# Simple Reserve Report Example

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#### Abstract

This document demonstrates how a very simple actuarial reserve report could be created using R. This document is only for display purposes. It was created using insurance loss data freely available on the CAS website. I am just getting started with LATEX and will have more clearly documented reports in subsequent examples.

## Purpose

Ractuary was requested by Nsure Ance Company (NAC) to provide a reserve estimate for their workers' compensation loss and alocated loss adjustment expense (ALAE) reserves. Losses are evaluated as of December 31, 1997...

## Background

NAC began offering workers' compensation coverage in 1988. Each policy is written on a calendar year basis (i.e. beginning January 1 and ending December 31). NAC has never purchased reinsurense coverage...

#### Other Stuff

Blah blah...

### Conclusions

A summary of our reserve analysis is as follows:

Exhibit I: Reserve Summary

|        | $Paid^1$    | $Incurred^2$ | $Ultimate^3$ | Case OS    | IBNR       | Total OS    |
|--------|-------------|--------------|--------------|------------|------------|-------------|
| 1988   | 125,049     | 133,513      | 138,993      | 8,464      | 5,480      | 13,944      |
| 1989   | $147,\!358$ | $161,\!673$  | 167,073      | $14,\!315$ | 5,400      | 19,715      |
| 1990   | 187,760     | 210,204      | 216,633      | 22,444     | $6,\!429$  | 28,873      |
| 1991   | $213,\!396$ | 244,669      | $252,\!263$  | $31,\!273$ | $7,\!594$  | $38,\!867$  |
| 1992   | 213,904     | $253,\!878$  | 261,087      | 39,974     | 7,209      | $47,\!183$  |
| 1993   | $193,\!676$ | 251,129      | $253,\!250$  | $57,\!453$ | 2,121      | $59,\!574$  |
| 1994   | 151,081     | 202,911      | 209,512      | 51,830     | 6,601      | 58,431      |
| 1995   | 111,268     | 174,496      | 211,166      | 63,228     | 36,670     | 99,898      |
| 1996   | 66,033      | 143,042      | $174,\!486$  | 77,009     | $31,\!444$ | $108,\!453$ |
| 1997   | $25,\!265$  | $125,\!429$  | 179,035      | 100,164    | $53,\!606$ | 153,770     |
| Totals | 1,434,790   | 1,900,944    | 2,063,498    | 466,154    | 162,554    | 628,708     |

From the table above, estimated ultimate loss & ALAE as of December 31, 1997 is %#0.0-1e indicating a total outstanding loss & ALAE of %#0.0-1e.

## Methodology

We used two actuarial projection techniques (paid projection and incurred projection) in creating the final estimated ultimate loss projection. The loss projections use loss experience for the more mature accident years to estimate the development of less mature accident years. See the following exhibits for detail regarding the projections and estimated ultimate loss and ALAE selection.

<sup>&</sup>lt;sup>1</sup>See Exhibit III, Sheet 1

<sup>&</sup>lt;sup>2</sup>See Exhibit IV, Sheet 1

<sup>&</sup>lt;sup>3</sup>See Exhibit II

## Exhibits

Exhibit II: Selection of Estimated Ultimate Loss and ALAE

|        | Paid Projection <sup>1</sup> | Incurred Projection <sup>2</sup> | Selected Ultimate <sup>3</sup> |
|--------|------------------------------|----------------------------------|--------------------------------|
| 1988   | 143,806                      | 134,181                          | 138,993                        |
| 1989   | 171,665                      | 162,481                          | 167,073                        |
| 1990   | 222,012                      | 211,255                          | 216,633                        |
| 1991   | 258,633                      | $245,\!892$                      | 252,263                        |
| 1992   | 267,026                      | $255{,}147$                      | 261,087                        |
| 1993   | 253,863                      | 252,637                          | 253,250                        |
| 1994   | 213,874                      | 205,150                          | 209,512                        |
| 1995   | 244,146                      | 178,186                          | 211,166                        |
| 1996   | 195,602                      | 153,370                          | 174,486                        |
| 1997   | 202,067                      | 156,003                          | 179,035                        |
| Totals | 2,172,694                    | 1,954,303                        | 2,063,498                      |

 $<sup>^1\</sup>mathrm{See}$  Exhibit III, Sheet 1  $^2\mathrm{See}$  Exhibit IV, Sheet 1  $^3\mathrm{The}$  average of the paid and incurred projections

Exhibit III, Sheet 1: Paid Projection

|      | 1           |                  |             |
|------|-------------|------------------|-------------|
|      | $Paid^1$    | $\mathrm{LDF}^2$ | Ultimate    |
| 1988 | 125,049     | 1.150            | 143,806     |
| 1989 | $147,\!358$ | 1.165            | $171,\!665$ |
| 1990 | 187,760     | 1.182            | 222,012     |
| 1991 | $213,\!396$ | 1.212            | $258,\!633$ |
| 1992 | 213,904     | 1.248            | 267,026     |
| 1993 | 193,676     | 1.311            | $253,\!863$ |
| 1994 | 151,081     | 1.416            | $213,\!874$ |
| 1995 | 111,268     | 2.194            | $244,\!146$ |
| 1996 | 66,033      | 2.962            | 195,602     |
| 1997 | $25,\!265$  | 7.998            | 202,067     |

<sup>&</sup>lt;sup>1</sup>See Exhibit III, Sheet 2 <sup>2</sup>See Exhibit III, Sheet 3

Exhibit III, Sheet 2: Paid Triangle

|      | 1          | 2           | 3           | 4           | 5           | 6           | 7           | 8       | 9           | 10      |
|------|------------|-------------|-------------|-------------|-------------|-------------|-------------|---------|-------------|---------|
| 1988 | 22,190     | 60,834      | 85,104      | 100,151     | 108,812     | 114,967     | 118,790     | 121,558 | 123,492     | 125,049 |
| 1989 | $26,\!542$ | 77,798      | $106,\!407$ | $122,\!422$ | $133,\!359$ | $138,\!599$ | 143,029     | 145,712 | $147,\!358$ |         |
| 1990 | 32,977     | 100,494     | 134,886     | 157,758     | 168,991     | 178,065     | 182,787     | 187,760 |             |         |
| 1991 | 38,604     | $114,\!428$ | 157,103     | 181,322     | 197,411     | 208,804     | $213,\!396$ |         |             |         |
| 1992 | $42,\!466$ | 125,820     | 164,776     | 189,045     | $204,\!377$ | 213,904     |             |         |             |         |
| 1993 | 46,447     | 116,764     | $154,\!897$ | 179,419     | 193,676     |             |             |         |             |         |
| 1994 | $41,\!368$ | 100,344     | 132,021     | 151,081     |             |             |             |         |             |         |
| 1995 | 35,719     | 83,216      | 111,268     |             |             |             |             |         |             |         |
| 1996 | 28,746     | 66,033      |             |             |             |             |             |         |             |         |
| 1997 | $25,\!265$ |             |             |             |             |             |             |         |             |         |

Exhibit III, Sheet 3:Paid Development Factor Triangle

|          | 1-2    | 2-3    | 3-4    | 4-5    | 5-6    | 6-7    | 7-8    | 8-9    | 9-10   | 10-Ult. |
|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 1988     | 2.7415 | 1.3990 | 1.1768 | 1.0865 | 1.0566 | 1.0333 | 1.0233 | 1.0159 | 1.0126 |         |
| 1989     | 2.9311 | 1.3677 | 1.1505 | 1.0893 | 1.0393 | 1.0320 | 1.0188 | 1.0113 |        |         |
| 1990     | 3.0474 | 1.3422 | 1.1696 | 1.0712 | 1.0537 | 1.0265 | 1.0272 |        |        |         |
| 1991     | 2.9641 | 1.3729 | 1.1542 | 1.0887 | 1.0577 | 1.0220 |        |        |        |         |
| 1992     | 2.9628 | 1.3096 | 1.1473 | 1.0811 | 1.0466 |        |        |        |        |         |
| 1993     | 2.5139 | 1.3266 | 1.1583 | 1.0795 |        |        |        |        |        |         |
| 1994     | 2.4256 | 1.3157 | 1.1444 |        |        |        |        |        |        |         |
| 1995     | 2.3297 | 1.3371 |        |        |        |        |        |        |        |         |
| 1996     | 2.2971 |        |        |        |        |        |        |        |        |         |
| Simple   | 2.6904 | 1.3464 | 1.1573 | 1.0827 | 1.0508 | 1.0284 | 1.0231 | 1.0136 | 1.0126 |         |
| Weighted | 2.6844 | 1.3421 | 1.1561 | 1.0823 | 1.0509 | 1.0274 | 1.0234 | 1.0134 | 1.0126 |         |
| Selected | 2.7000 | 1.3500 | 1.5500 | 1.0800 | 1.0500 | 1.0300 | 1.0250 | 1.0150 | 1.0130 | 1.1500  |

Incurred Projection

|      | $Incurred^1$ | $LDF^2$ | Ultimate    |
|------|--------------|---------|-------------|
| 1988 | $133,\!513$  | 1.005   | 134,181     |
| 1989 | $161,\!673$  | 1.005   | $162,\!481$ |
| 1990 | $210,\!204$  | 1.005   | $211,\!255$ |
| 1991 | 244,669      | 1.005   | 245,892     |
| 1992 | $253,\!878$  | 1.005   | 255,147     |
| 1993 | $251,\!129$  | 1.006   | $252,\!637$ |
| 1994 | 202,911      | 1.011   | $205,\!150$ |
| 1995 | $174,\!496$  | 1.021   | $178,\!186$ |
| 1996 | 143,042      | 1.072   | $153,\!370$ |
| 1997 | $125,\!429$  | 1.244   | 156,003     |

<sup>&</sup>lt;sup>1</sup>See Exhibit IV, Sheet 2 <sup>2</sup>See Exhibit IV, Sheet 3

Exhibit IV, Sheet 2: Incurred Triangle

|      | 1           | 2           | 3           | 4           | 5           | 6           | 7       | 8           | 9       | 10      |
|------|-------------|-------------|-------------|-------------|-------------|-------------|---------|-------------|---------|---------|
| 1988 | 91,892      | 120,466     | 129,785     | 134,401     | 134,051     | 134,264     | 134,169 | 133,158     | 133,800 | 133,513 |
| 1989 | $117,\!540$ | 160,490     | 163,802     | $162,\!824$ | 164,650     | $163,\!326$ | 161,246 | 161,836     | 161,673 |         |
| 1990 | $155,\!671$ | 210,607     | $208,\!274$ | 211,660     | 209,823     | 208,629     | 208,662 | $210,\!204$ |         |         |
| 1991 | 189,021     | $251,\!182$ | $253,\!292$ | 247,771     | $244,\!882$ | $245,\!666$ | 244,669 |             |         |         |
| 1992 | $229,\!435$ | 289,785     | $268,\!235$ | $255,\!528$ | $252,\!878$ | $253,\!878$ |         |             |         |         |
| 1993 | 251,804     | 259,975     | $245,\!594$ | $251,\!196$ | 251,129     |             |         |             |         |         |
| 1994 | $212,\!555$ | $212,\!160$ | 206,811     | 202,911     |             |             |         |             |         |         |
| 1995 | $178,\!437$ | 181,175     | 174,496     |             |             |             |         |             |         |         |
| 1996 | 151,415     | 143,042     |             |             |             |             |         |             |         |         |
| 1997 | $125,\!429$ |             |             |             |             |             |         |             |         |         |

Exhibit IV, Sheet 3: Incurred Development Factor Triangle

|          | 1-2    | 2-3    | 3-4    | 4-5    | 5-6    | 6-7    | 7-8    | 8-9    | 9-10   | 10-Ult. |
|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|
| 1988     | 1.3110 | 1.0774 | 1.0356 | 0.9974 | 1.0016 | 0.9993 | 0.9925 | 1.0048 | 0.9979 |         |
| 1989     | 1.3654 | 1.0206 | 0.9940 | 1.0112 | 0.9920 | 0.9873 | 1.0037 | 0.9990 |        |         |
| 1990     | 1.3529 | 0.9889 | 1.0163 | 0.9913 | 0.9943 | 1.0002 | 1.0074 |        |        |         |
| 1991     | 1.3289 | 1.0084 | 0.9782 | 0.9883 | 1.0032 | 0.9959 |        |        |        |         |
| 1992     | 1.2630 | 0.9256 | 0.9526 | 0.9896 | 1.0040 |        |        |        |        |         |
| 1993     | 1.0324 | 0.9447 | 1.0228 | 0.9997 |        |        |        |        |        |         |
| 1994     | 0.9981 | 0.9748 | 0.9811 |        |        |        |        |        |        |         |
| 1995     | 1.0153 | 0.9631 |        |        |        |        |        |        |        |         |
| 1996     | 0.9447 |        |        |        |        |        |        |        |        |         |
| Simple   | 1.1791 | 0.9879 | 0.9972 | 0.9963 | 0.9990 | 0.9957 | 1.0012 | 1.0019 | 0.9979 |         |
| Weighted | 1.1592 | 0.9789 | 0.9936 | 0.9953 | 0.9995 | 0.9958 | 1.0022 | 1.0016 | 0.9979 |         |
| Selected | 1.1600 | 1.0500 | 1.0100 | 1.0050 | 1.0010 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0050  |