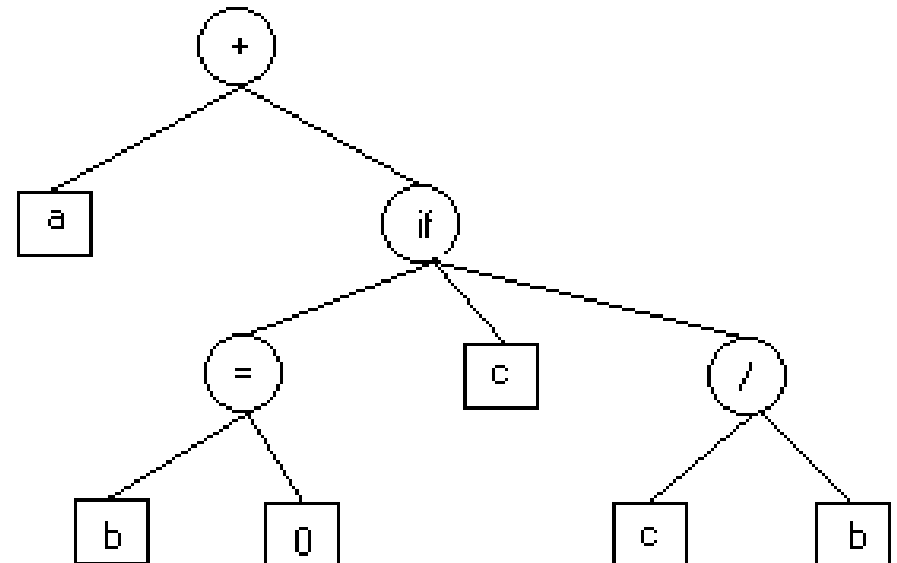
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## Implementation Problems

**1. Uniform evaluation rules do not apply for evaluating all types of expressions.**

✓ **Consider this:**

`a + if b = 0 then c else c/b`



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## Implementation Problems

### 2. Side effects are possible.

- ✓ Side effect is a form of **ambiguity**.
- ✓ **Functional side effect** - when the function changes either one of its parameters or global variables.
- ✓ Given the following:  
`a = 1`  
`f(a) // this function simply adds 1 to a.`
- ✓ **What is the output of  $a + f(a) * a$ ?**
  - 3 – if  $a$  is fetched once.
  - 5 – if  $a$  is fetched twice, before and after evaluating  $f(a)$ .

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## Approaches to Side Effects

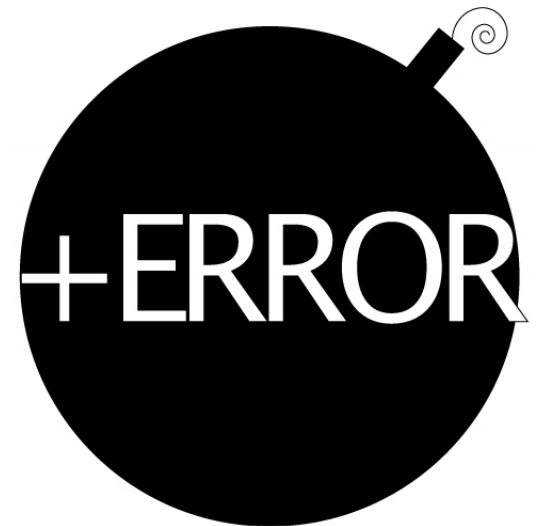
- 1. Disallow the user to access global variables from a function.**
  - Affects the flexibility and efficiency of programs.
- 2. Allow and state explicitly how the evaluation will proceed.**
  - Disallows optimization methods used by compilers.

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## Implementation Problems

### 3. No uniform way of handling error conditions.

- ✓ When an error is detected by the system on some primitive operations, control is passed to the operating system.
- ✓ One common solution is to simply abort the execution without trying to recover.





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## Implementation Problems

### 4. Short circuit evaluation may be necessary for some expressions.

- ✓ **Short circuit evaluation** - result is determined without evaluating all of the operands and/or operators.

**Eg 1:**

~~**$(a * 10) * (20 + b / 2)$**~~

// if  $a = 0$

**Eg 2:**

~~**$a + \text{if } b = 0 \text{ or } c/b > 1 \text{ then } c \text{ else } d$**~~

// if  $b = 0$

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## Short Circuit Evaluation

### Eg 3:

(In Java) Given that **list** has a **listlen** elements and **key** is the searched for value.

```
index = 1;
while ((index < listlen) && (list[index] <> key))
    index = index + 1;
```

### What could happen if evaluation is not short circuit?

**Solution:** In ADA, the keywords "and then" and "or else".

```
i := 0;
while (i < listlen) and then (list(i) /= 2)
loop
    i := i + 1;
end loop
```

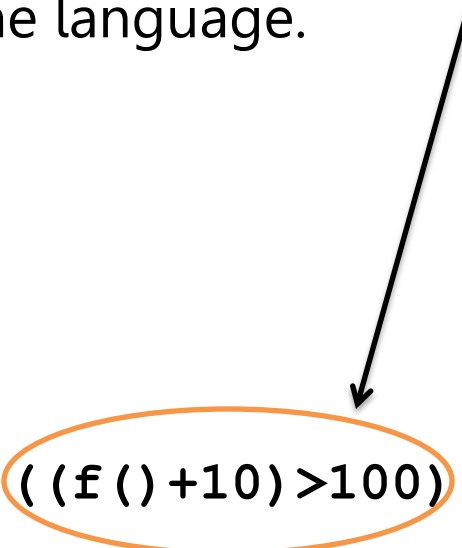
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## Short Circuit Evaluation

### Eg 4:

Short circuit evaluation, can result in serious errors when side effect is also allowed in the language.

```
int x = 10;
int f() {
    x = 100;
}
main() {
    if (a > 0) && ((f()+10)>100)
        x = 0;
    else
        x = 1;
}
```



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## Translation Considerations

### ➤ Design of the Translator

- **Translator 1:** Builds a parse tree and generates object code from the said tree. (optimized)
- **Translator 2:** Generates object code directly from the source code. (faster implementation)

### ➤ Number of Registers

- More registers - the more efficient!

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## Approaches to Implementation of Expressions

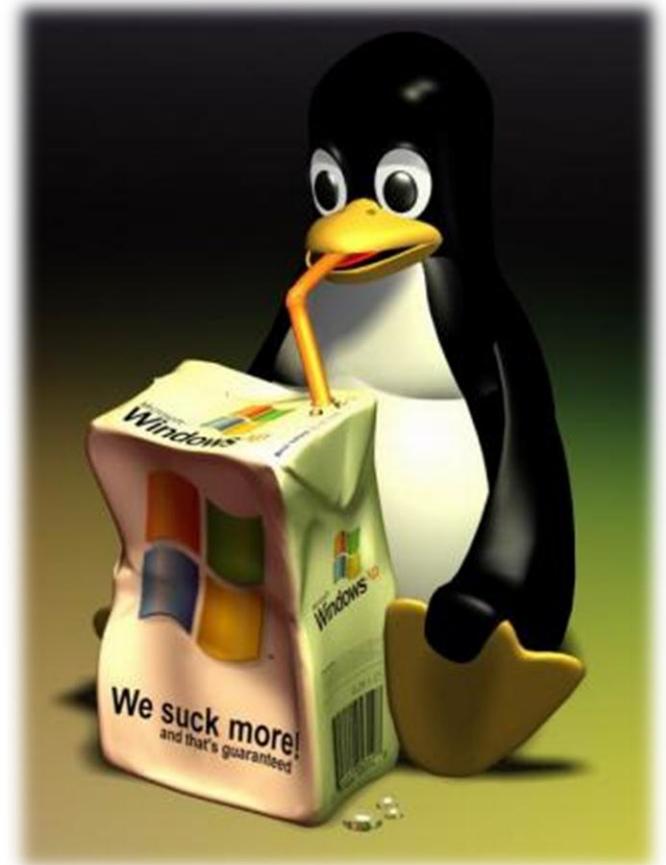
1. Generating Code Directly
2. Generating Code from Postfix Expression
3. Generating Code from Parse Trees



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## Generating Code Directly

- A compiler generates the target machine code as it scans the source code.
- It reads one token in advance before it proceeds to generate the target machine code for the sub-expression it has already scanned.



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## Generating Code Directly

**Consider this:**  $a + b * c = d + e$

Scanned Token	Lookahead	Compiler's Action
a	+	Load into the accumulator the value of a
+	b	Remember +
b	*	Push onto the stack the value a Load into the accumulator the value of b
*	c	Remember * ahead of +

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## Generating Code Directly

**Consider this:**  $a + b * c = d + e$

c	=	Push onto the stack the value b Load into the accumulator the value of c Pop from the stack the value b and multiply it with the value c in the accumulator leaving $b*c$ in the accumulator Pop from the stack the value a and add it with value $b*c$ in the accumulator leaving $a+b*c$ in the accumulator
=	d	Remember =



# Chapter 6: Expressions

## Generating Code Directly

**Consider this:**  $a + b * c = d + e$

d	+	Push onto the stack the value $a+b*c$ Load into the accumulator the value of d
+	e	Remember + ahead of =
e	end	Push onto the stack the value d Load into the accumulator the value e Pop from the stack the value d and add it with the value e in the accumulator leaving $d+e$ in the accumulator Pop from the stack the value $a+b*c$ and check if it is = with the value $d+e$ in the accumulator leaving the result in the accumulator

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## Generating Code from Postfix Expression

- The compiler converts an expression to postfix notation.
- The postfix expression is used by the compiler to generate target machine code.



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## Generating Code from Postfix Expression

**Consider this:**  $a + b * c = d + e \rightarrow ((a,(b,c)^*), (d,e)^+)=$

Scanned Token	Lookahead	Compiler's Action
(	(	
(	a	
a	(	Load into the accumulator the value of a
(	b	
b	c	Push onto the stack the value a Load into the accumulator the value of b
c	)	Push onto the stack the value b Load into the accumulator the value of c

# Chapter 6: Expressions

## Generating Code from Postfix Expression

**Consider this:**  $a + b * c = d + e \rightarrow ((a,(b,c)^*), (d,e)^+)=$

)	*	
*	)	Pop from the stack the value b and multiply it with the value c in the accumulator leaving $b*c$ in the accumulator
)	+	
+	(	Pop from the stack the value a and add it with value $b*c$ in the accumulator leaving $a+b*c$ in the accumulator
(	d	
d	e	Push onto the stack the value $a+b*c$ Load into the accumulator the value of d

# Chapter 6: Expressions

## Generating Code from Postfix Expression

**Consider this:**  $a + b * c = d + e \rightarrow ((a,(b,c)^*), (d,e)^+)=$

e	)	Push onto the stack the value d Load into the accumulator the value of e
)	+	
+	)	Pop from the stack the value d and add it with the value e in the accumulator leaving d+e in the accumulator
)	=	
=	end	Pop from the stack the value a+b*c and check if it is = with the value d+e in the accumulator leaving the result in the accumulator

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## Generating Code from Parse Tree

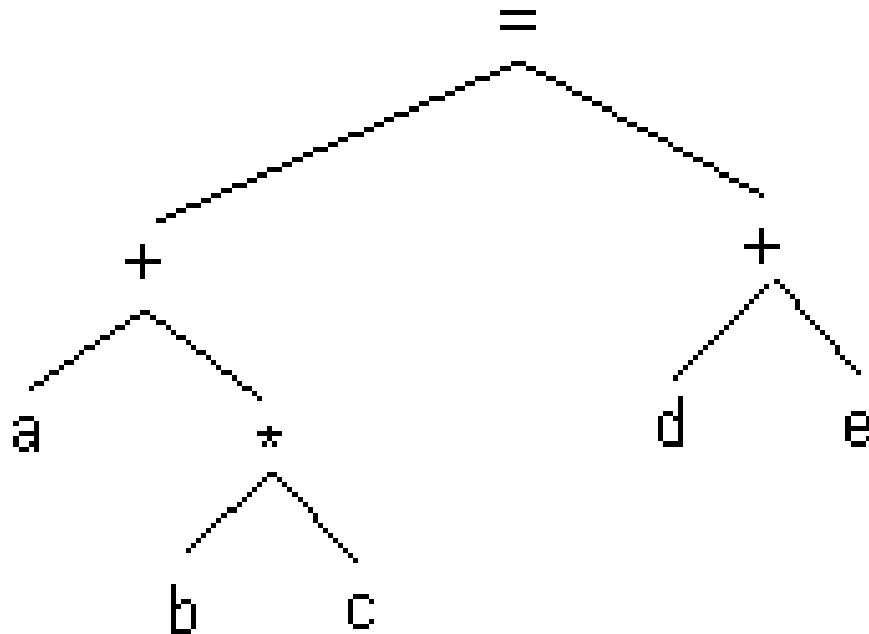
- A compiler constructs a parse tree from an expression.
- Then, the parse tree is traversed by the compiler generating code while it is traversing the parse tree.



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## Generating Code from Parse Tree

➤ **Consider this:**  $a + b * c = d + e$



# Chapter 6: Expressions

## Generating Code from Parse Tree

Node Visited	Compiler's Action
a	Load into the accumulator the value of a
b	Push onto the stack the value a Load into the accumulator the value b
c	Push onto the stack the value b Load into the accumulator the value c
*	Pop from the stack the value b and multiply it with the value c in the accumulator leaving $b*c$ in the accumulator
+	Pop from the stack the value a and add it with the value $b*c$ in the accumulator leaving $a+b*c$ in the accumulator



# Chapter 6: Expressions

## Generating Code from Parse Tree

d	Push onto the stack the value $a+b*c$ Load into the accumulator the value d
e	Push onto the stack the value d Load into the accumulator the value e
+	Pop from the stack the value d and add it with the value e in the accumulator leaving $d+e$ in the accumulator
=	Pop from the stack the value $a+b*c$ and check if it is = with the value $d+e$ in the accumulator leaving the result in the accumulator