Simple Reserve Report Example

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Abstract

This document demonstrates how a very simple actuarial reserve report could be created using R. This document is only for display purposes. It was created using insurance loss data freely available on the CAS website. This report could be greatly improved by having better documentation for the relationships among tables. I am just getting started with LATEX and will have more clearly documented reports in subsequent examples.

Purpose

Ractuary was requested by Nsure Ance Company (NAC) to provide a reserve estimate for their workers' compensation loss and alocated loss adjustment expense (ALAE) reserves. Losses are evaluated as of December 31, 1997...

Background

NAC began offering workers' compensation coverage in 1988. Each policy is written on a calendar year basis (i.e. beginning January 1 and ending December 31). NAC has never purchased reinsurense coverage...

Other Stuff

Blah blah...

Conclusions

A summary of our reserve analysis is as follows:

Exhibit I: Reserve Summary

	$Paid^1$	$Incurred^2$	$Ultimate^3$	Case OS	IBNR	Total OS
1988	125,049	133,513	138,993	8,464	5,480	13,944
1989	$147,\!358$	$161,\!673$	167,073	$14,\!315$	5,400	19,715
1990	187,760	210,204	216,633	22,444	$6,\!429$	28,873
1991	$213,\!396$	244,669	$252,\!263$	$31,\!273$	$7,\!594$	$38,\!867$
1992	213,904	$253,\!878$	261,087	39,974	7,209	$47,\!183$
1993	$193,\!676$	251,129	$253,\!250$	$57,\!453$	2,121	$59,\!574$
1994	151,081	202,911	209,512	51,830	6,601	58,431
1995	111,268	174,496	$211,\!166$	63,228	36,670	99,898
1996	66,033	143,042	$174,\!486$	77,009	$31,\!444$	$108,\!453$
1997	$25,\!265$	$125,\!429$	179,035	100,164	$53,\!606$	153,770
Totals	1,434,790	1,900,944	2,063,498	466,154	162,554	628,708

From the table above, estimated ultimate loss & ALAE as of December 31, 1997 is 2,063,498 indicating a total outstanding loss & ALAE of 628,708.2.

Methodology

We used two actuarial projection techniques (paid projection and incurred projection) in creating the final estimated ultimate loss projection. The loss projections use loss experience for the more mature accident years to estimate the development of less mature accident years. See the following exhibits for detail regarding the projections and estimated ultimate loss and ALAE selection.

¹See Exhibit III, Sheet 1

²See Exhibit IV, Sheet 1 ³See Exhibit II

Exhibits

Exhibit II: Selection of Estimated Ultimate Loss and ALAE

	Paid Projection ¹	Incurred Projection ²	Selected Ultimate ³
1988	143,806	134,181	138,993
1989	$171,\!665$	162,481	167,073
1990	222,012	211,255	216,633
1991	258,633	245,892	252,263
1992	267,026	$255{,}147$	261,087
1993	$253,\!863$	252,637	253,250
1994	213,874	205,150	209,512
1995	244,146	178,186	211,166
1996	195,602	153,370	174,486
1997	202,067	156,003	179,035
Totals	2,172,694	1,954,303	2,063,498

 $^{^1\}mathrm{See}$ Exhibit III, Sheet 1 $^2\mathrm{See}$ Exhibit IV, Sheet 1 $^2\mathrm{The}$ average of the paid and incurred projections

Exhibit III, Sheet 1: Paid Projection

	1		
	$Paid^1$	LDF^2	Ultimate
1988	125,049	1.150	143,806
1989	$147,\!358$	1.165	$171,\!665$
1990	187,760	1.182	222,012
1991	$213,\!396$	1.212	$258,\!633$
1992	213,904	1.248	267,026
1993	193,676	1.311	$253,\!863$
1994	151,081	1.416	$213,\!874$
1995	111,268	2.194	$244,\!146$
1996	66,033	2.962	195,602
1997	$25,\!265$	7.998	202,067

¹See Exhibit III, Sheet 2 ²See Exhibit III, Sheet 3

Exhibit III, Sheet 2: Paid Triangle

	1	2	3	4	5	6	7	8	9	10
1988	22,190	60,834	85,104	100,151	108,812	114,967	118,790	121,558	123,492	125,049
1989	$26,\!542$	77,798	$106,\!407$	$122,\!422$	$133,\!359$	$138,\!599$	143,029	145,712	$147,\!358$	
1990	32,977	100,494	134,886	157,758	168,991	178,065	182,787	187,760		
1991	38,604	$114,\!428$	157,103	181,322	197,411	208,804	$213,\!396$			
1992	$42,\!466$	125,820	164,776	189,045	$204,\!377$	213,904				
1993	46,447	116,764	$154,\!897$	179,419	193,676					
1994	$41,\!368$	100,344	132,021	151,081						
1995	35,719	83,216	111,268							
1996	28,746	66,033								
1997	$25,\!265$									

Exhibit III, Sheet 3:Paid Development Factor Triangle

	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-Ult.
1988	2.7415	1.3990	1.1768	1.0865	1.0566	1.0333	1.0233	1.0159	1.0126	
1989	2.9311	1.3677	1.1505	1.0893	1.0393	1.0320	1.0188	1.0113		
1990	3.0474	1.3422	1.1696	1.0712	1.0537	1.0265	1.0272			
1991	2.9641	1.3729	1.1542	1.0887	1.0577	1.0220				
1992	2.9628	1.3096	1.1473	1.0811	1.0466					
1993	2.5139	1.3266	1.1583	1.0795						
1994	2.4256	1.3157	1.1444							
1995	2.3297	1.3371								
1996	2.2971									
Simple	2.6904	1.3464	1.1573	1.0827	1.0508	1.0284	1.0231	1.0136	1.0126	
Weighted	2.6844	1.3421	1.1561	1.0823	1.0509	1.0274	1.0234	1.0134	1.0126	
Selected	2.7000	1.3500	1.5500	1.0800	1.0500	1.0300	1.0250	1.0150	1.0130	1.1500

Incurred Projection

	$Incurred^1$	LDF^2	Ultimate
1988	$133,\!513$	1.005	134,181
1989	$161,\!673$	1.005	$162,\!481$
1990	$210,\!204$	1.005	$211,\!255$
1991	244,669	1.005	245,892
1992	$253,\!878$	1.005	255,147
1993	$251,\!129$	1.006	$252,\!637$
1994	202,911	1.011	$205,\!150$
1995	$174,\!496$	1.021	$178,\!186$
1996	143,042	1.072	$153,\!370$
1997	$125,\!429$	1.244	156,003

¹See Exhibit IV, Sheet 2 ²See Exhibit IV, Sheet 3

Exhibit IV, Sheet 2: Incurred Triangle

	1	2	3	4	5	6	7	8	9	10
1988	91,892	120,466	129,785	134,401	134,051	134,264	134,169	133,158	133,800	133,513
1989	$117,\!540$	160,490	163,802	$162,\!824$	164,650	$163,\!326$	161,246	161,836	161,673	
1990	$155,\!671$	210,607	$208,\!274$	211,660	209,823	208,629	208,662	210,204		
1991	189,021	$251,\!182$	$253,\!292$	247,771	$244,\!882$	$245,\!666$	244,669			
1992	$229,\!435$	289,785	$268,\!235$	$255,\!528$	$252,\!878$	$253,\!878$				
1993	251,804	259,975	$245,\!594$	$251,\!196$	251,129					
1994	$212,\!555$	$212,\!160$	206,811	202,911						
1995	$178,\!437$	181,175	174,496							
1996	151,415	143,042								
1997	$125,\!429$									

Exhibit IV, Sheet 3: Incurred Development Factor Triangle

	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-Ult.
1988	1.3110	1.0774	1.0356	0.9974	1.0016	0.9993	0.9925	1.0048	0.9979	
1989	1.3654	1.0206	0.9940	1.0112	0.9920	0.9873	1.0037	0.9990		
1990	1.3529	0.9889	1.0163	0.9913	0.9943	1.0002	1.0074			
1991	1.3289	1.0084	0.9782	0.9883	1.0032	0.9959				
1992	1.2630	0.9256	0.9526	0.9896	1.0040					
1993	1.0324	0.9447	1.0228	0.9997						
1994	0.9981	0.9748	0.9811							
1995	1.0153	0.9631								
1996	0.9447									
Simple	1.1791	0.9879	0.9972	0.9963	0.9990	0.9957	1.0012	1.0019	0.9979	
Weighted	1.1592	0.9789	0.9936	0.9953	0.9995	0.9958	1.0022	1.0016	0.9979	
Selected	1.1600	1.0500	1.0100	1.0050	1.0010	1.0000	1.0000	1.0000	1.0000	1.0050