



III. STRUCTURED ASSEMBLY LANGUAGE PROGRAMMING TECHNIQUES

Modular Programming
(Recursive Functions)





Recursive Function

- a subprogram which calls itself
- define base case
- define recursive case





Recursive Function

- Countdown:
 - Countdown(n)
 - print(n) , print(n-1) , print(n-2) , ... , print(2) , print(1), print(0)
 - print(n) , Countdown(n-1)
 - Countdown(0) = print(0)





Recursive Functions

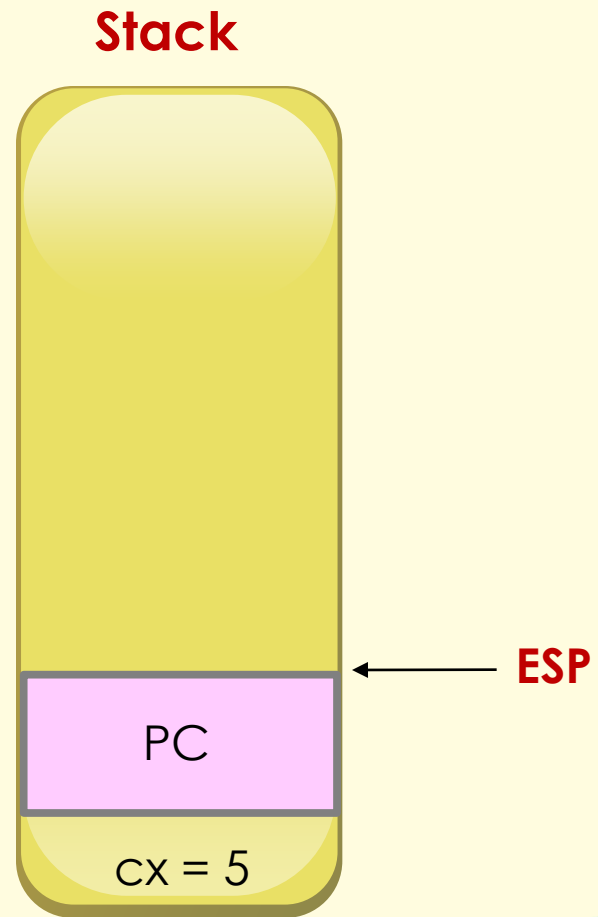
```
void countDown (int n) {  
    if (n == 0)  
        printf("%i",n);  
    else{  
        printf("%i",n);  
        countDown(n-1);  
    }  
}
```





Recursive Functions

```
mov cx, 5  
push cx  
call countDown
```



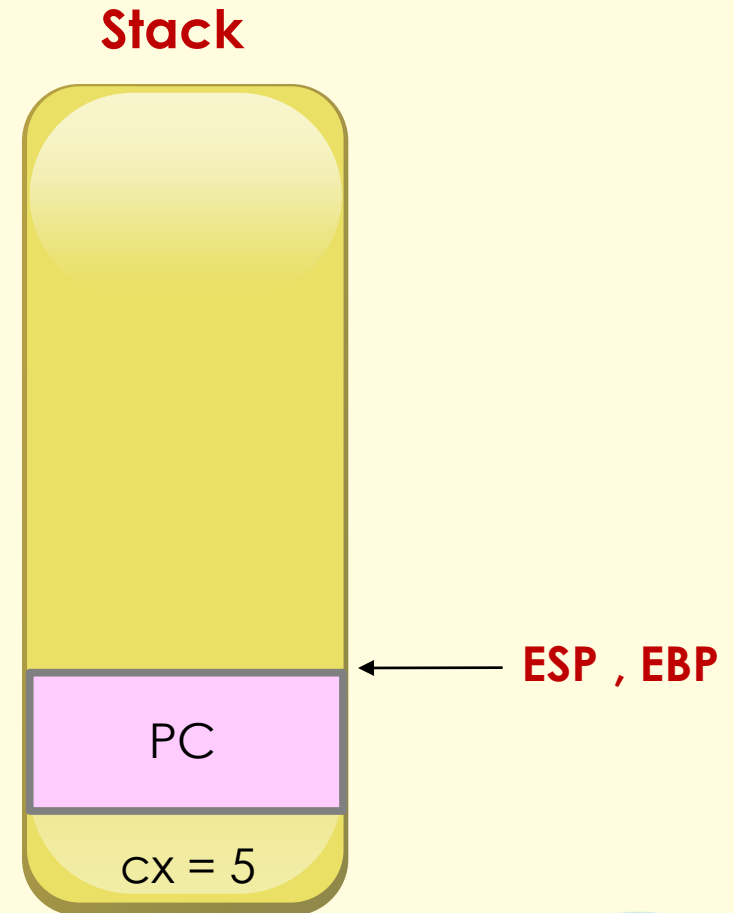


Recursive Functions

```
mov cx, 5  
push cx  
call countDown
```

...

```
countDown:  
mov ebp, esp
```





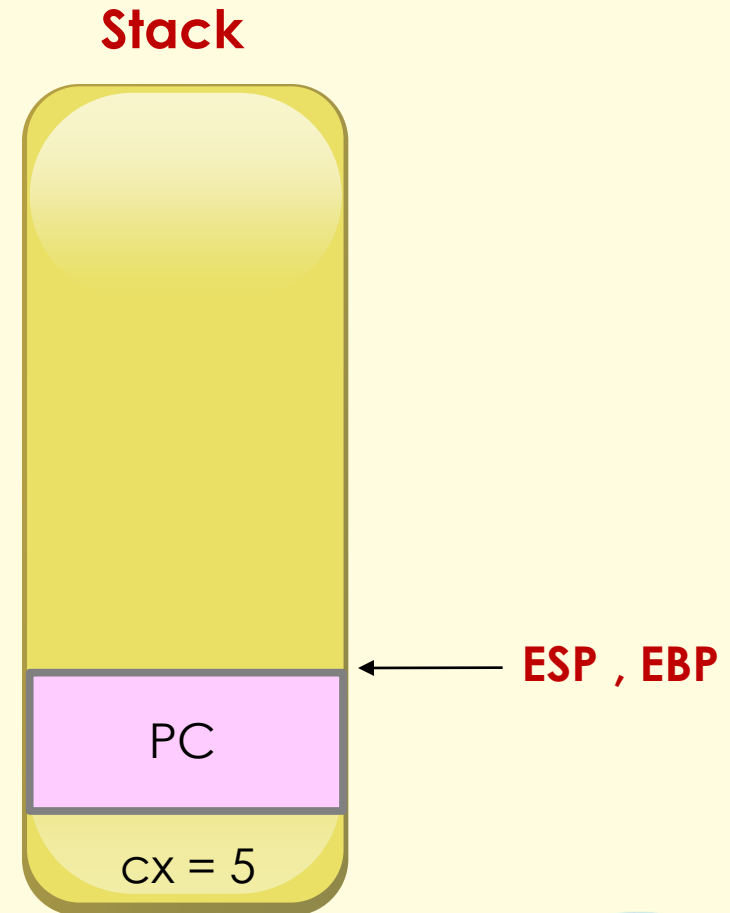
Recursive Functions

countDown:

```
mov ebp, esp
```

```
cmp [ebp+4], 0
```

```
jl countEnd
```



Recursive Functions

countDown:

```
mov ebp, esp
cmp [ebp+4], 0
jl countEnd
add [ebp+4], 30h
mov eax, 4
mov ebx, 1
lea ecx, [ebp+4]
mov edx, 1
int 80h
sub [ebp+4], 30h
```

Stack



ESP, EBP

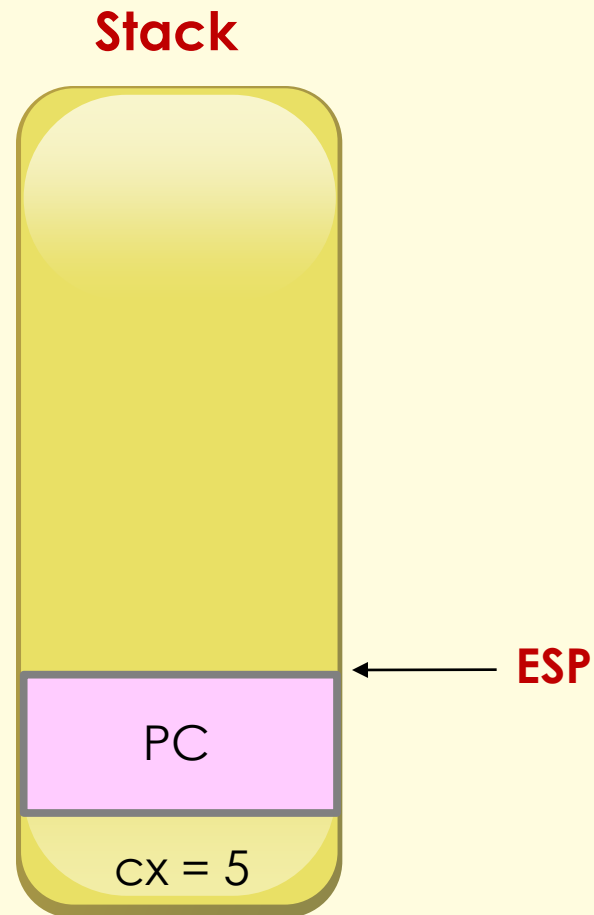
CX = 5





Recall

```
mov cx, 5  
push cx  
call countdown
```



Recursive Functions

countDown:

```
mov ebp, esp
cmp [ebp+4], 0
jl countEnd
add [ebp+4], 30h
mov eax, 4
mov ebx, 1
lea ecx, [ebp+4]
mov edx, 1
int 80h
sub [ebp+4], 30h
mov cx, [ebp+4]
```

Stack



ESP, EBP

CX = 5





Recursive Functions

countDown:

...

mov eax, 4

mov ebx, 1

lea ecx, [ebp+4]

mov edx, 1

int 80h

sub [ebp+4], 30h

mov cx, [ebp+4]

dec cx

Stack



ESP, EBP



Recursive Functions

countDown:

...

mov eax, 4

mov ebx, 1

lea ecx, [ebp+4]

mov edx, 1

int 80h

sub [ebp+4], 30h

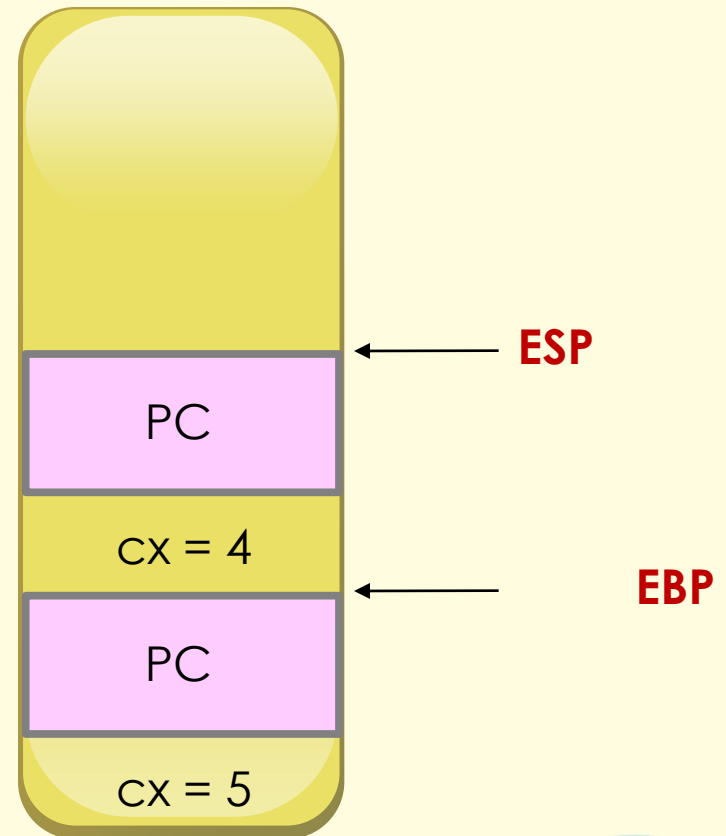
mov cx, [ebp+4]

dec cx

push cx

call countDown

Stack





Recursive Functions

countDown:

```
mov ebp, esp
```

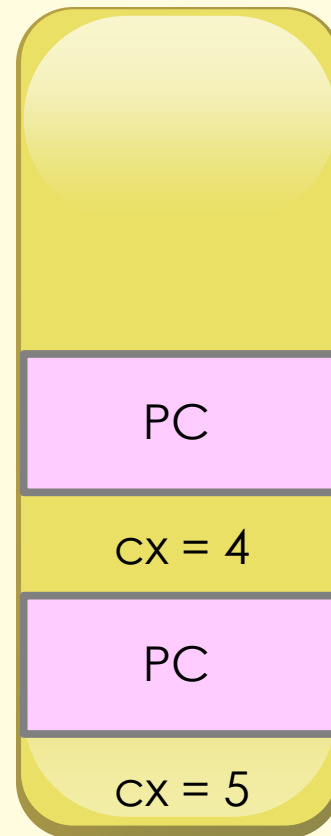
```
cmp [ebp+4], 0
```

```
jl countEnd
```

...

```
call countDown
```

Stack





Recursive Functions

countDown:

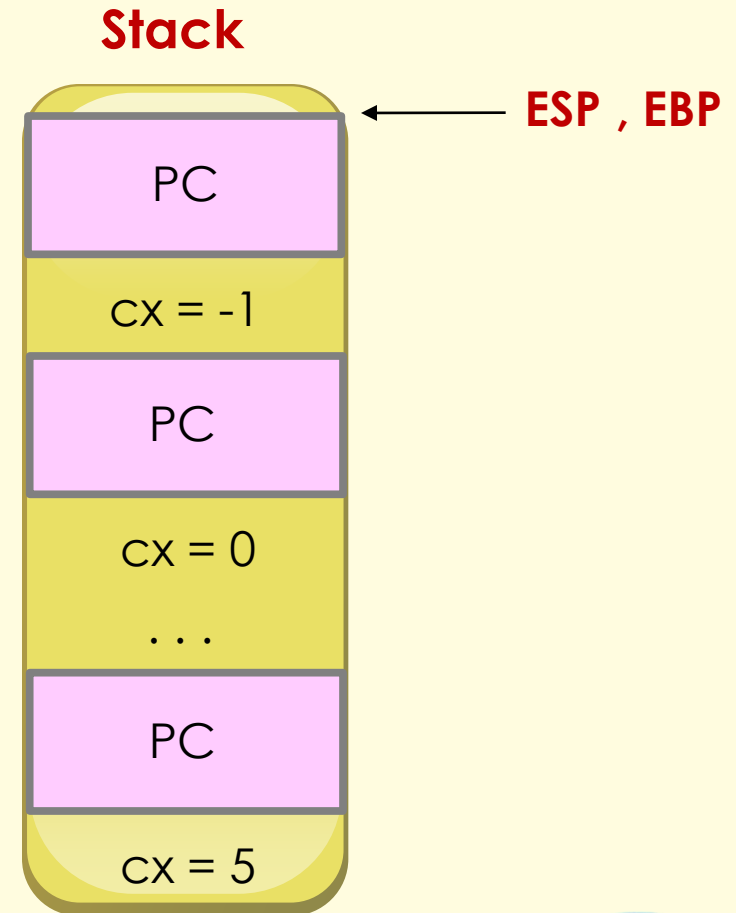
```
mov ebp, esp
```

```
cmp [ebp+4], 0
```

```
jl countEnd
```

...

```
call countDown
```



Recursive Functions

countDown:

```
mov ebp, esp
```

```
cmp [ebp+4], 0
```

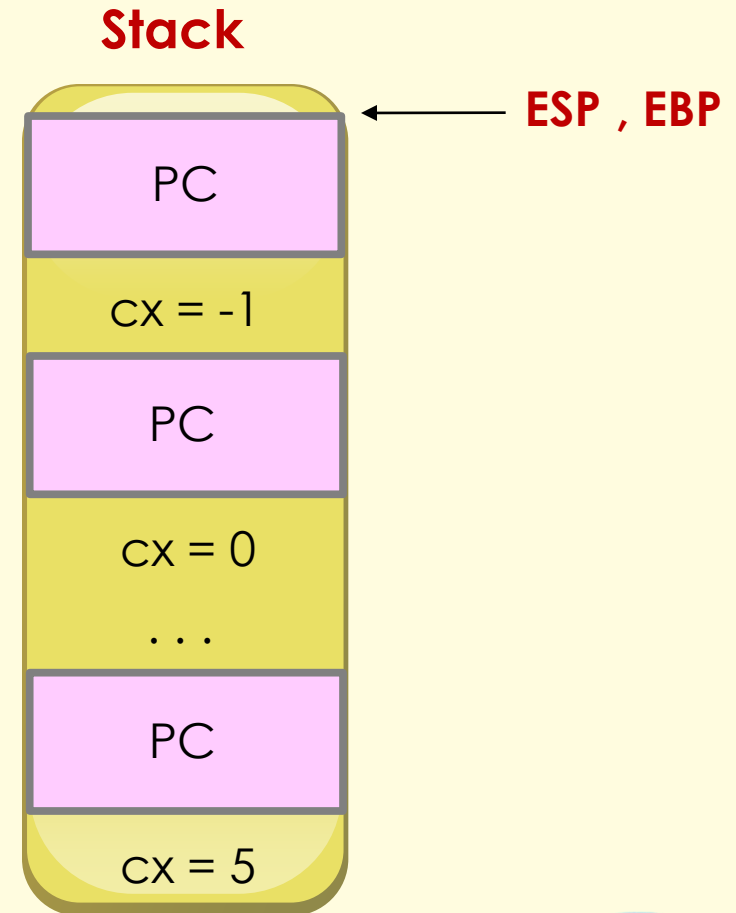
```
jl countEnd
```

...

```
call countDown
```

countEnd:

```
ret 2
```



Recursive Functions

countDown:

```
mov ebp, esp
```

```
cmp [ebp+4], 0
```

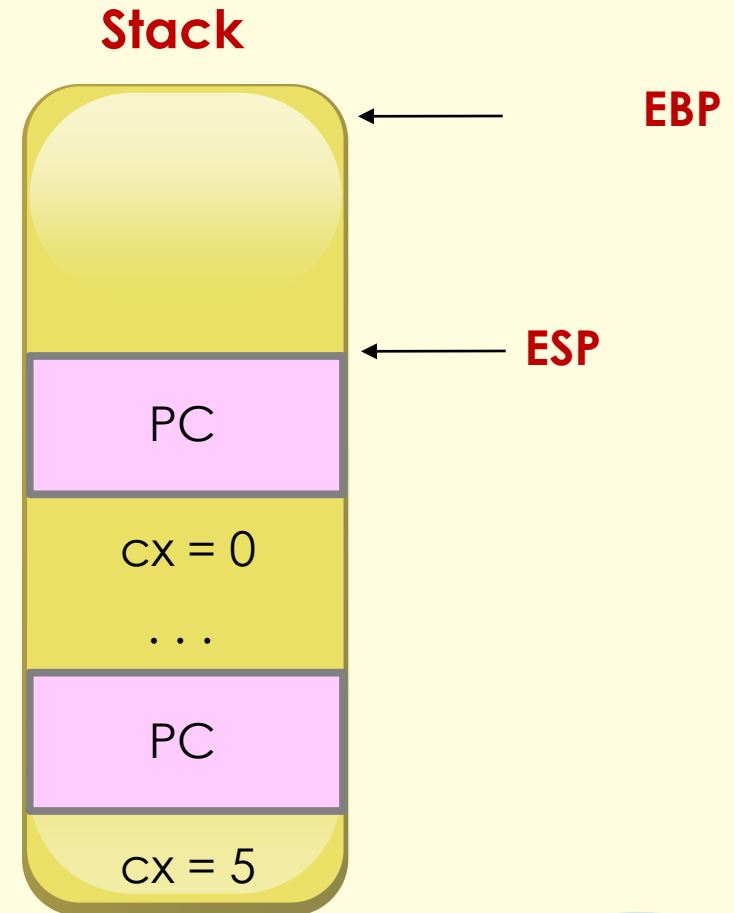
```
jl countEnd
```

...

```
call countDown
```

countEnd:

```
ret 2
```



Recursive Functions

countDown:

```
mov ebp, esp
```

```
cmp [ebp+4], 0
```

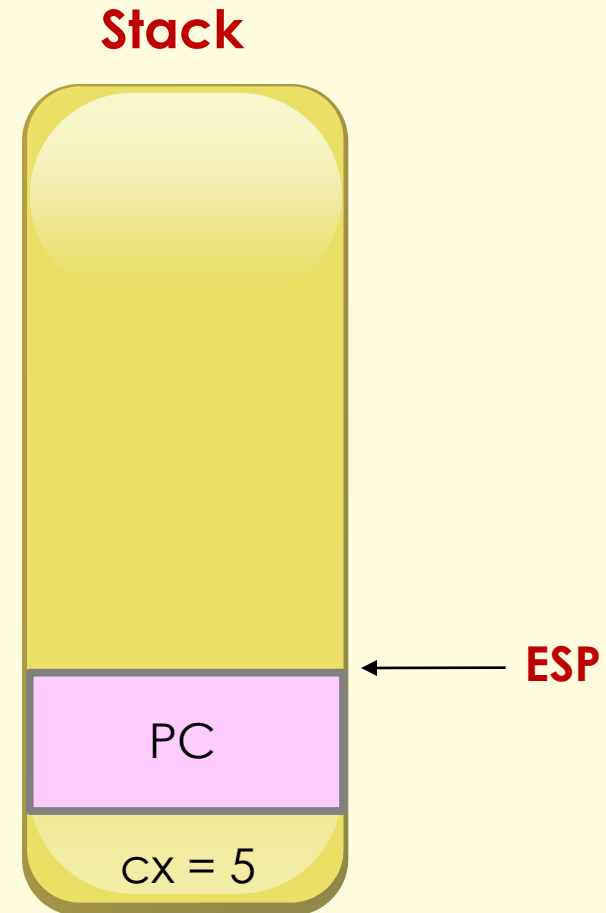
```
jl countEnd
```

...

```
call countDown
```

countEnd:

```
ret 2
```





Recursive Functions

```
mov cx, 5  
push cx  
call countDown  
...
```

countDown:

```
mov ebp, esp  
cmp [ebp+4], 0  
jl countEnd  
add [ebp+4], 30h
```

```
mov eax, 4  
mov ebx, 1  
lea ecx, [ebp+4]  
mov edx, 1  
int 80h  
sub [ebp+4], 30h  
mov cx, [ebp+4]  
dec cx  
push cx  
call countDown  
countEnd:  
ret 2
```





Recursive Functions

- product of X and Y by recursive addition
- $X * Y = X + [X * (Y - 1)]$
- $X * 1 = X$
- $X * 0 = 0$





Recursive Functions

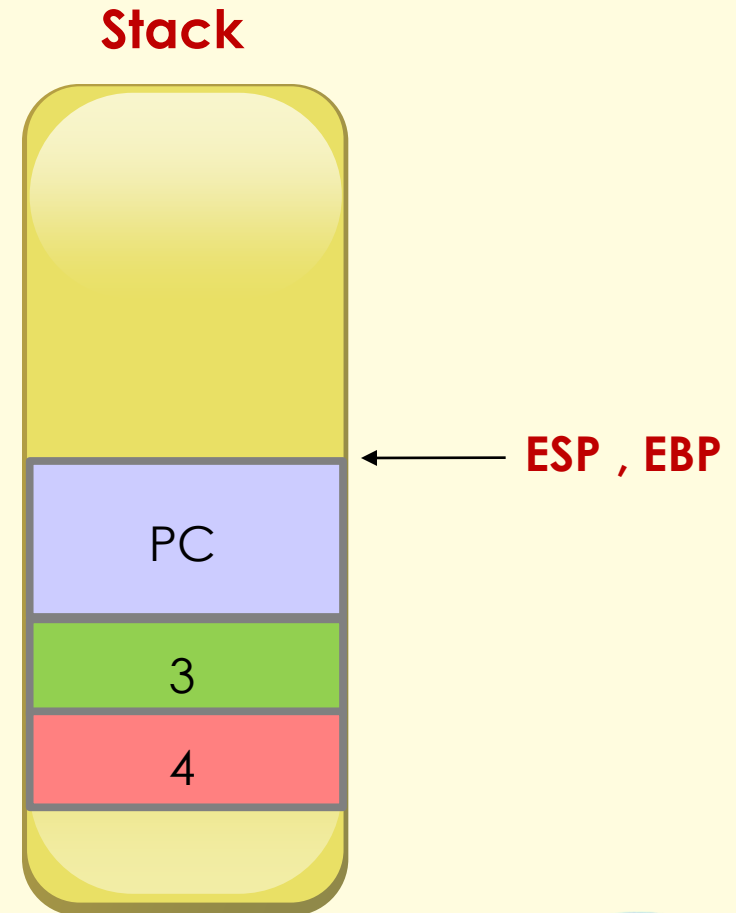
```
int product (int x, int y) {  
    if (y == 1) return x;  
    if (y == 0) return 0;  
    return (x + product(x, y-1));  
}
```

Example: `prod = product(4,3);`



Recursive Functions

```
sub esp, 2  
push word[x]  
push word[y]  
call product  
pop word[prod]
```

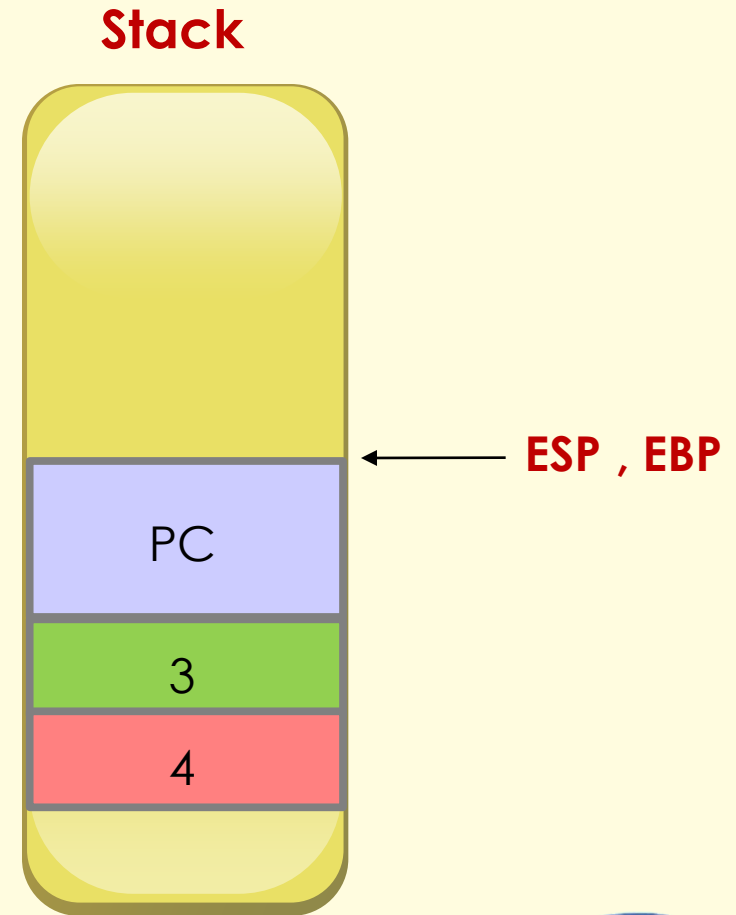




Recursive Functions

product:

```
mov ebp, esp
```





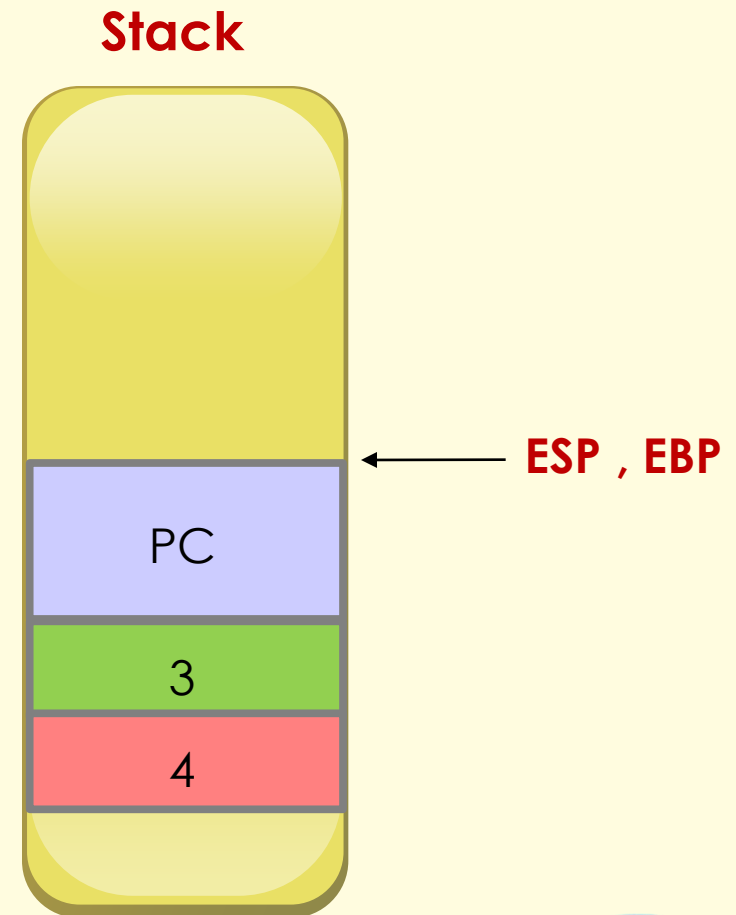
Recursive Functions

product:

```
mov ebp, esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```



Recursive Functions

product:

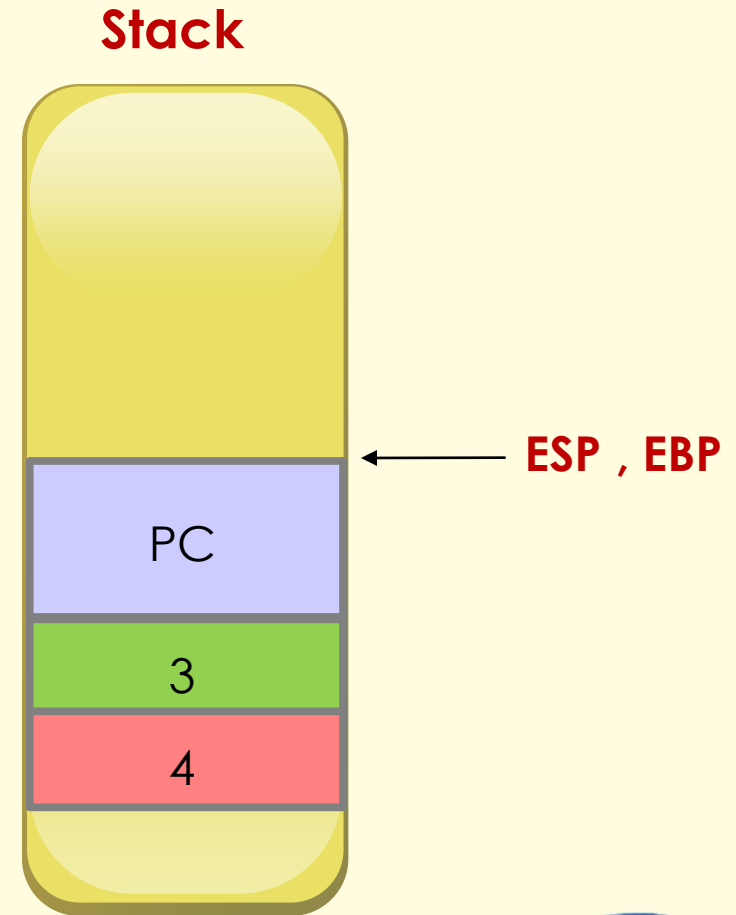
```
mov ebp, esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```

```
cmp word[ebp+4], 0
```

```
je return_o
```



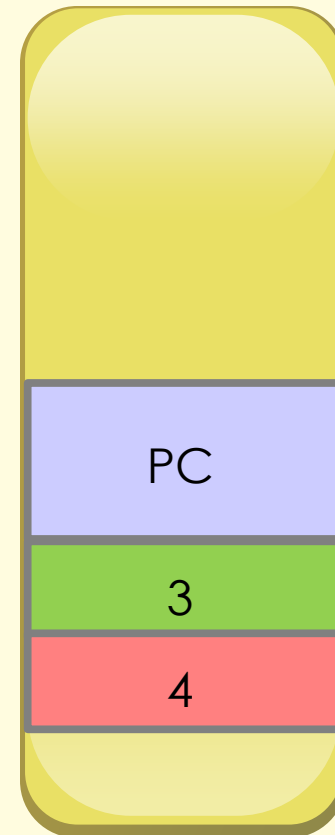
Recursive Functions

product:

```
mov ebp, esp  
cmp word[ebp+4], 1  
je return_x  
cmp word[ebp+4], 0  
je return_o  
mov ax, [ebp+4]
```

Stack

ax = 3



ESP, EBP





Recursive Functions

product:

```
mov ebp, esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```

```
cmp word[ebp+4], 0
```

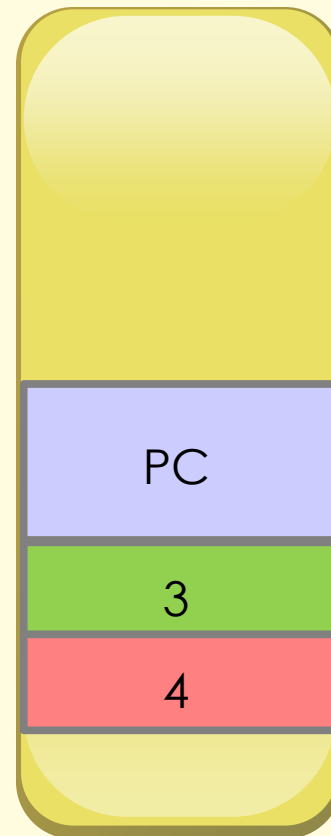
```
je return_o
```

```
mov ax, [ebp+4]
```

```
dec ax
```

Stack

ax = 2



ESP , EBP



Recursive Functions

product:

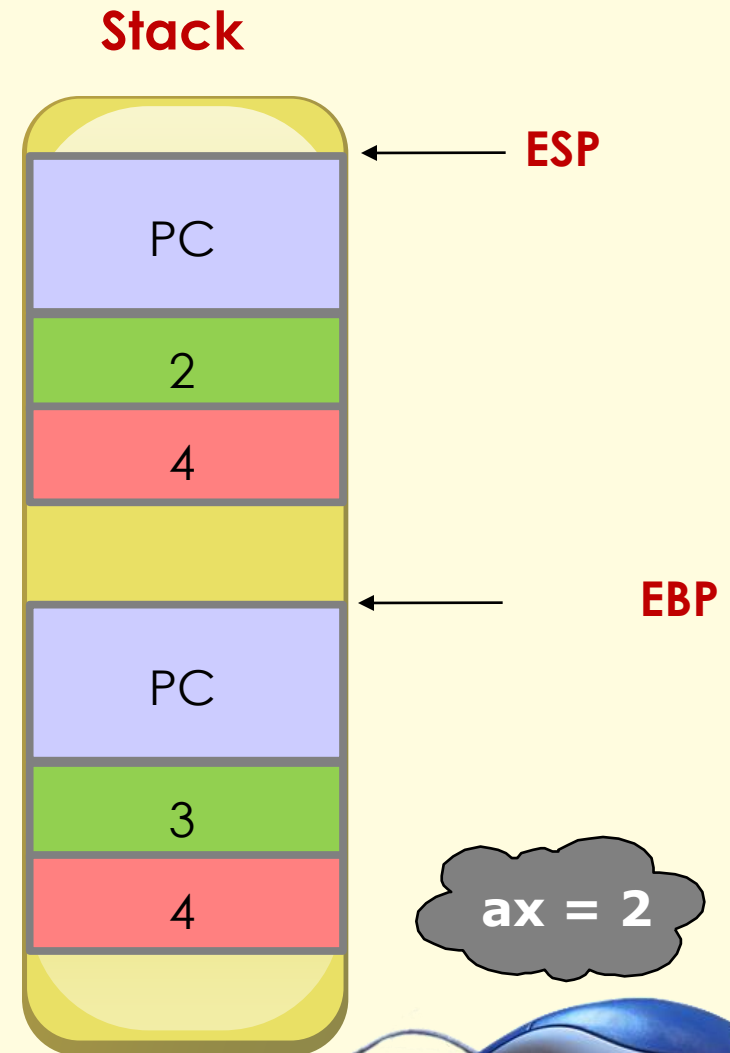
; recursive call

sub esp, 2

push word[ebp+6]

push ax

call product



Recursive Functions

product:

```
mov ebp,esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```

```
cmp word[ebp+4], 0
```

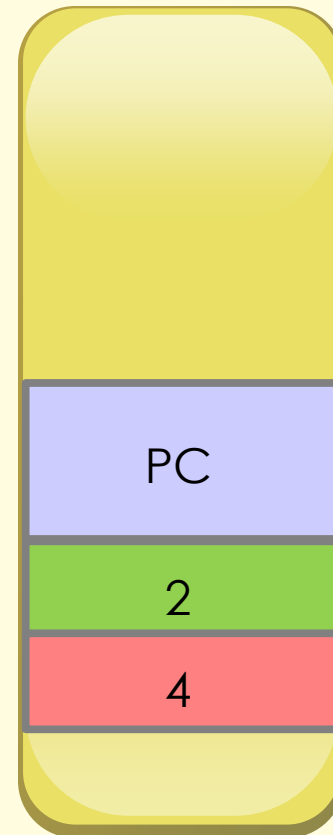
```
je return_o
```

```
mov ax, [ebp+4]
```

```
dec ax
```

Stack

ax = 1



ESP, EBP



Recursive Functions

product:

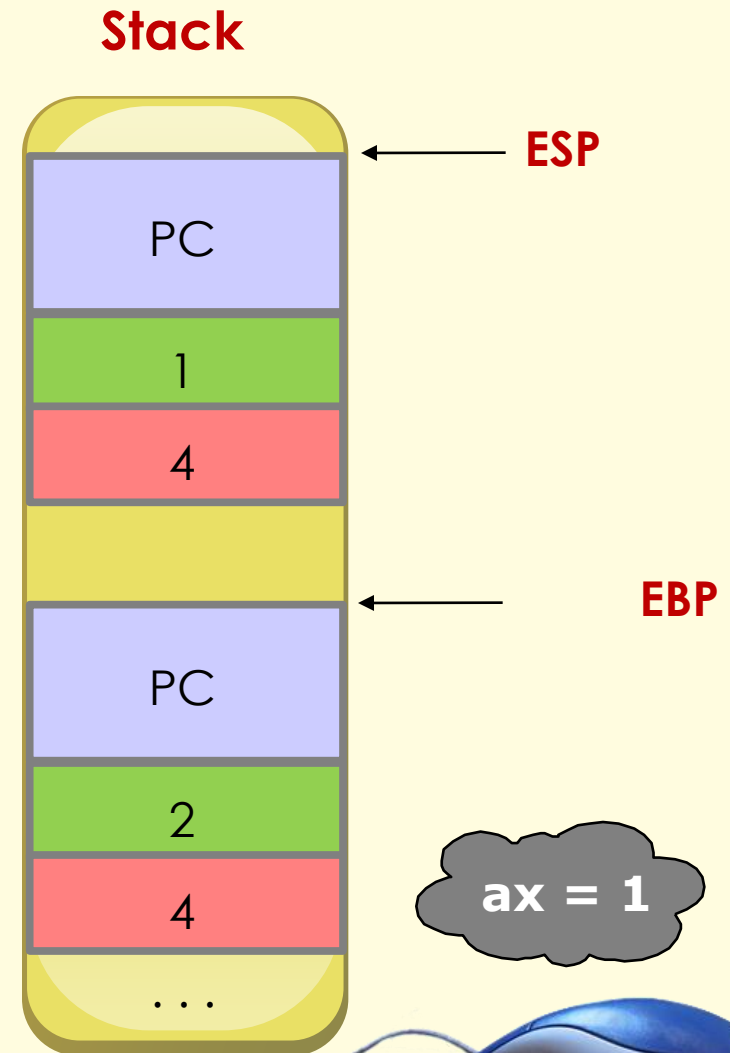
; recursive call

sub esp, 2

push word[ebp+6]

push ax

call product





Recursive Functions

product:

```
mov ebp,esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```

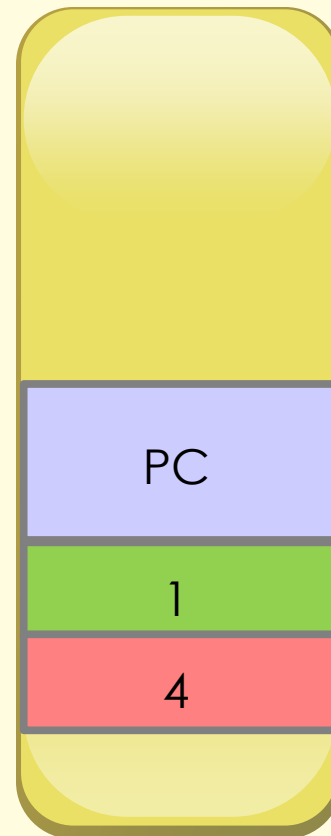
```
cmp word[ebp+4], 0
```

```
je return_o
```

```
mov ax, [ebp+4]
```

```
dec ax
```

Stack



ESP , EBP





Recursive Functions

product:

```
mov ebp,esp
```

```
cmp word[ebp+4], 1
```

```
je return_x
```

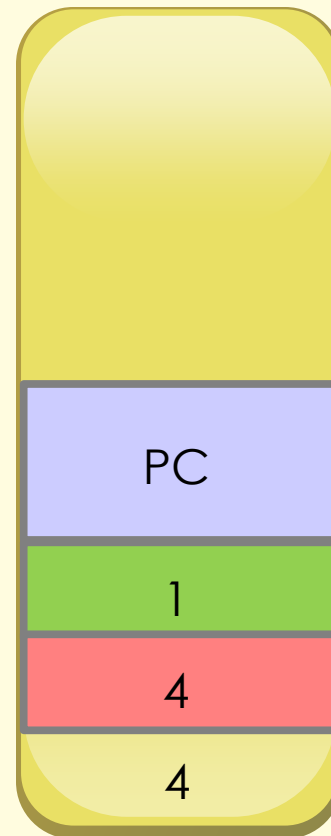
```
cmp word[ebp+4], 0
```

```
je return_o
```

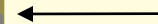
```
mov ax, [ebp+4]
```

```
dec ax
```

Stack



ESP , EBP



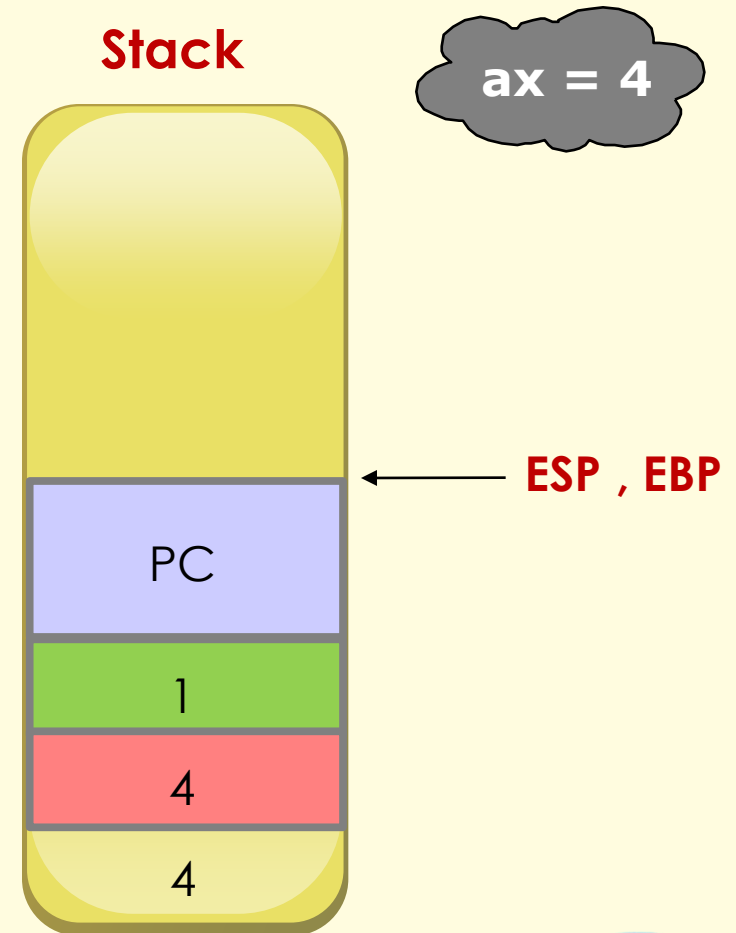
Recursive Functions

return_x:

mov ax, [ebp+6]

mov [ebp+8], ax

jmp exit



Recursive Functions

```
return_x:
```

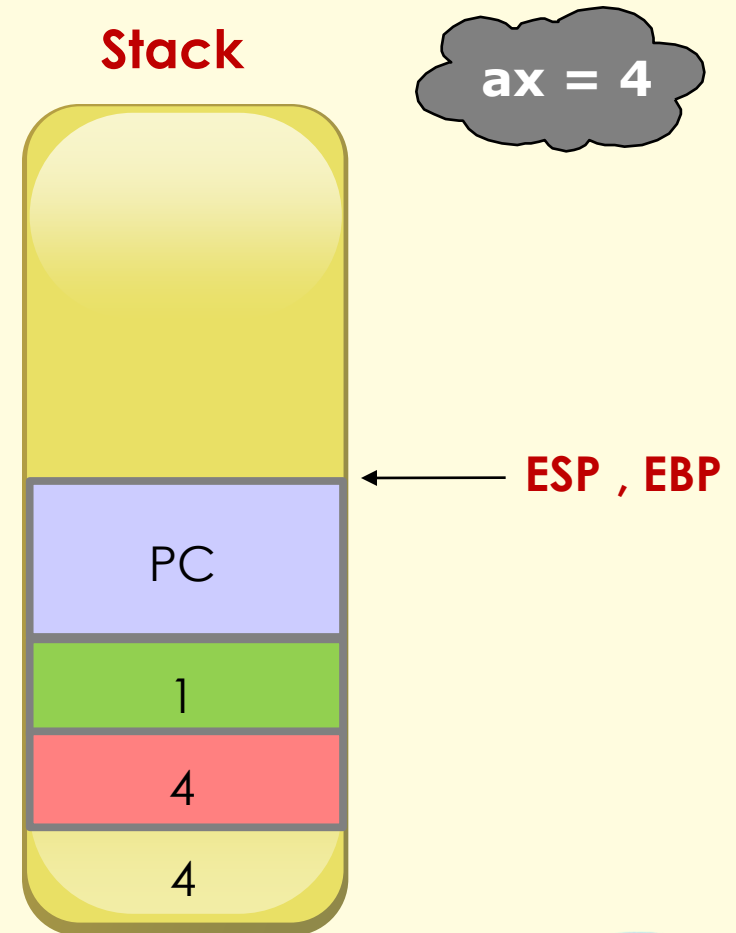
```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```



Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

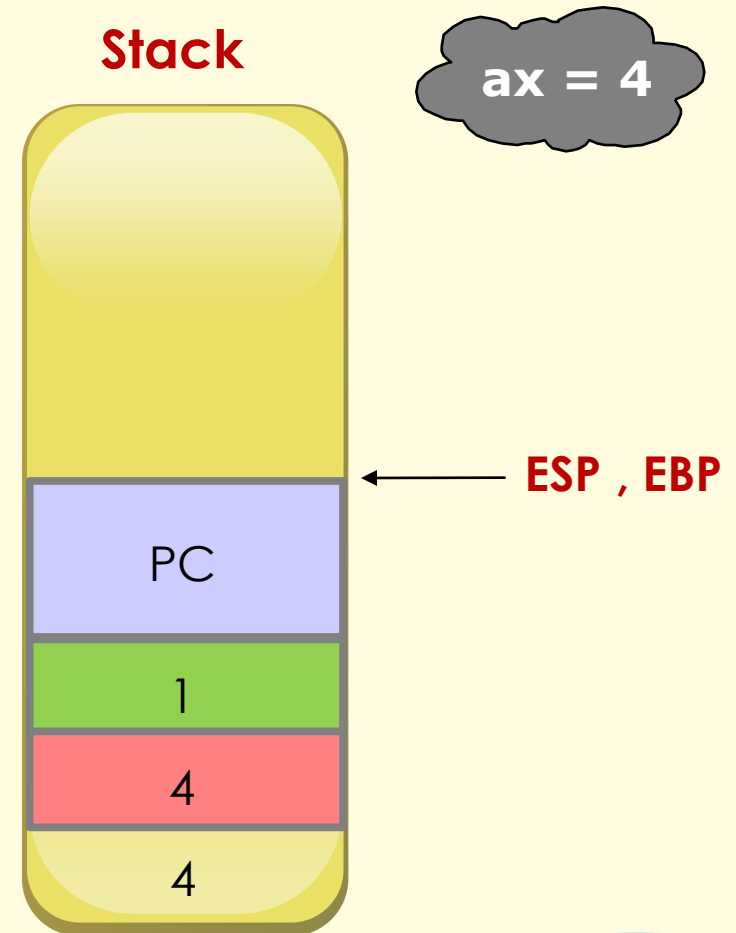
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

```
    ret 4
```



Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

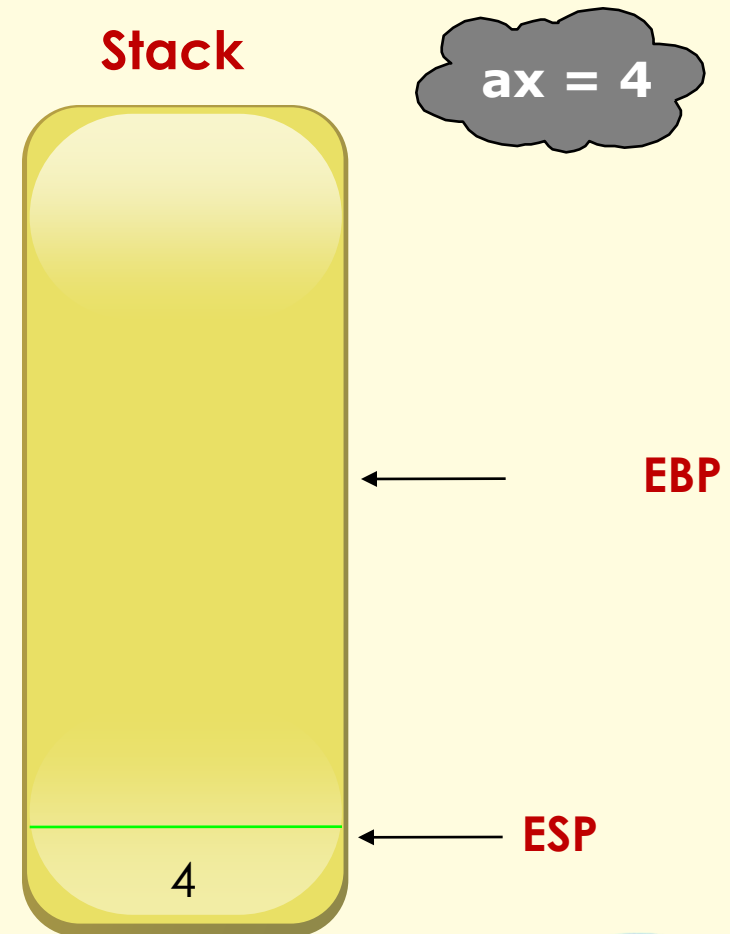
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

```
    ret 4
```





Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

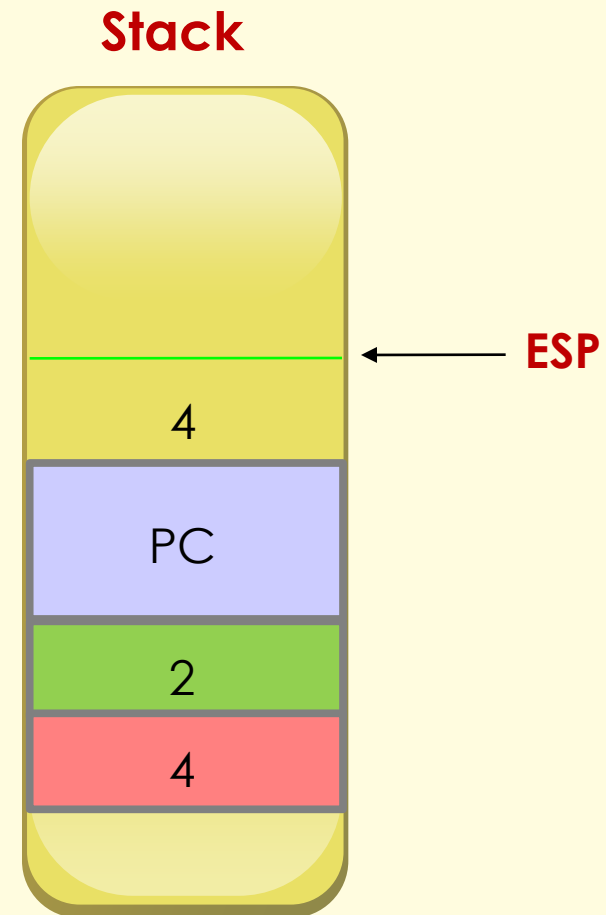
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

```
    ret 4
```





Recursive Functions

product:

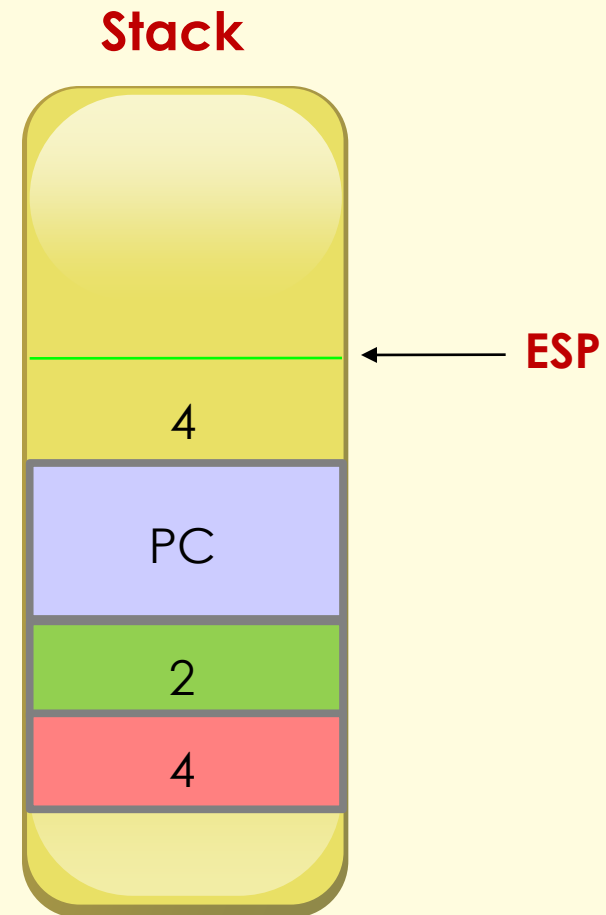
; recursive call

sub esp, 2

push word[ebp+6]

push ax

call product





Recursive Functions

product:

; recursive call

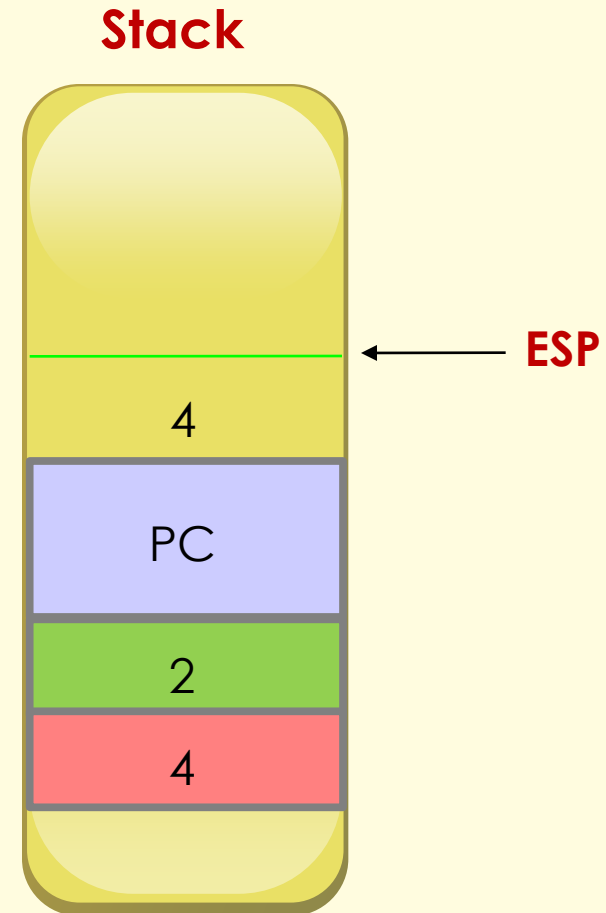
sub esp, 2

push word[ebp+6]

push ax

call product

pop bx



Recursive Functions

product:

; recursive call

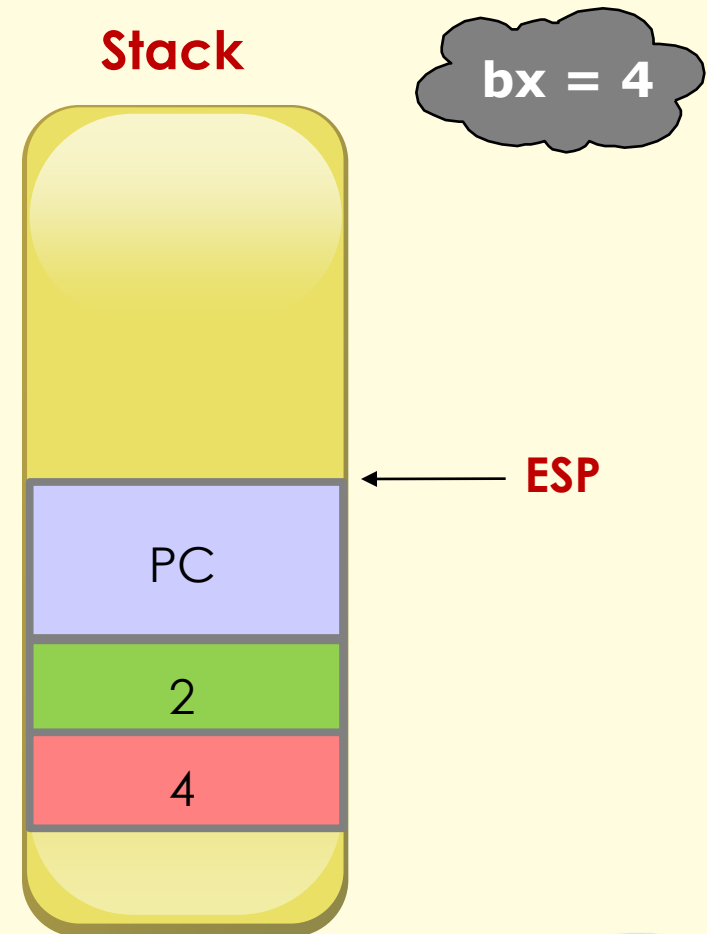
sub esp, 2

push word[ebp+6]

push ax

call product

pop bx



Recursive Functions

product:

; recursive call

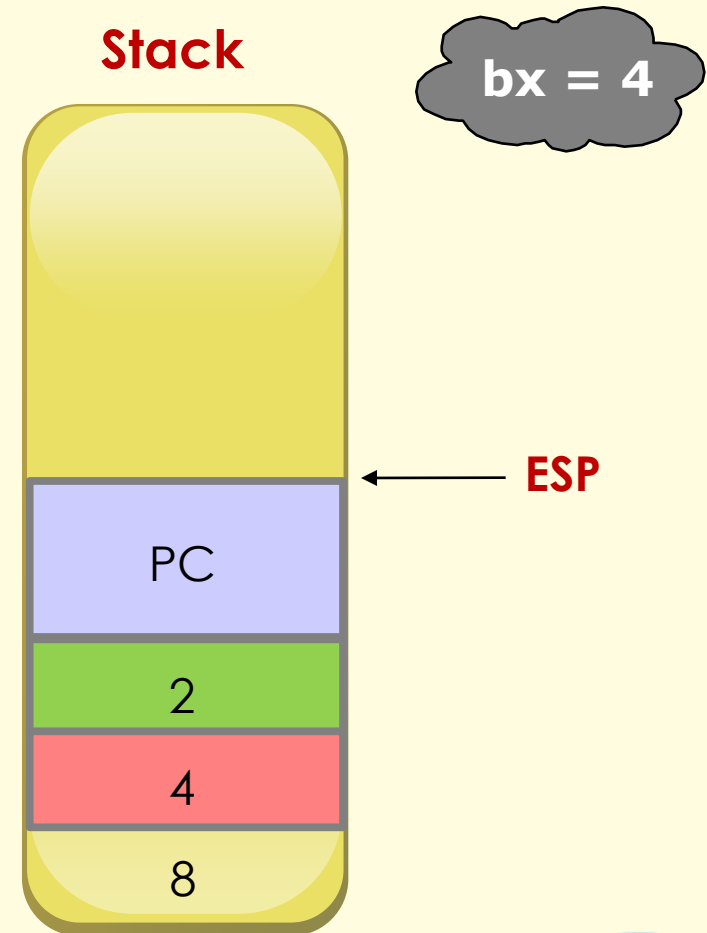
sub esp, 2

push word[ebp+6]

push ax

call product

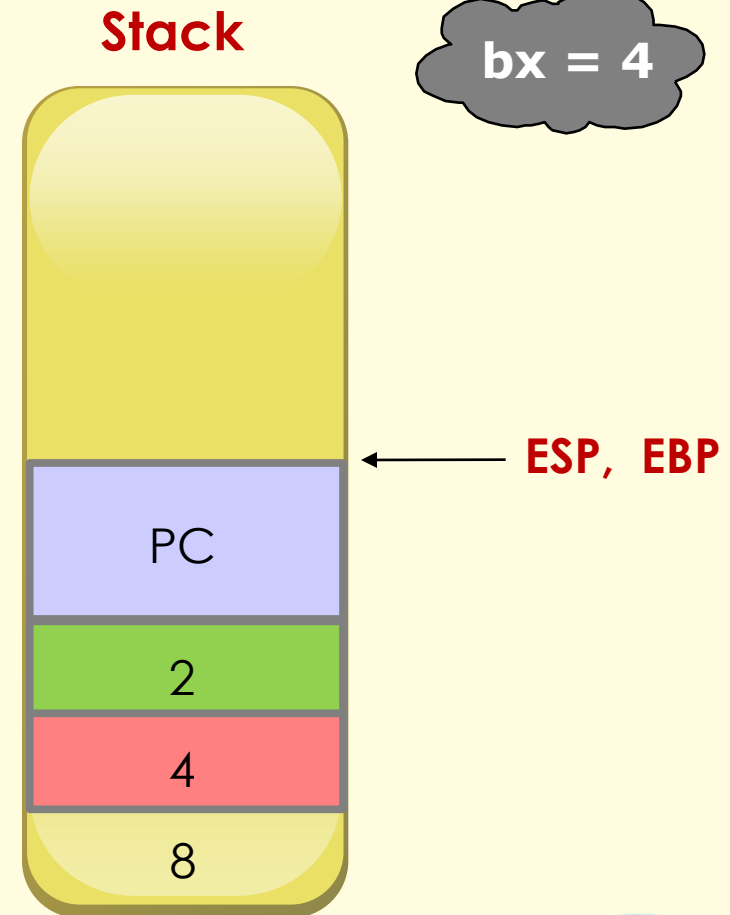
pop bx



Recursive Functions

product:

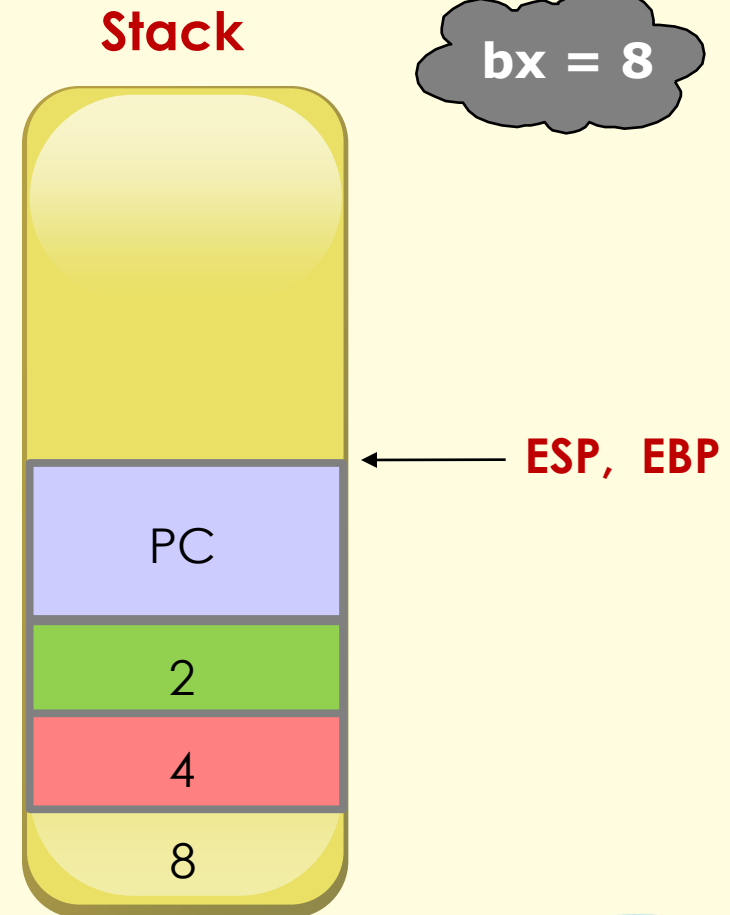
```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]
```



Recursive Functions

product:

```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]  
mov [ebp+8], bx  
jmp exit
```





Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

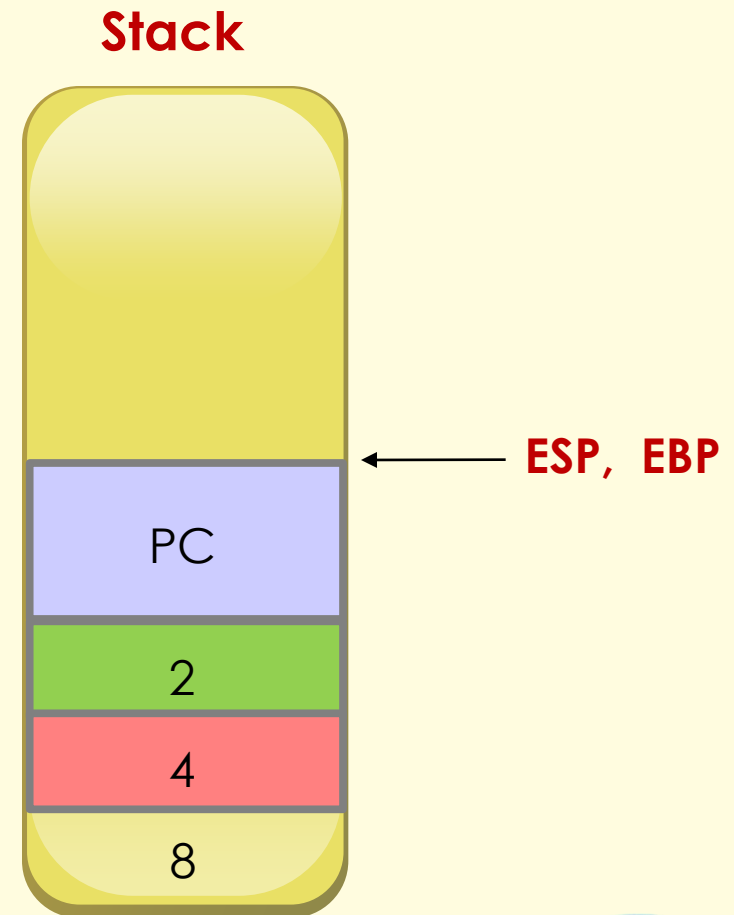
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

```
    ret 4
```





Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

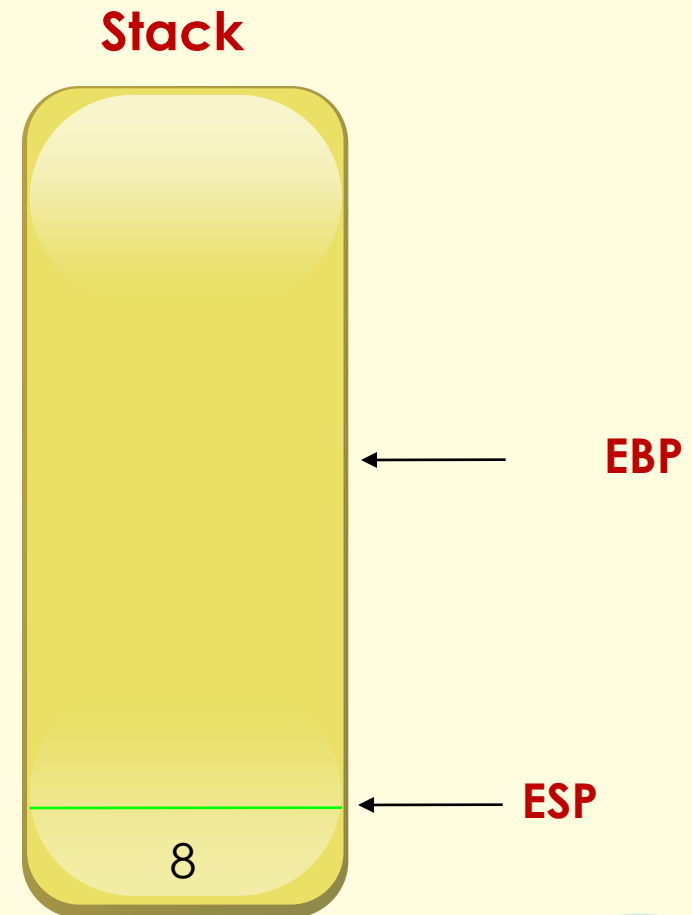
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

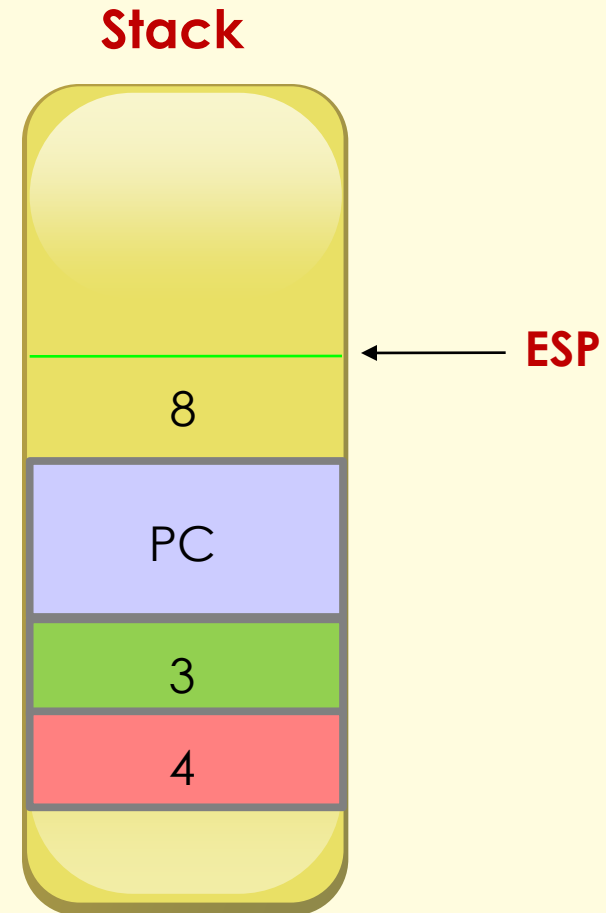
```
    ret 4
```



Recursive Functions

product:

```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]  
mov [ebp+8], bx  
jmp exit
```



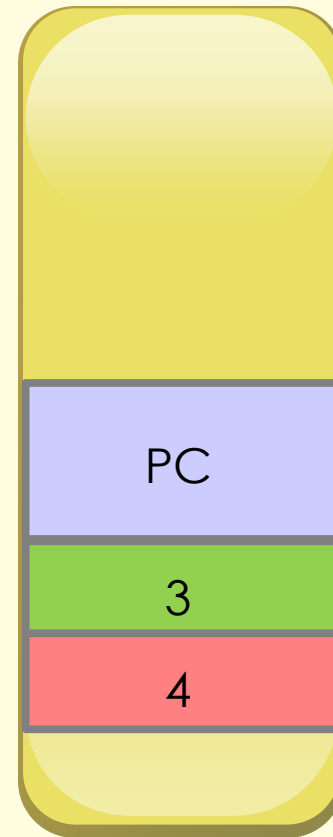
Recursive Functions

product:

```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]  
mov [ebp+8], bx  
jmp exit
```

Stack

bx = 8



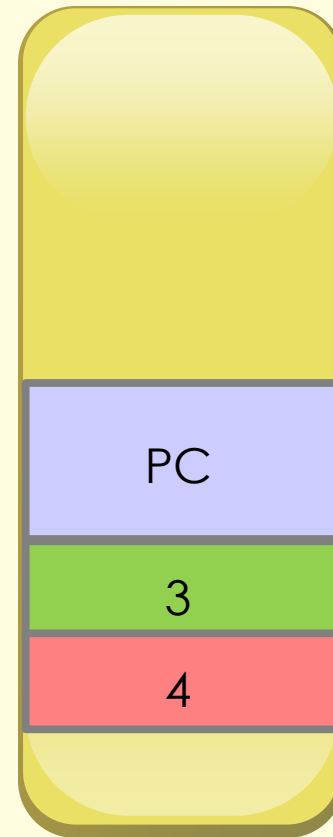
Recursive Functions

product:

```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]  
mov [ebp+8], bx  
jmp exit
```

Stack

bx = 12



ESP



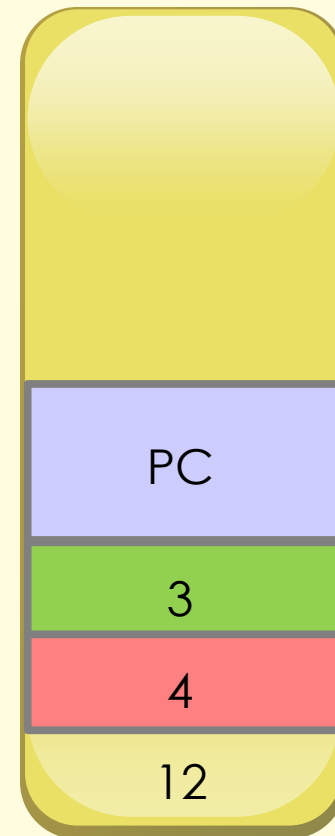
Recursive Functions

product:

```
; recursive call  
sub esp, 2  
push word[ebp+6]  
push ax  
call product  
pop bx  
mov ebp, esp  
add bx, [ebp+6]  
mov [ebp+8], bx  
jmp exit
```

Stack

bx = 12





Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

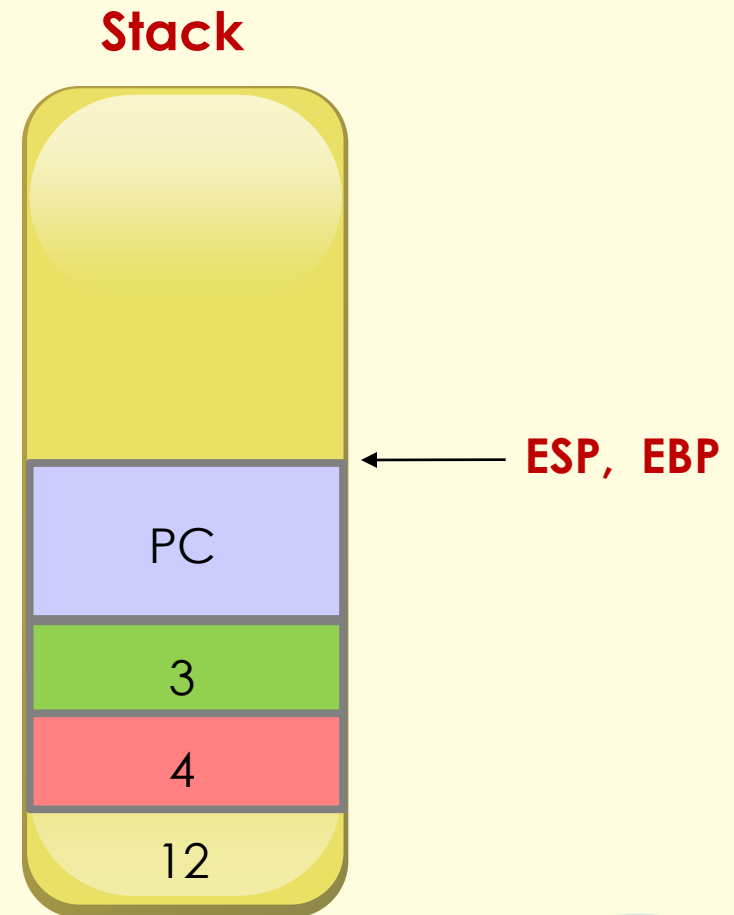
```
    jmp exit
```

```
return_o:
```

```
    mov word[ebp+8], 0
```

```
exit:
```

```
    ret 4
```





Recursive Functions

```
return_x:
```

```
    mov ax, [ebp+6]
```

```
    mov [ebp+8], ax
```

```
    jmp exit
```

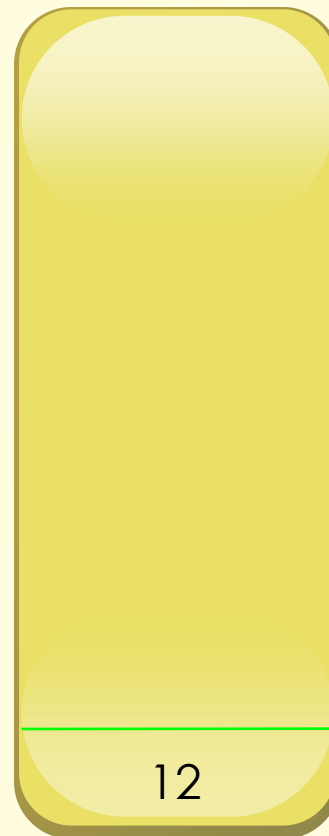
```
return_o:
```

```
    mov word[ebp+8], 0
```

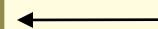
```
exit:
```

```
    ret 4
```

Stack



ESP



12





Recursive Functions

product:

```
mov ebp, esp
cmp word[ebp+4], 1
je return_x
cmp word[ebp+4], 0
je return_o
mov ax, [ebp+4]
dec ax
sub esp, 2
push word[ebp+6]
push ax
call product
```

```
pop bx
mov ebp, esp
add bx, [ebp+6]
mov [ebp+8], bx
jmp exit
return_x:
    mov ax, [ebp+6]
    mov [ebp+8], ax
    jmp exit
return_o:
    mov word[ebp+8], 0
exit:
    ret 4
```





Recursive Functions

- define base case
- define recursive case
- Factorial:
 - $X!$
 - $x * (x-1) * (x-2) * \dots * 2 * 1$
 - $x * (x-1)!$
 - $1! = 1$
 - $0! = 1$





Recursive Functions

```
int factorial (int x) {  
    if (x == 1) return 1;  
    if (x == 0) return 1;  
    return (x*factorial(x-1));  
}
```

```
f = factorial (n);
```

```
; function call
```

```
sub esp, 2
```

```
push word [n]
```

```
call factorial
```

```
pop word [f]
```





Recursive Functions

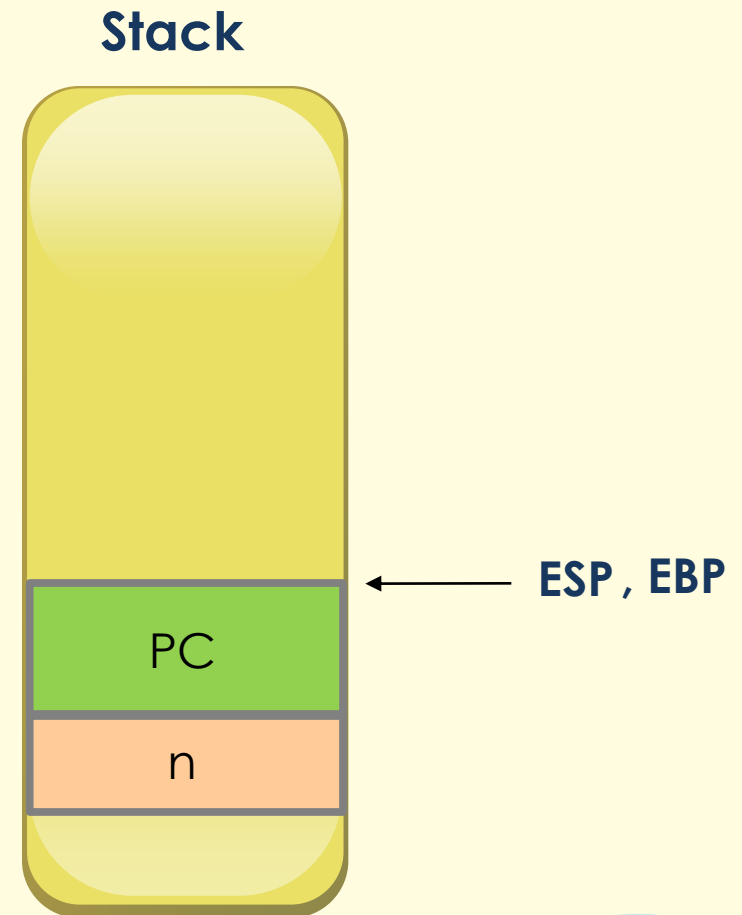
; function call

sub esp, 2

push word [n]

call factorial

pop word [f]





Recursive Functions

; function

factorial:

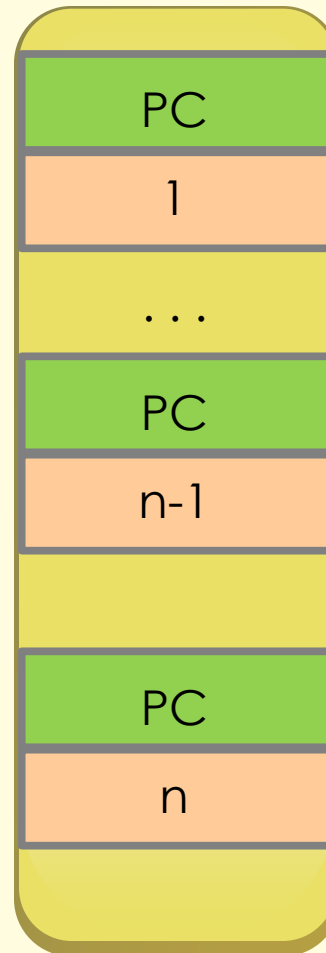
mov ebp, esp

...

; recursive call

...

Stack



**recursive
calls**





Recursive Functions

factorial:

```
mov ebp, esp
```

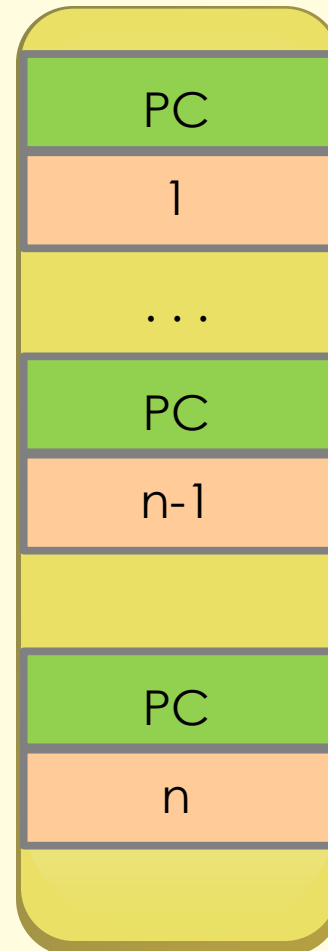
```
cmp [ebp + 4], 1
```

```
je factorial_end
```

```
cmp [ebp + 4], 0
```

```
je factorial_end
```

Stack



**recursive
calls**





Recursive Functions

factorial:

```
mov ebp, esp
```

```
...
```

```
mov cx, [ebp+4]
```

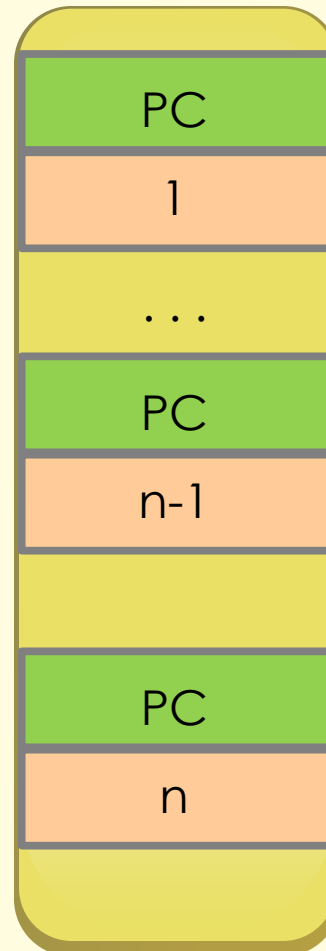
```
dec cx
```

```
sub esp, 2
```

```
push cx
```

```
call factorial
```

Stack





Recursive Functions

factorial:

```
mov ebp, esp
```

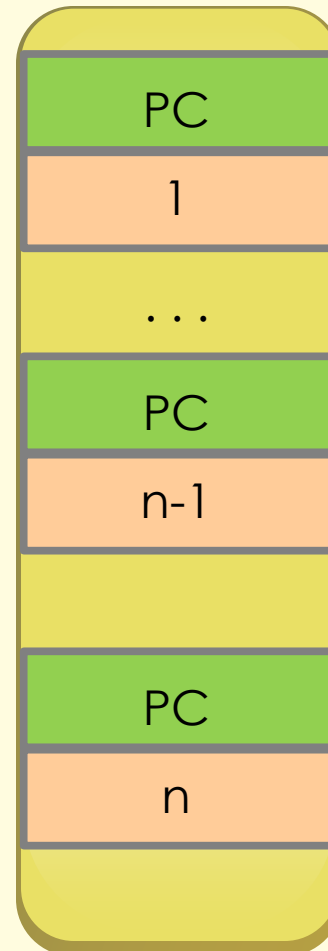
```
cmp [ebp + 4], 1
```

```
je factorial_end
```

```
cmp [ebp + 4], 0
```

```
je factorial_end
```

Stack



**recursive
calls**



Recursive Functions

factorial:

...

```
mov cx, [ebp+4]
```

```
dec cx
```

```
sub esp, 2
```

```
push cx
```

```
call factorial
```

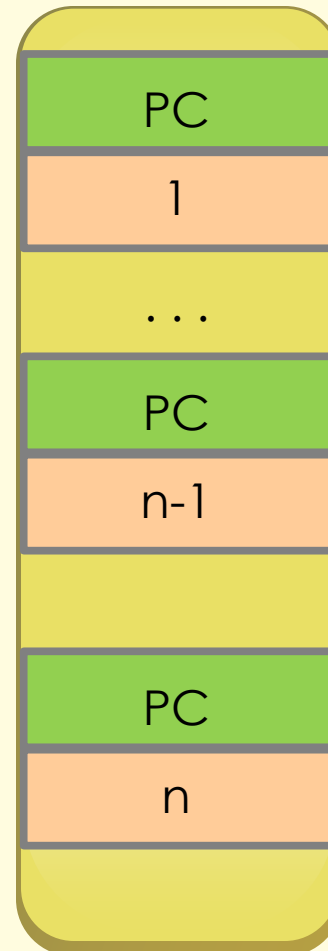
...

factorial_end:

```
mov word [ebp + 6], 1
```

```
ret 2
```

Stack



**recursive
calls**



Recursive Functions

factorial:

...

```
mov cx, [ebp+4]
```

```
dec cx
```

```
sub esp, 2
```

```
push cx
```

```
call factorial
```

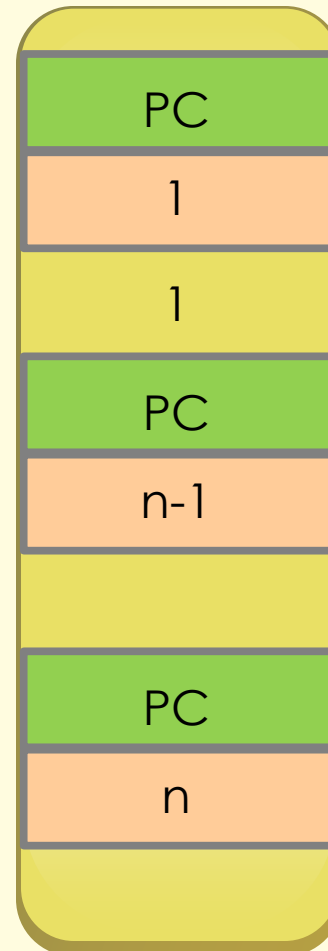
...

```
factorial_end:
```

```
mov word [ebp + 6], 1
```

```
ret 2
```

Stack



**recursive
calls**





Recursive Functions

factorial:

...

```
mov cx, [ebp+4]
```

```
dec cx
```

```
sub esp, 2
```

```
push cx
```

```
call factorial
```

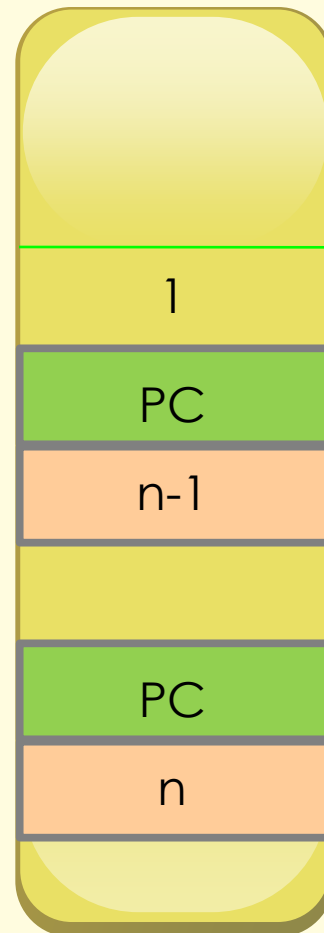
...

factorial_end:

```
mov word [ebp + 6], 1
```

```
ret 2
```

Stack



**recursive
calls**



Recursive Functions

factorial:

...

```
mov cx, [ebp+4]
```

```
dec cx
```

```
sub esp, 2
```

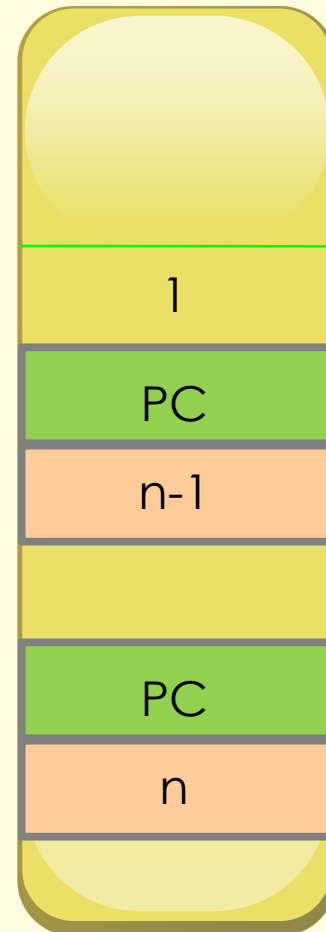
```
push cx
```

```
call factorial
```

```
pop cx
```

...

Stack



**recursive
calls**



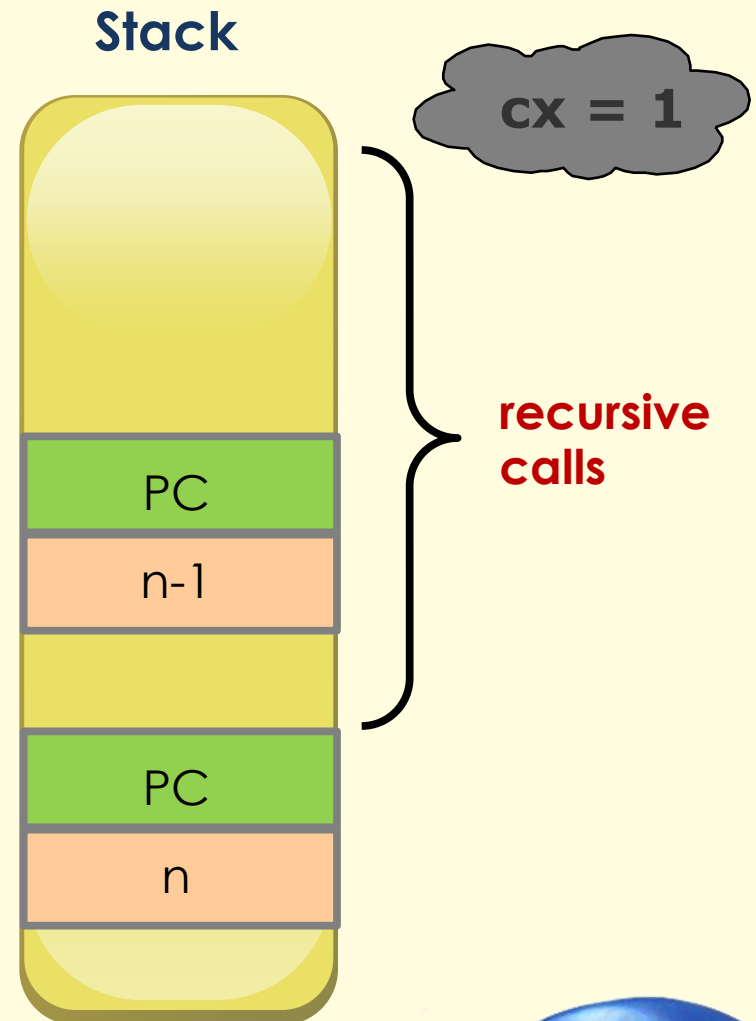


Recursive Functions

factorial:

...

pop cx





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

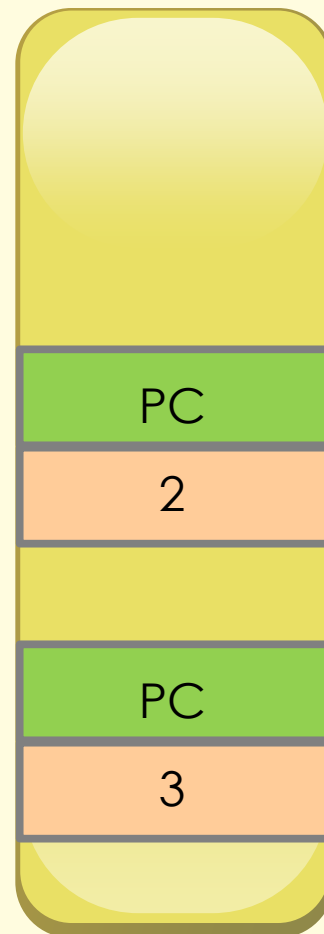
mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack



CX = 1

**recursive
calls**





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

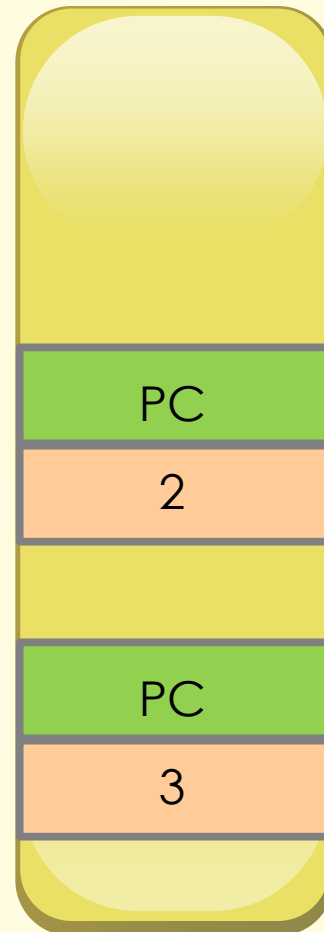
mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack



ax = 1

**recursive
calls**





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

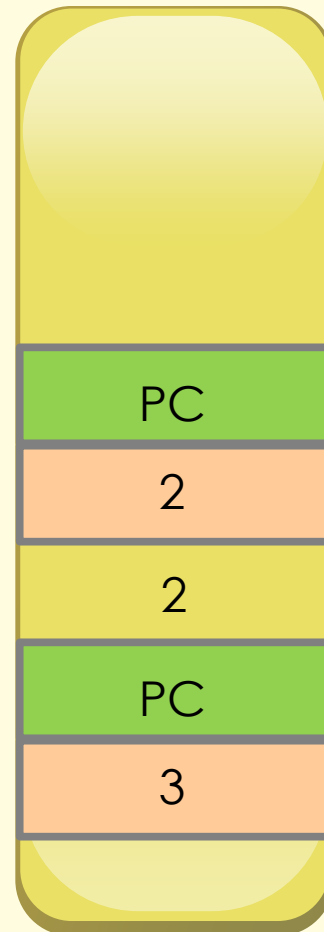
mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack



ax = 2

**recursive
calls**





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

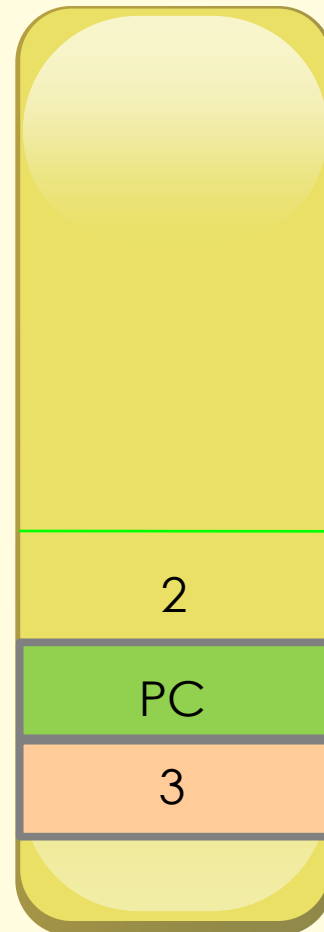
mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack



ax = 2

**recursive
calls**





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack





Recursive Functions

factorial:

...

pop cx

mov ebp, esp

mov ax, cx

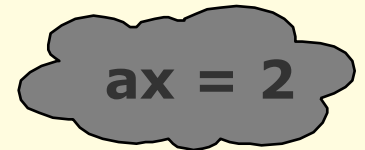
mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

...

Stack





Recursive Functions

factorial:

```
mov ebp, esp
cmp [ebp + 4], 1
je factorial_end
cmp [ebp + 4], 0
je factorial_end
mov cx, [ebp+4]
dec cx
sub esp, 2
push cx
call factorial
```

pop cx

mov ebp, esp

mov ax, cx

mul word [ebp + 4]

mov word [ebp + 6], ax

ret 2

factorial_end:

mov word [ebp + 6], 1

ret 2

