



# An Introduction to Deep Learning on Meshes

## SIGGRAPH COURSE 2021

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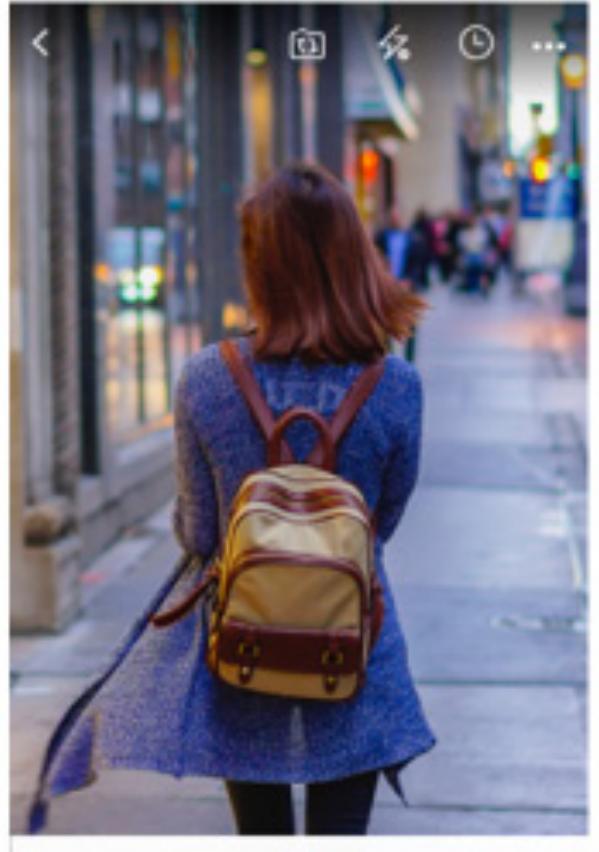
THE UNIVERSITY OF  
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# Real world success of deep learning

Reverse image search



Alibaba Pailitao

Facial recognition



Facebook Photo Tags

Speech recognition /  
Language processing



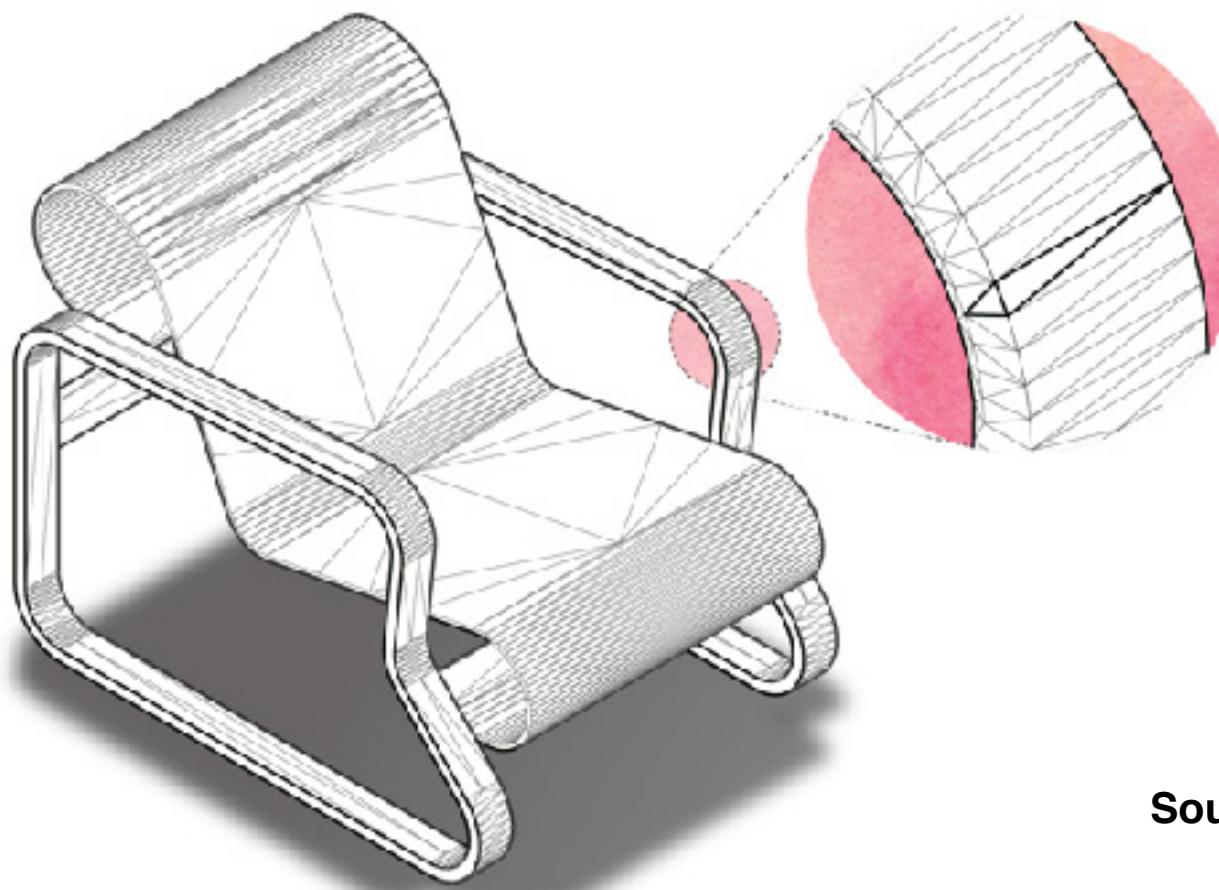
Apple Siri

machine translation

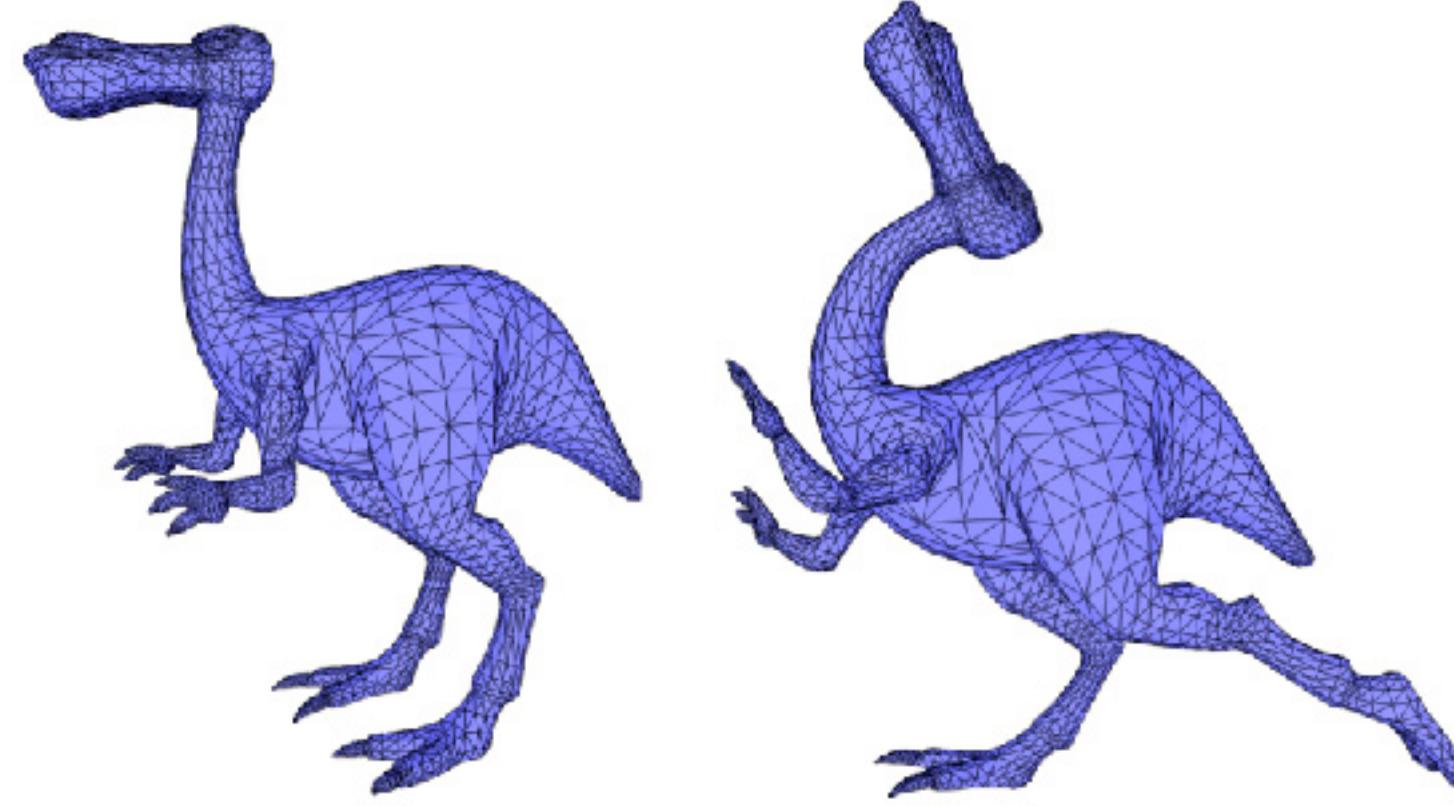


Google translate

# Meshes are popular in computer graphics



Source: Sorkine & Alexa 2007



Source: Sawhney & Crane  
2017



Source: Li et. al 2020



fast to render

adaptive

efficient to texture

intuitively deformable

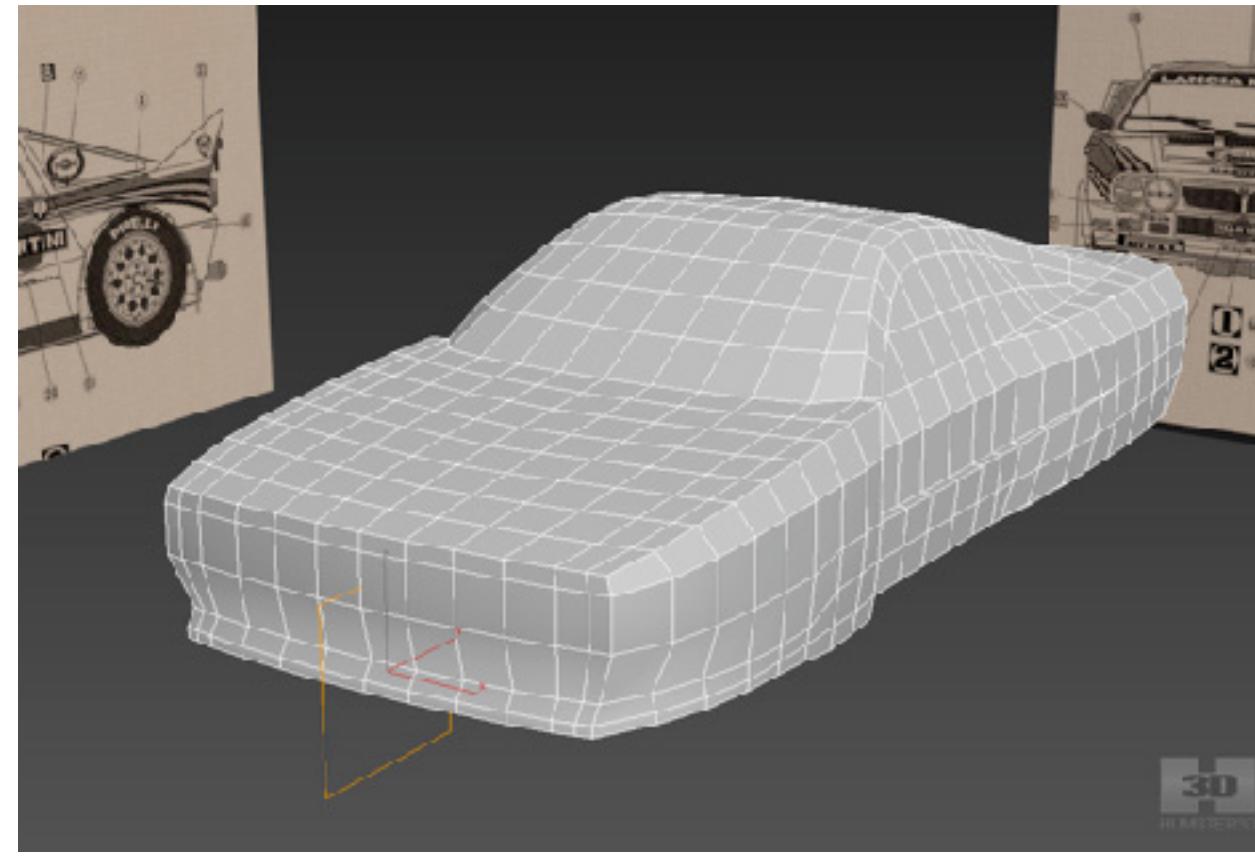
physics simulation

# Combining the power of deep learning & meshes

## for many applications in geometry processing



**Modeling**



**Editing**



**Reconstruction**



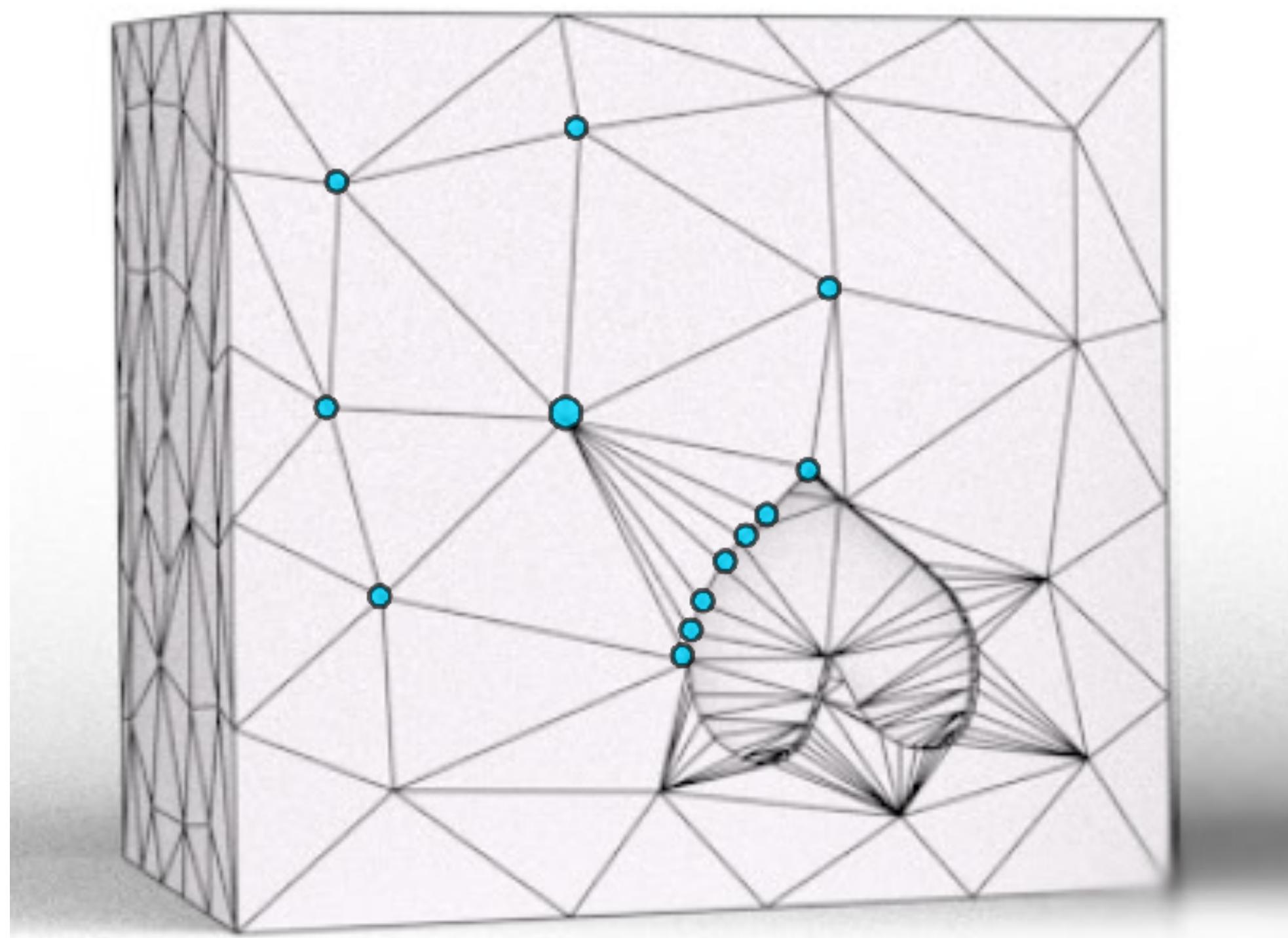
**Shape Analysis**

# **Challenges for deep learning on meshes**

**Representation**

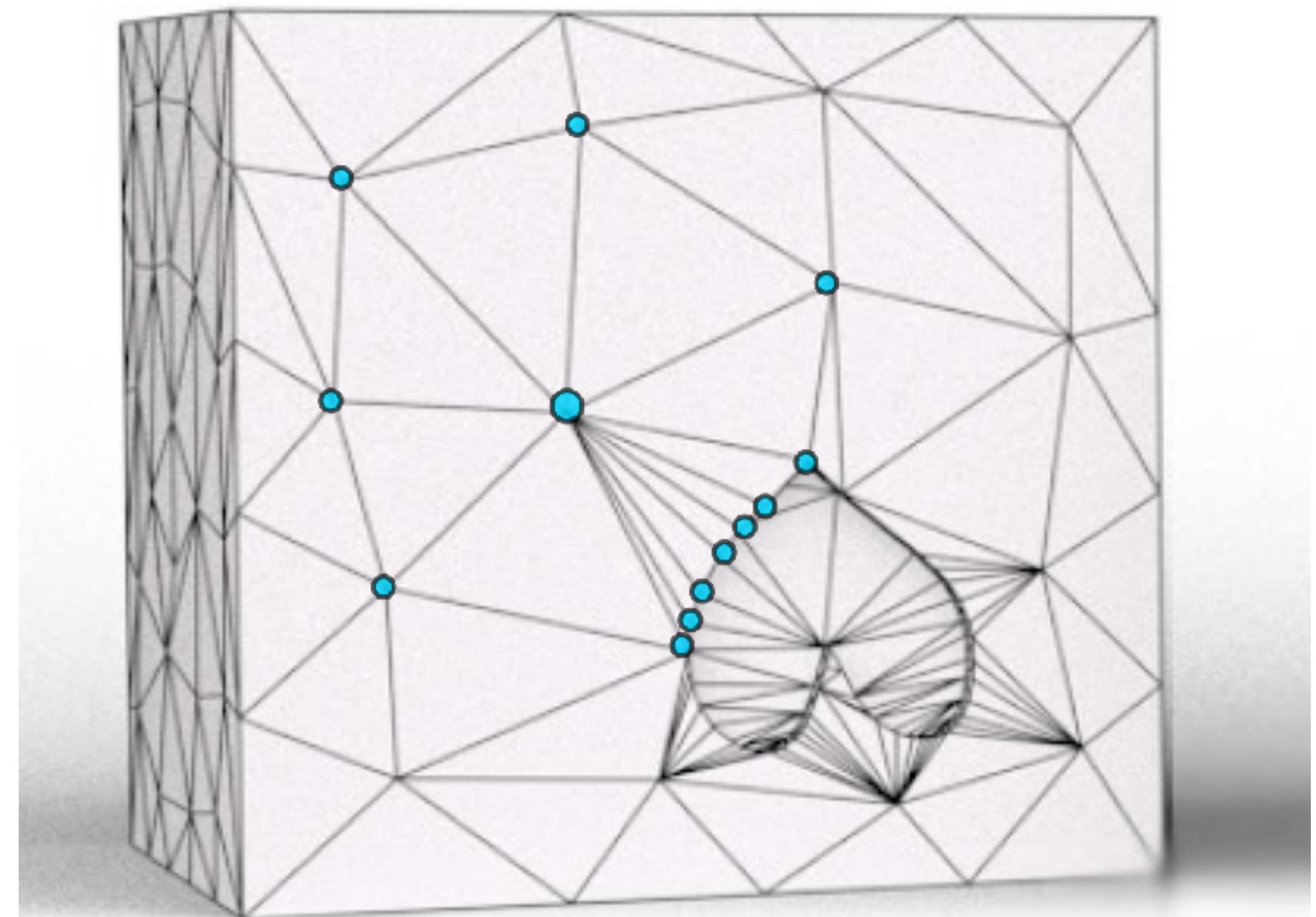
**Data Accessibility**

# Irregular

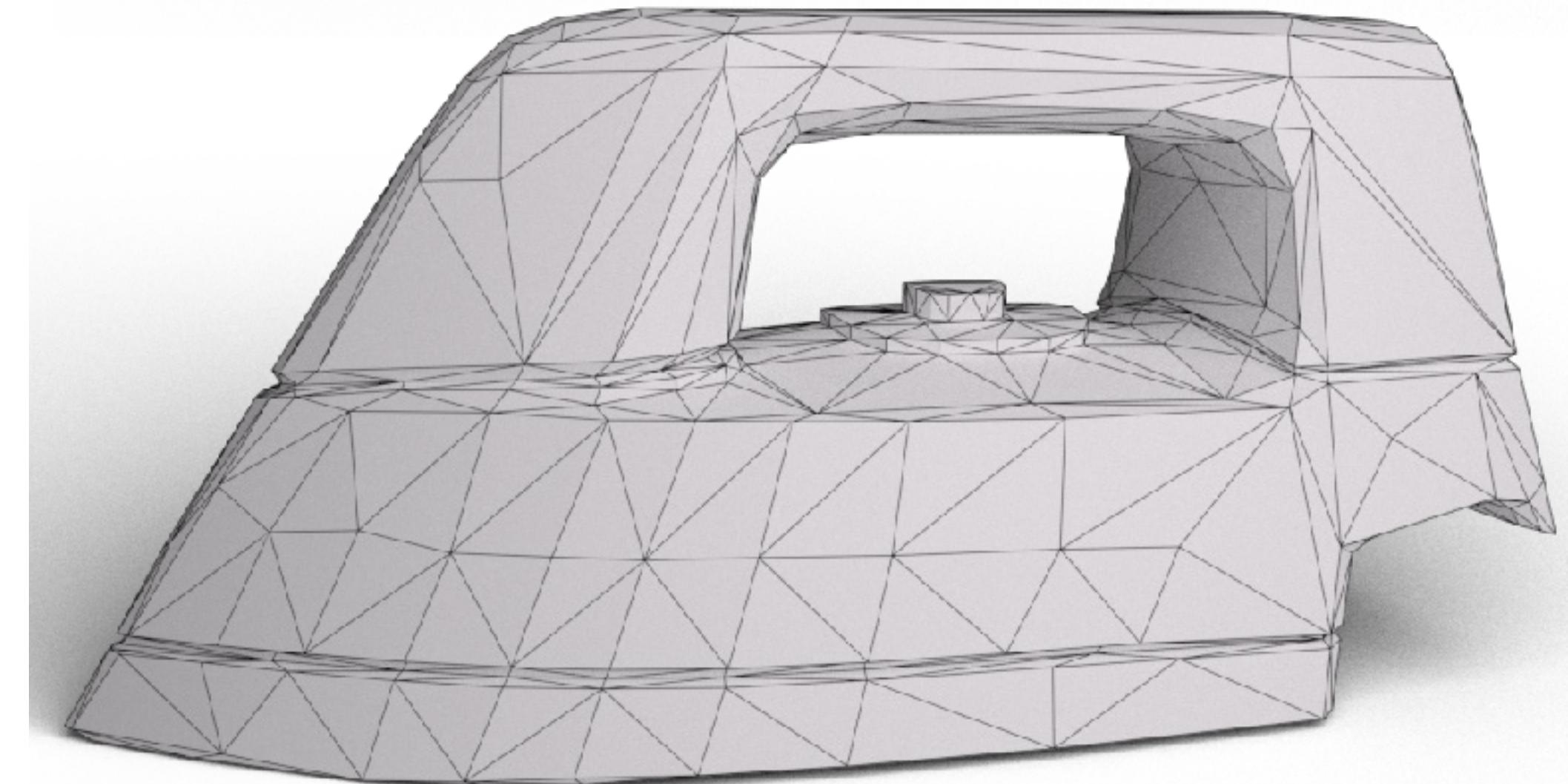
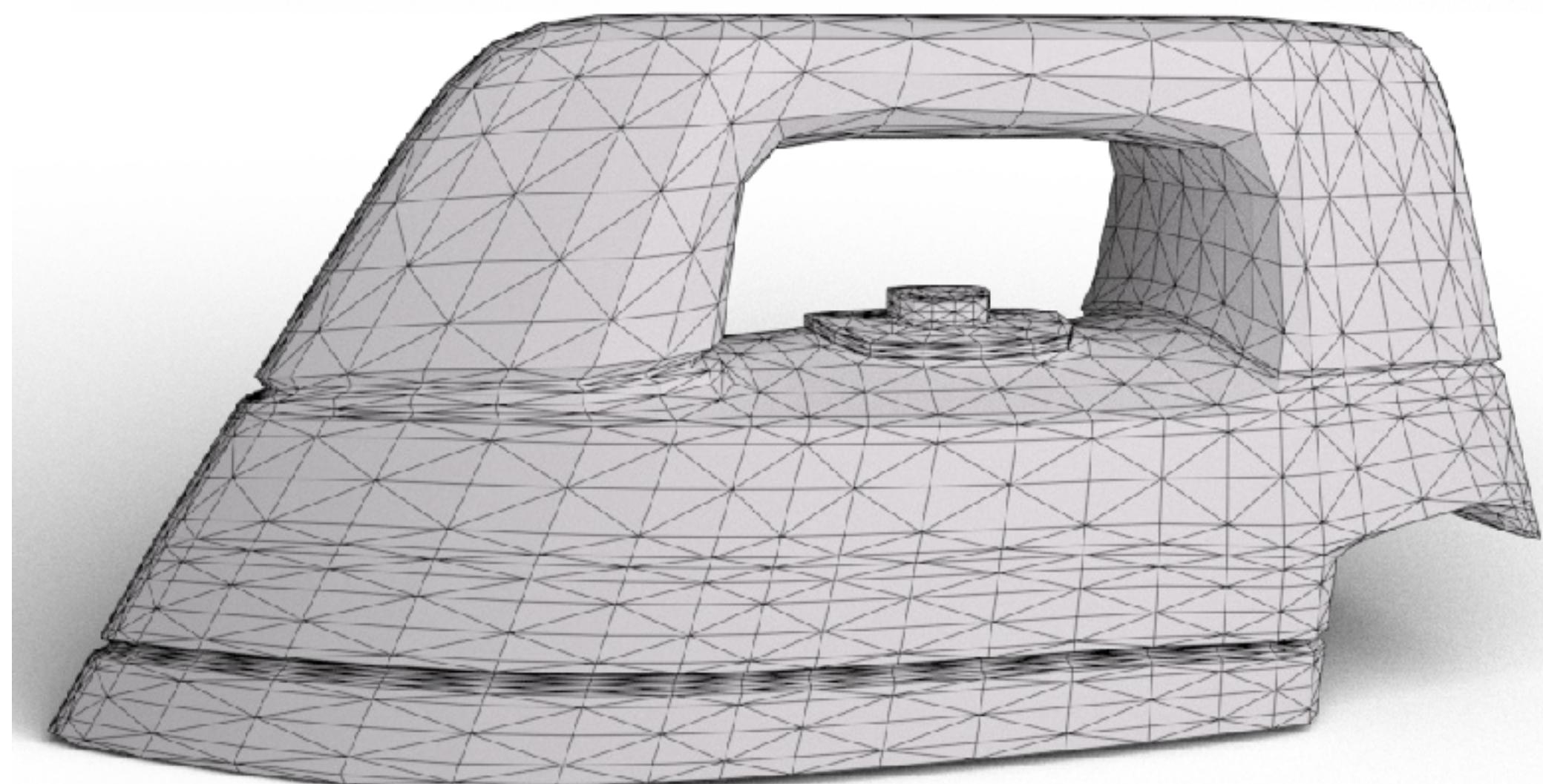
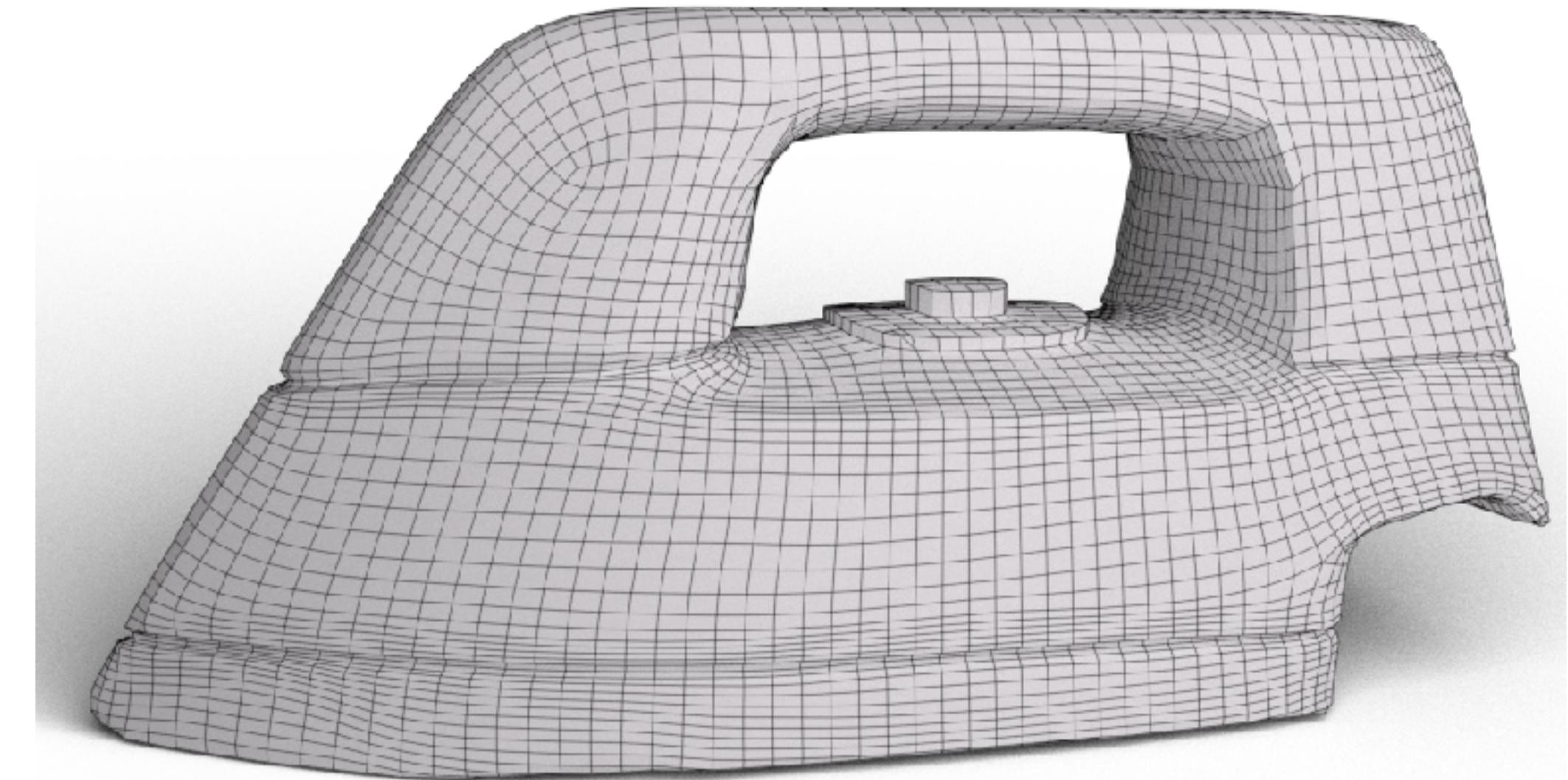


# Unordered

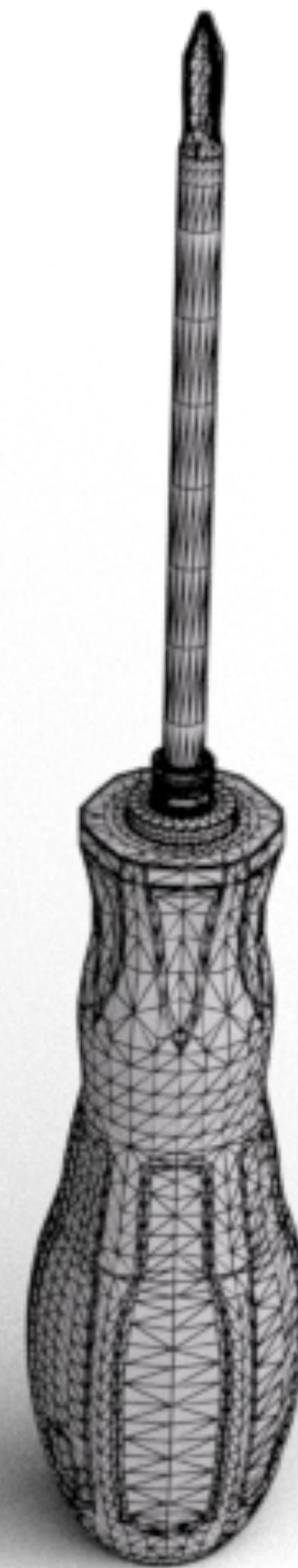
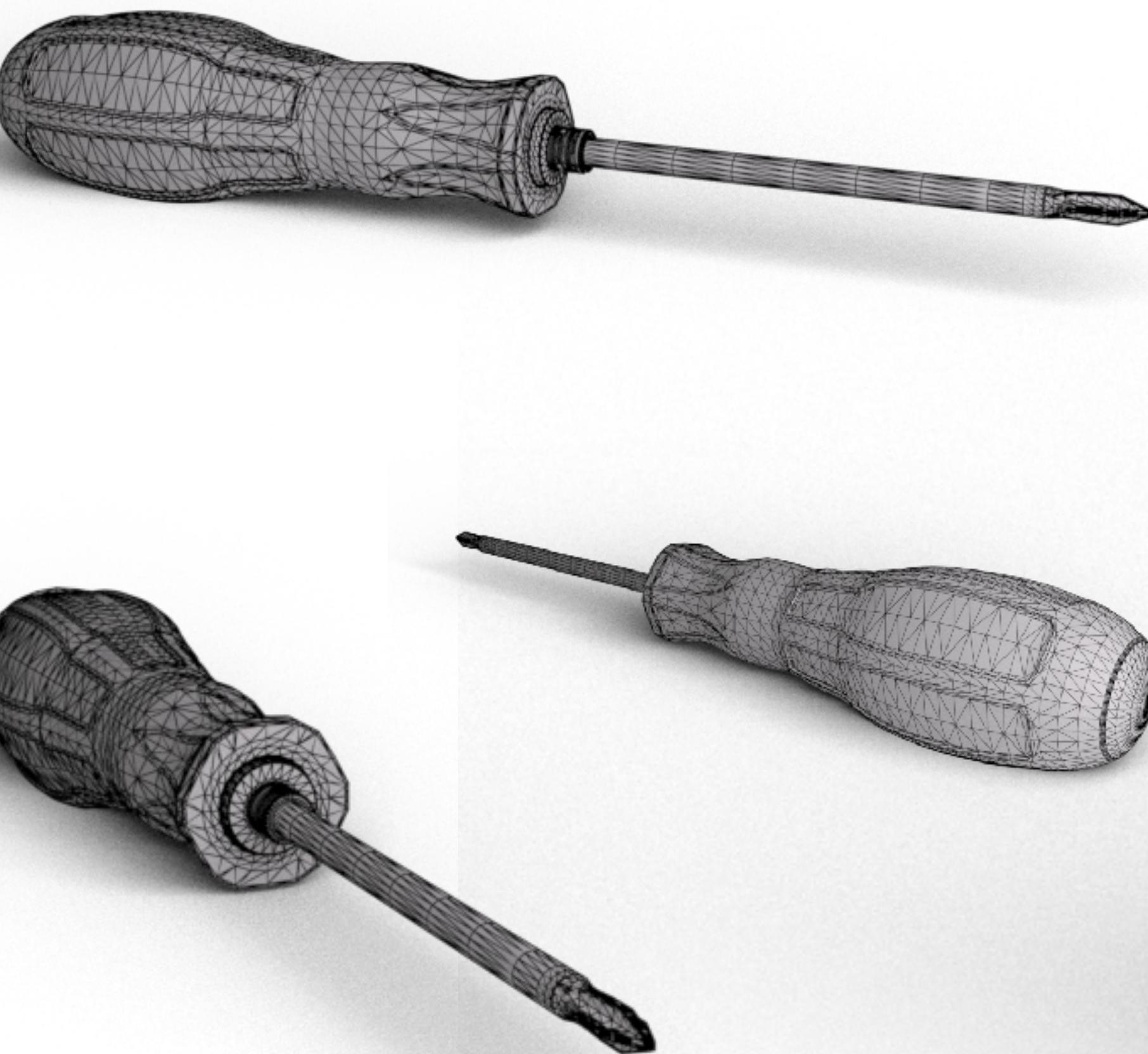
<b>&lt;x, y, z&gt;</b>
<b>&lt;1.2, 3.1, -0.7&gt;</b>
<b>&lt;1.2, 3.4, -0.8&gt;</b>
<b>&lt;1.5, 3.4, -0.6&gt;</b>
<b>&lt;1.5, 3.1, -0.7&gt;</b>
<b>&lt;1.5, 3.7, -0.7&gt;</b>
<b>&lt;1.7, 3.4, -0.7&gt;</b>



# Inconsistent



# Unoriented

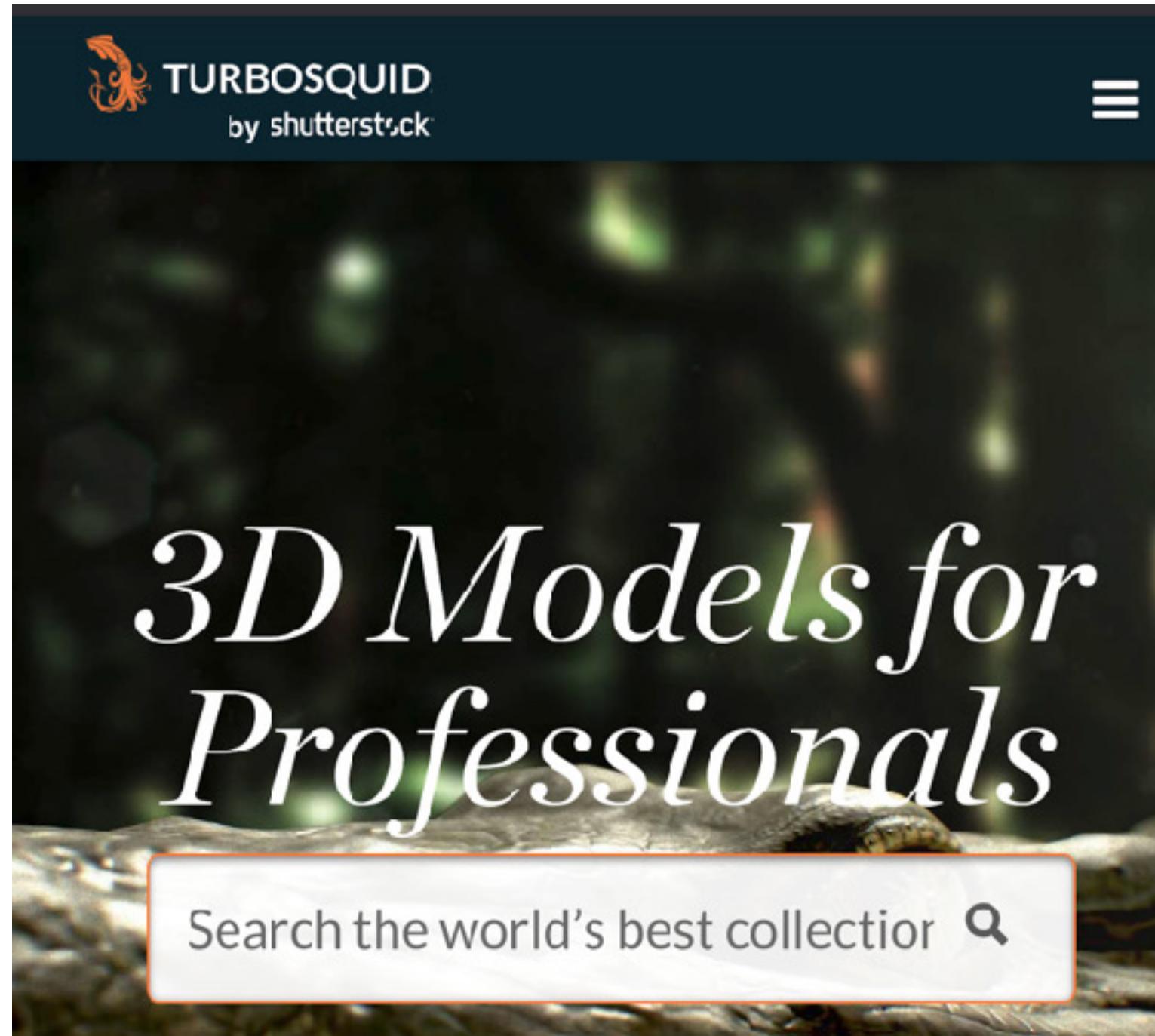


# **Challenges for deep learning on meshes**

**Representation**

**Data Accessibility**

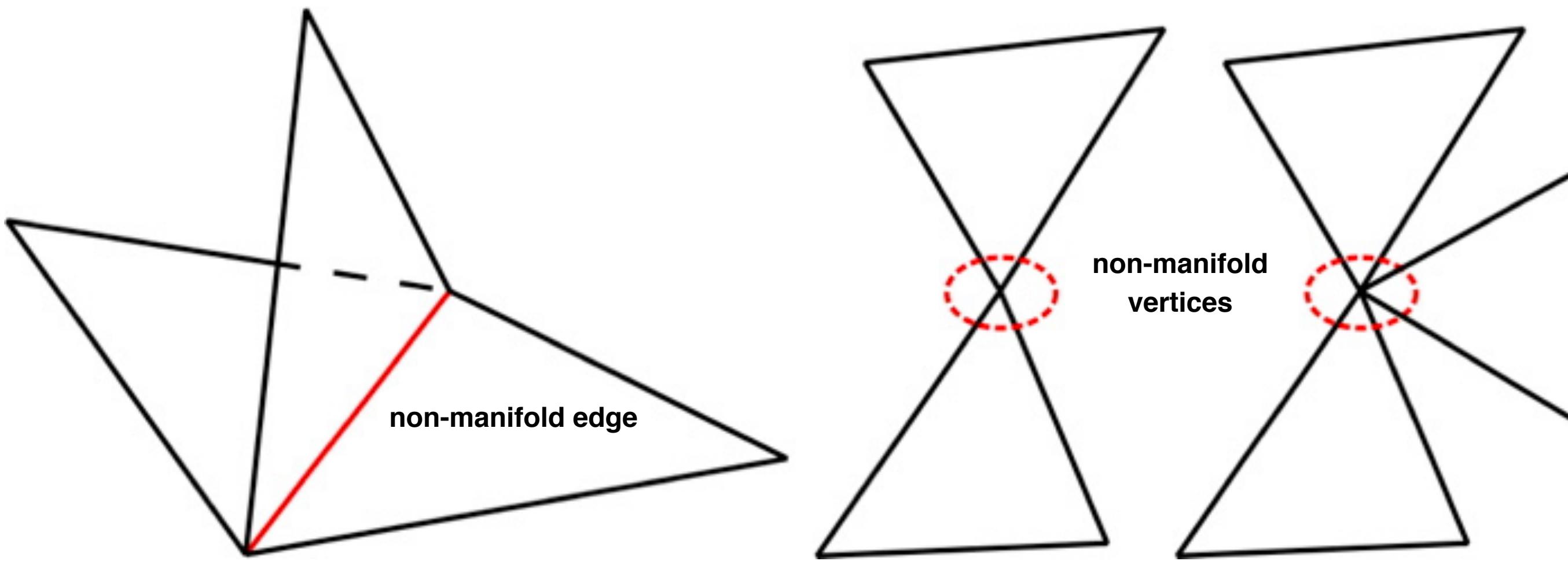
# Large Warehouses of 3D Mesh Data



The image displays a grid of 3D model thumbnails from a warehouse website. It is organized into three main sections: CARS, VEHICLES, and FURNITURE. Each section has a title and a row of five models with navigation arrows on either side.

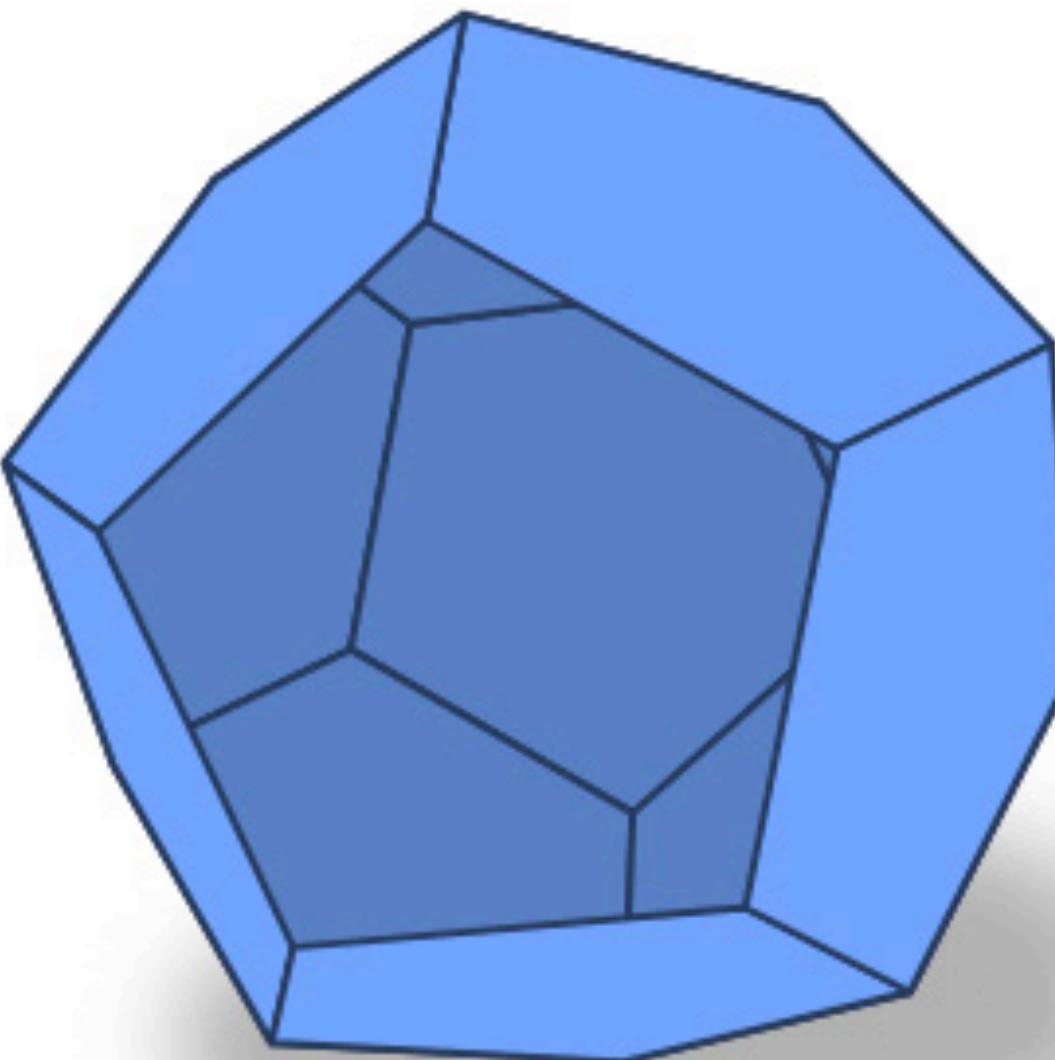
- CARS:** Includes SPORTS CAR, SEDAN, PICK-UP TRUCK, COUPE, SUV, and HATCHBACK.
- VEHICLES:** Includes MOTORCYCLE, AIRPLANE, HELICOPTER, BICYCLE, TANK, and TRAINS.
- FURNITURE:** Includes CHAIR, TABLE, DESK, SOFA, SINK, and OFFICE CHAIR.

# High bar for geometric computation

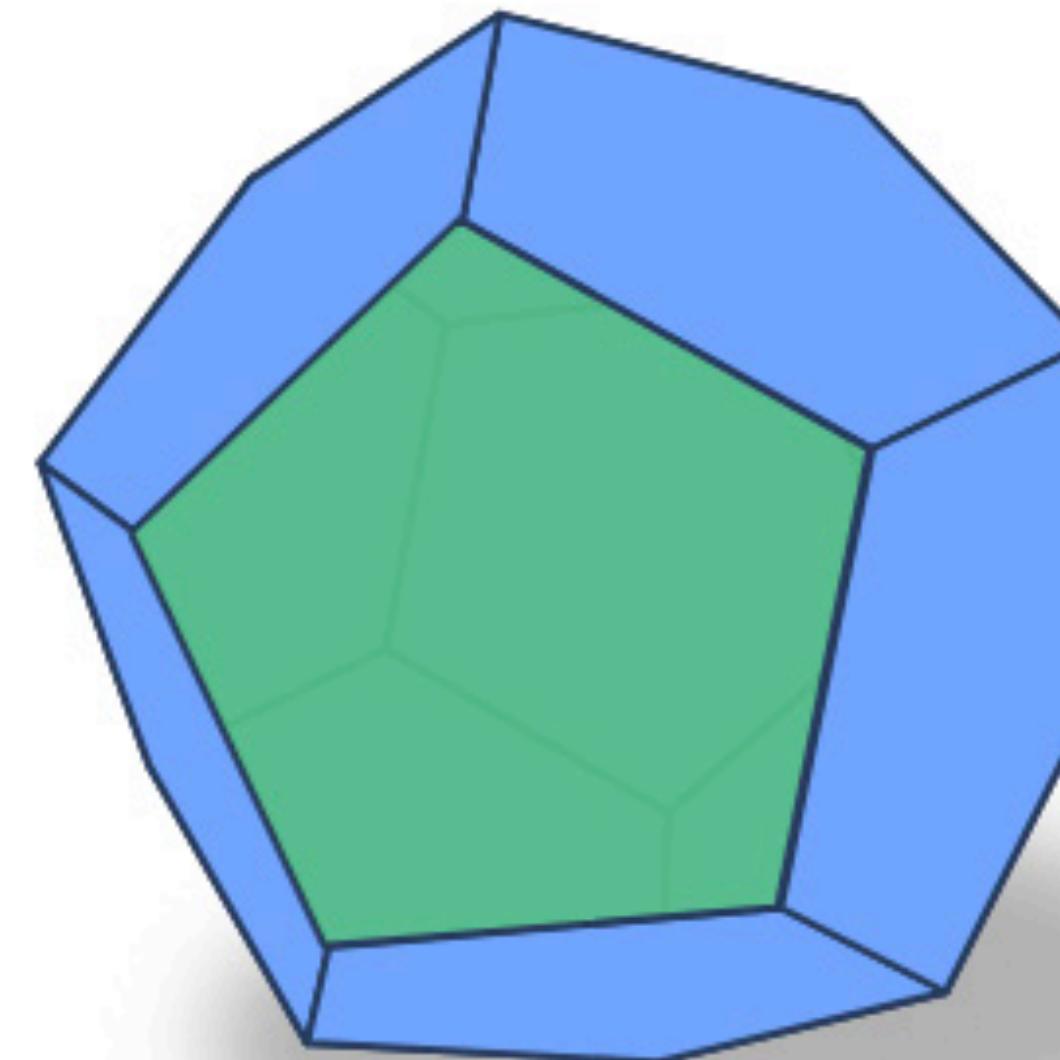


**non-manifold**

# High bar for geometric computation



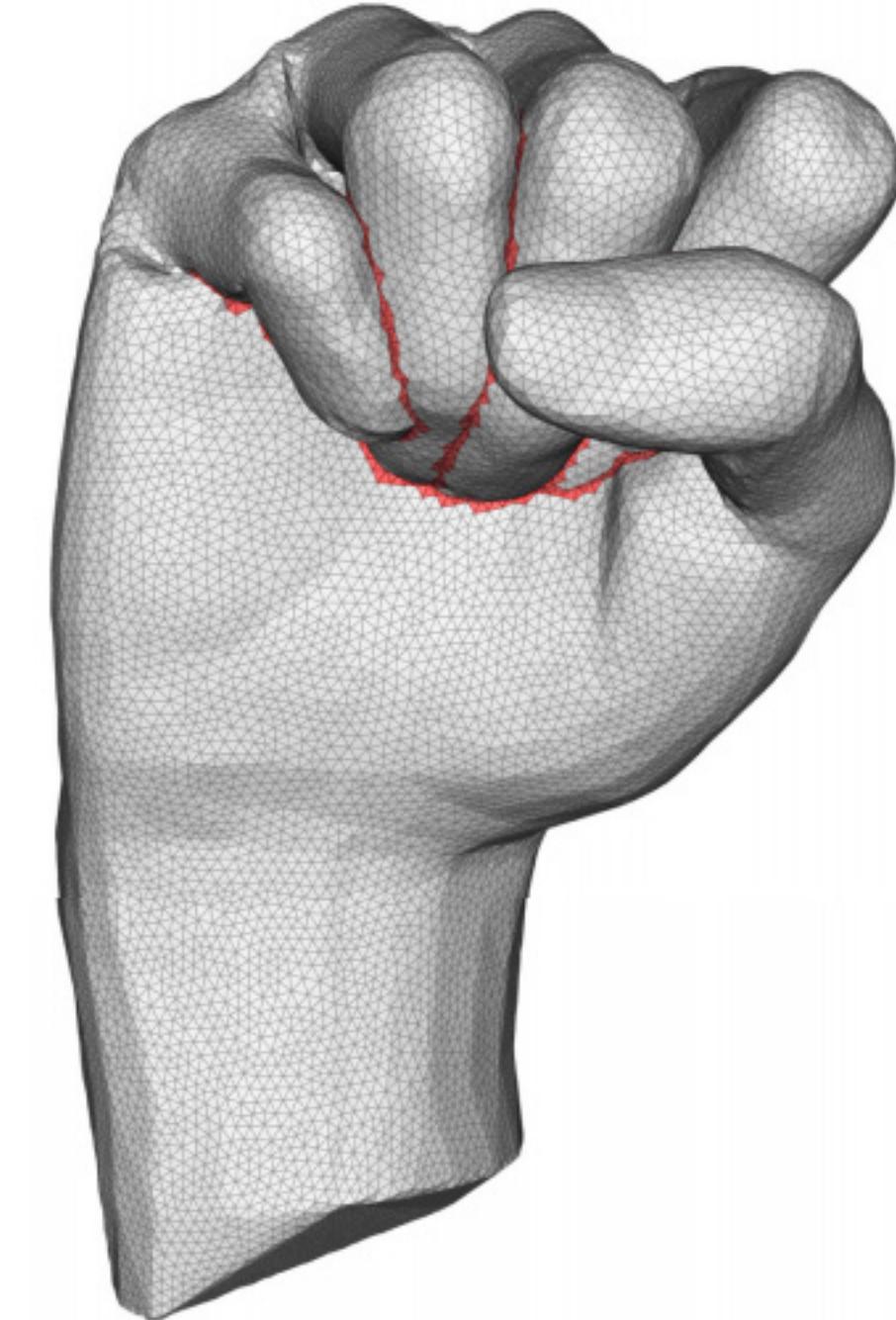
**non-manifold**



**not watertight**

Source: geometry central

# High bar for geometric computation



Source: Sacht et. al 2013

**non-manifold**

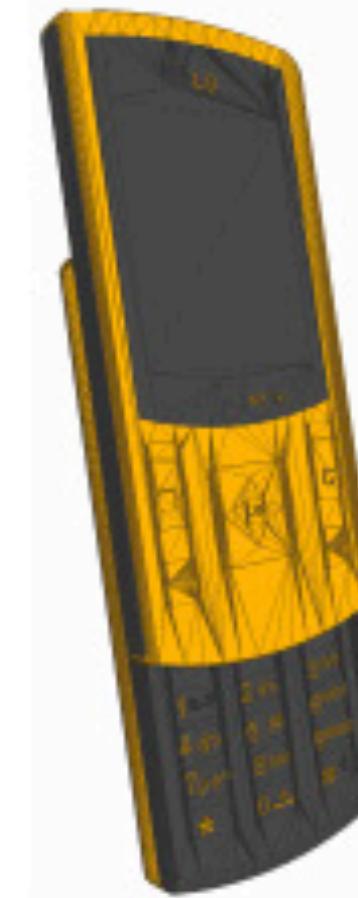
**not watertight**

**intersections**

# High bar for geometric computation



non-manifold



not watertight



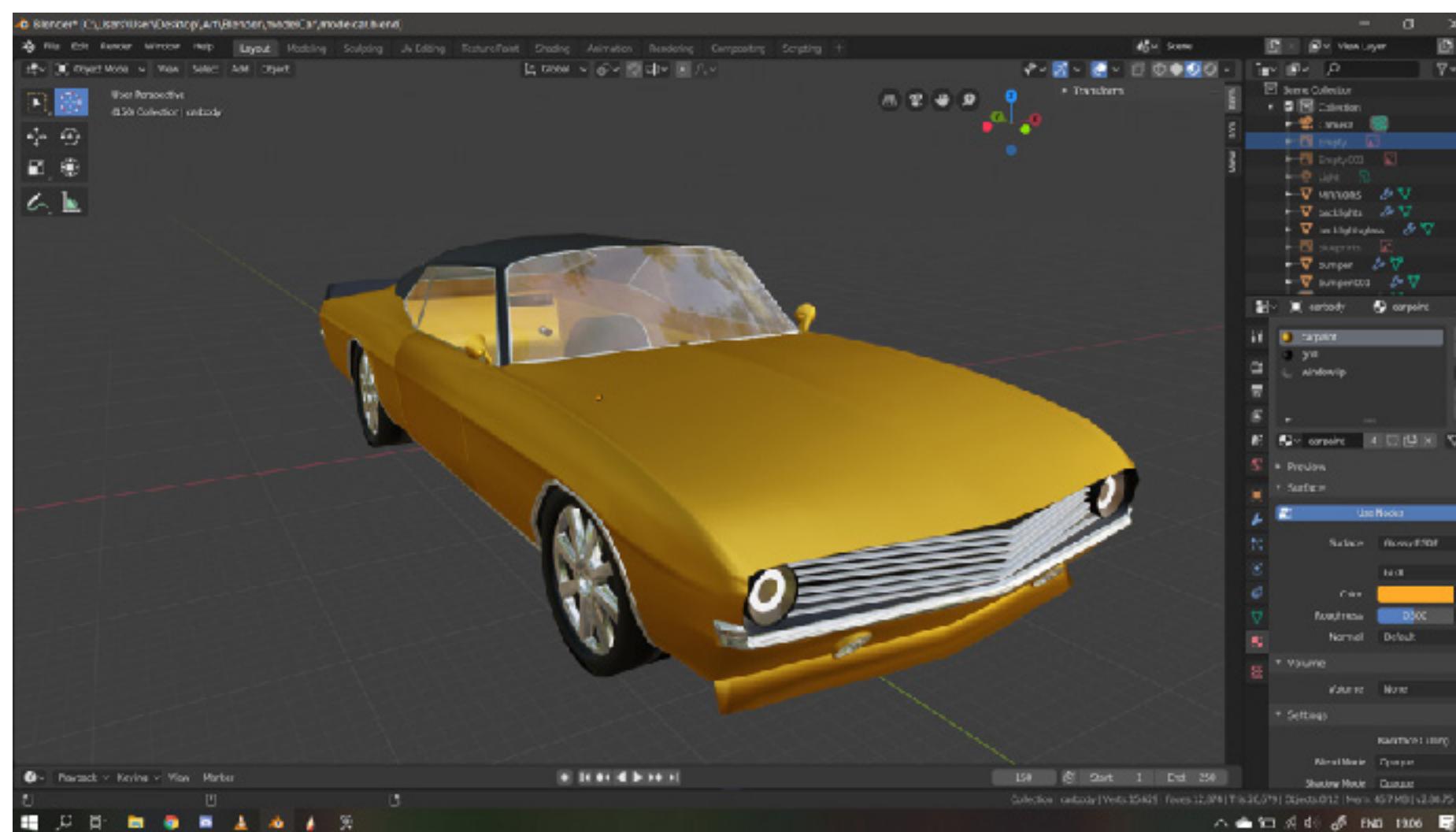
intersections



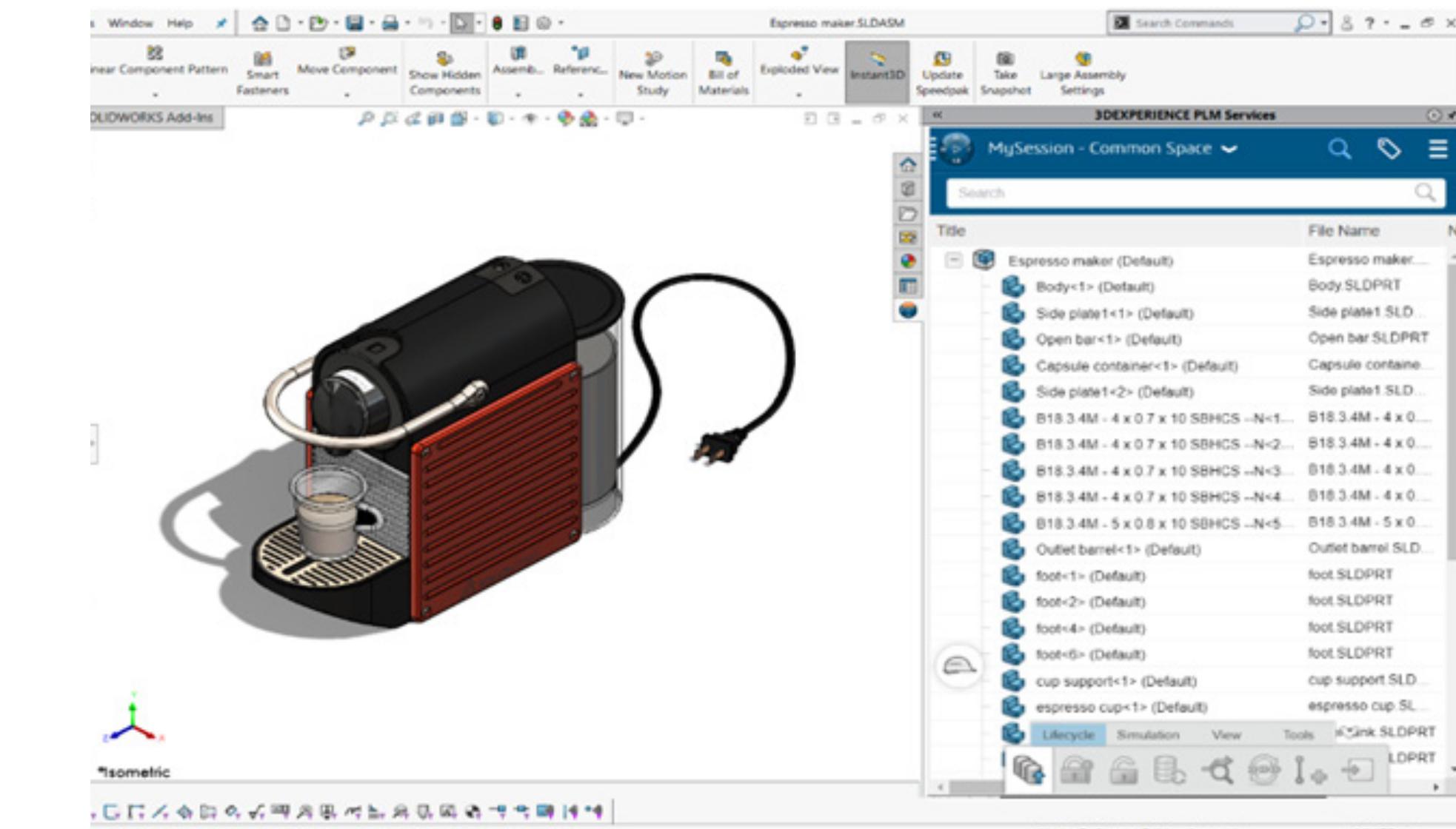
face orientation

Source: Takayama et. al 2014

# Hard to Create 3D Data

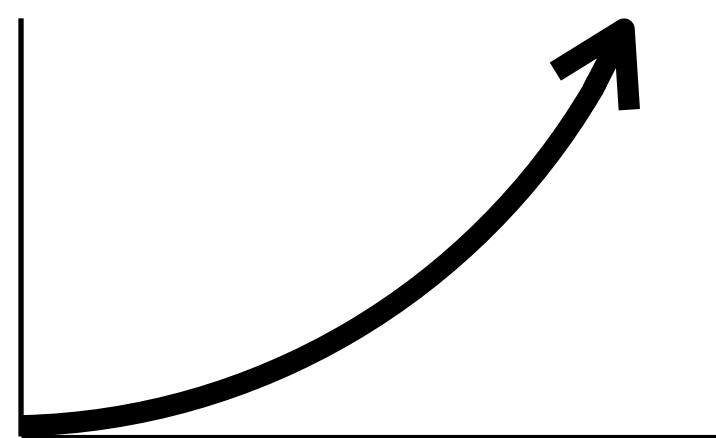
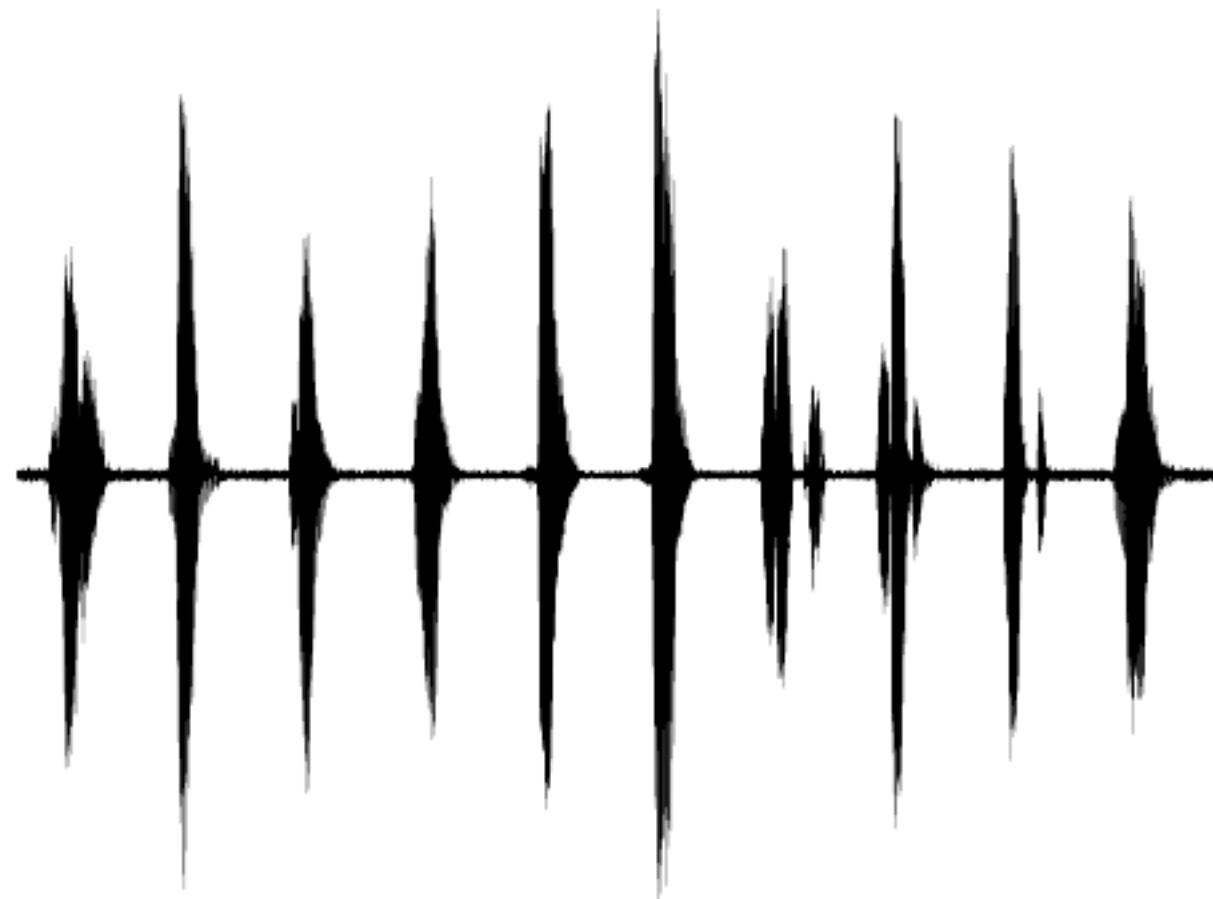


Blender

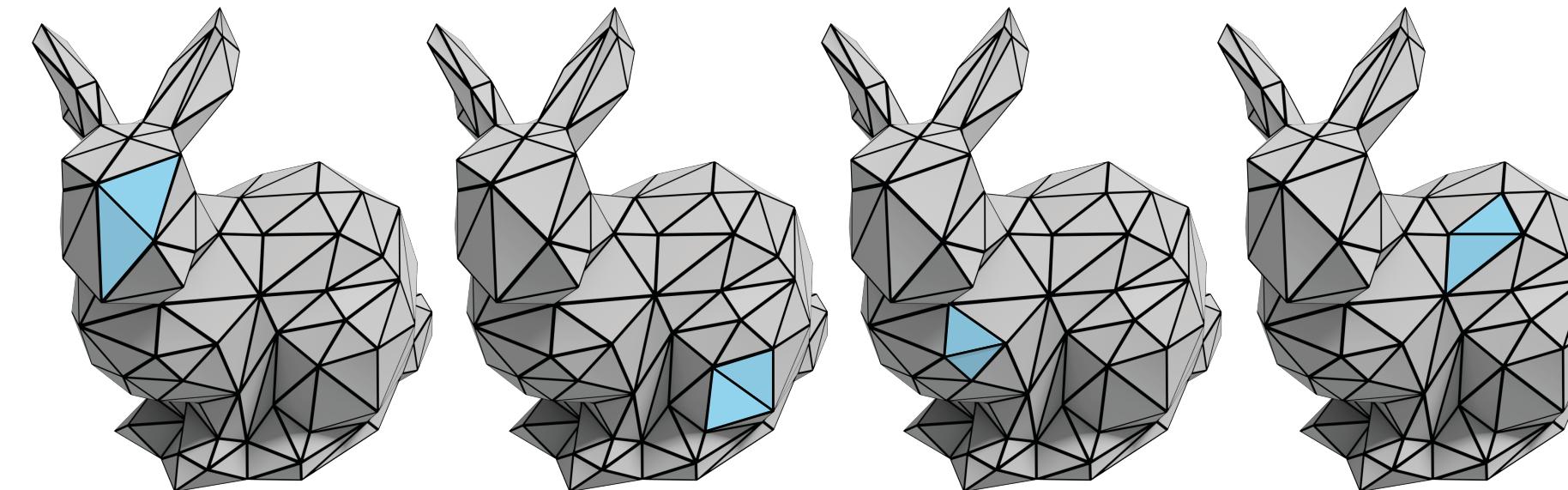


SolidWorks

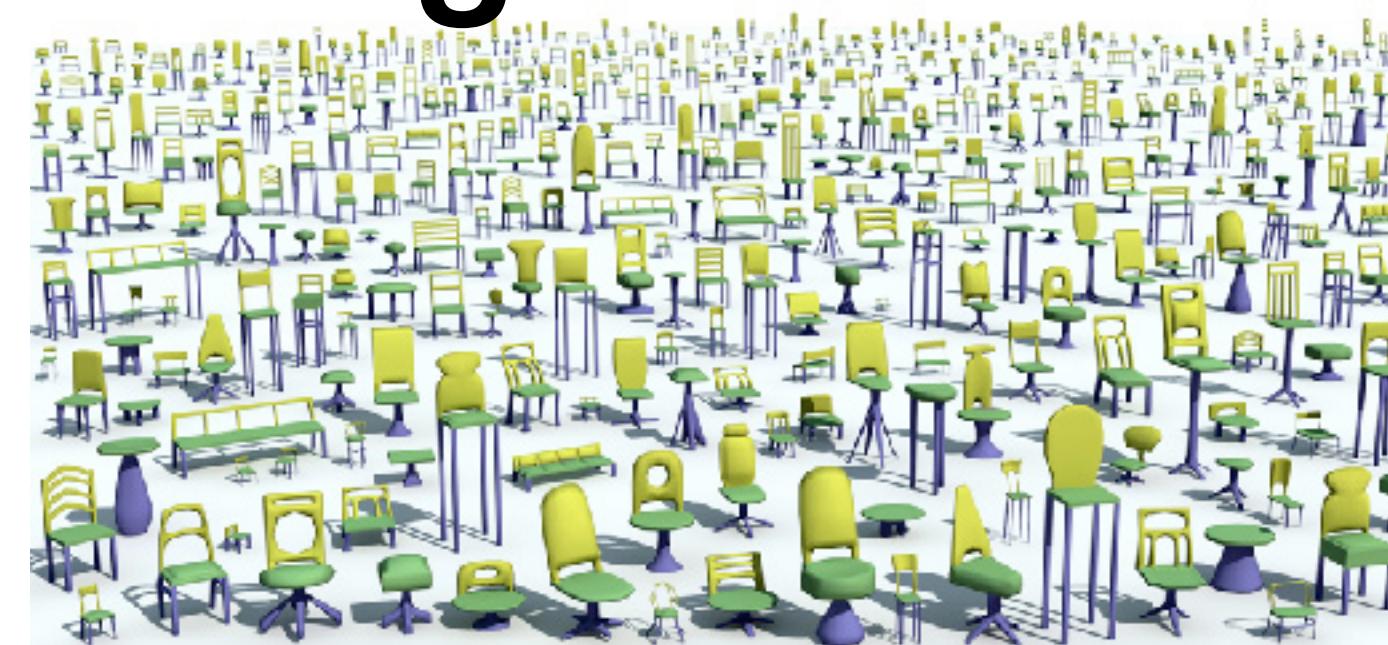
# Curse of dimensionality



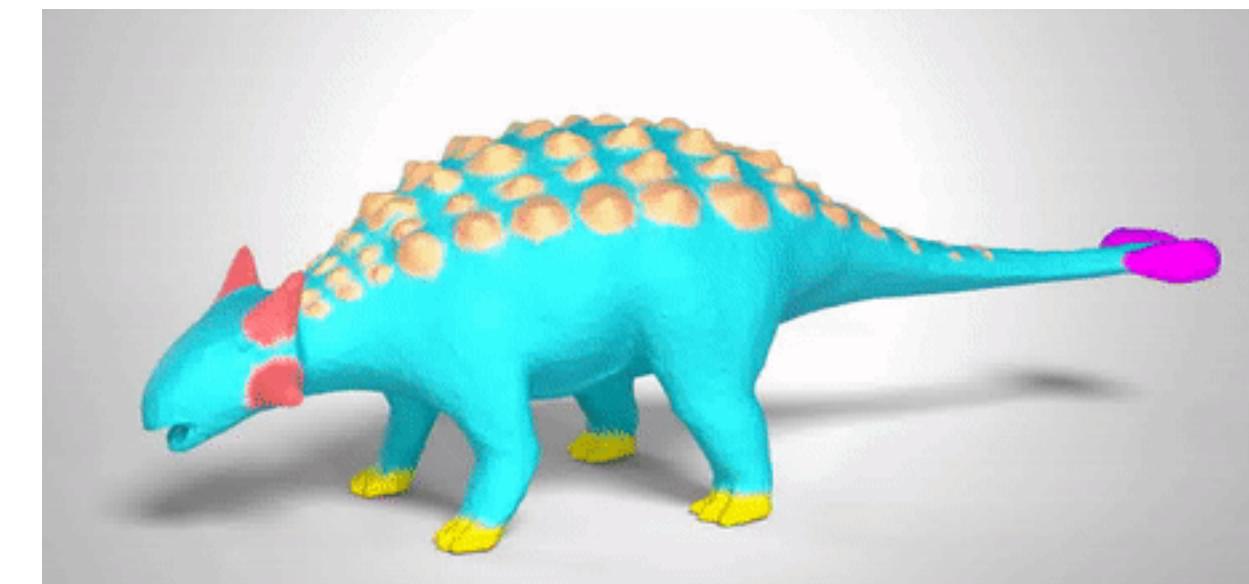
# Mesh Convolutional Neural Networks



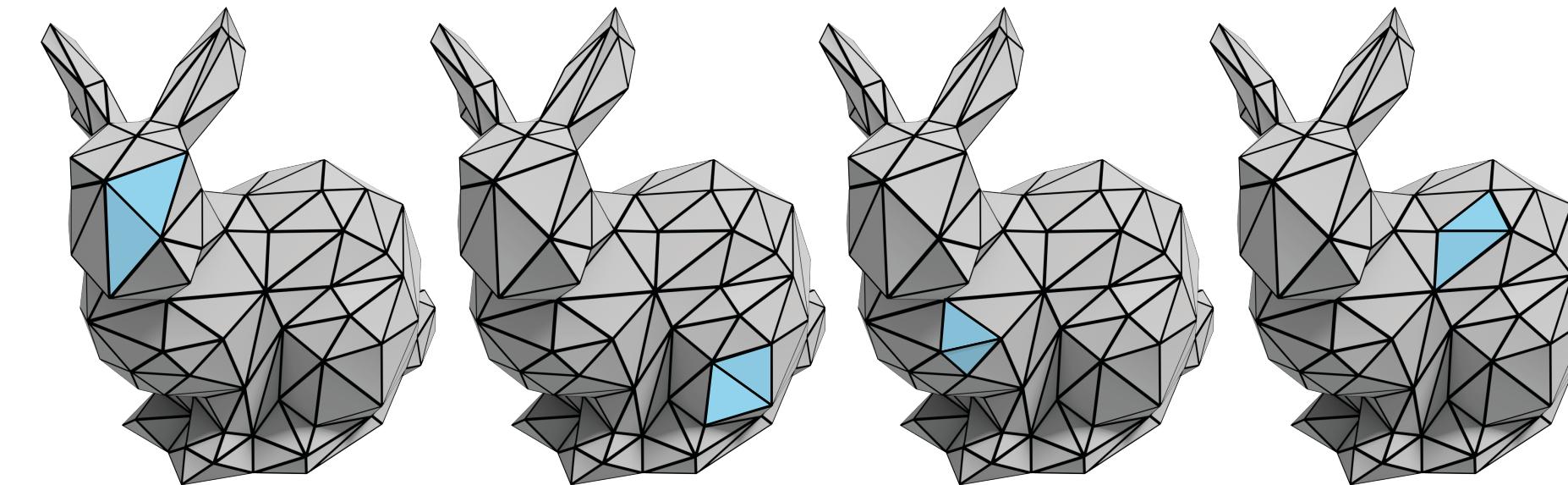
# Machine Learning & Geometry Processing



# Learning from a Single Mesh



# Mesh Convolutional Neural Networks



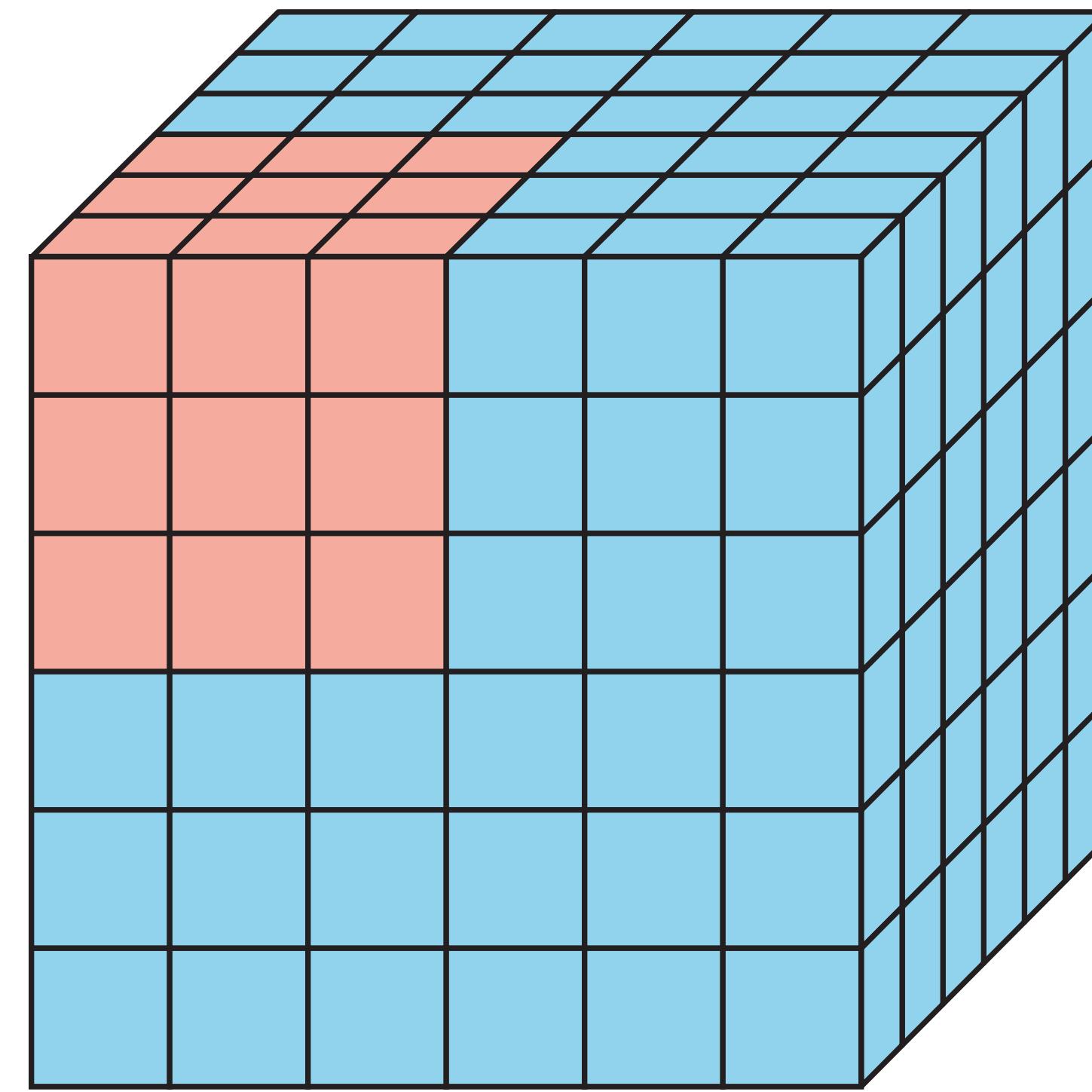
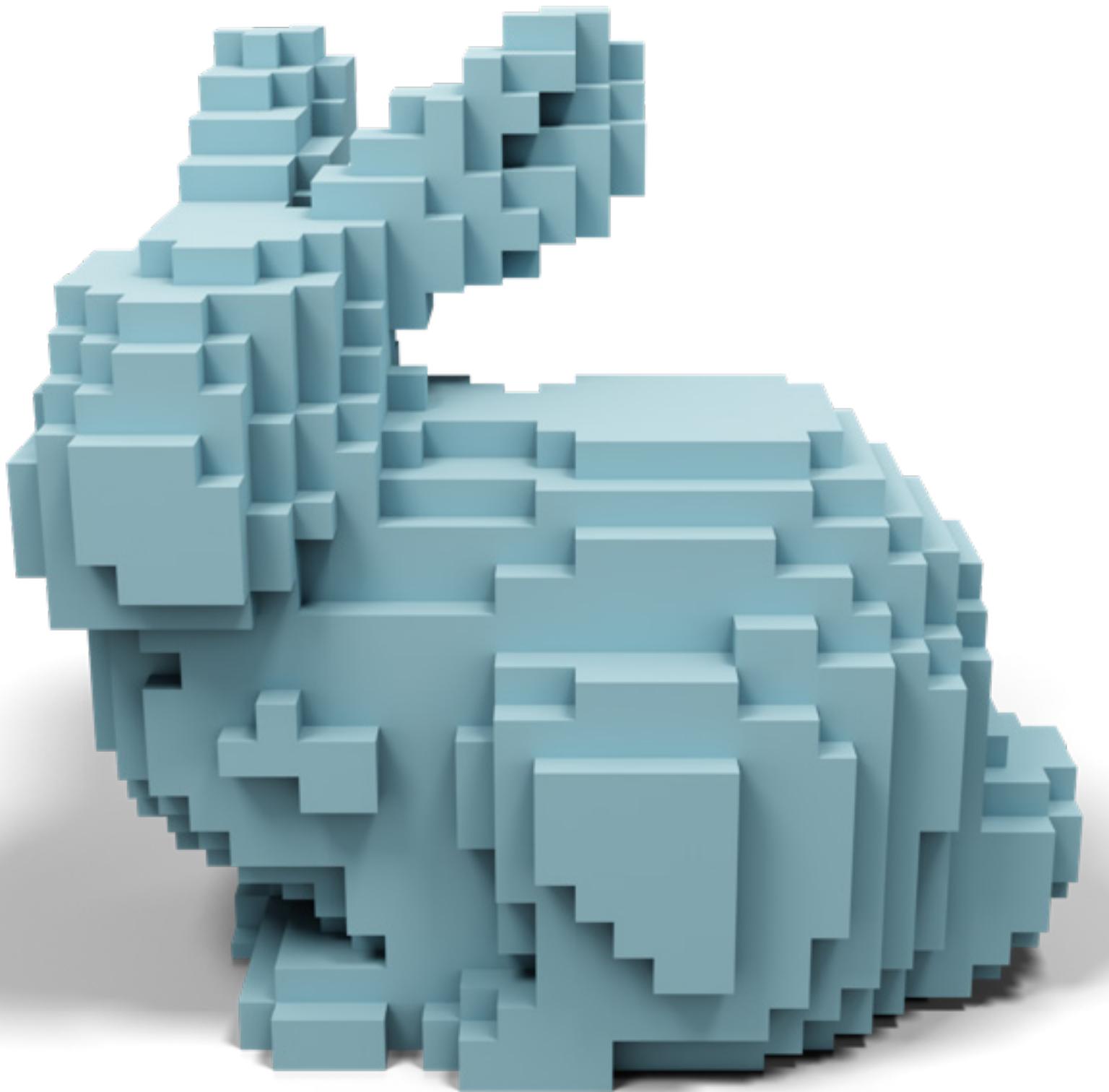
## Machine Learning & Geometry Processing



## Learning from a Single Mesh

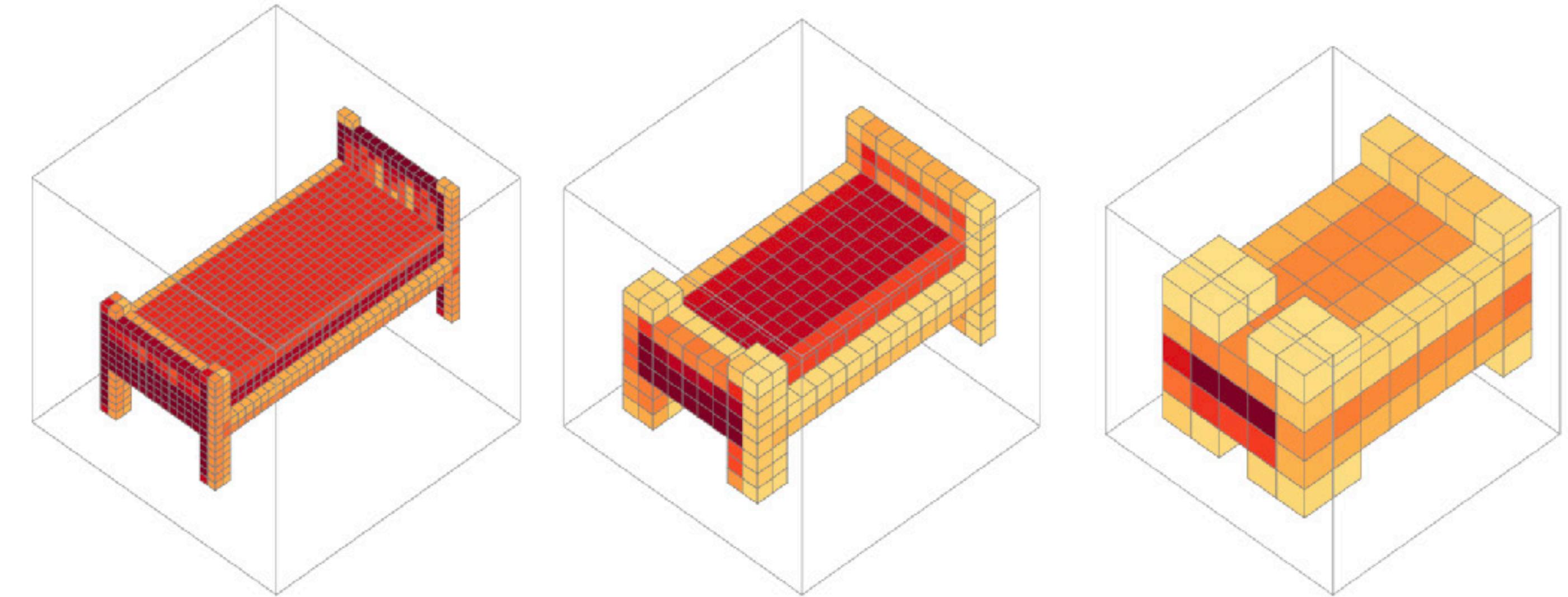
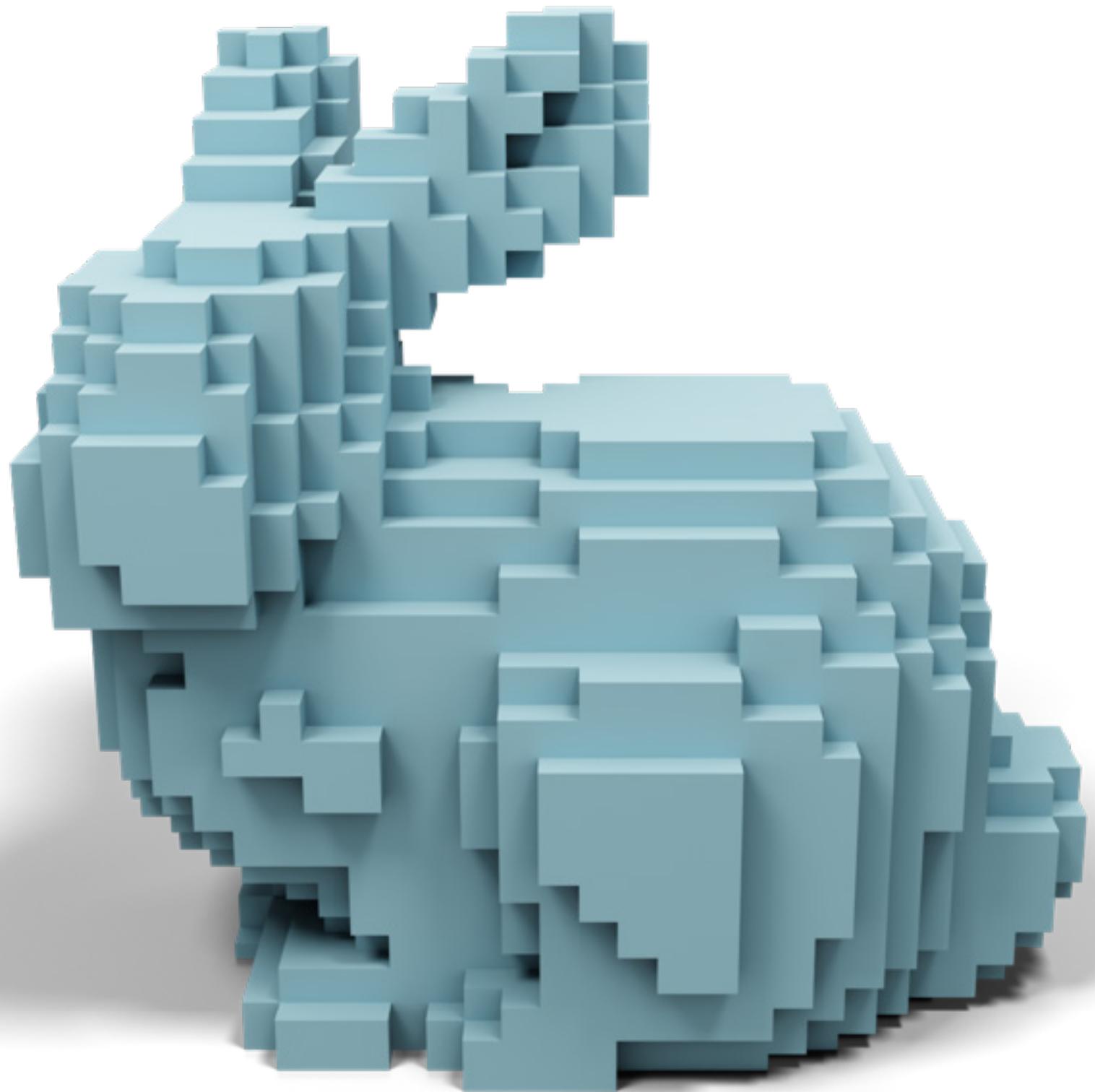


# Voxel (3D Pixel) Representation



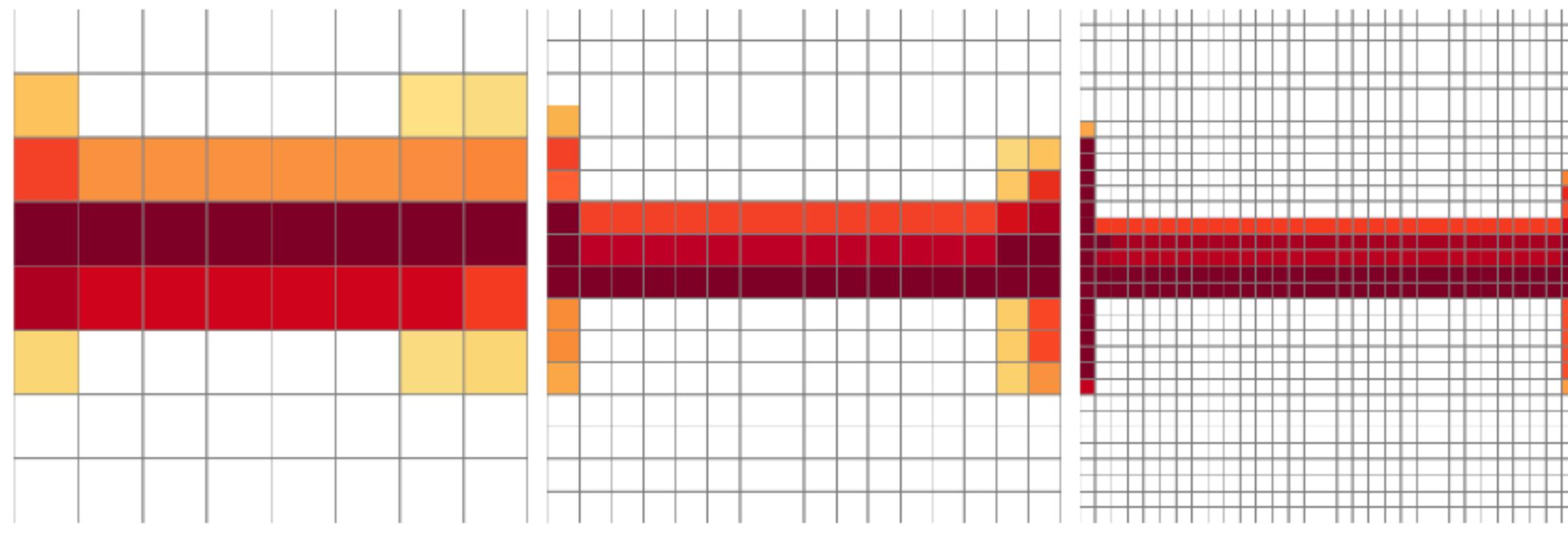
convolution

# Voxel (3D Pixel) Representation

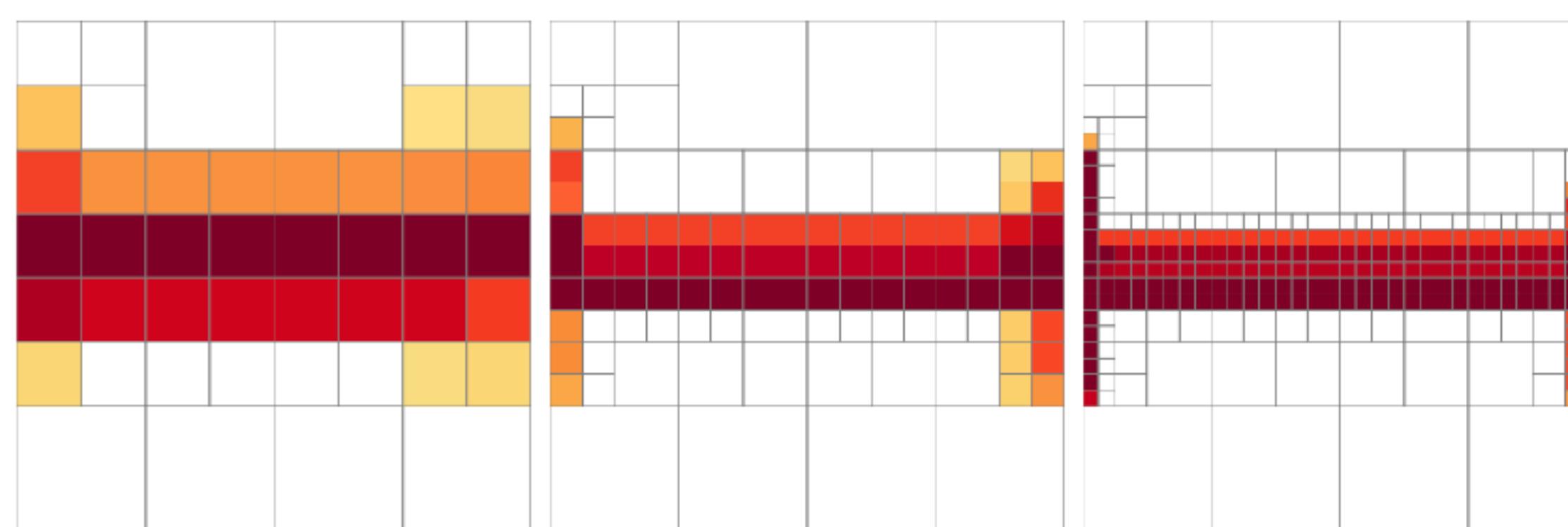


pooling

# Large Memory Cost



Octree



## O-CNN: Octree-based Convolutional Neural Networks for 3D Shape Analysis

PENG-SHUAI WANG, Tsinghua University and Microsoft Research Asia

YANG LIU, Microsoft Research Asia

YU-XIAO GUO, University of Electronic Science and Technology of China and Microsoft Research Asia

CHUN-YU SUN, Tsinghua University and Microsoft Research Asia

XIN TONG, Microsoft Research Asia

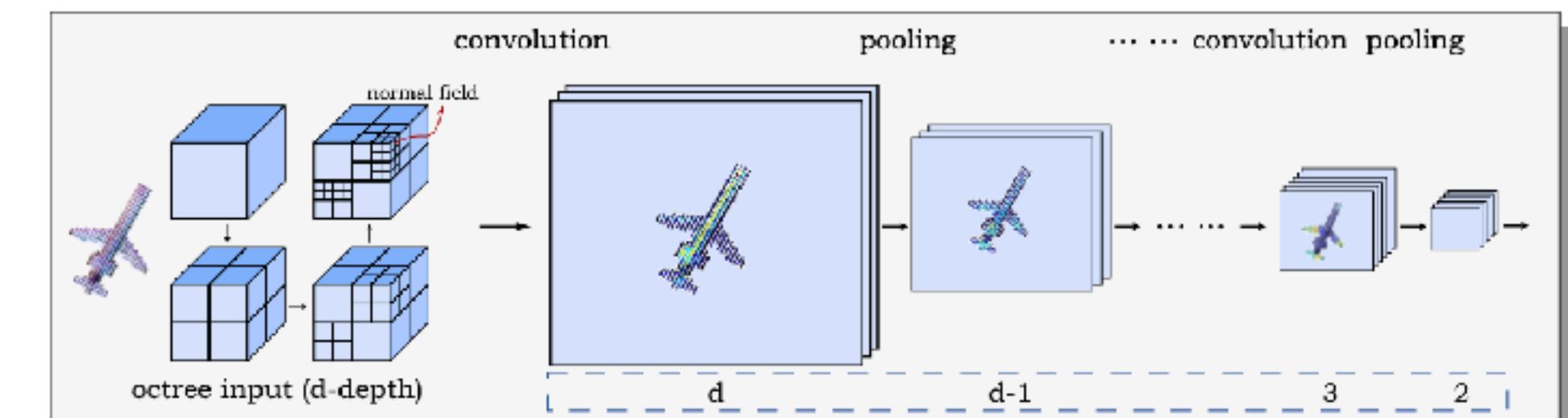


Fig. 1. An illustration of our octree-based convolutional neural network (O-CNN). Our method represents the input shape with an octree and feeds the averaged normal vectors stored in the finest leaf octants to the CNN as input. All the CNN operations are efficiently executed on the GPU and the resulting features are stored in the octree structure. Numbers inside the blue dashed square denote the depth of the octants involved in computation.

We present O-CNN, an Octree-based Convolutional Neural Network (CNN) for 3D shape analysis. Built upon the octree representation of 3D shapes, our method takes the average normal vectors of a 3D model sampled in the finest leaf octants as input and performs 3D CNN operations on the octants occupied by the 3D shape surface. We design a novel octree data structure to efficiently store the octant information and CNN features into the graphics memory and execute the entire O-CNN training and evaluation on the GPU. O-CNN supports various CNN structures and works for 3D shapes in different representations. By restraining the computations on the octants occupied by 3D surfaces, the memory and computational costs of the O-CNN grow quadratically as the depth of the octree increases, which makes the 3D CNN feasible for high-resolution 3D models. We compare the performance of the O-CNN with other existing 3D CNN solutions and demonstrate the efficiency and efficacy of O-CNN in three shape analysis tasks, including object classification, shape retrieval, and shape segmentation.

CCS Concepts: • Computing methodologies → Mesh models; Point-based models; Neural networks;

Additional Key Words and Phrases: octree, convolutional neural network, object classification, shape retrieval, shape segmentation

ACM Reference format:

Peng-Shuai Wang, Yang Liu, Yu-Xiao Guo, Chun-Yu Sun, and Xin Tong. 2017. O-CNN: Octree-based Convolutional Neural Networks for 3D Shape Analysis. *ACM Trans. Graph.* 36, 4, Article 72 (July 2017), 11 pages.

<https://doi.org/10.1145/3022959.3023608>

## 1 INTRODUCTION

With recent advances in low-cost 3D acquisition devices and 3D modeling tools, the amount of 3D models created by end users has been increasing quickly. Analyzing and understanding these 3D shapes, as for classification, segmentation, and retrieval, have become more and more important for many graphics and vision applications. A key technique for these shape analysis tasks is to extract features of 3D models that can sufficiently characterize their shapes and parts.

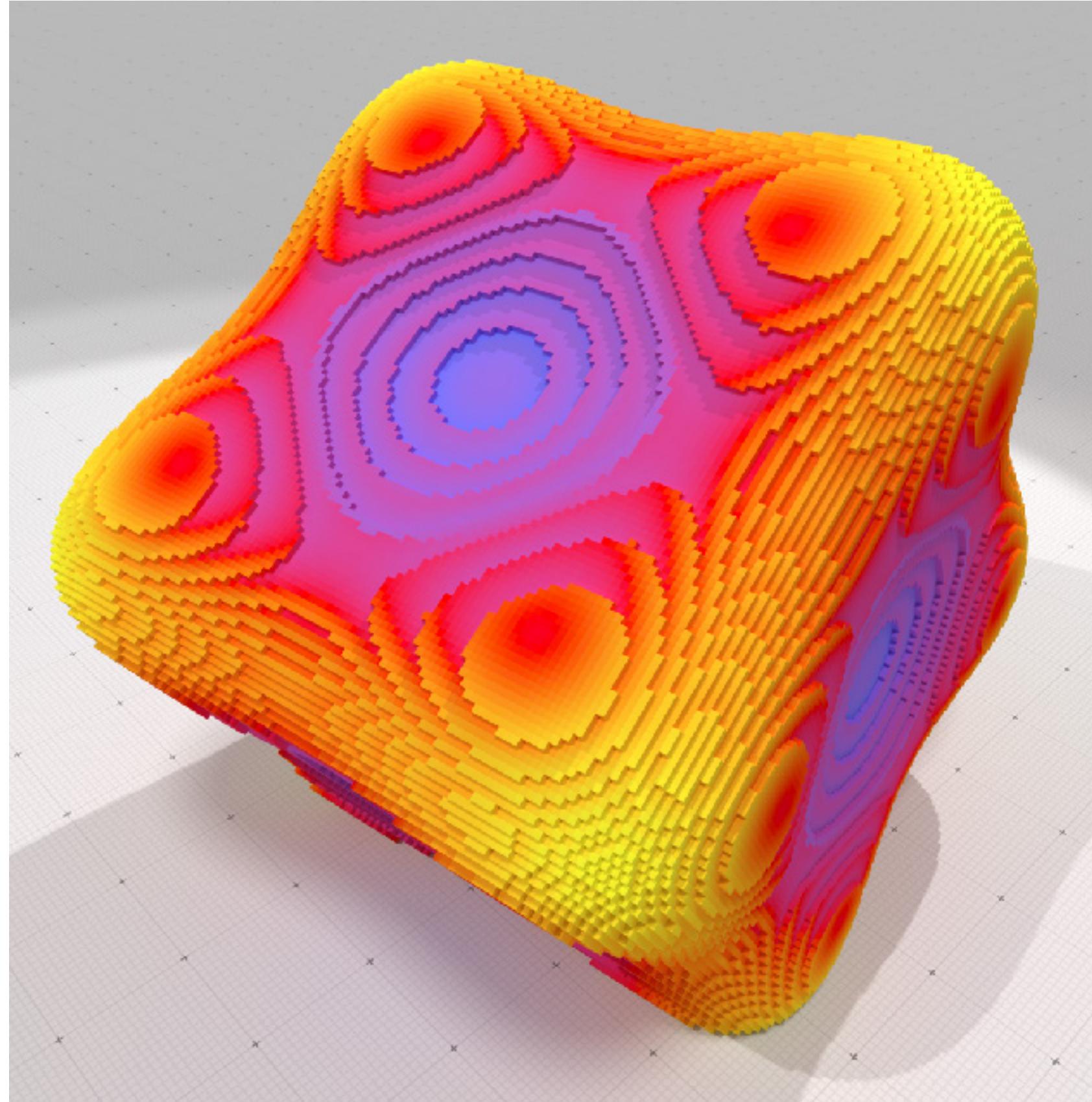
In the computer vision field, convolutional neural networks (CNNs) are widely used for image feature extraction and have demonstrated their advantages over manually-crafted solutions in most image analysis and understanding tasks. However, it is a non-trivial task to adapt a CNN designed for regularly sampled 2D images to 3D shapes modeled by irregular triangle meshes or point clouds. A set of methods convert the 3D shapes to regularly sampled representations and apply a CNN to them. Voxel-based methods [Maturana and Scherer 2015; Wu et al. 2015] rasterize a 3D shape as an indicator function or distance function sampled over dense voxels and apply a 3D CNN over the entire 3D volume. Since the memory and computation cost grow cubically as the voxel resolution increases, these methods become prohibitively expensive for high-resolution voxels. Manifold-based methods [Boscaini et al. 2015, 2016; Masci

# Not a smooth representation



source: minecraft

# Estimating surface quantities on voxels

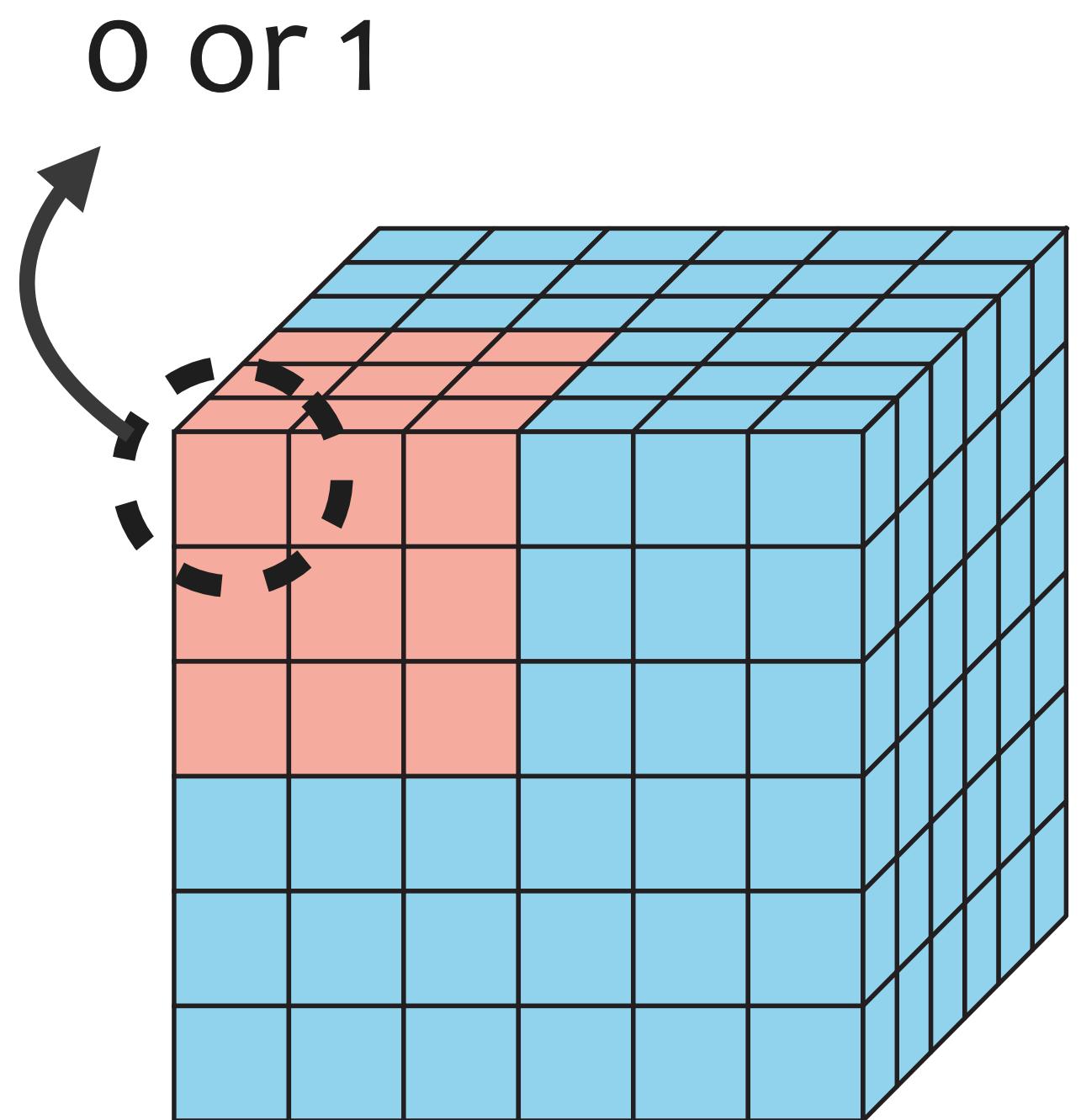


Caissard et al. 2019



Lachaud et al. 2020

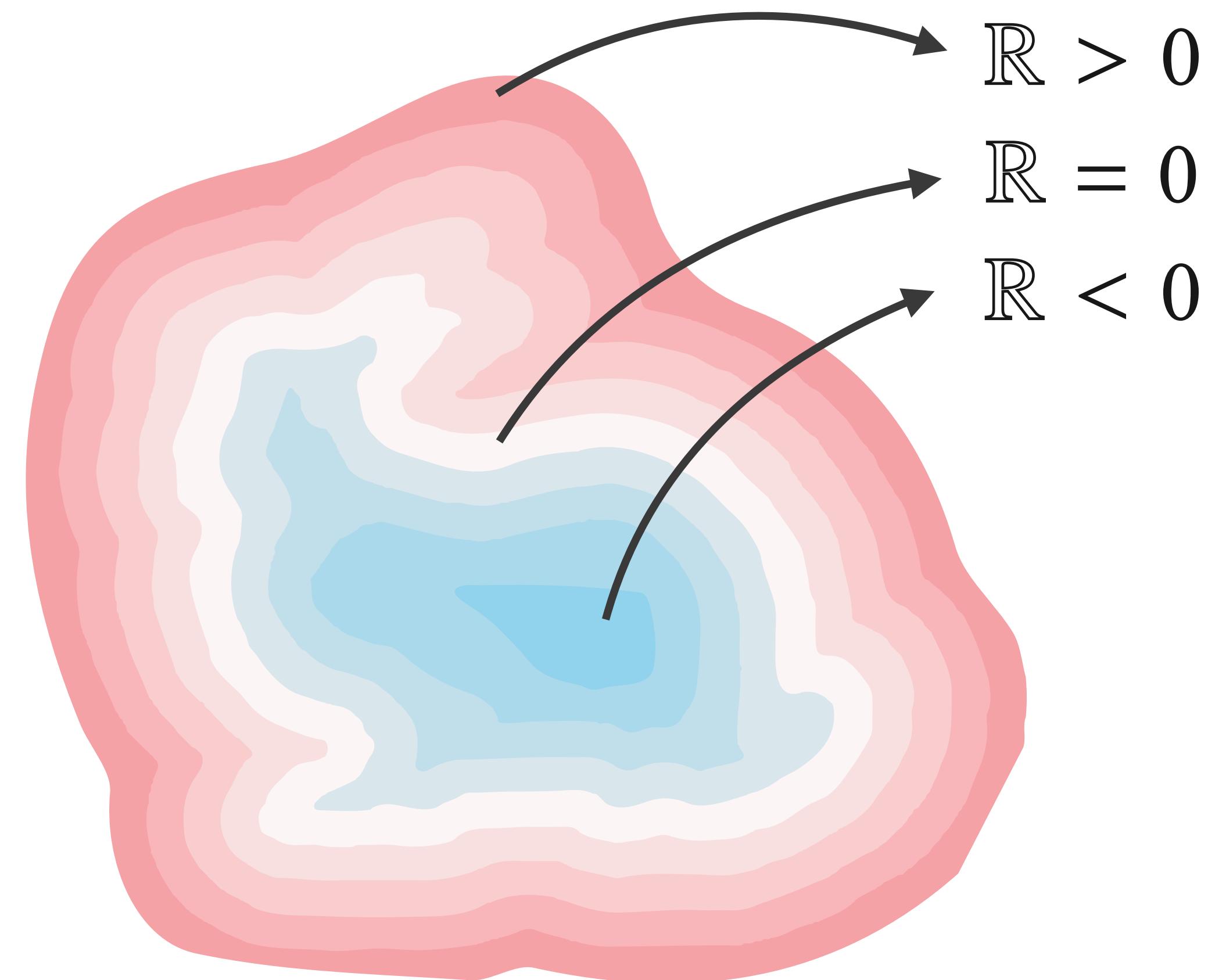
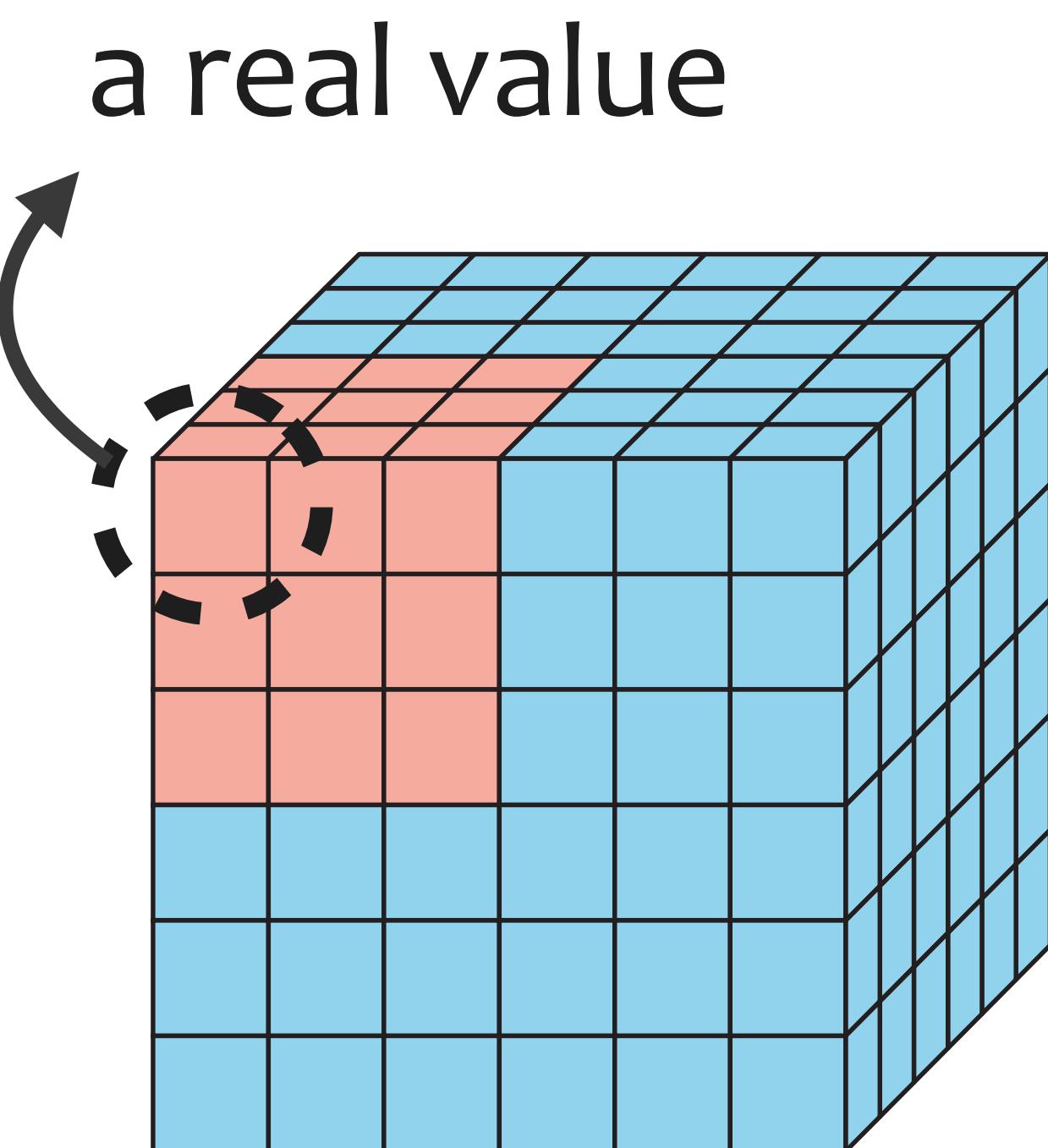
# Not store {0,1}



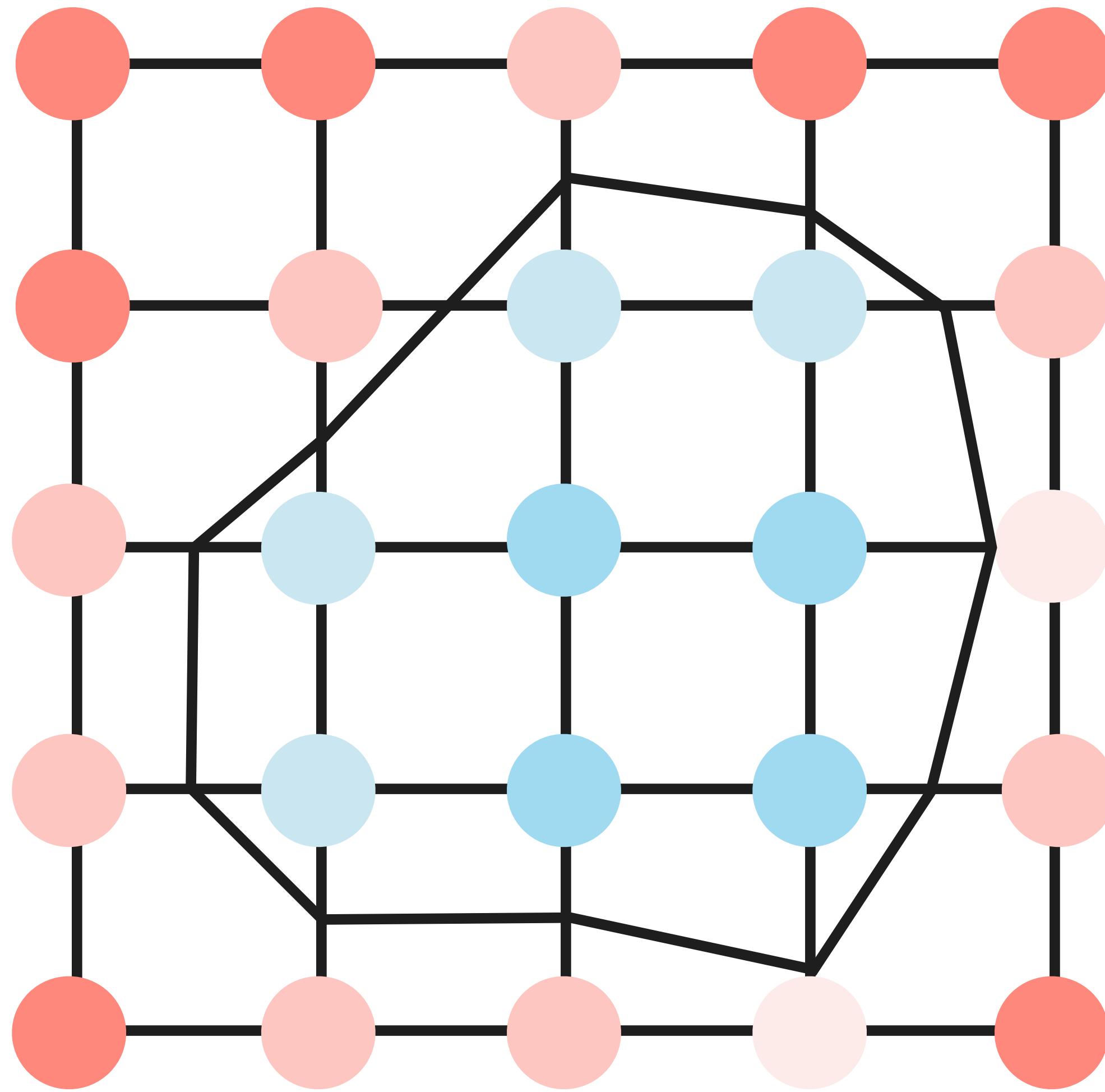
# Not store {0,1}

signed distance function (SDF)

[Dai et al. 2017, Zeng et al. 2017, Stutz et al. 2018]

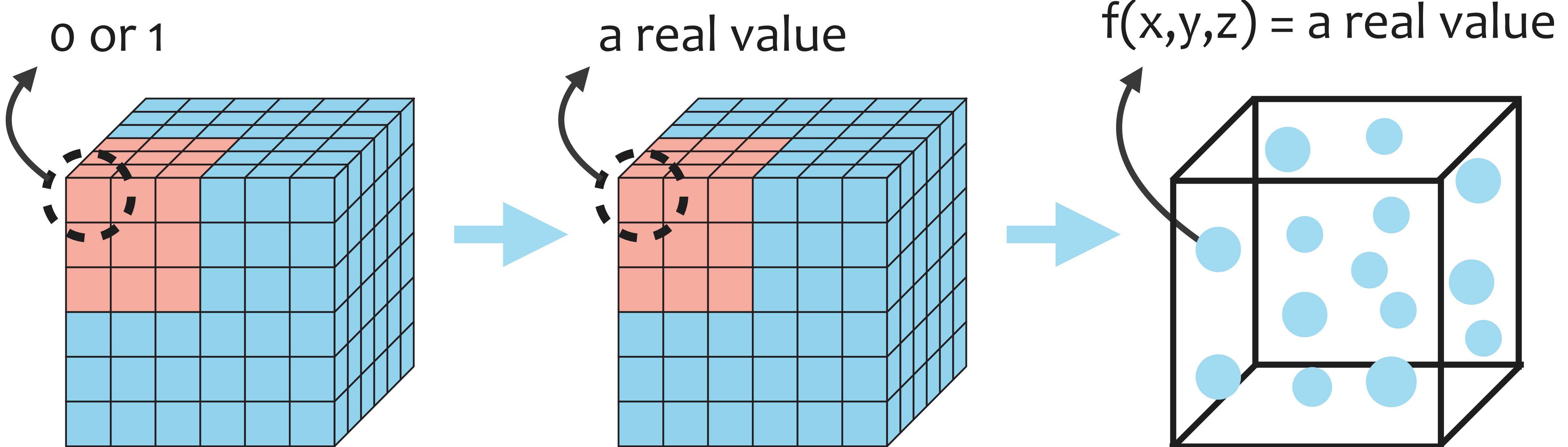


# SDF to sub-pixel resolution

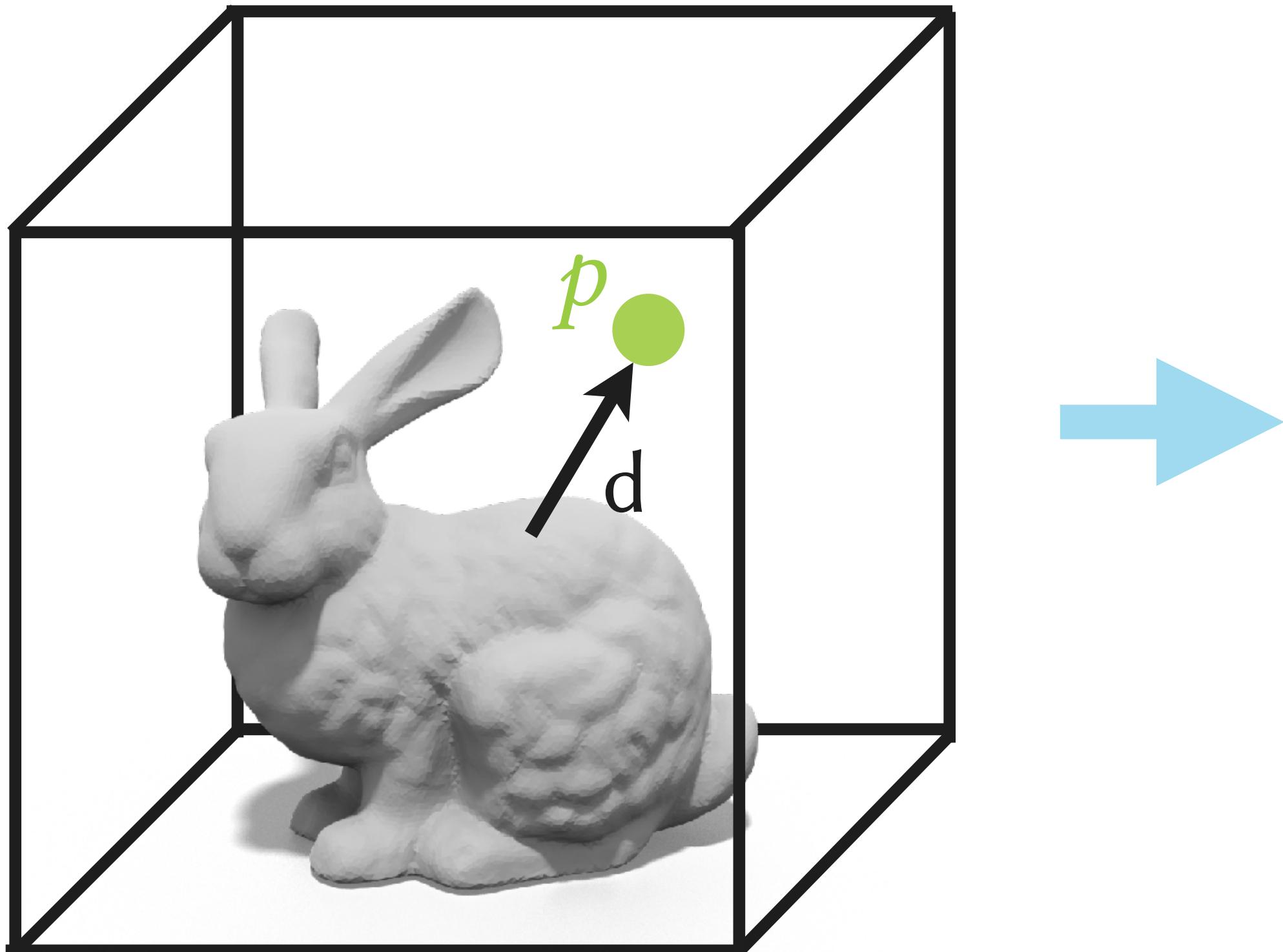


[Dai et al. 2017]

# Get rid of the voxel grid

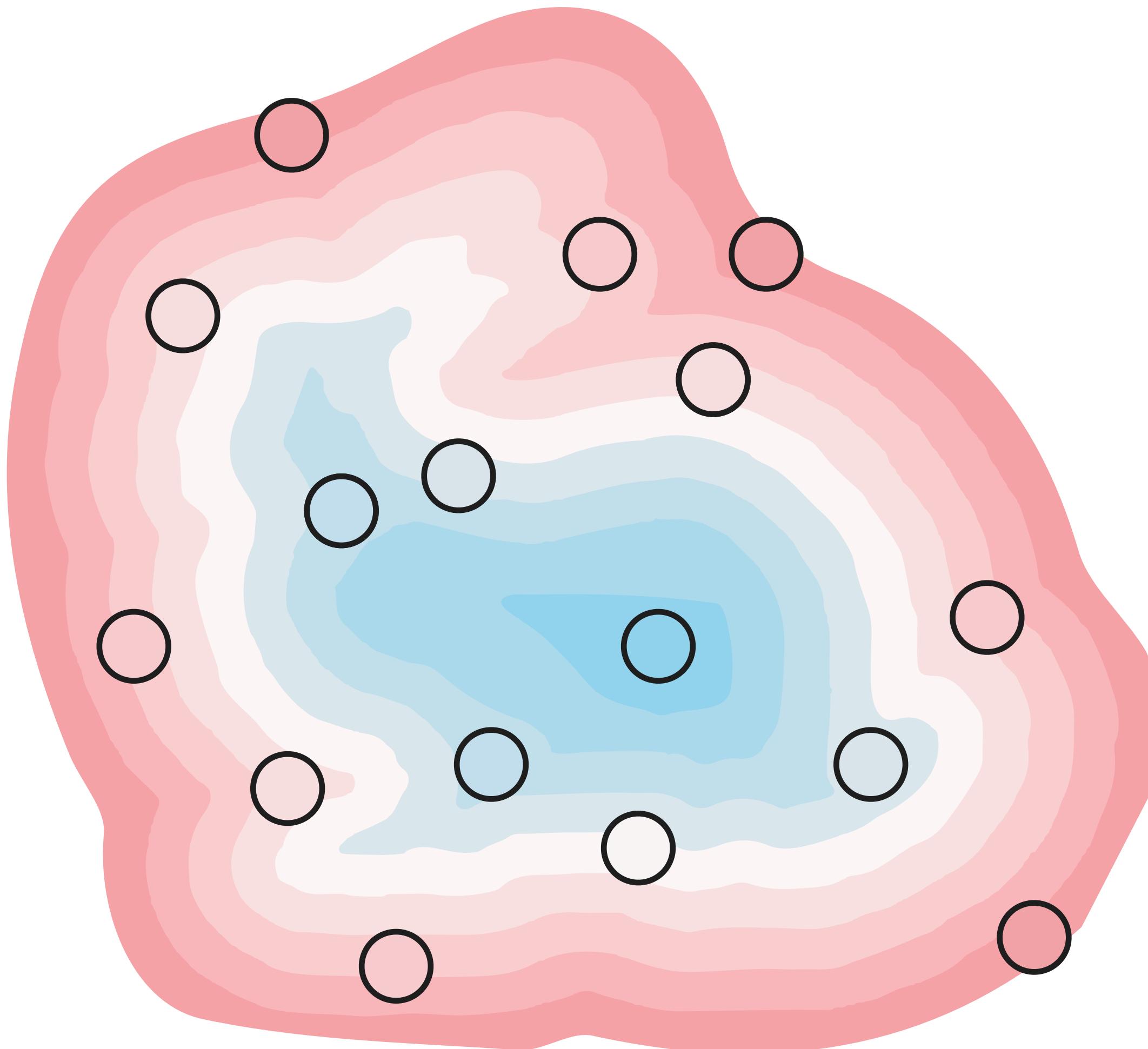


# Neural Signed Distance Function



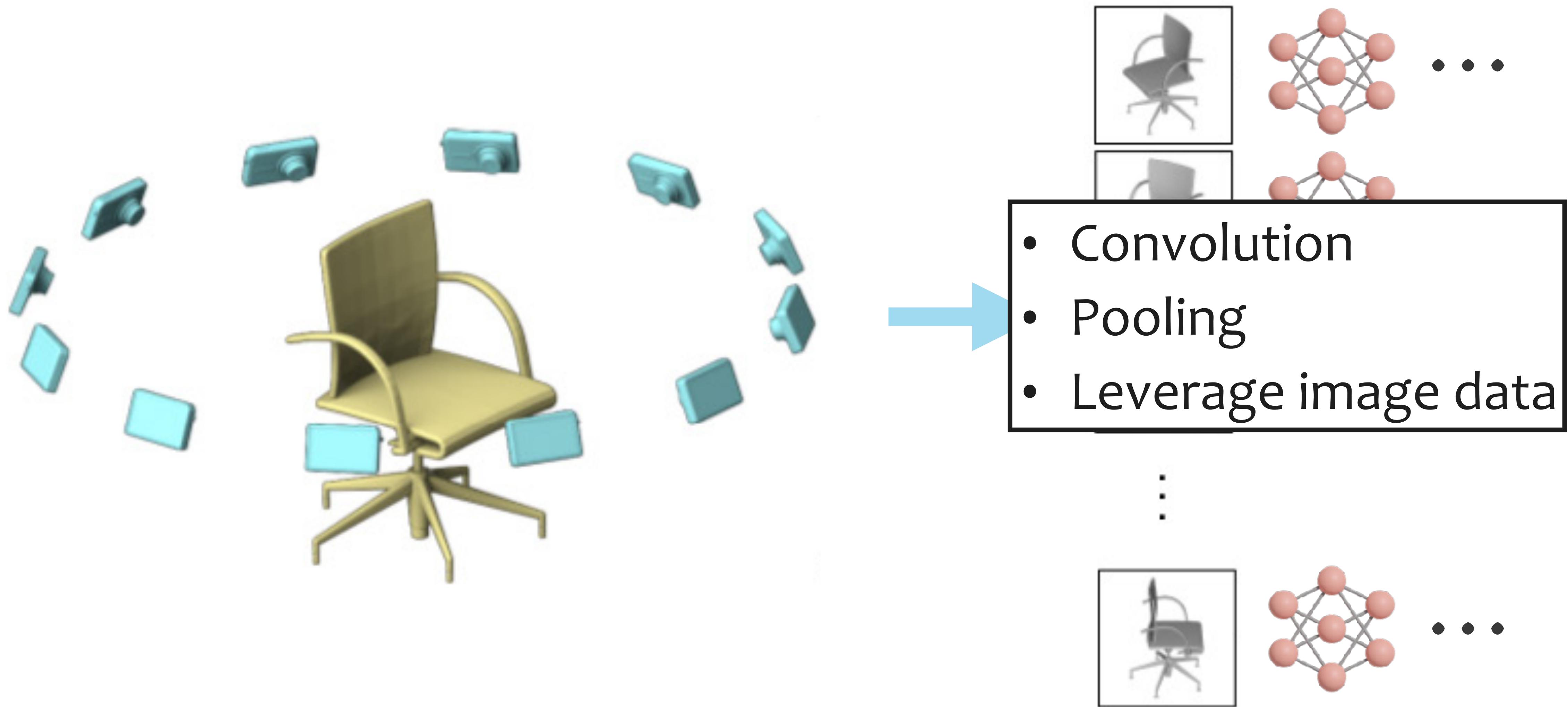
$$f_{\theta}(p_x, p_y, p_z) = \text{signed distance}$$

# An Alternative Shape Representation



- missing basic ingredients:
- differential operators
  - differential quantities
  - shape editing
  - ...

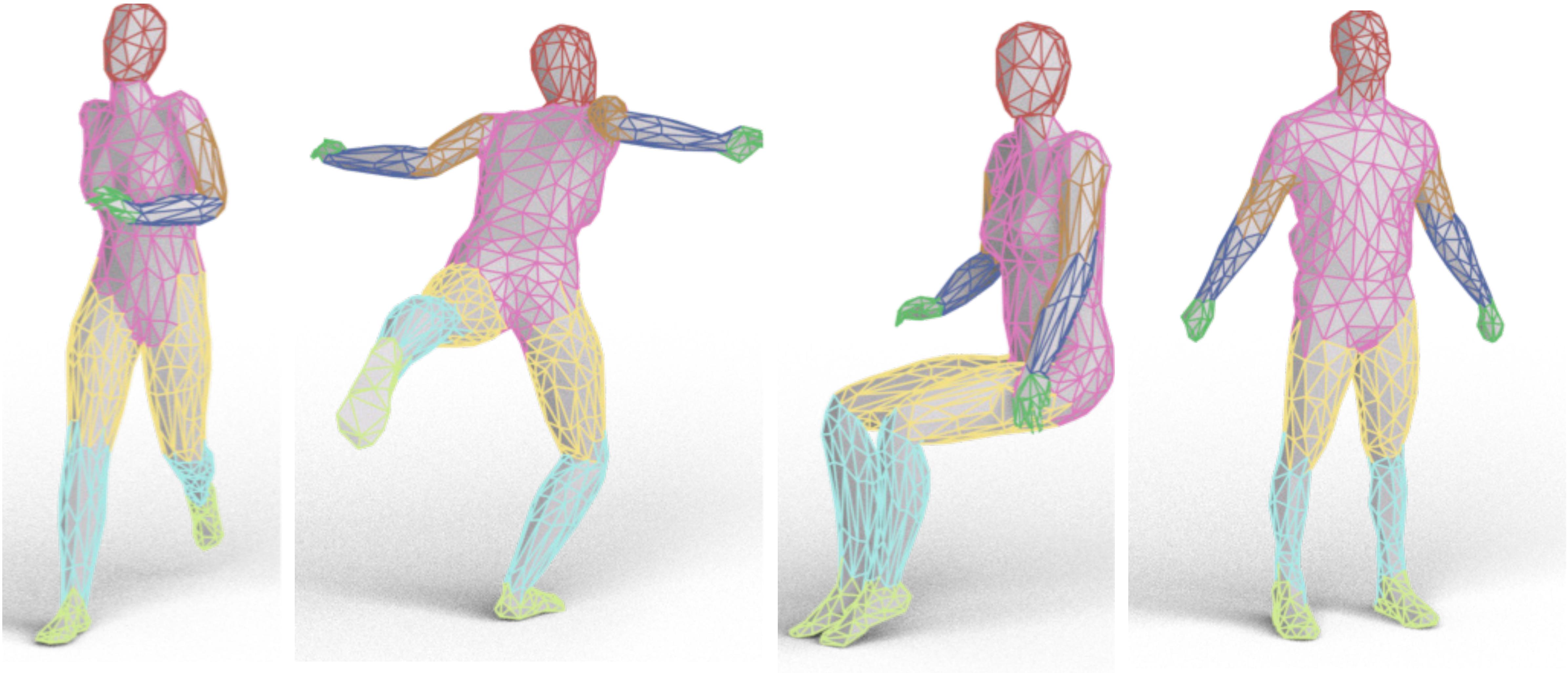
# Use image convolution on surfaces



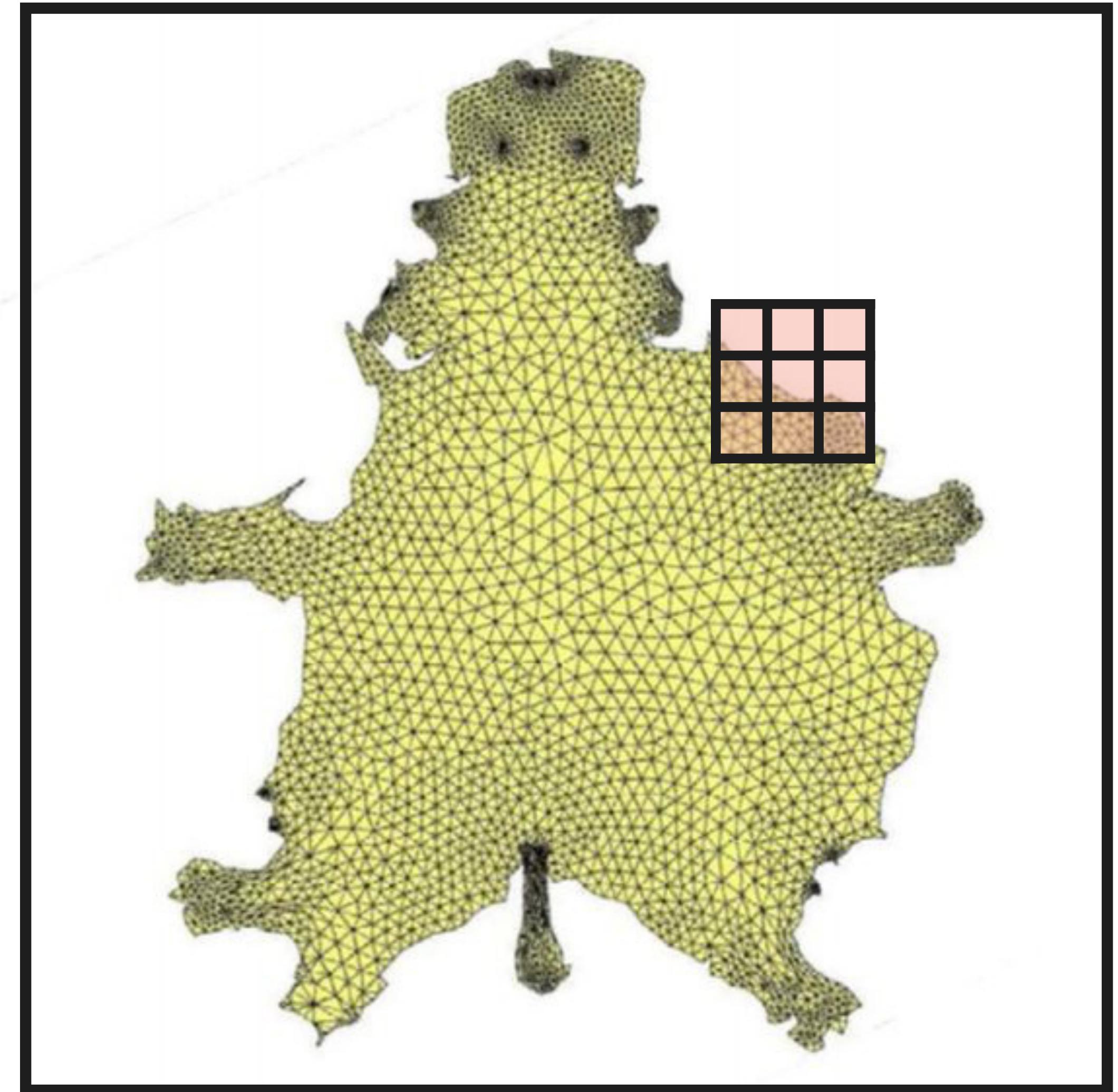
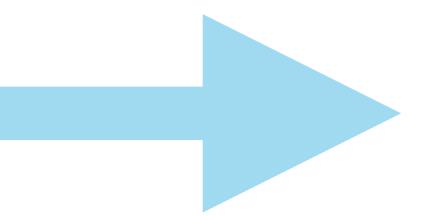
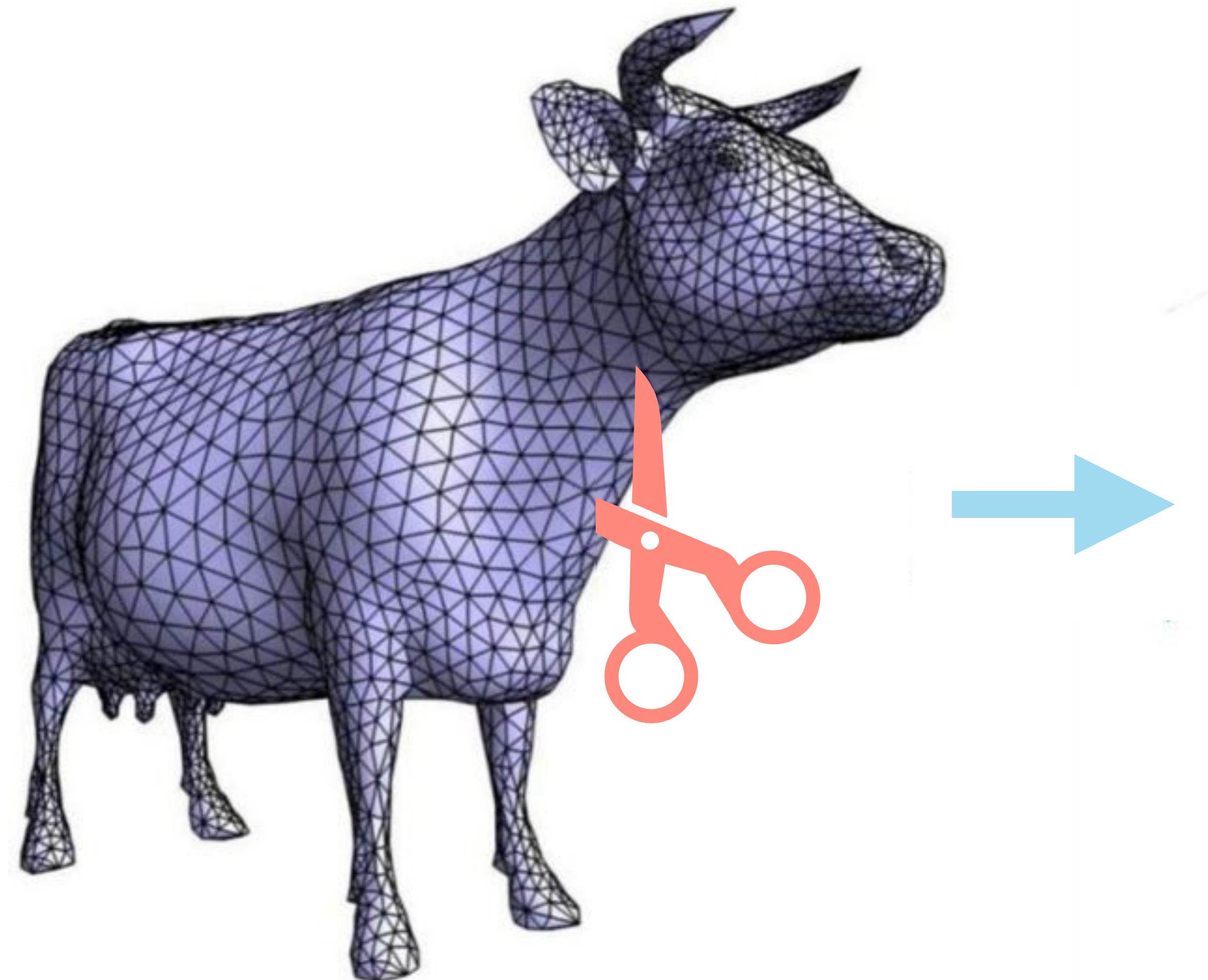
# Leverage Image Data



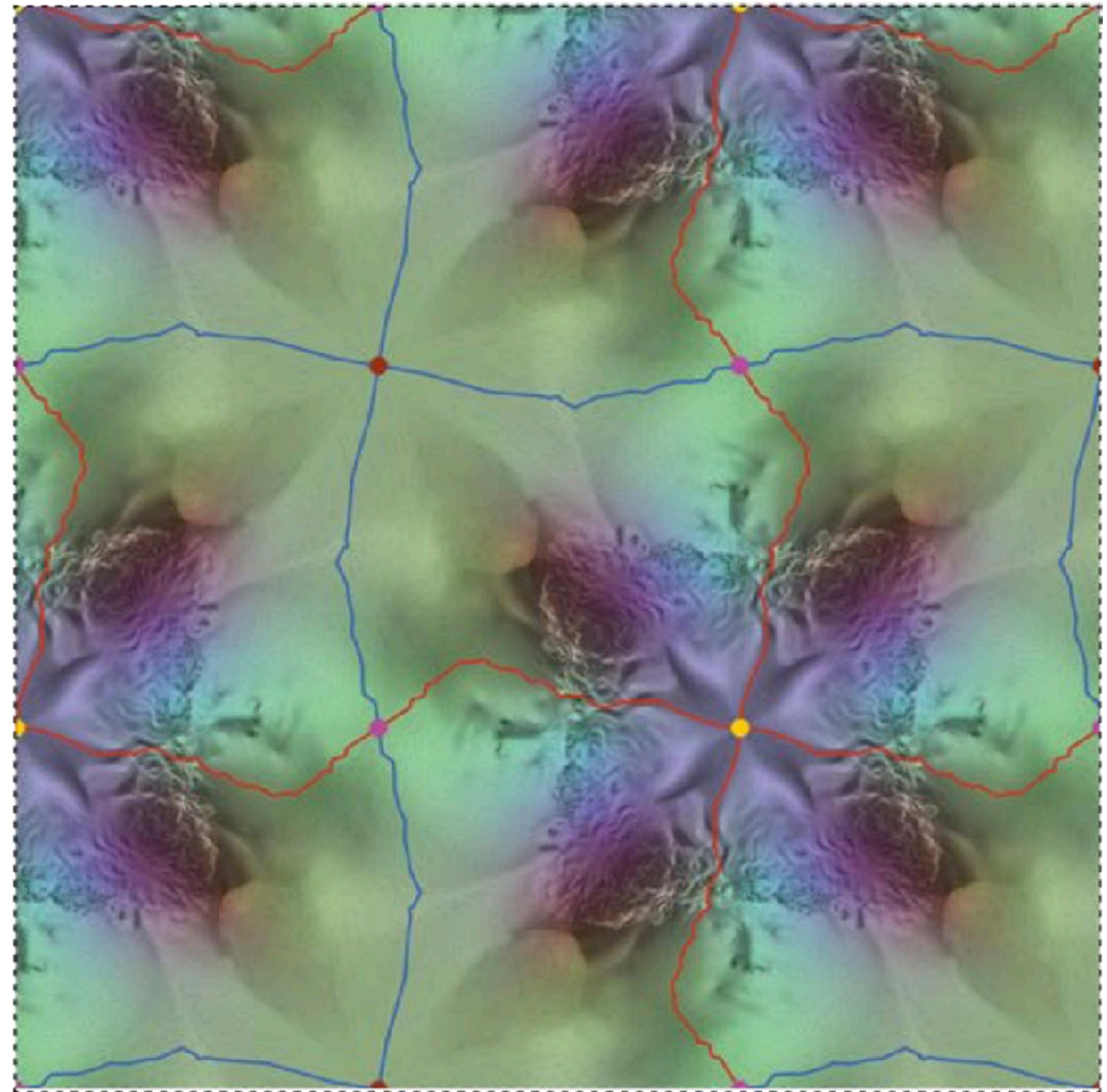
# Extending to local tasks is hard



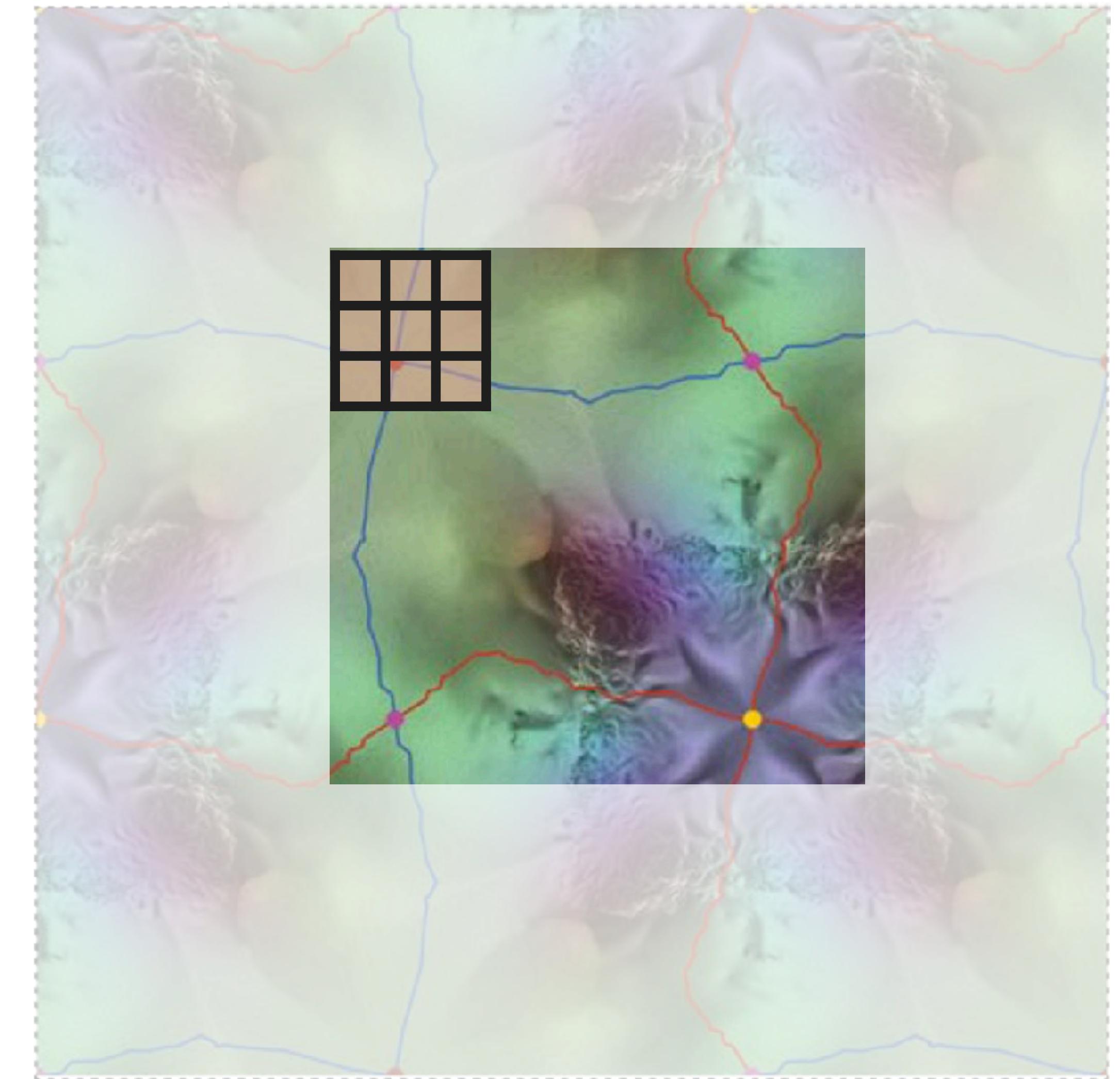
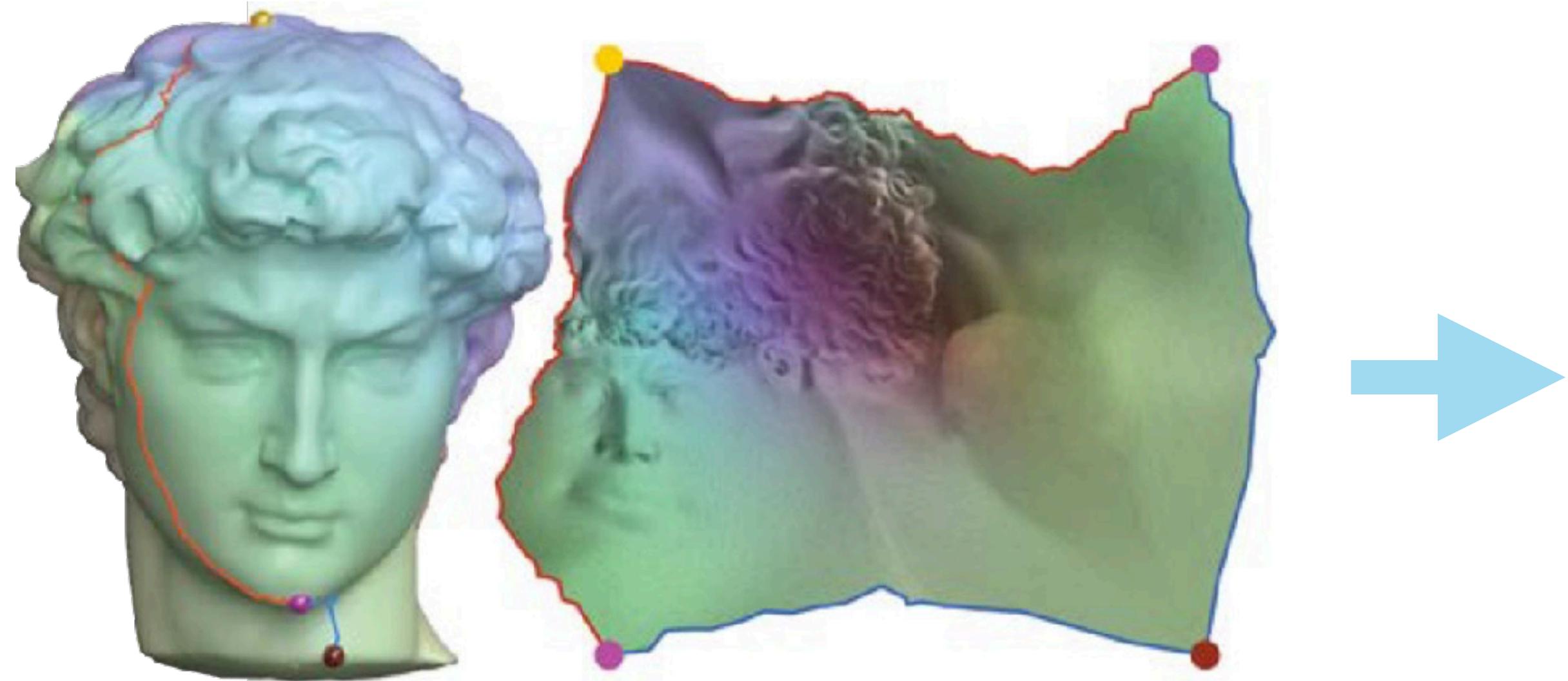
# Global Parameterization



# Seamless Parameterization

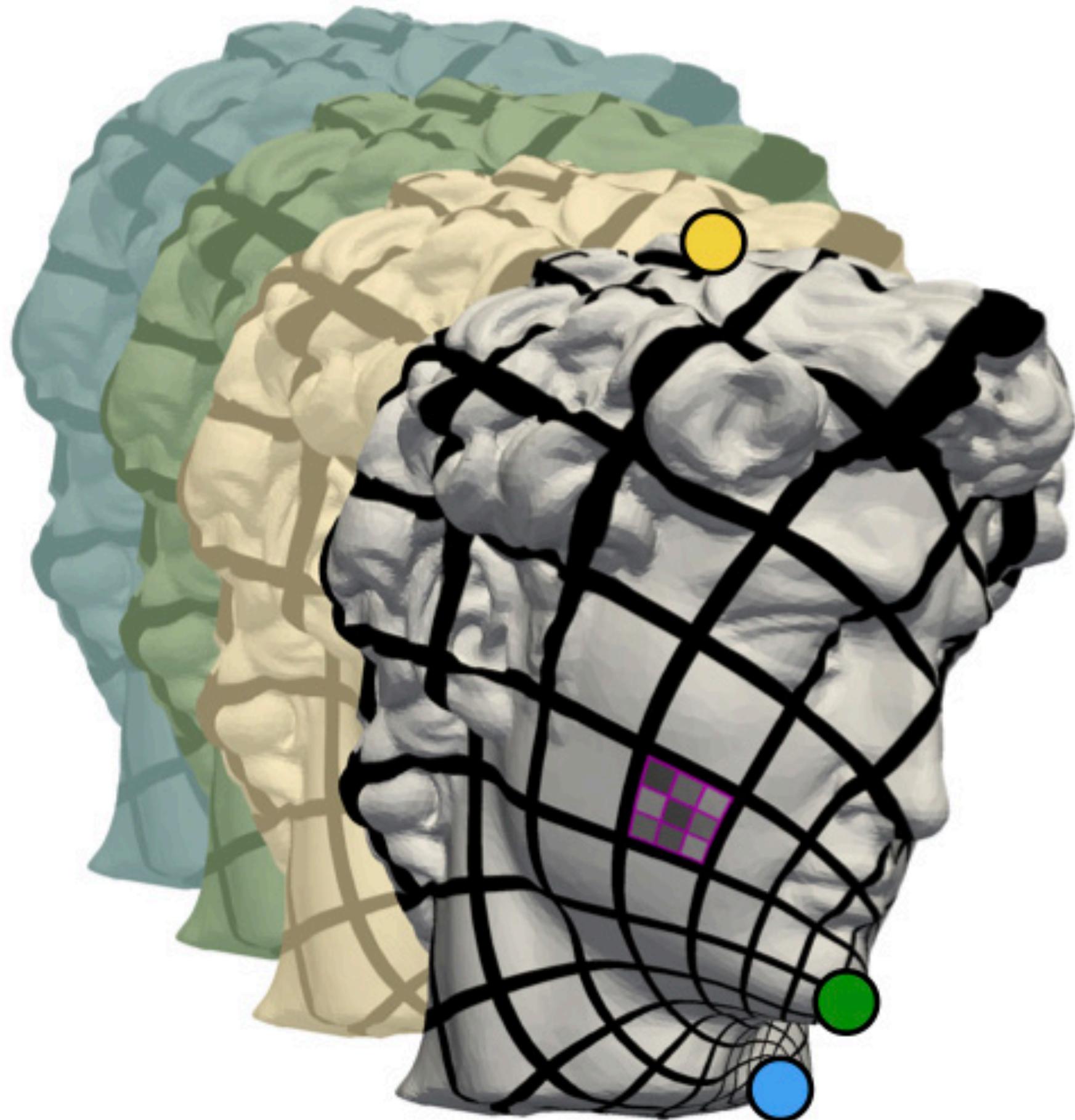


# Seamless Parameterization

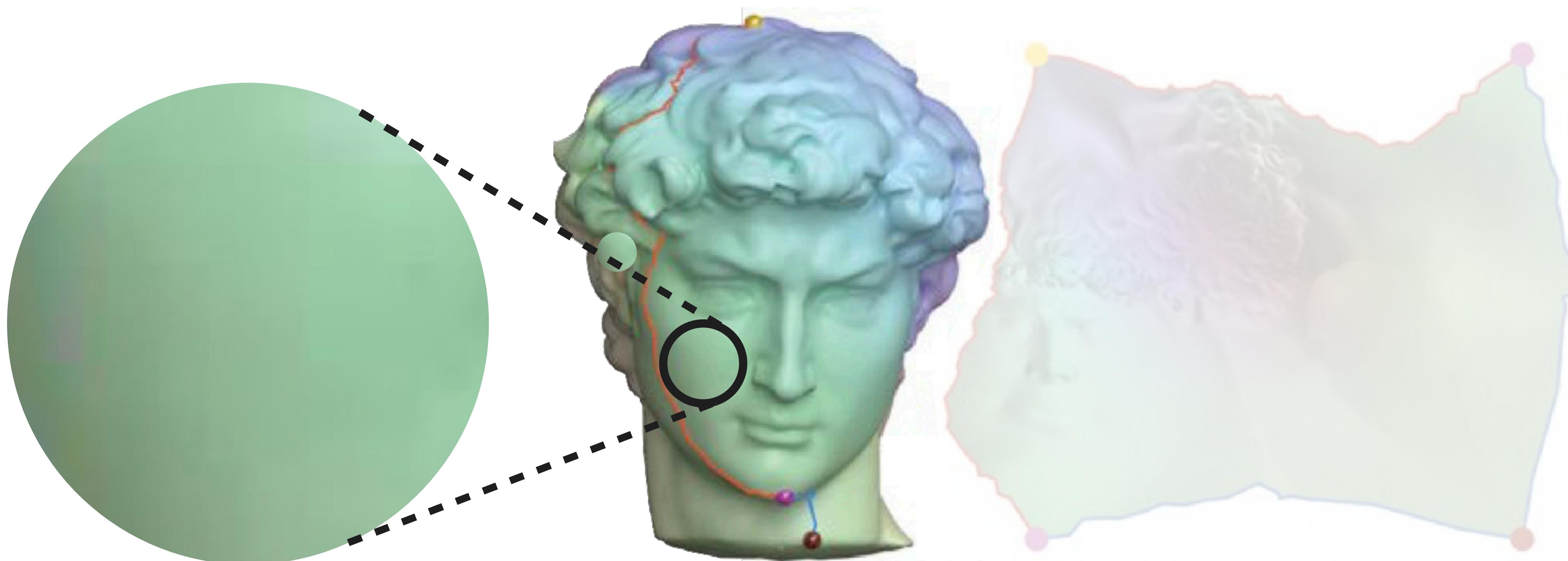


# Challenges

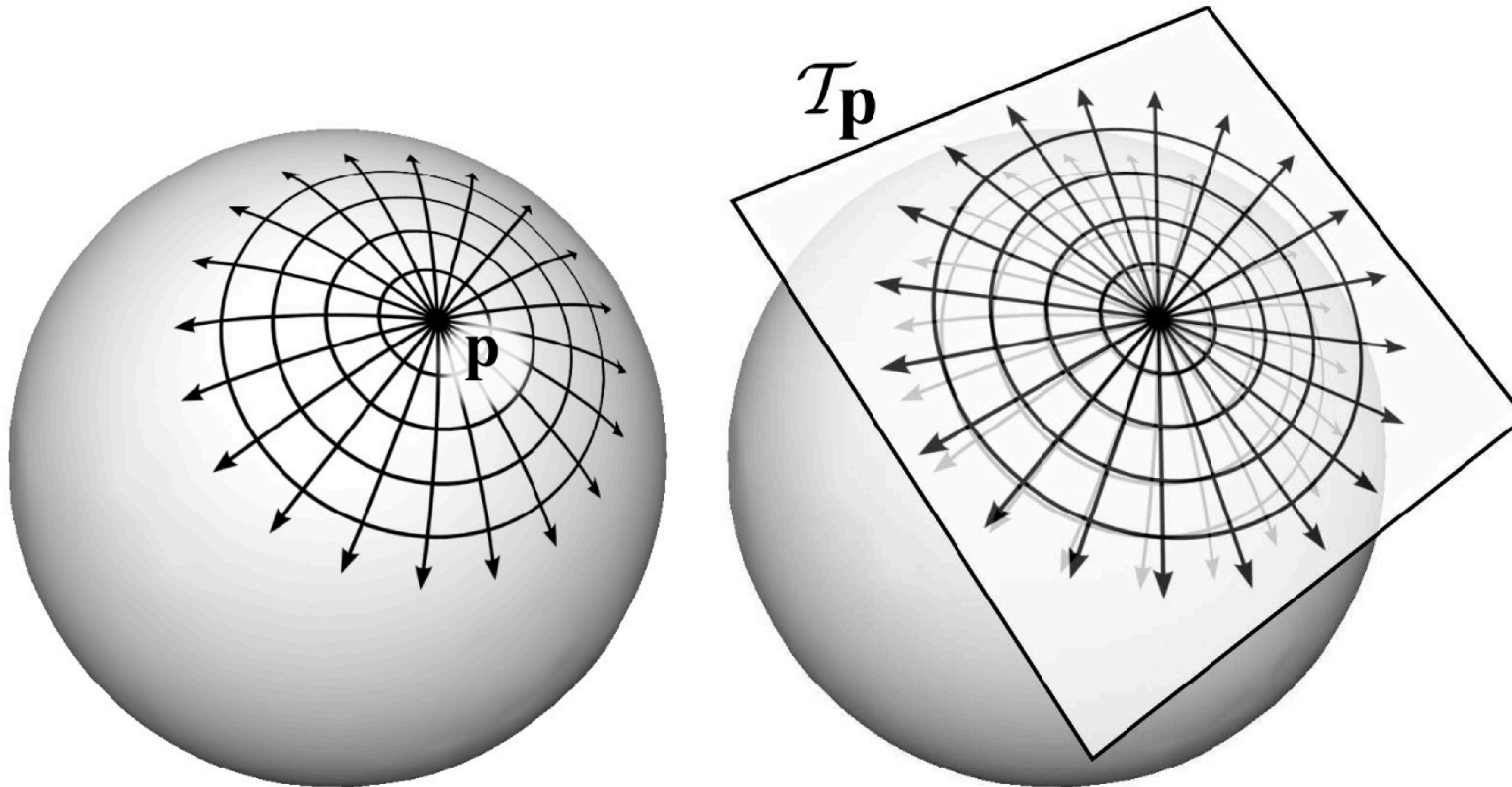
- Not unique
- Orientation
- Cannot avoid distortion



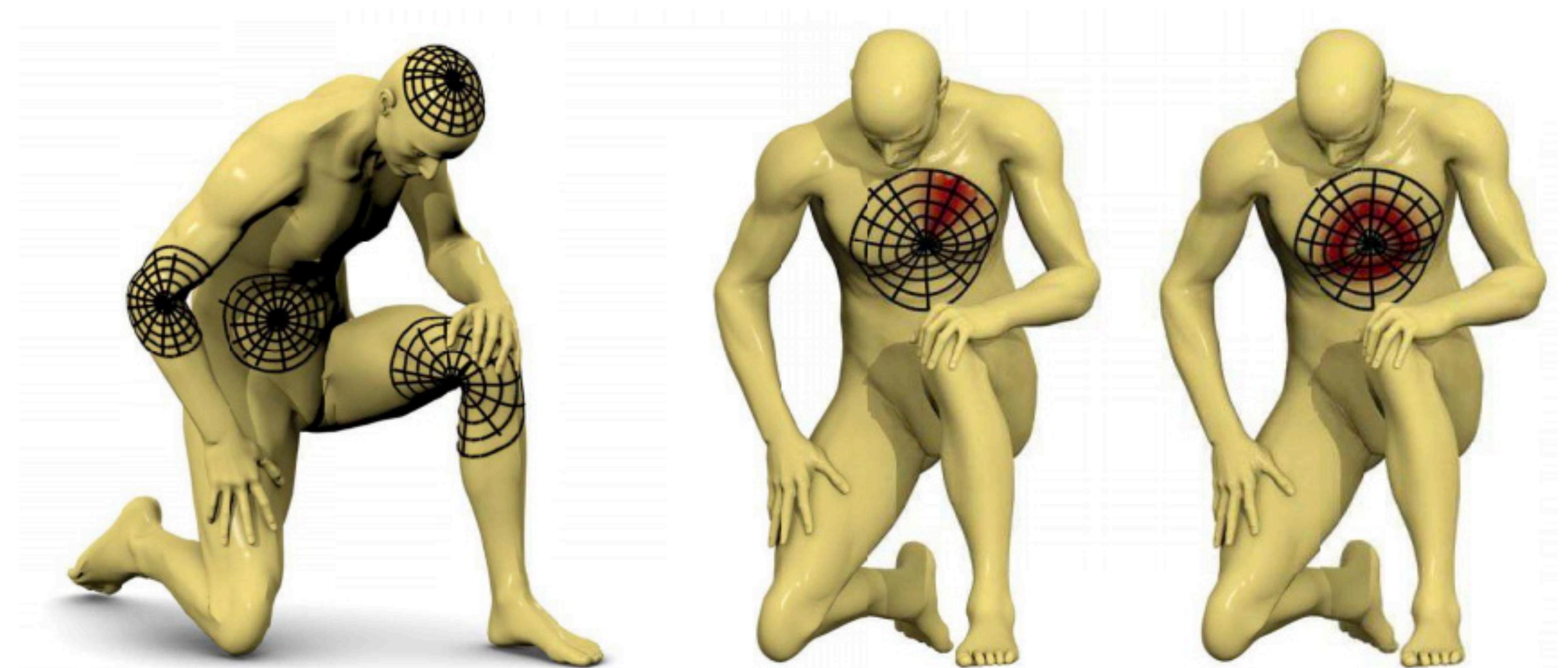
# Local Parameterization



# Exponential Maps



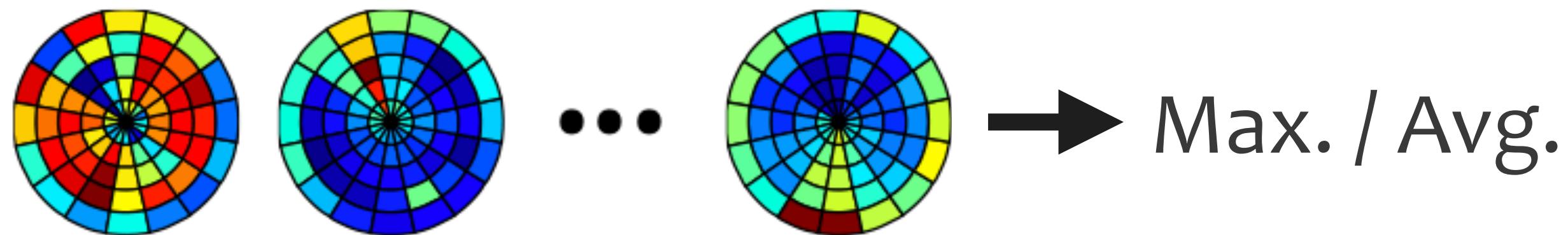
# Geodesic CNNs



Yann LeCun, Yoshua Bengio, Gert Rätsch, Bernhard Schölkopf, Klaus-Robert Müller, Nicolè de Foufoula-Deleage, and Klaus-Robert Müller

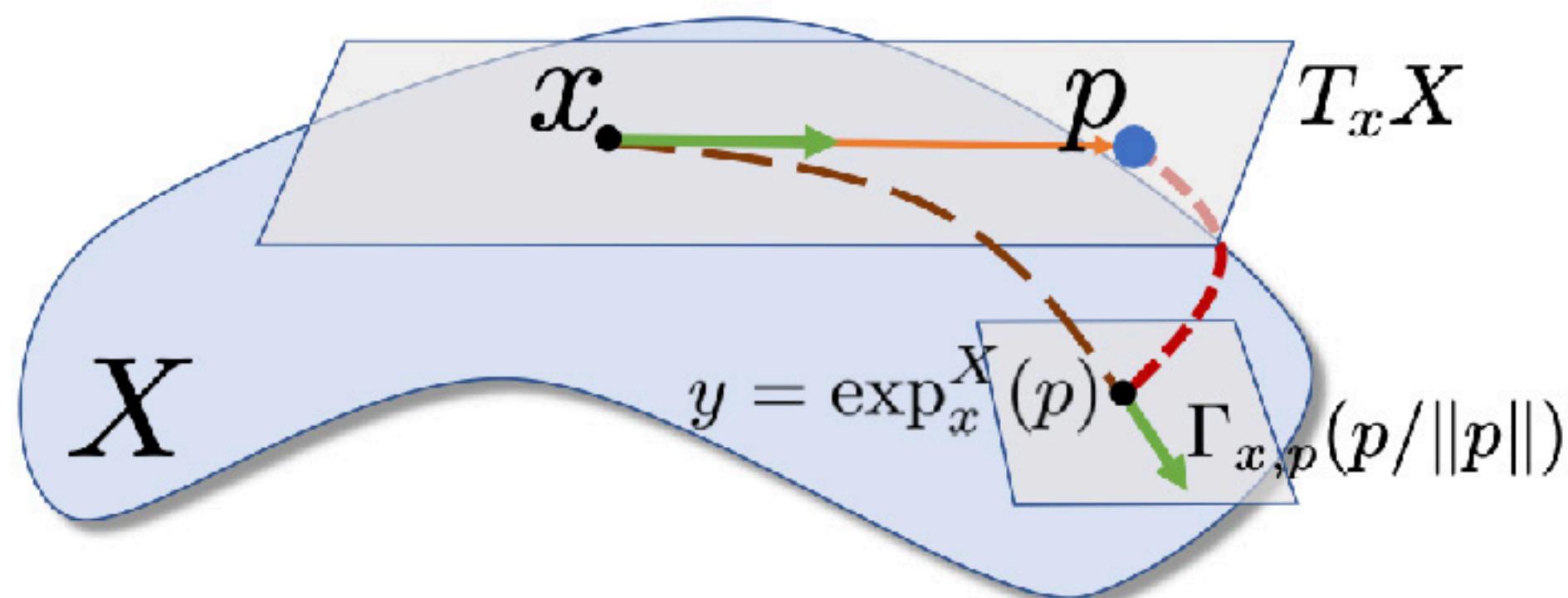
# Which direction to use?

Consider all orientations  
[Masci et al. 2015]



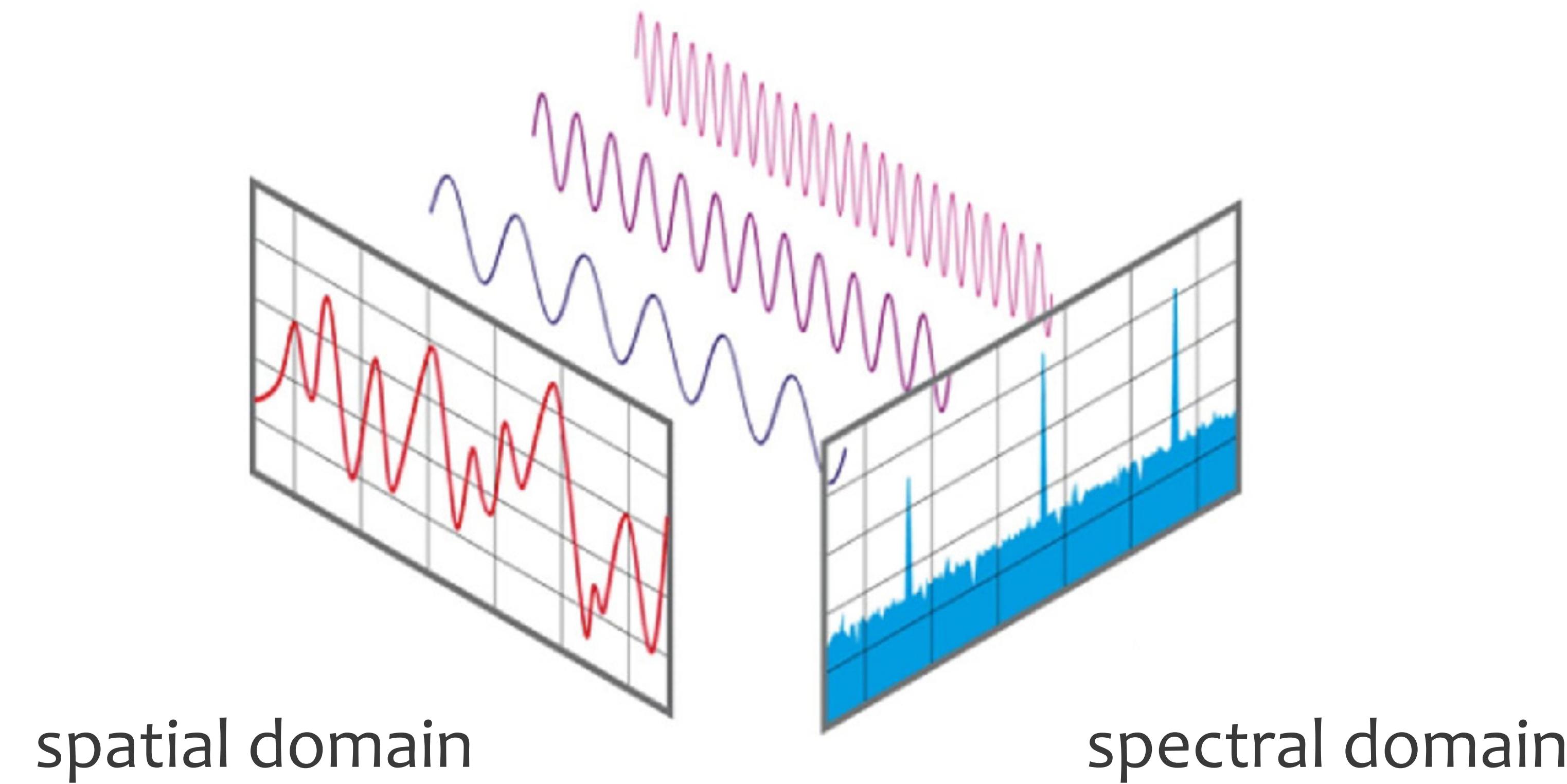
Rotation-Equivariant  
[Wiersma et al. 2020]

Pick one direction at a time  
[Poulenard & Ovsjanikov 2018]

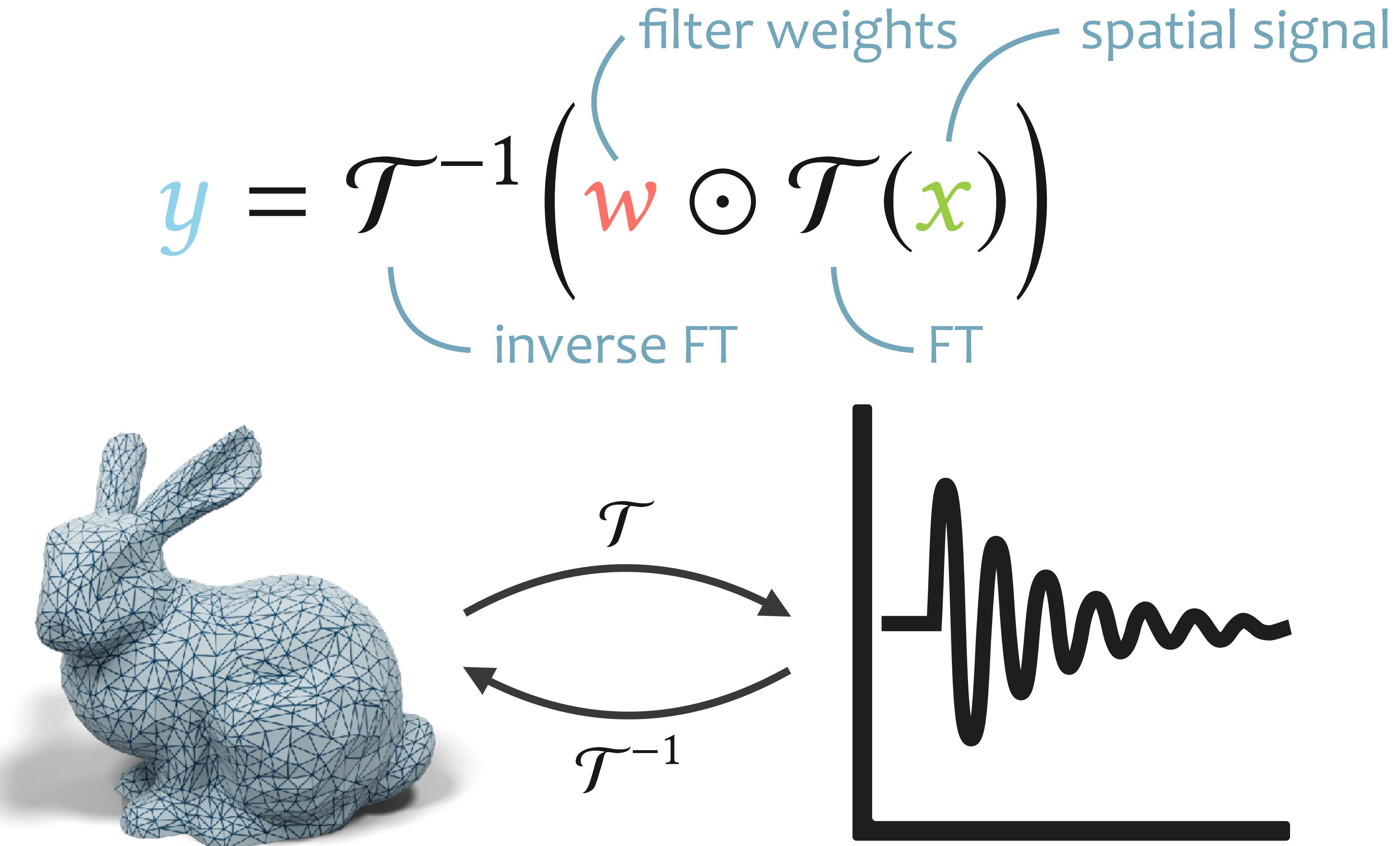


# Spectral Convolution

**Convolution** in the spatial domain is the **point-wise product** in the spectral domain.



# Spectral Convolution (e.g., [Defferrard et al. 2016])



# Issues on Efficiency, Localization, Memory

## Convolutional Neural Networks on Graphs with Fast Localized Spectral Filtering

Michaël Defferrard

Xavier Bresson

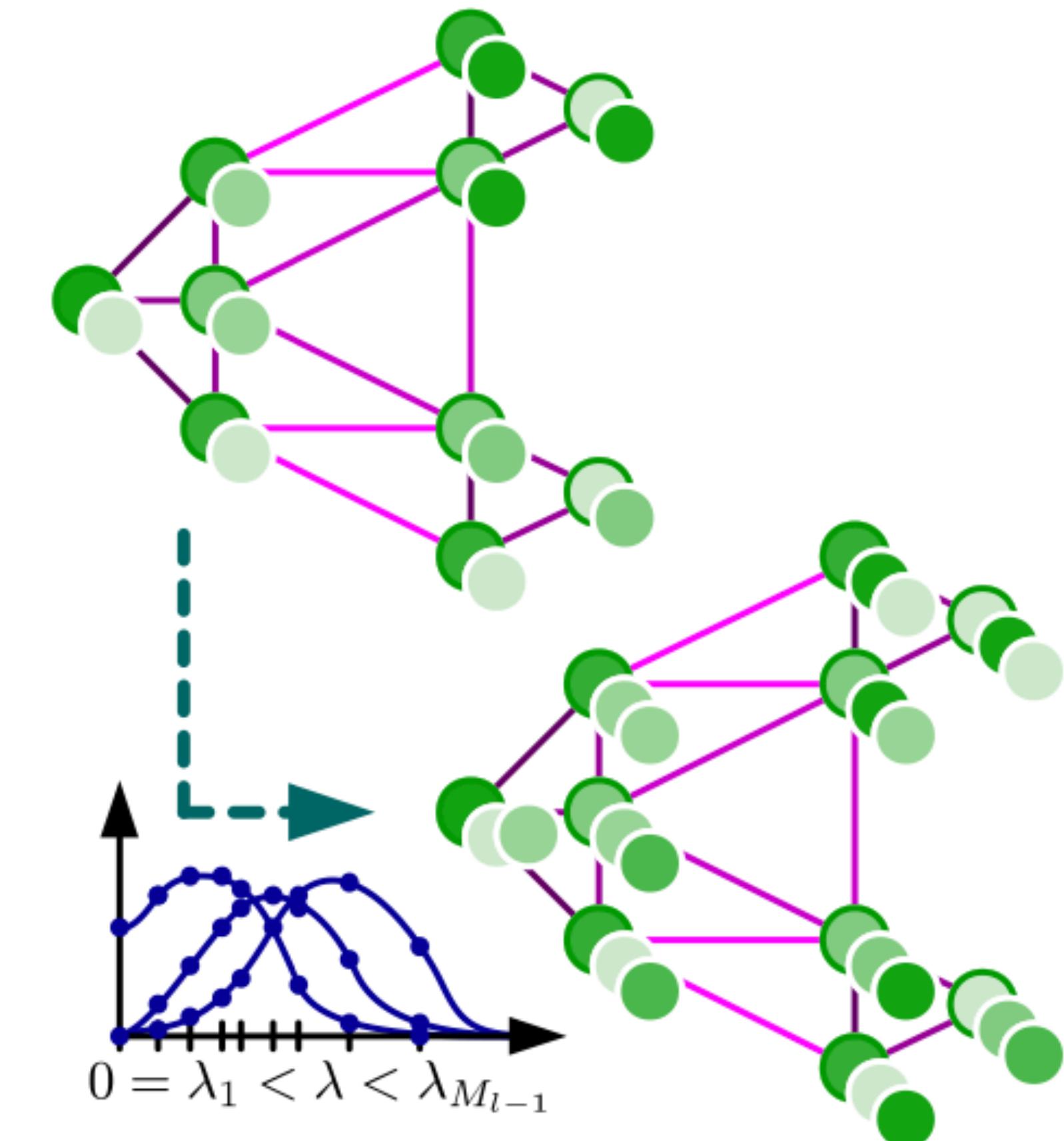
Pierre Vandergheynst

EPFL, Lausanne, Switzerland

{michael.defferrard,xavier.bresson,pierre.vandergheynst}@epfl.ch

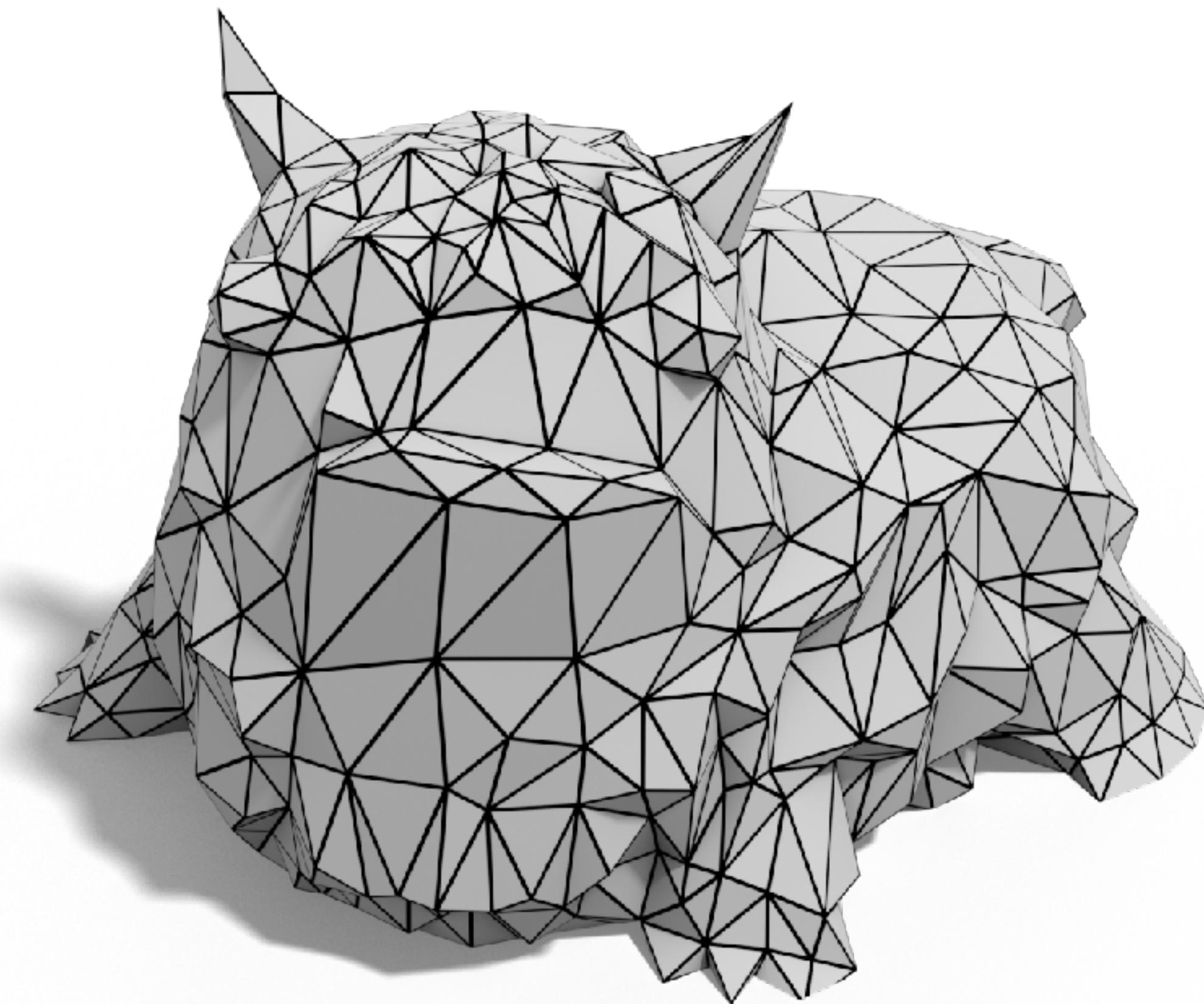
### Abstract

In this work, we are interested in generalizing convolutional neural networks (CNNs) from low-dimensional regular grids, where image, video and speech are represented, to high-dimensional irregular domains, such as social networks, brain connectomes or words' embedding, represented by graphs. We present a formulation of CNNs in the context of spectral graph theory, which provides the necessary mathematical background and efficient numerical schemes to design fast localized convolutional filters on graphs. Importantly, the proposed technique offers the same linear computational complexity and constant learning complexity as classical CNNs, while being universal to any graph structure. Experiments on MNIST and 20NEWS demonstrate the ability of this novel deep learning system to learn local, stationary, and compositional features on graphs.



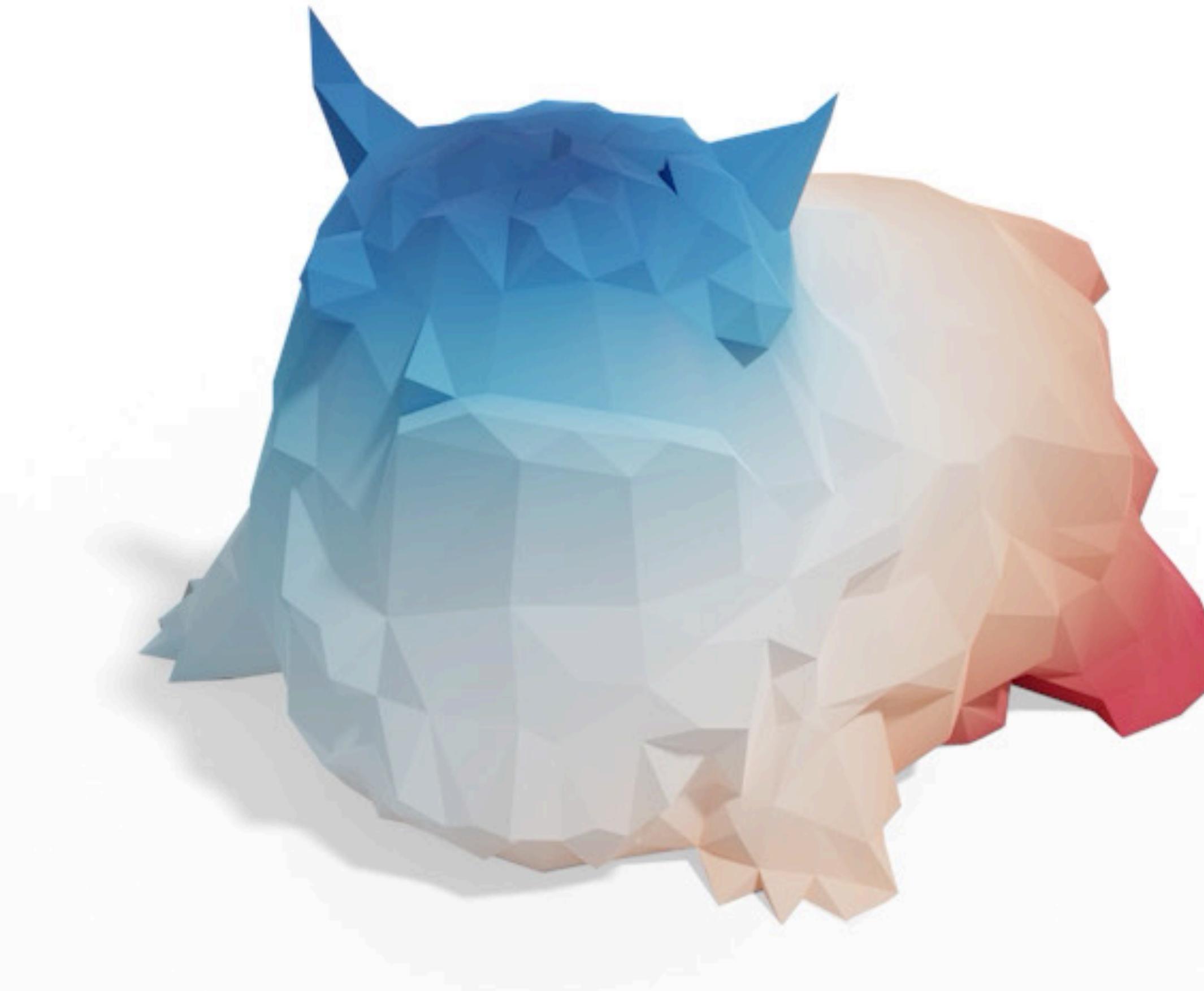
# Do not generalize to other shapes

(even the same shape with a different connectivity)



# Do not generalize to other shapes

(even the same shape with a different connectivity)



different Fourier bases

# Synchronizing Spectral Spaces

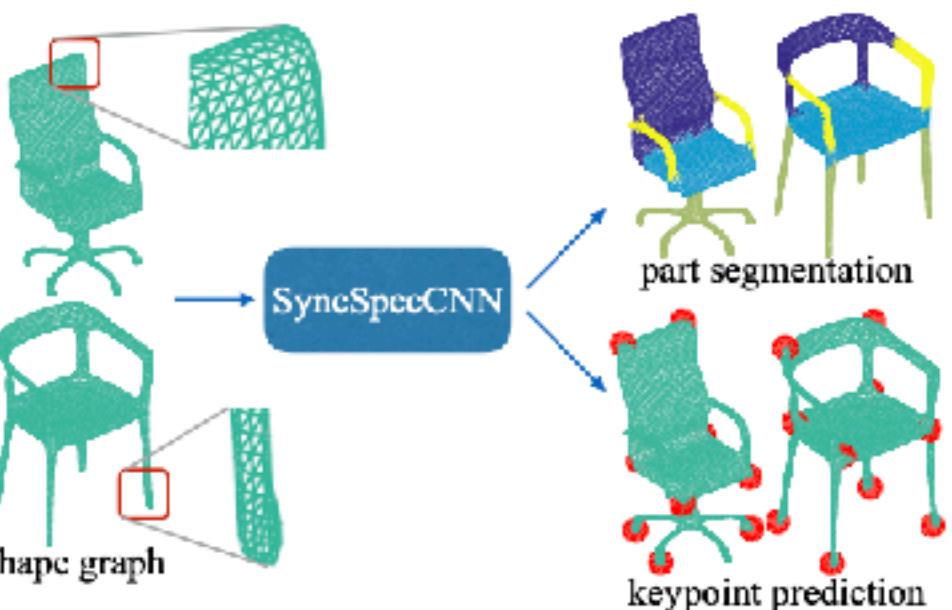
## SyncSpecCNN: Synchronized Spectral CNN for 3D Shape Segmentation

Li Yi<sup>1</sup> Hao Su<sup>1</sup> Xingwen Guo<sup>2</sup> Leonidas Guibas<sup>1</sup>

<sup>1</sup>Stanford University <sup>2</sup>The University of Hong Kong

### Abstract

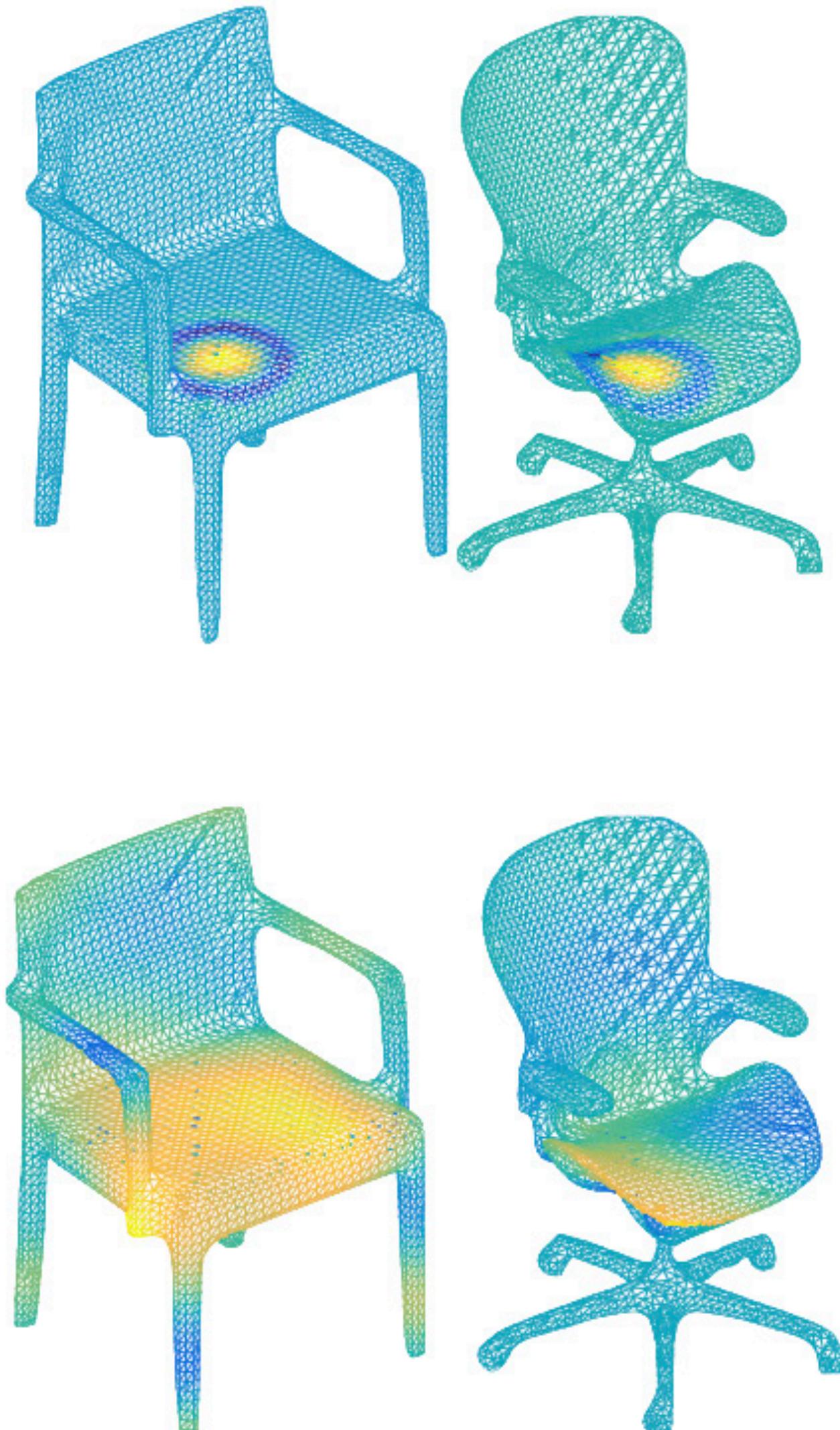
In this paper, we study the problem of semantic annotation on 3D models that are represented as shape graphs. A functional view is taken to represent localized information on graphs, so that annotations such as part segment or keypoint are nothing but 0-1 indicator vertex functions. Compared with images that are 2D grids, shape graphs are irregular and nonisomorphic data structures. To enable the prediction of vertex functions on them by convolutional neural networks, we resort to spectral CNN method that enables weight sharing by parameterizing kernels in the spectral domain spanned by graph laplacian eigenbases. Under this setting, our network, named SyncSpecCNN, strive to overcome two key challenges: how to share coefficients and conduct multi-scale analysis in different parts of the graph for a single shape, and how to share information across related but different shapes that may be represented by very different graphs. Towards these goals, we introduce a spectral parameterization of dilated convolutional kernels and a spectral transformer network. Experimentally we tested our SyncSpecCNN on various tasks, including 3D shape part segmentation and 3D keypoint prediction. State-of-the-art performance has been achieved on all benchmark datasets.



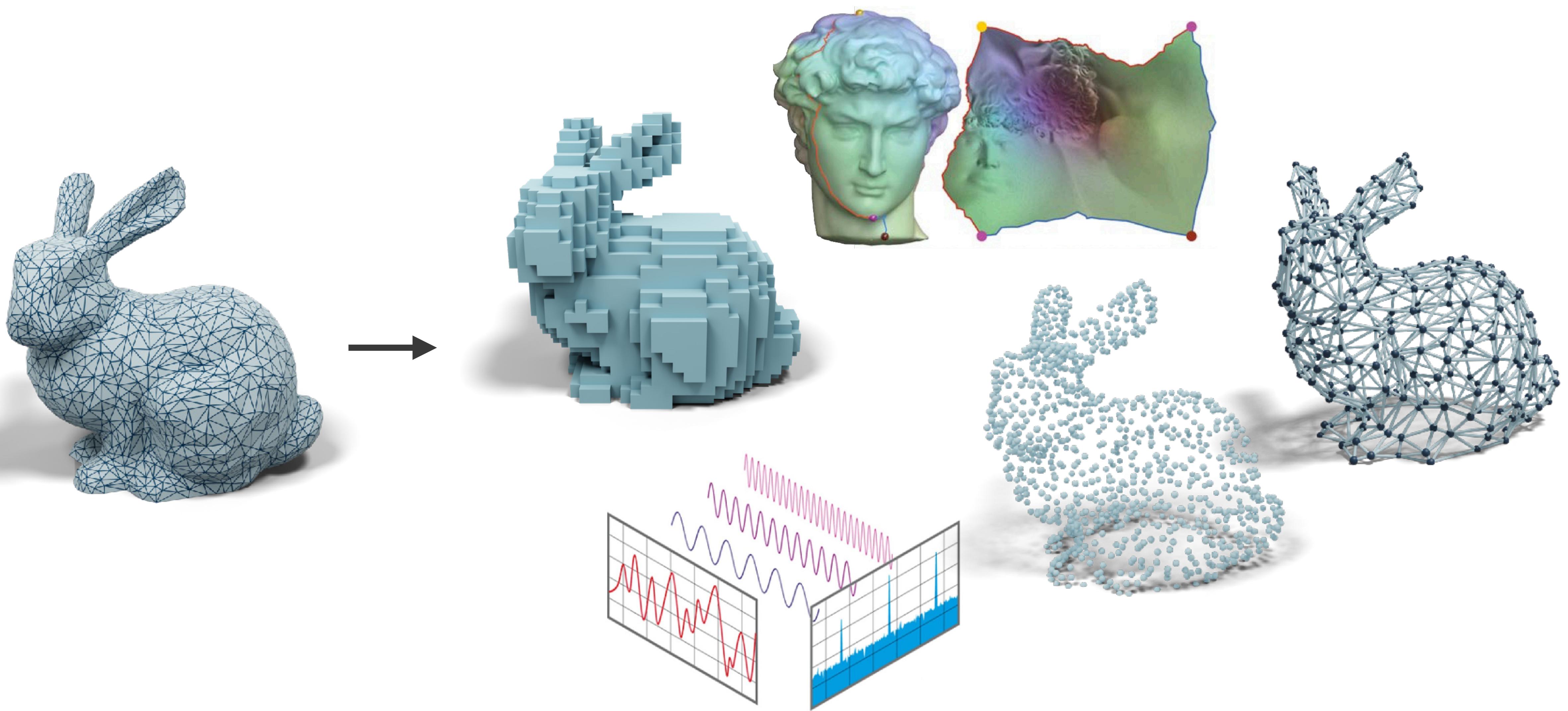
**Figure 1.** Our SyncSpecCNN takes a shape graph equipped with vertex functions (i.e. spatial coordinate function) as input and predicts a per-vertex label. The framework is general and not limited to a specific type of output. We show 3D part segmentation and 3D keypoint prediction as example outputs here.

It is not straightforward to apply traditional deep learning approaches to 3D models because a mesh representation can be combinatorially irregular and does not permit the optimizations exploited by convolutional approaches, such as weight sharing, which depend on regular grid structures. In this paper we take a functional approach to represent information about shapes, starting with the observation that a shape part is itself nothing but a 0-1 indicator function defined on the shape.

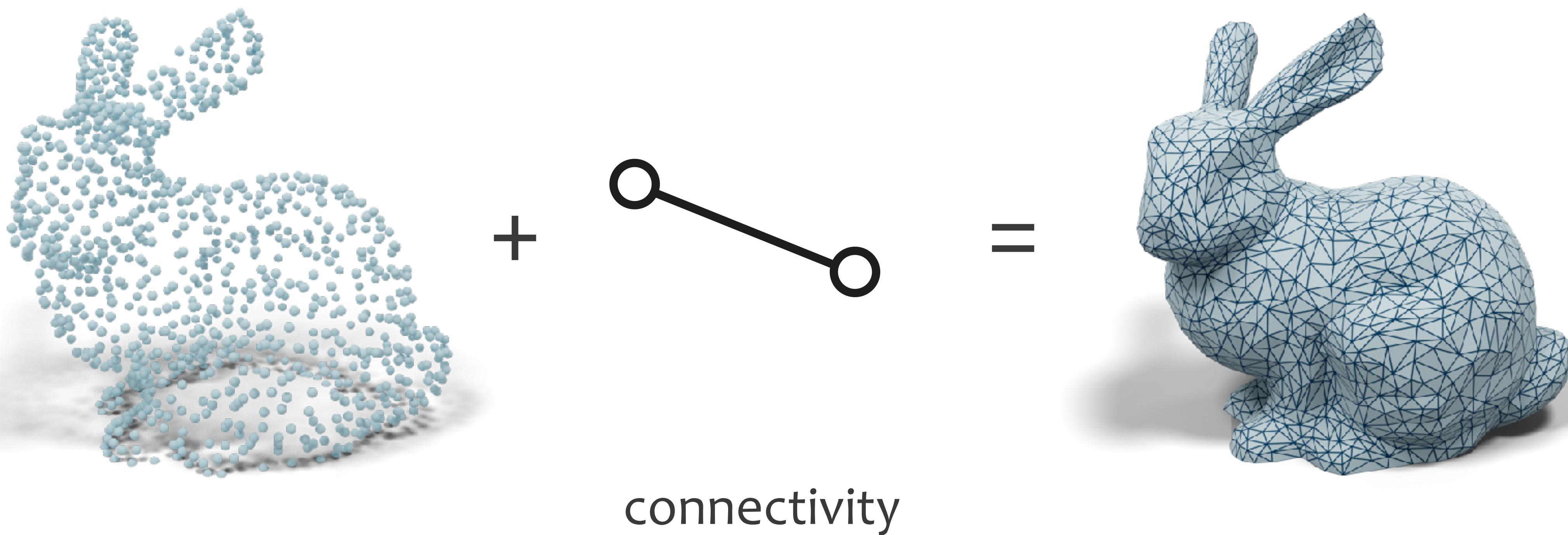
Our basic problem is to learn functions on shapes. We start with example functions provided on a given shape



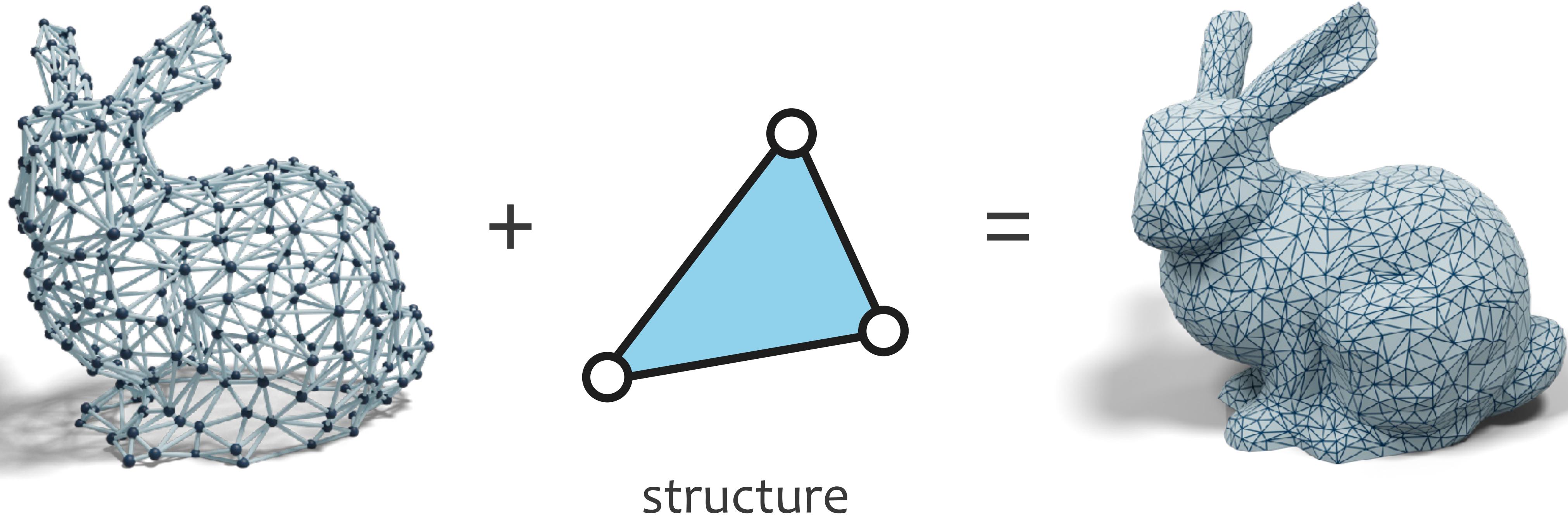
# Different representations



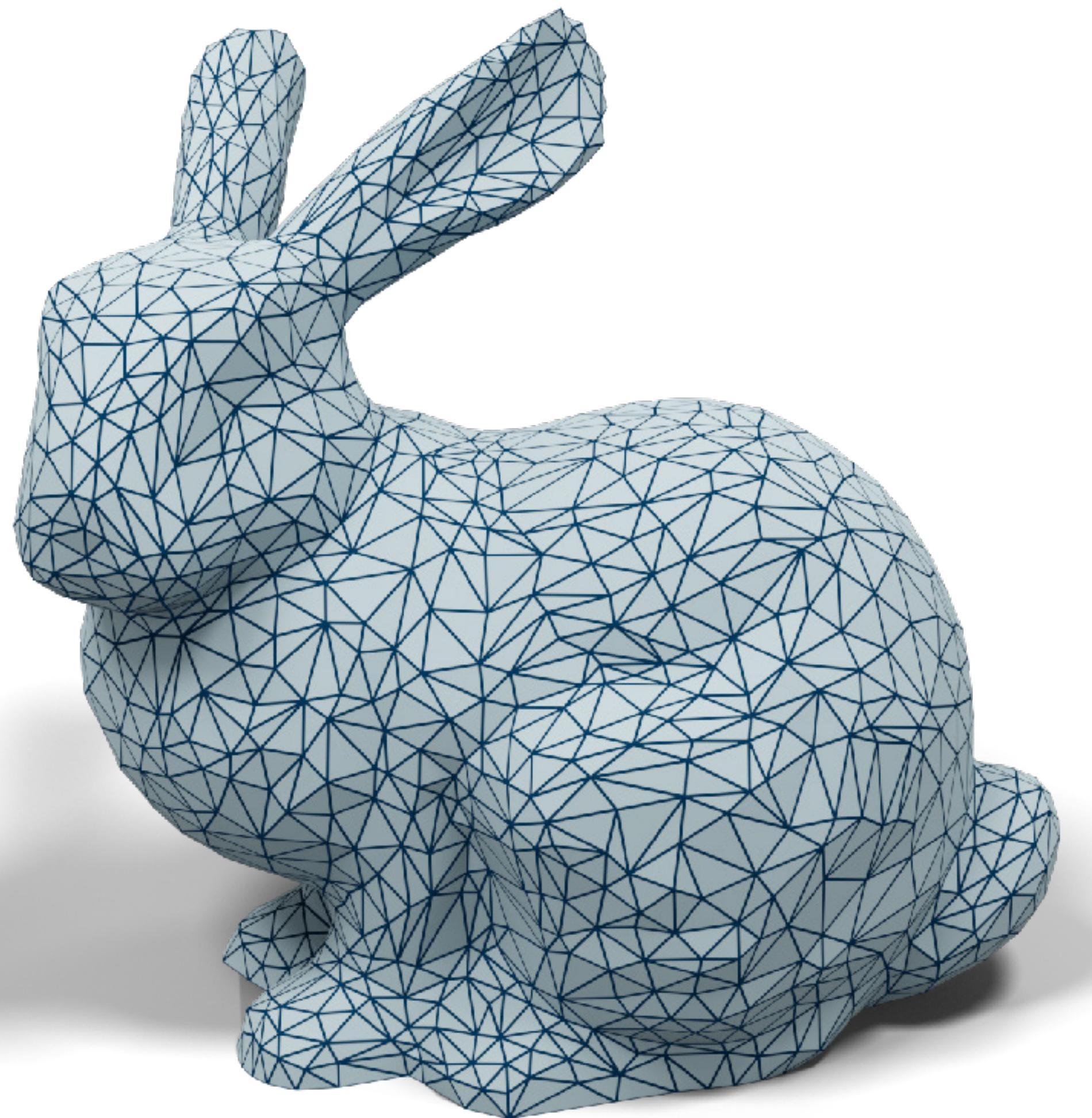
# Why not point cloud convolution?



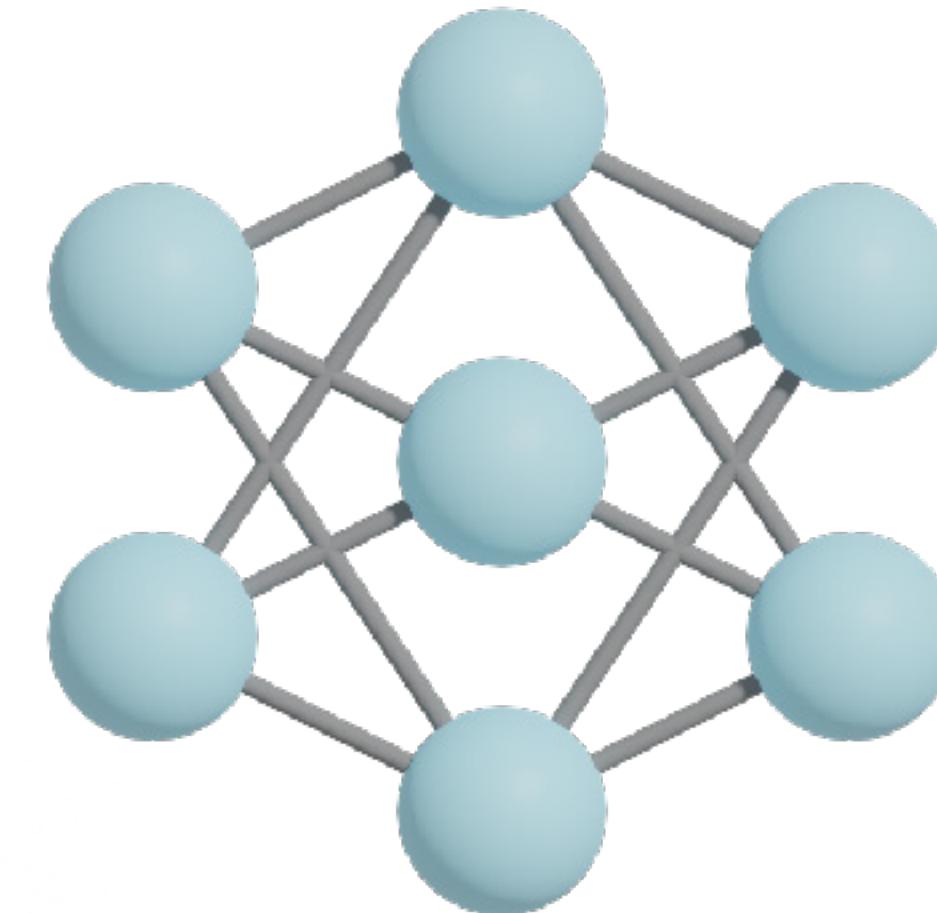
# Why not graph convolution?



# Surface Meshes



# Neural Networks on Meshes



## Example Outputs

Global shape descriptor

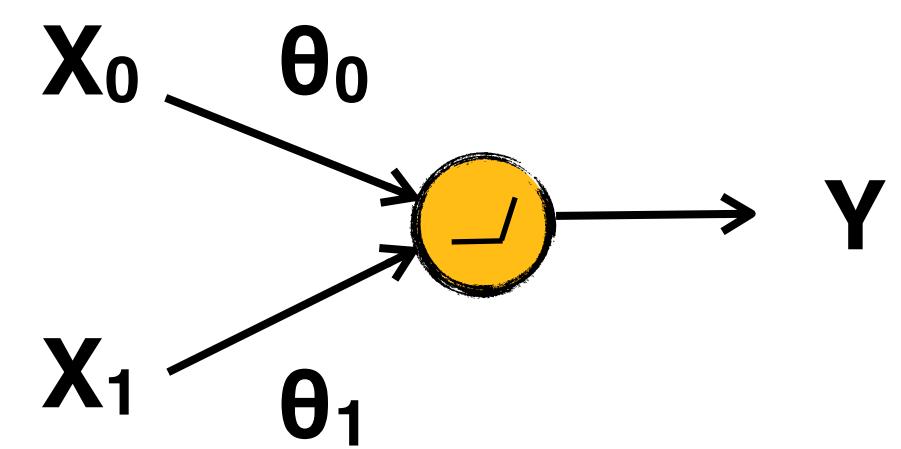
Probability to collapse an edge

Displacement per vertex

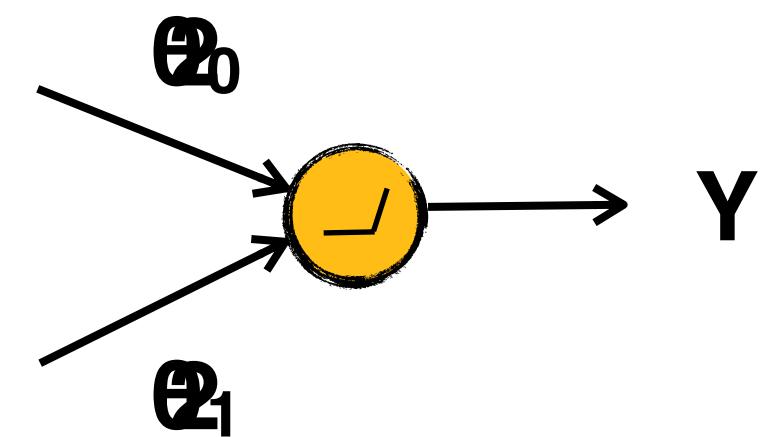
Segmentation label per-face

:

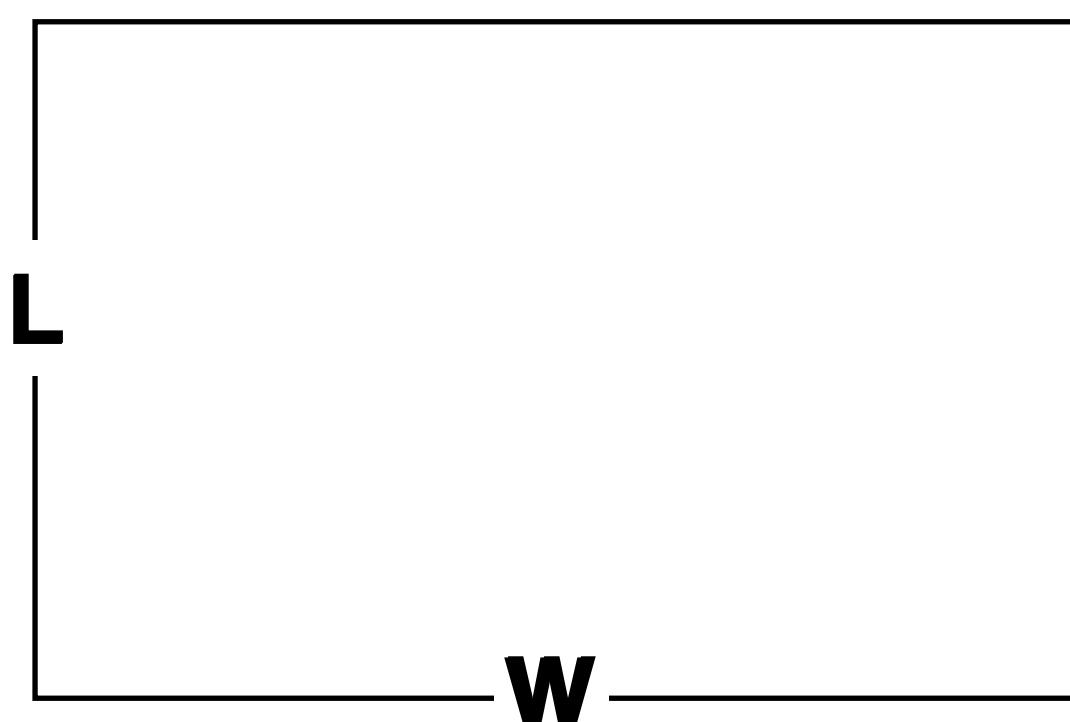
# Neuron



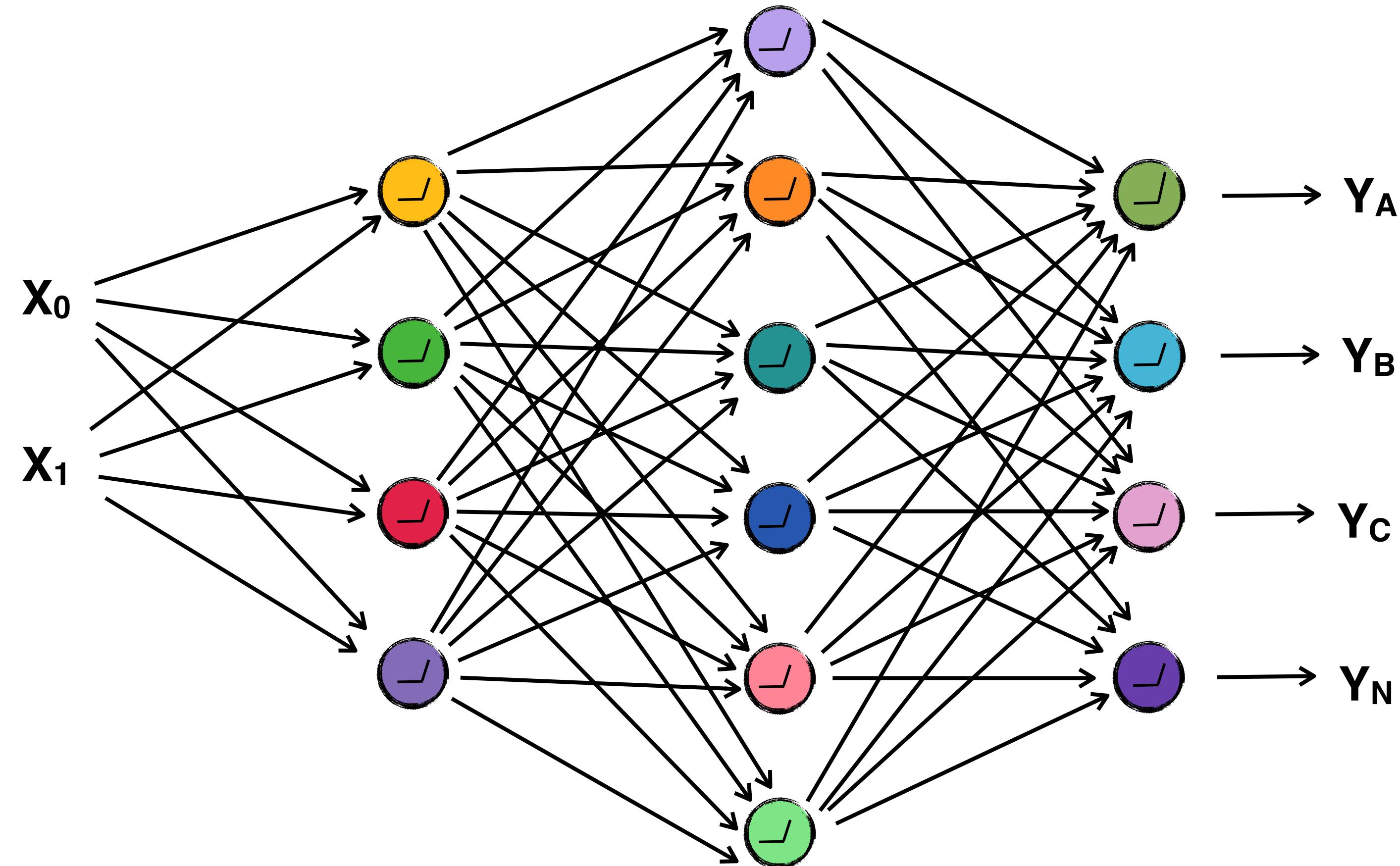
# Neuron



$$Y = \text{ReLU}(2 \times L + 2 \times W)$$

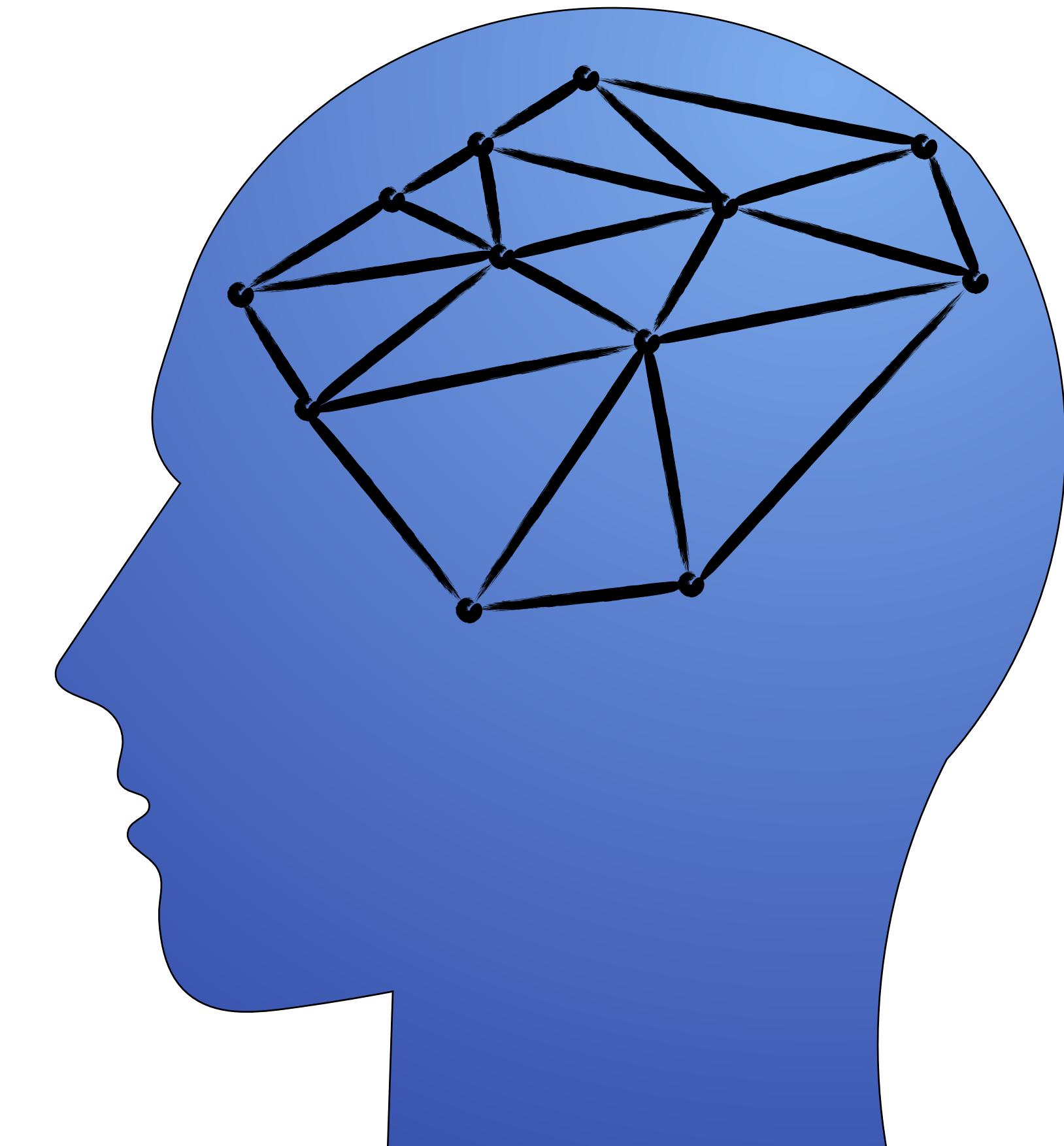


# Fully-connected



# Inductive Bias

The set of assumptions that we encode into our network, which make it better suited for the task

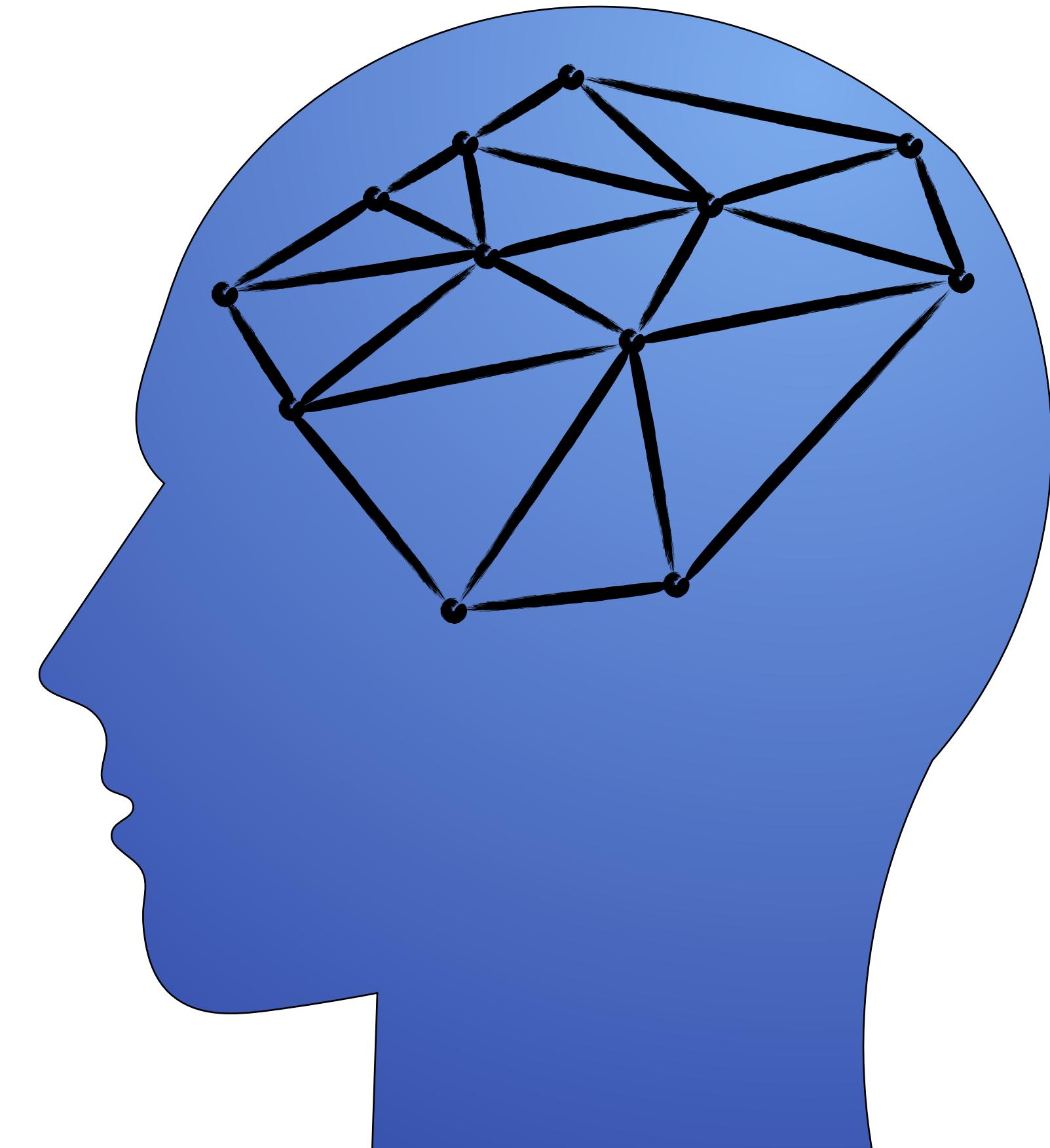


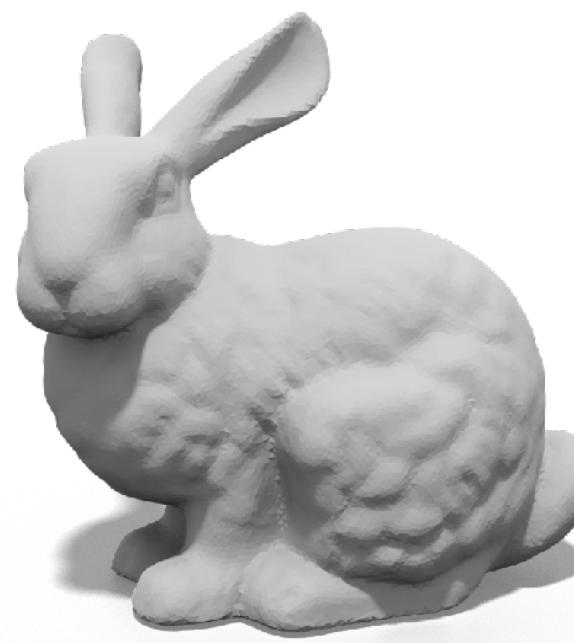
Good

## Inductive Bias

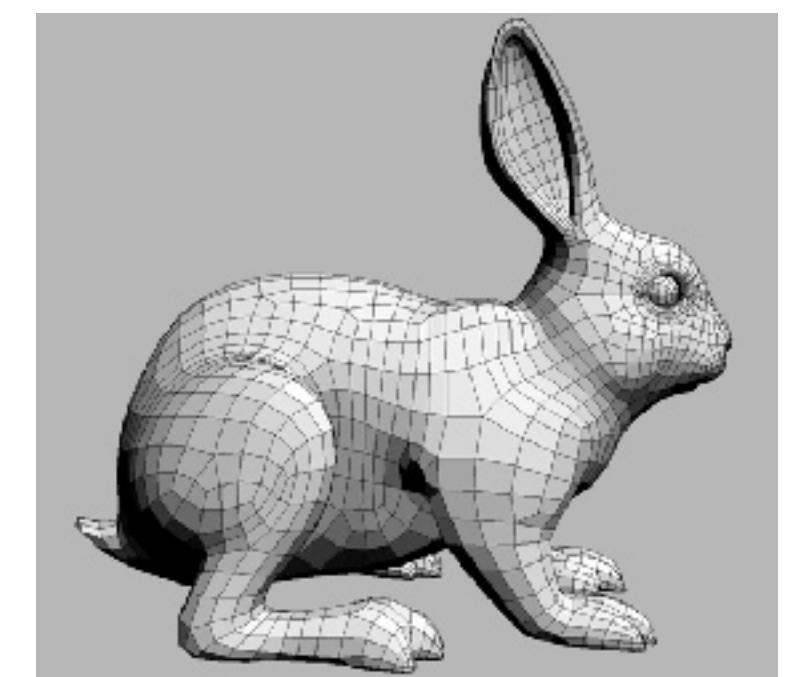


Robust to irrelevant  
variations of the input





$\approx$

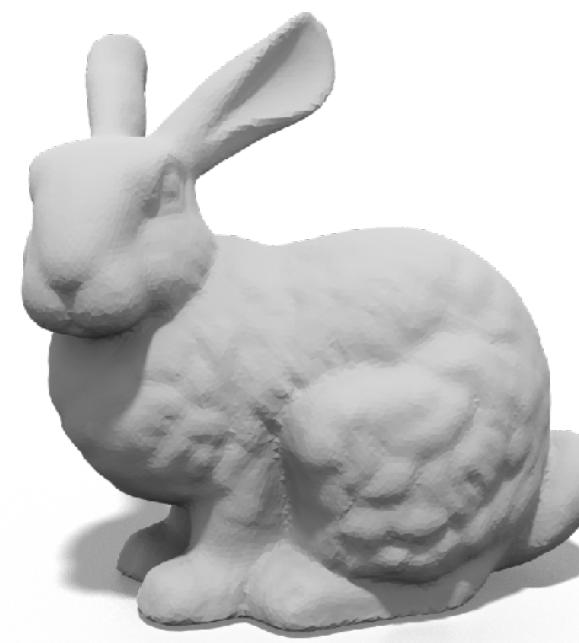


$\neq$

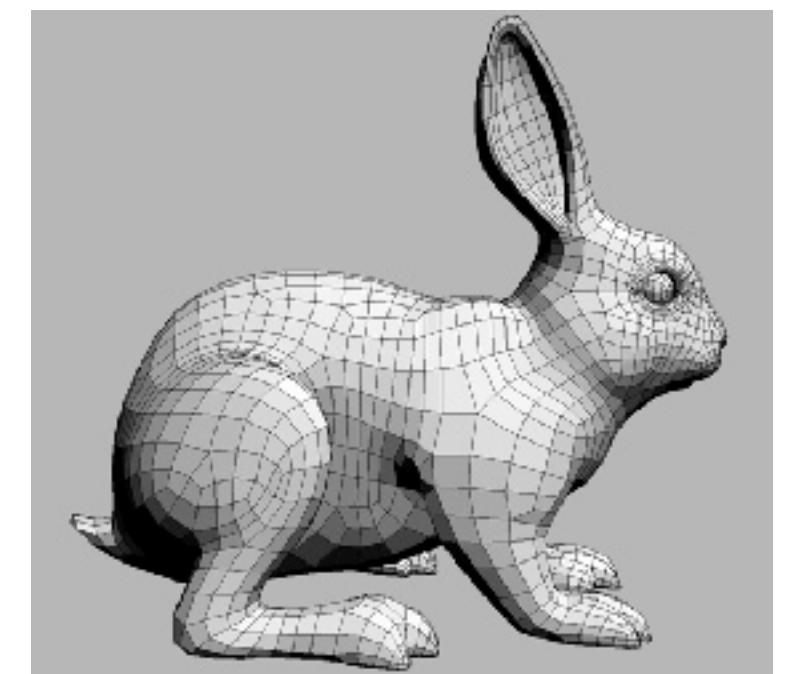


**Local tasks**

**Global tasks**



$\approx$

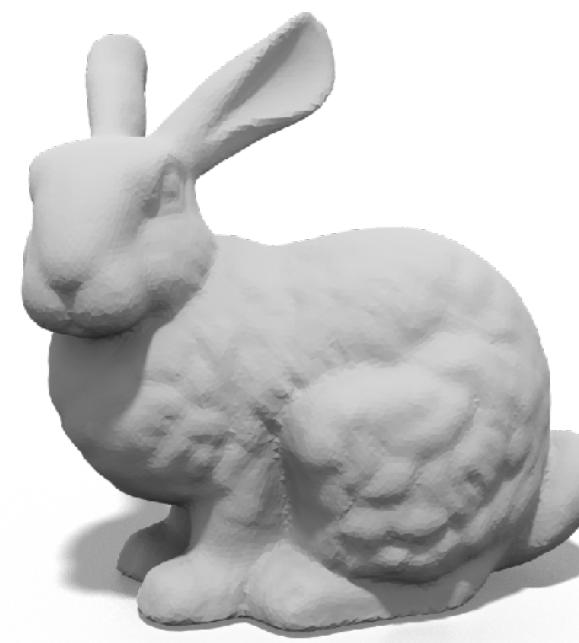


$\neq$

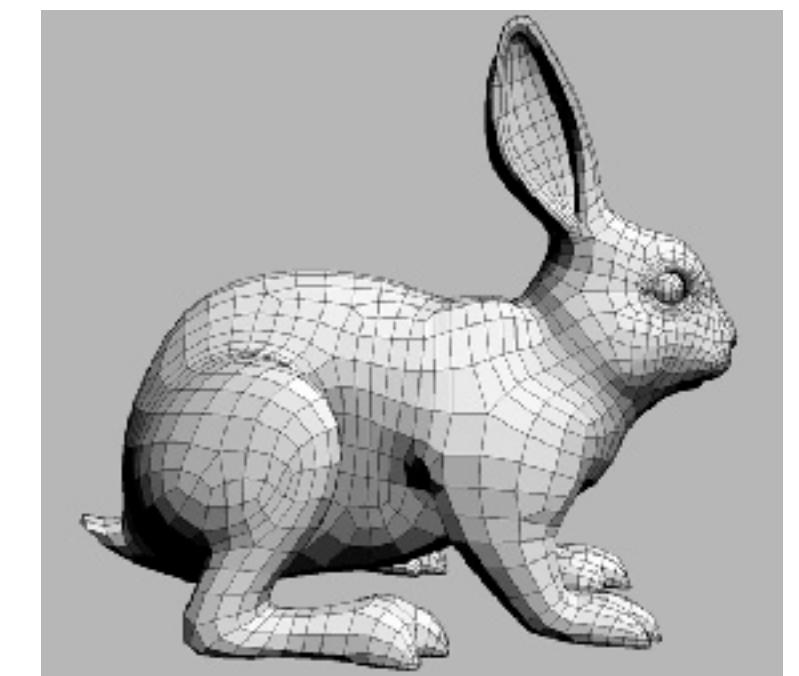


**Local tasks**

**Global tasks**



$\approx$



$\neq$

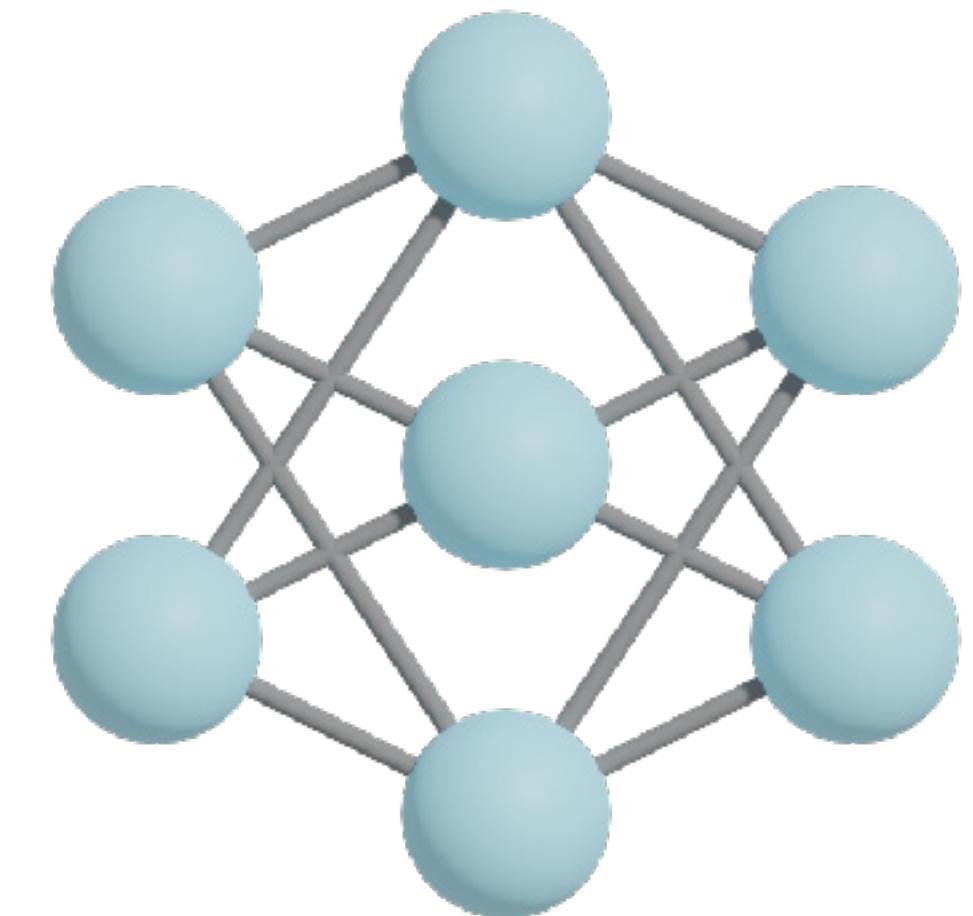


**Local tasks**

**Global tasks**

# Local task

**predict values per mesh element**

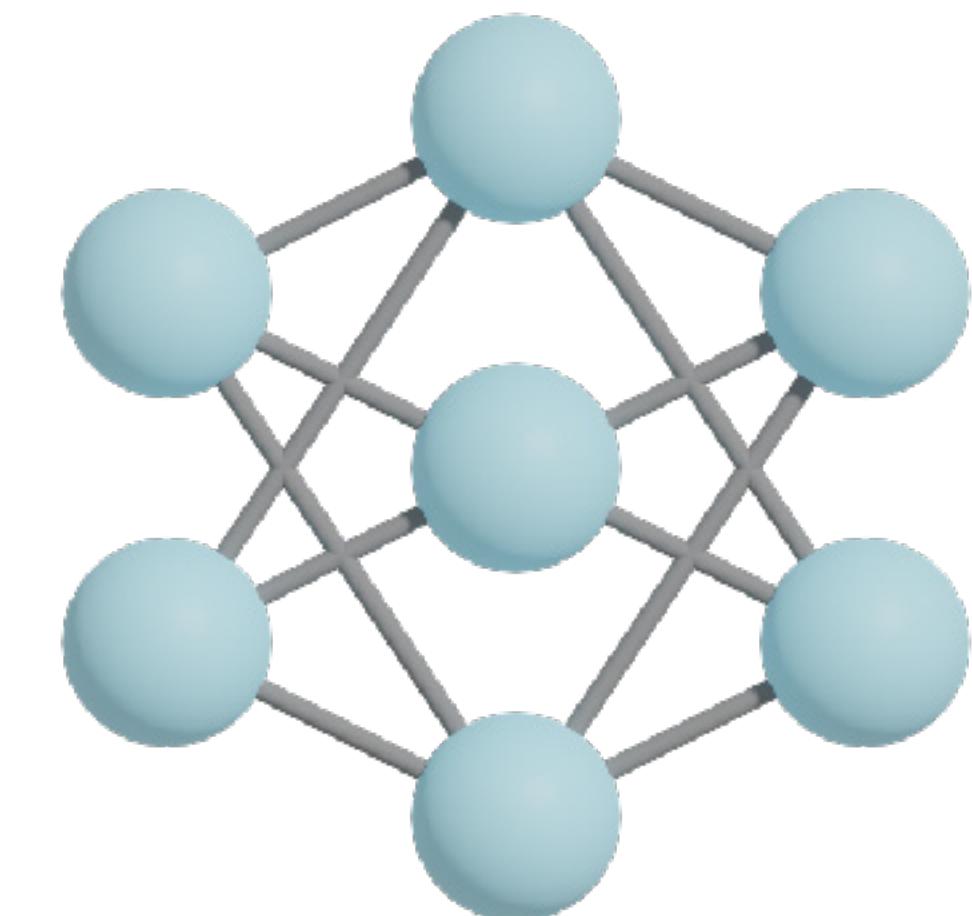


# Local task

**predict values per mesh element**

**Faces**

$f_0$   
 $f_1$   
 $f_2$   
 $f_3$   
 $f_4$   
⋮  
 $f_N$



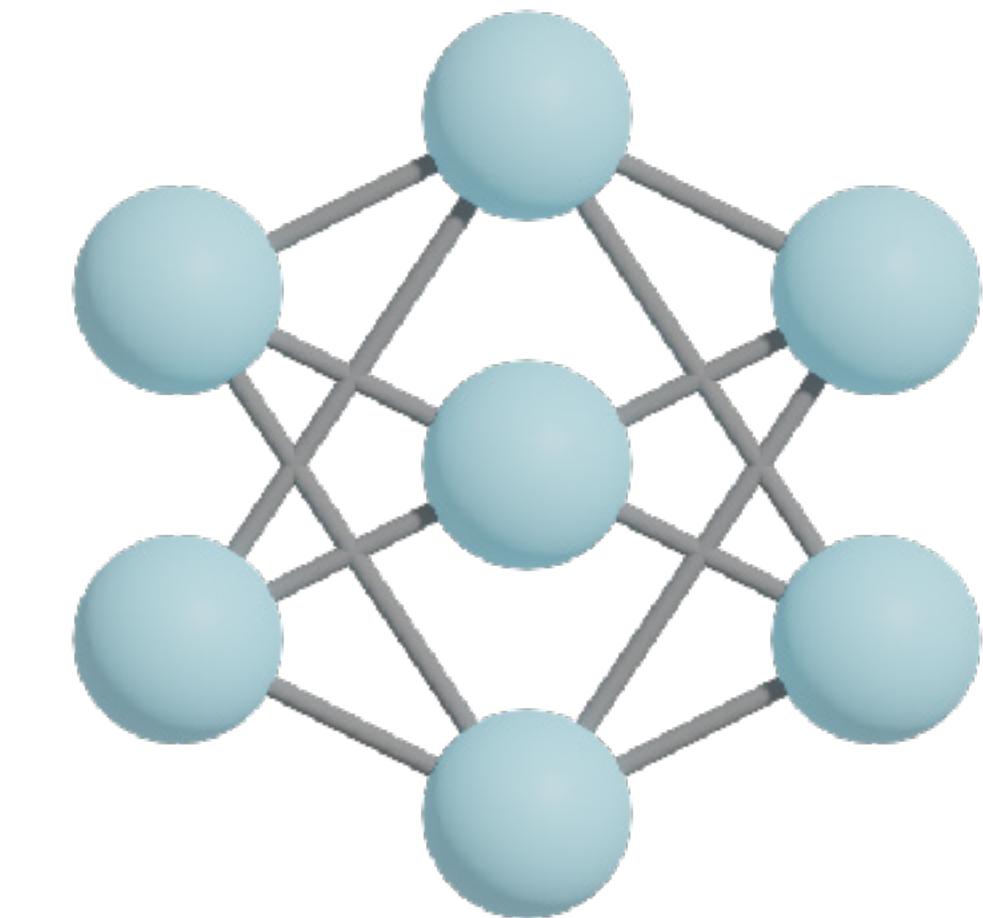
seat  
legs  
back  
seat  
legs  
⋮  
seat

# Local task

**predict values per mesh element**

**Faces**

$f_0$   
 $f_1$   
 $f_2$   
 $f_3$   
 $f_4$   
⋮  
 $f_N$

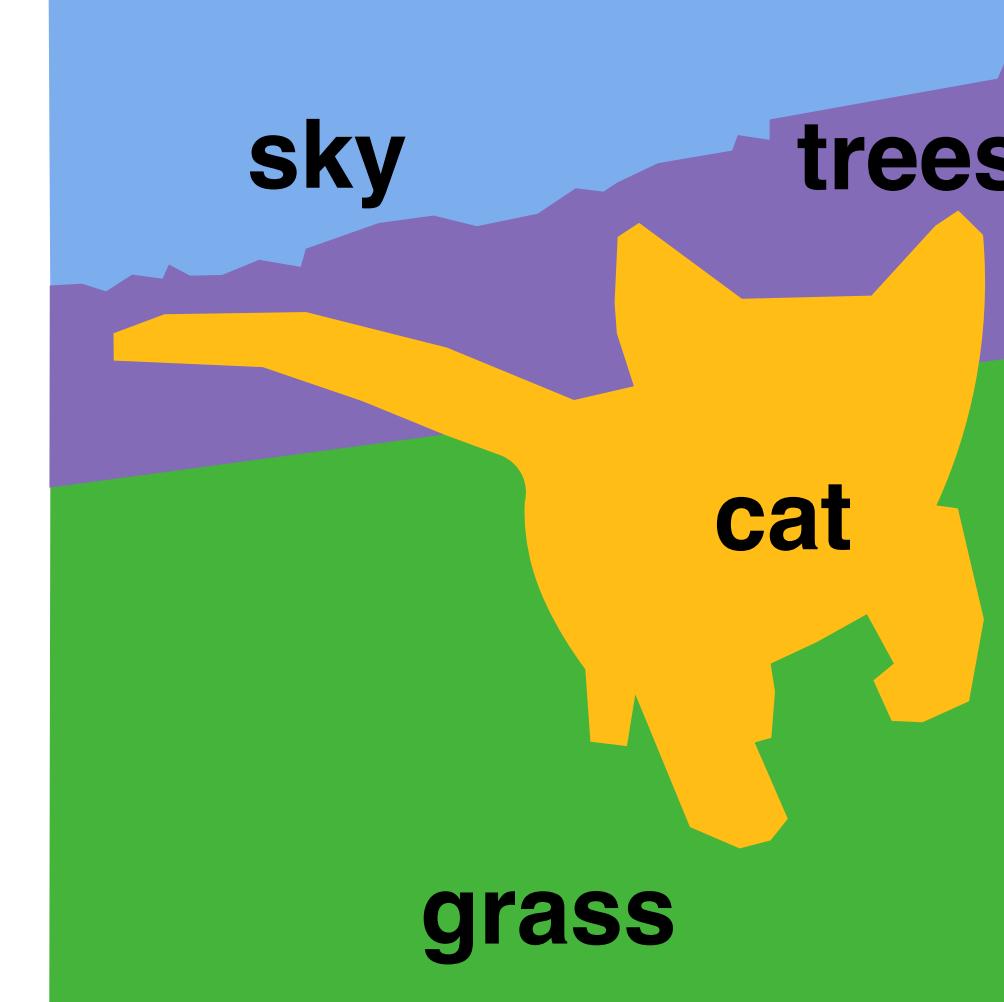
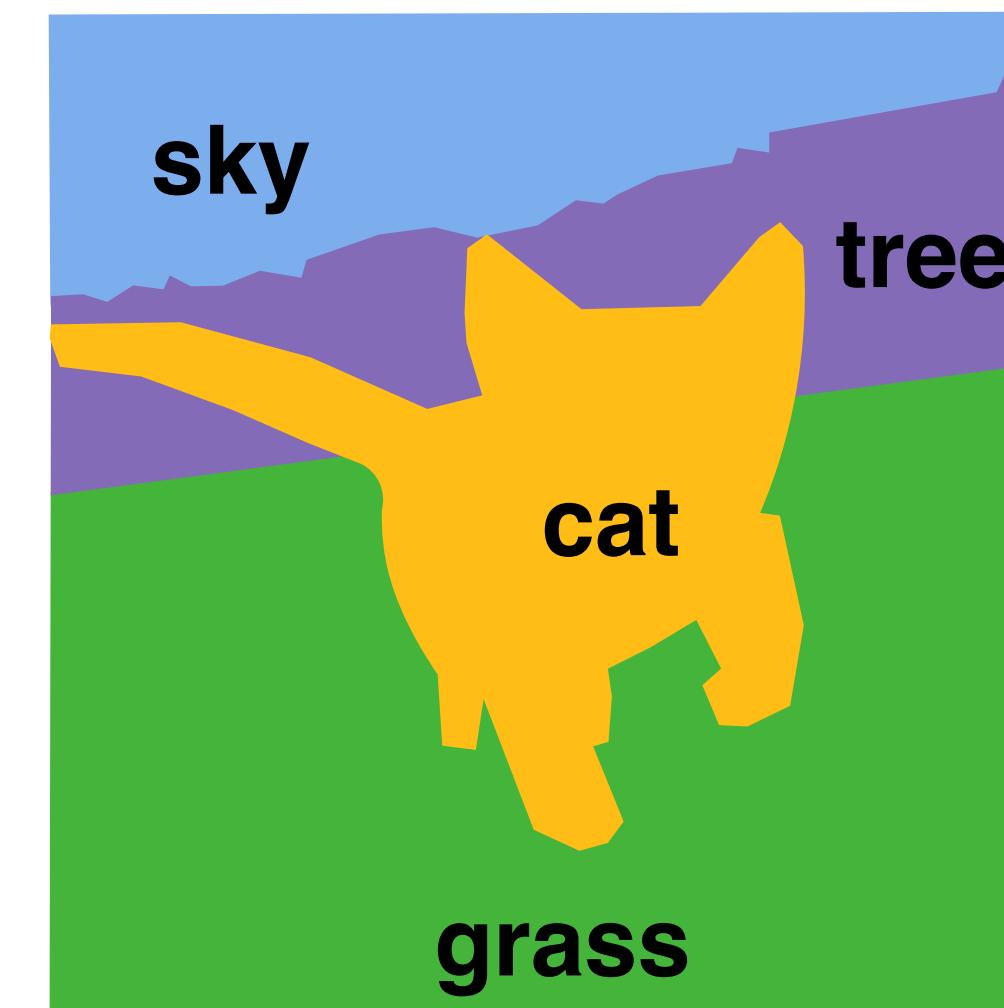


seat  
legs  
back  
seat  
legs  
⋮  
seat

**Fully connected network not suitable for this task**

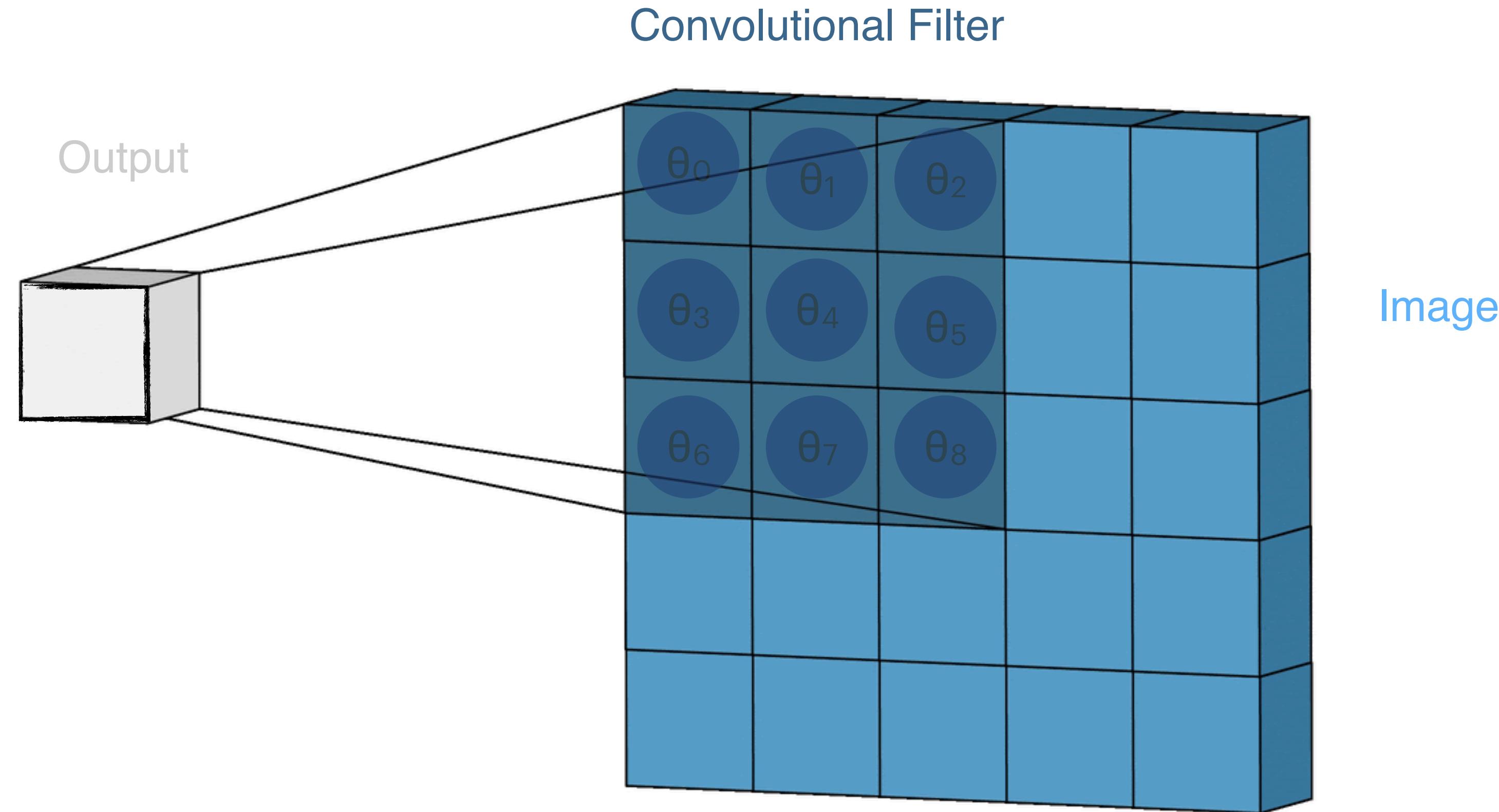
# Inspiration: image segmentation

Shared weights are a good inductive bias

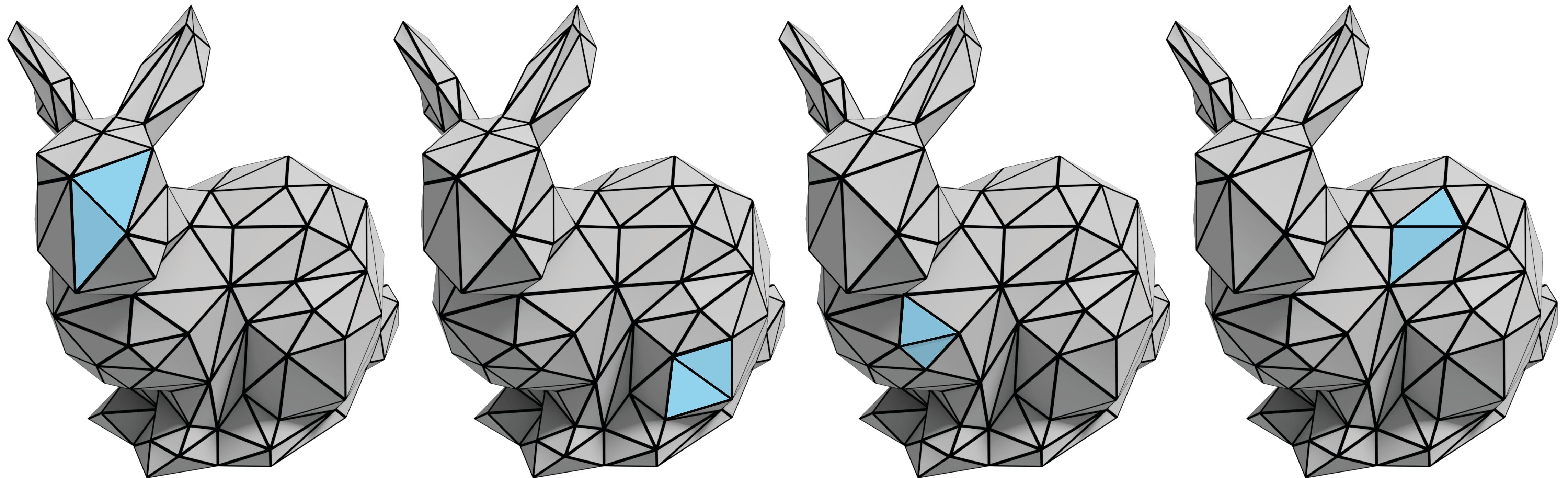


# Convolution

## Shared-weights

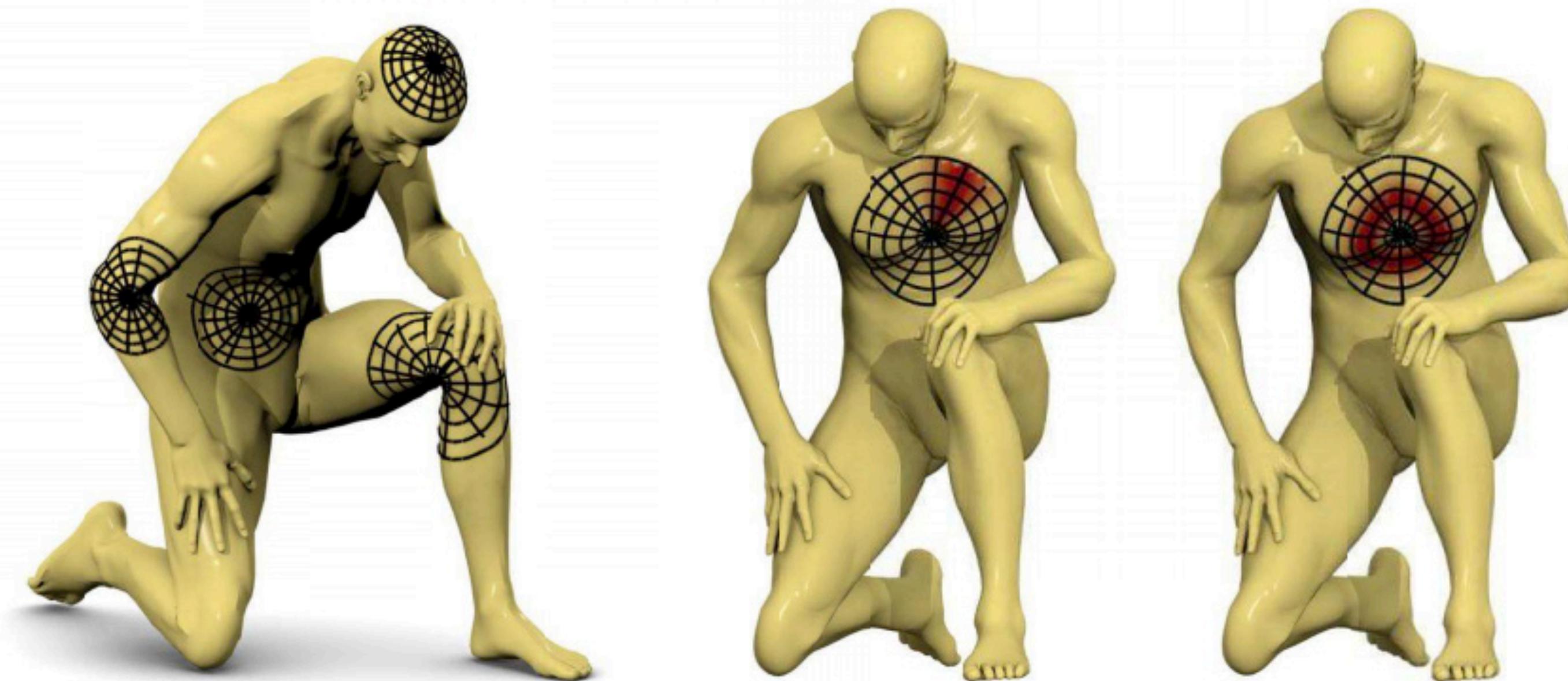


# Convolutions on meshes

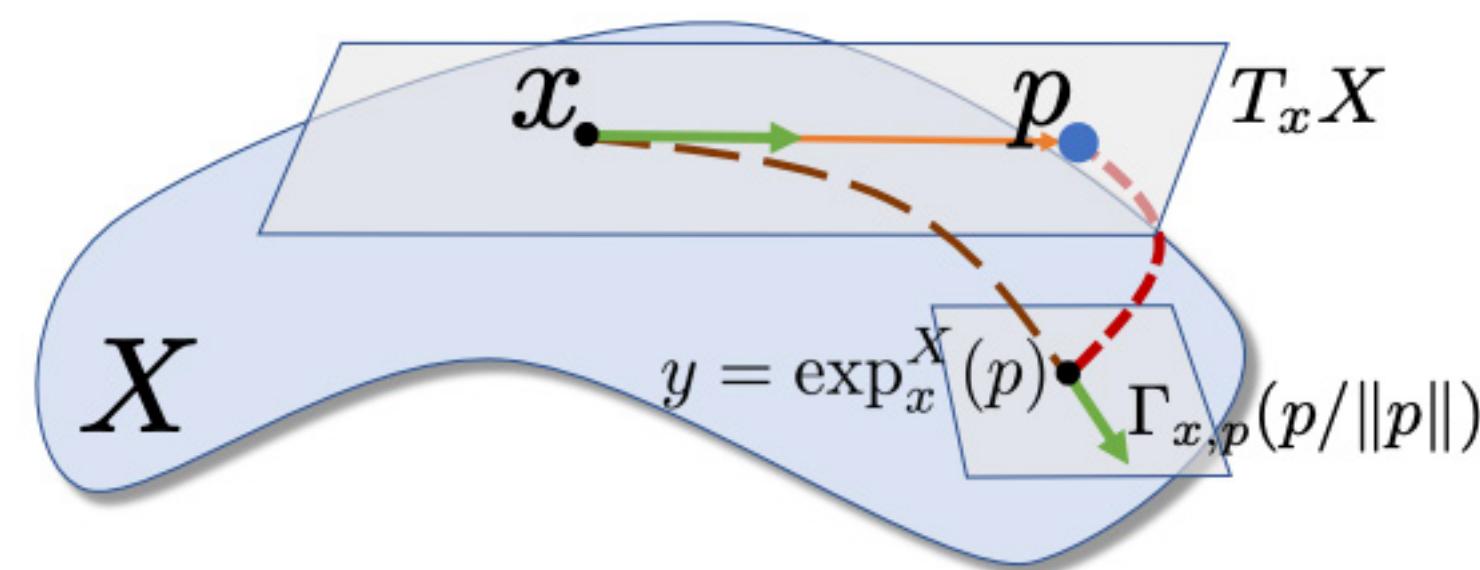


# Learn over intrinsic patches

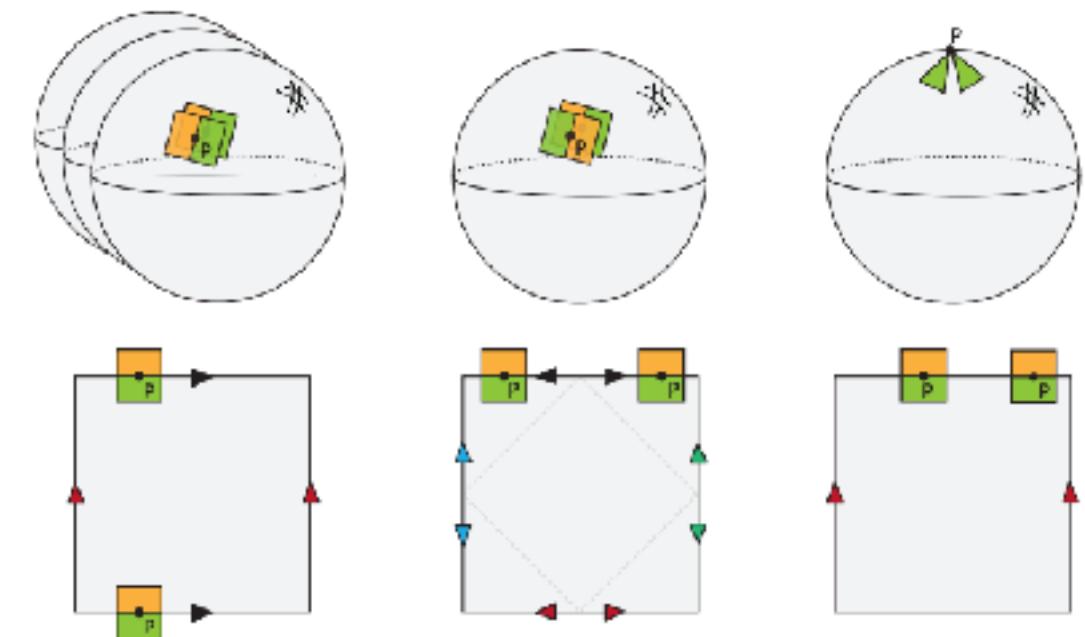
local parameterizations



# Intrinsic Techniques



MDGCNN. Poulenard & Ovsjanikov [SIGGRAPH Asia 2018]

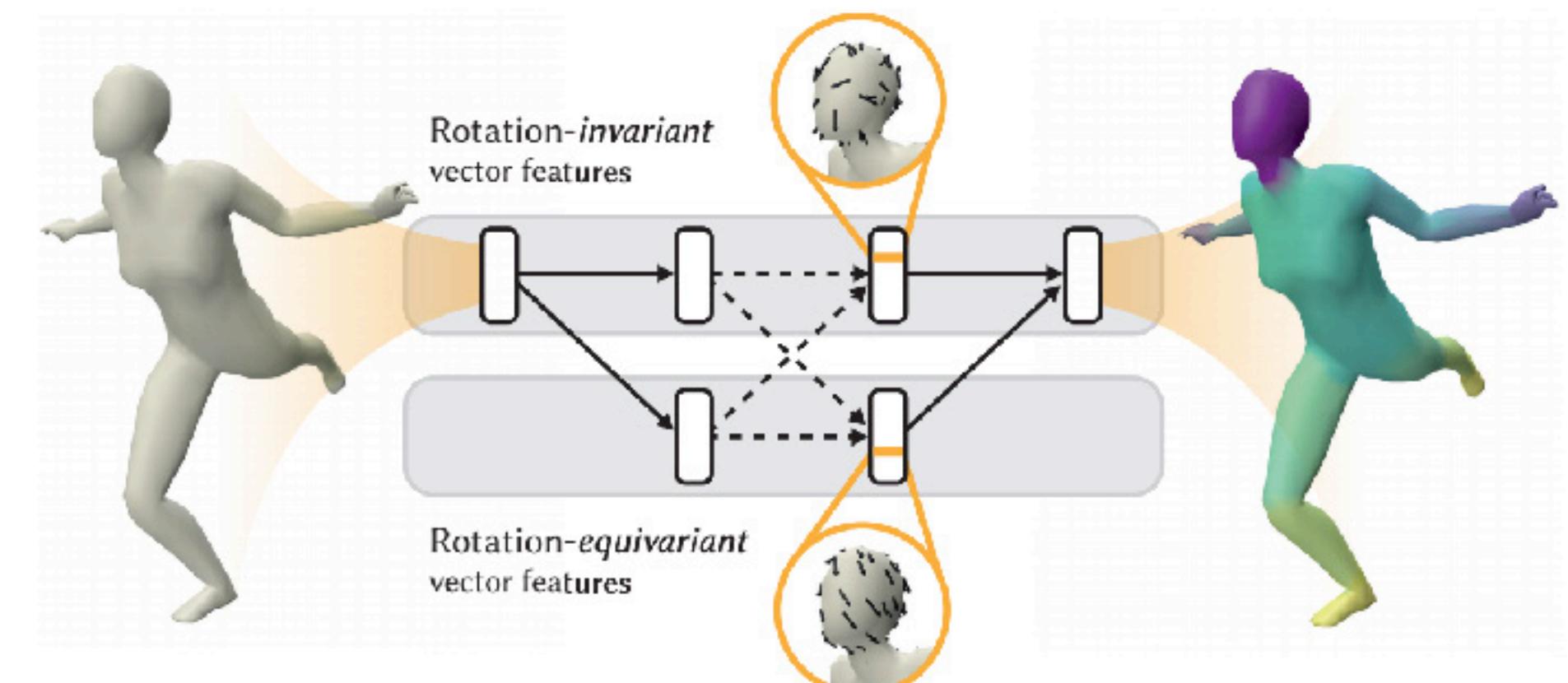


Surface Networks via General Covers. Haim et. al [ICCV 2019]

Toric Covers. Maron et. al [SIGGRAPH 2017]

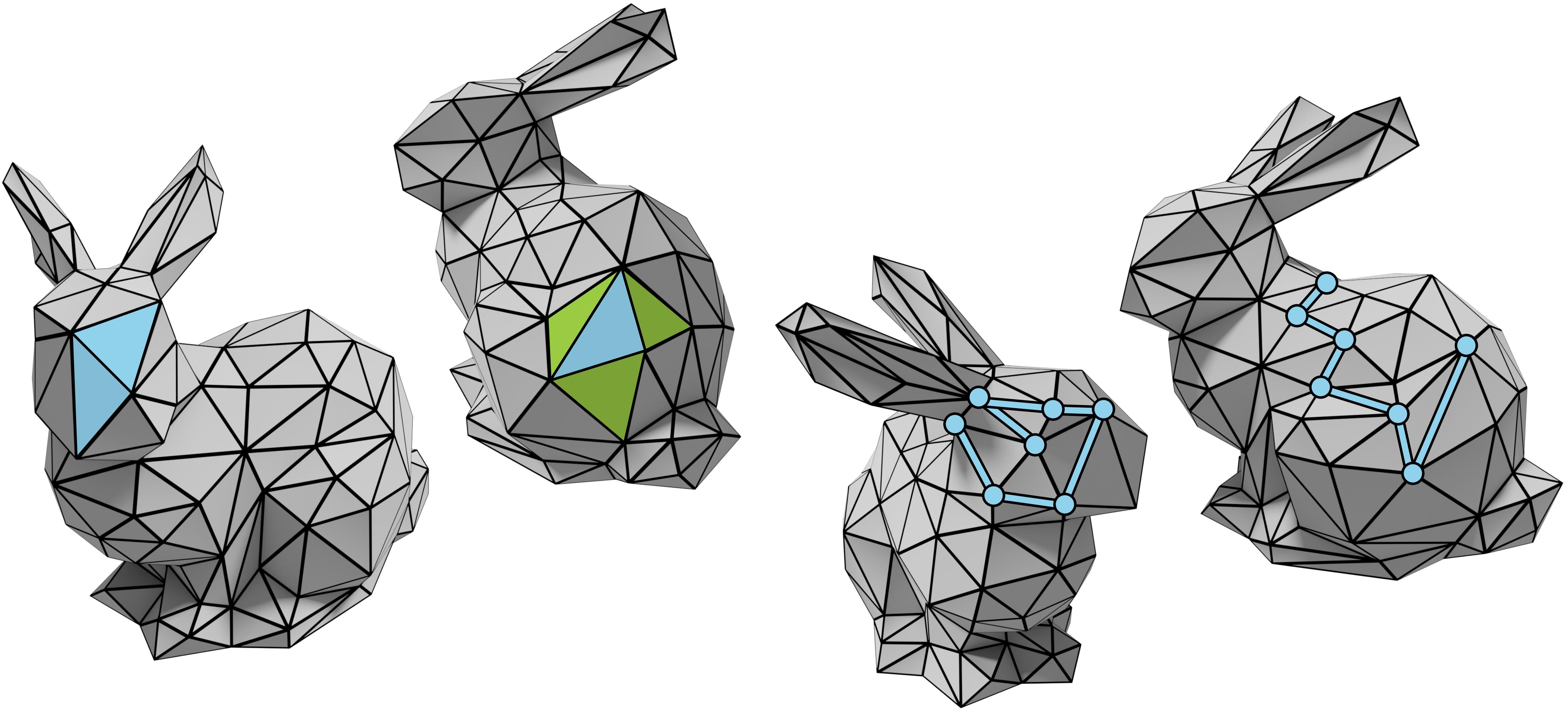


HodgeNet. Smirnov & Solomon [SIGGRAPH 2021]



CNNs on Surfaces. Wiersma & Eisemann [SIGGRAPH 2020]

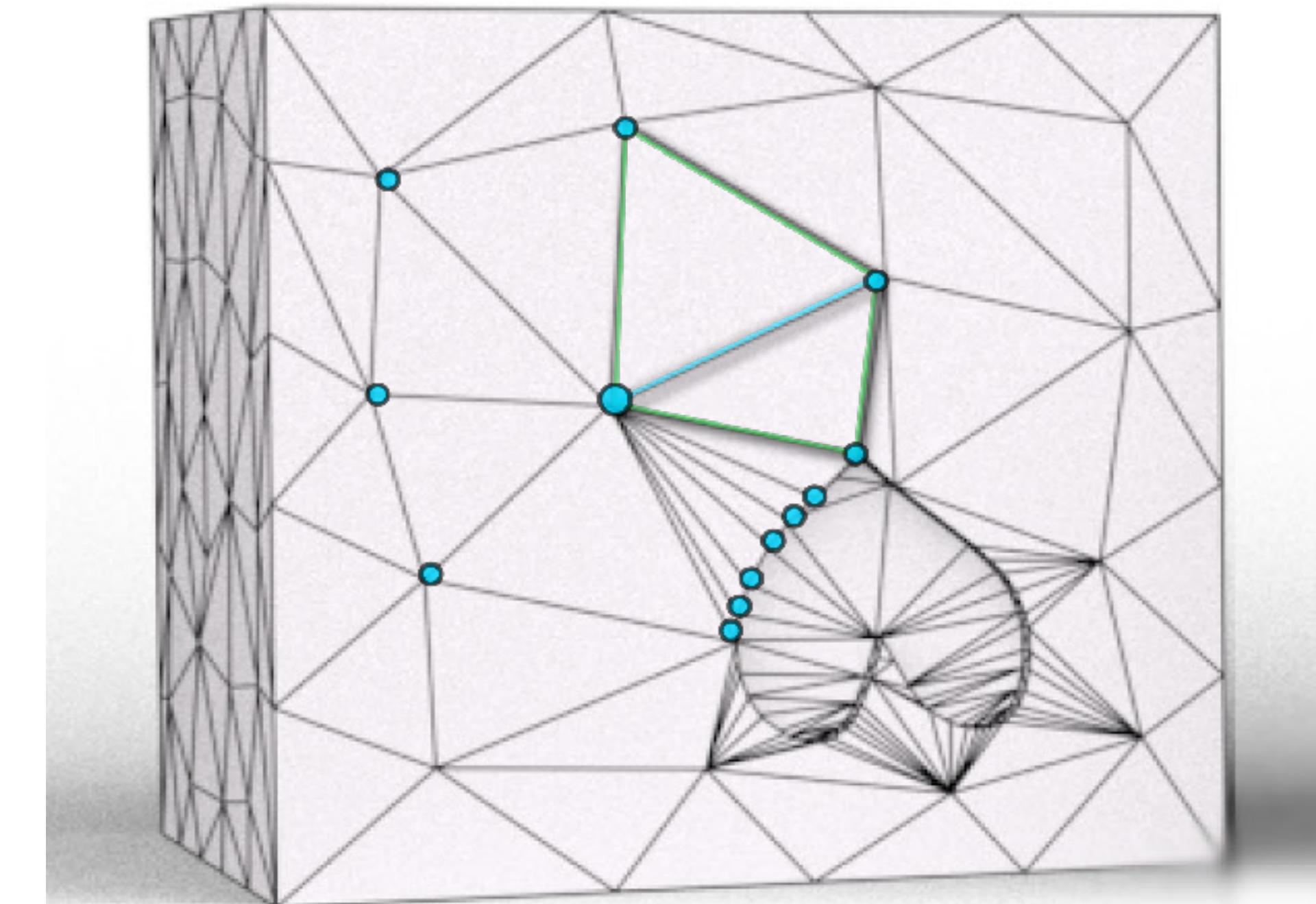
# Convolutions on meshes



# Fixed size neighborhood



**Mesh edges have  
4 edge-neighbors**

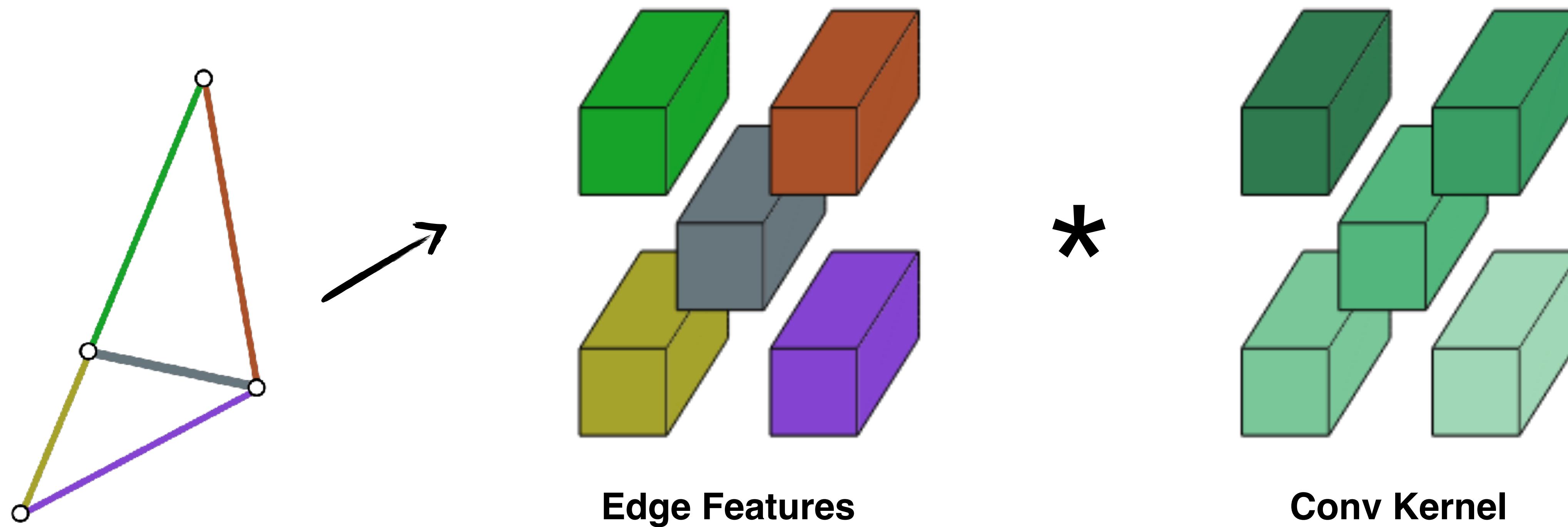


**Vertices**  
 $\langle x, y, z \rangle$

**Edges**  
 $\langle v_i, v_j \rangle$

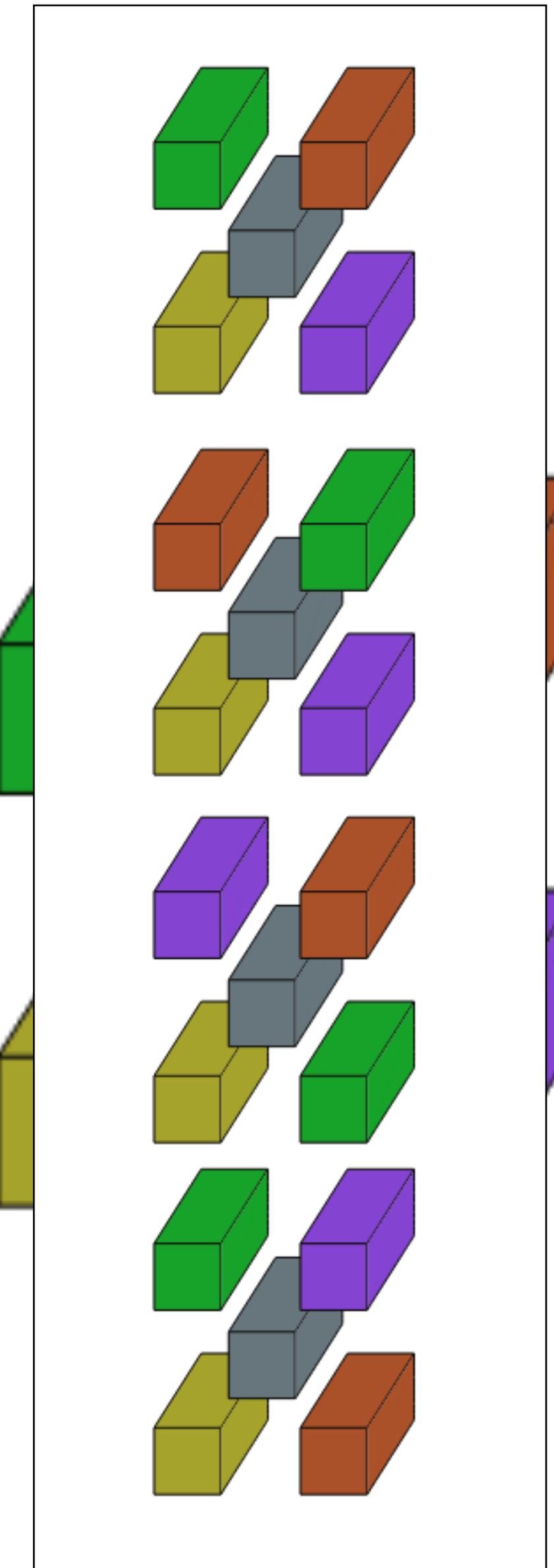
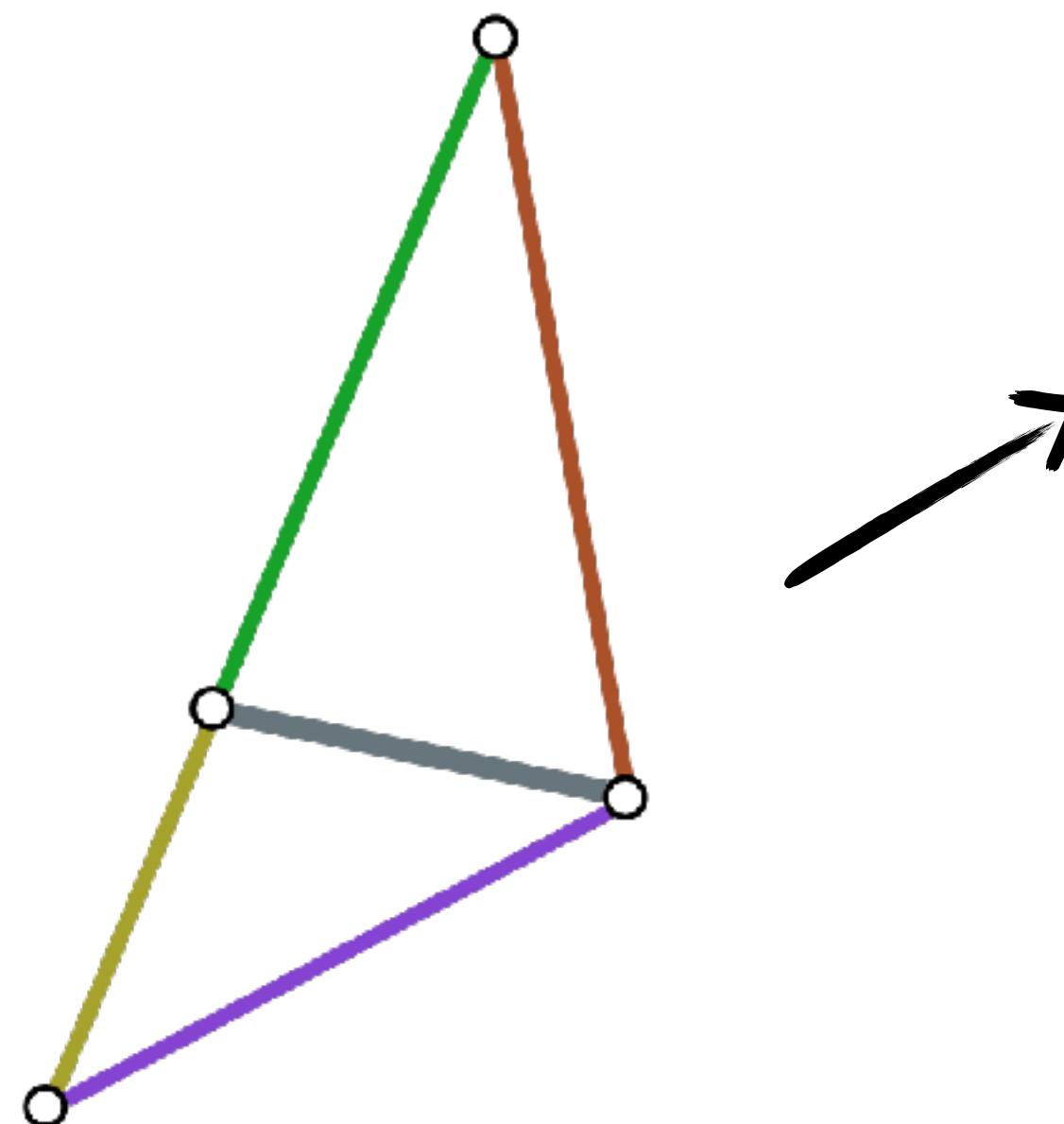
**Faces**  
 $\langle v_i, v_j, v_k \rangle$

# Learn Filters on Edge Features

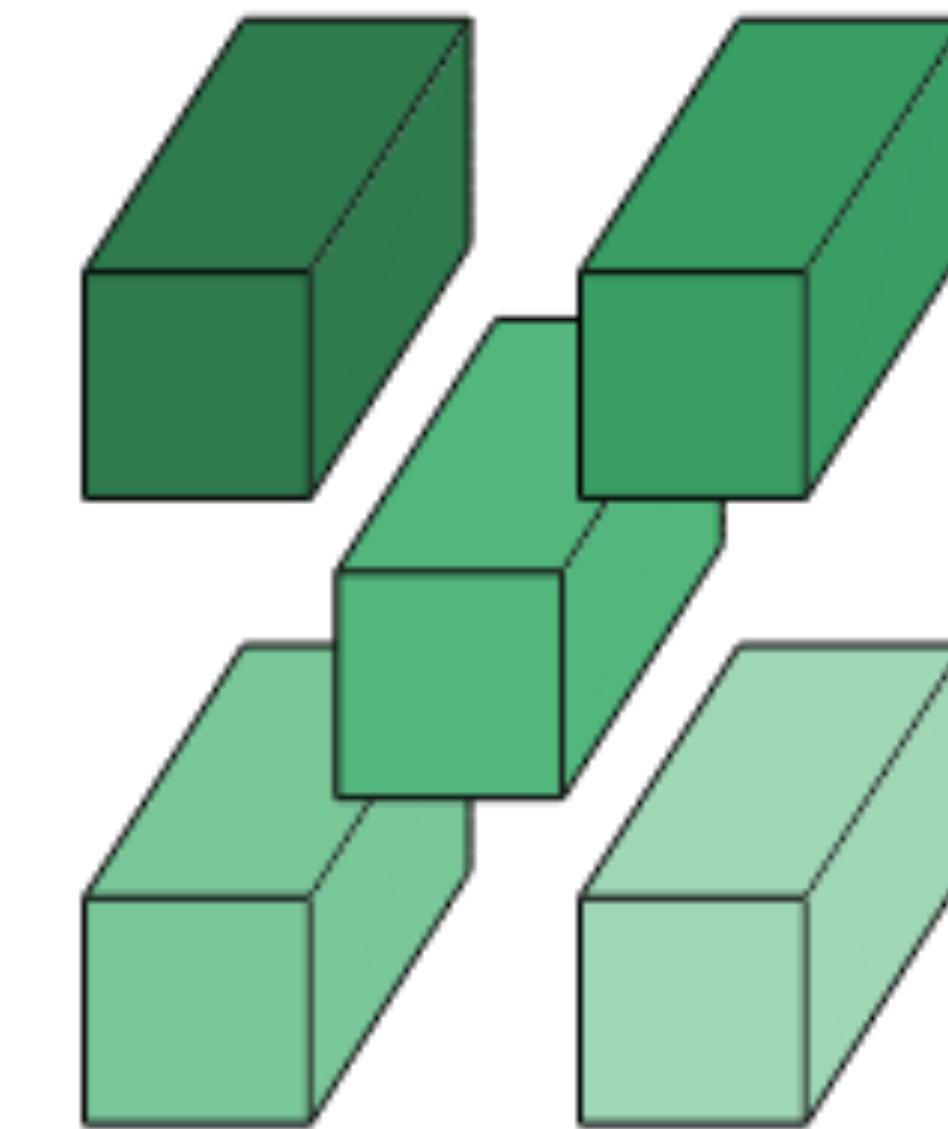


# Learn Filters on Edge Features

Different ordering of edge indices

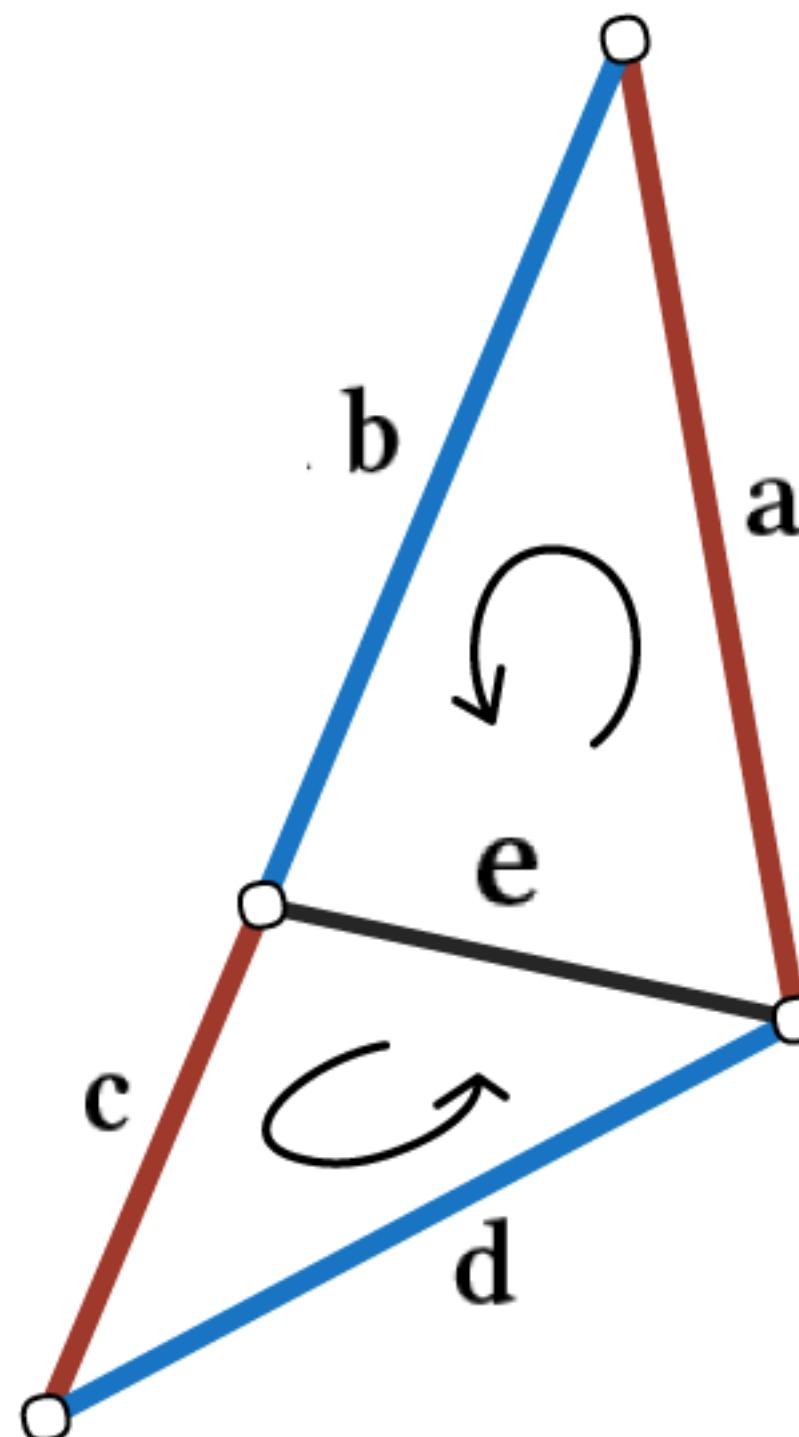


\*



**Conv Kernel**

# Mesh Convolution Order



Face normal

- Consistent ordering in each face
- Two *valid* orderings

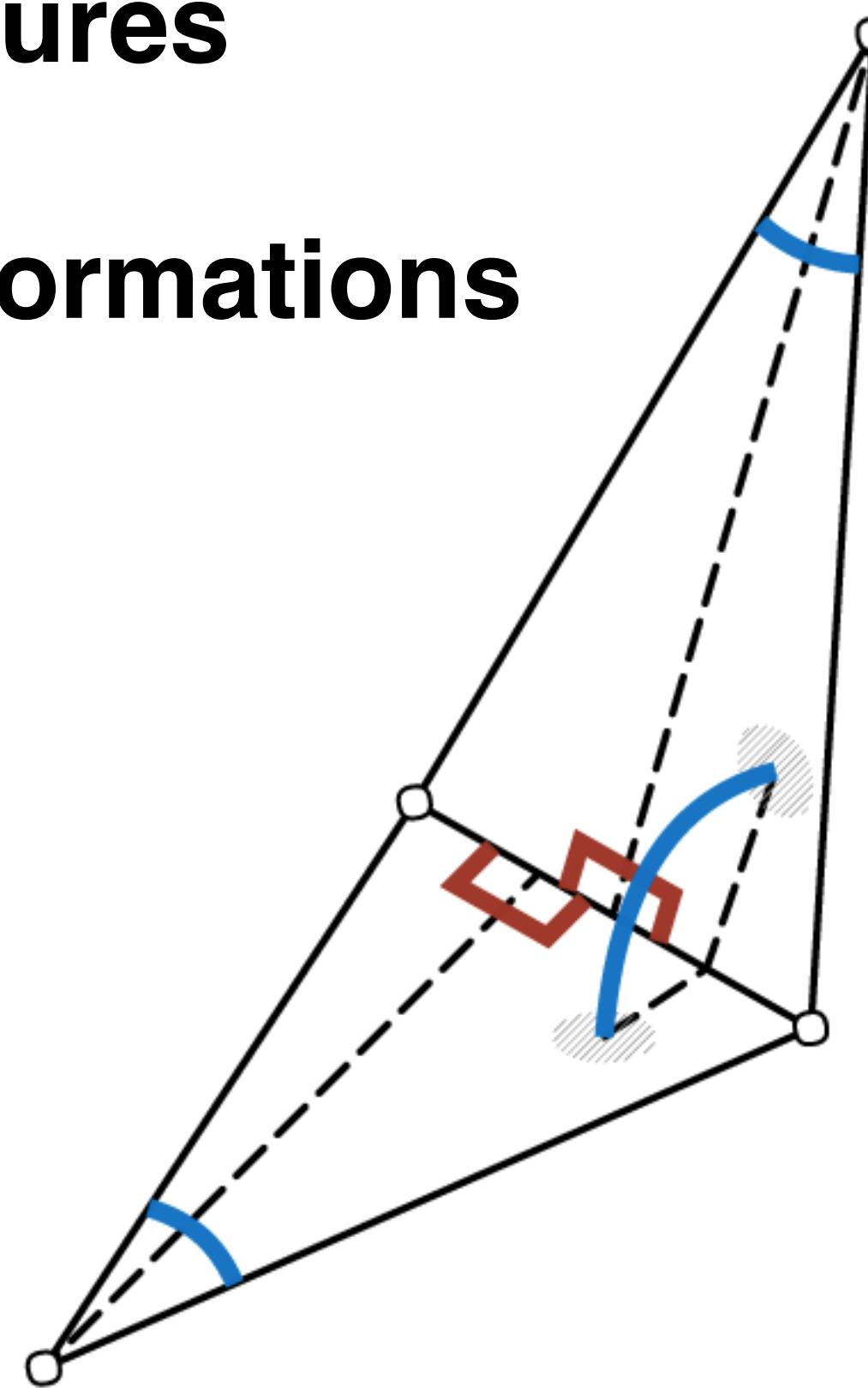
Build symmetric features

$e \rightarrow (a+c, |a-c|, b+d, |b-d|)$

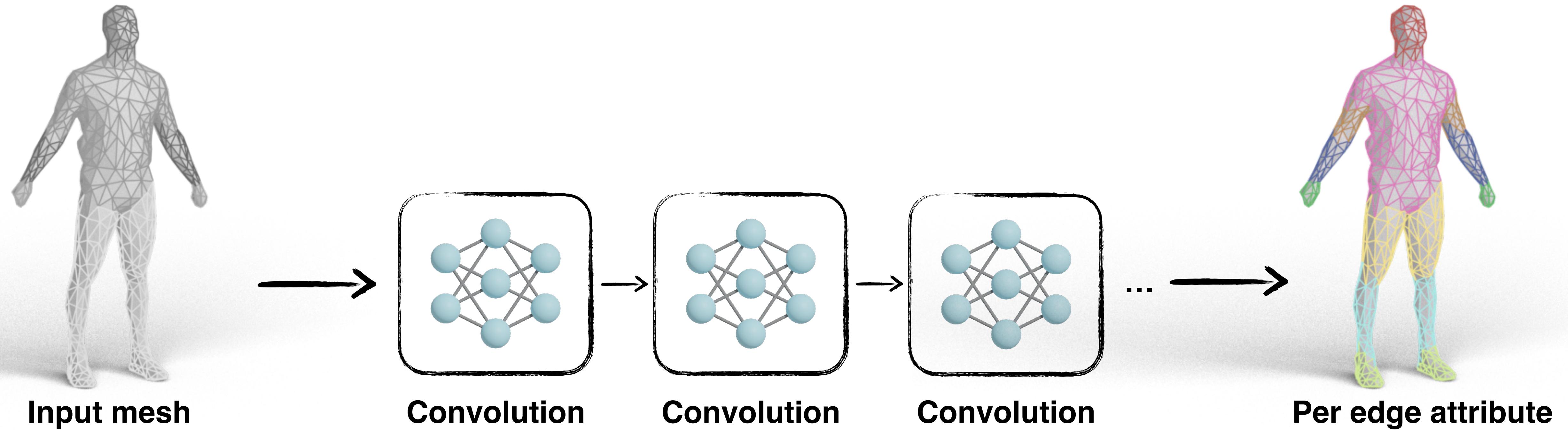
# Input edge features

**Relative geometric features**

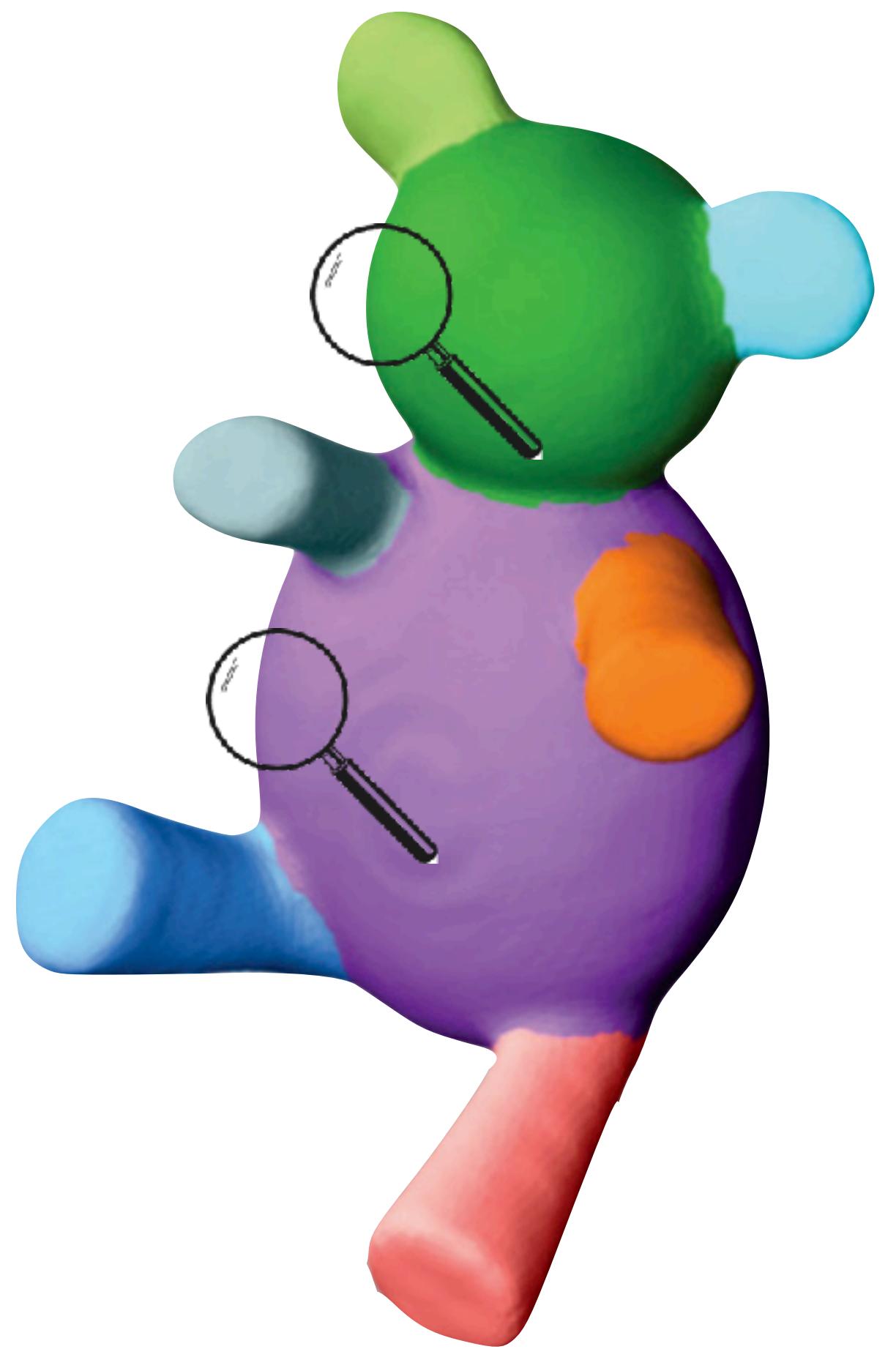
**Invariant to rigid transformations**



# Recap: learning local descriptors



# Incorporating more context



# Inspiration: image pooling

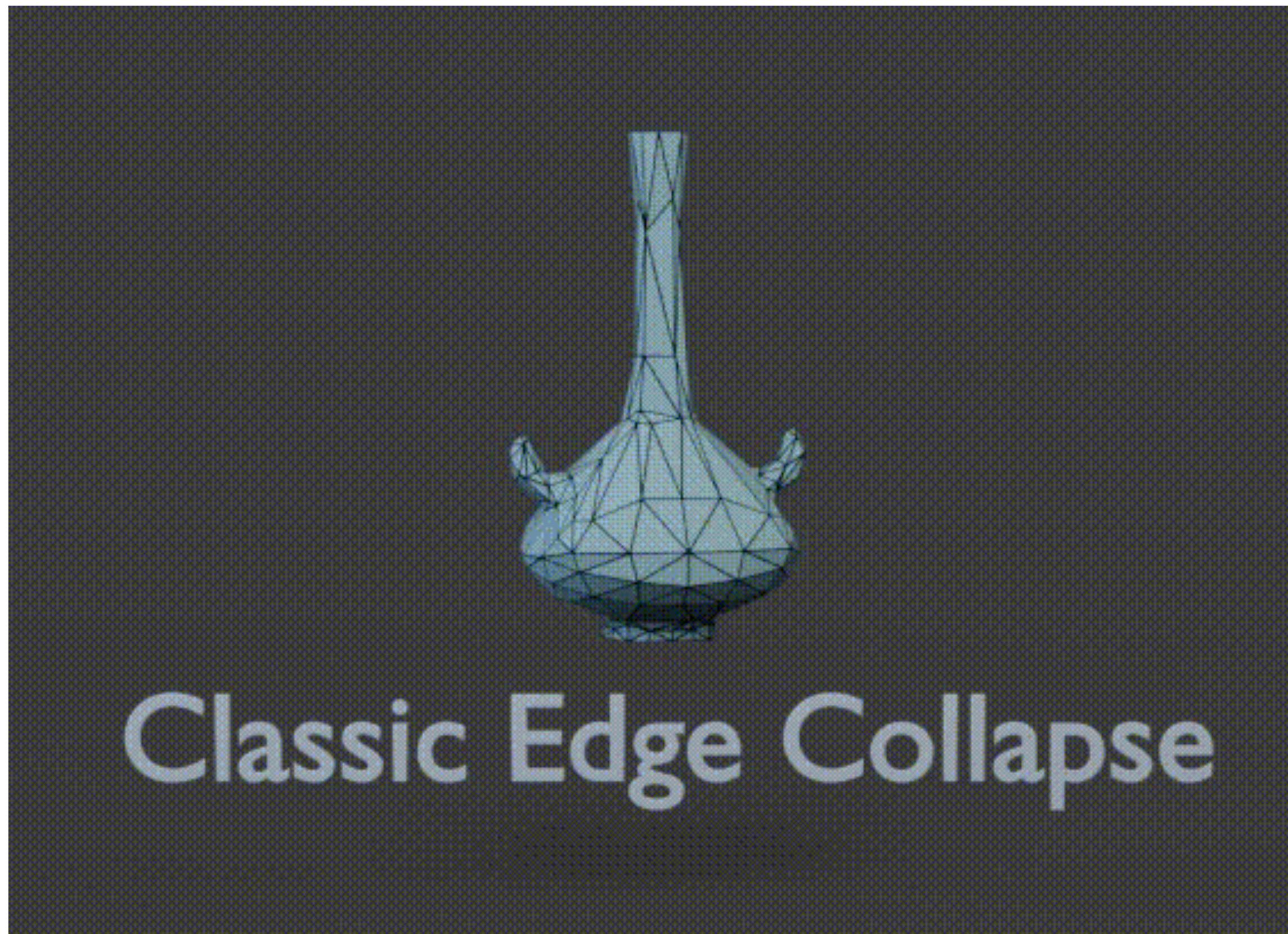
4	6	1	1
1	3	1	3
4	0	0	8
8	5	4	0

**Input (4x4)**



**Output (2x2)**

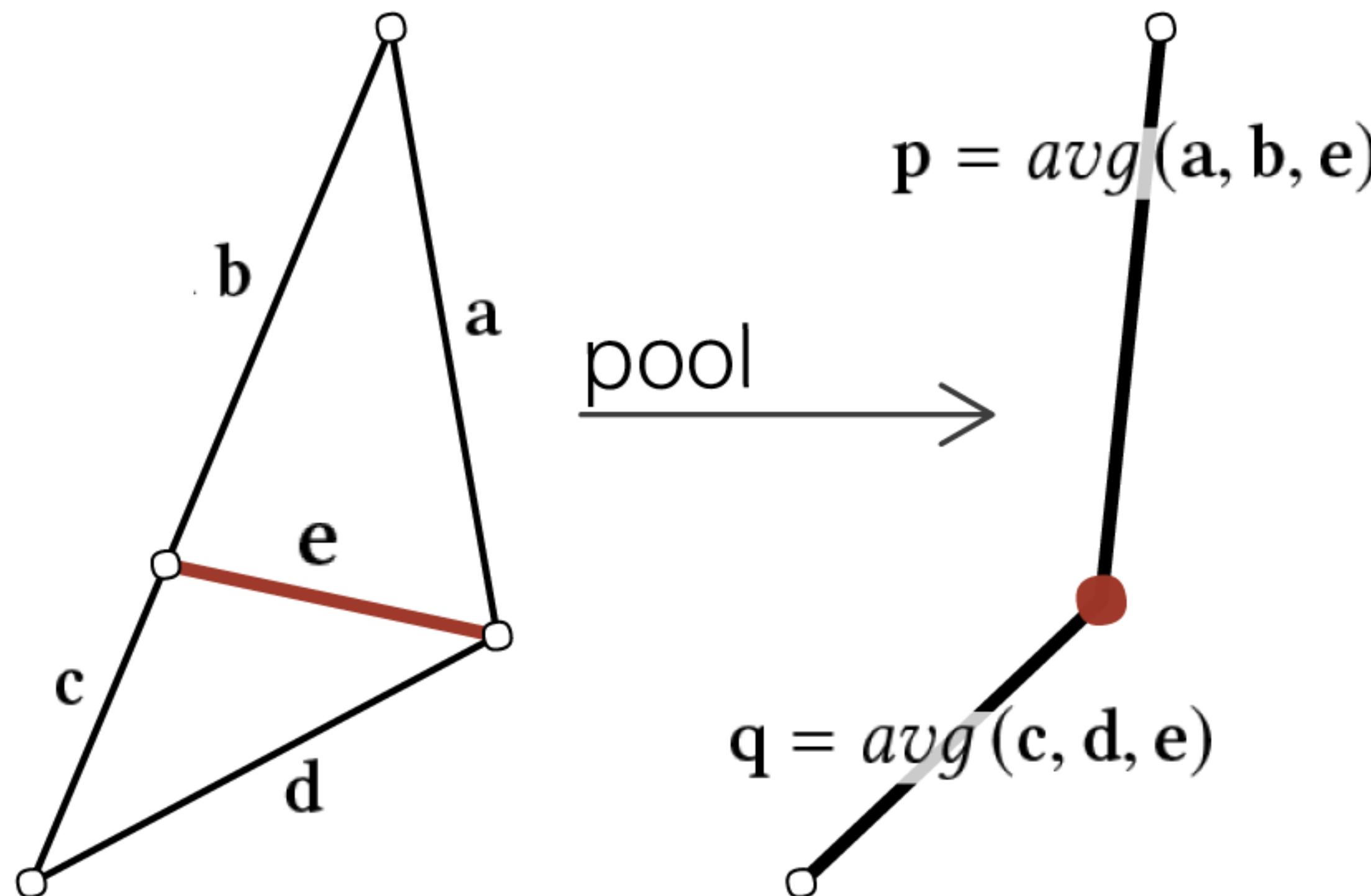
# Mesh pooling via edge collapse



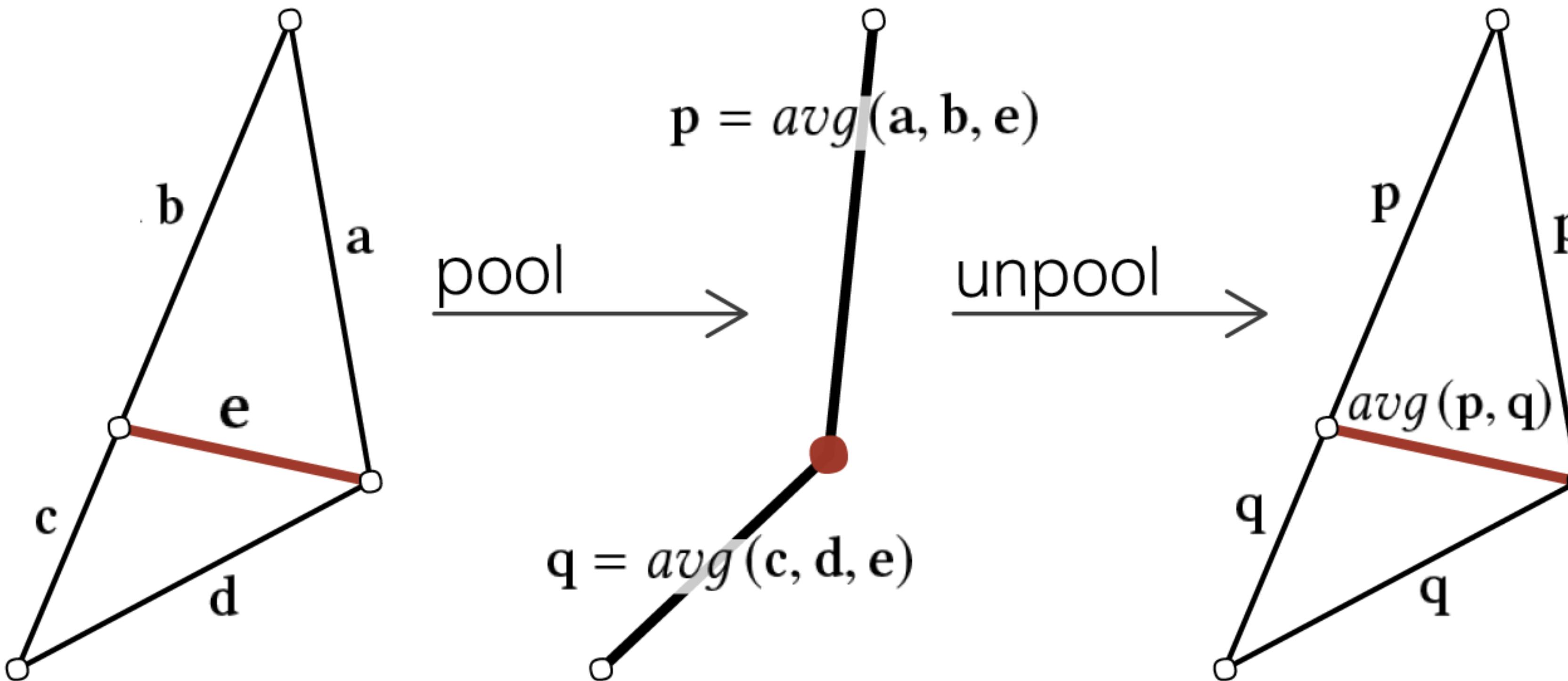
# Mesh pooling via edge collapse



# Mesh pooling via edge collapse

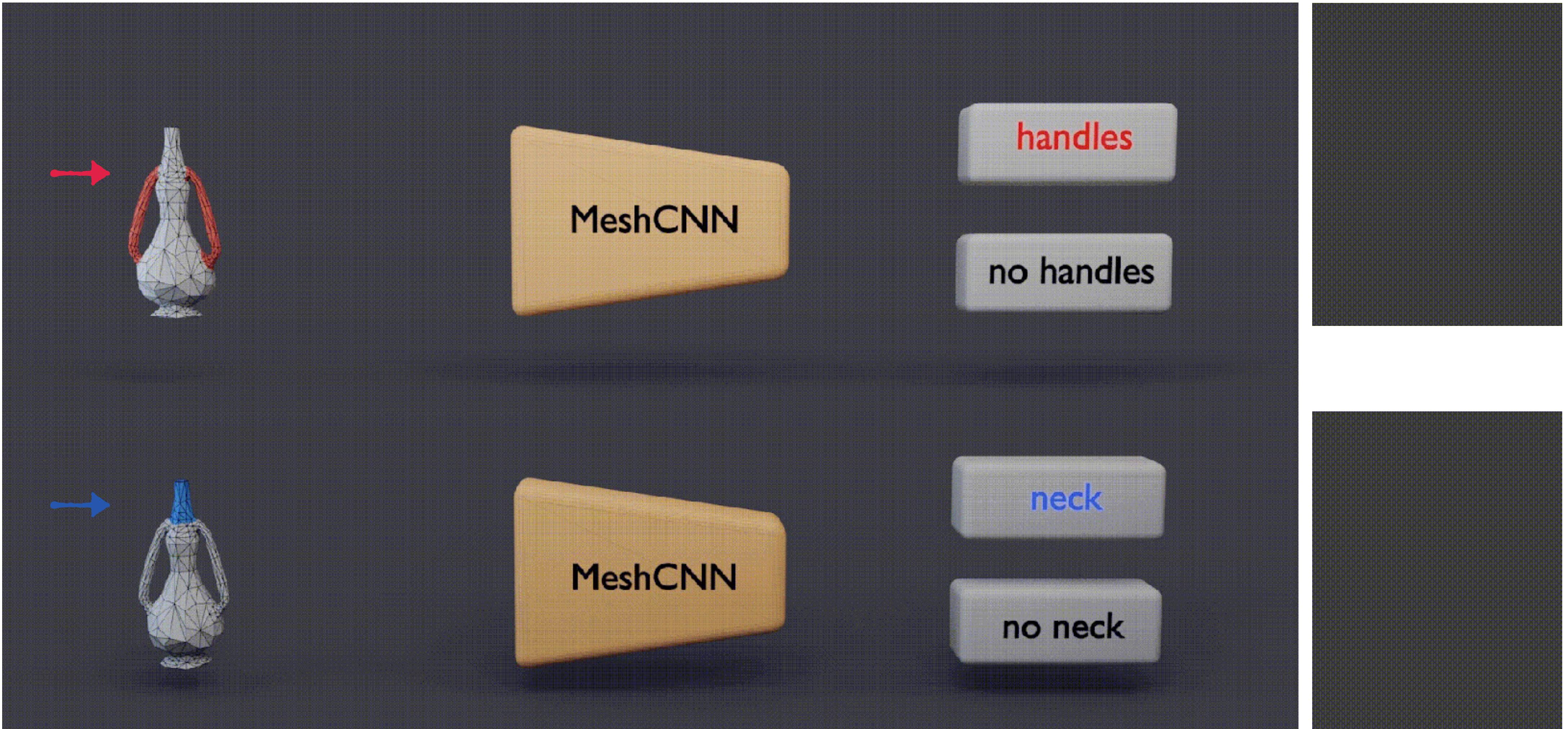


# Mesh unpooling

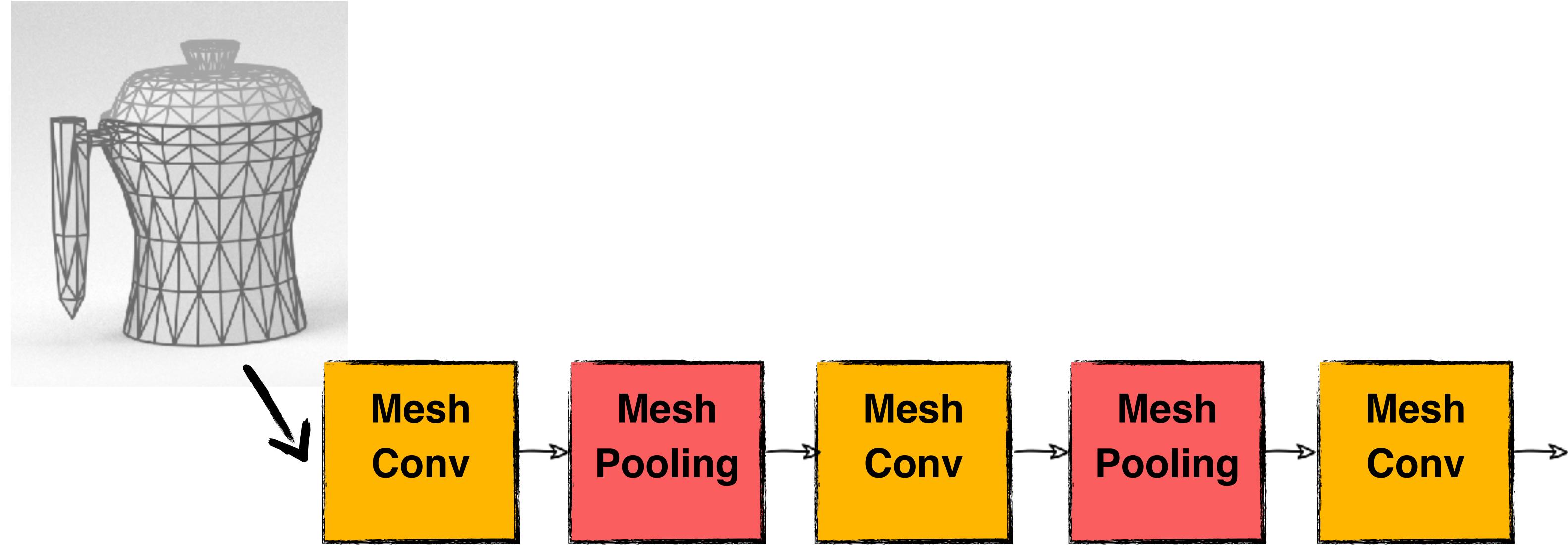


# Different tasks

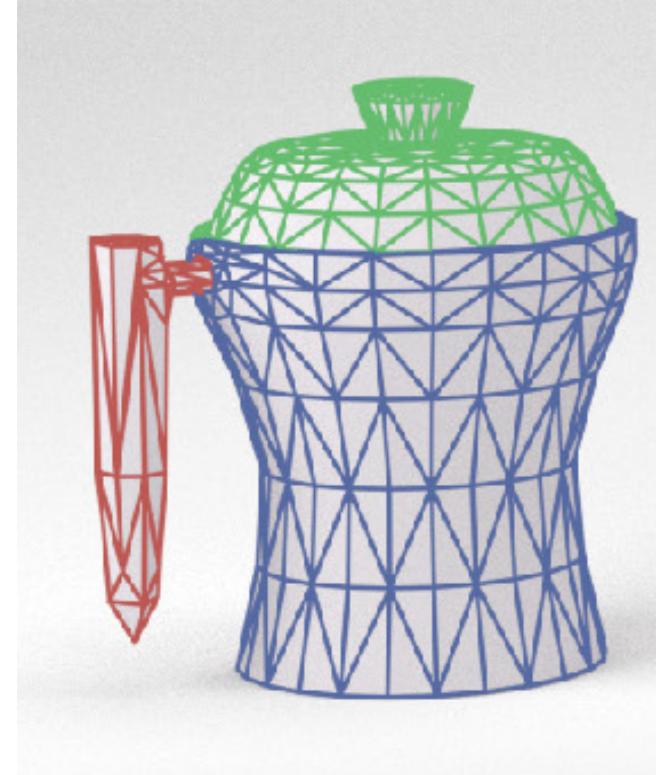
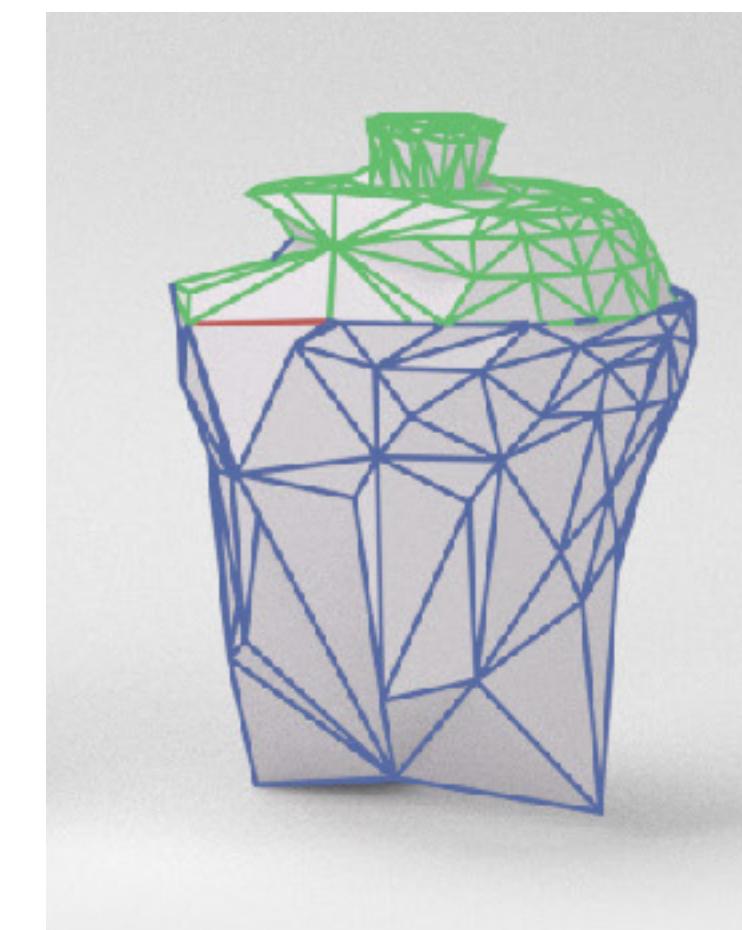
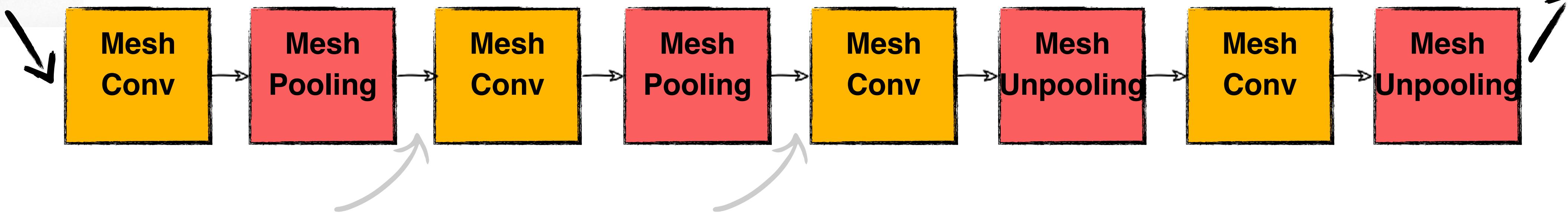
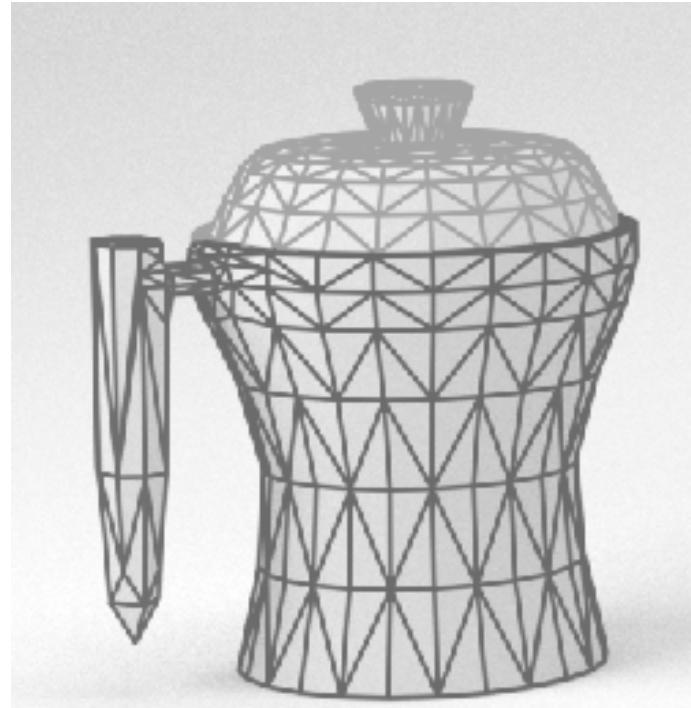
## Different simplifications



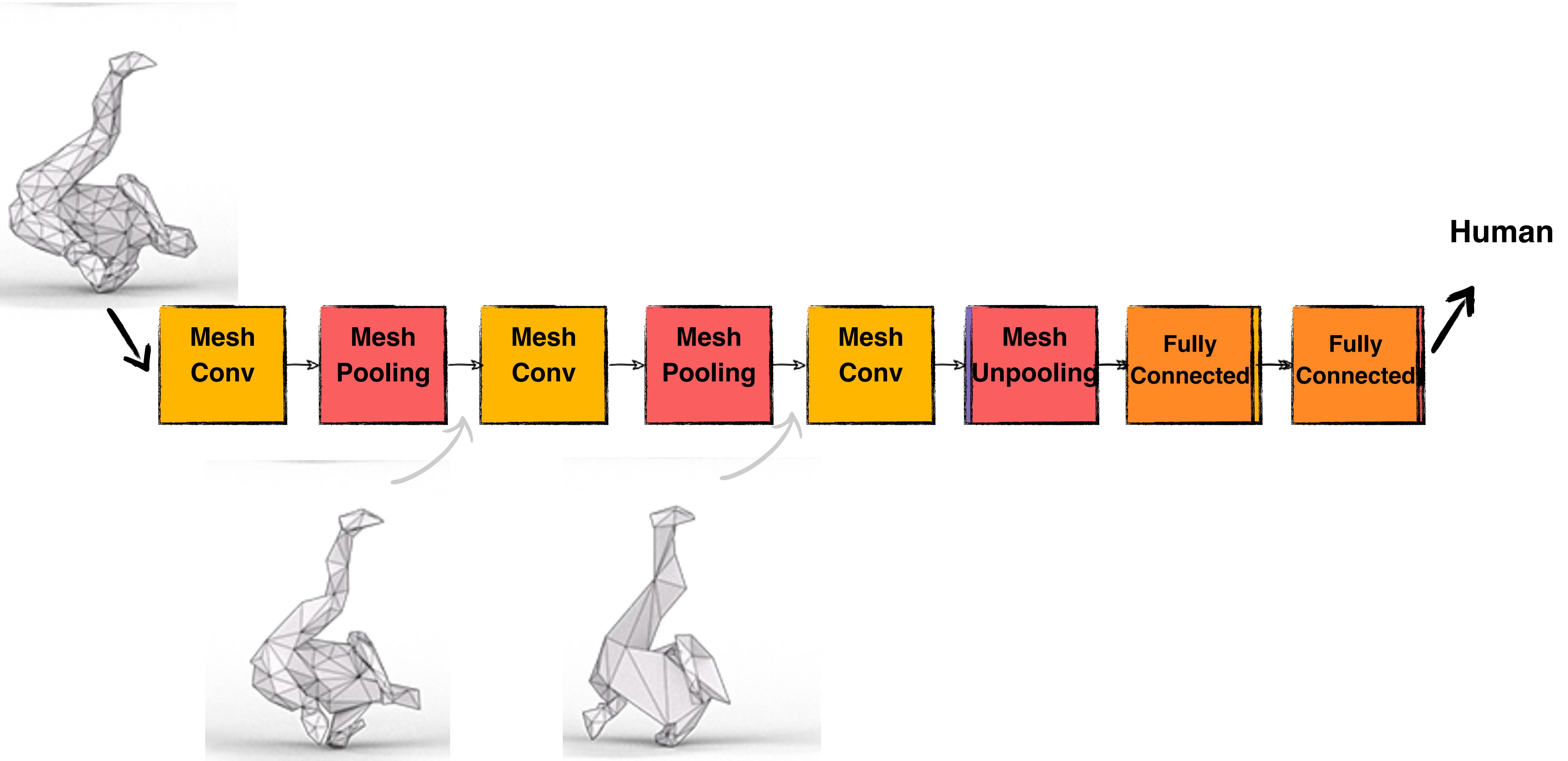
# MeshCNN



# MeshCNN Segmentation Overview

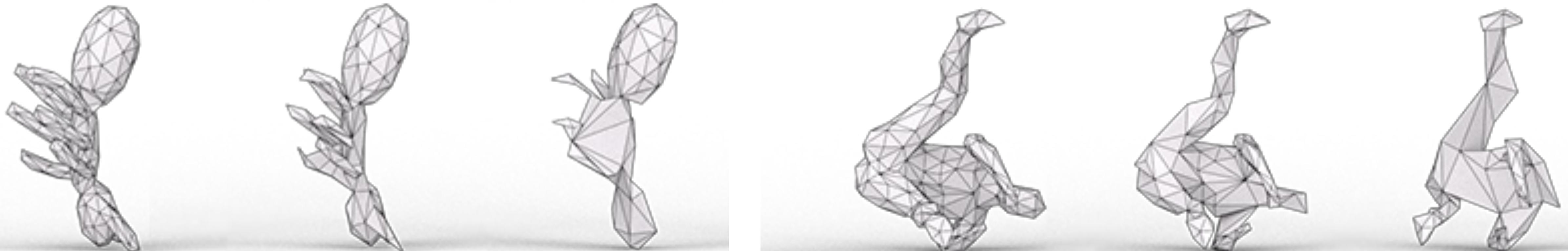


# MeshCNN Classification Overview

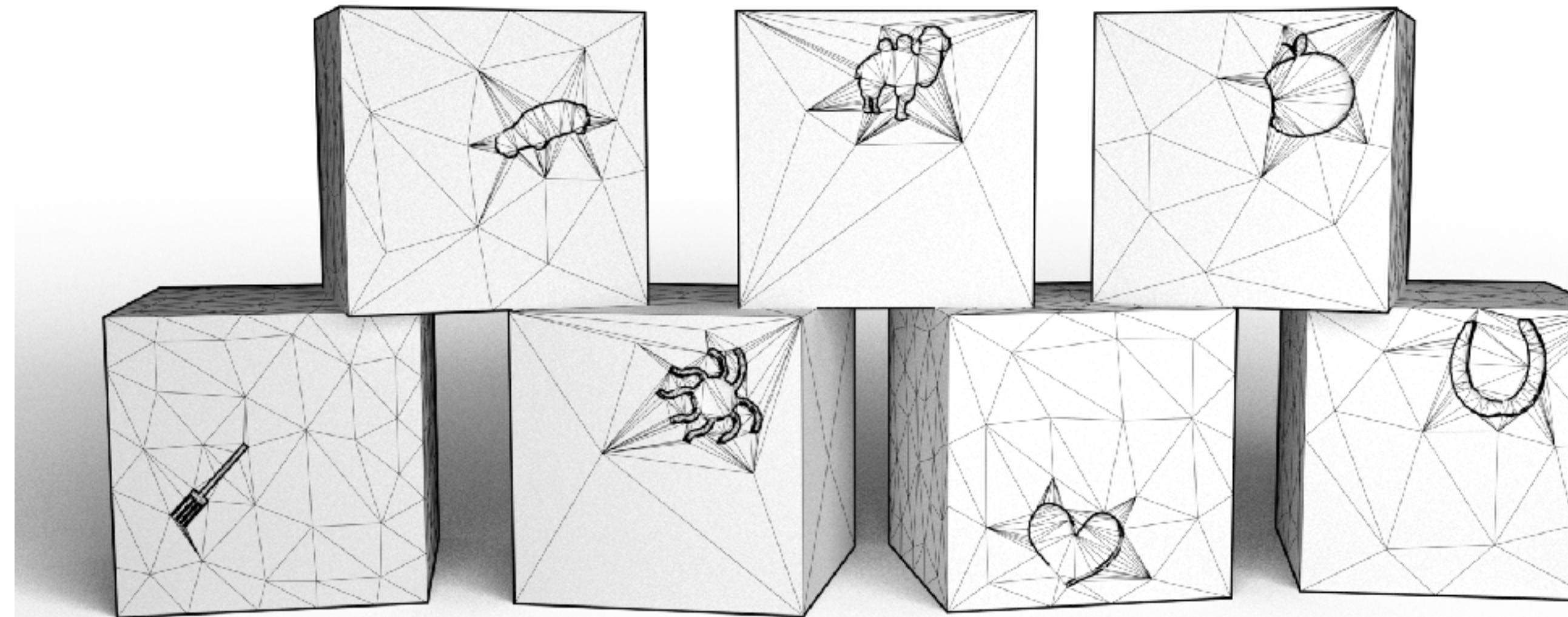


# Shape Classification

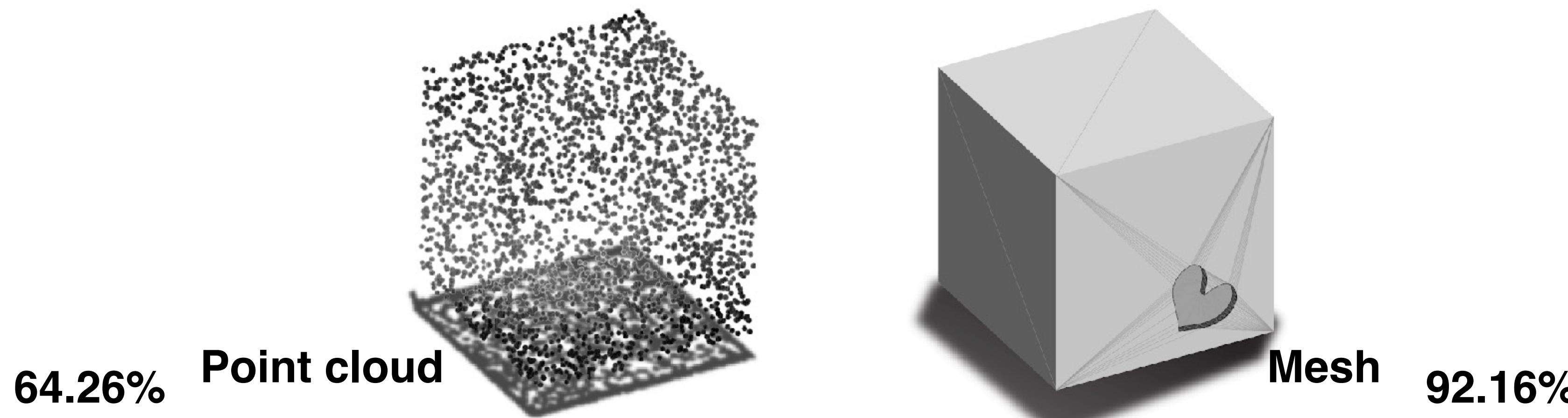
Method	Split 16	Split 10
<b>MeshCNN</b>	<b>98.6</b>	<b>91.0%</b>
GWCNN	96.6%	90.3%
GI	96.6%	88.6%
SN	48.4%	52.7%
SG	70.8%	62.6%



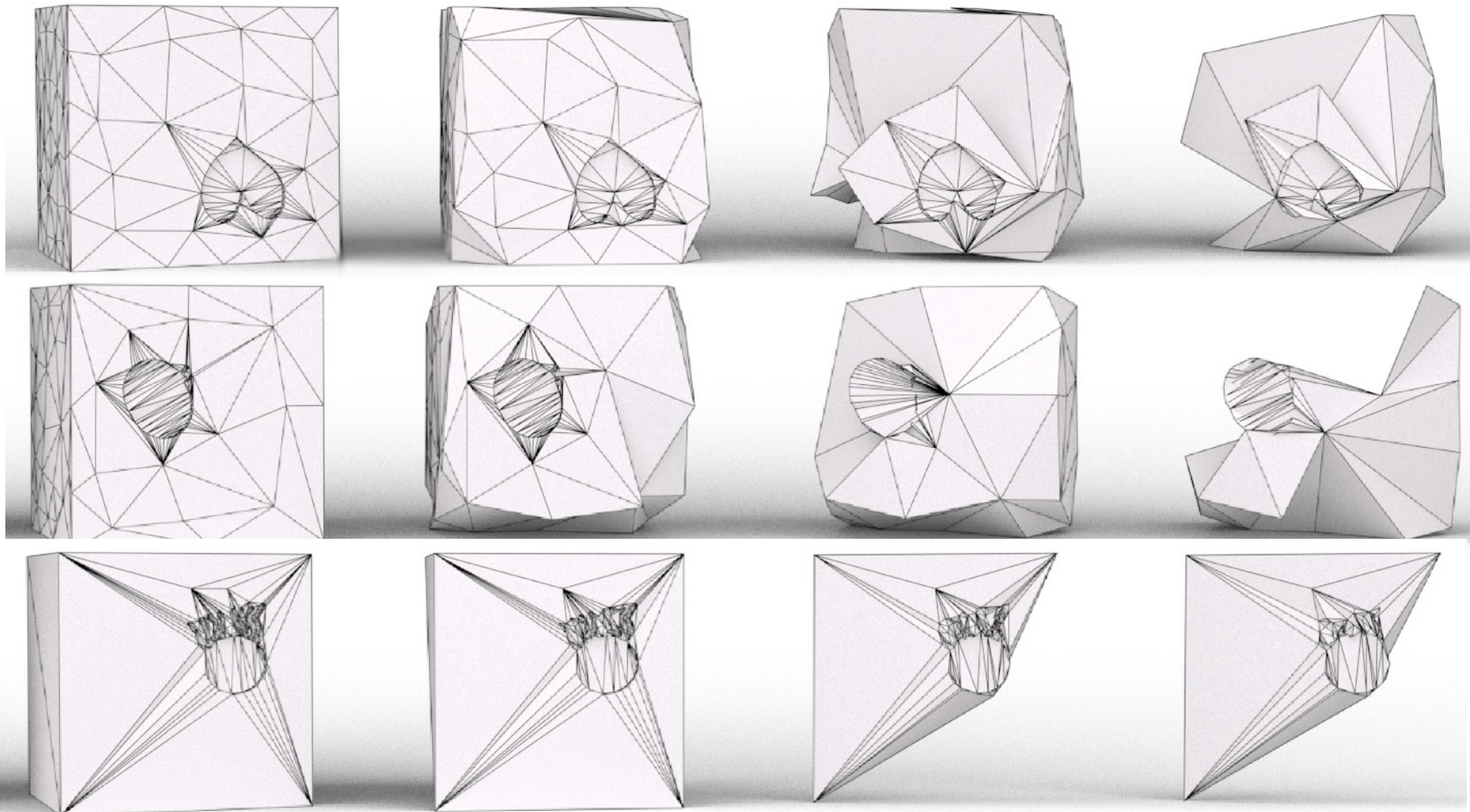
# Cube Engraving Classification



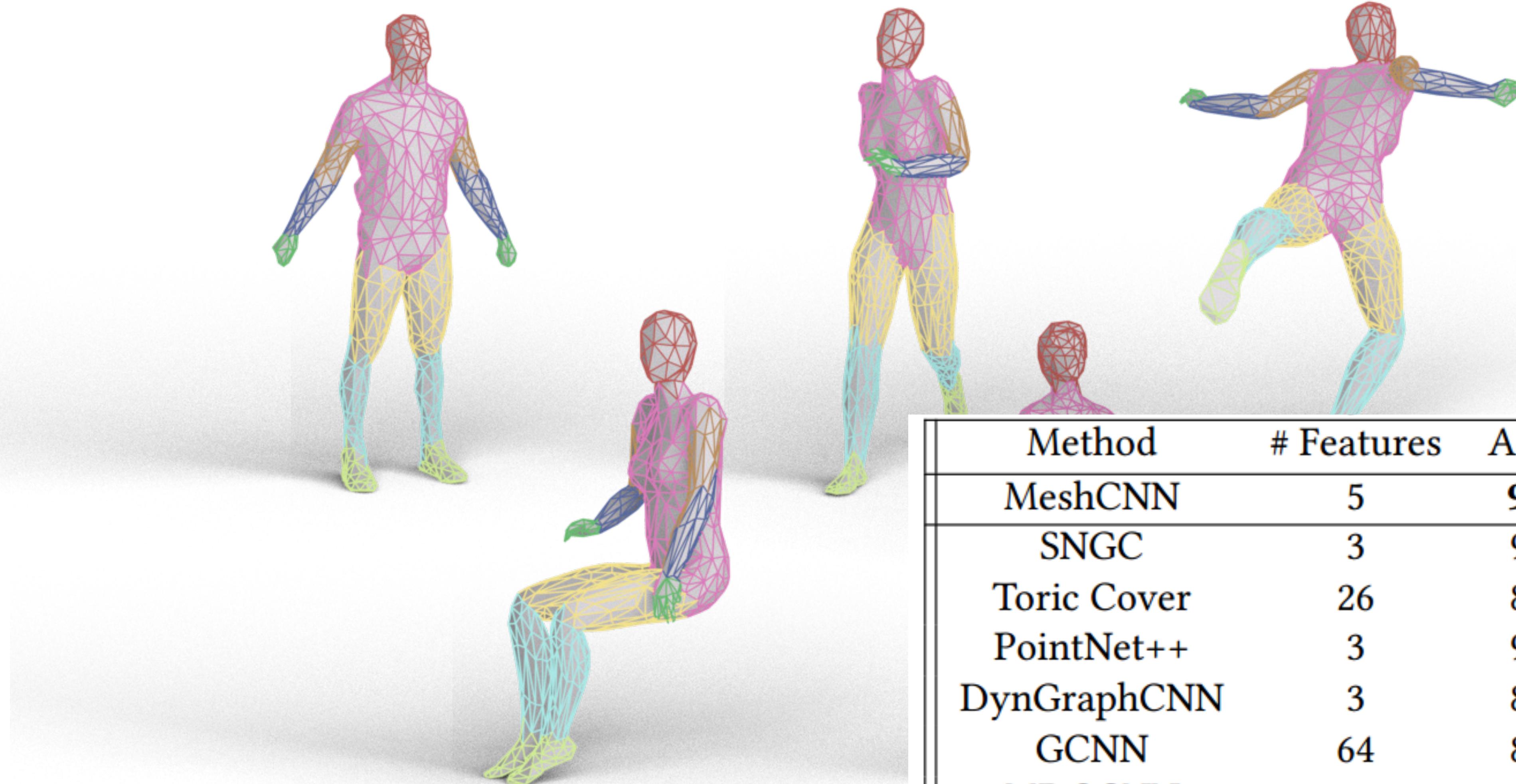
Which engraving does this have?



# Intermediate Mesh Pooling

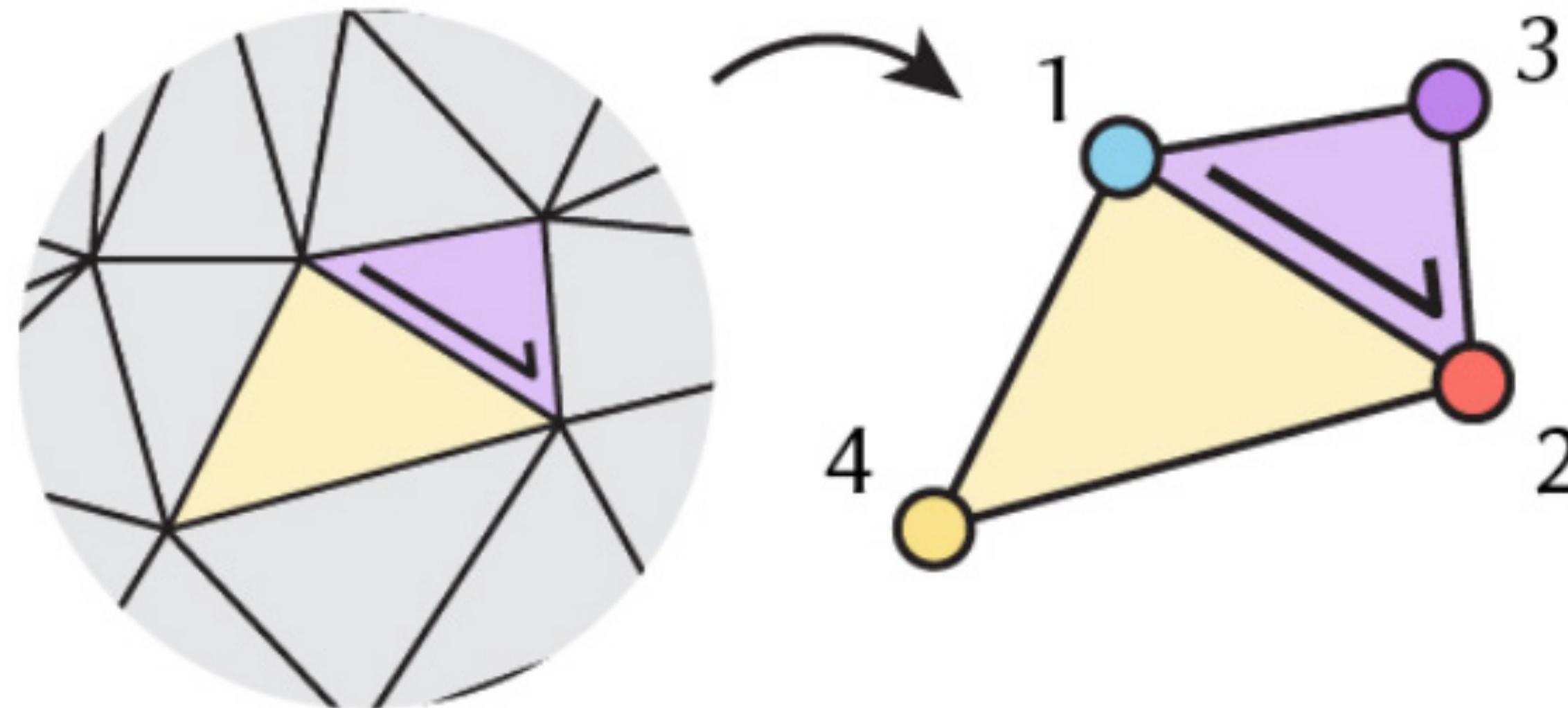


# Human Segmentation



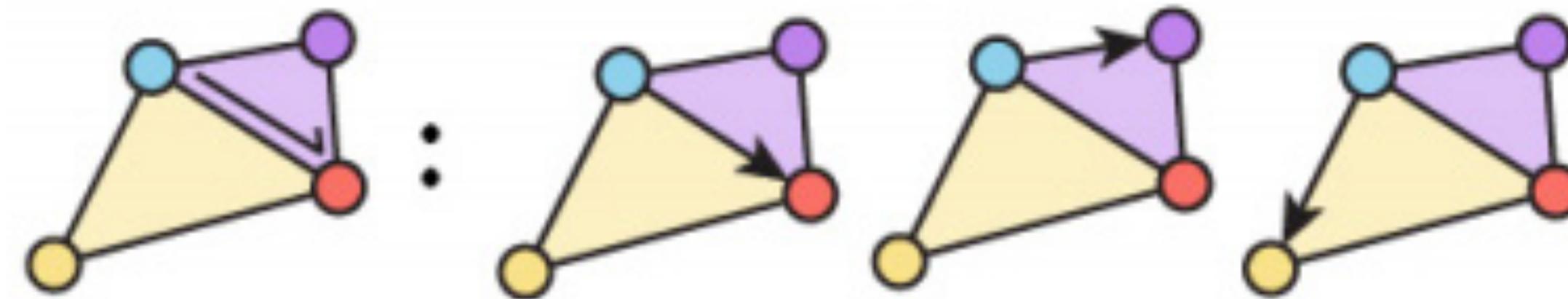
Method	# Features	Accuracy
MeshCNN	5	<b>92.30%</b>
SNGC	3	91.02%
Toric Cover	26	88.00%
PointNet++	3	90.77%
DynGraphCNN	3	89.72%
GCNN	64	86.40%
MDGCNN	64	89.47%

# Convolutions on half-edges

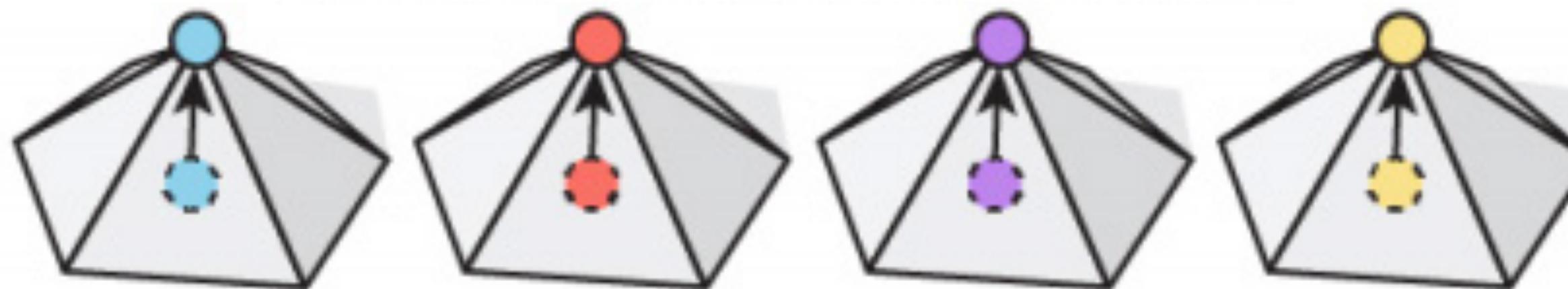


# Half-edge input features

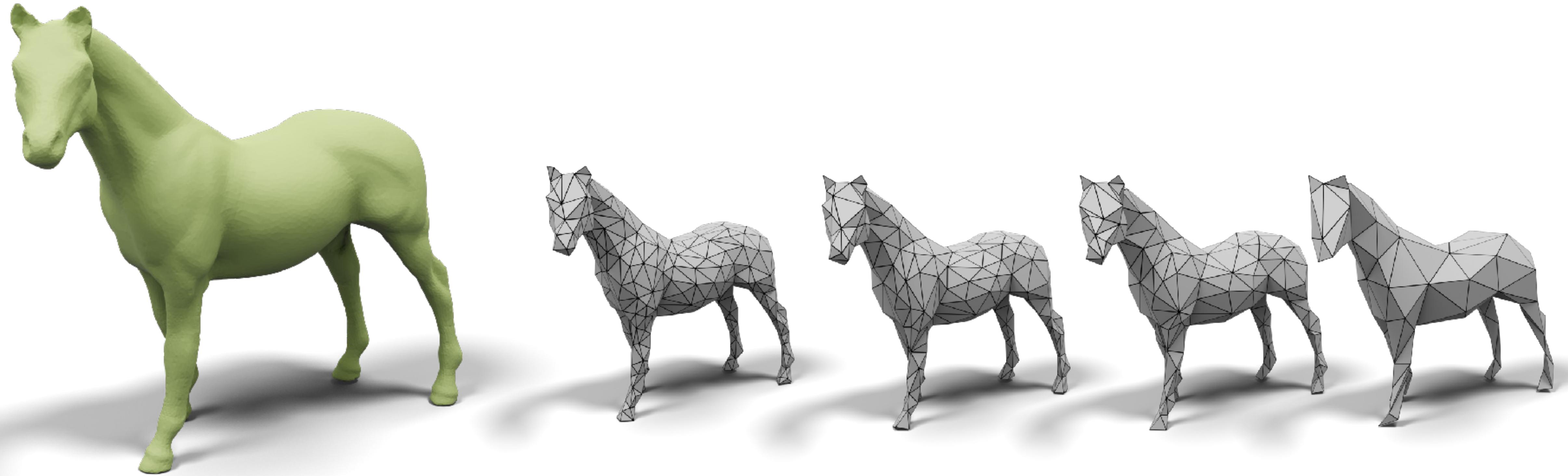
**Edge vectors**



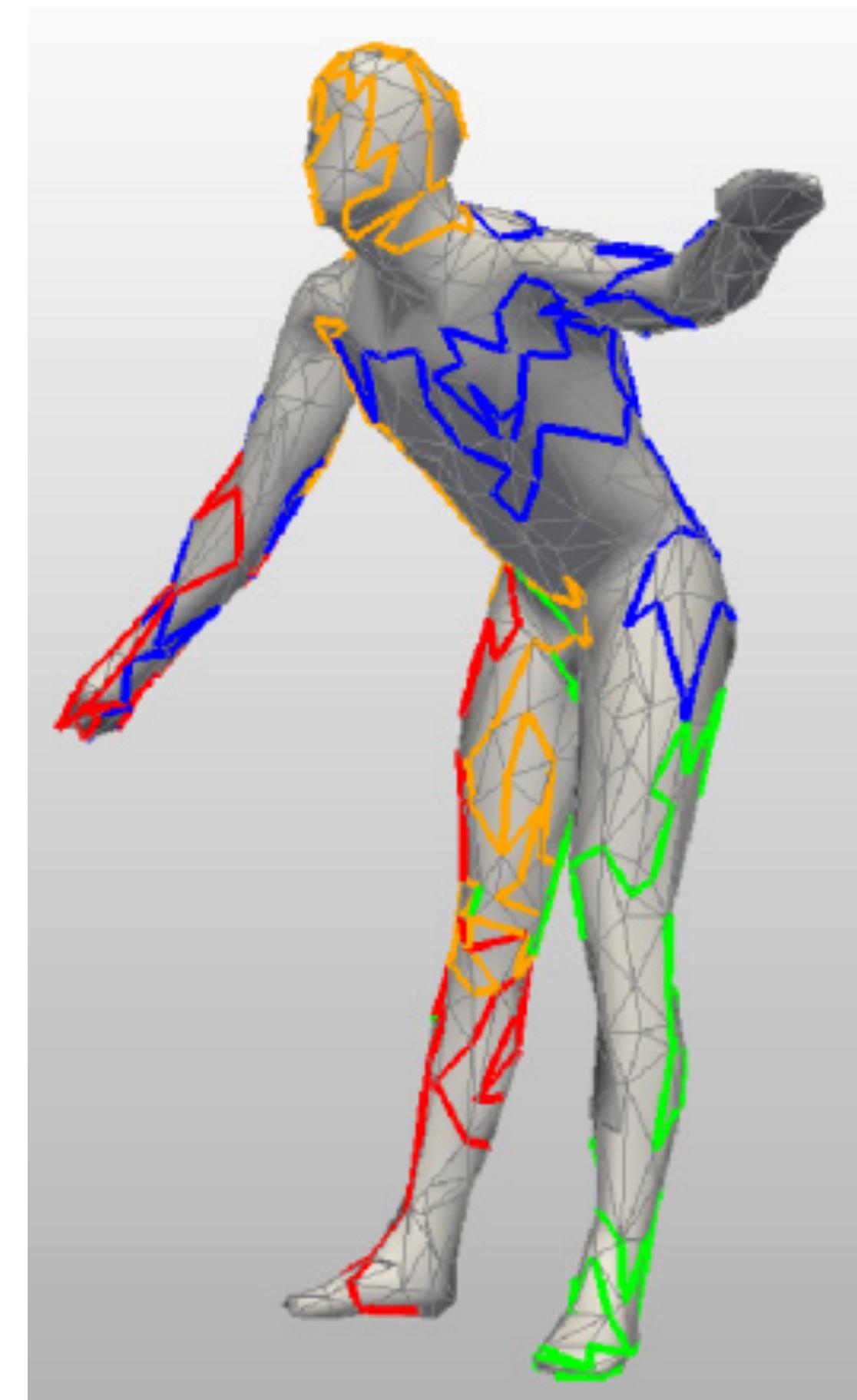
**Differential coordinates**



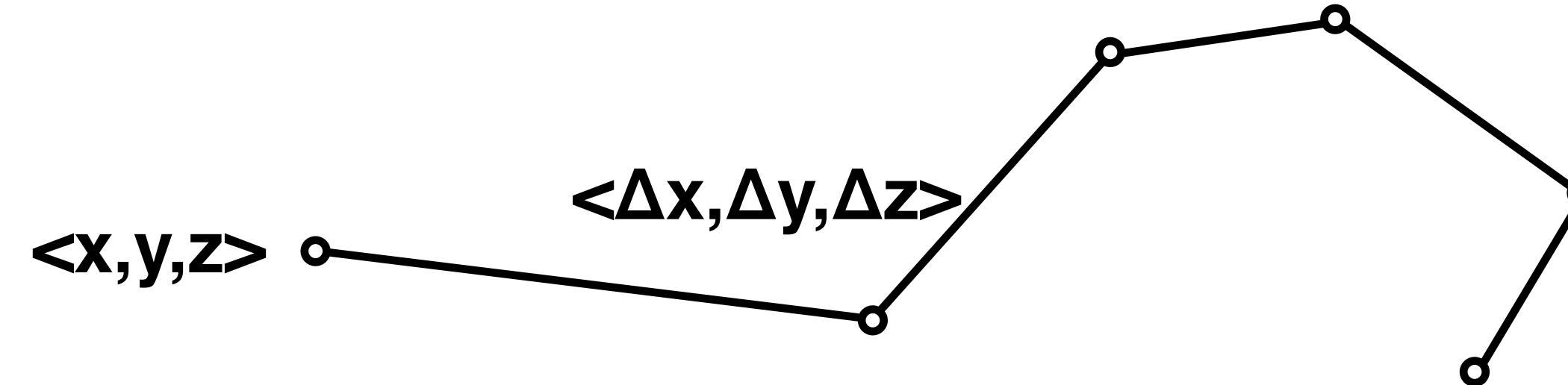
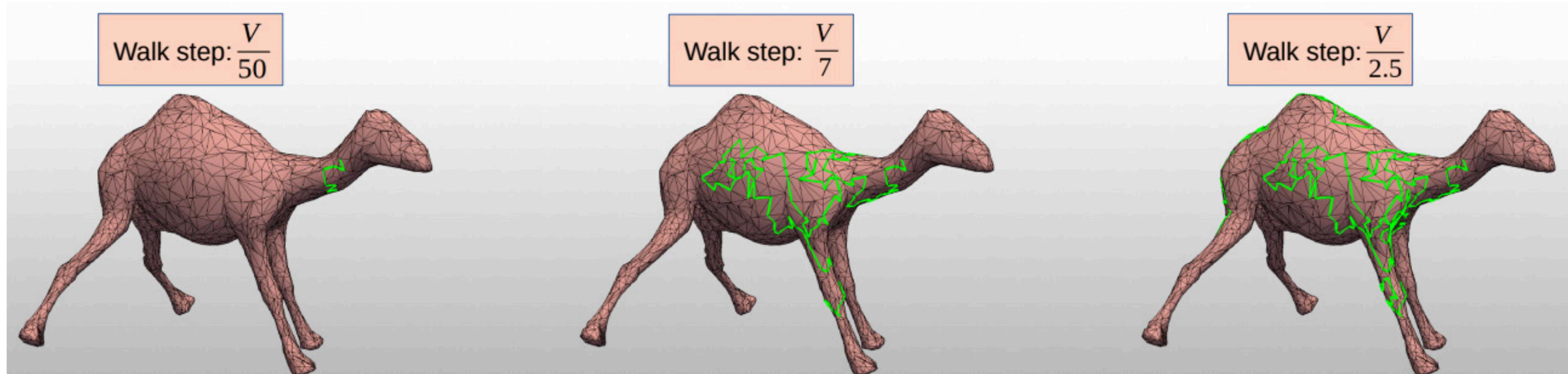
# Input mesh coarsening



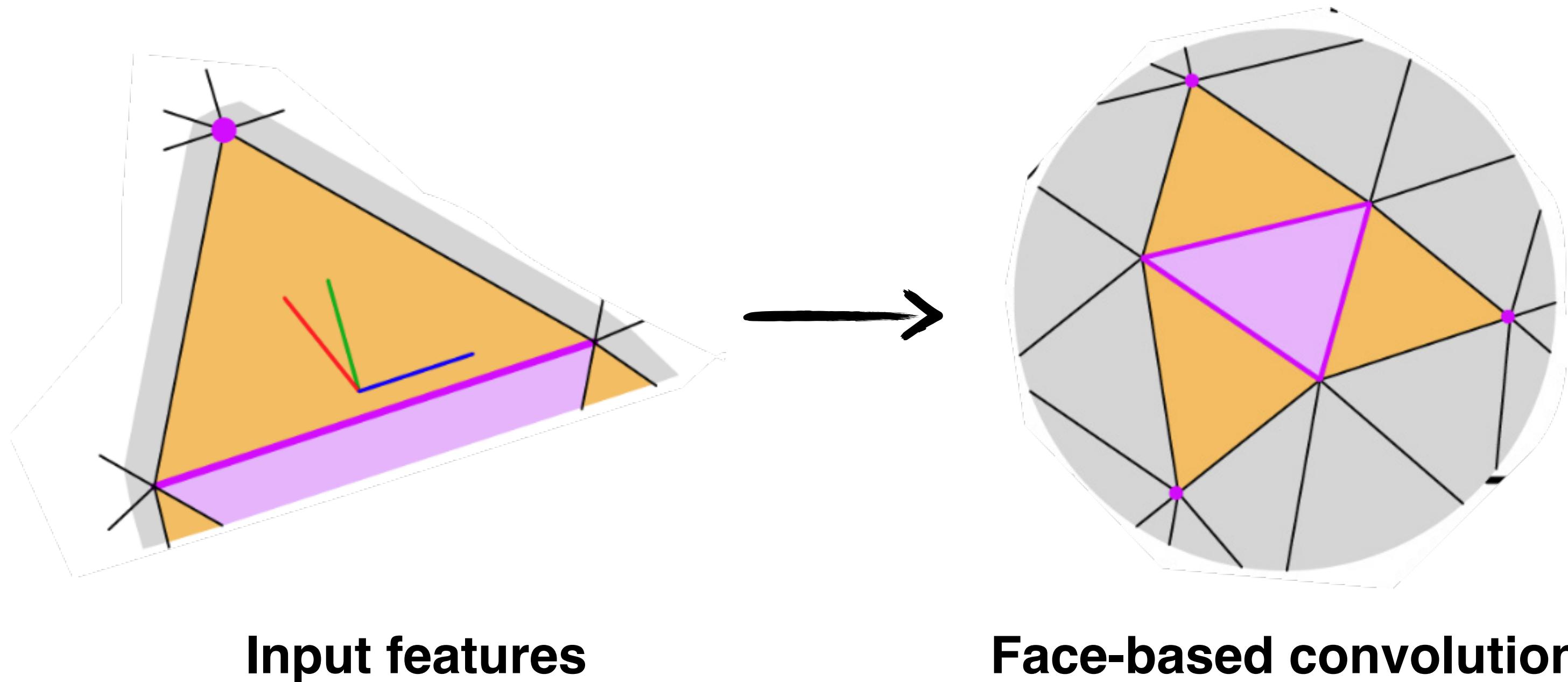
# Learning on random walks



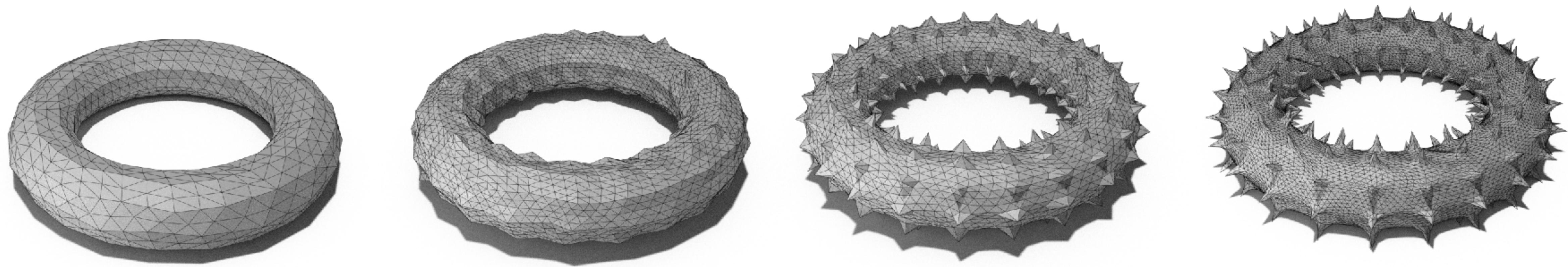
# Learning on random walks



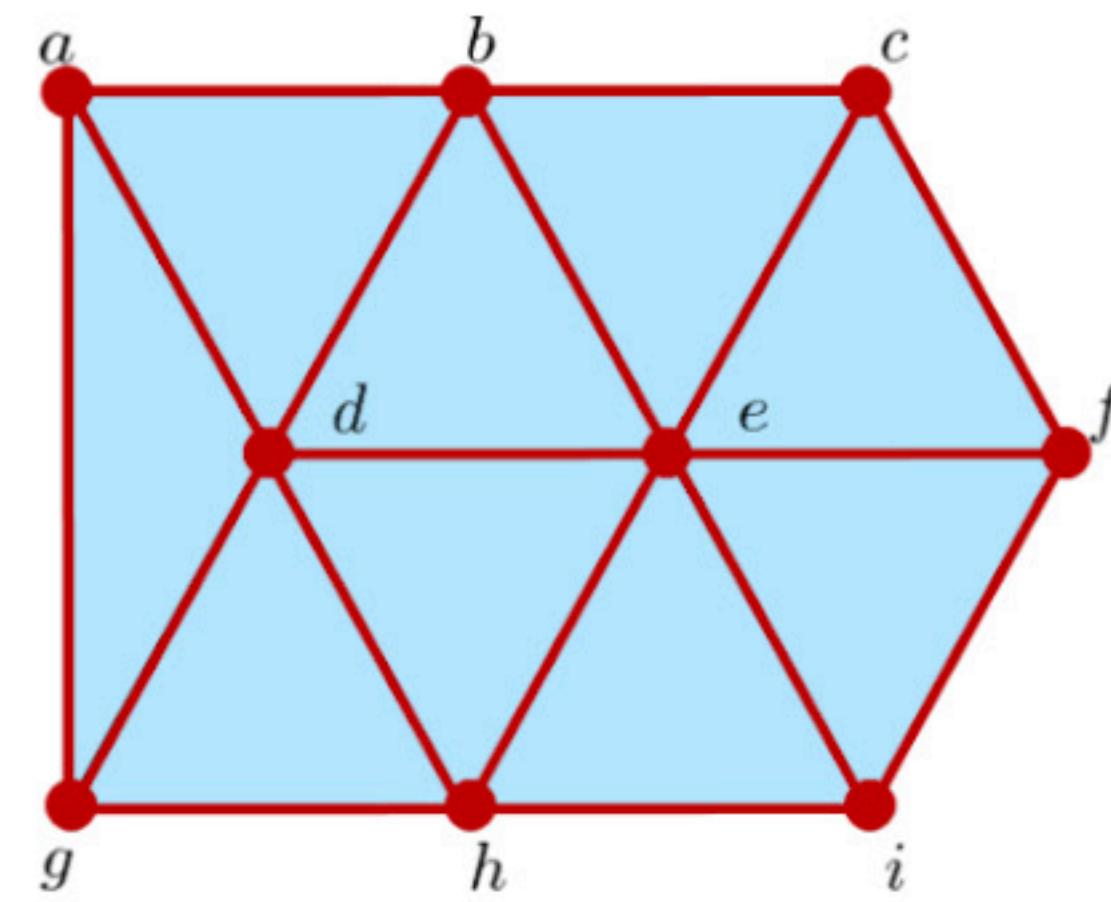
# Convolutions on mesh faces



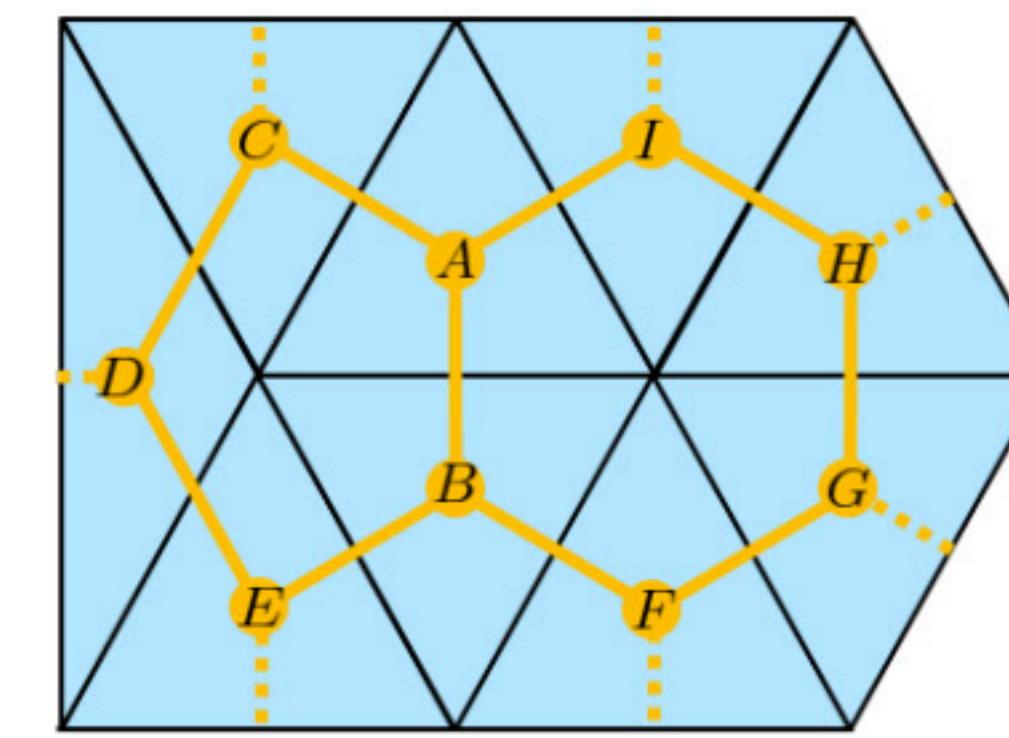
# Input mesh untexturing



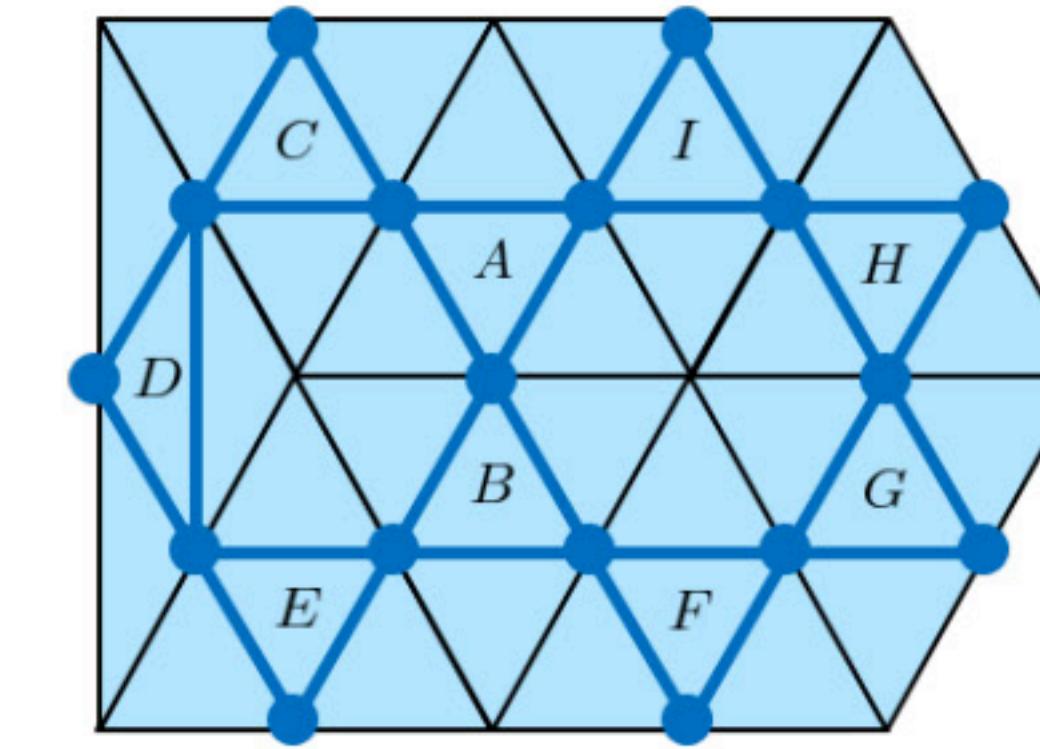
# Convolutions on primal/dual mesh graphs



Mesh

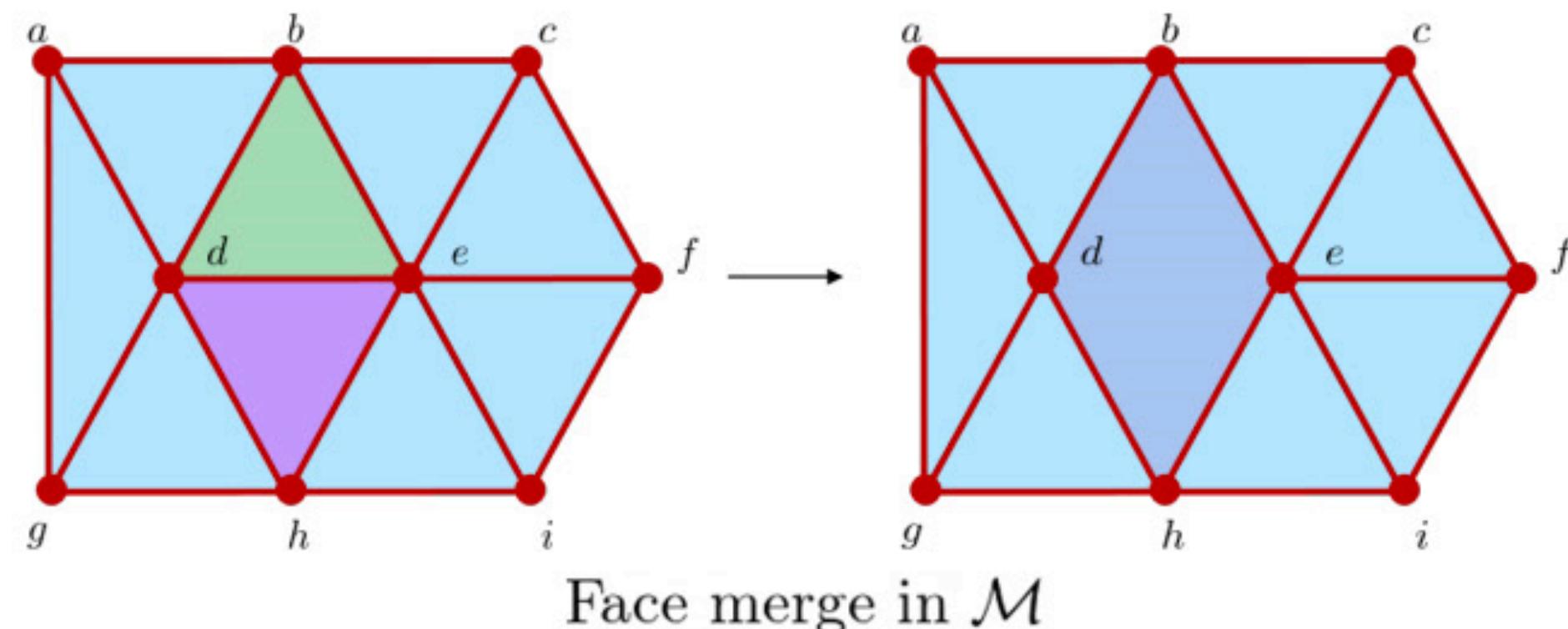
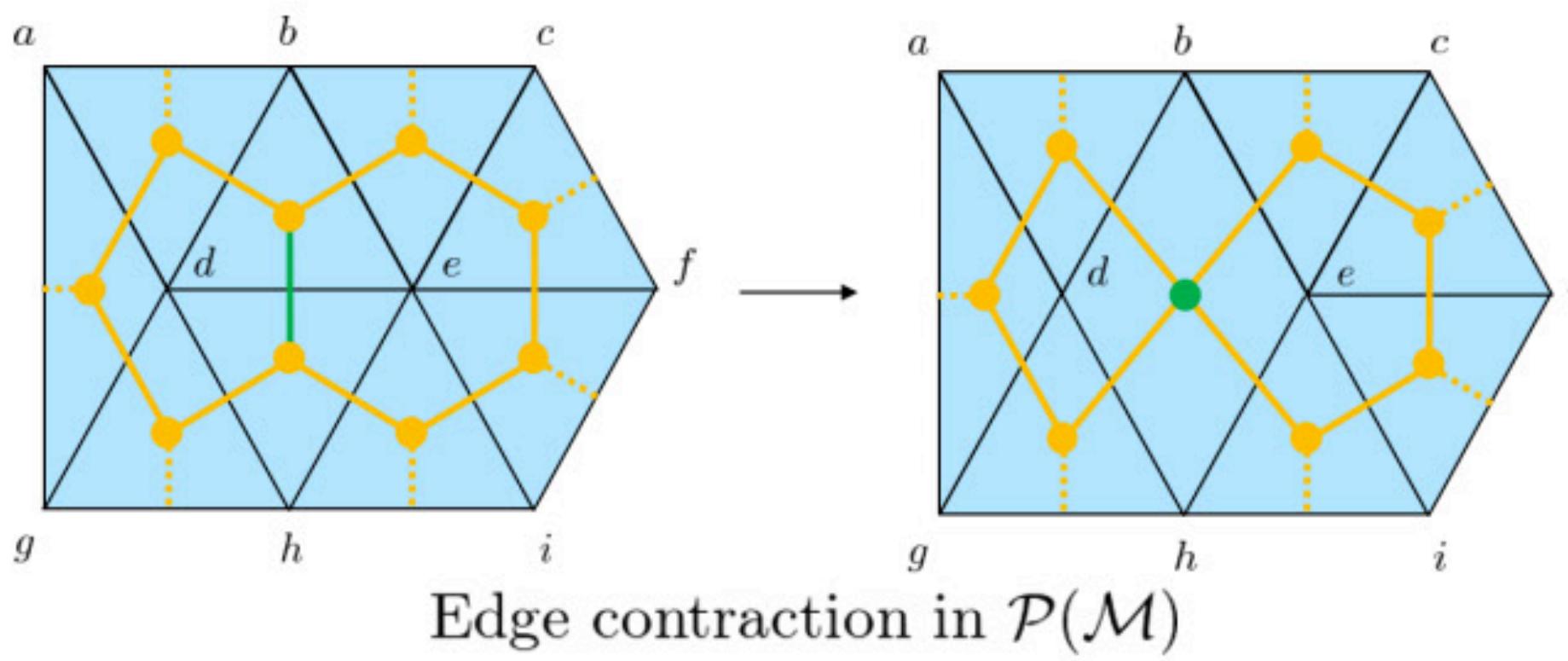


Primal Graph

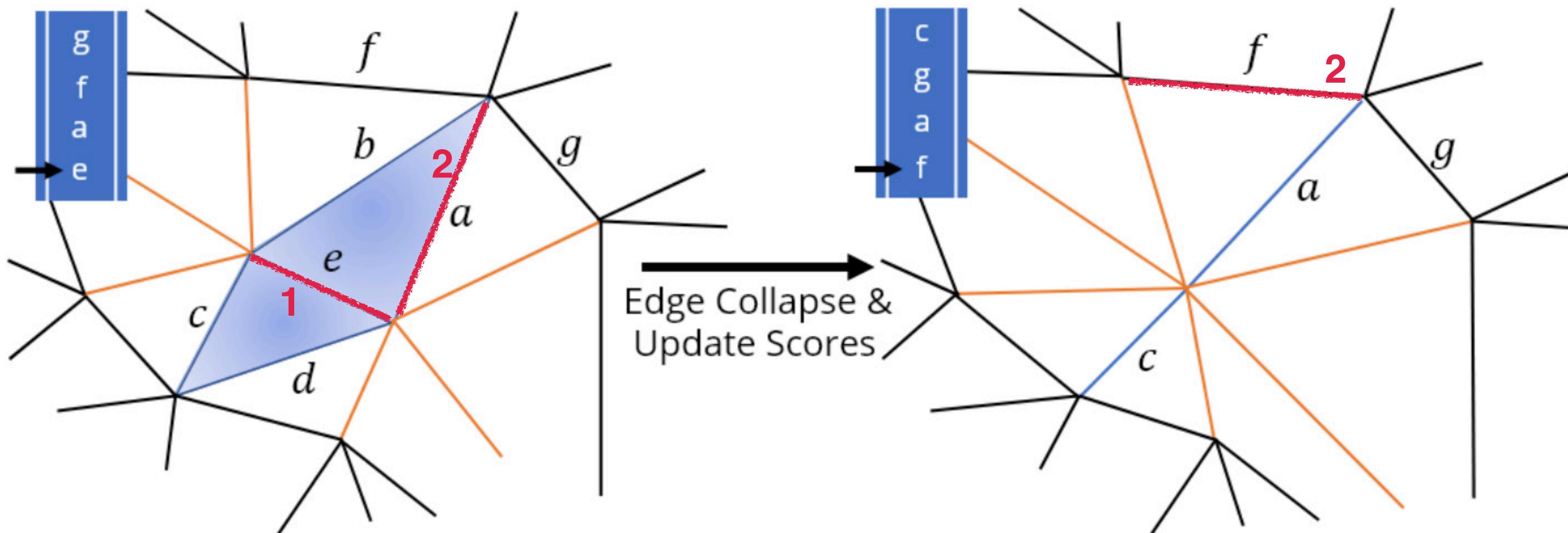


Dual Graph

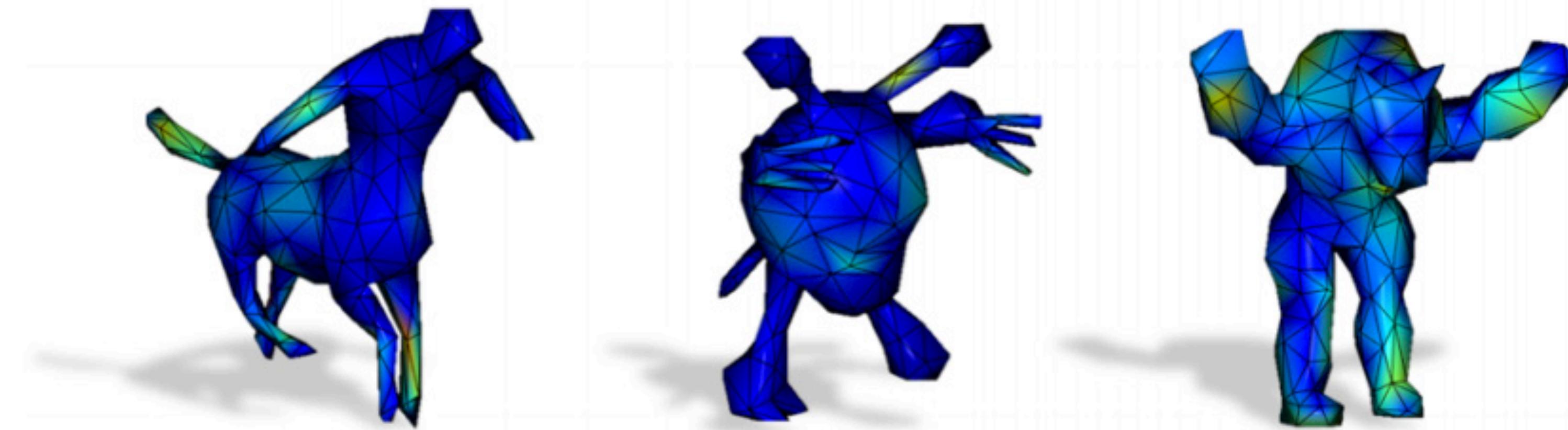
# Mesh Pooling via Edge Contraction



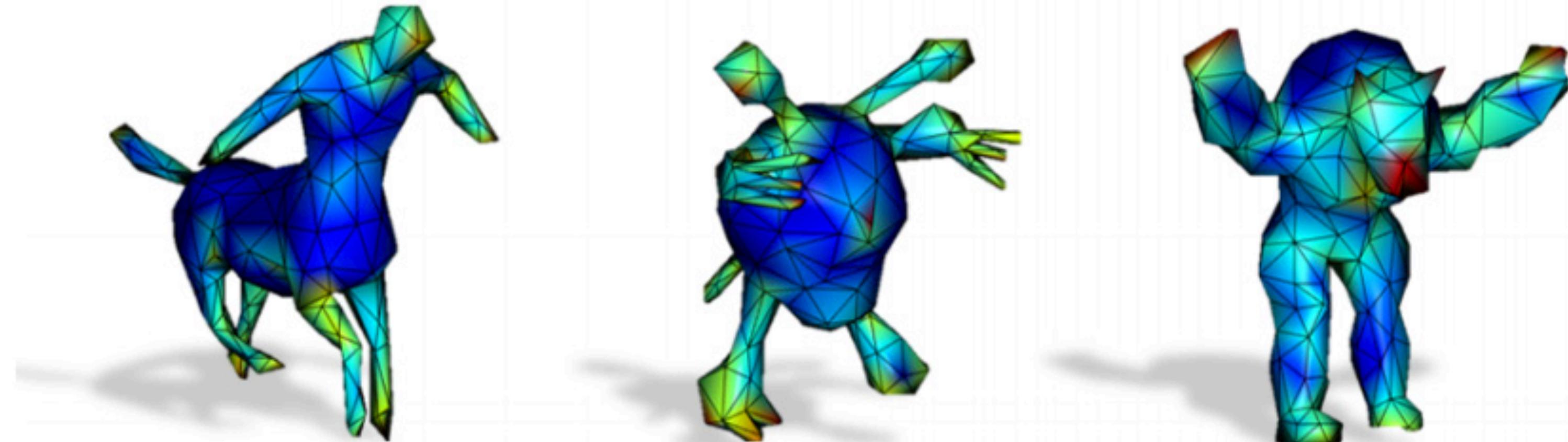
# Enhanced mesh pooling



# Enhanced mesh pooling

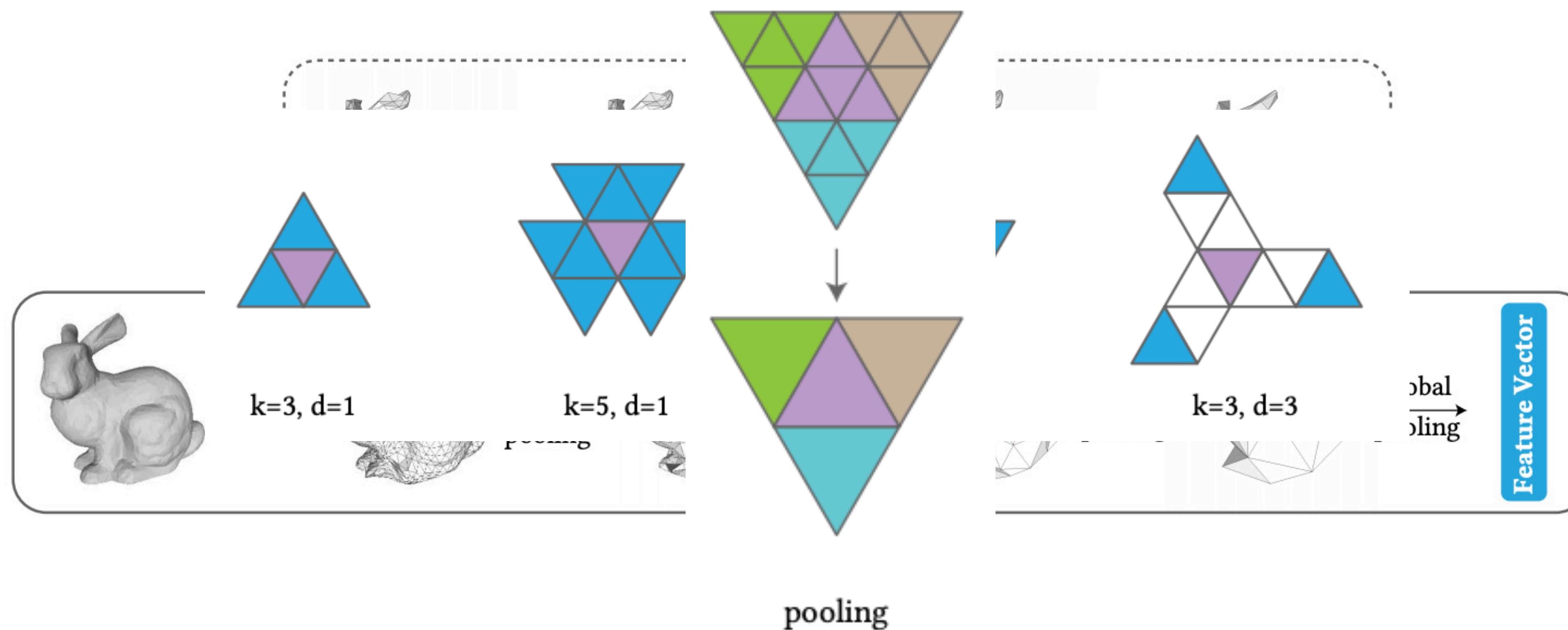


Original mesh pooling

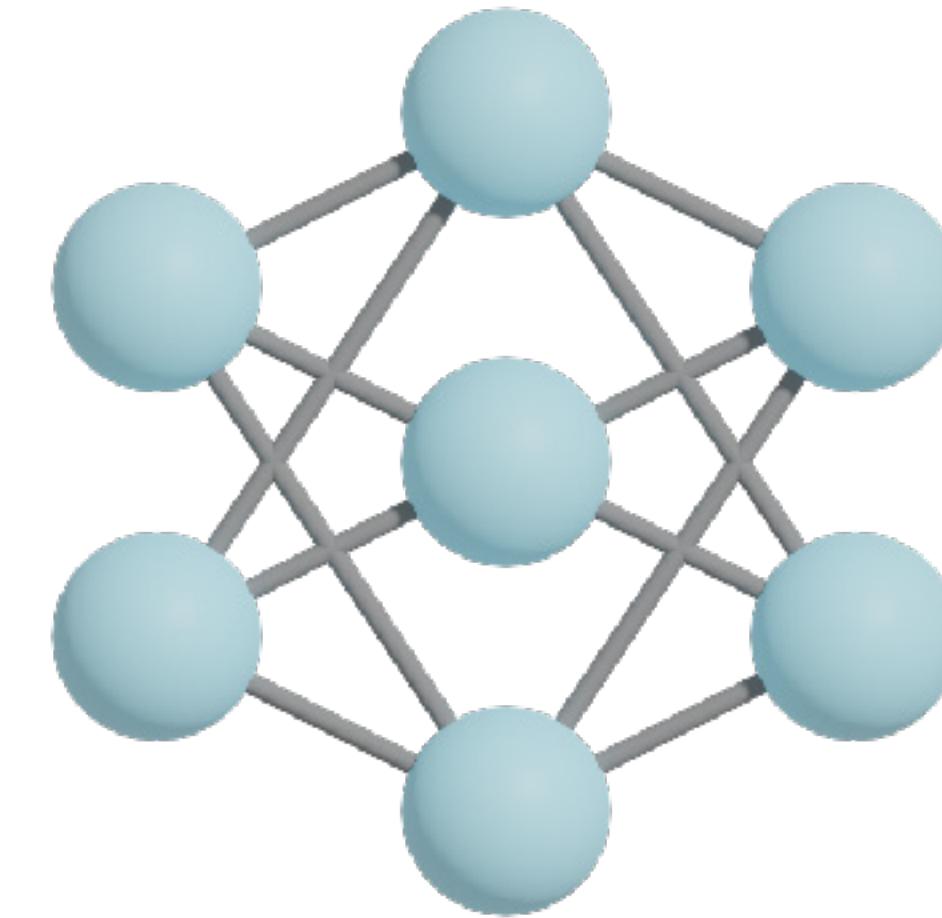
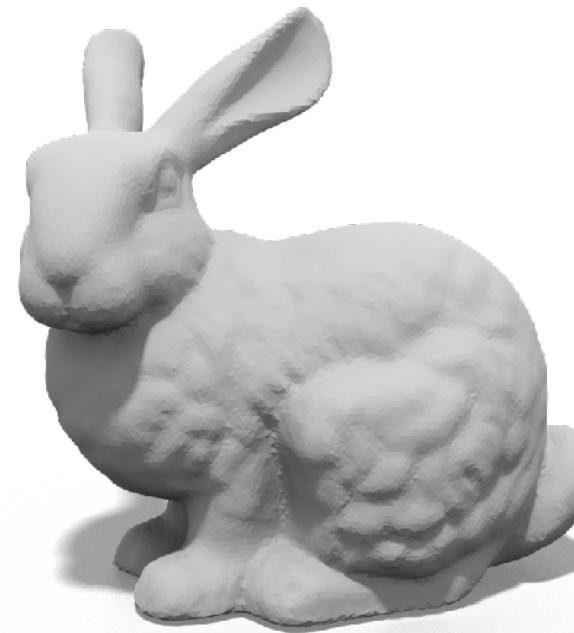


Enhanced mesh pooling

# Convolution and pooling from subdivision



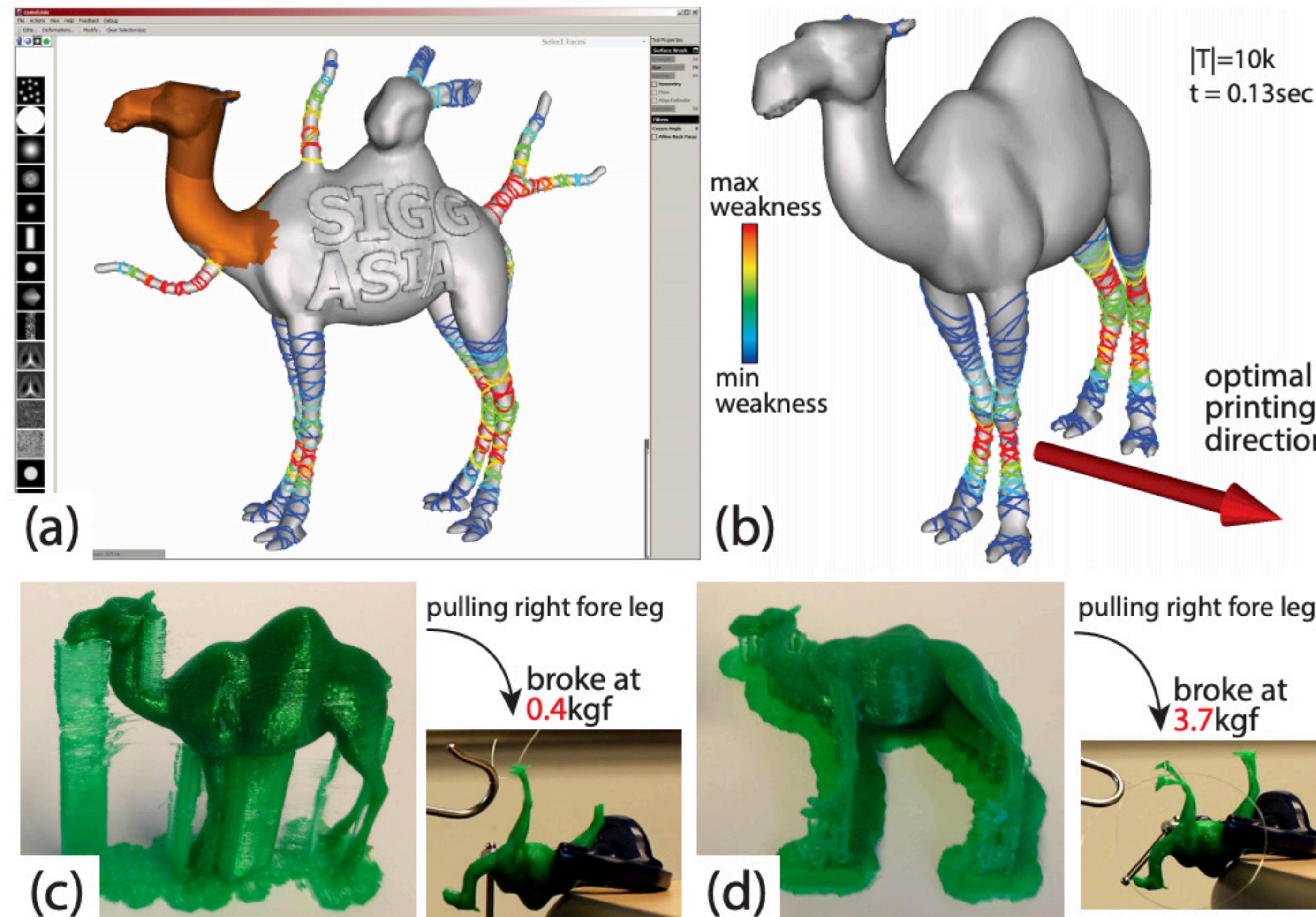
# Invariance to rigid transformations



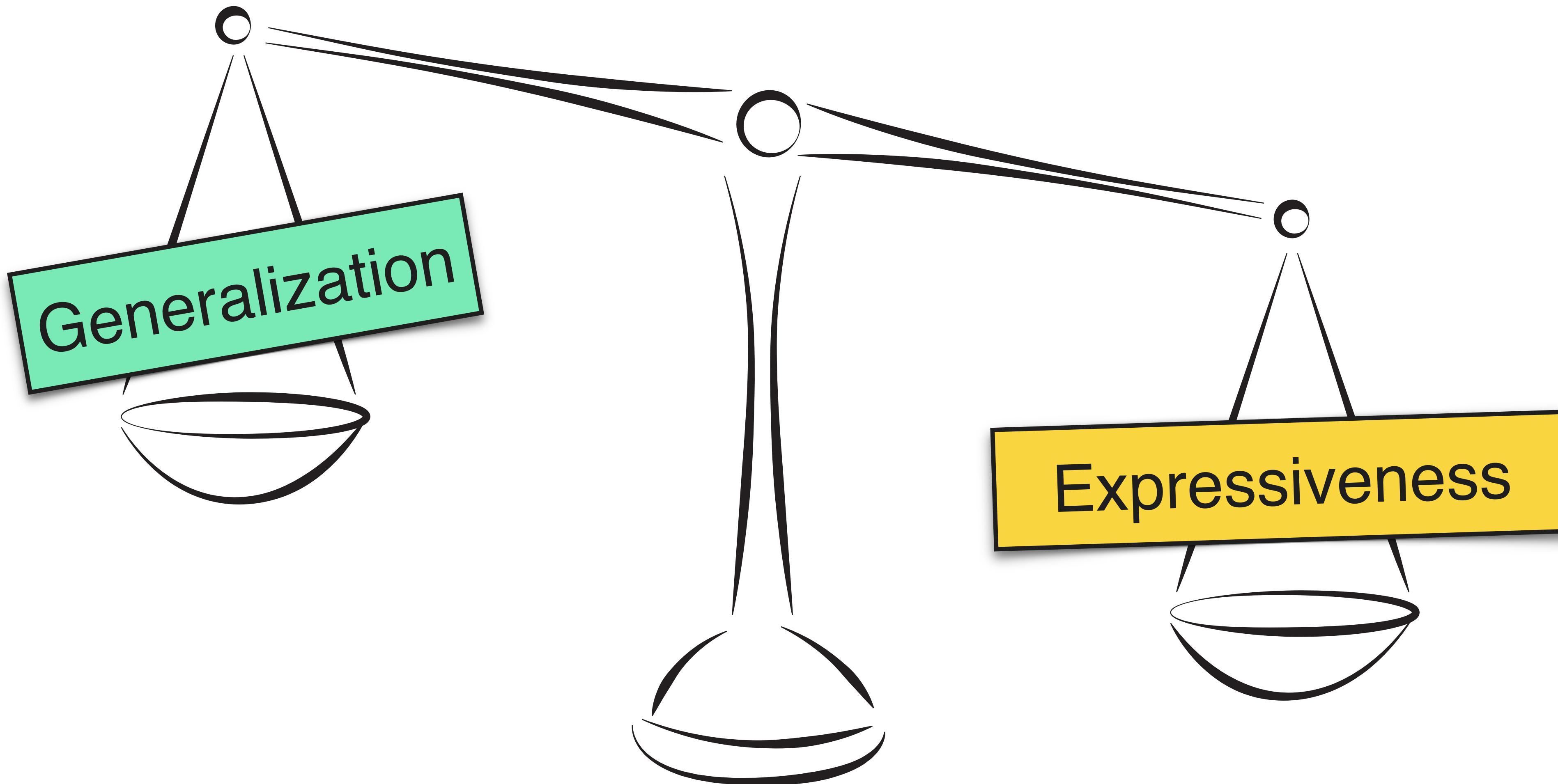
*still*  
↓  
**It's a bunny**

# Invariance to rigid transformations

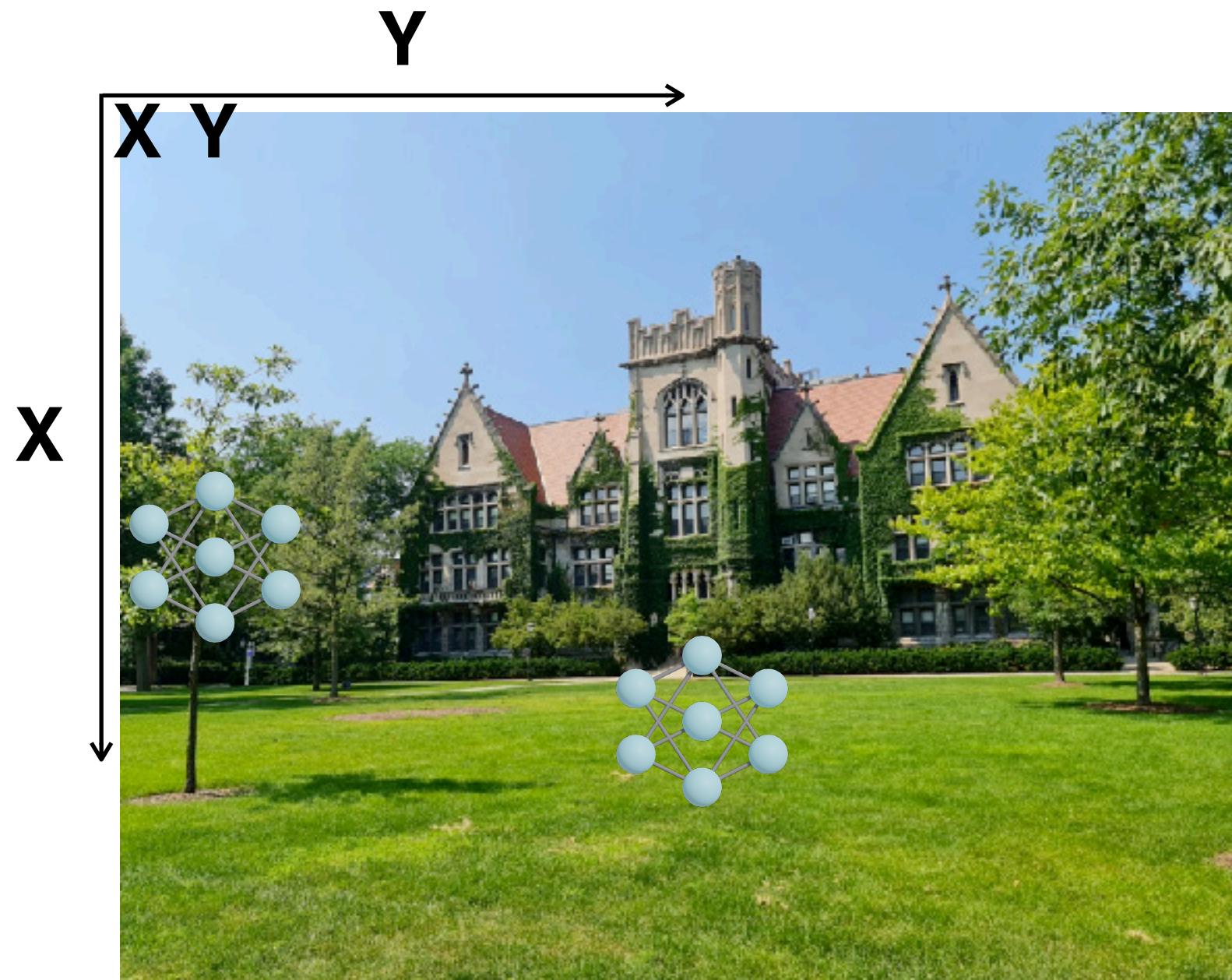
... sometimes this can be too restrictive



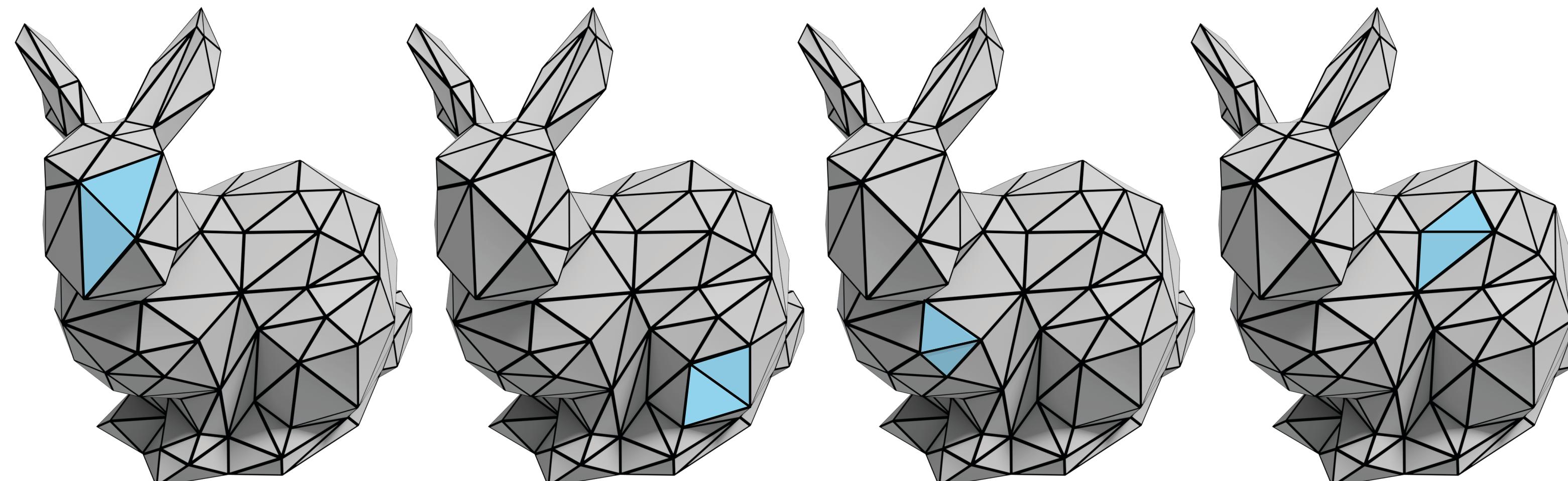
# Expressiveness vs. Generalization



# Break shift-invariance

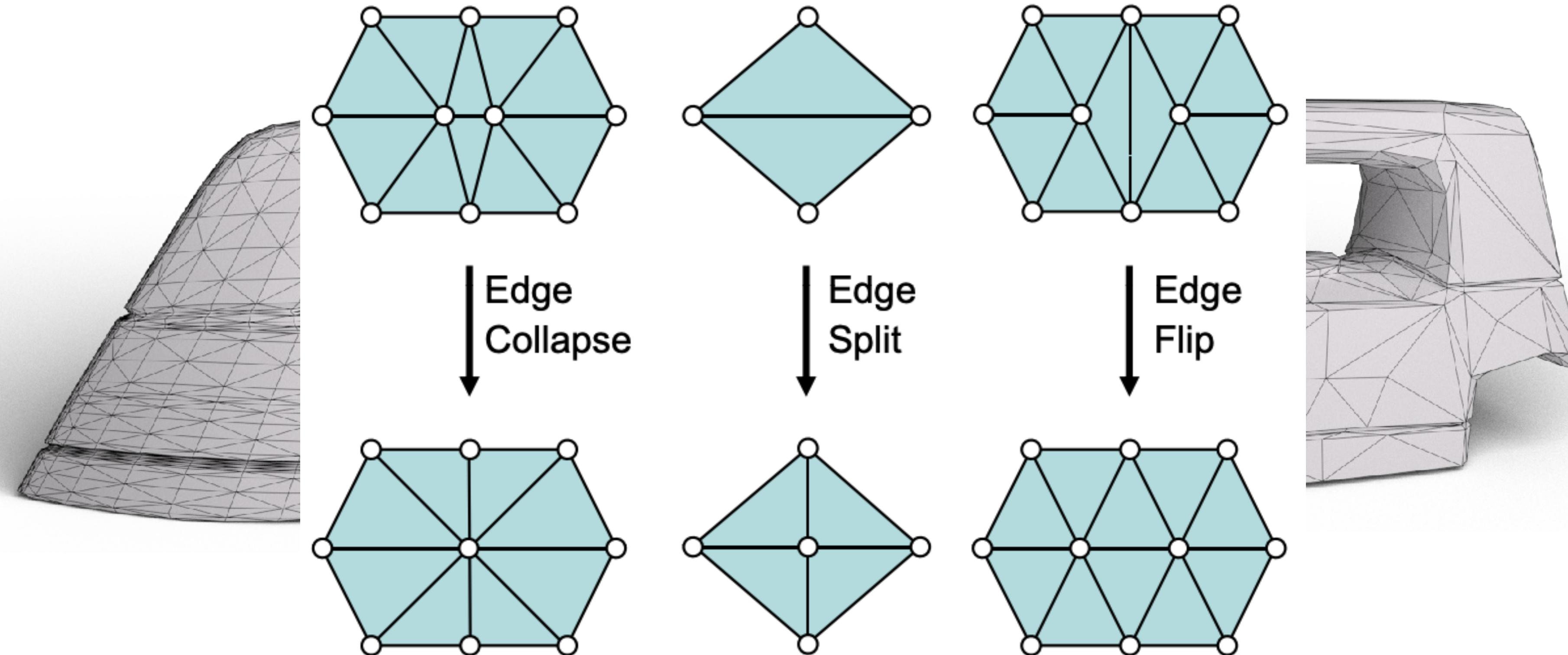


**Gain expressive power**  
**Helps better fit the data**

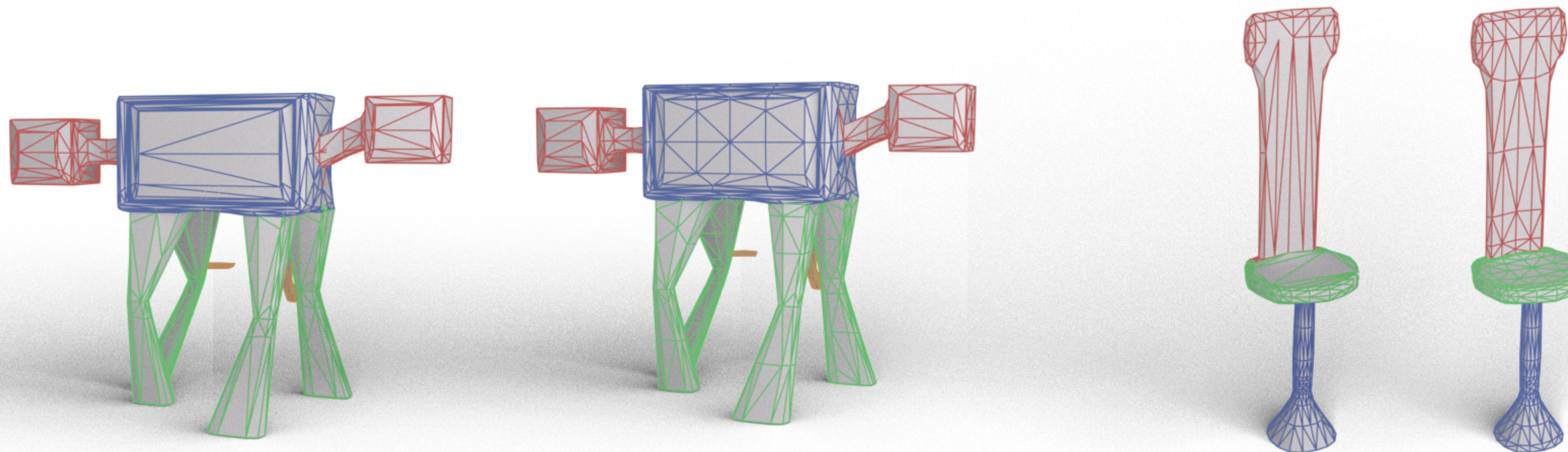


# Triangulation robustness

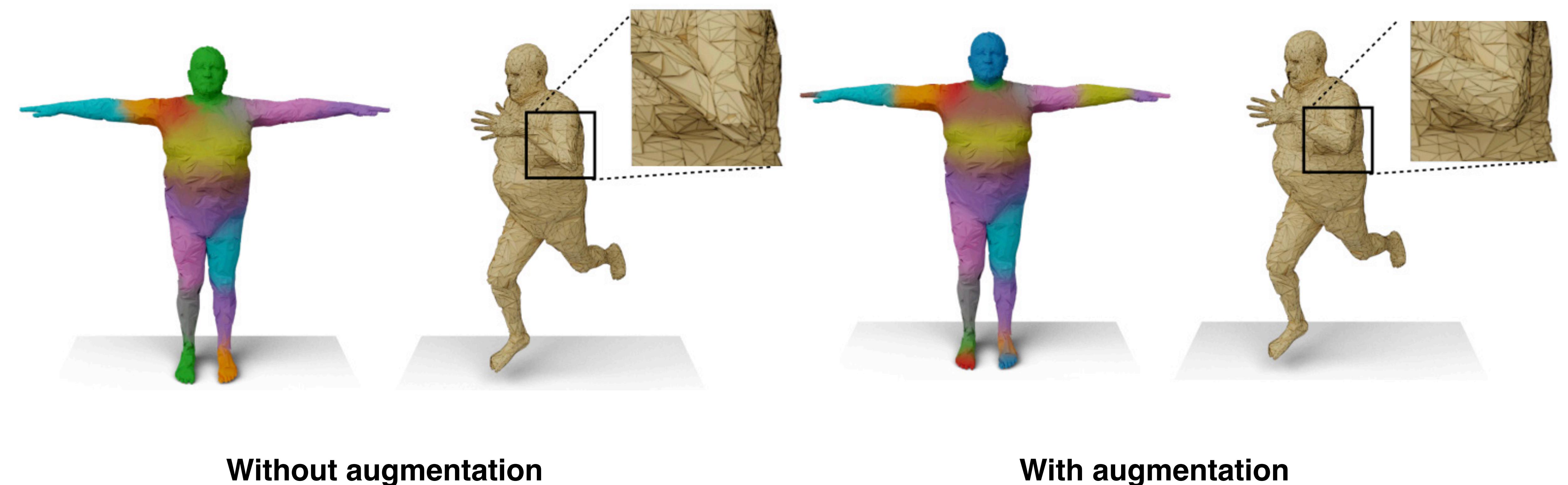
Perform simple augmentations



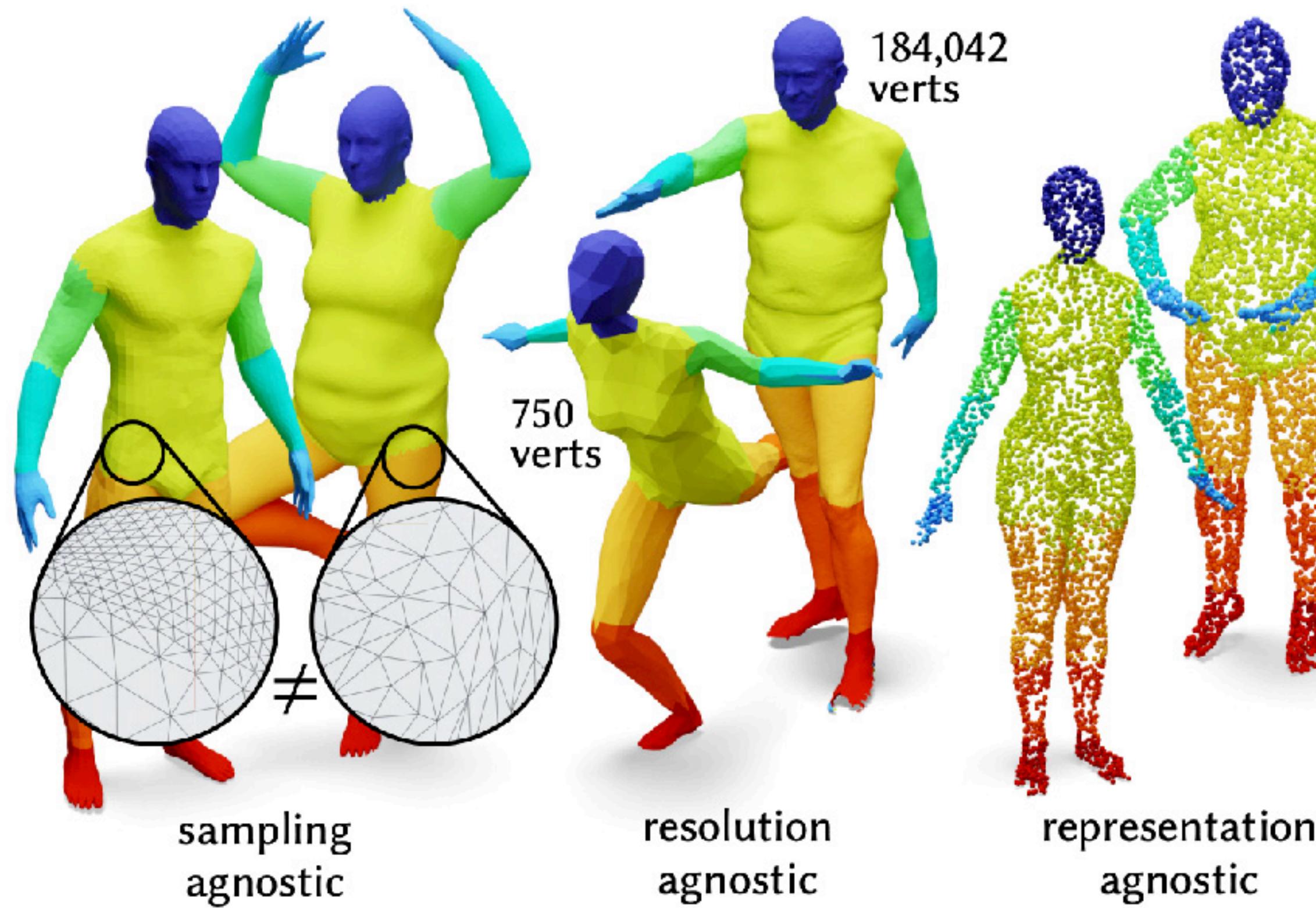
# Triangulation robustness in segmentation



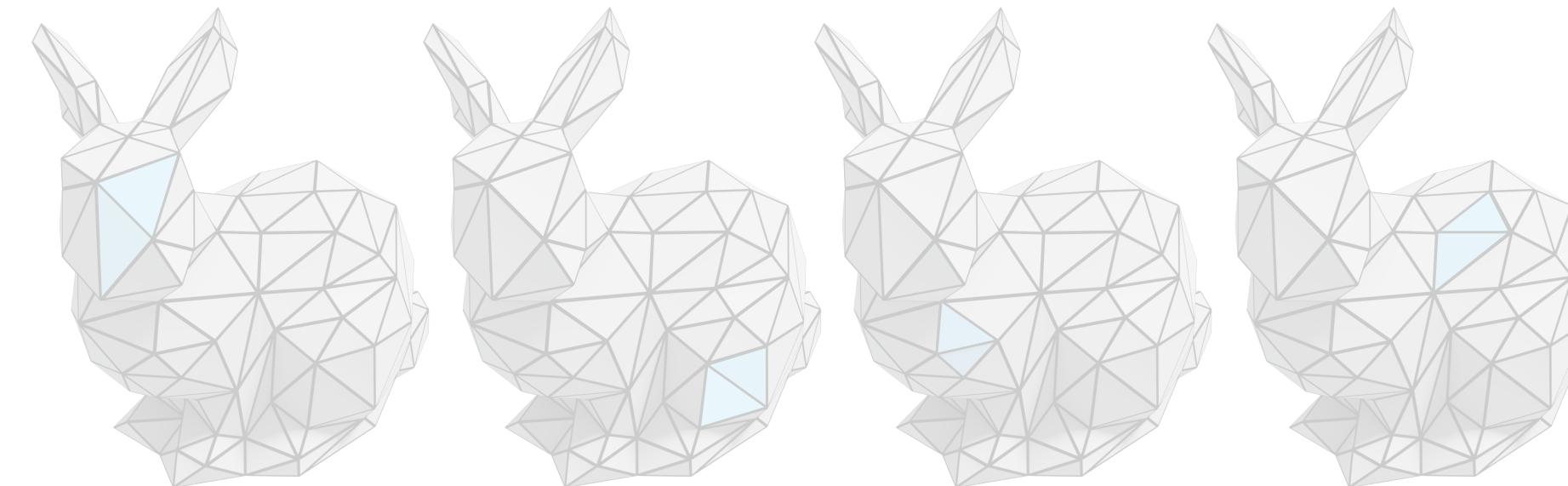
# Triangulation robustness in deformation



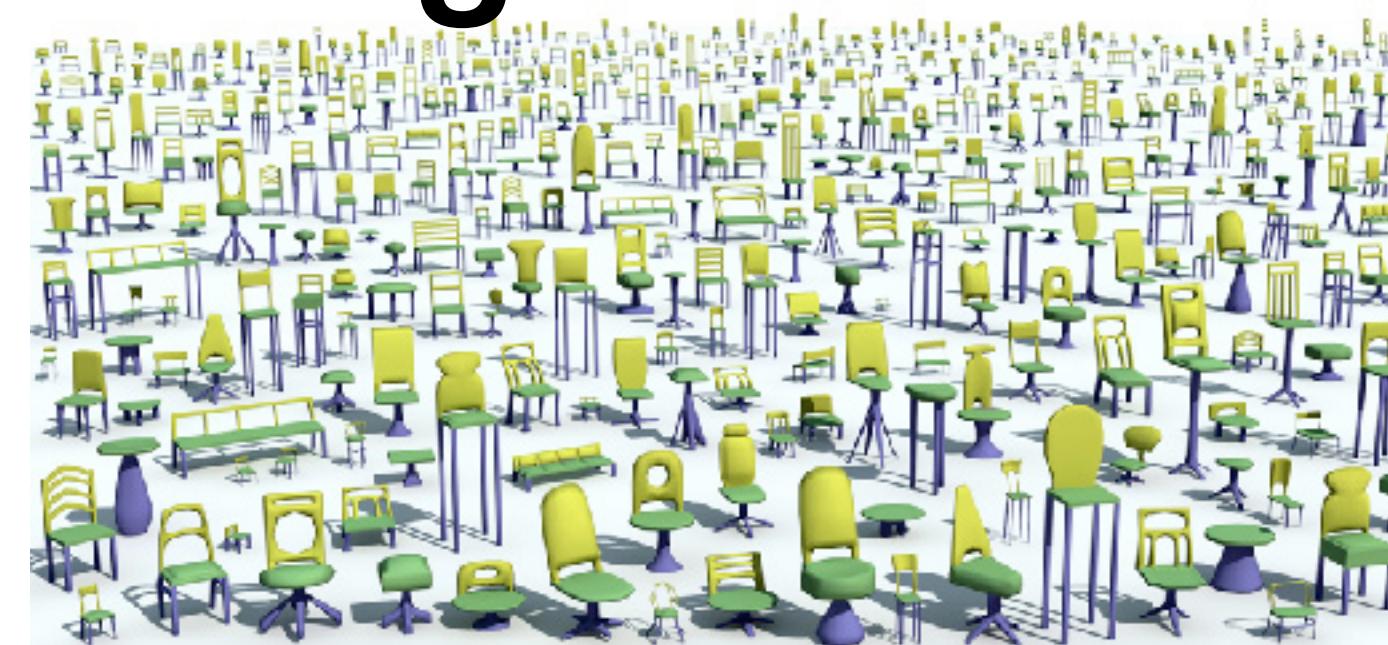
# Triangulation robustness via diffusion



# Mesh Convolutional Neural Networks



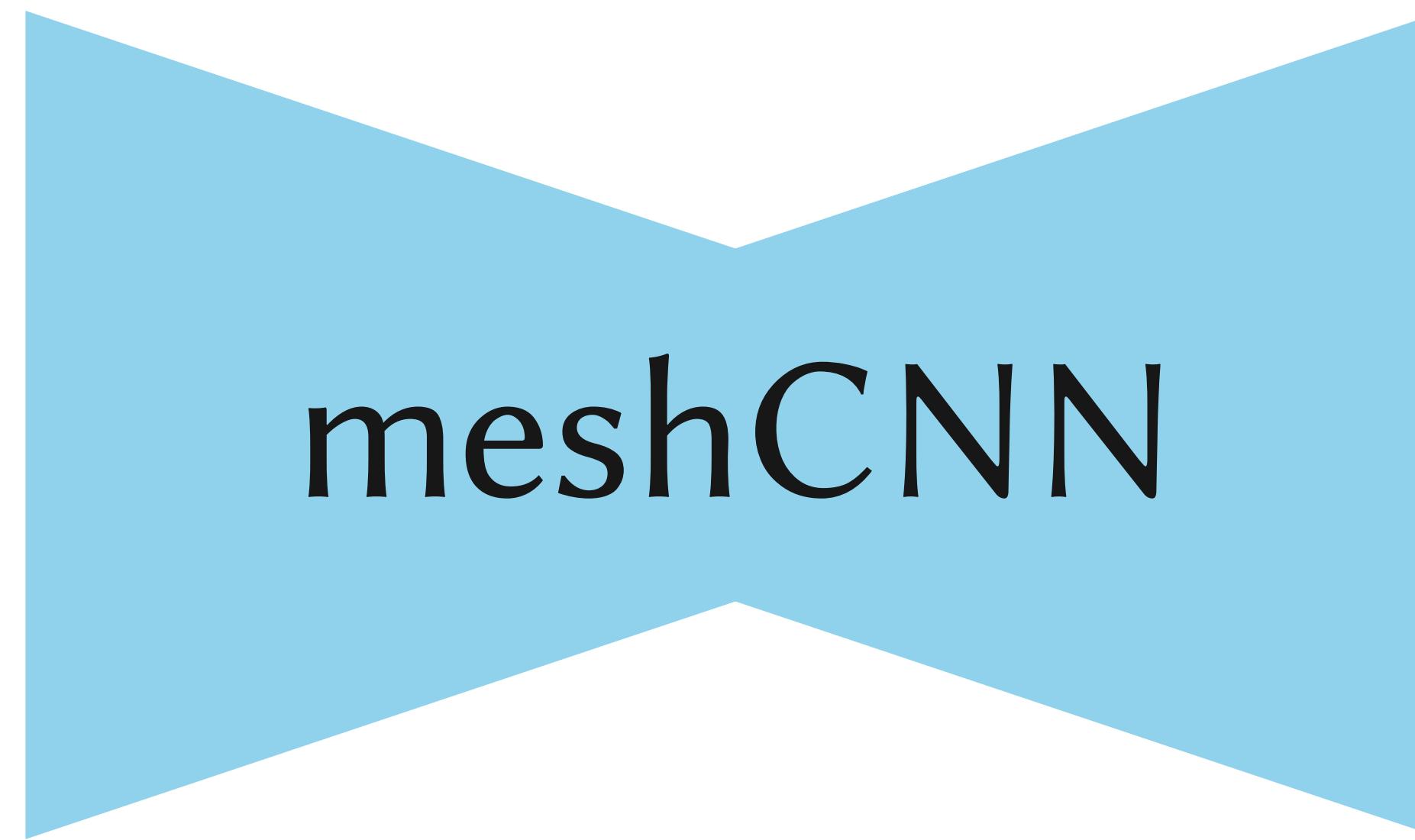
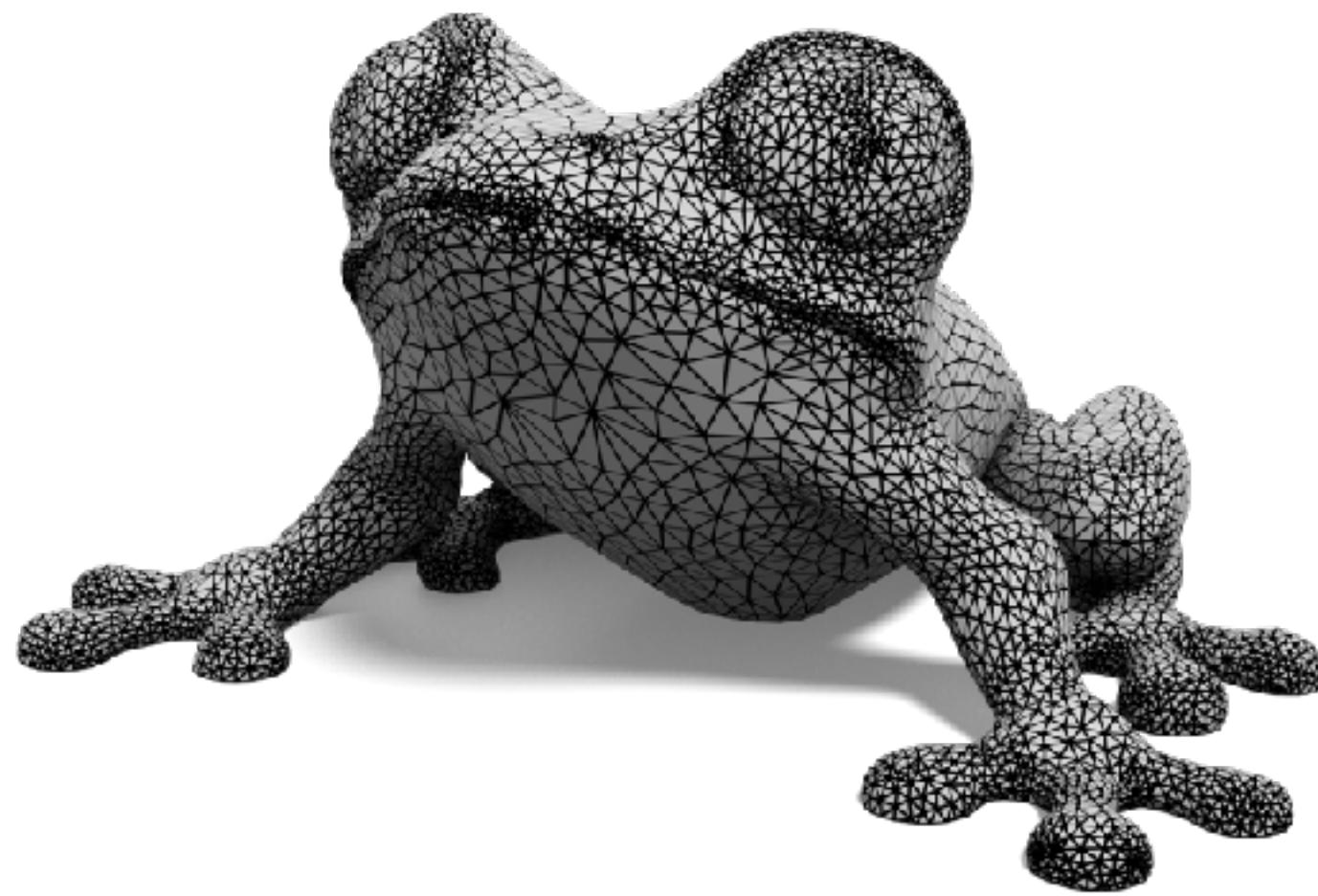
## Machine Learning & Geometry Processing



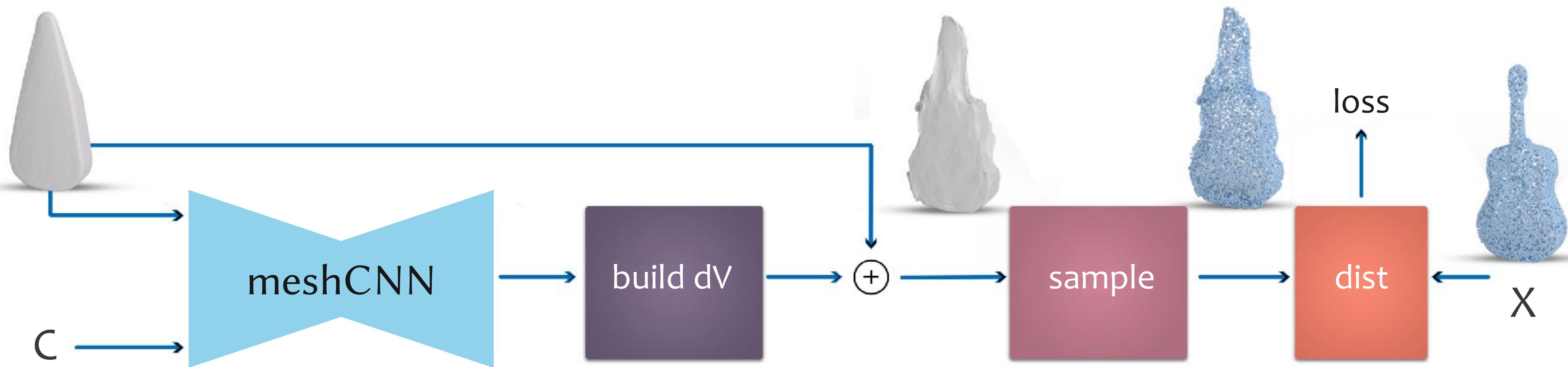
## Learning from a Single Mesh



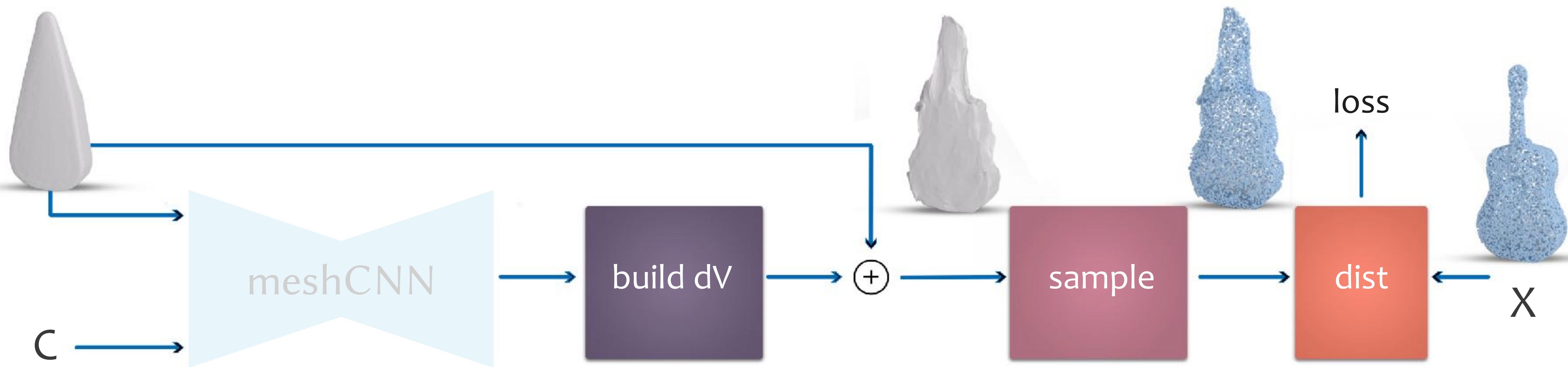
# A Fundamental Tool: MeshCNN

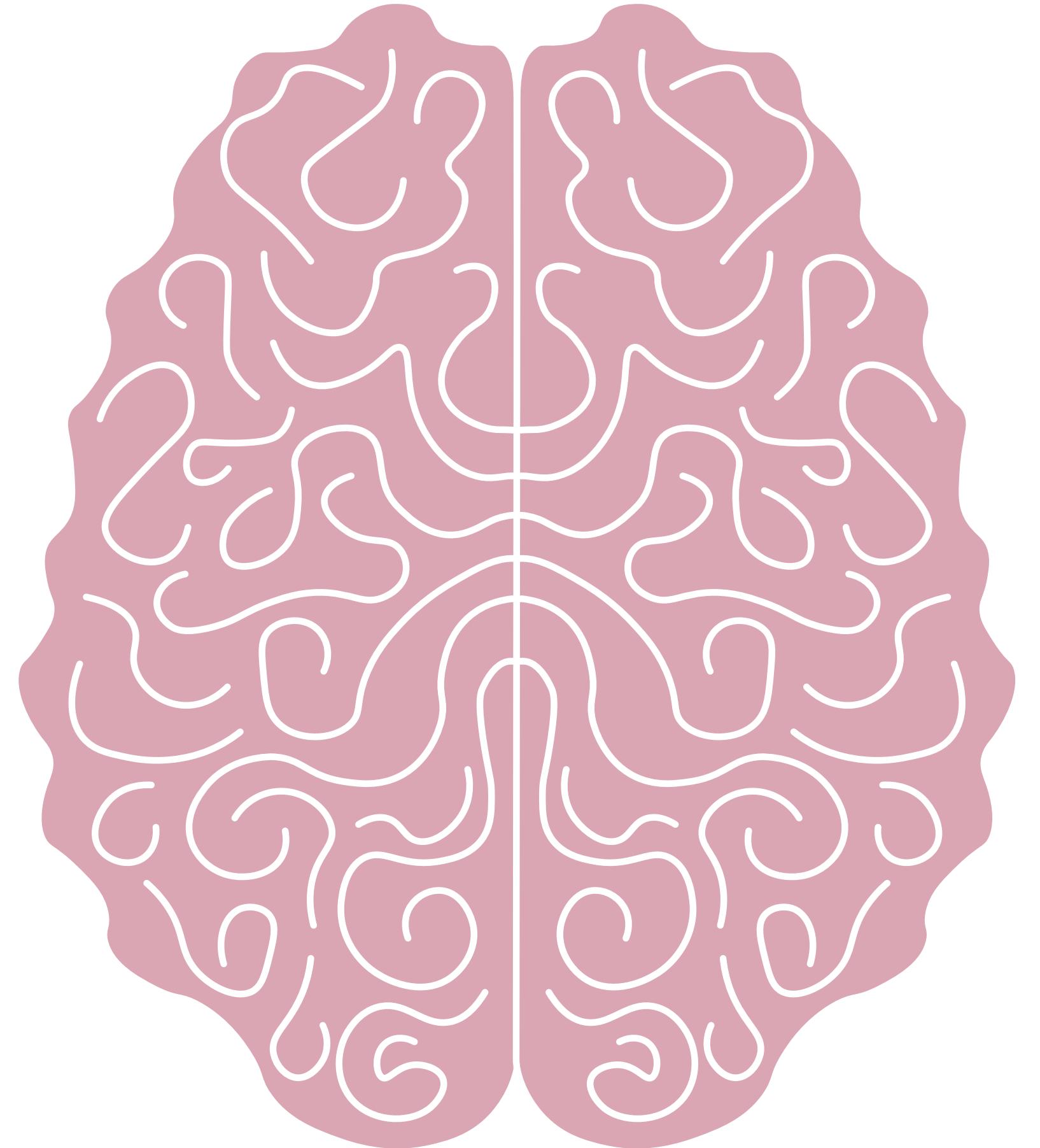


# A Small Component

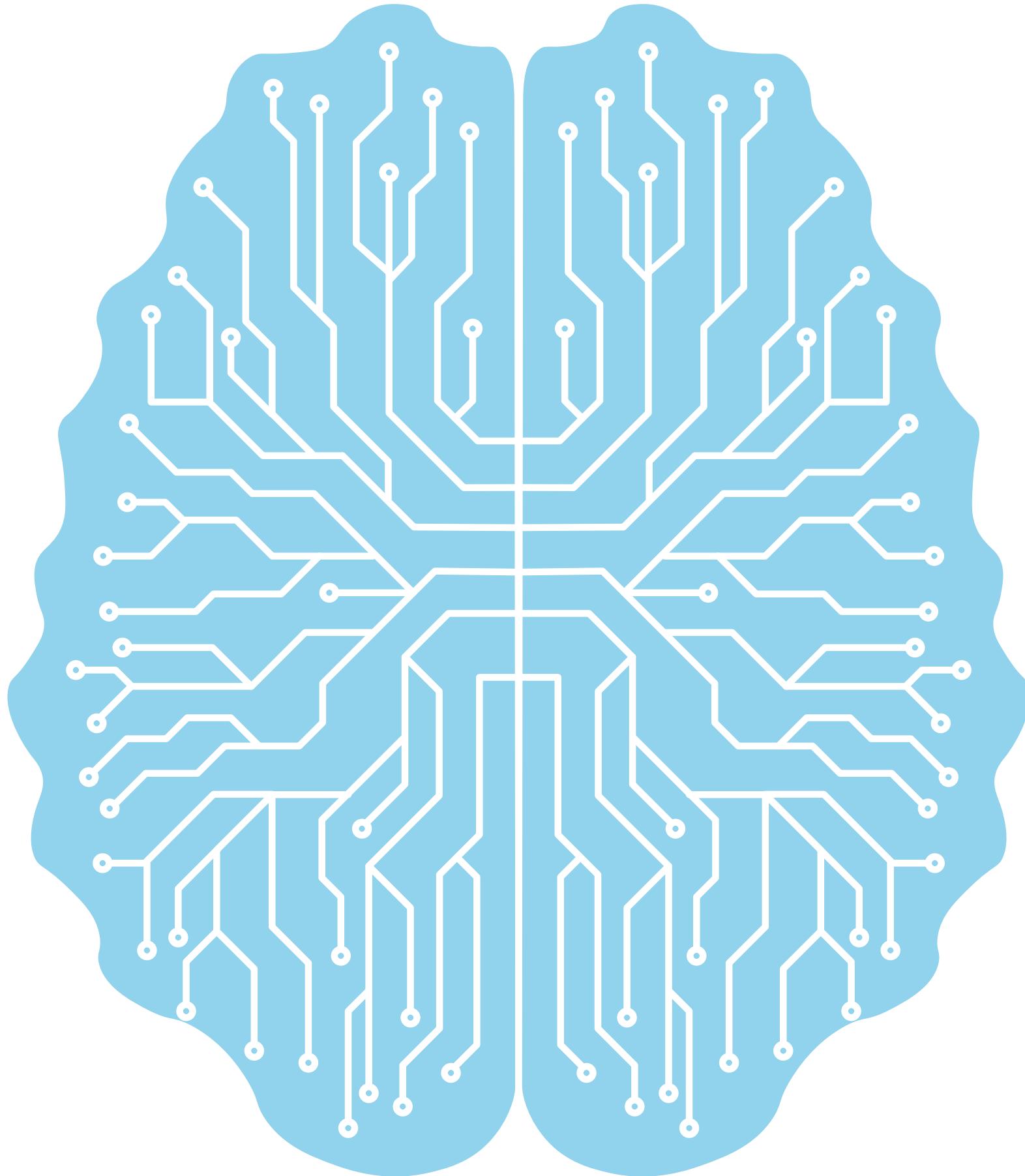


# A Small Component





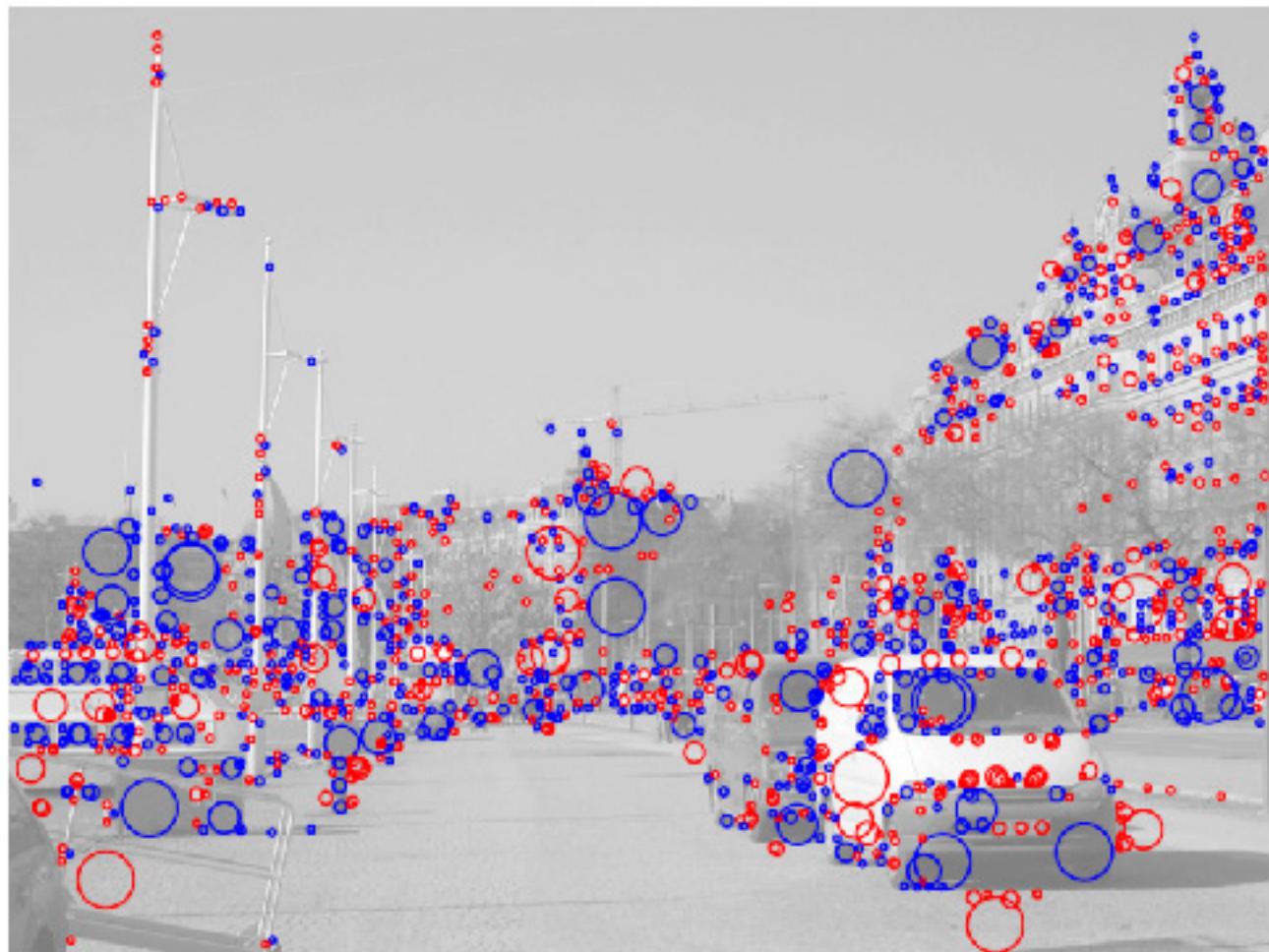
VS



# Image Processing



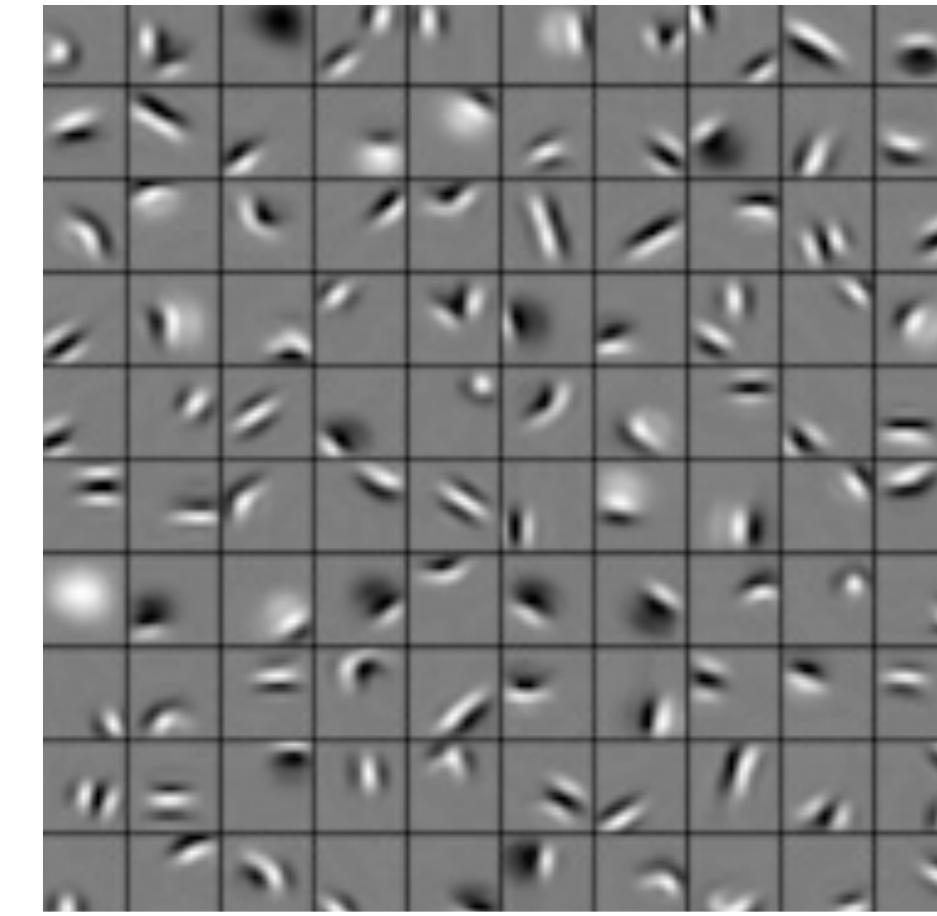
SIFT  
[Lowe 1999]



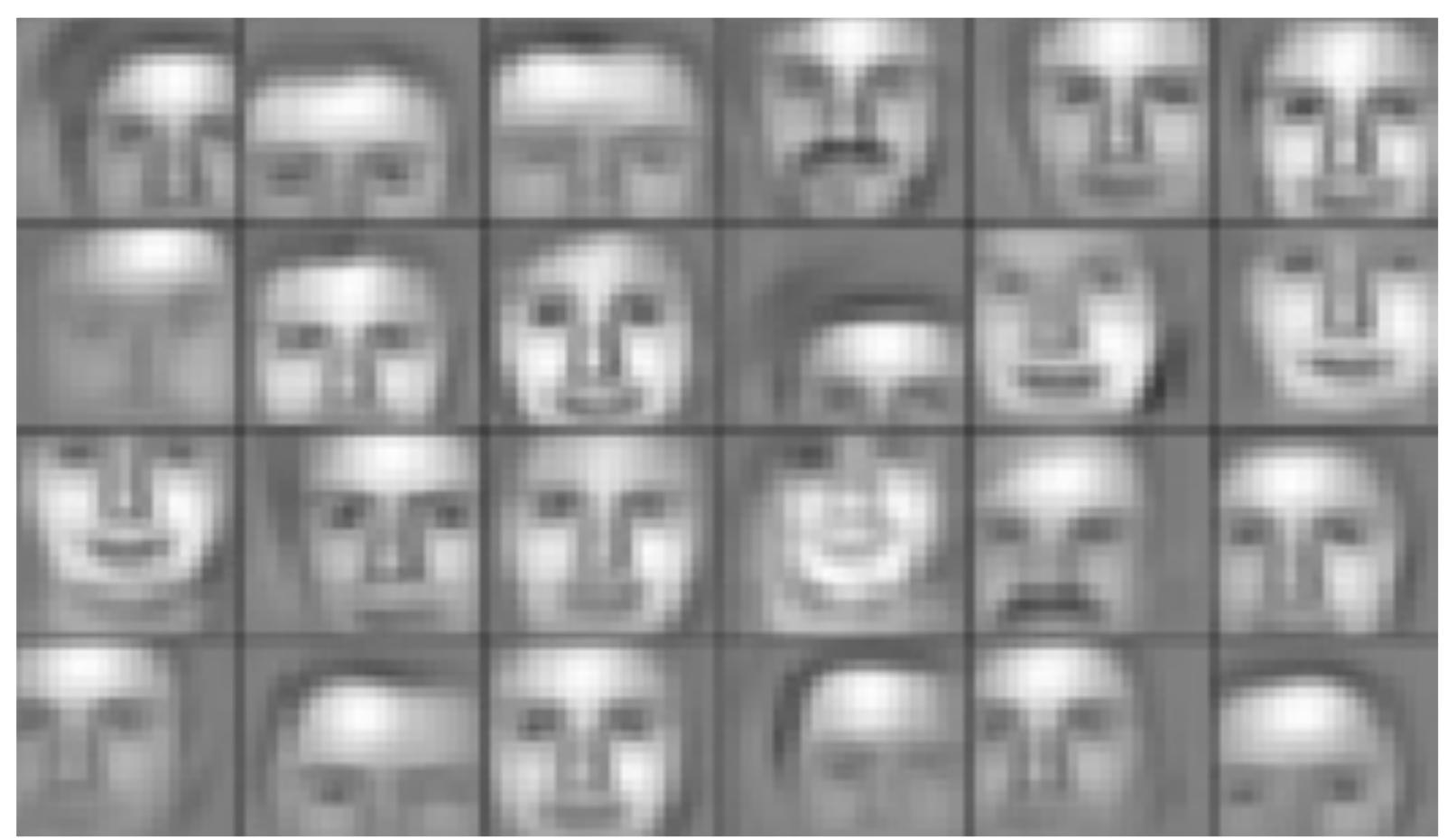
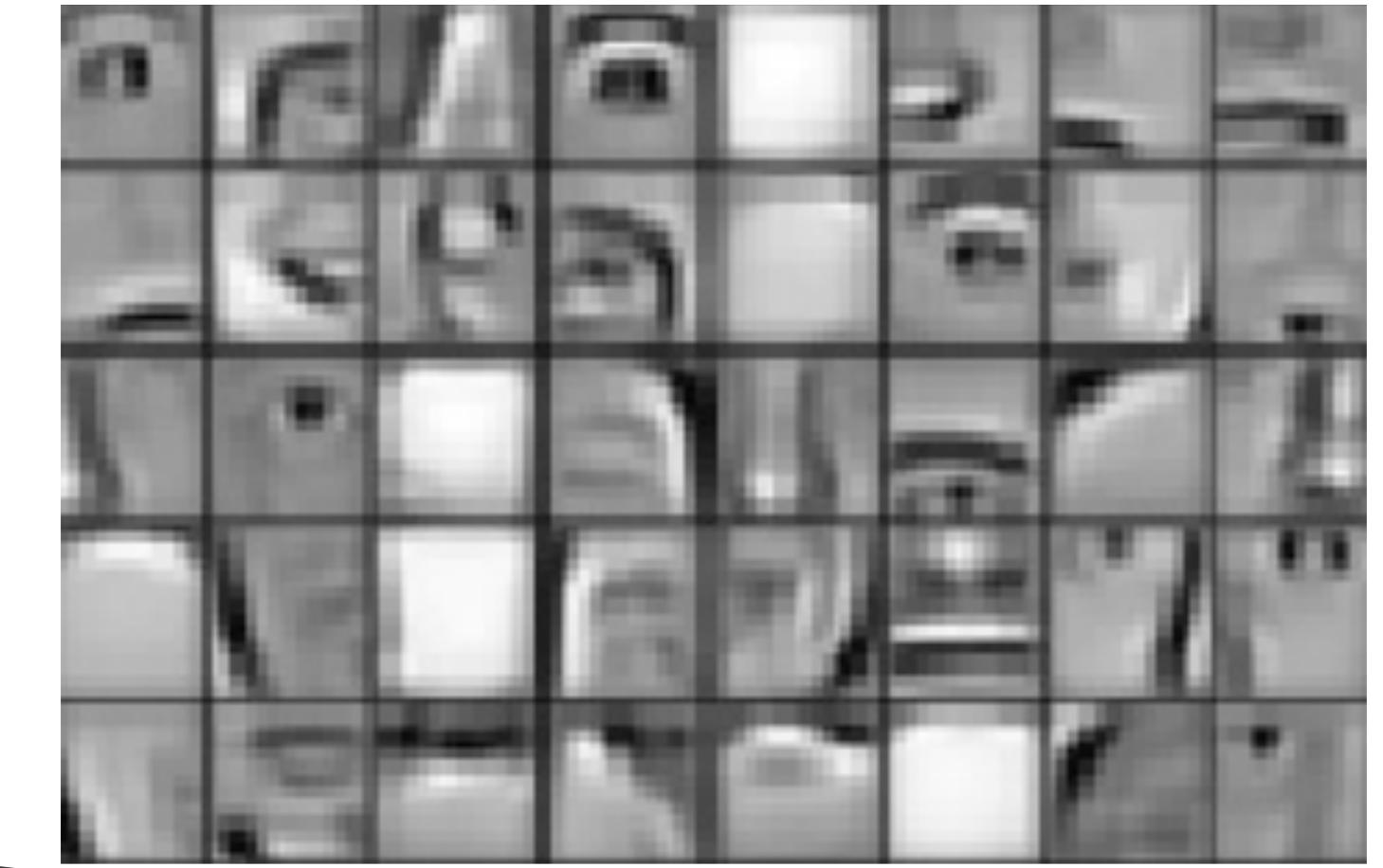
# Image Processing



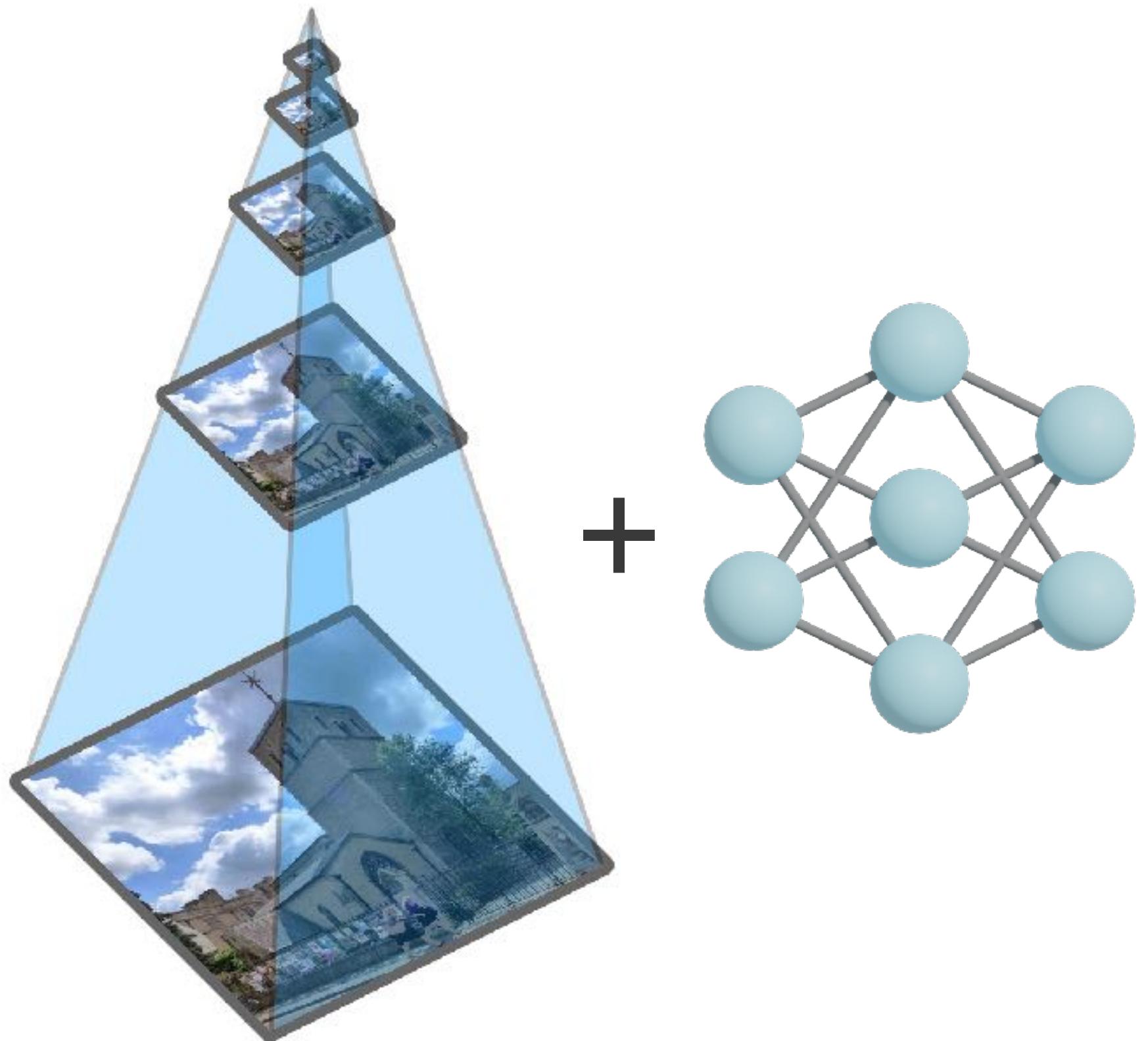
SIFT  
[Lowe 1999]



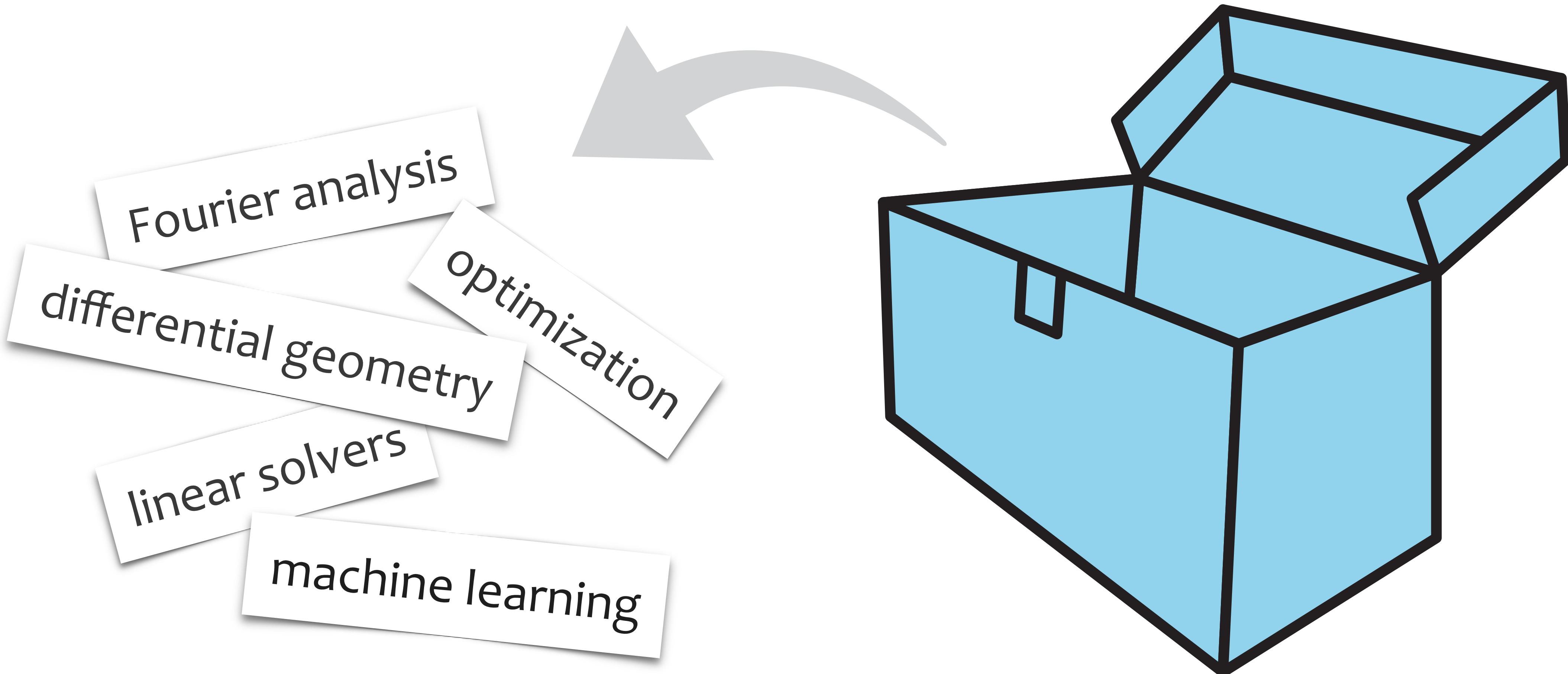
learned  
features



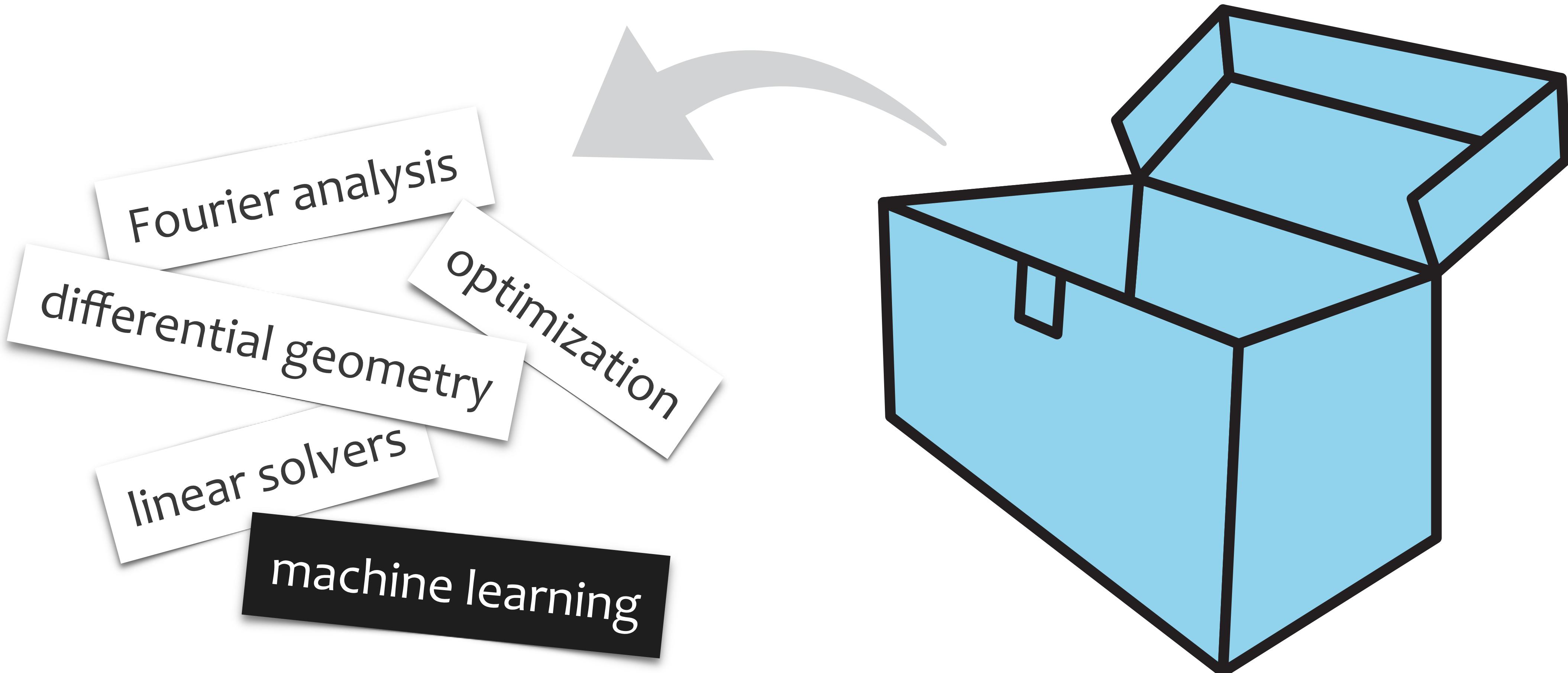
# E.g., Optimal Flow via Pyramid



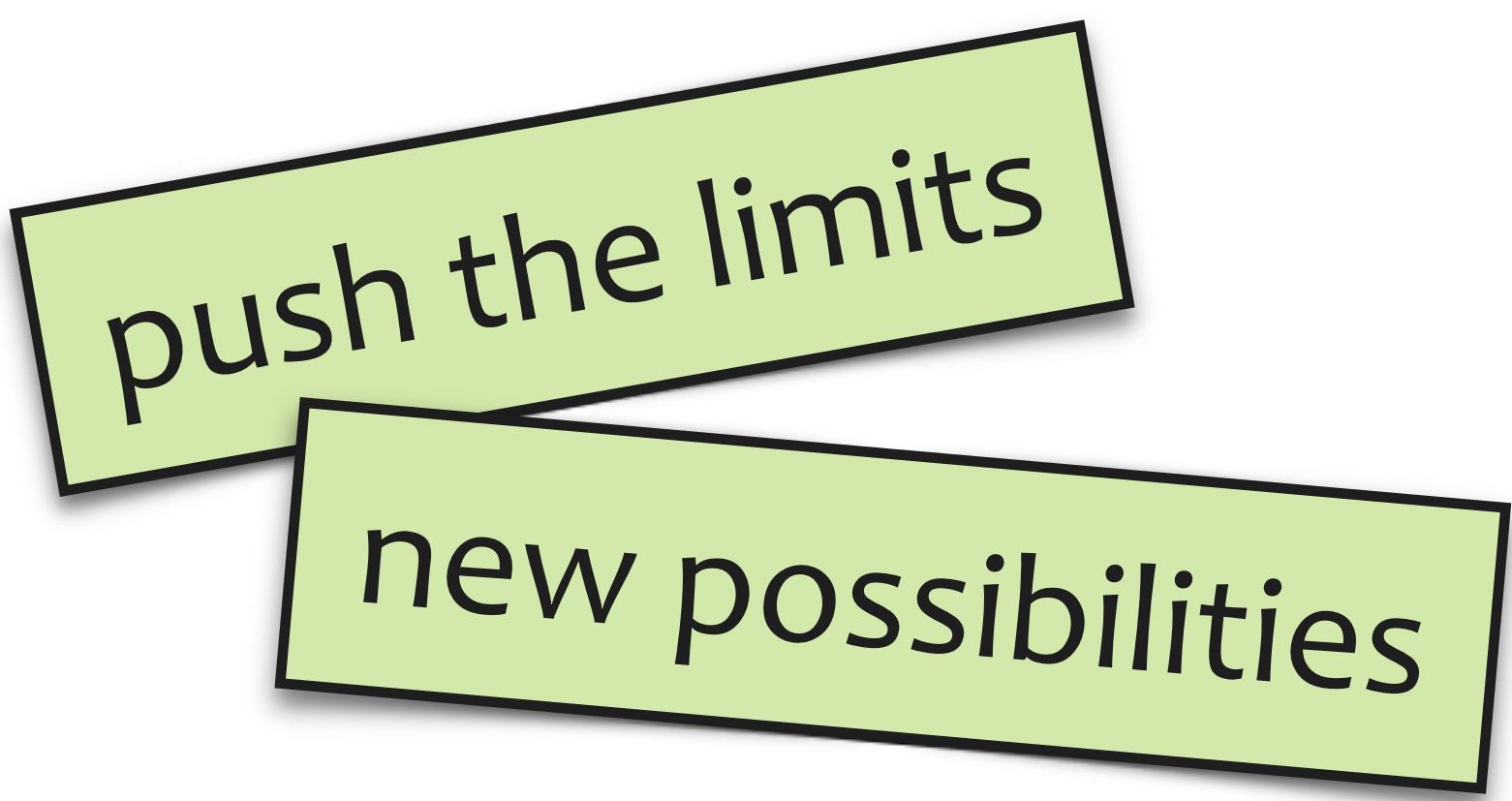
# A tool in our toolbox



# A tool in our toolbox



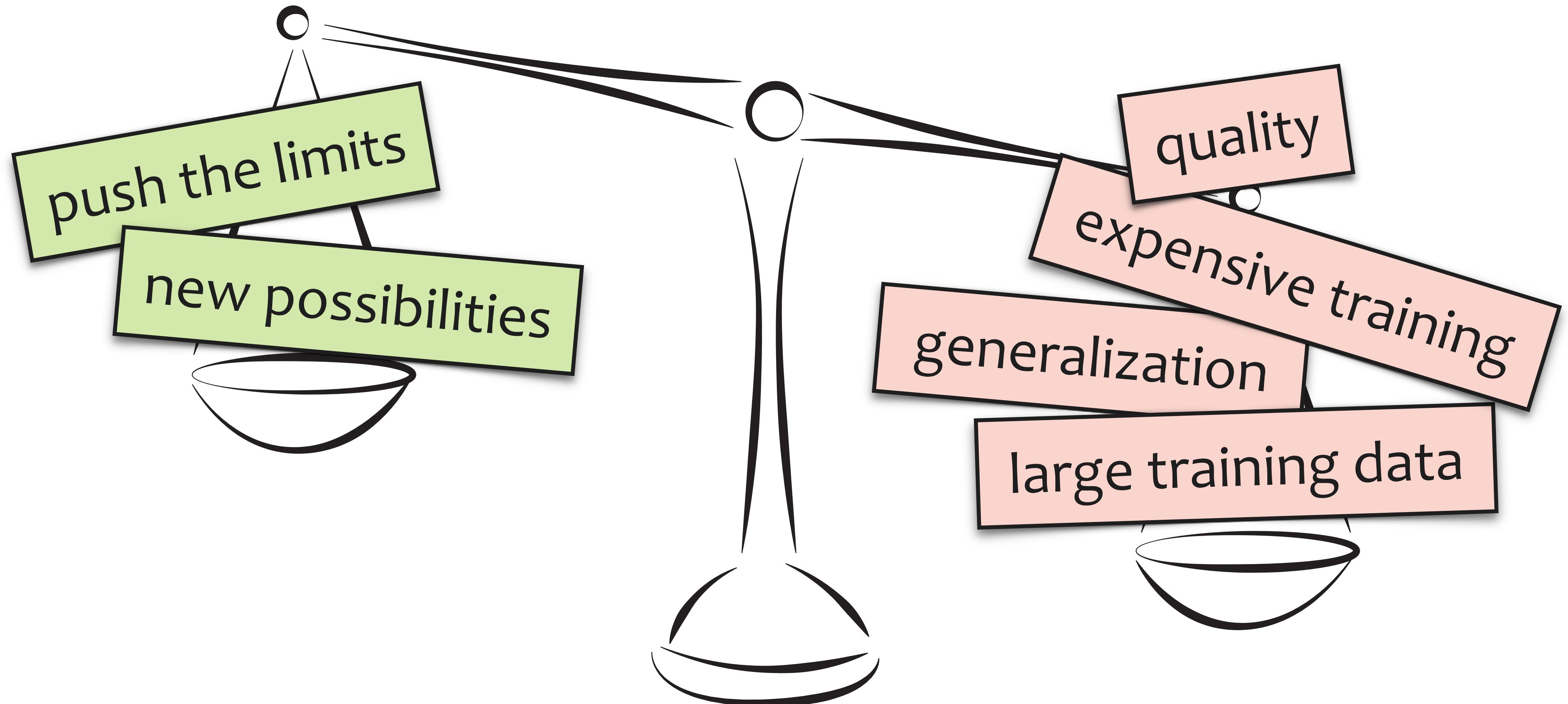
# No-free-lunch



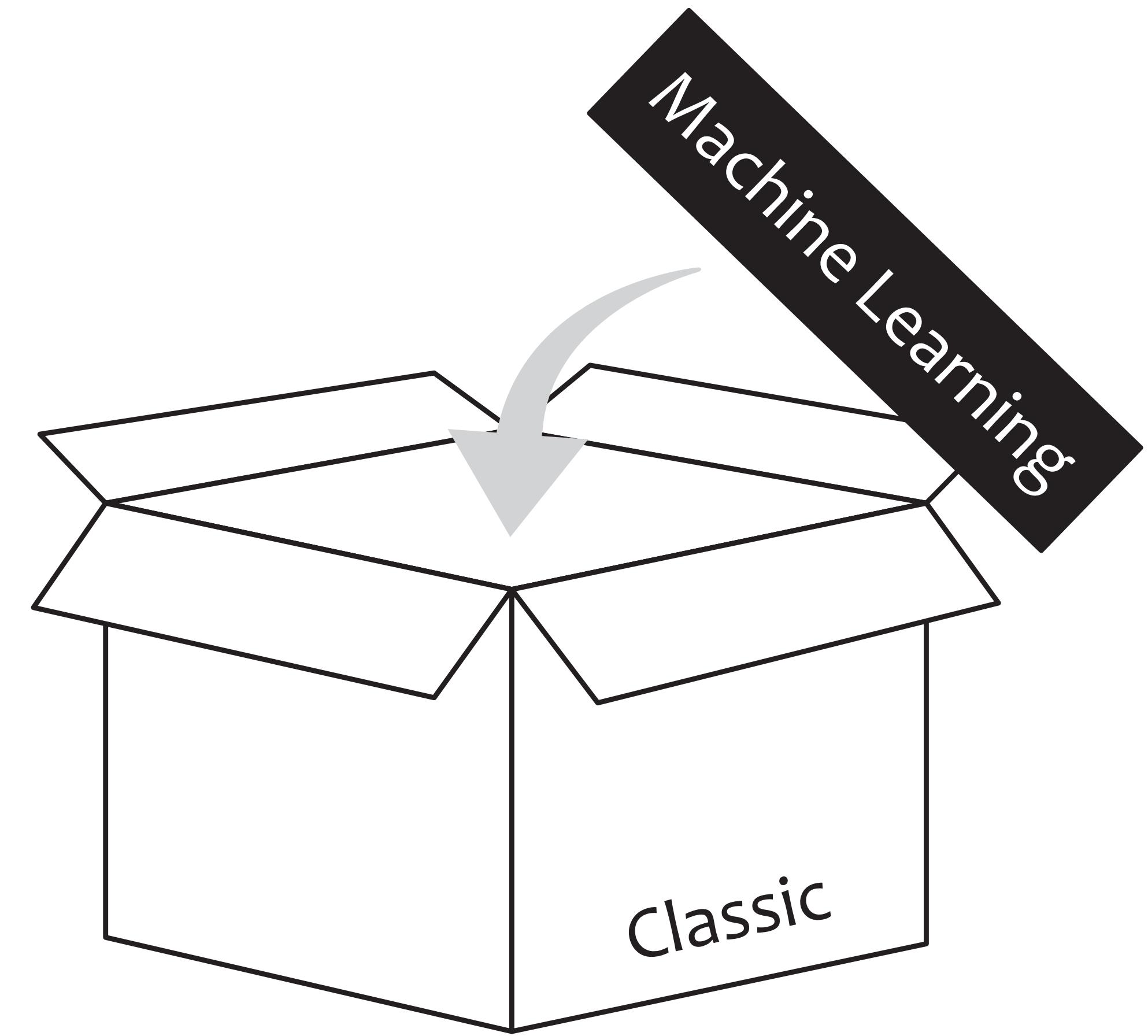
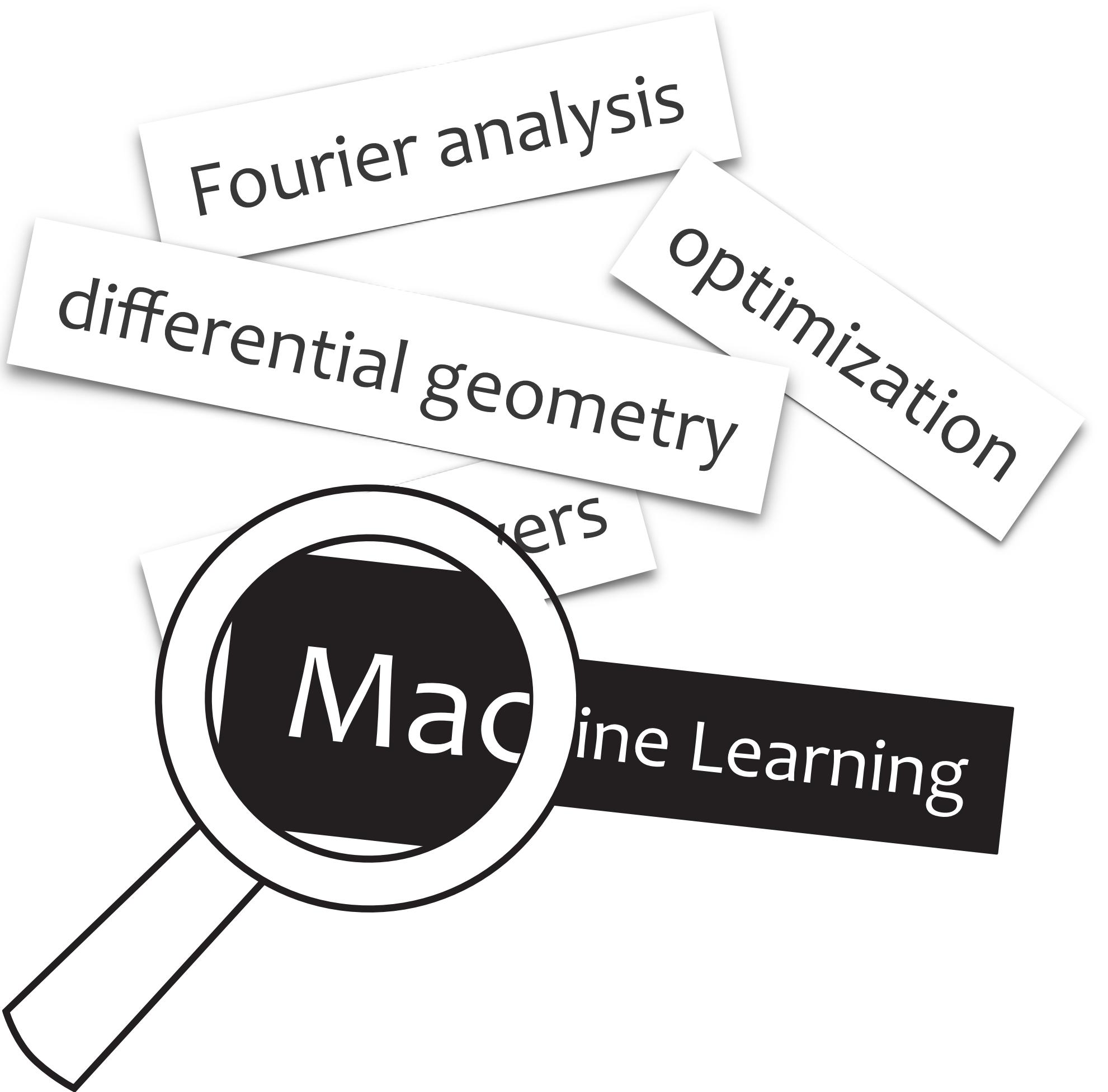
push the limits

new possibilities

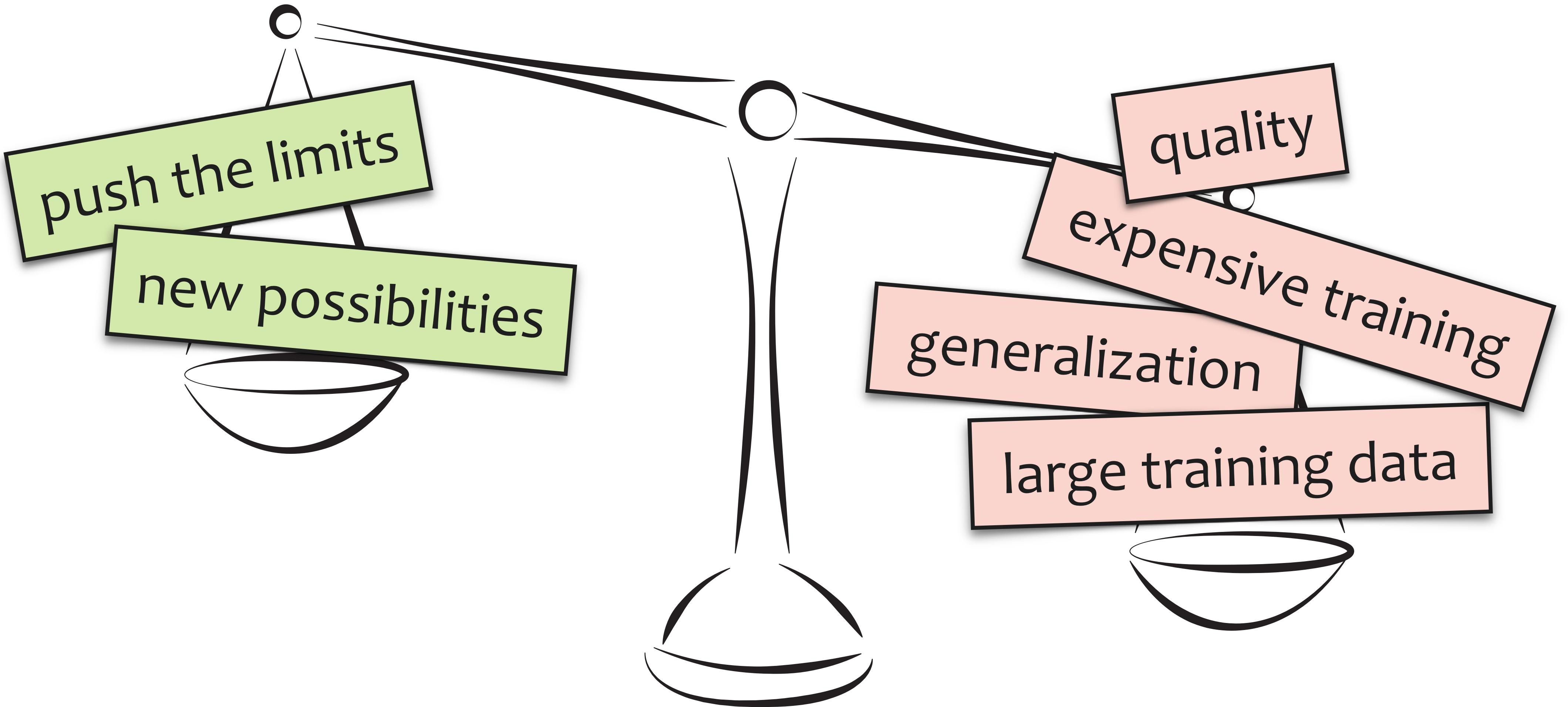
# No-free-lunch



# Overview



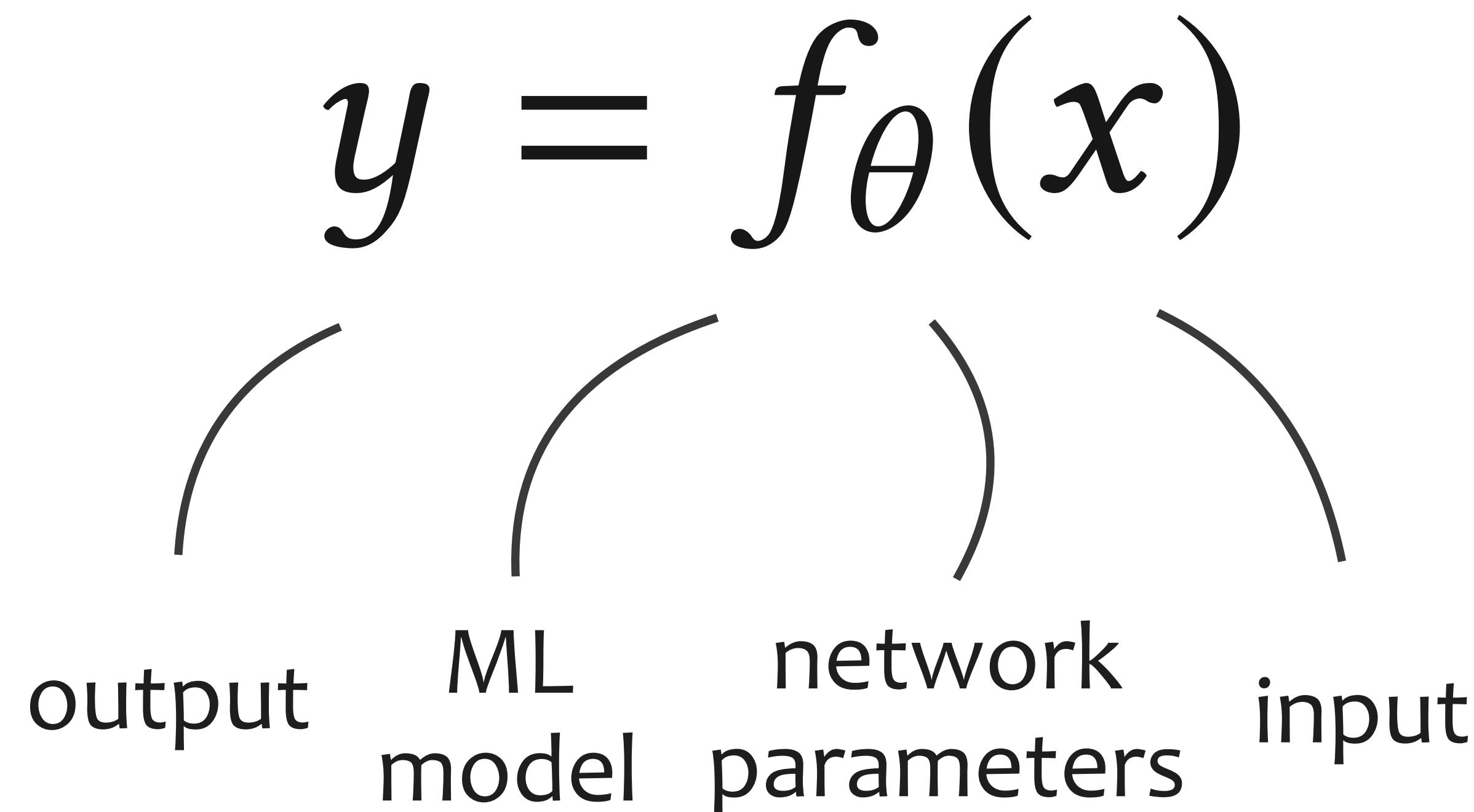
# Alleviate Limitations



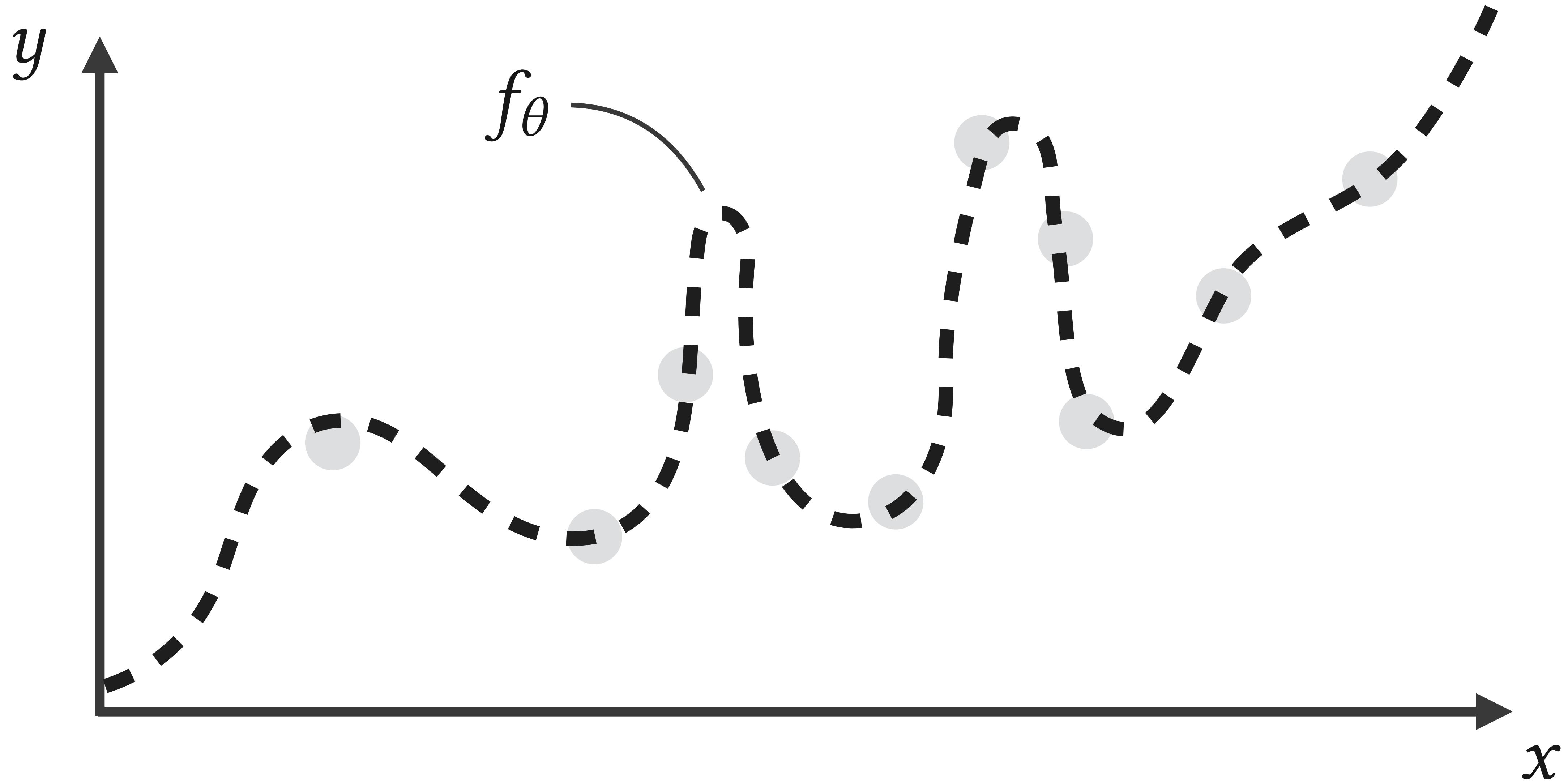
# ROLES OF MACHINE LEARNING



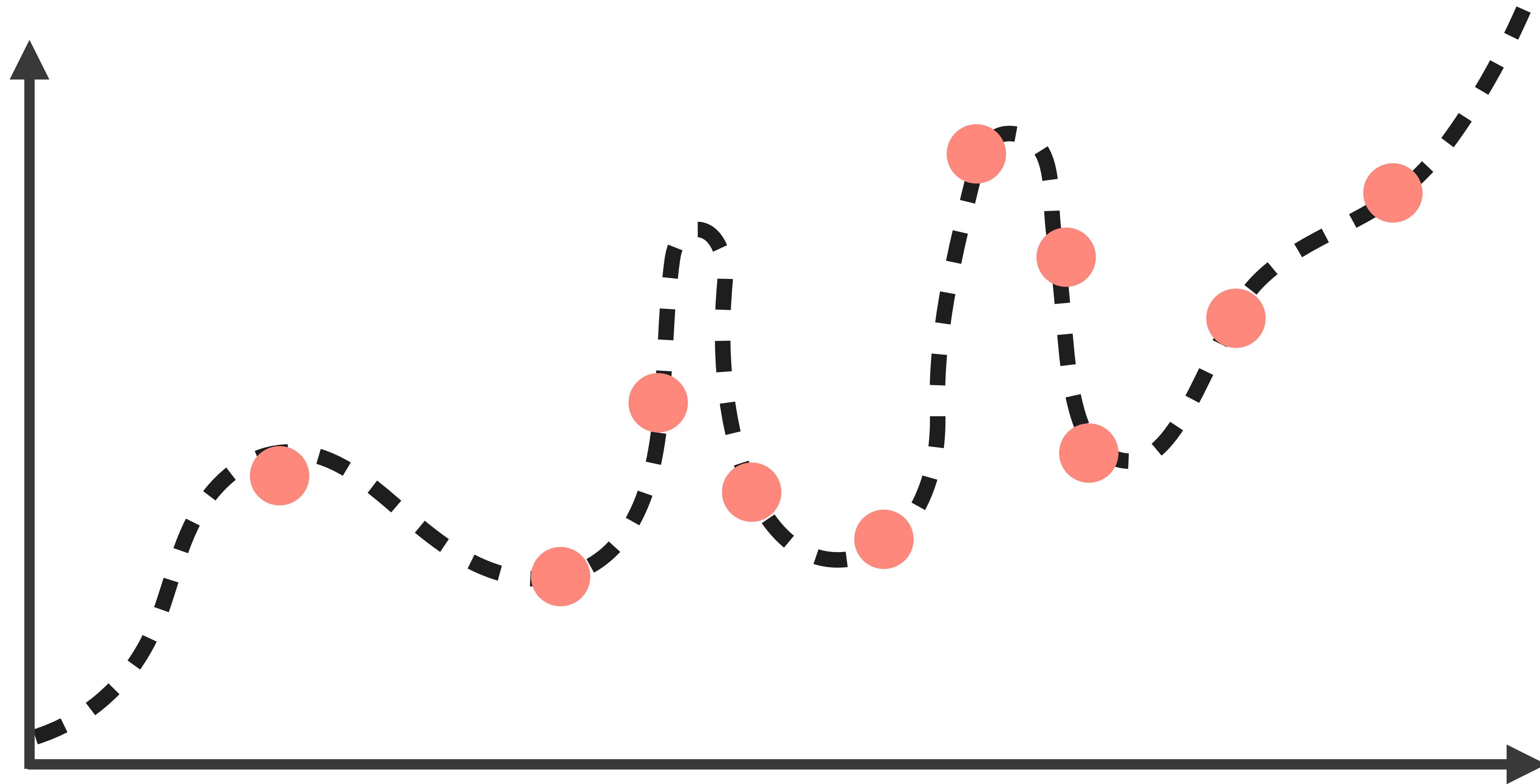
# Non-linear Function Approximator



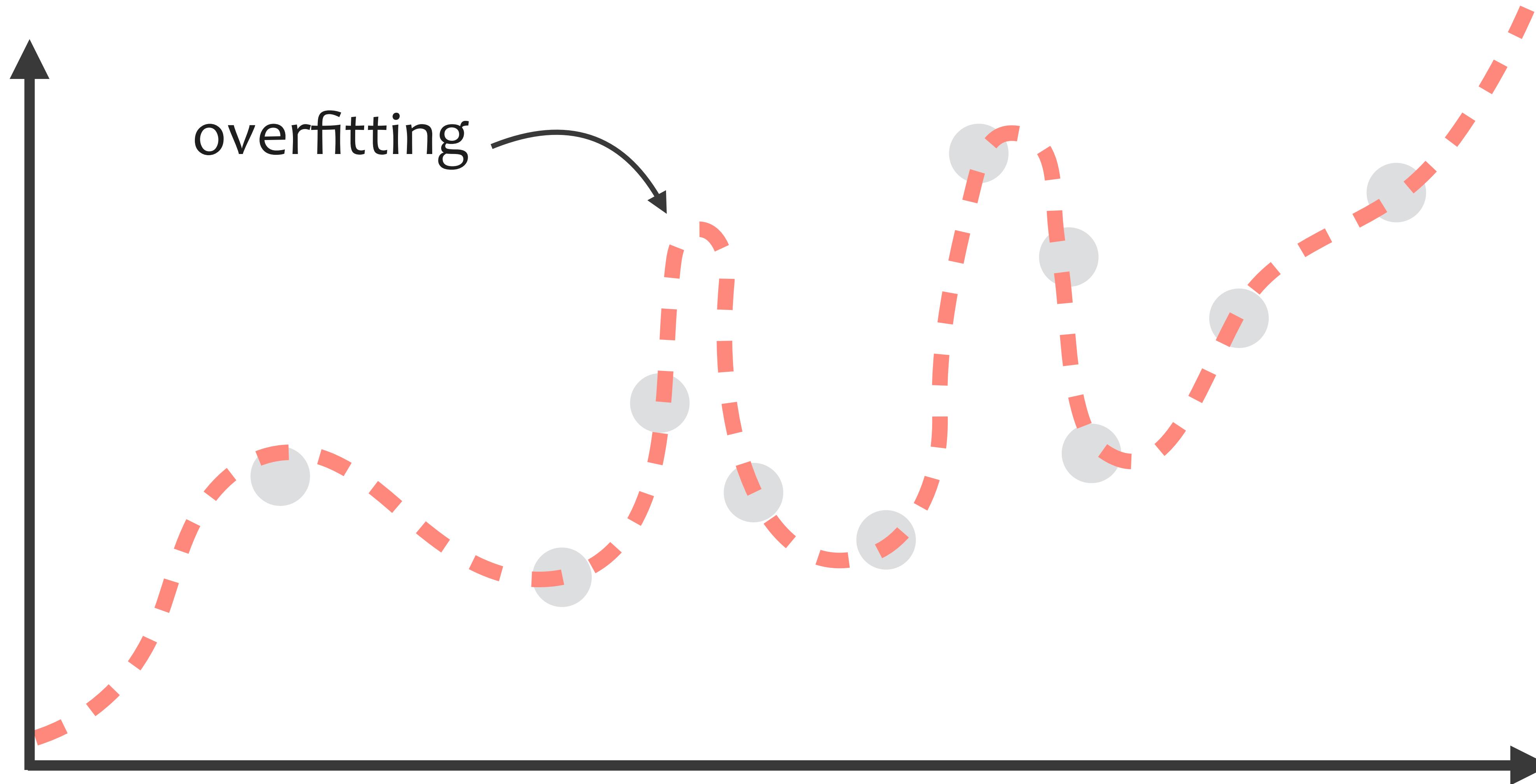
# Non-linear Function Approximator



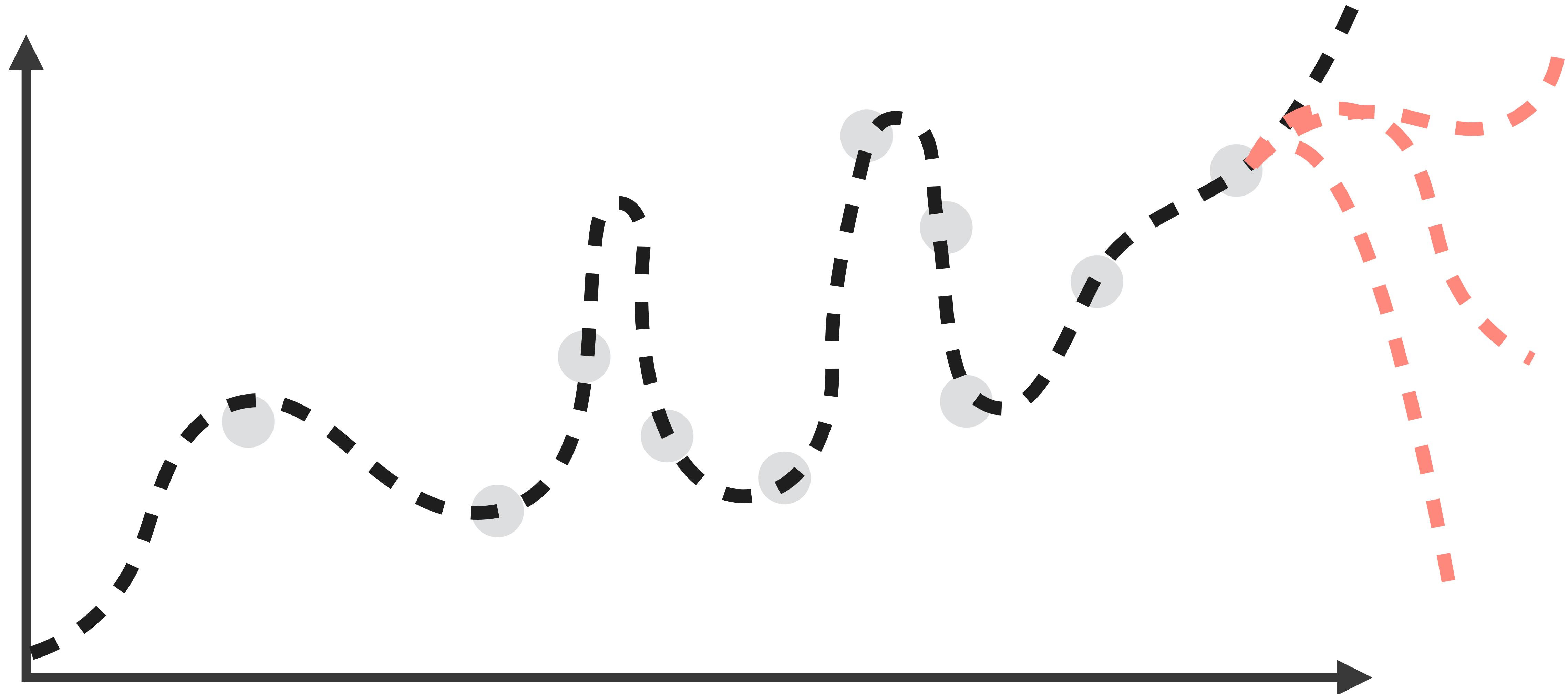
# Need a lot of training data



# May suffer from overfitting



# Difficult to Generalize

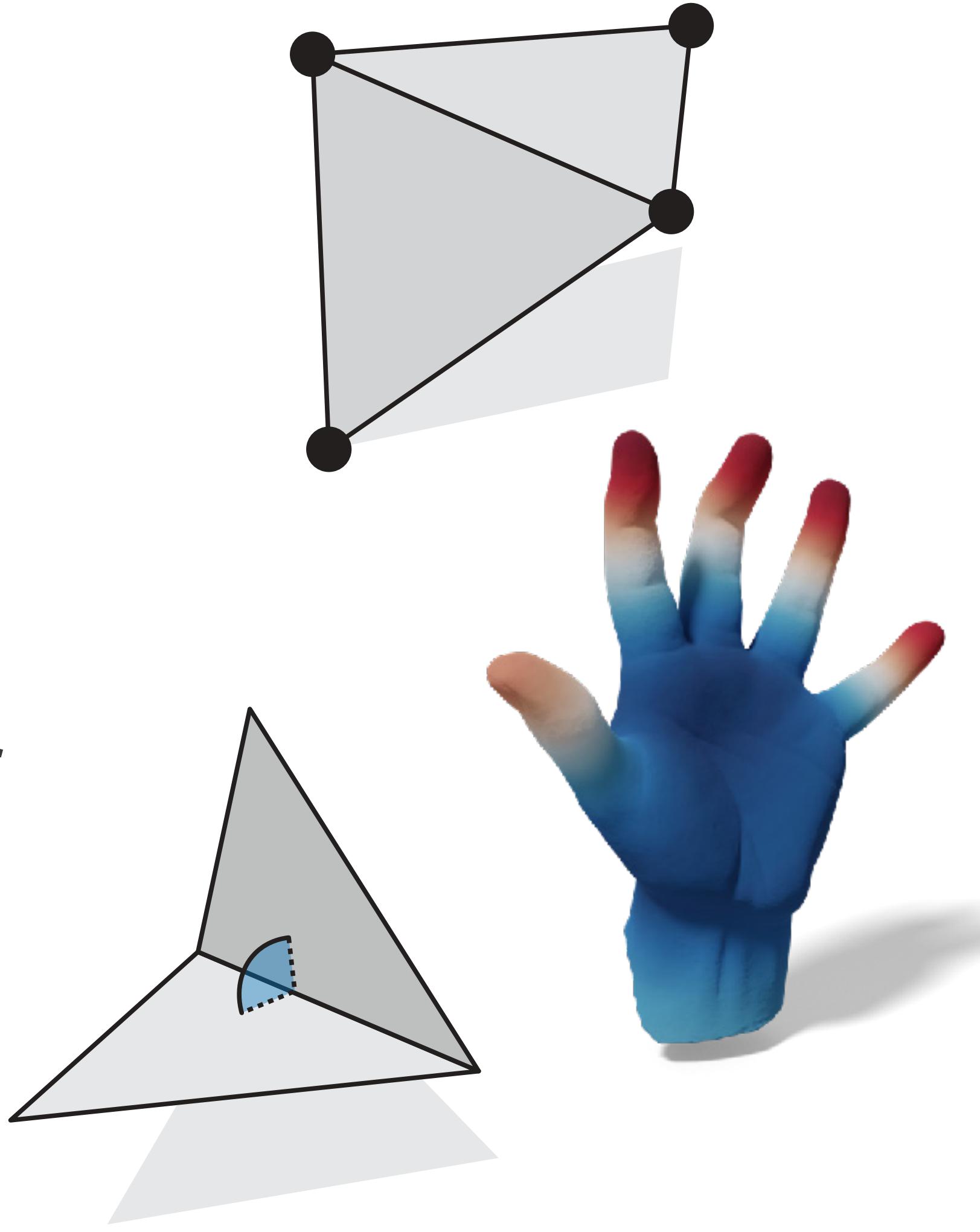


# Machine learning as a feature extractor

# Feature extractor



$$y = f_{\theta}(x)$$



# Shape Classification



human

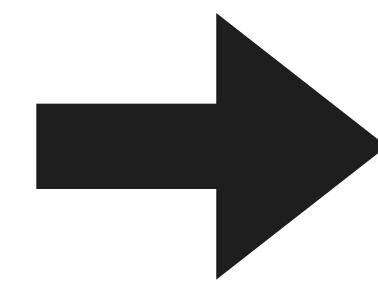


not human

# Global Shape Descriptors



entire shape

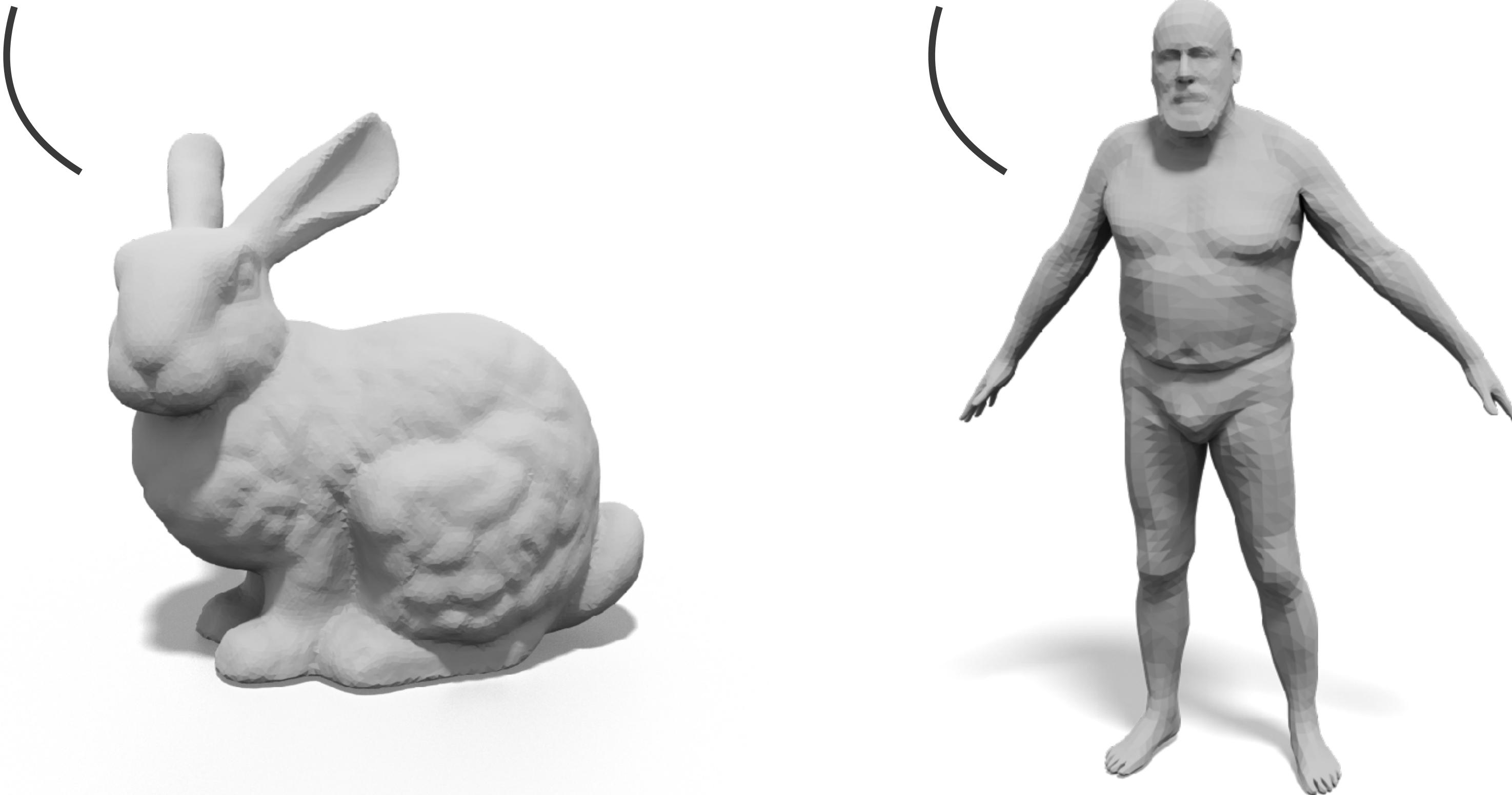


$$[a_1, a_2, \dots, a_n]$$

a fixed dimensional vector

# Measure Shape Difference

$$\| [a_1, a_2, \dots, a_n] - [b_1, b_2, \dots, b_n] \| = \uparrow$$

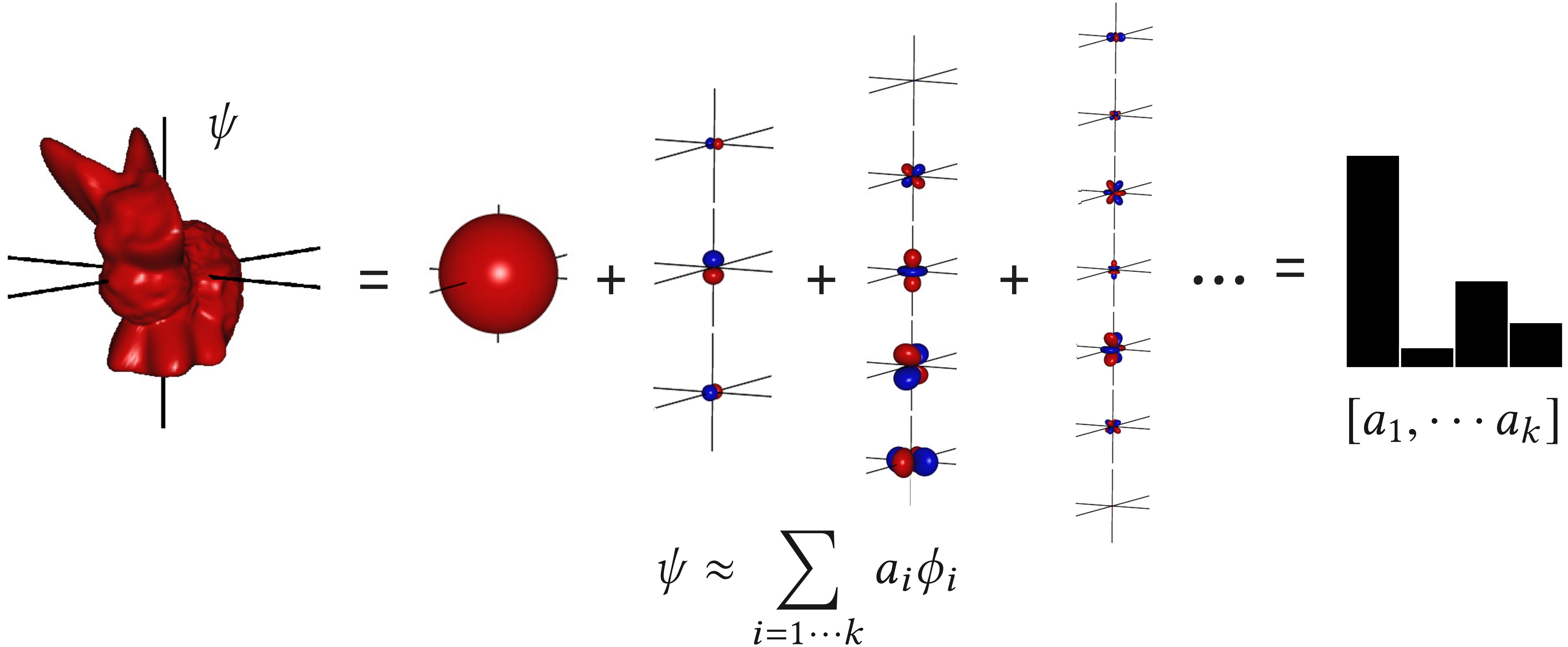


# Measure Shape Difference

$$\| [c_1, c_2, \dots, c_n] - [b_1, b_2, \dots, b_n] \| = \downarrow$$



# E.g., Spherical Harmonics



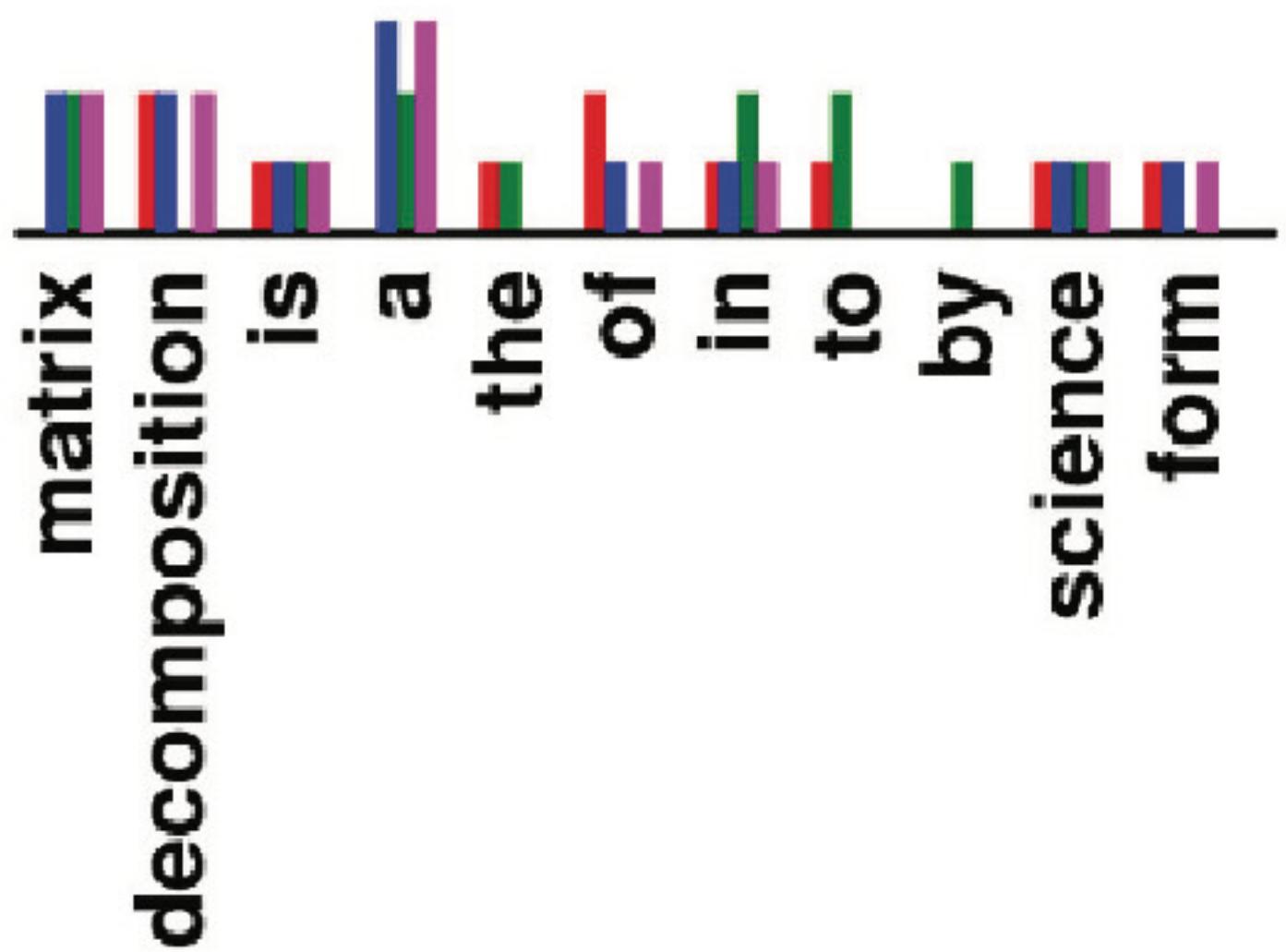
# E.g., Bags of Words

in math science, matrix decomposition is a factorization of a matrix into some canonical form. each type of decomposition is used in a particular problem.

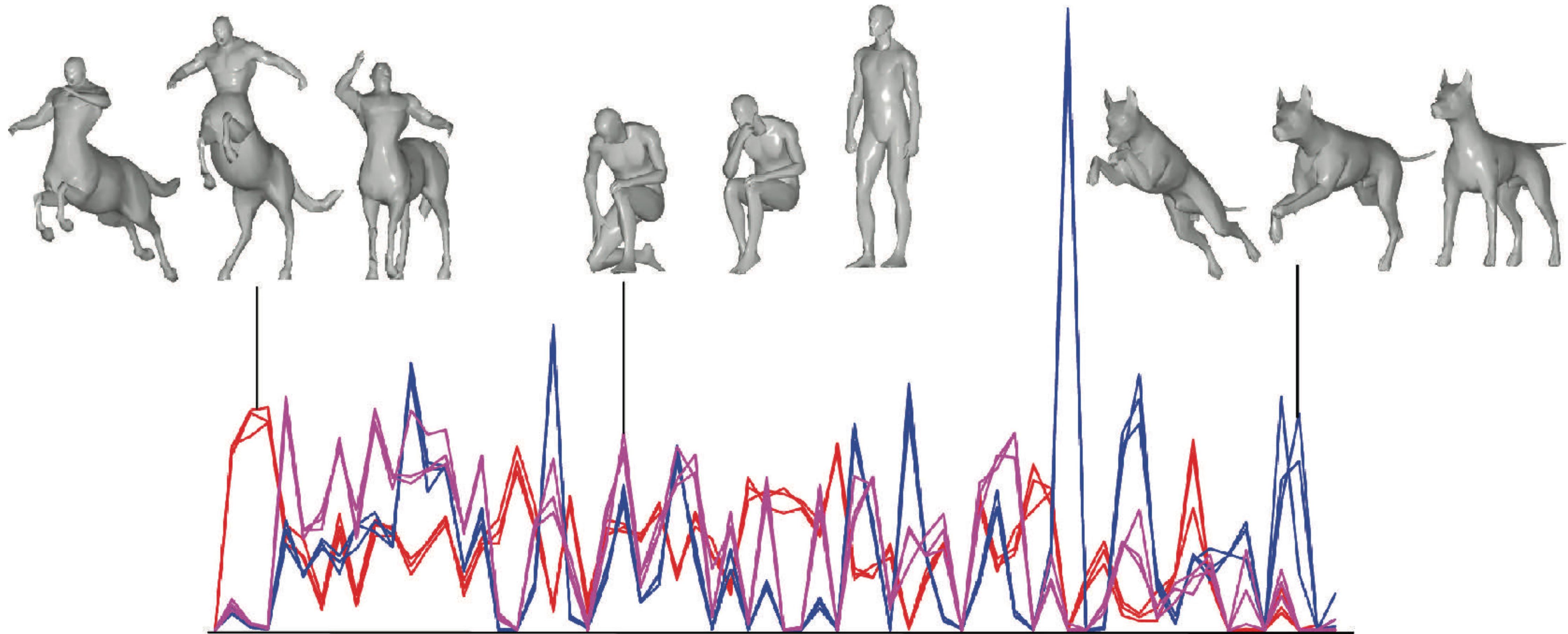
in particular **matrix** used type **a** some **science decomposition** form a factorization of **is canonical** matrix math **decomposition** is in a each problem into of

in biological **science**, **decomposition** is the process **of** organisms **to** break down into simpler **form of** matter. usually, **decomposition** occurs after death.

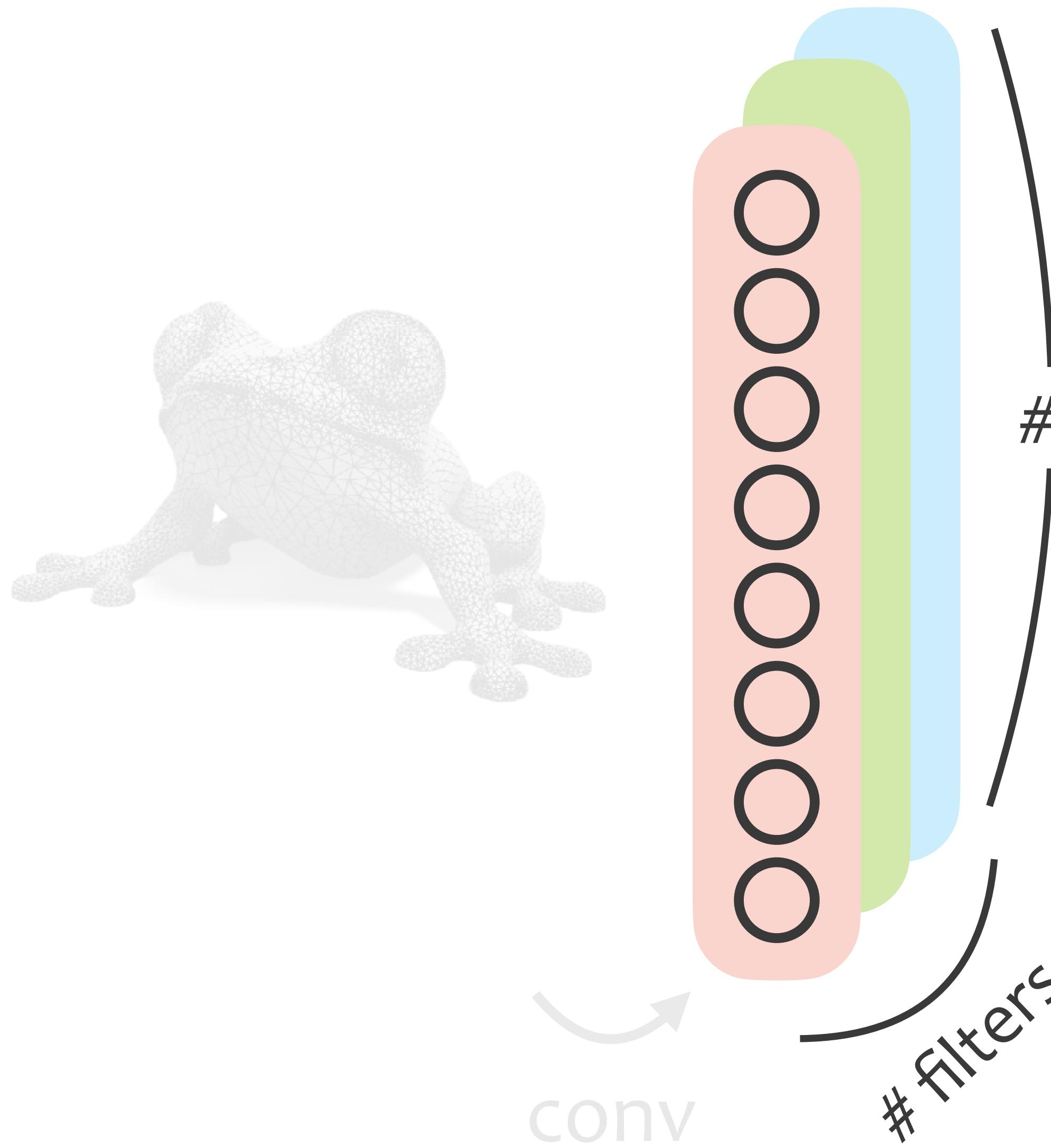
**matrix** is a science fiction movie released in 1999. **matrix** refers to a simulated reality created by machines in order to subdue the human population.



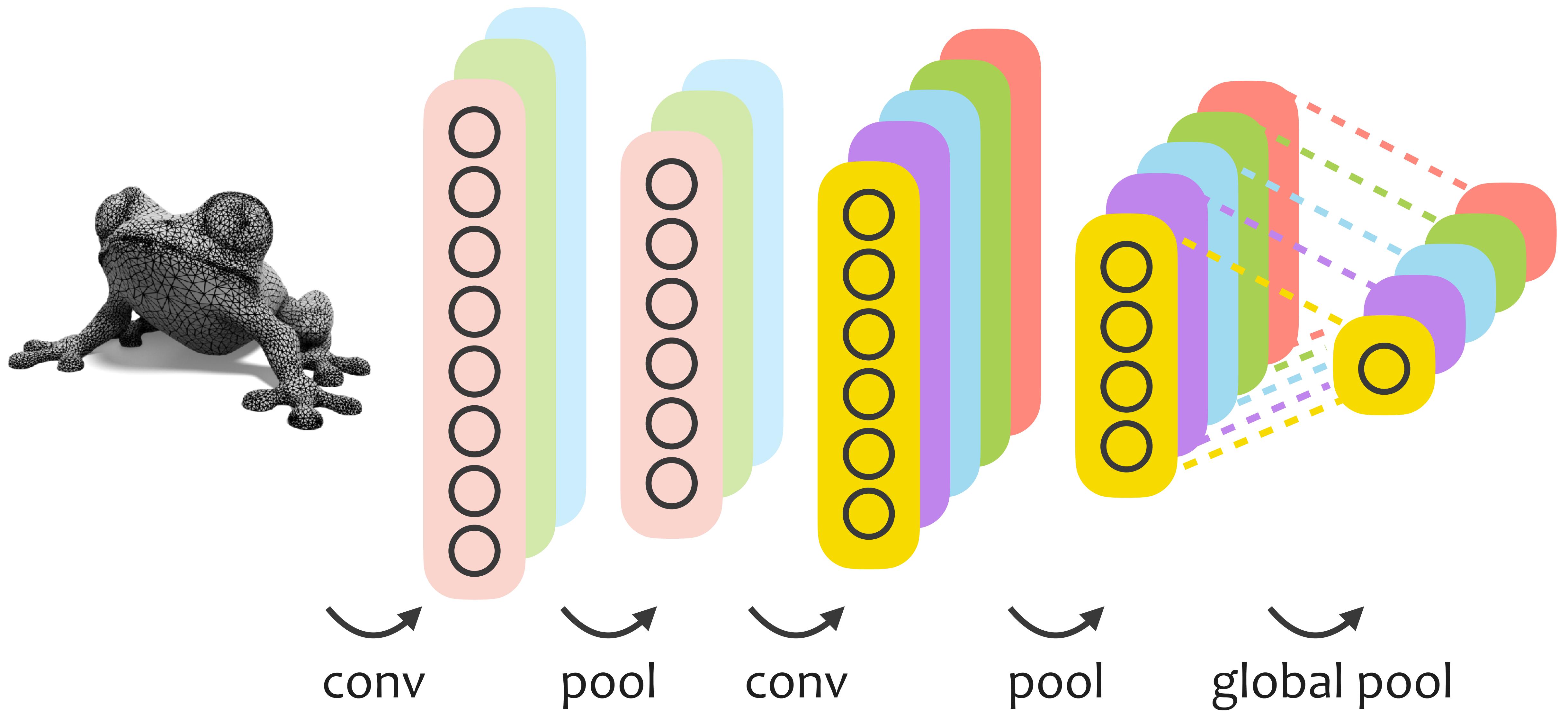
# E.g., Bags of Features



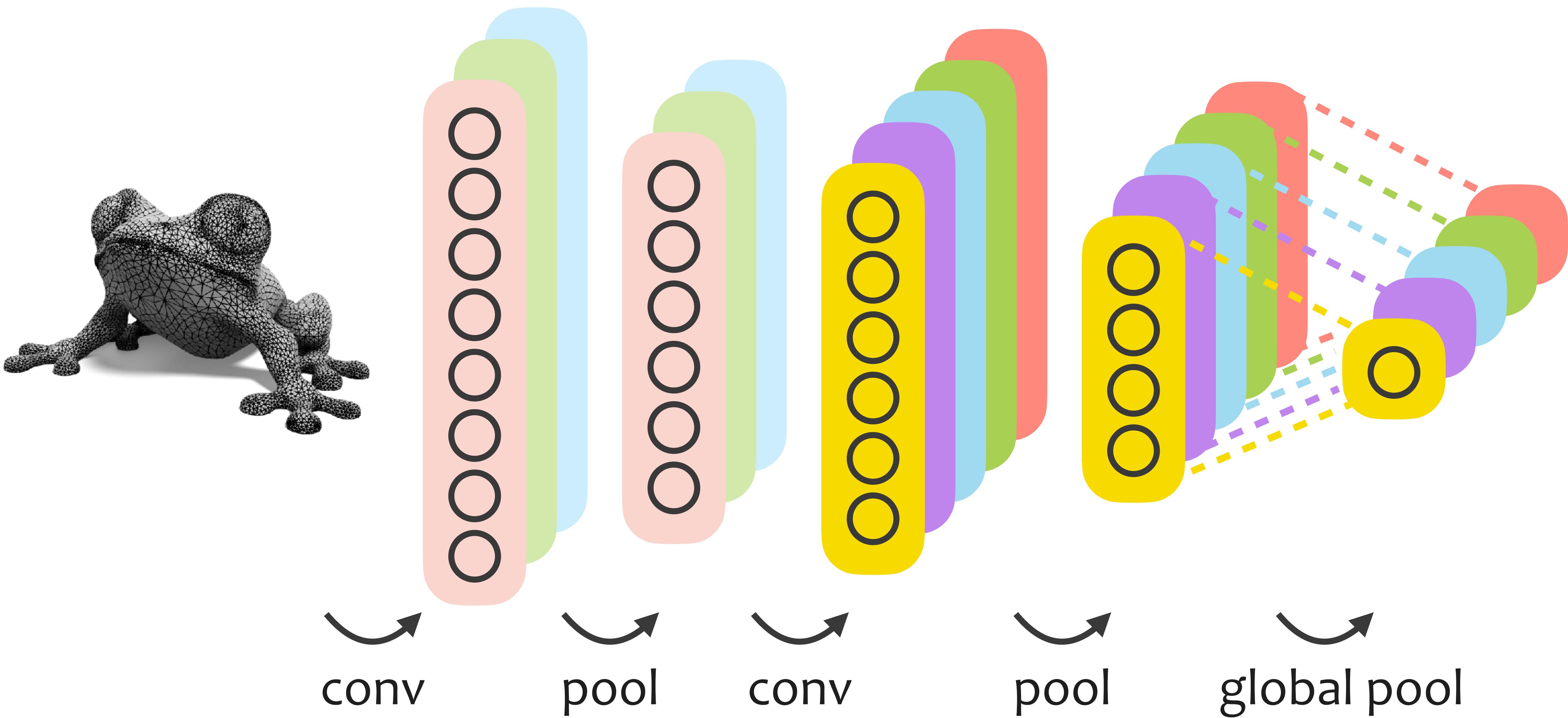
# Learned Global Descriptors



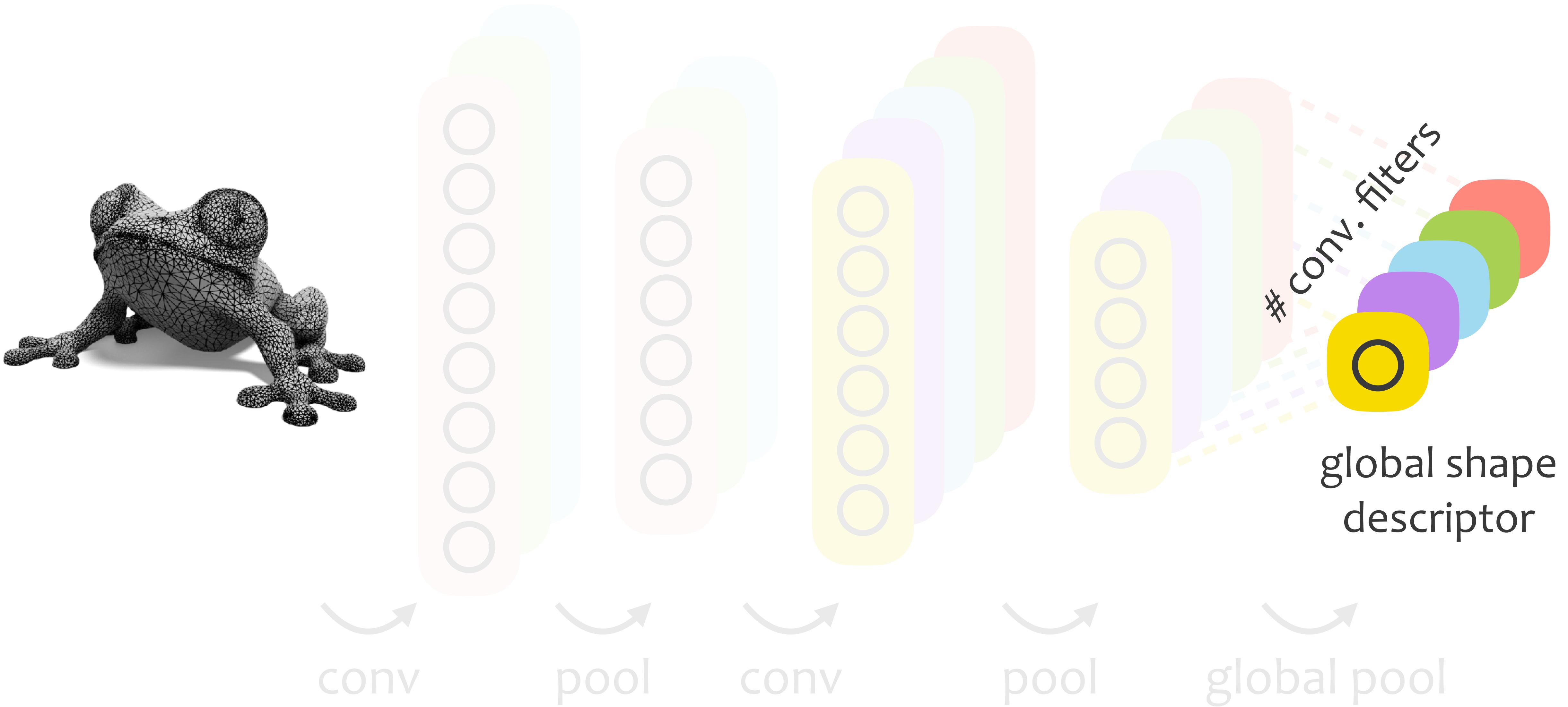
# Learned Global Descriptors



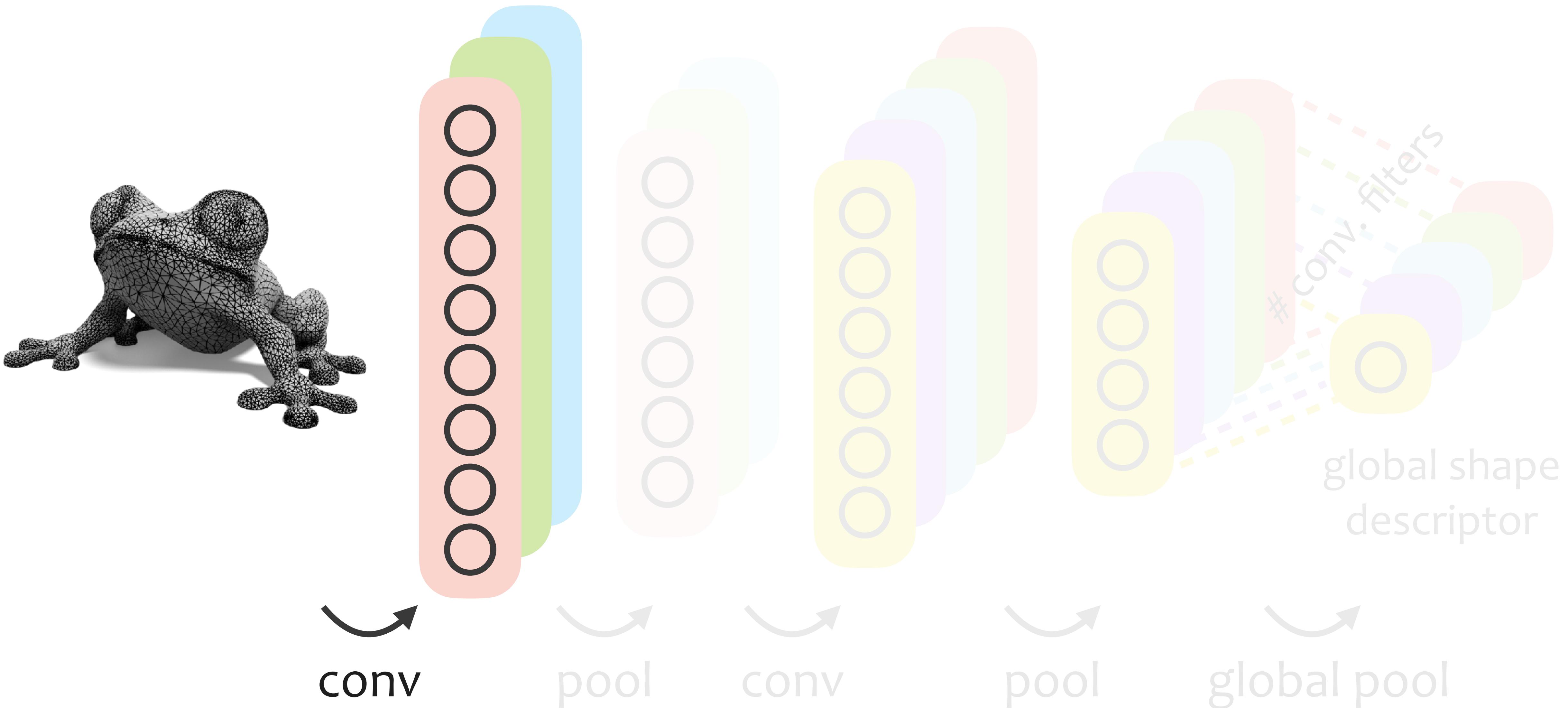
# Learned Global Descriptors



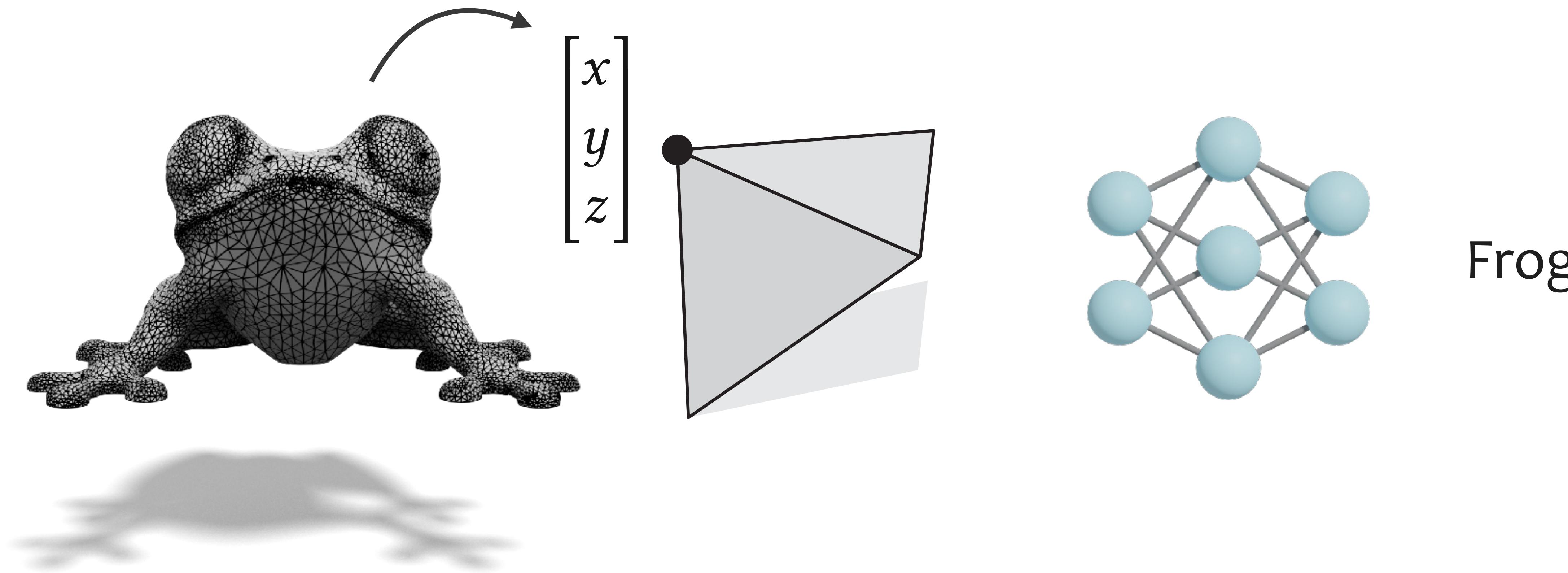
# Learned Global Descriptors



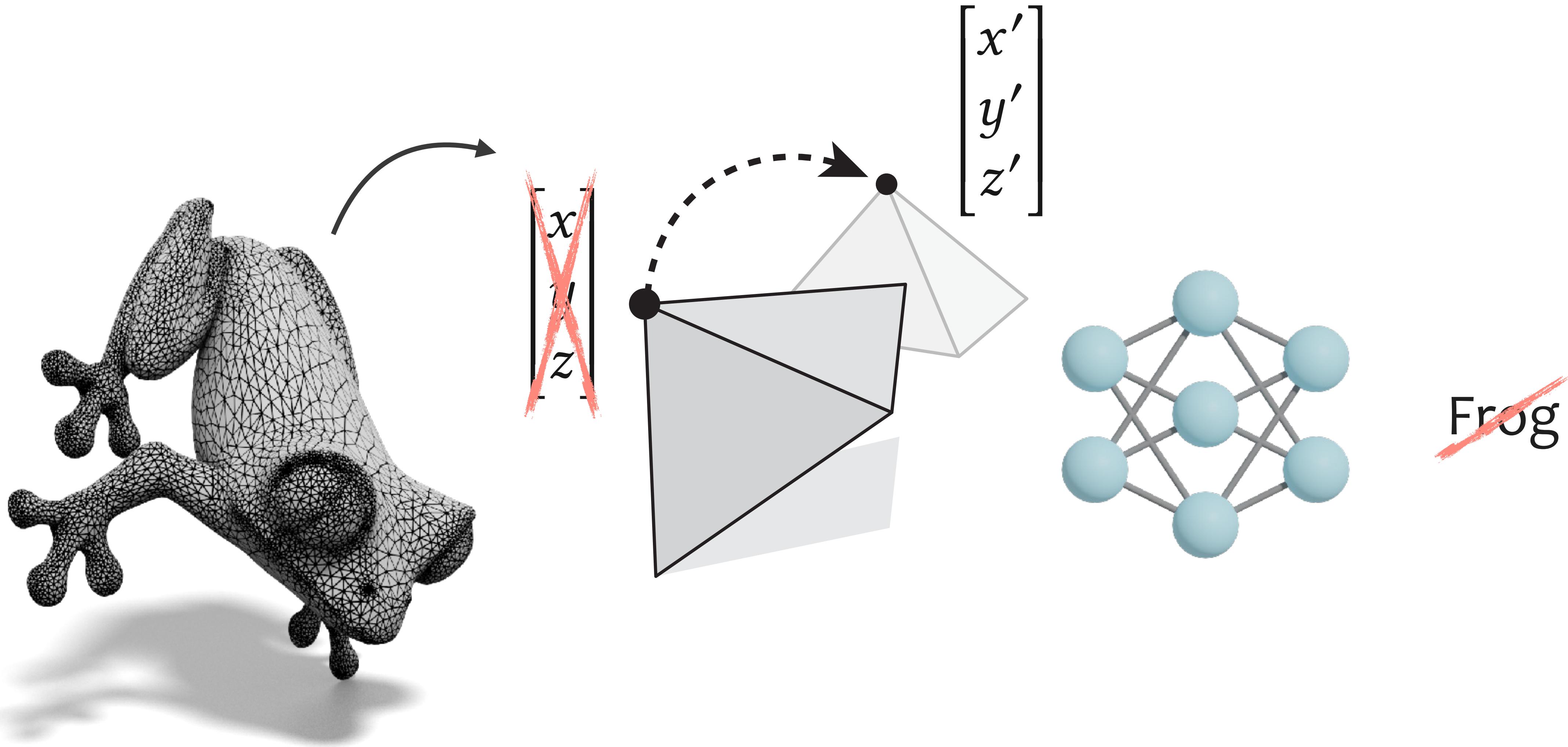
# Inputs to the network



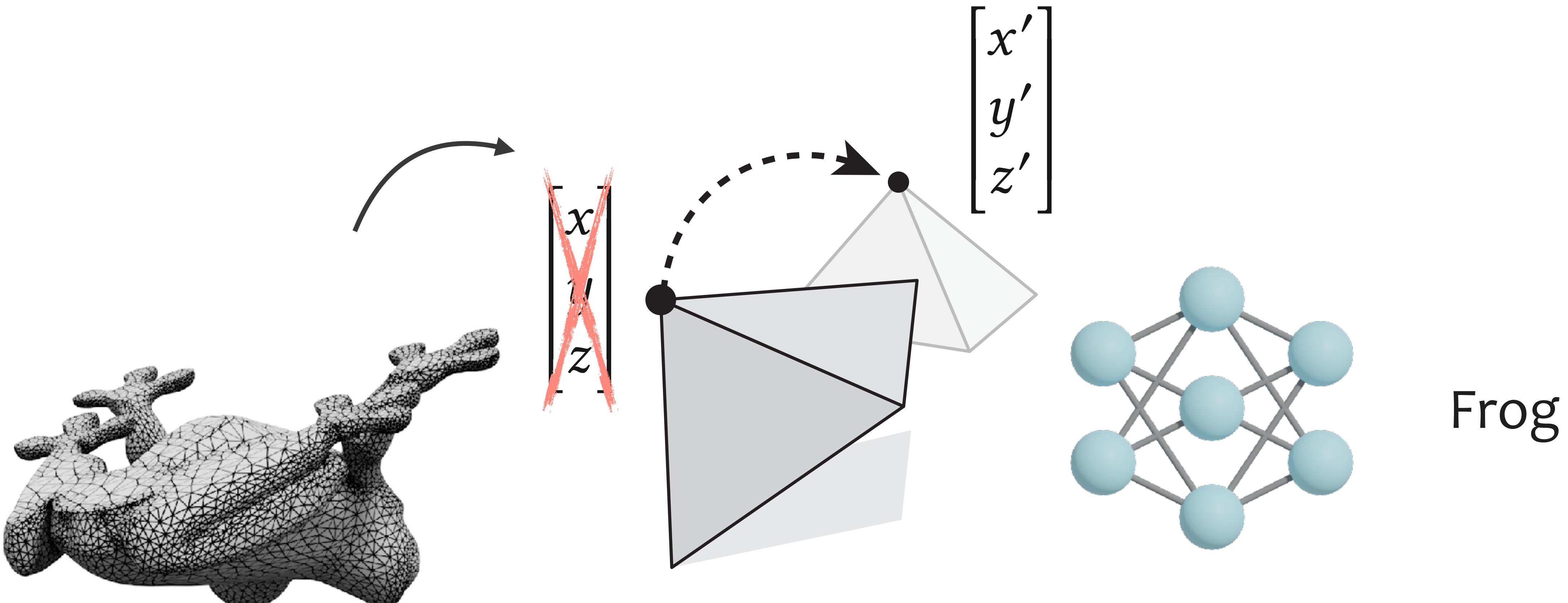
# Not Orientation Invariant



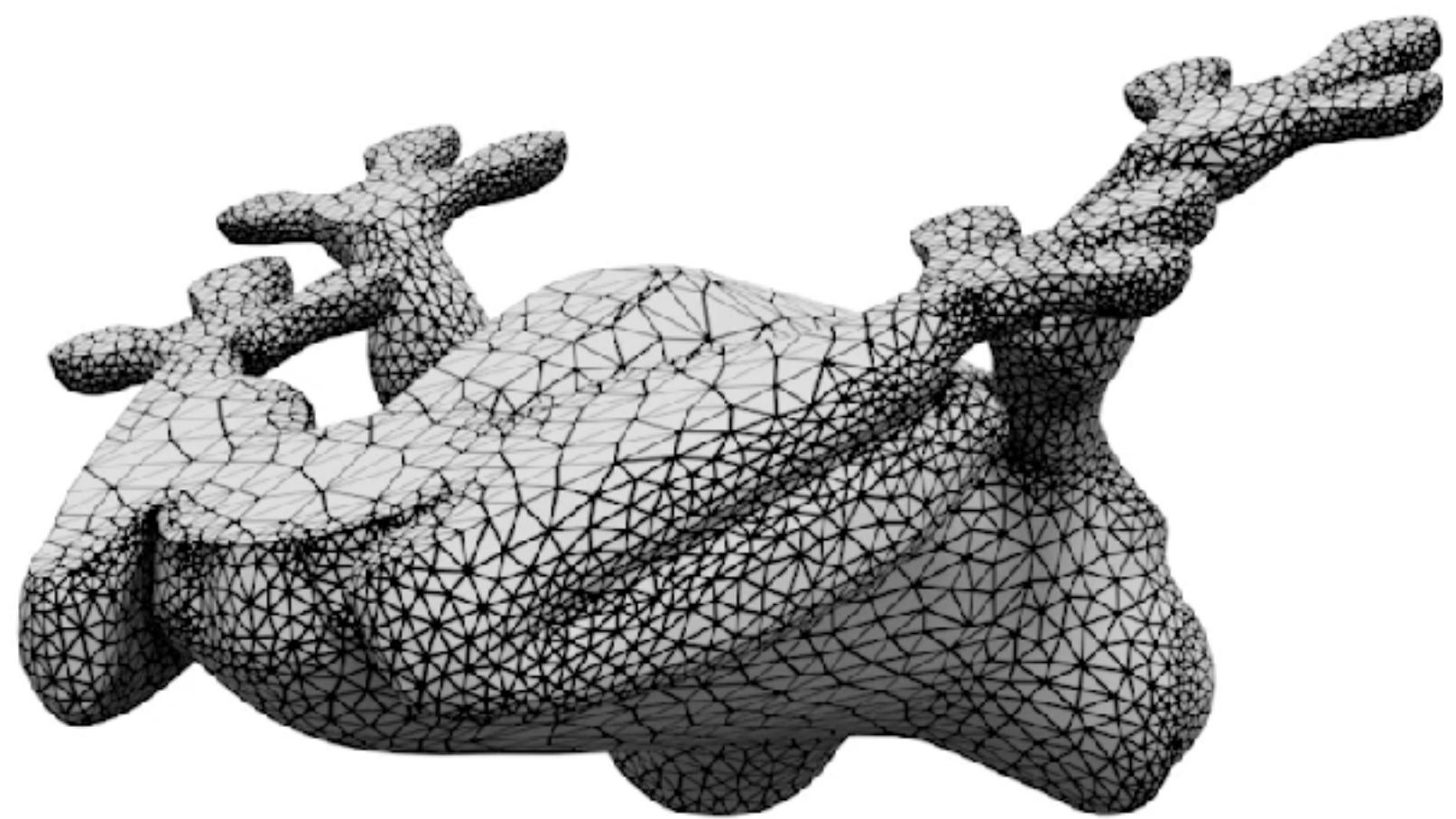
# Not Orientation Invariant



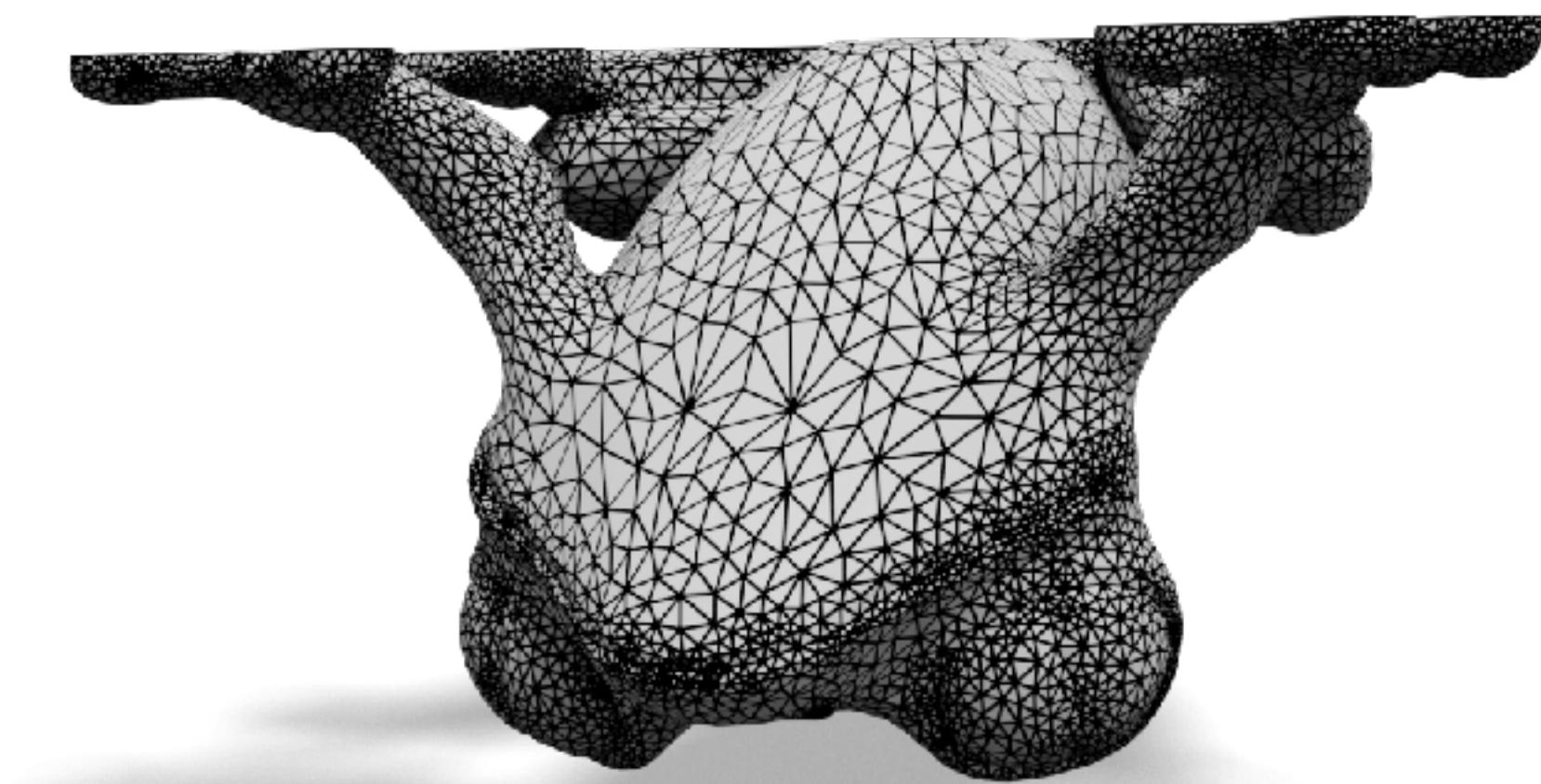
# One Solution: Data Augmentation



# It helps, but ...

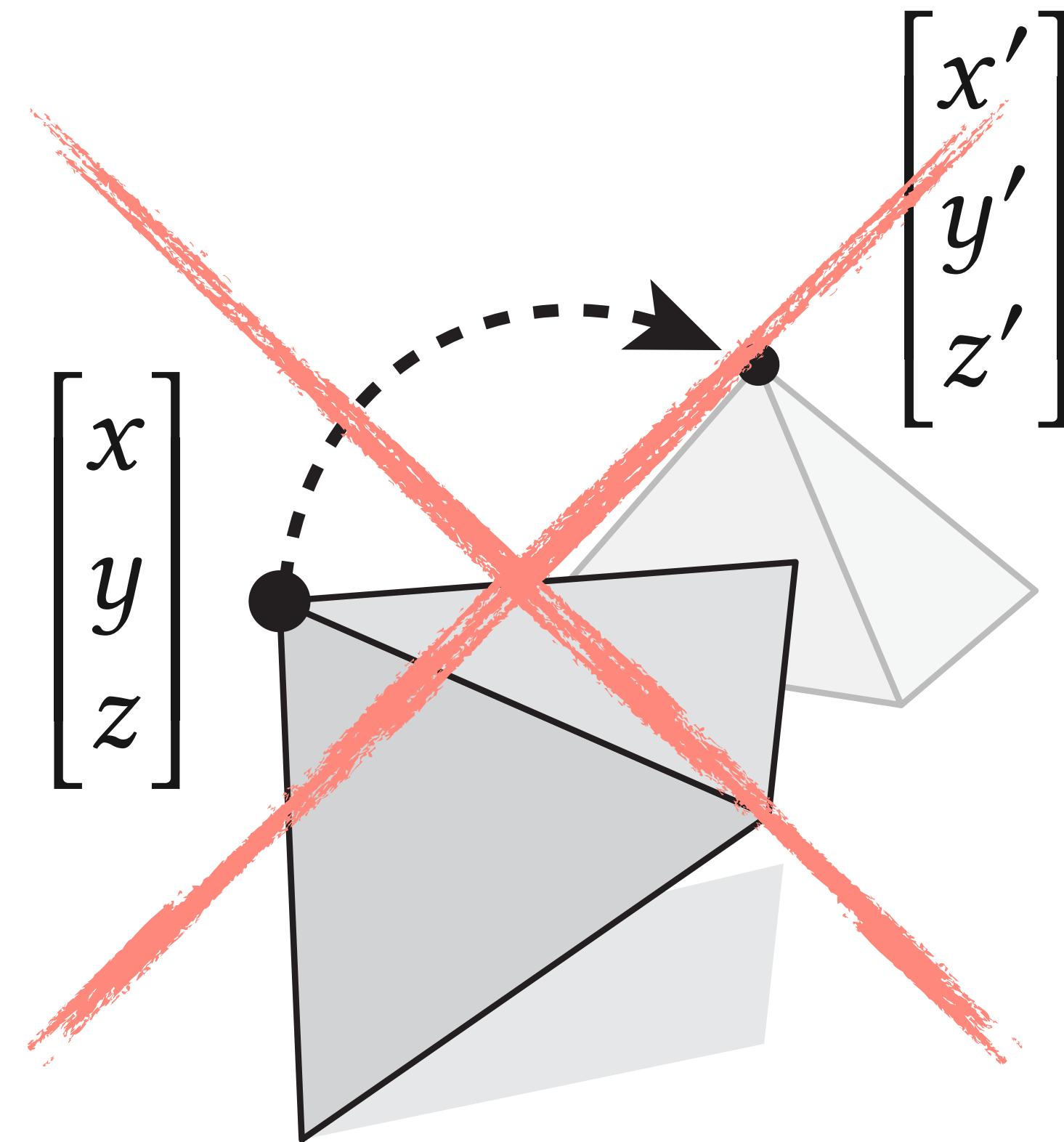


longer to train

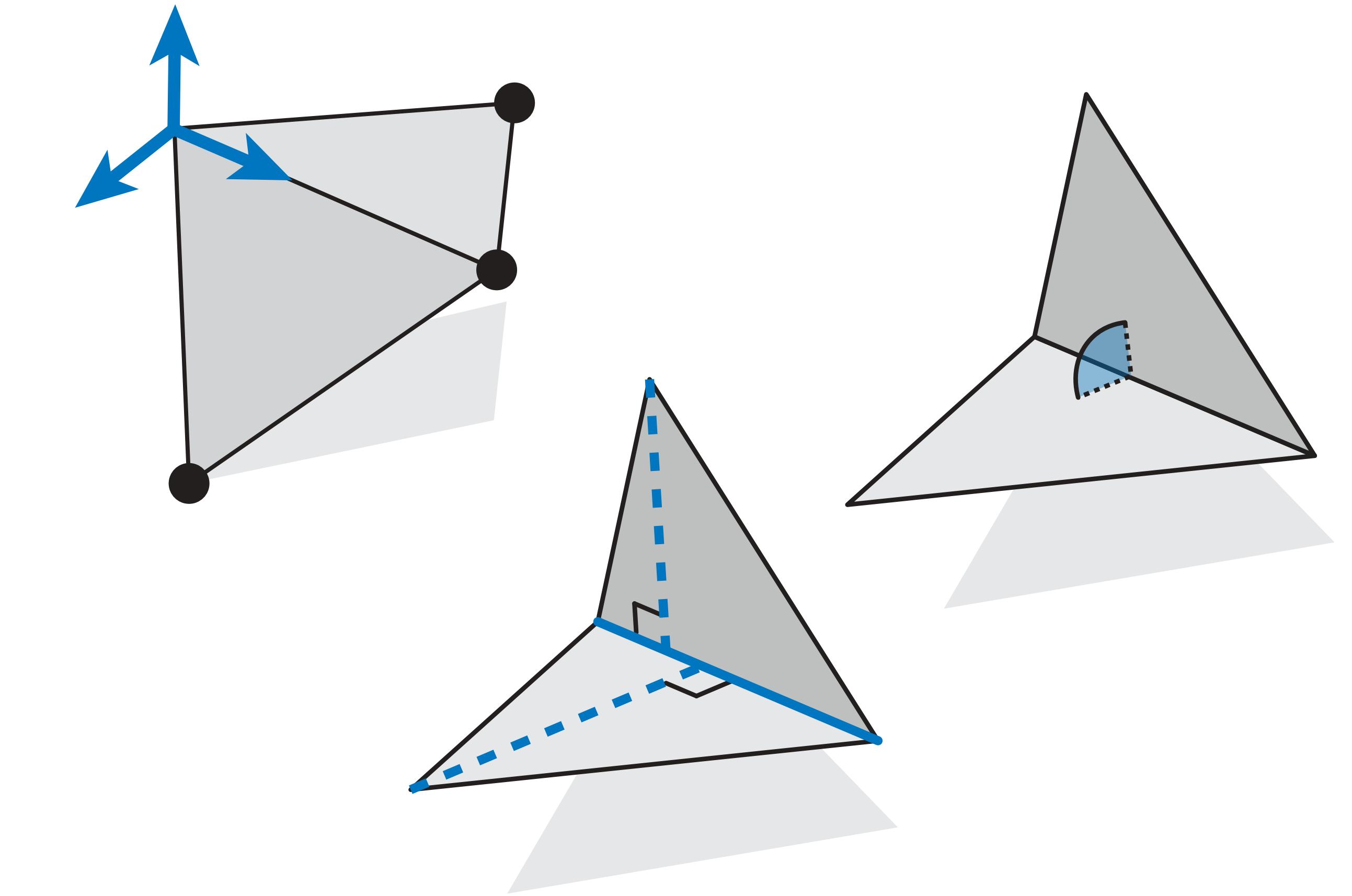


Adversarial attack

# Leverage mesh structure

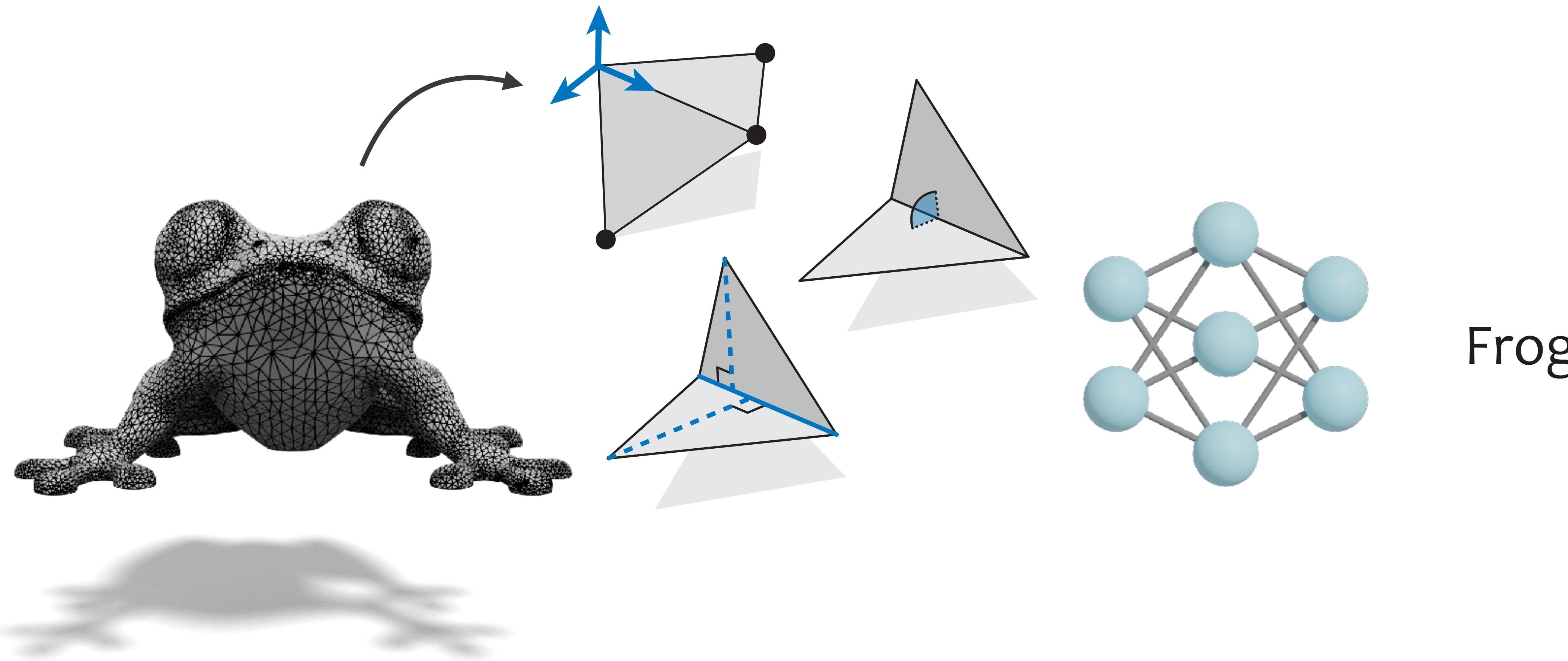


not invariant quantities

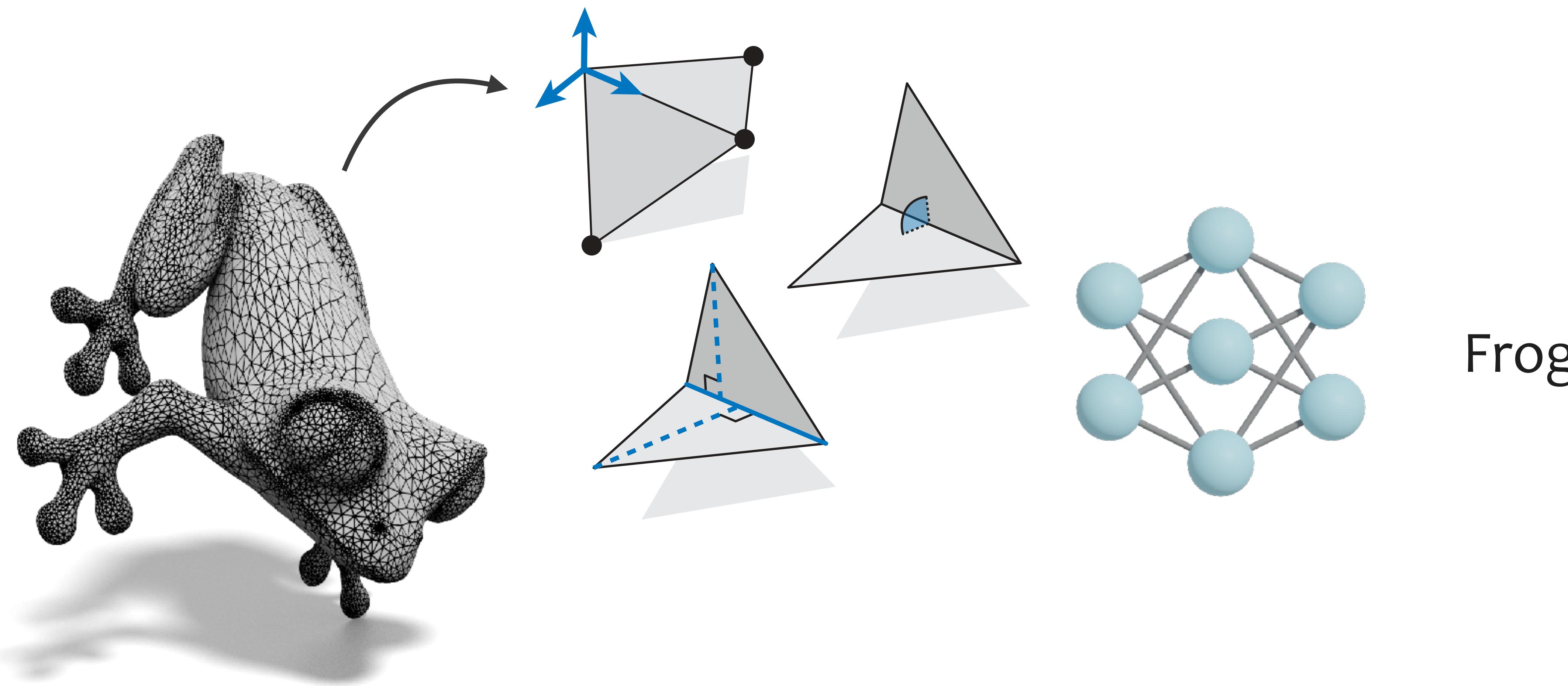


rotation invariant quantities

# Orientation Invariant

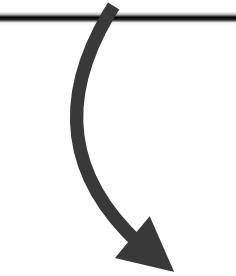


# Orientation Invariant



# Push the limits

Method	Split 16	Split 10
MeshCNN	98.6	91.0%
GWCNN	96.6%	90.3%
GI	96.6%	88.6%
SN	48.4%	52.7%
SG	70.8%	62.6%



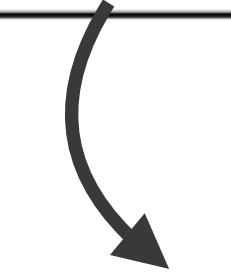
Classic method

[Bronstein et al. 2011]

# Push the limits

Classification SHREC

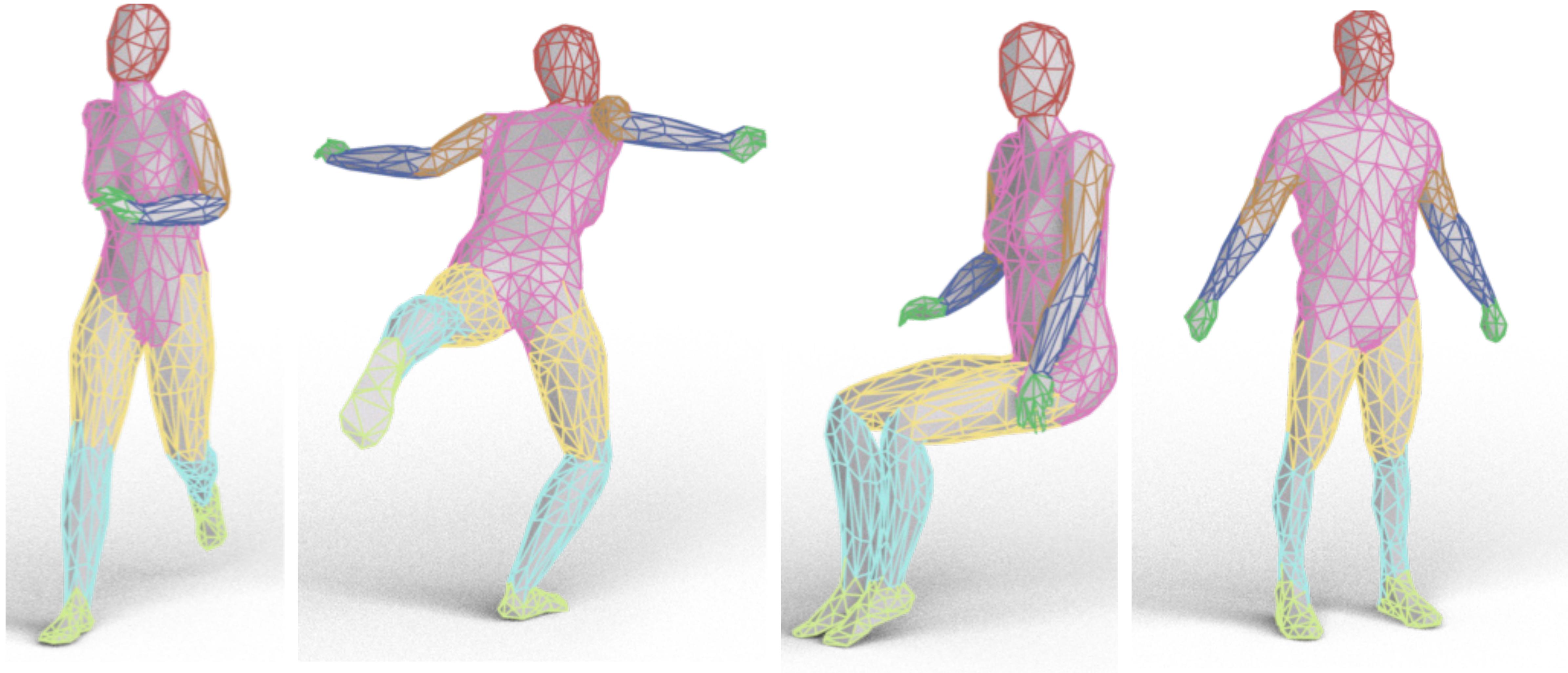
Method	Split 16	Split 10
<b>MeshCNN</b>	<b>98.6</b>	<b>91.0%</b>
GWCNN	96.6%	90.3%
GI	96.6%	88.6%
SN	48.4%	52.7%
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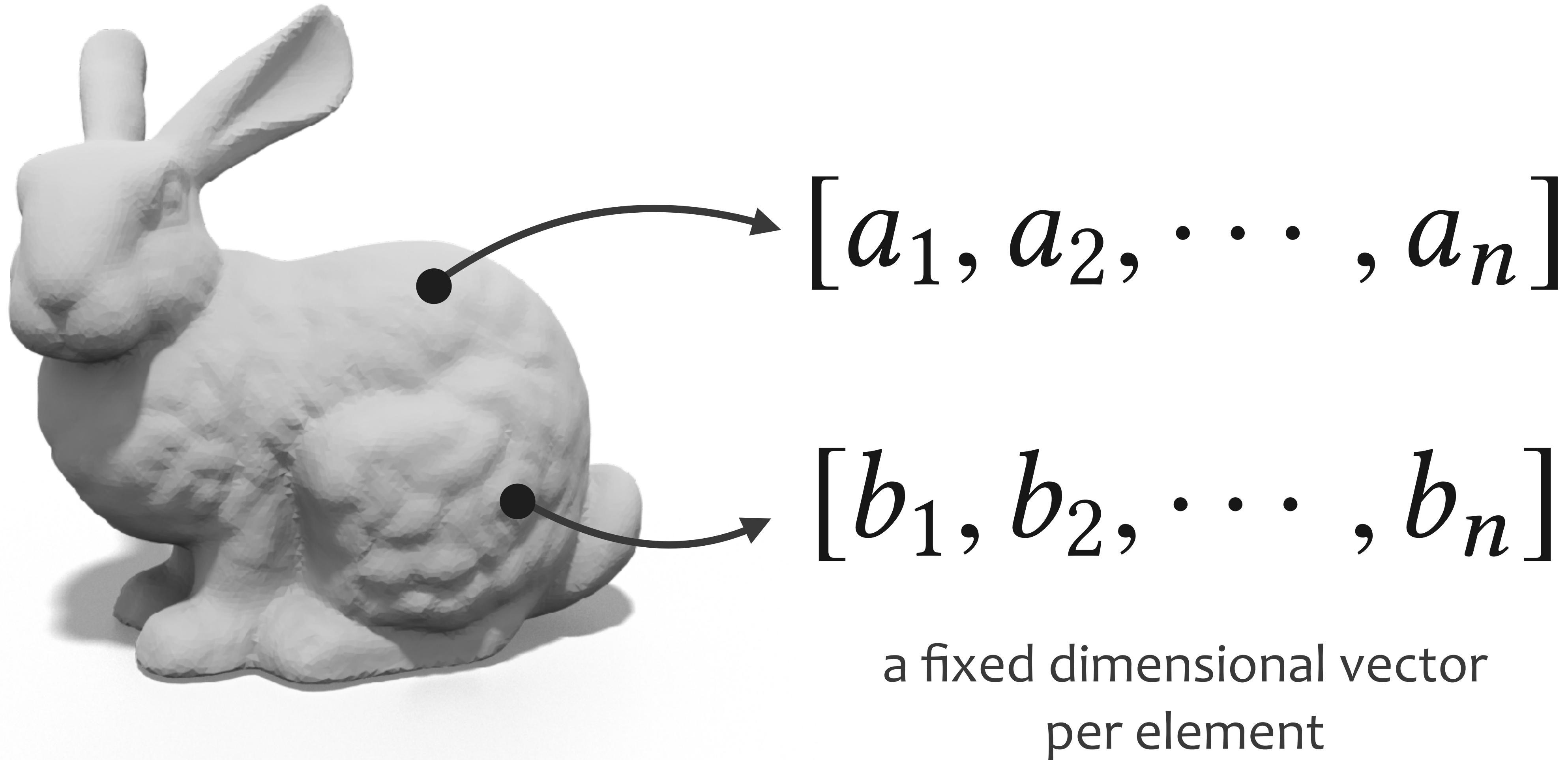
Classic method

[Bronstein et al. 2011]

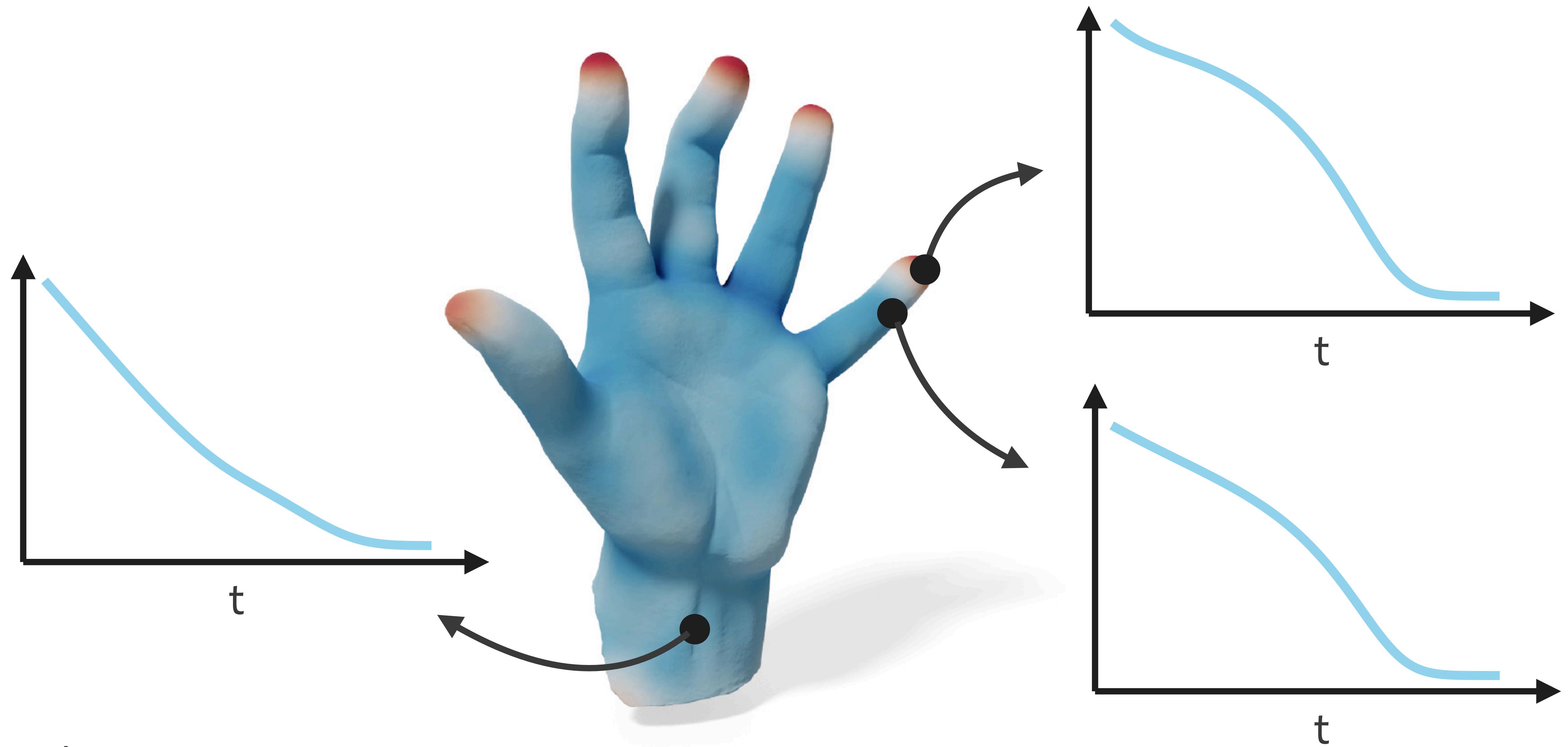
# Shape Segmentation



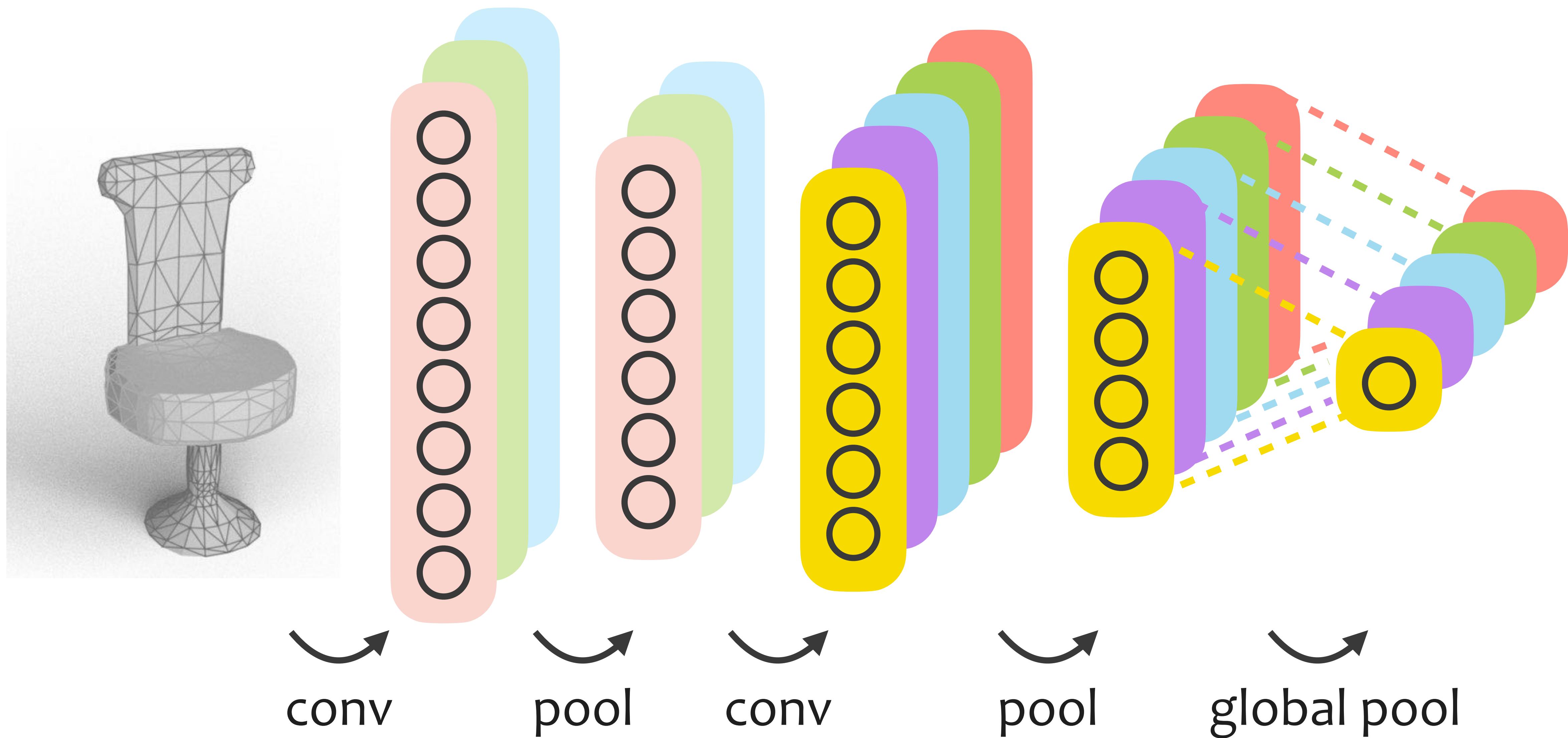
# Local Shape Descriptors



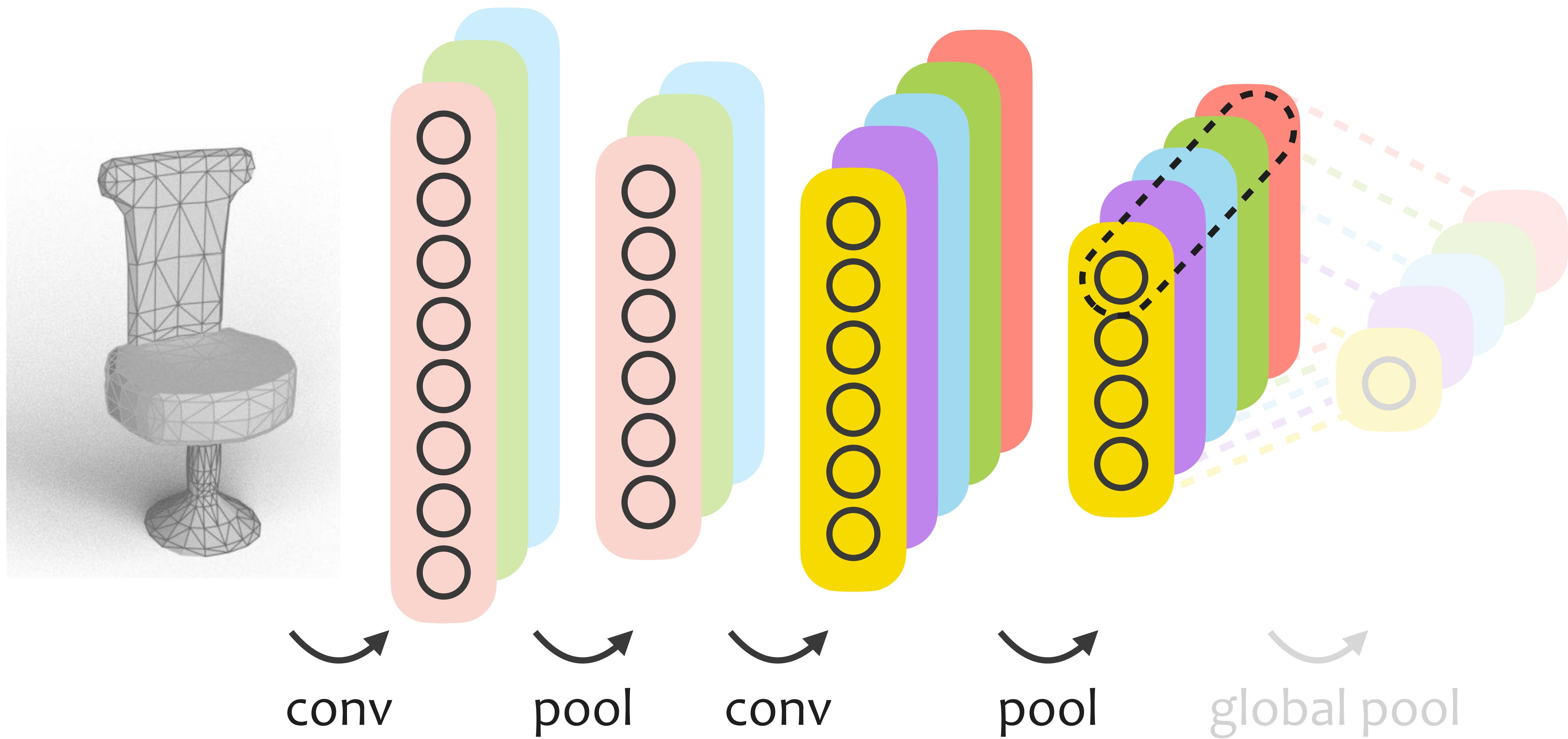
# E.g., Heat Kernel Signature



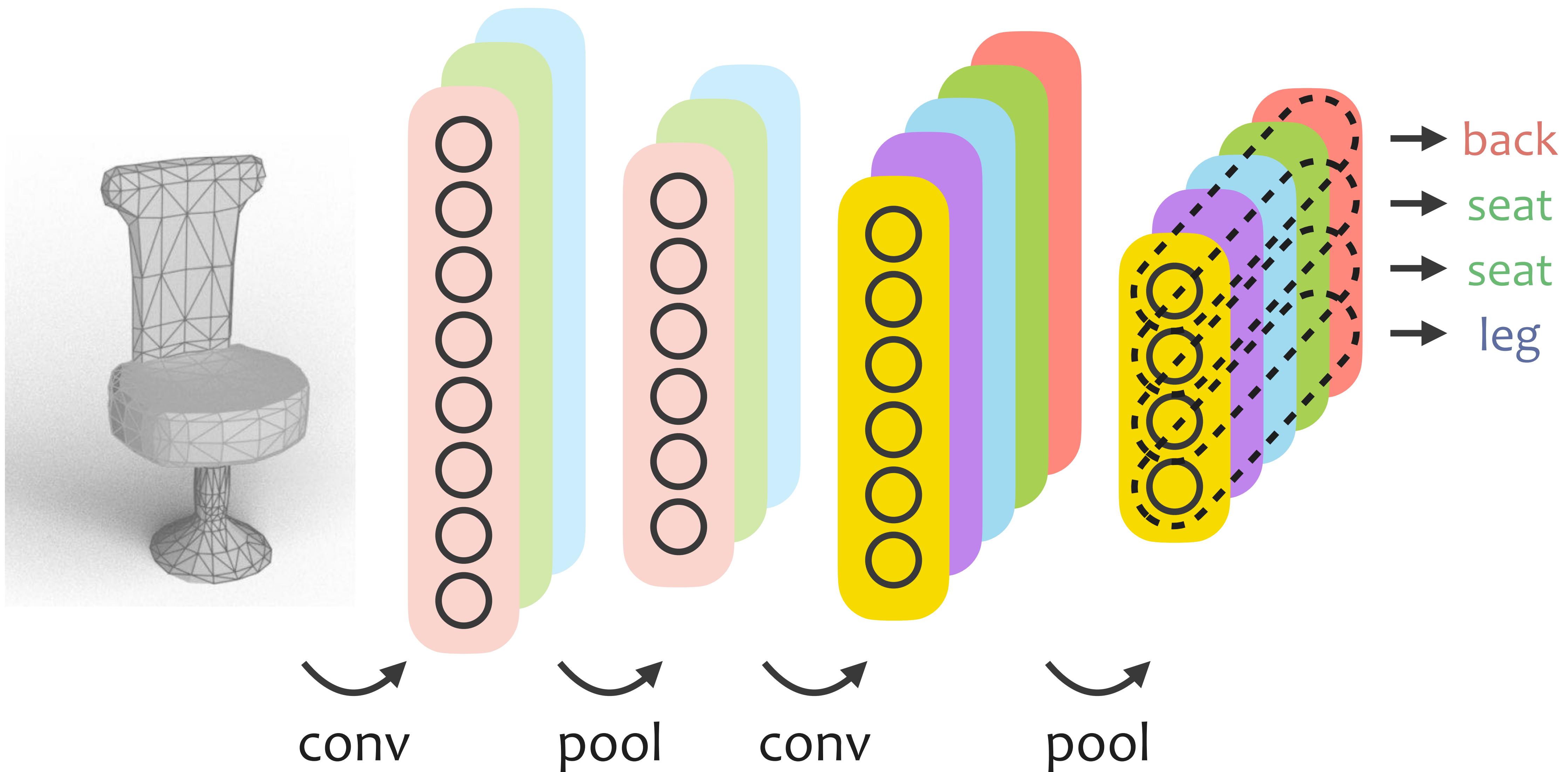
# Learned Local Descriptors



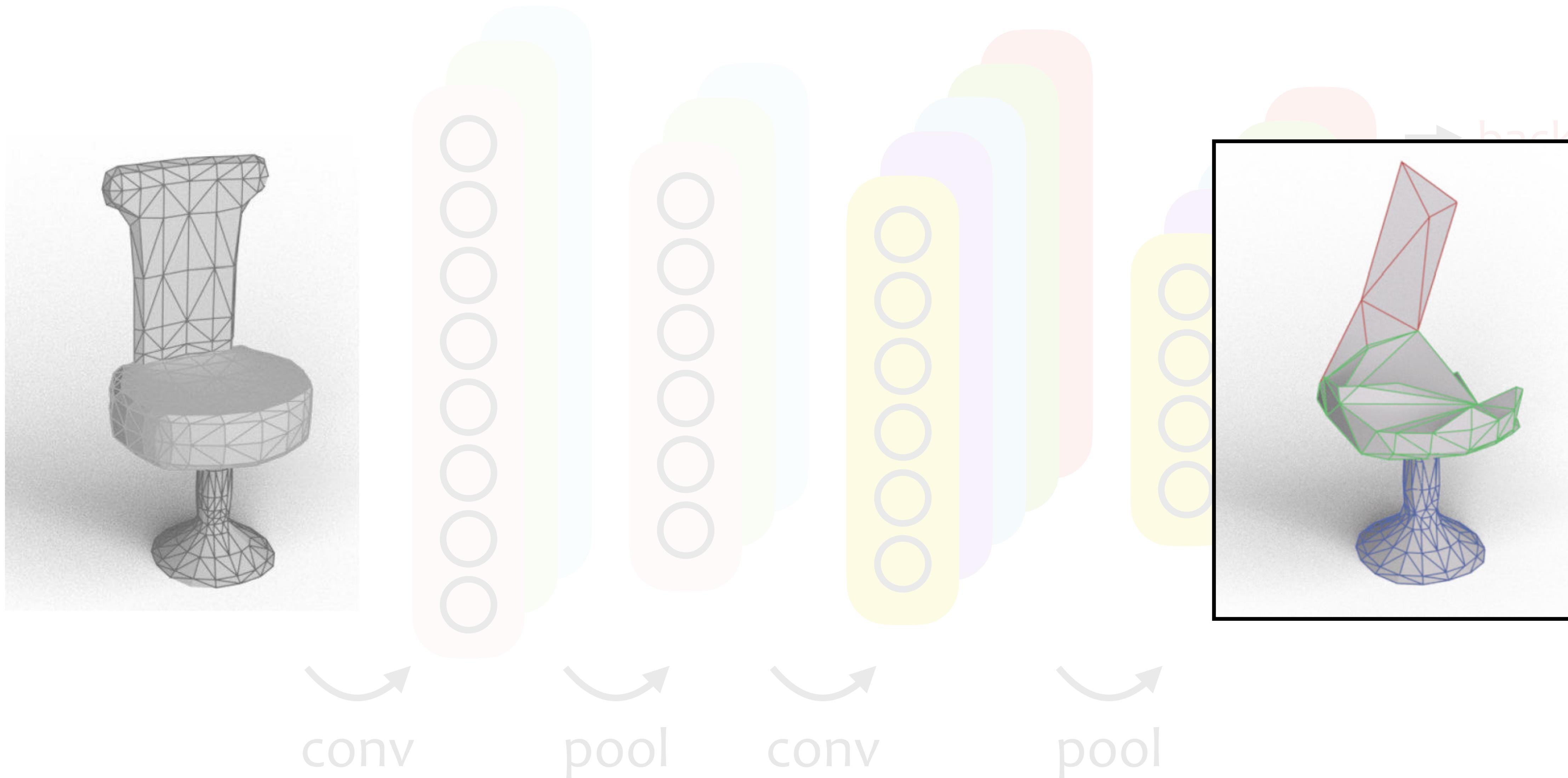
# Learned Local Descriptors



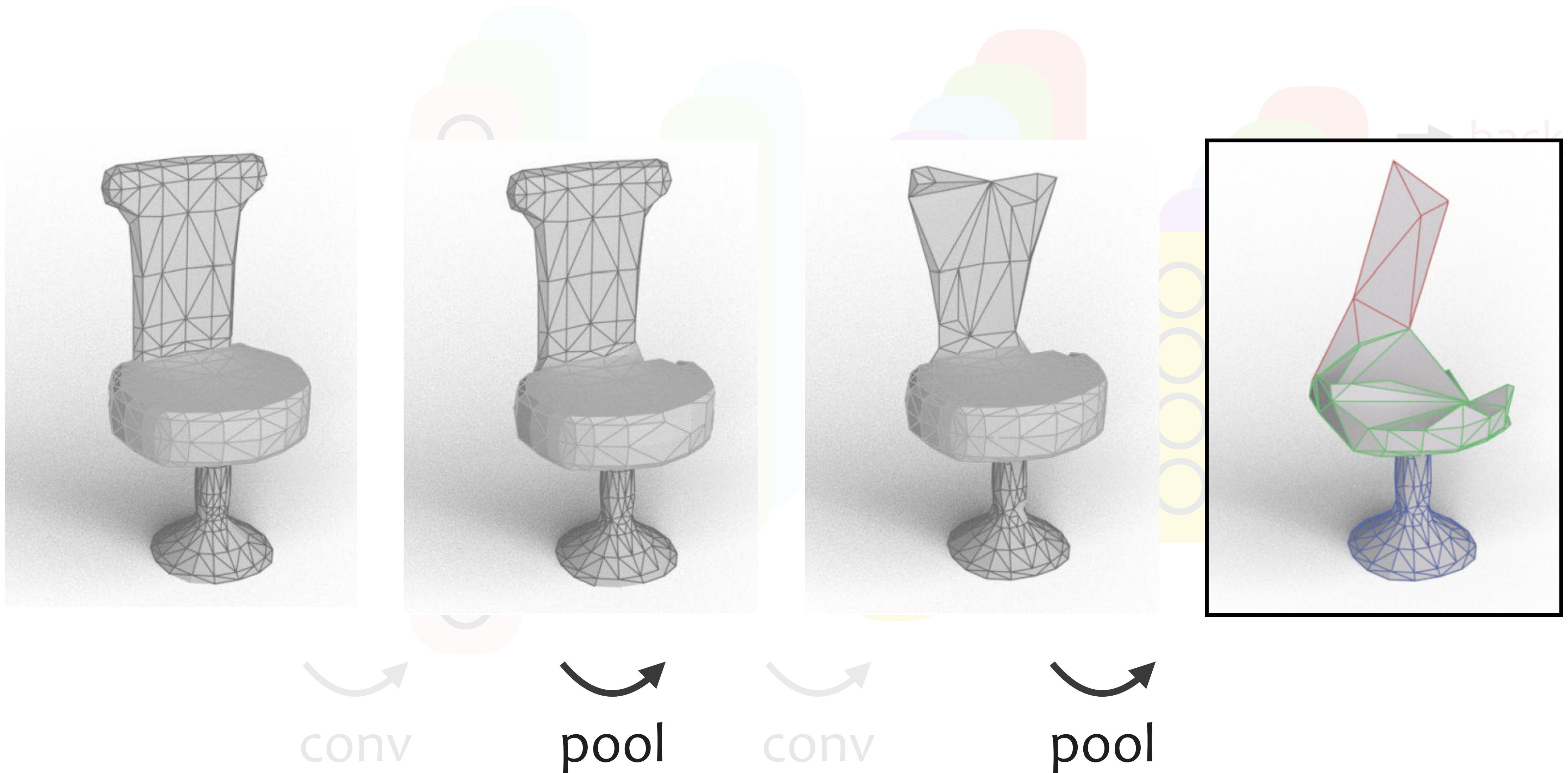
# Learned Local Descriptors



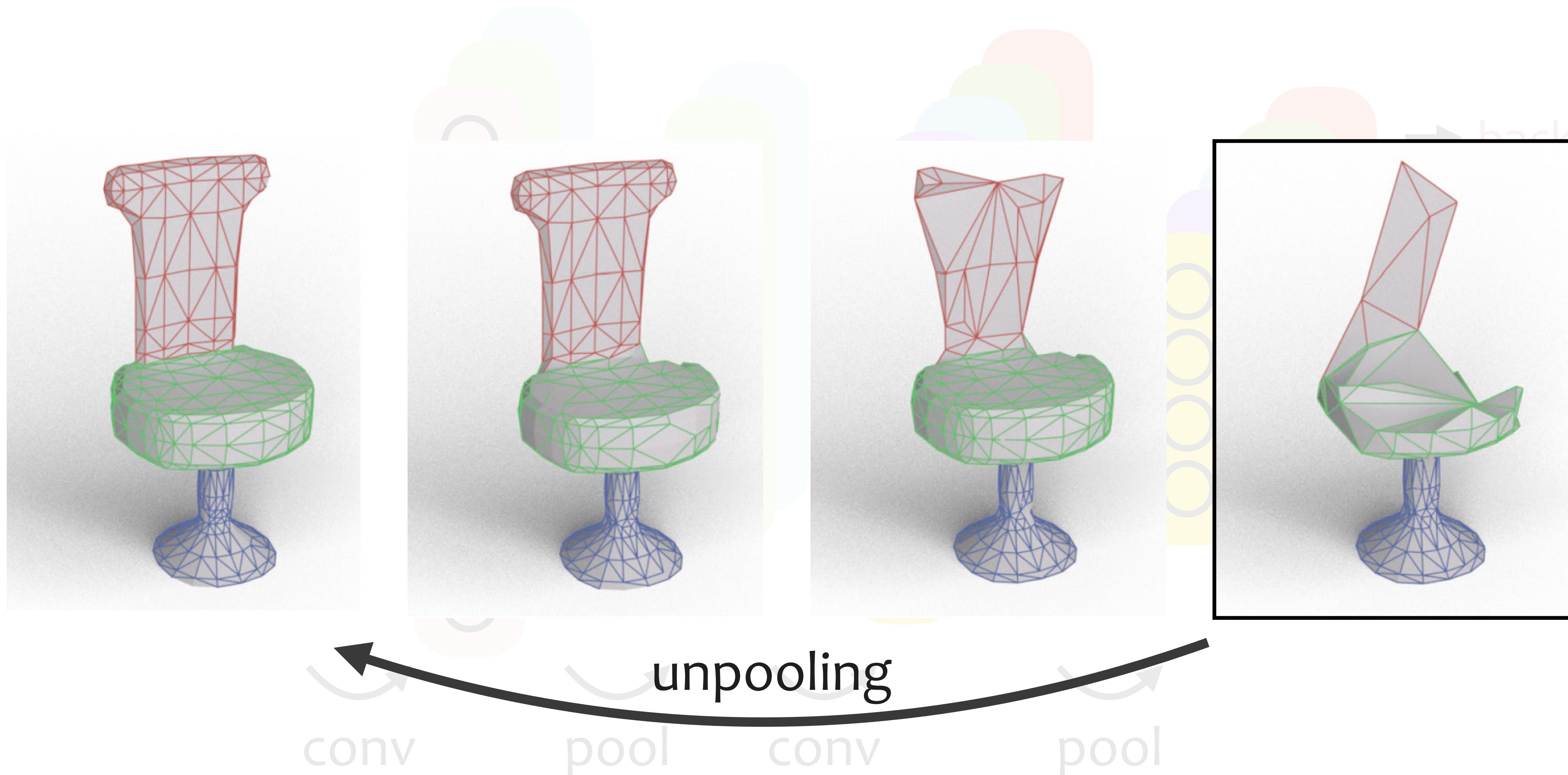
# Machine Learning Segmentation



# Machine Learning Segmentation



# Machine Learning Segmentation



# Handle Shape Variants



isometry

# Handle Shape Variants

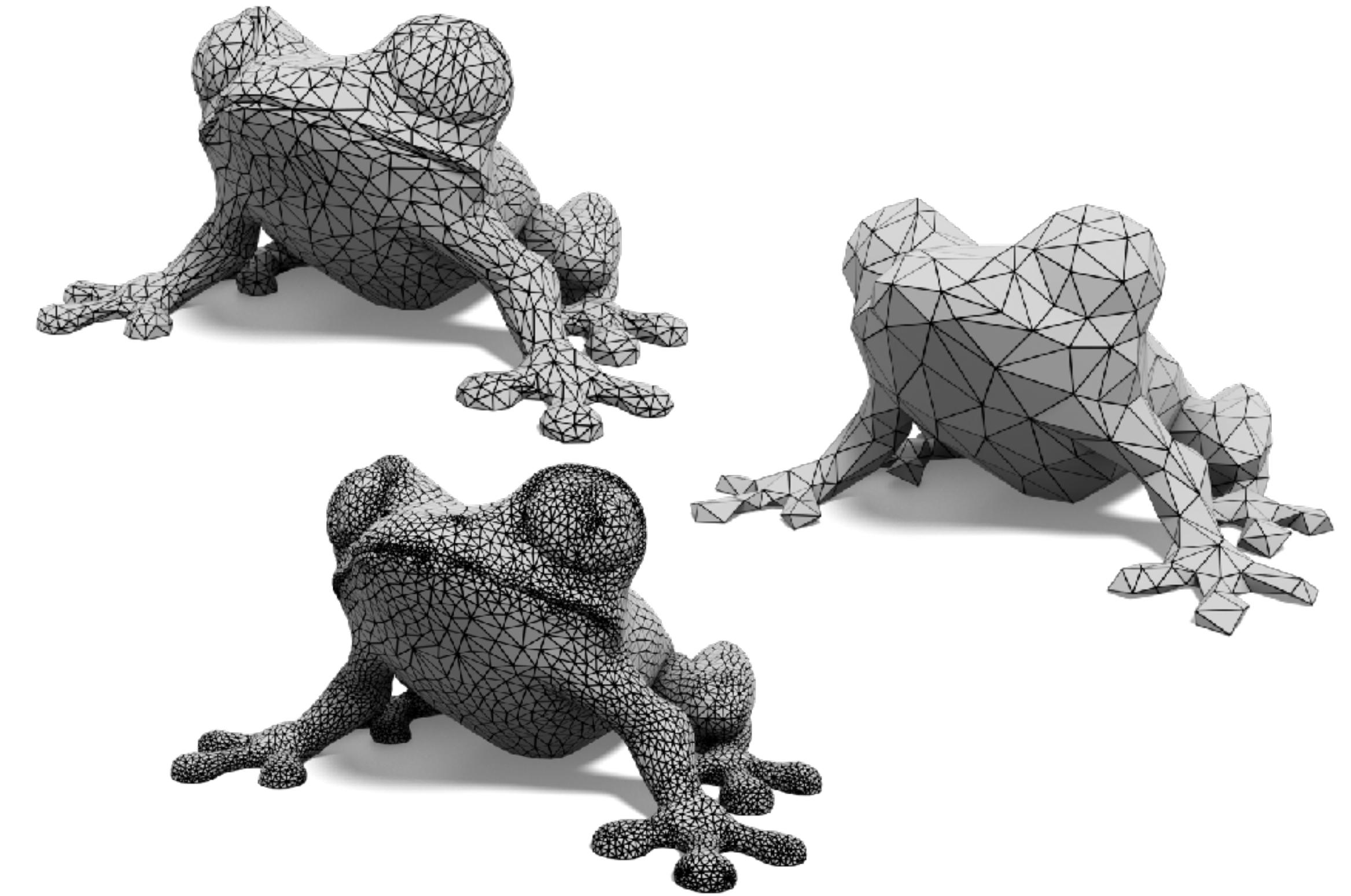


isometry invariant quantities

# Handle Shape Variants



isometry invariant quantities



discretizations

# Handle Shape Variants

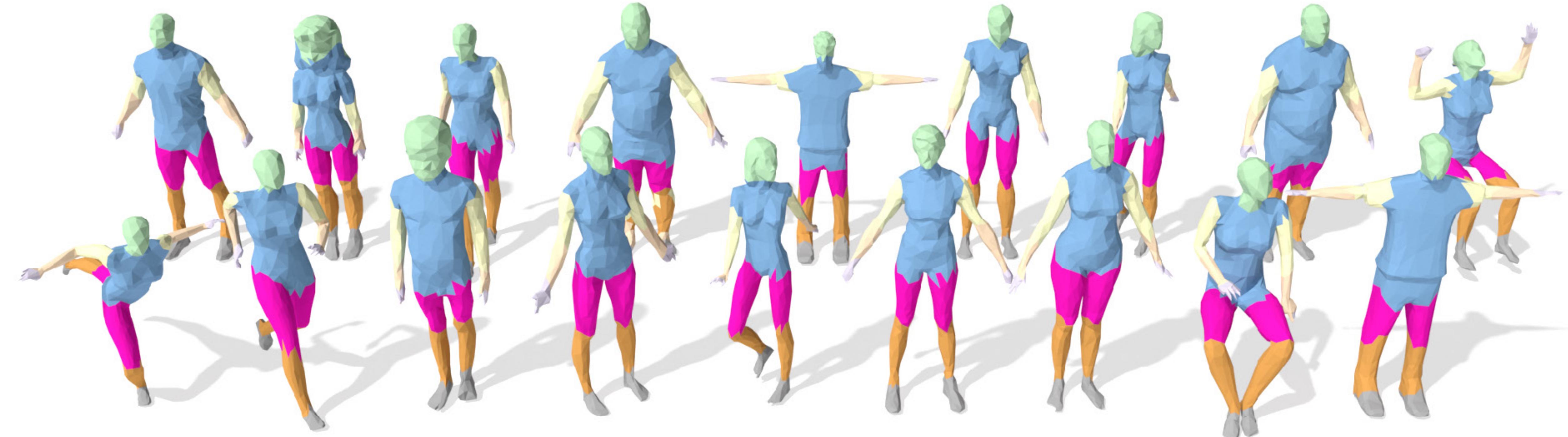


isometry invariant quantities

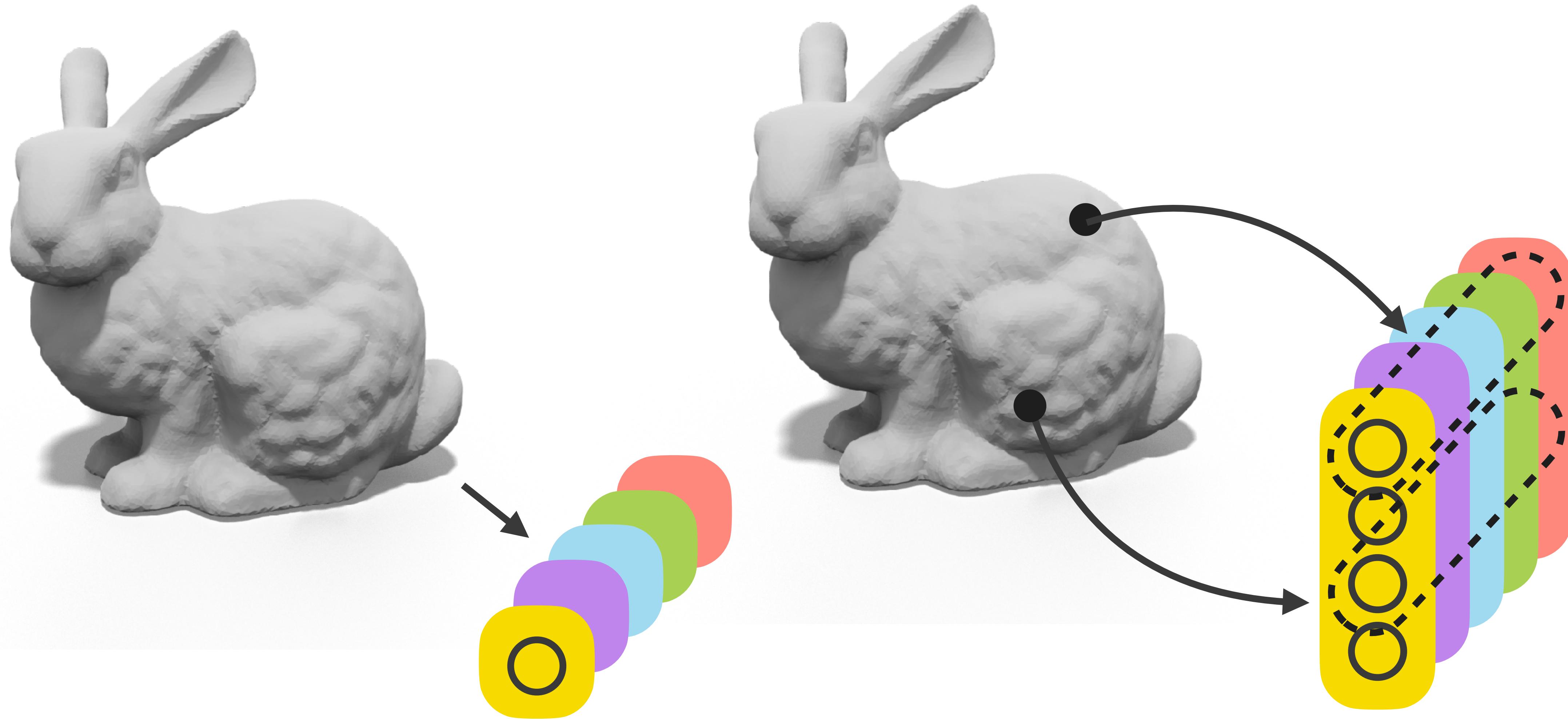


discretization agnostic convolution  
(e.g., Sharp et al. 2021)

# Segmentation

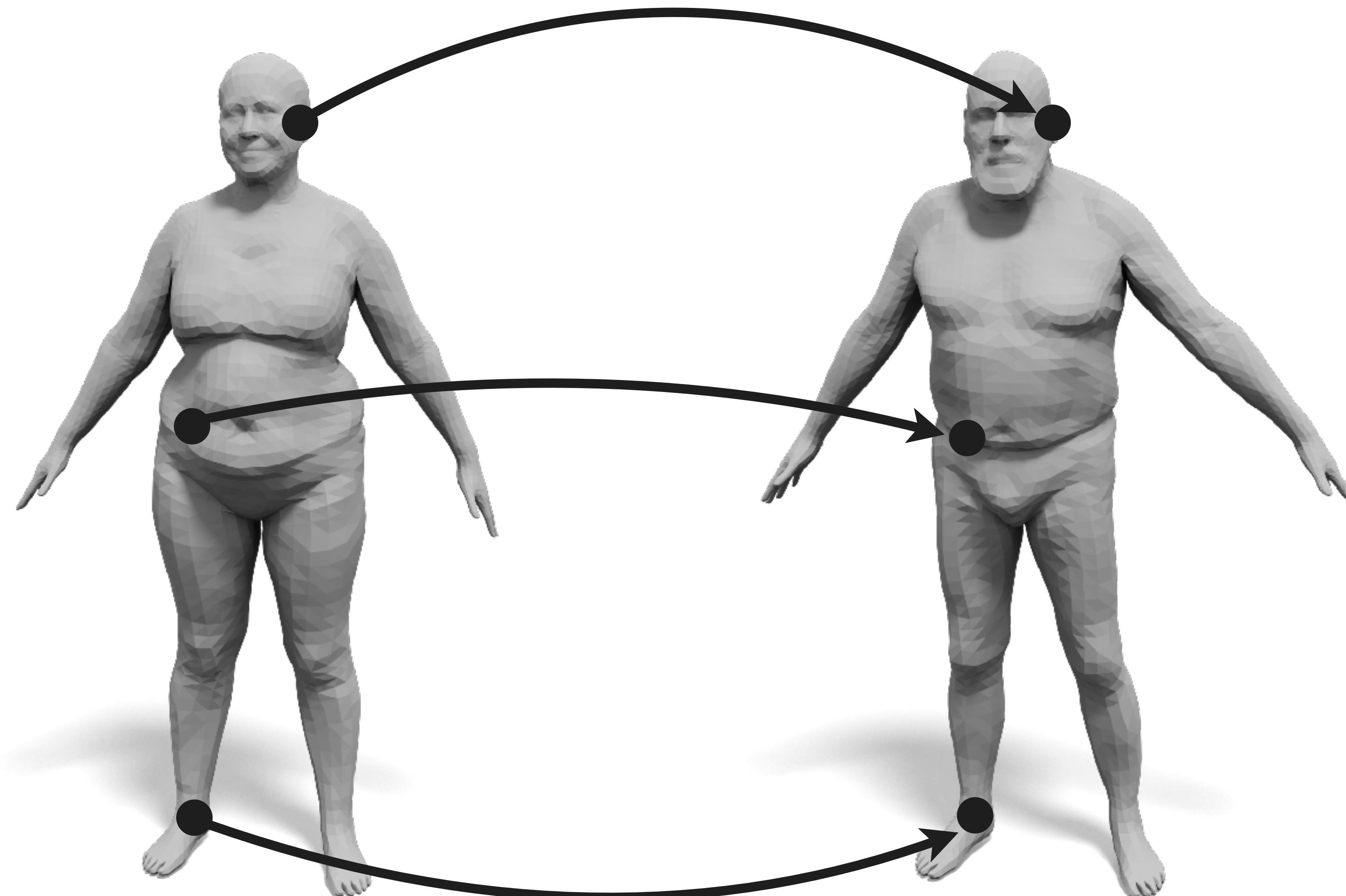


# ML as Feature Extractors

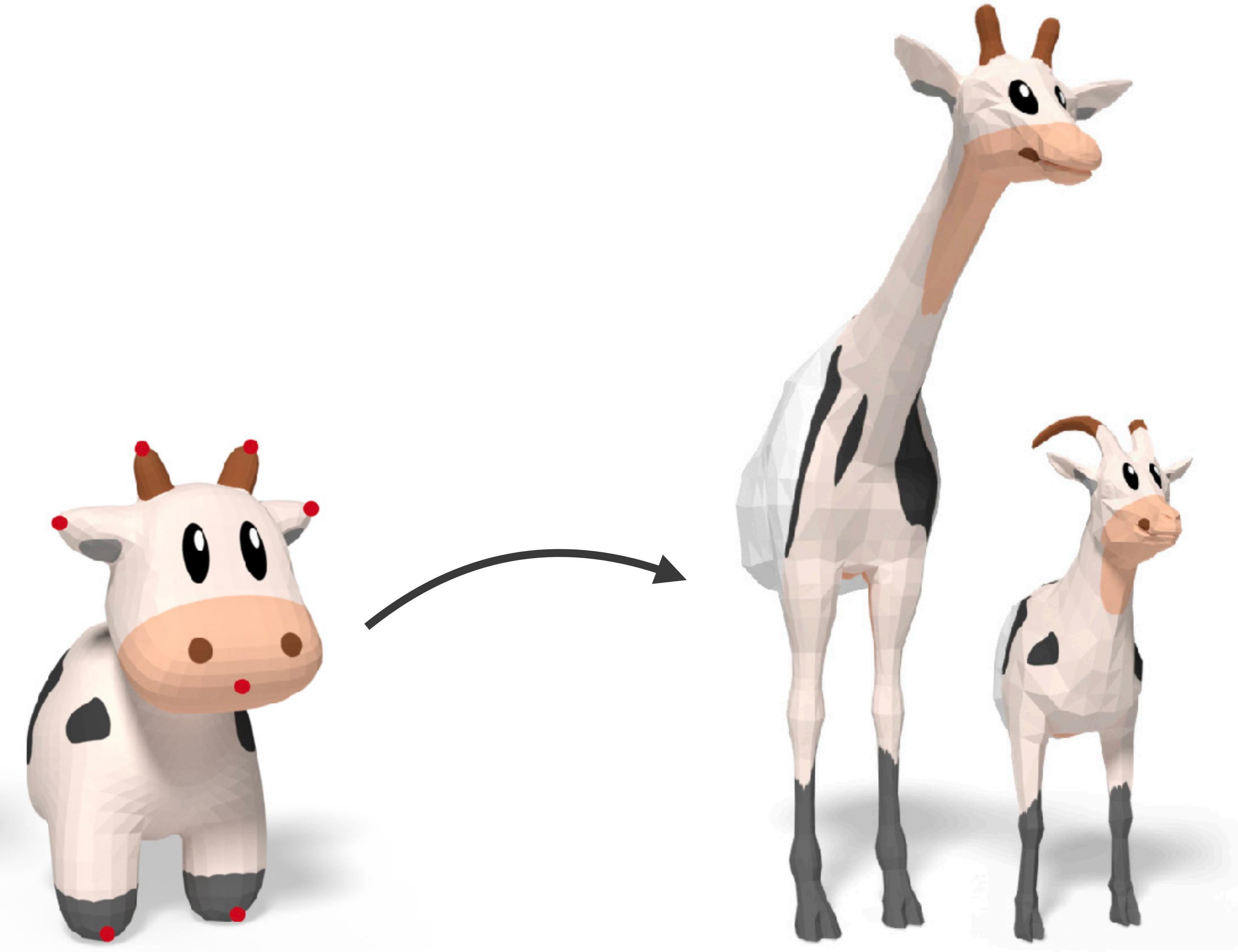


Applications of learned feature extractors  
— combined with classic methods —

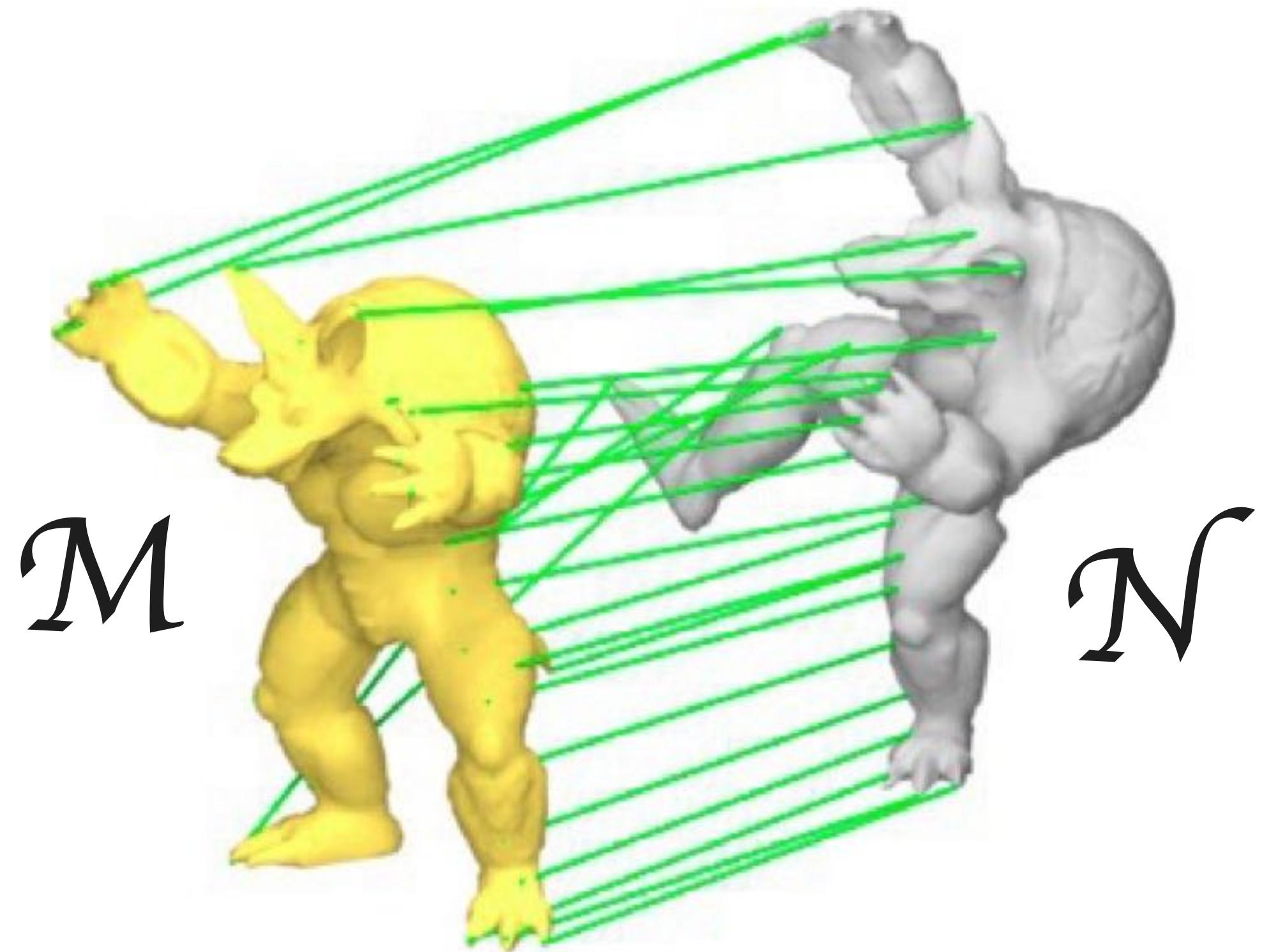
# Example: Shape Matching



# Texture Transfer

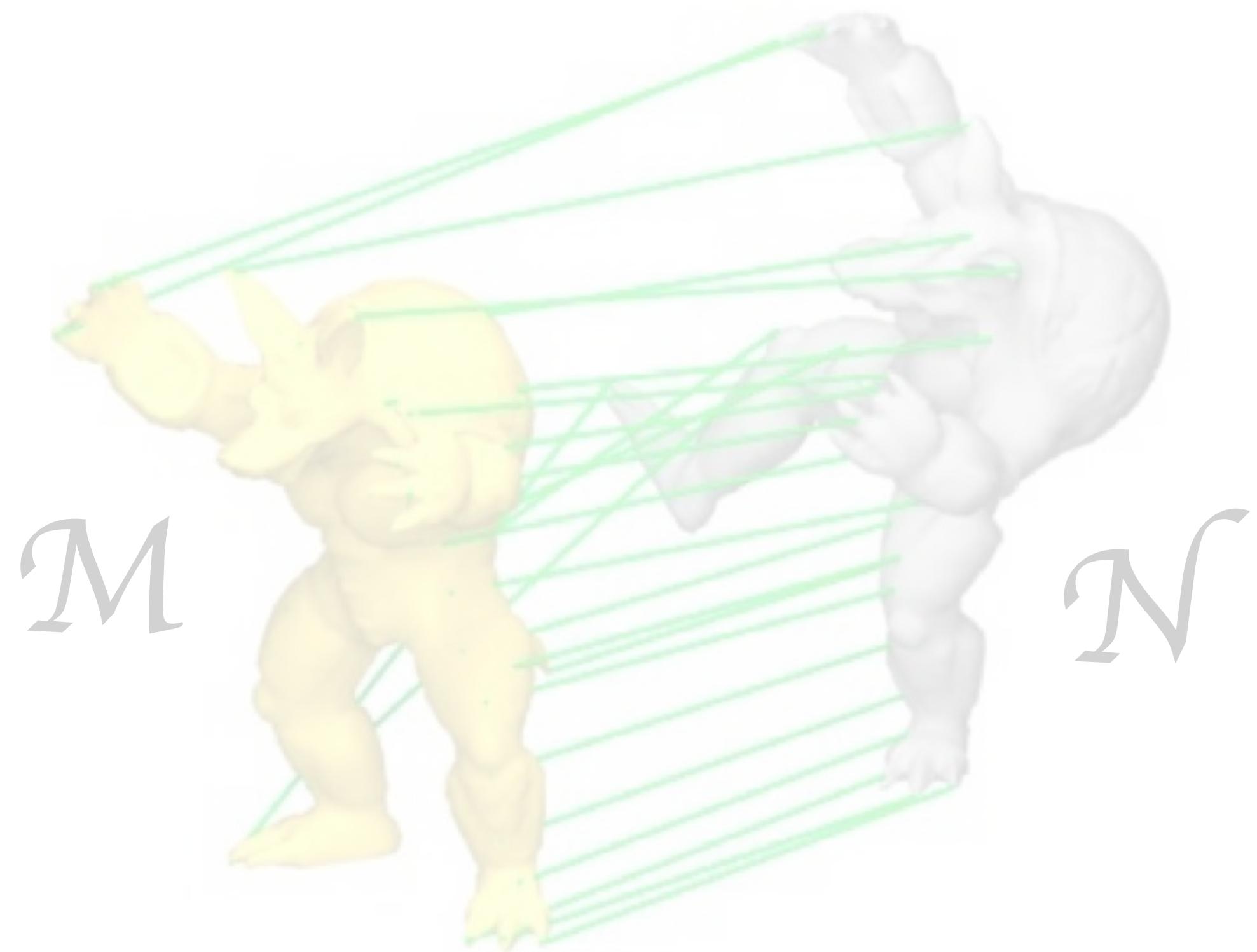


# Point Maps



a point on  $\mathcal{M}$  → a point on  $\mathcal{N}$

# Functional Maps

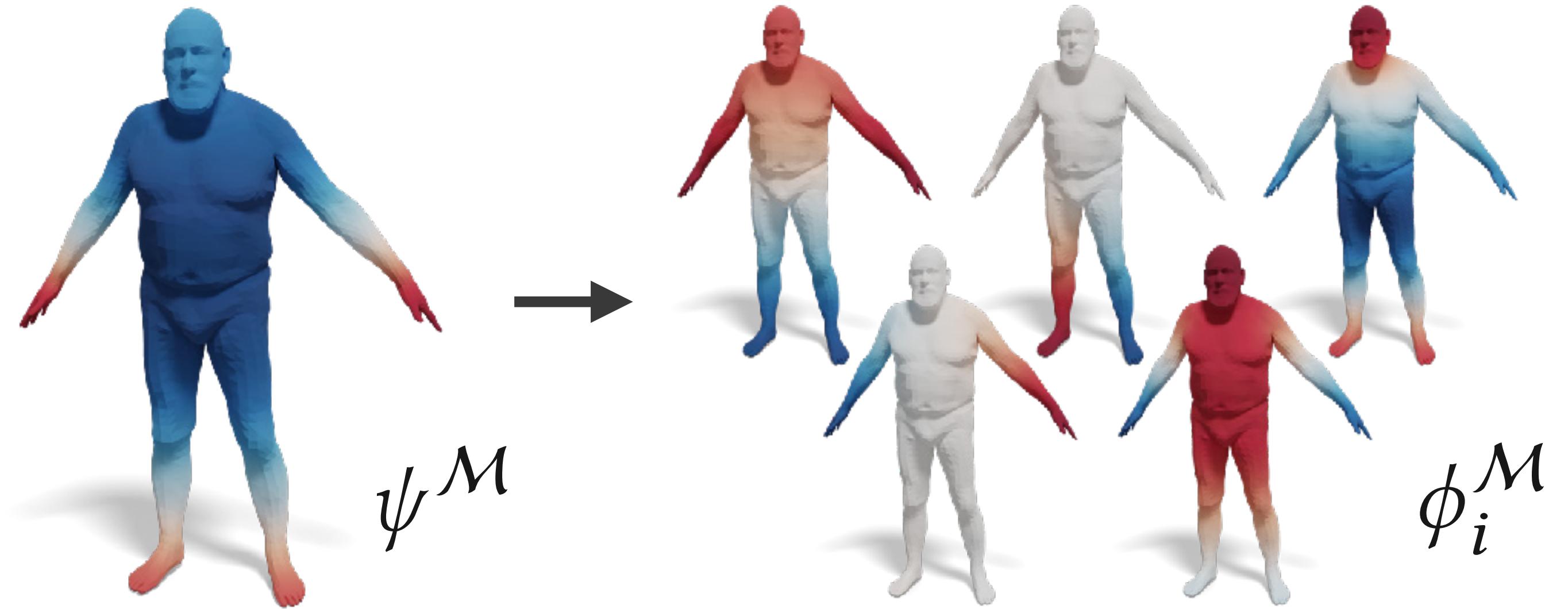


a point on  $\mathcal{M}$  → a point on  $\mathcal{N}$

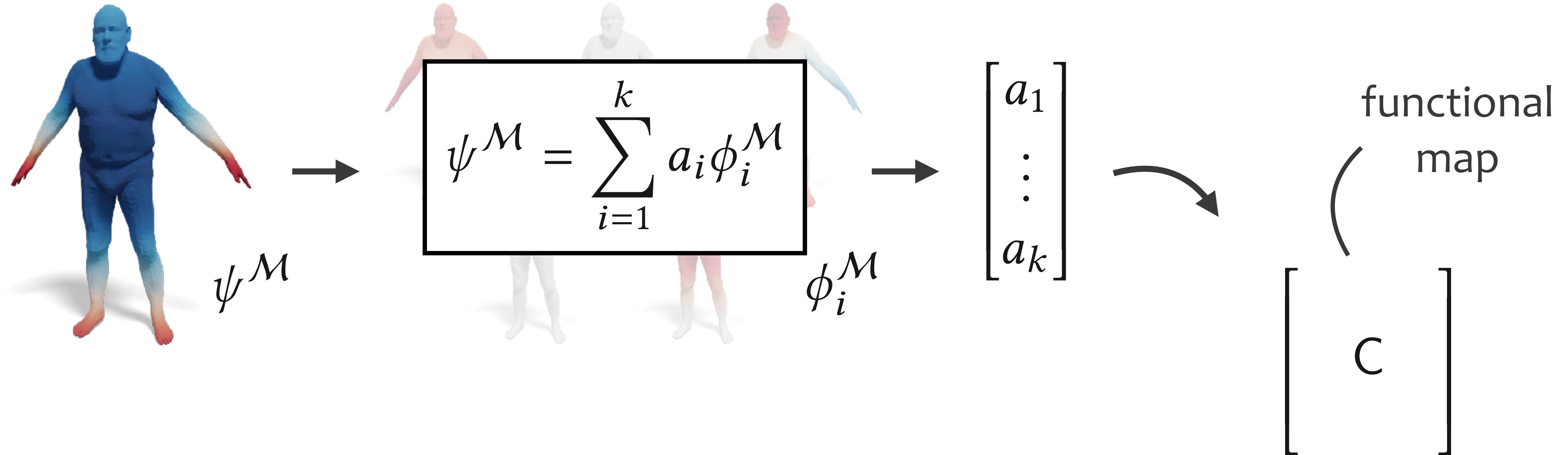


a function on  $\mathcal{M}$  → a function on  $\mathcal{N}$

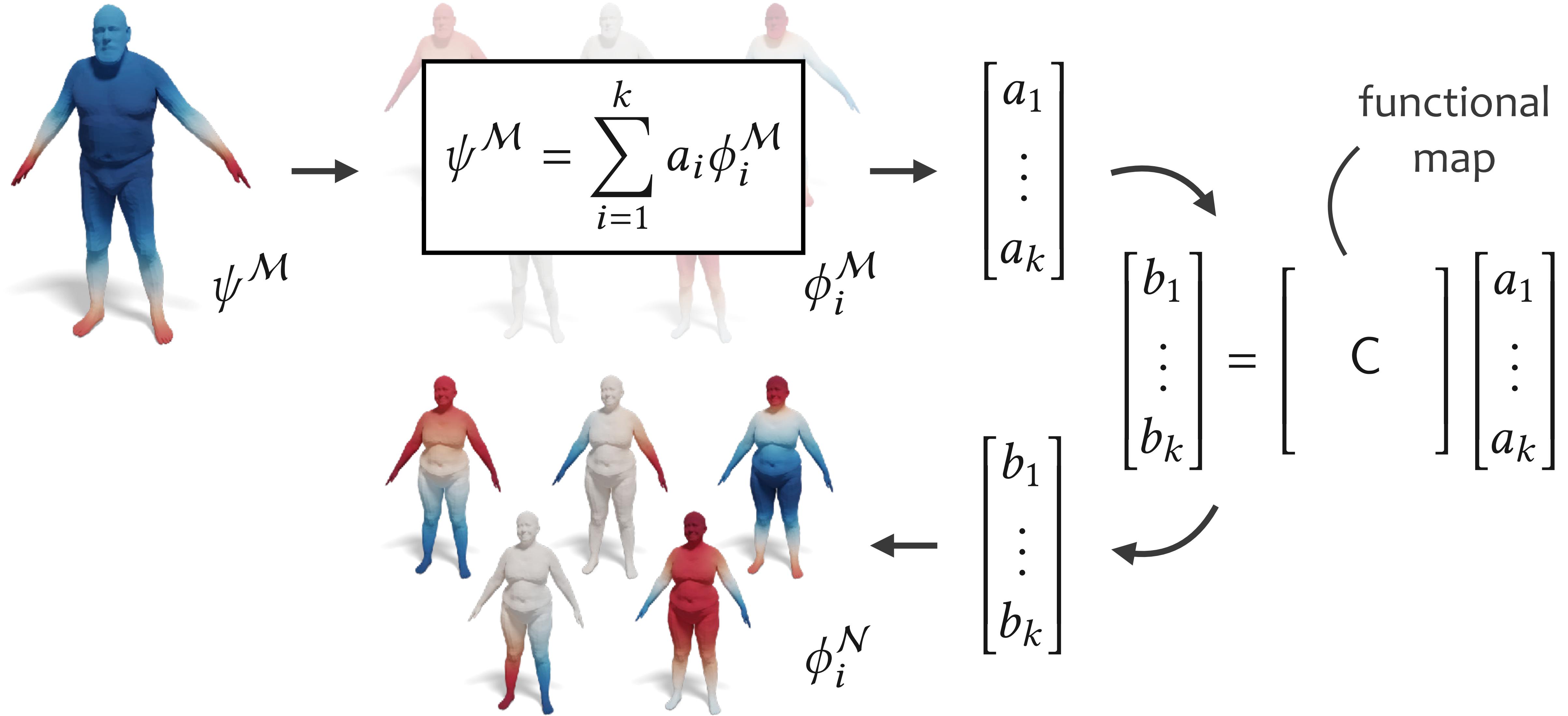
# Functional Maps Overview



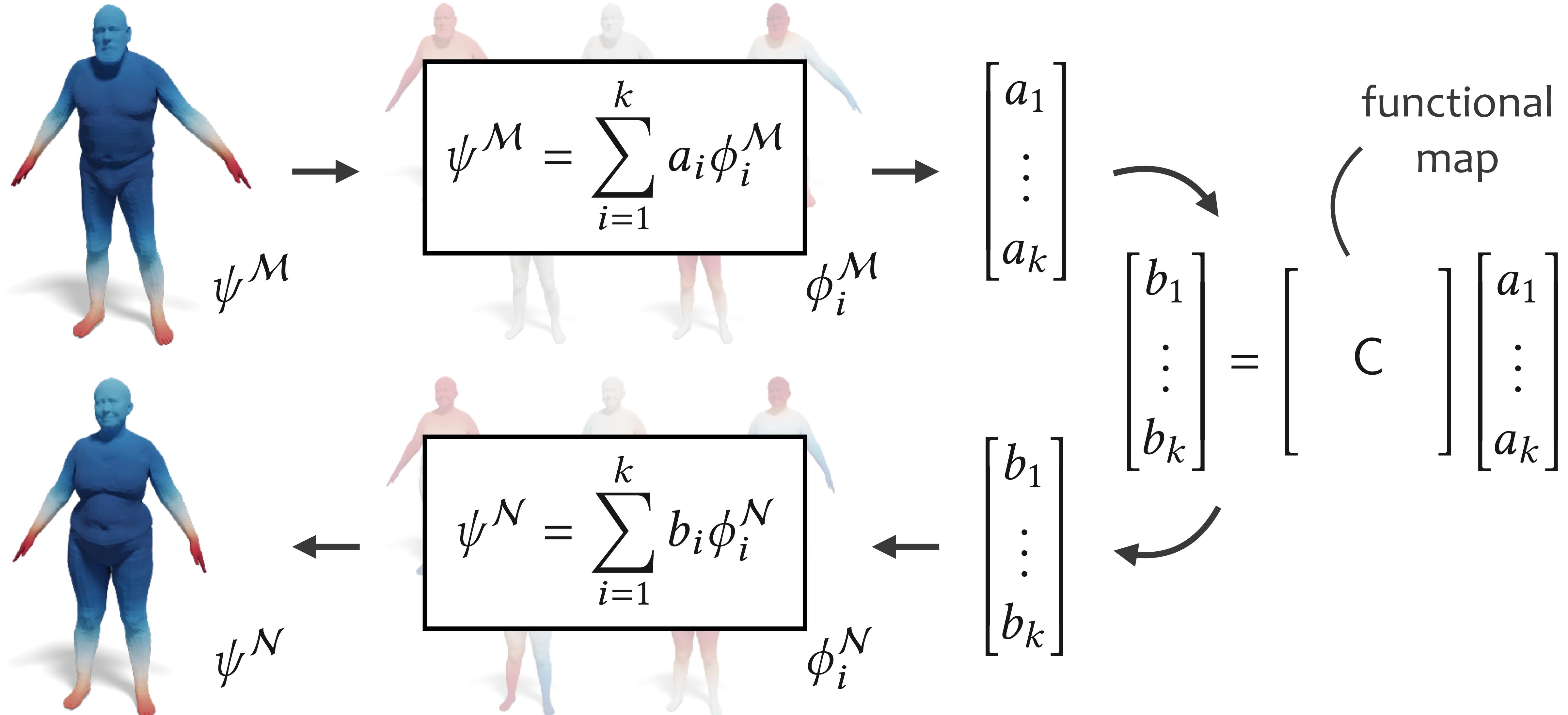
# Functional Maps Overview



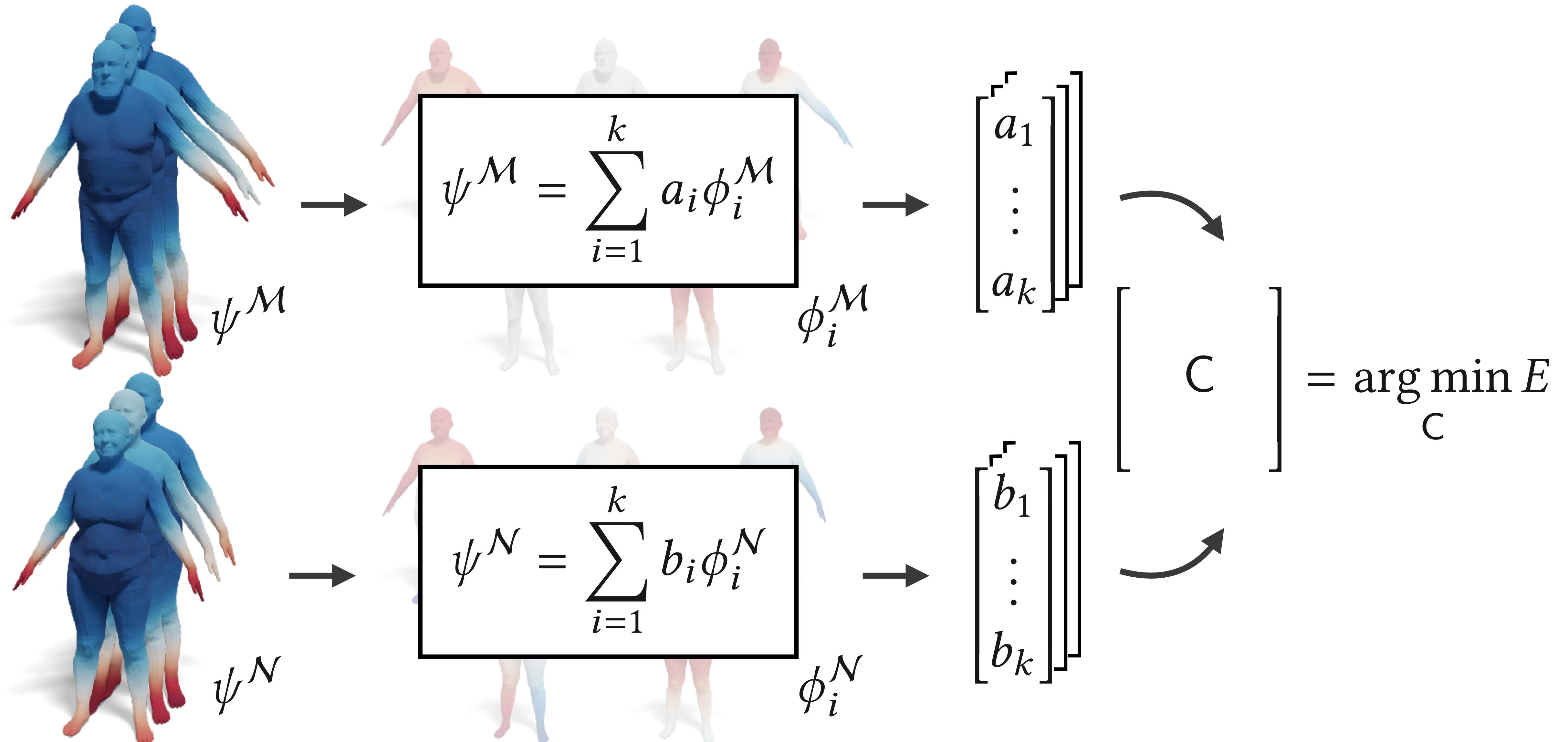
# Functional Maps Overview



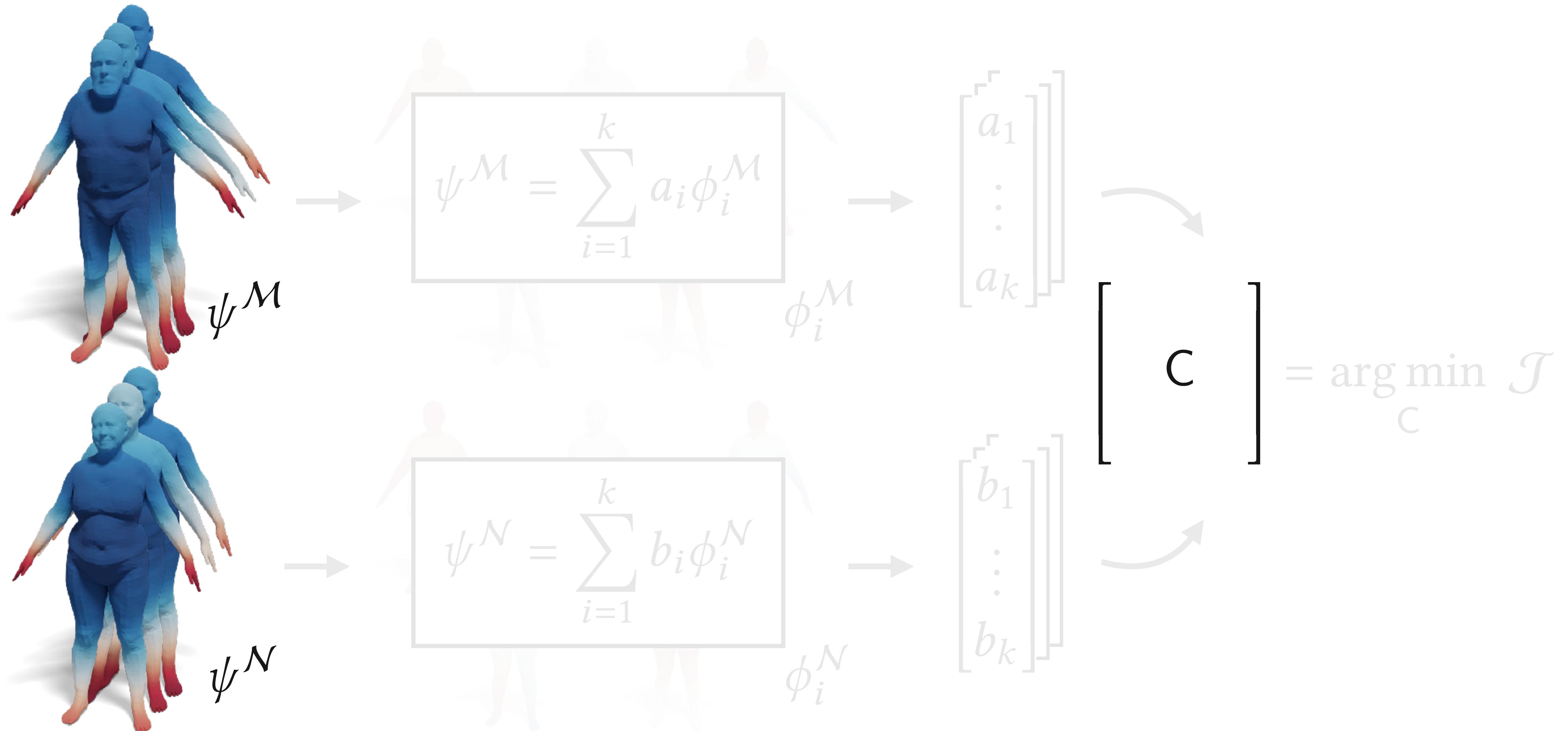
# Functional Maps Overview



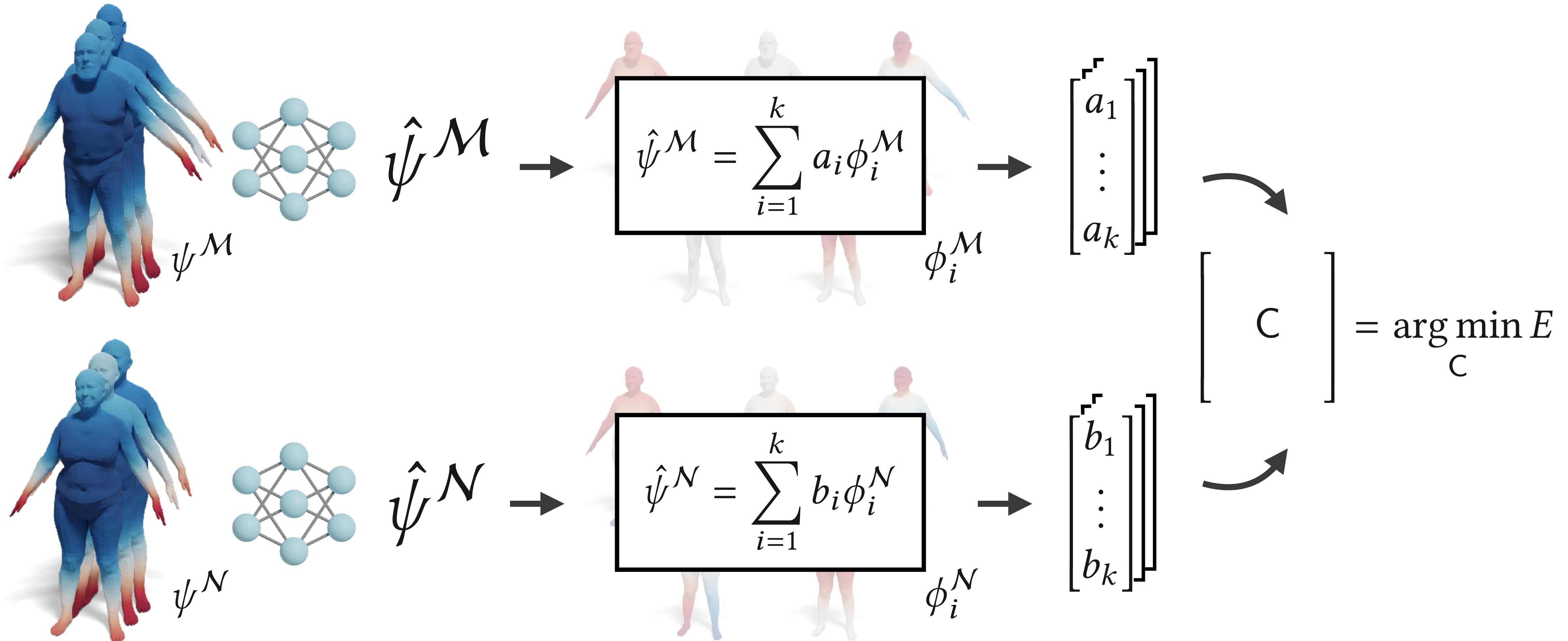
# Computing Functional Maps



# Computing Functional Maps



# Deep Functional Maps



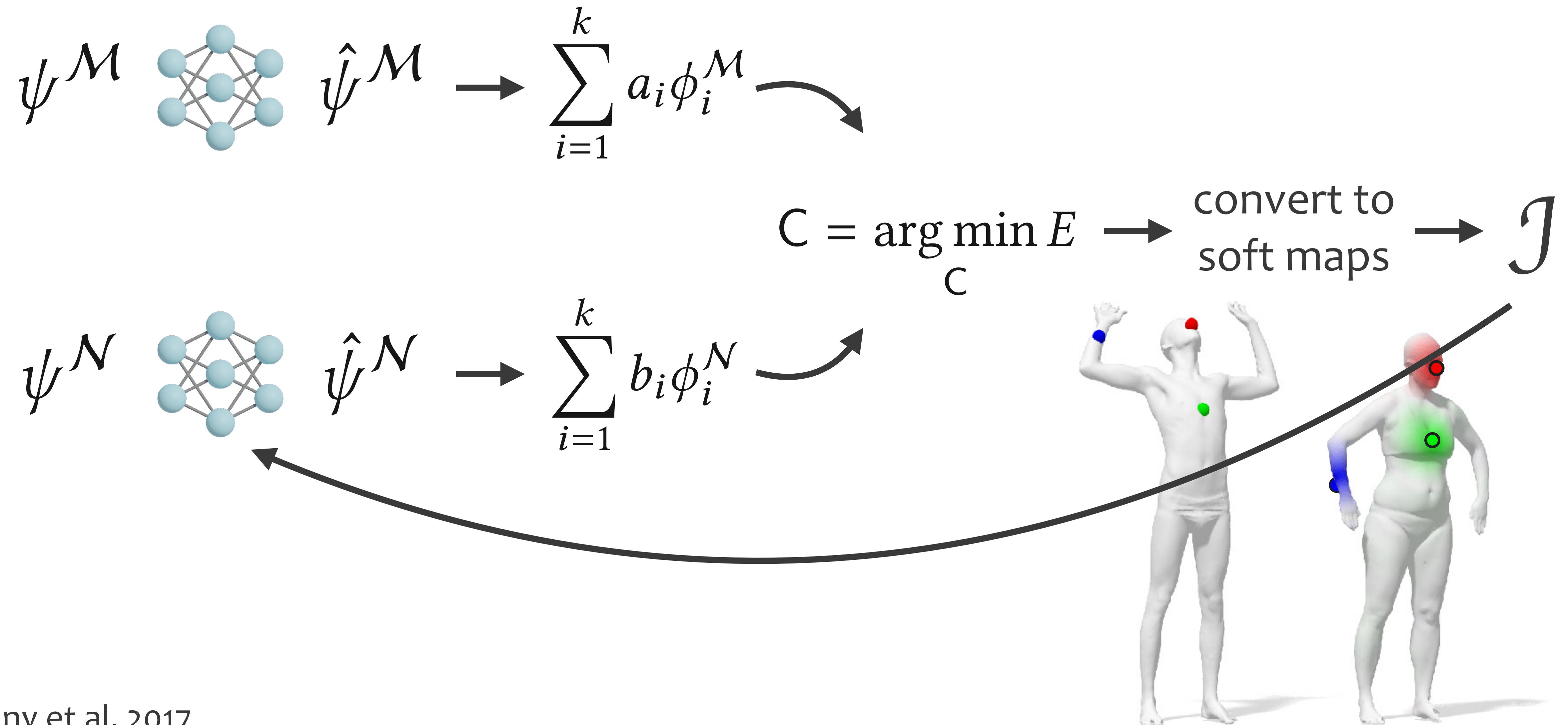
# Deep Functional Maps

$$\psi^{\mathcal{M}} \quad \text{graph icon} \quad \hat{\psi}^{\mathcal{M}} \rightarrow \sum_{i=1}^k a_i \phi_i^{\mathcal{M}}$$

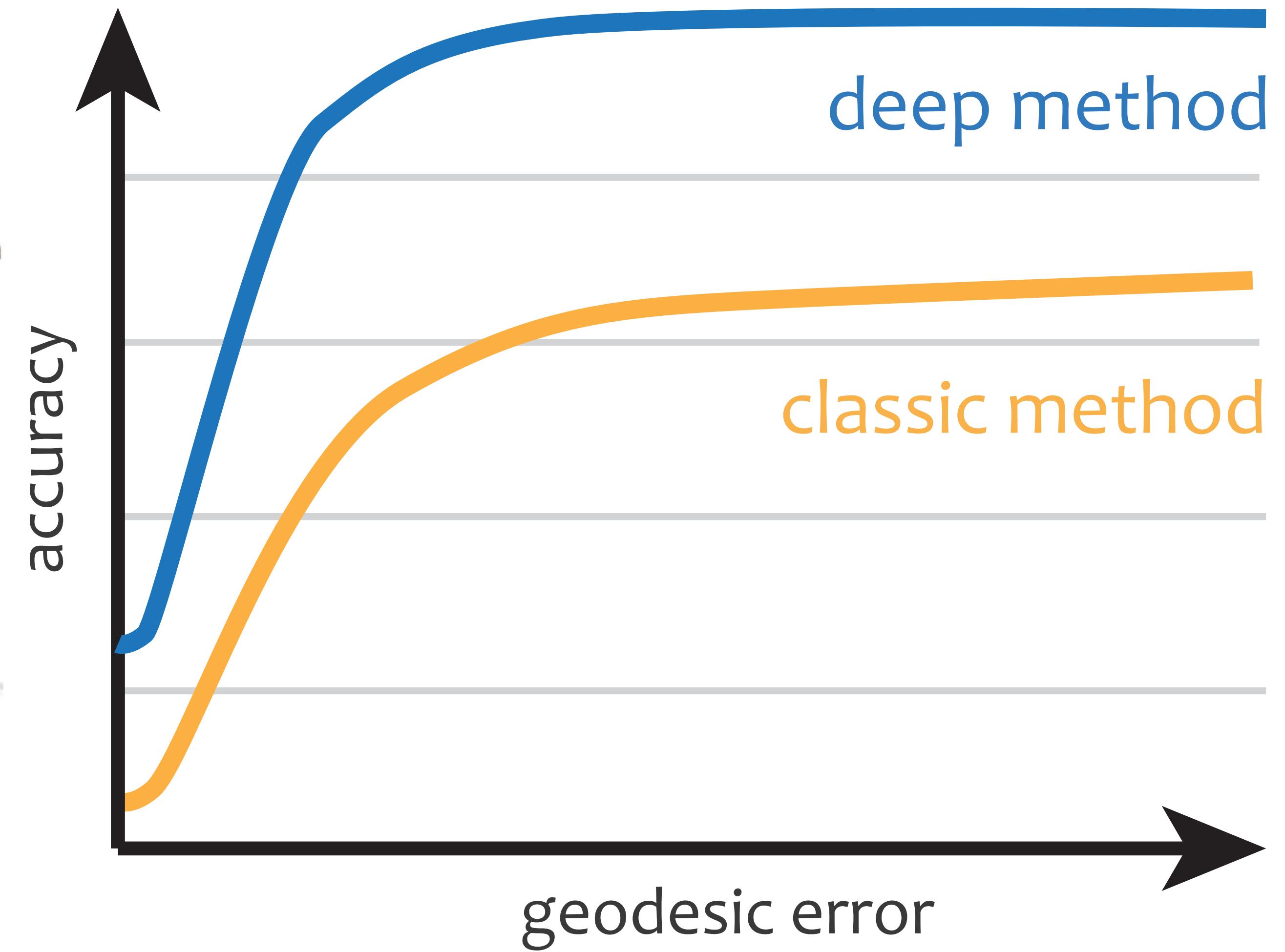
$$C = \arg \min_C E$$

$$\psi^{\mathcal{N}} \quad \text{graph icon} \quad \hat{\psi}^{\mathcal{N}} \rightarrow \sum_{i=1}^k b_i \phi_i^{\mathcal{N}}$$

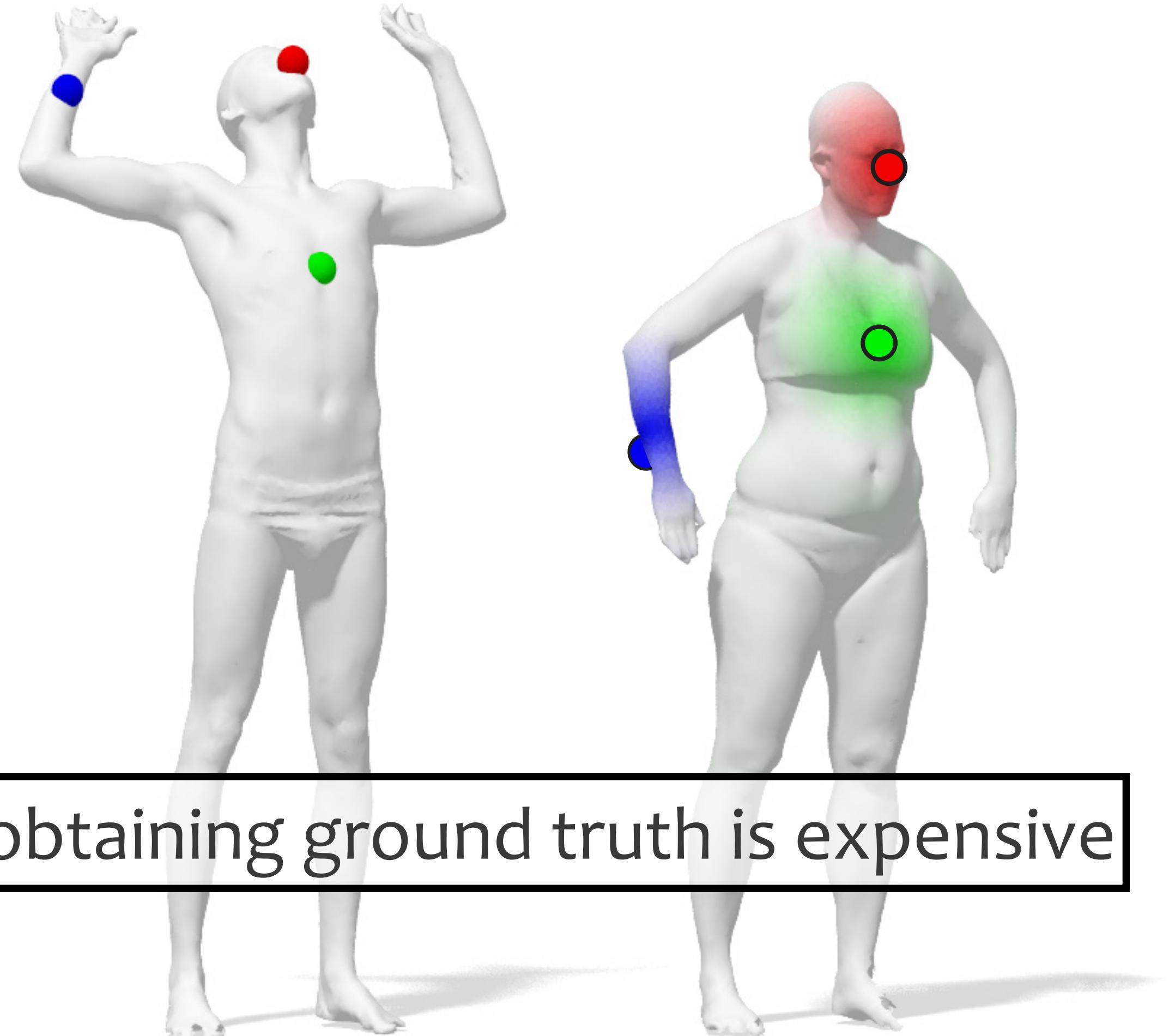
# Deep Functional Maps



# Push the limits

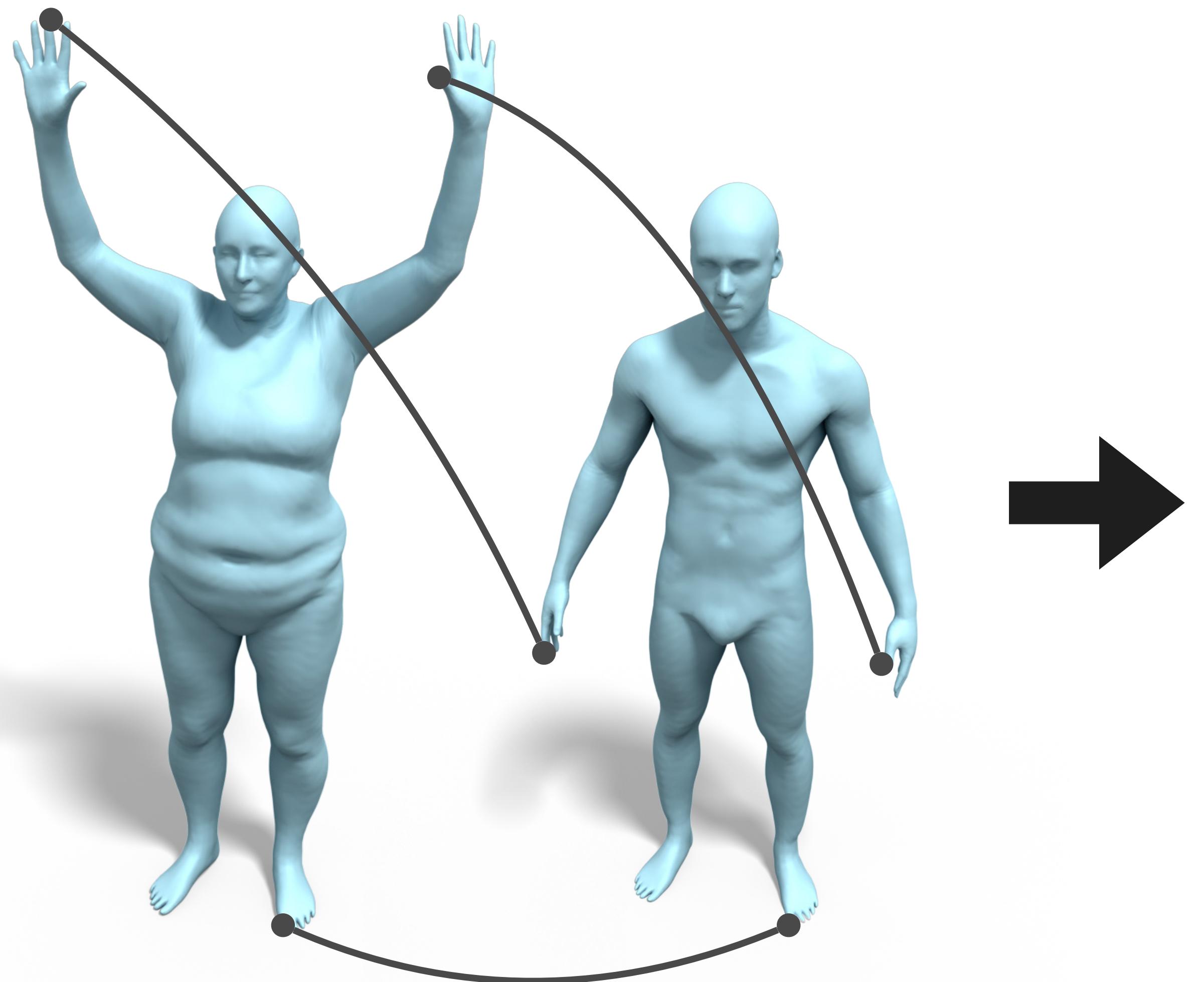


# Requires Supervision



obtaining ground truth is expensive

# Classic Approaches

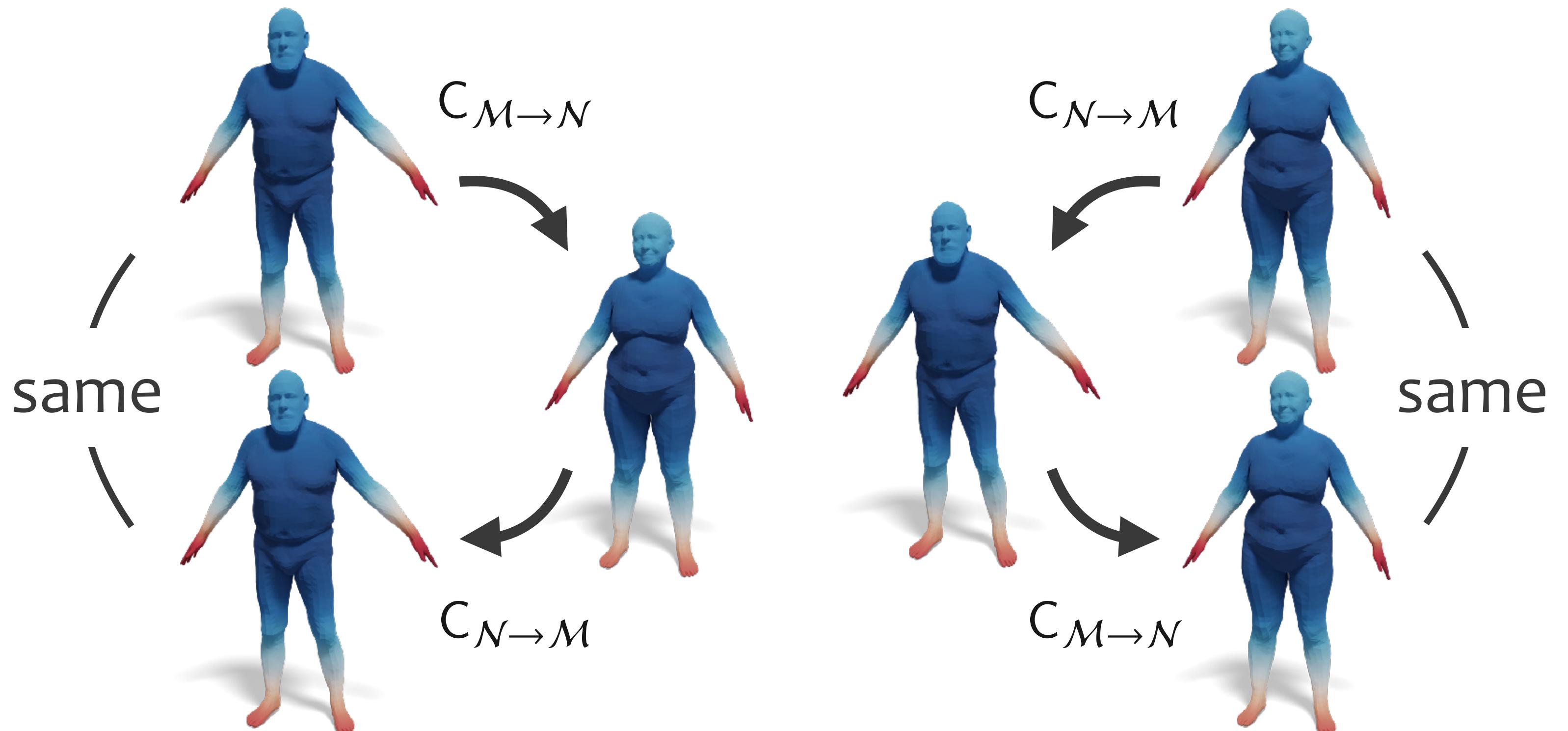


$$\arg \min_C \mathcal{E}(C)$$

$$\begin{aligned}\mathcal{E}(C) = & \alpha_1 E_1(C) + \alpha_2 E_2(C) \\ & + \alpha_3 E_3(C) + \alpha_4 E_4(C)\end{aligned}$$

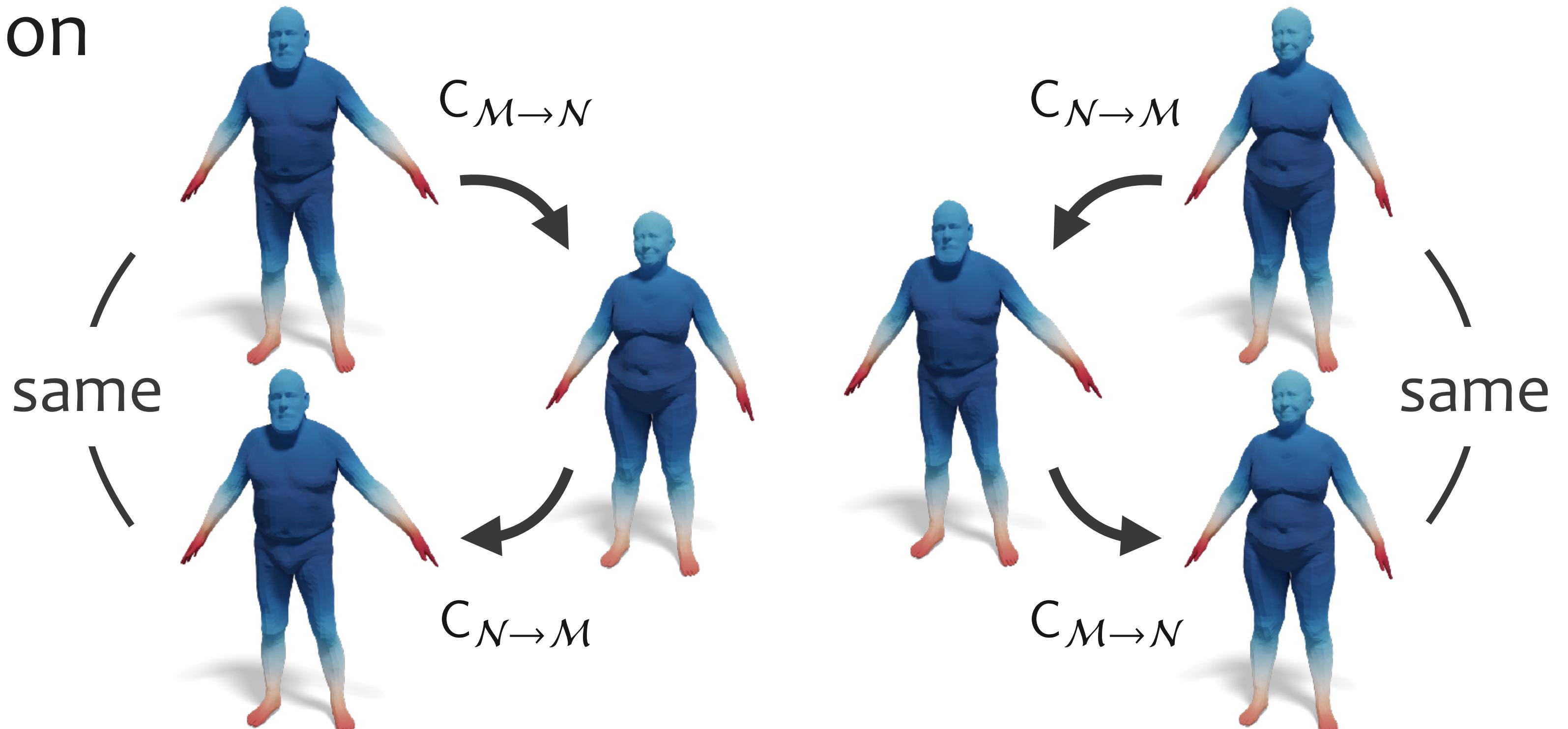
# Desired Properties

- Bijectivity

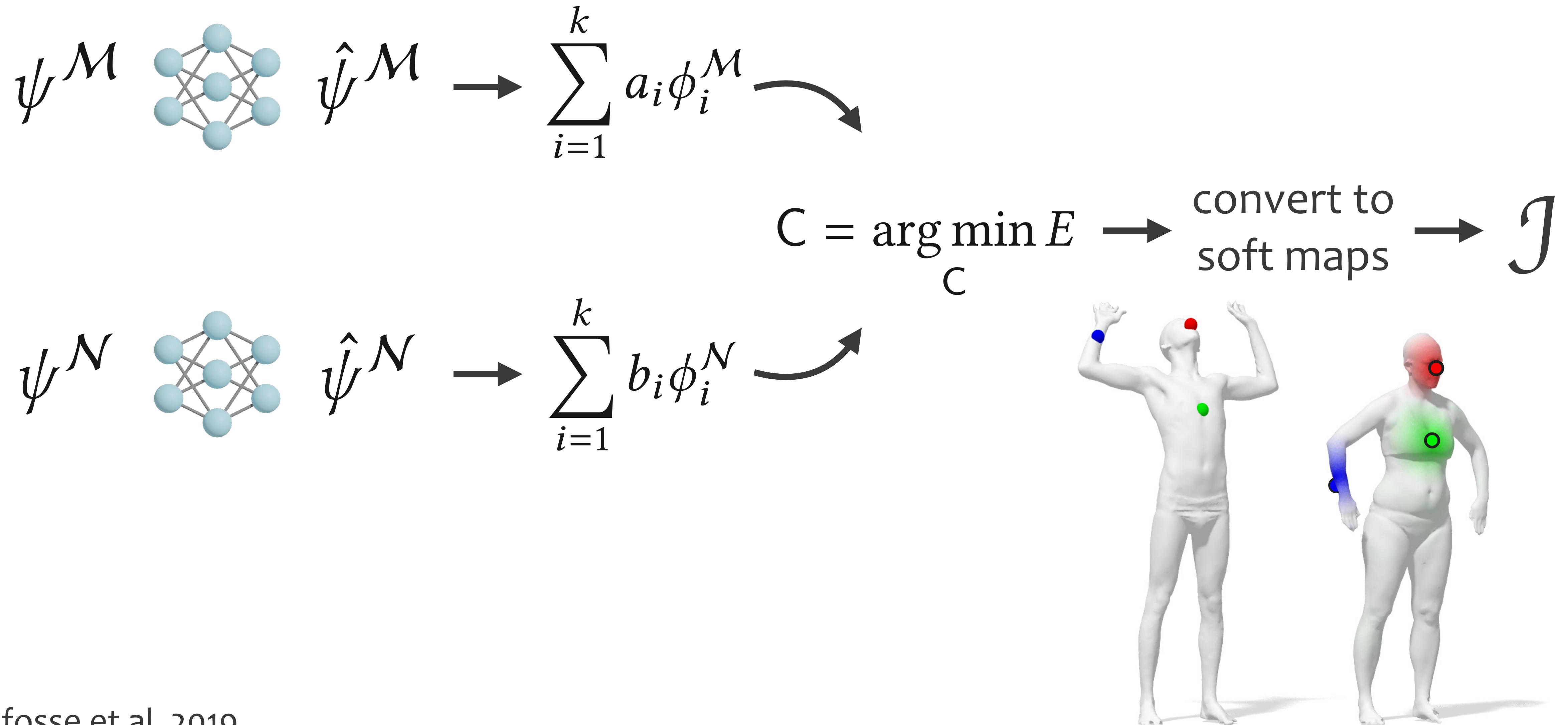


# Desired Properties

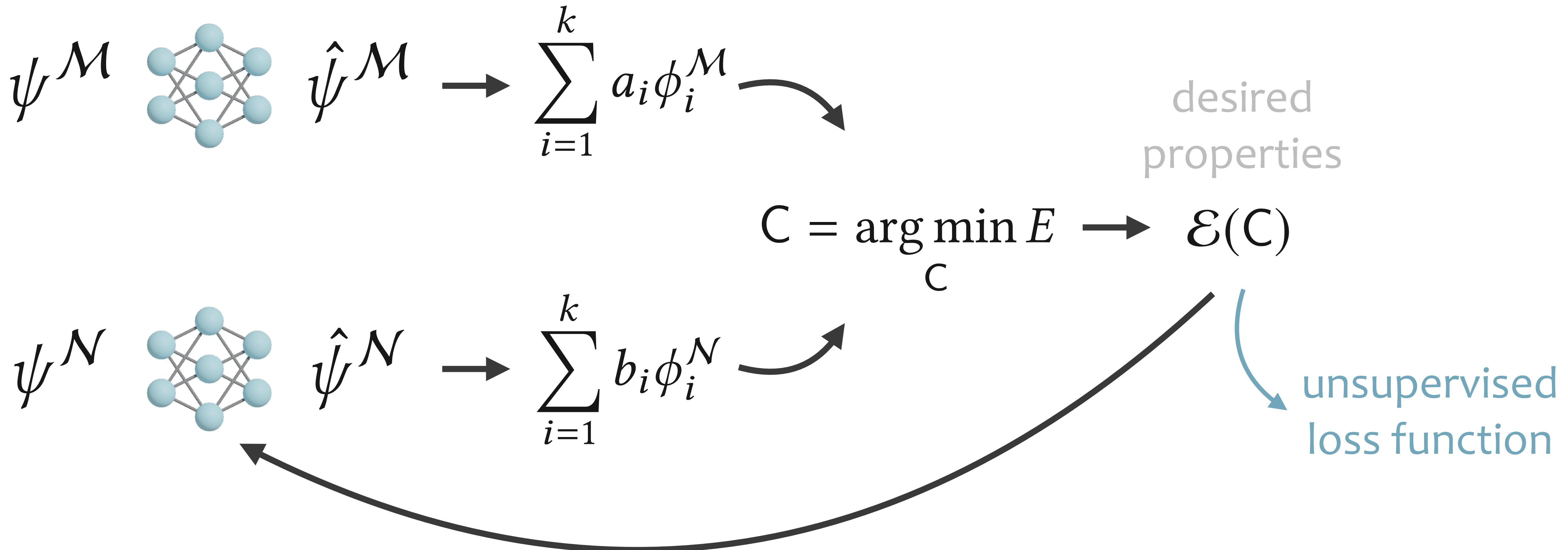
- Bijectivity
- Area preservation
- Laplacian commutativity
- Descriptor preservation
- ...



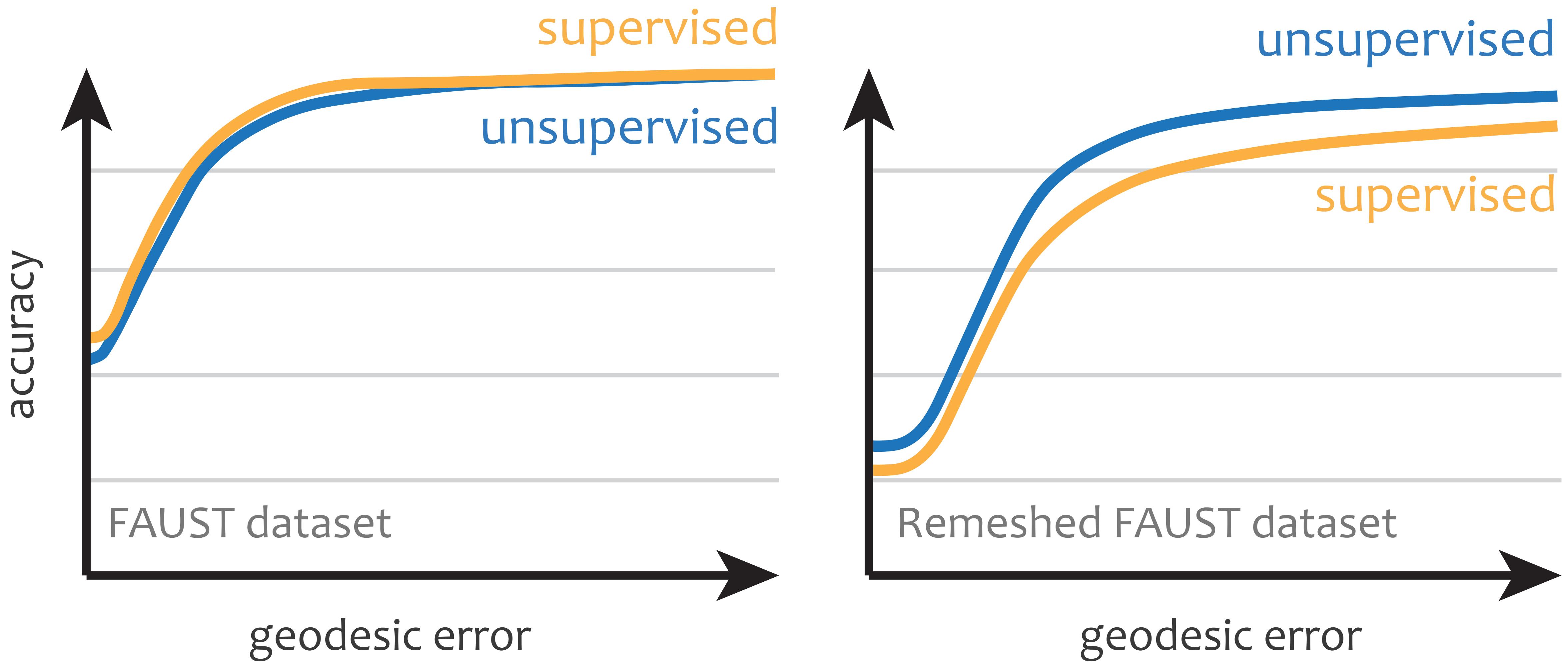
# From Supervised to Unsupervised



# From Supervised to Unsupervised



# Comparable Results



# Key Takeaways

good results, but not perfect

use machine  
learning

push the limit

require supervision

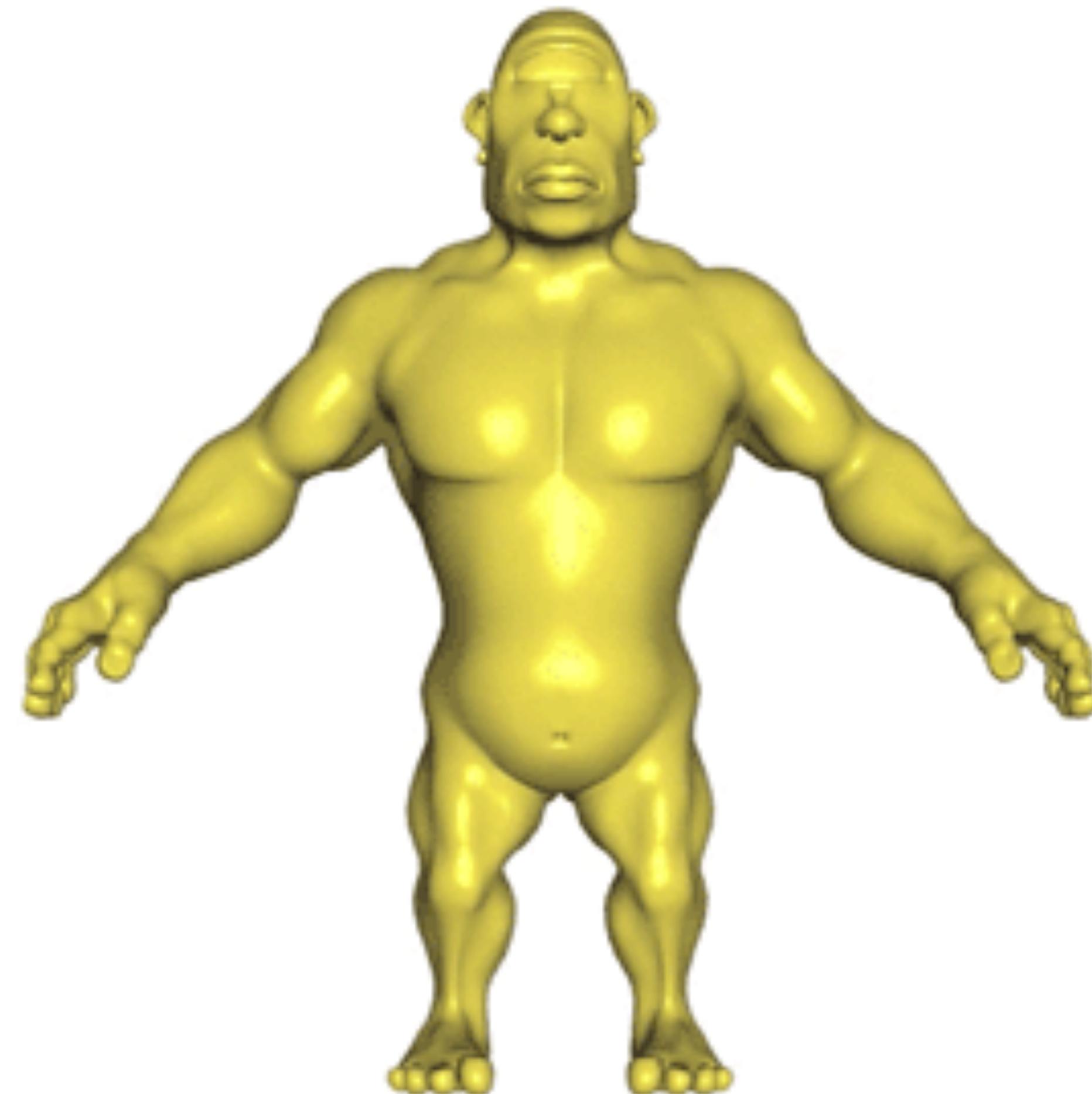
combine with  
classic method

push the limit

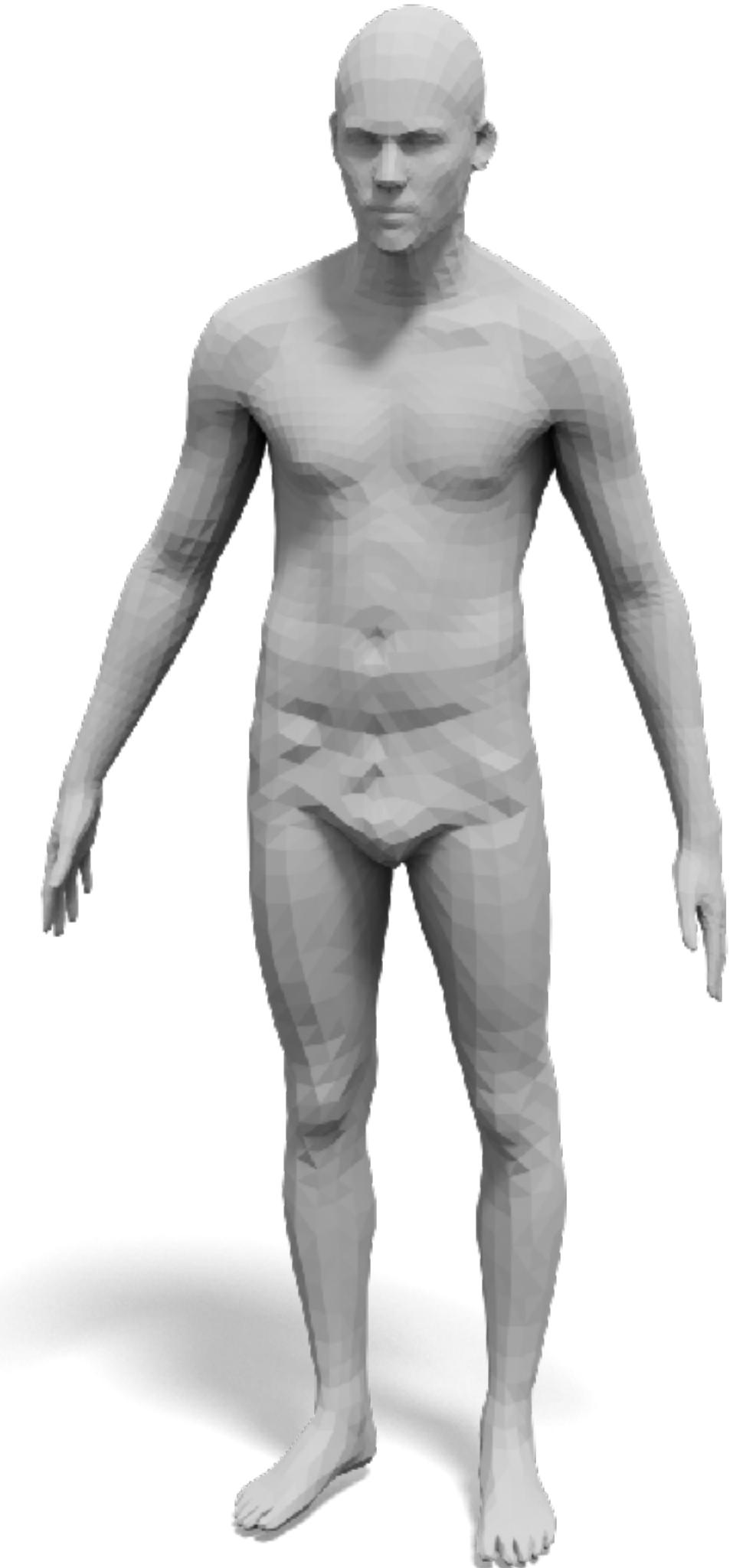
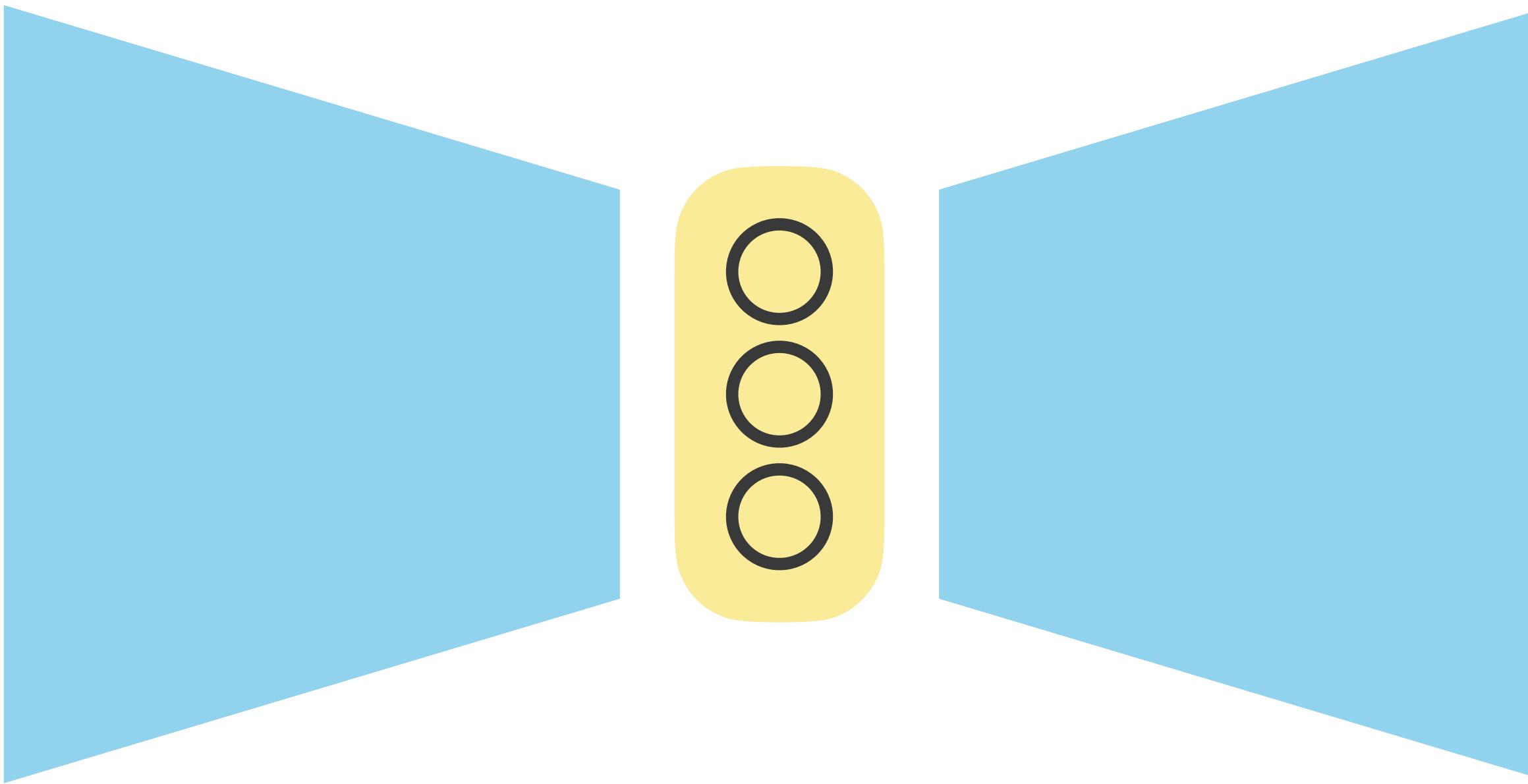
weak/no supervision

open questions

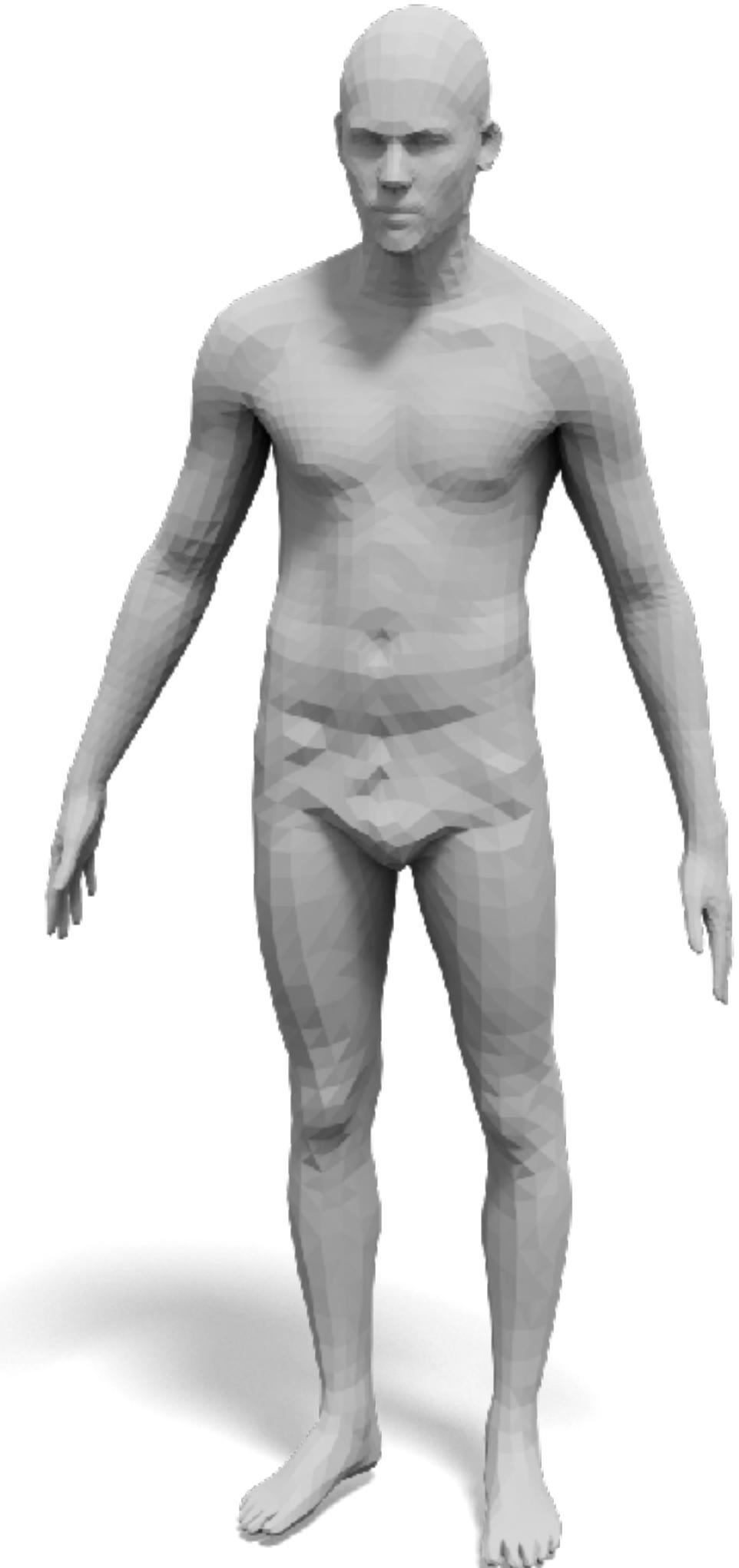
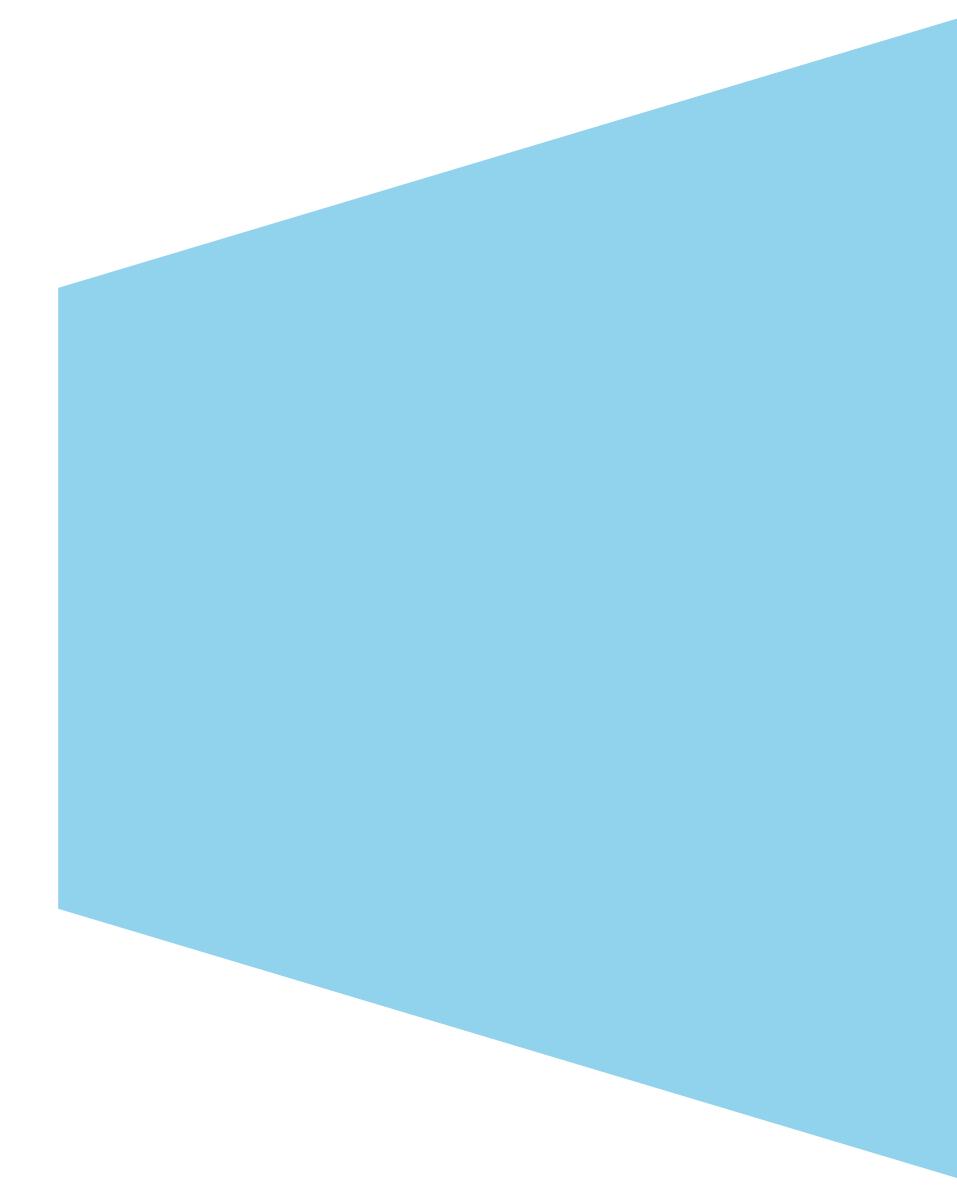
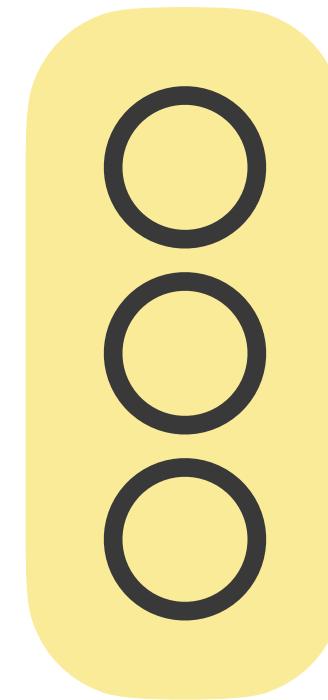
# Example: Shape Deformation



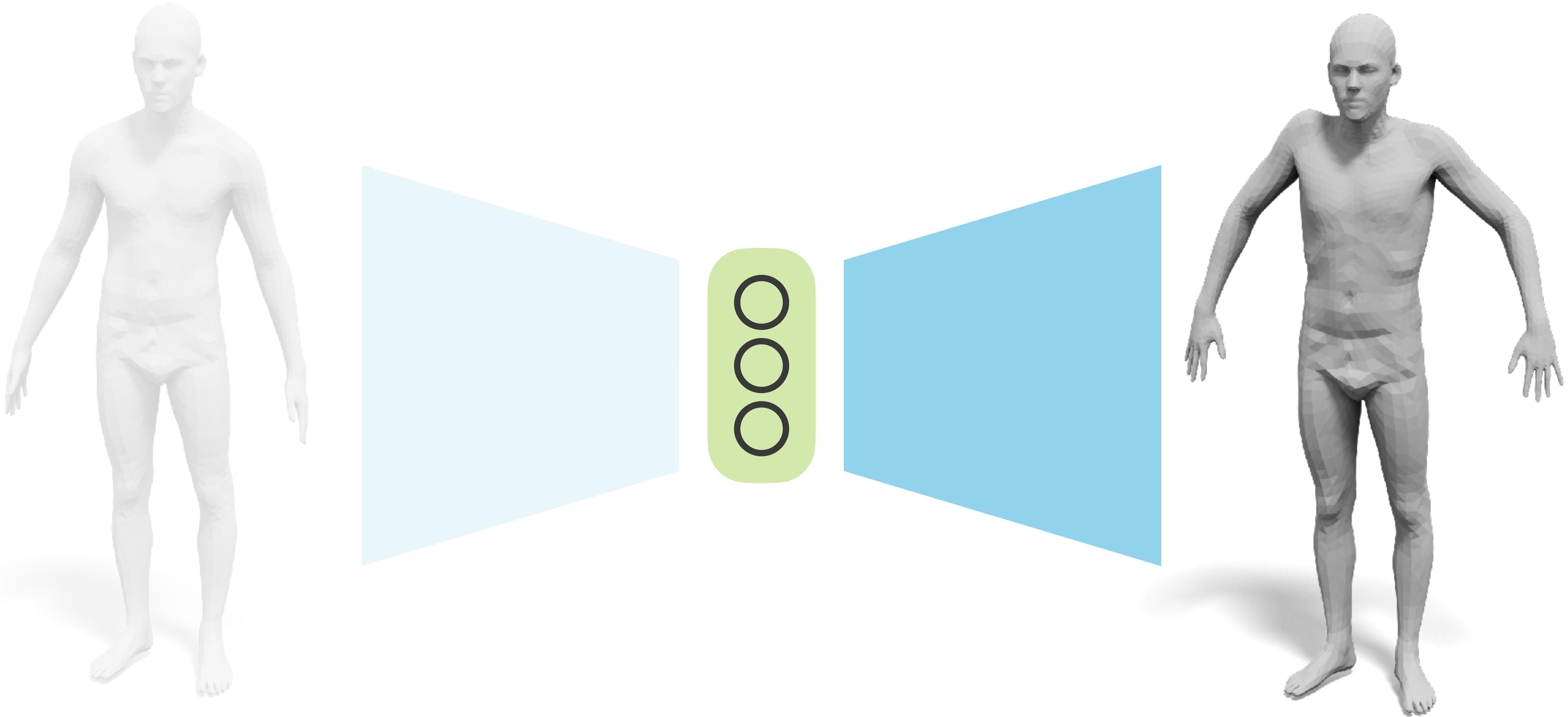
# Learning Shape Deformation



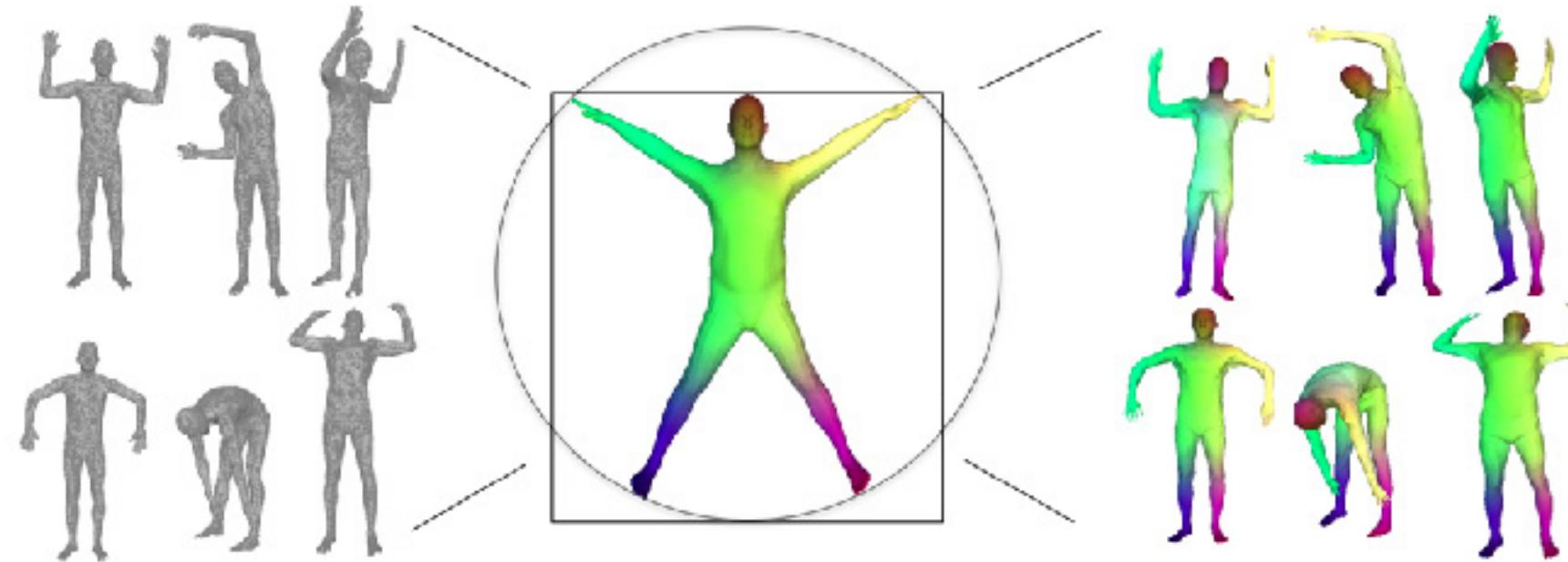
# Learning Shape Deformation



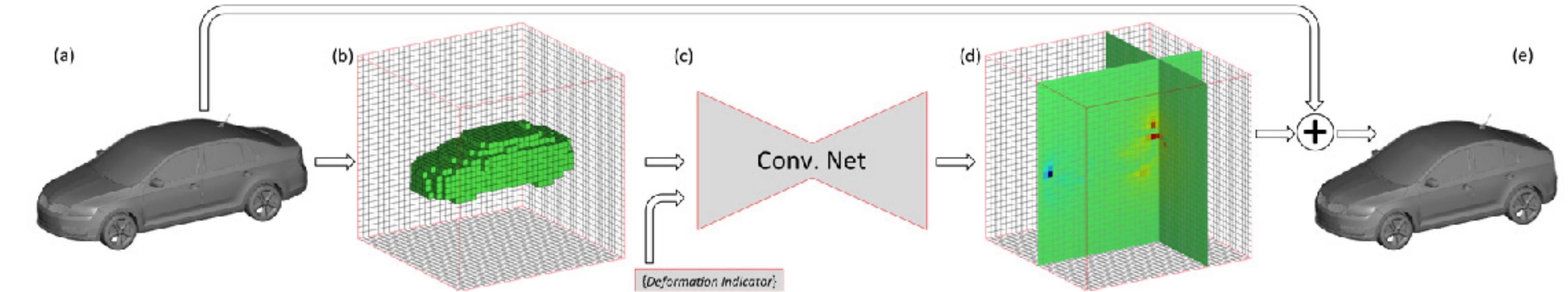
# Learning Shape Deformation



# Learning Shape Deformation



Groueix et al. 2018



Yumer & Mitra 2016

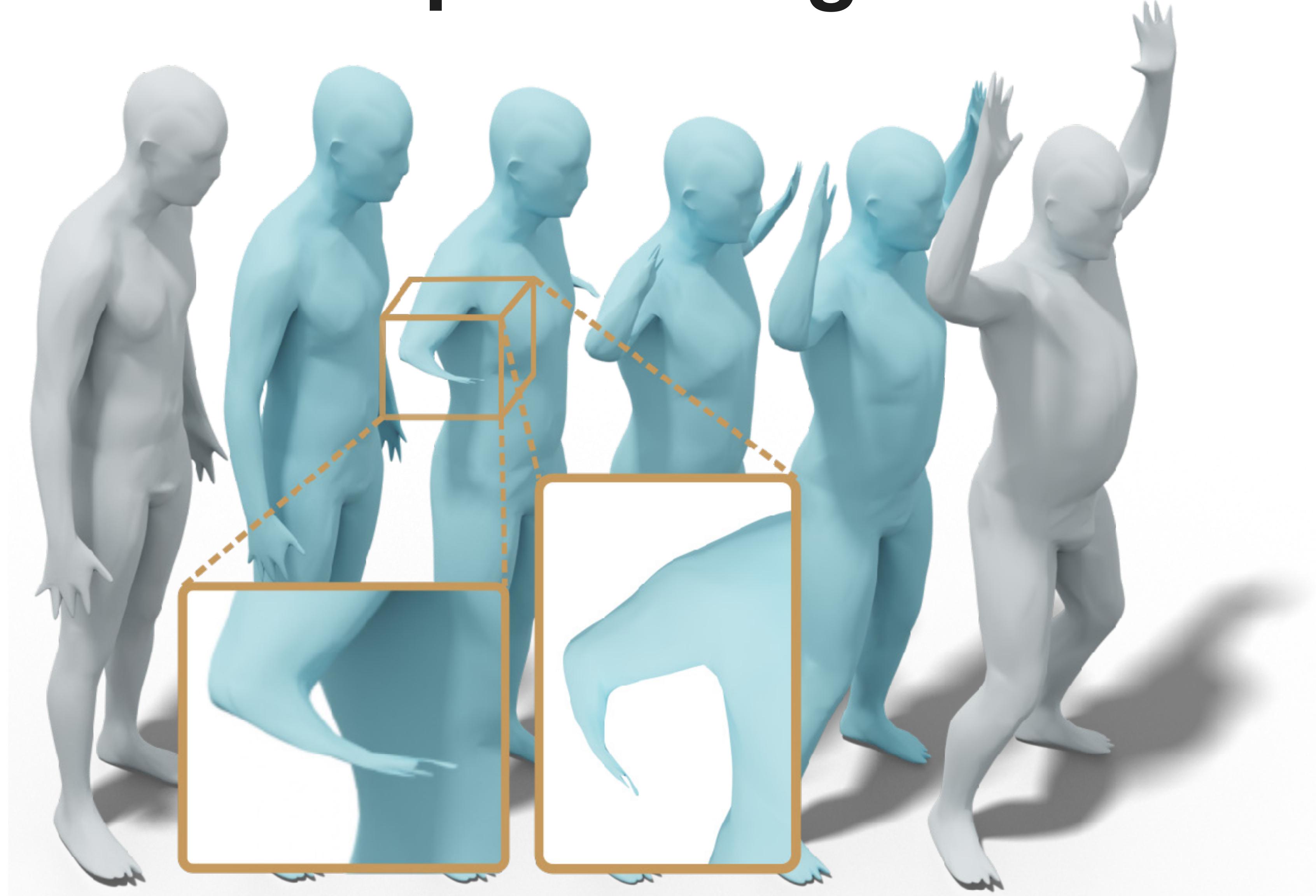


Gao et al. 2019



Rakotosaona & Ovsjanikov, 2020

# Issues of preserving details



# Linear Blend Skinning

$$v'_i = \sum_{j=1}^m w_{i,j} T_j v_i$$

new vertex locations

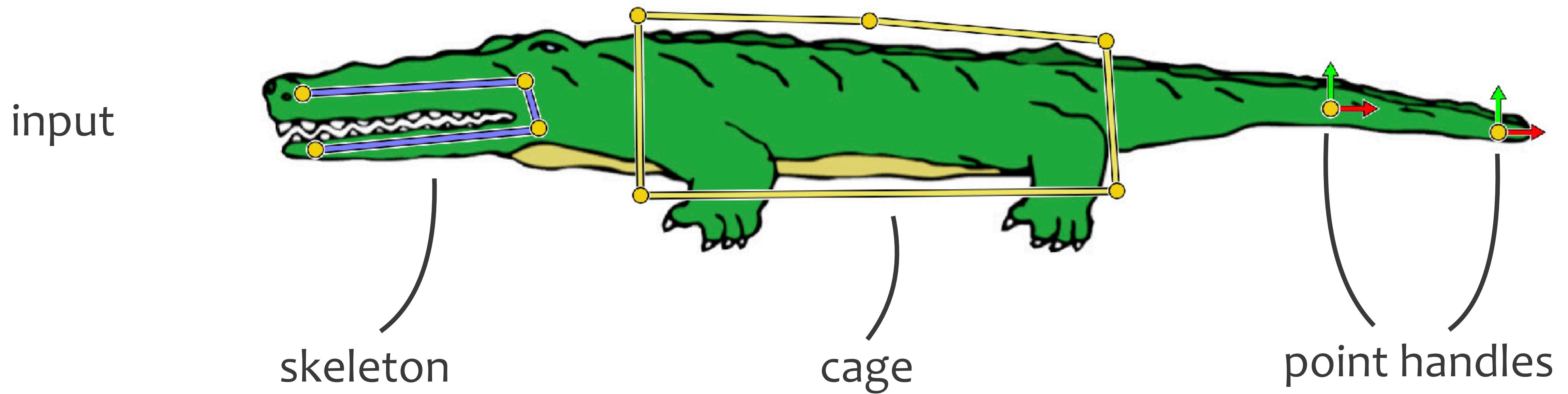
input vertex locations

weight

transformation of e.g., handles

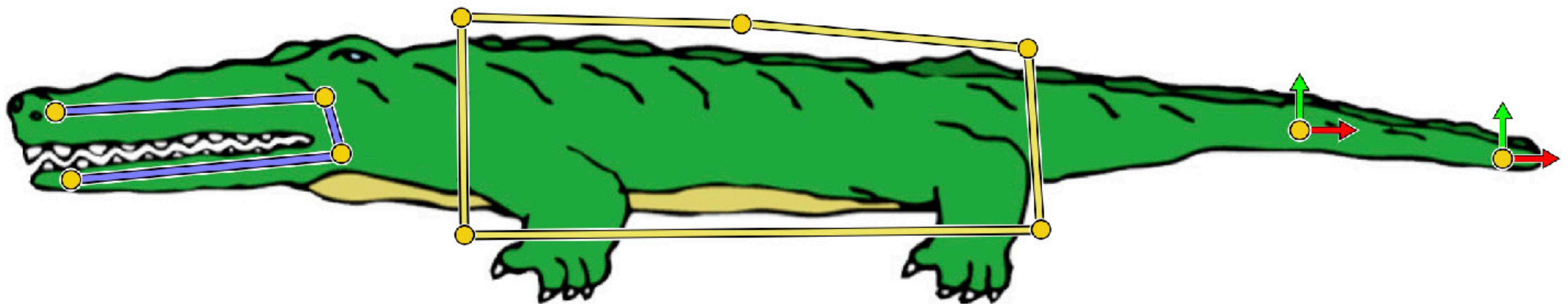
The diagram illustrates the formula for Linear Blend Skinning. It shows the calculation of a new vertex location  $v'_i$  as a weighted sum of input vertex locations  $v_i$ , each transformed by a specific transformation  $T_j$ . The weight  $w_{i,j}$  is indicated by a curved arrow pointing from the term  $w_{i,j} T_j v_i$  to the label 'weight'. The input vertex locations  $v_i$  are indicated by a curved arrow pointing from the term  $v_i$  to the label 'input vertex locations'. The new vertex locations  $v'_i$  are indicated by a curved arrow pointing from the result  $v'_i$  to the label 'new vertex locations'. The transformations  $T_j$  are indicated by a curved arrow pointing from the term  $T_j$  to the label 'transformation of e.g., handles'.

# Linear Blend Skinning

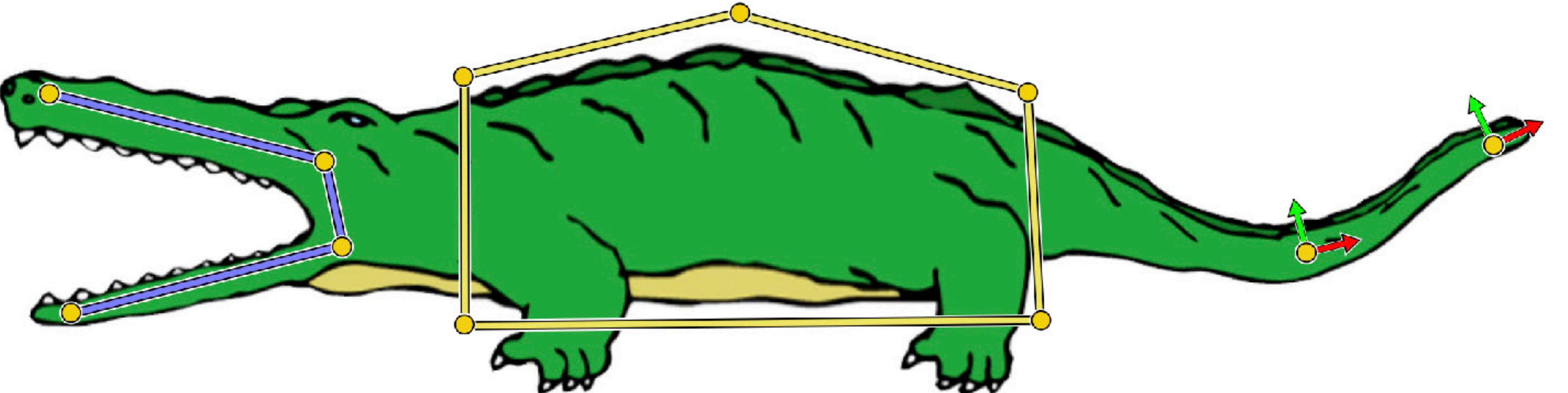


# Linear Blend Skinning

input

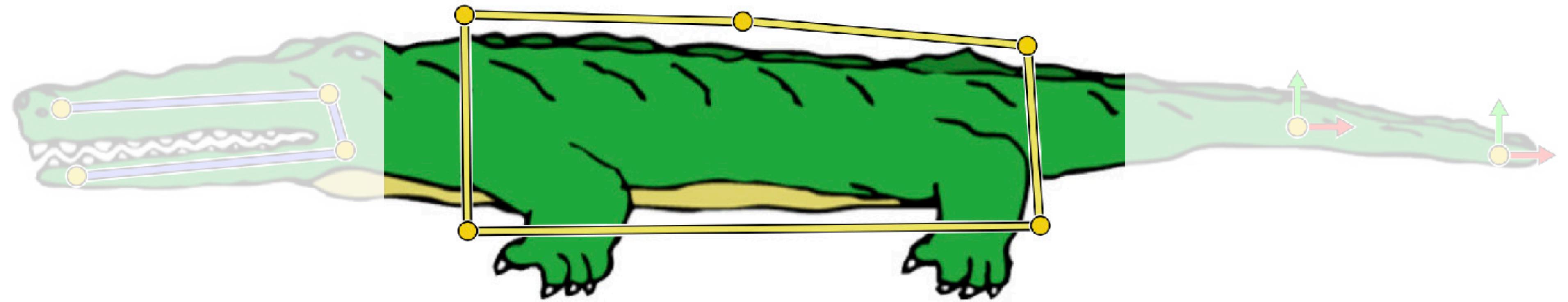


deformed

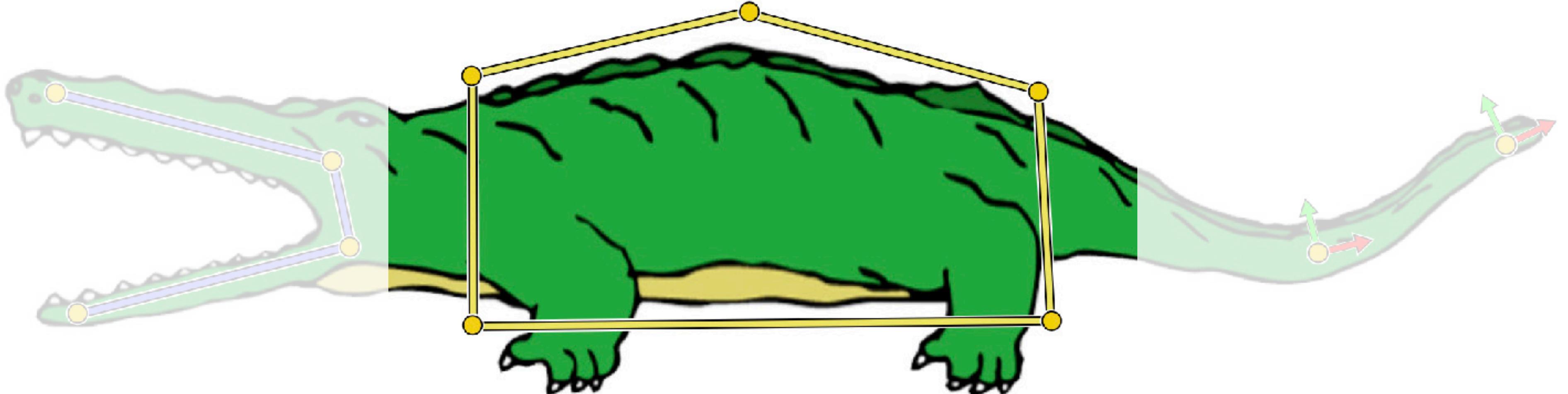


# Linear Blend Skinning

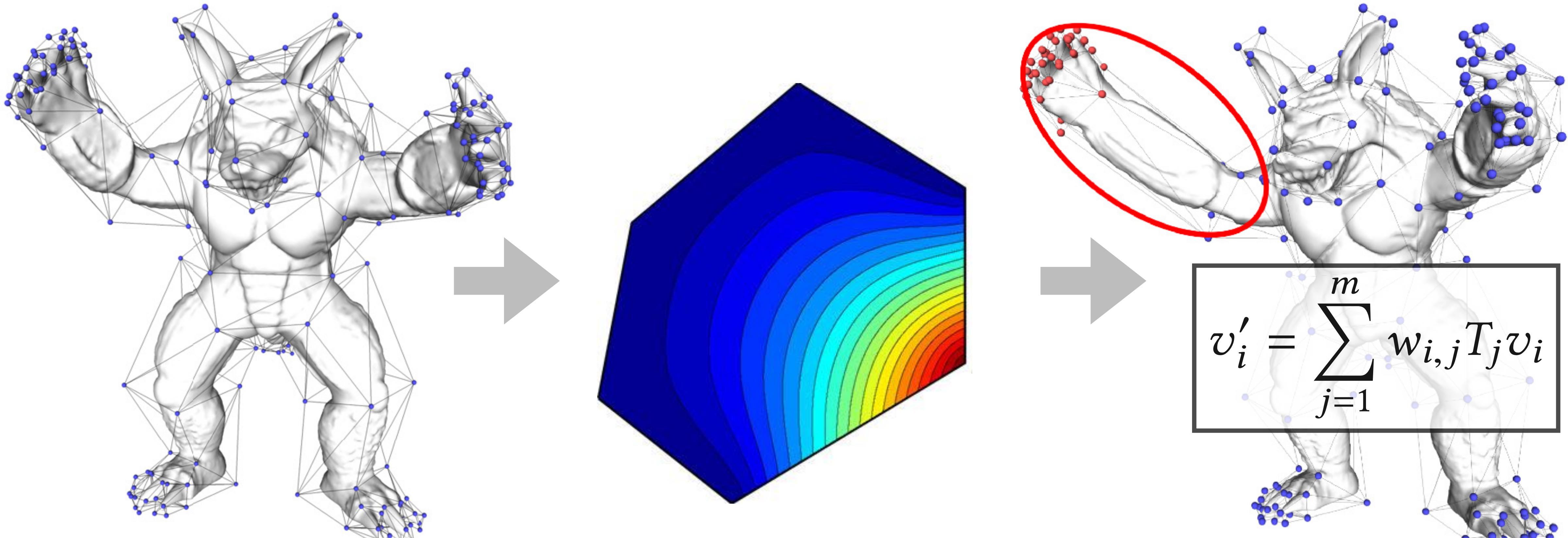
input



deformed



# Cage-Based Deformation



construct a cage

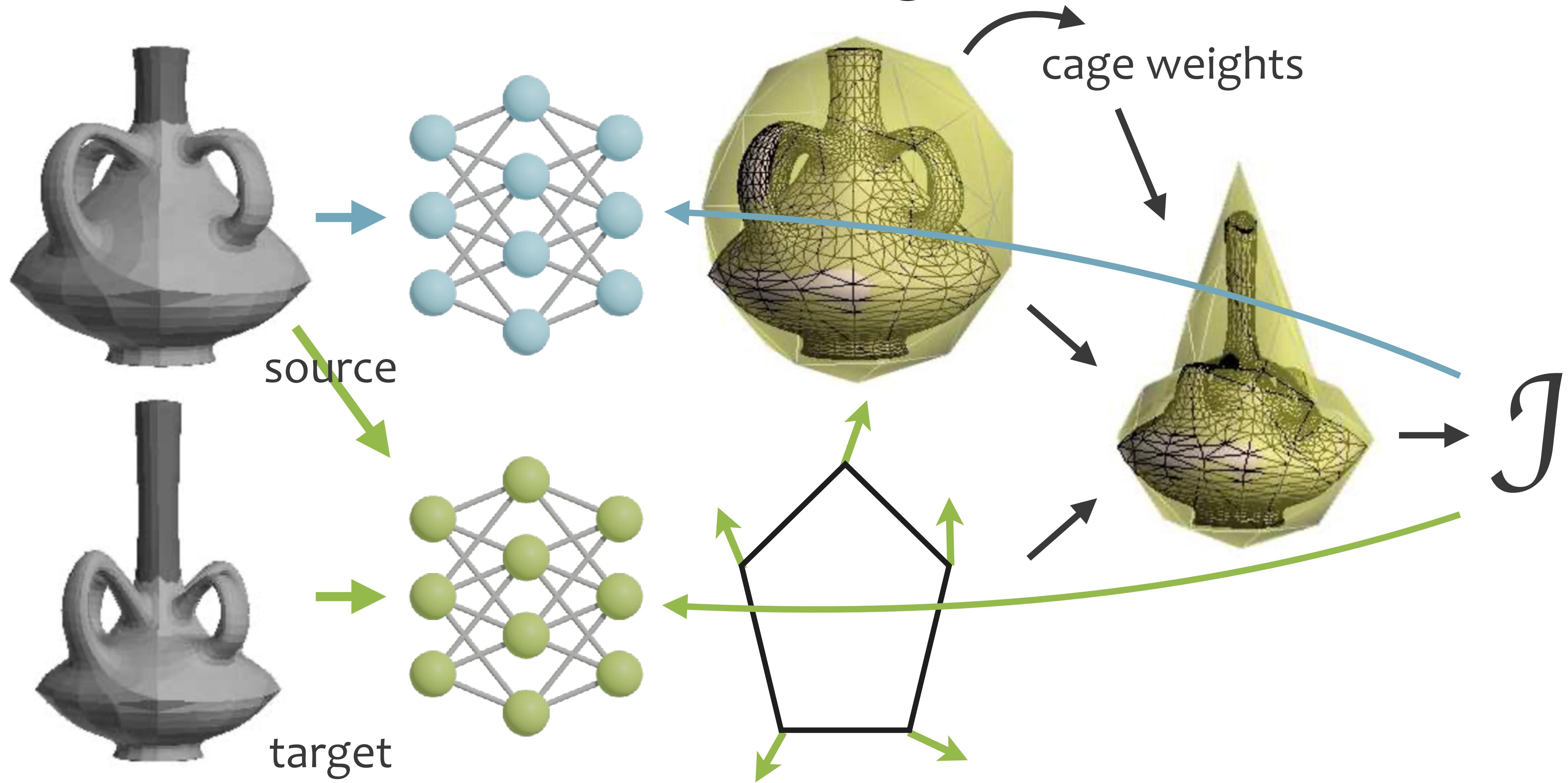
compute cage weights

deform the model

# Neural Cages



# Neural Cages



# Loss Function

$$\mathcal{J} = w_1 \mathcal{L}_{\text{MVC}} + w_2 \mathcal{L}_{\text{align}} + w_3 \mathcal{L}_{\text{shape}}$$

“nice” cage  
(e.g., not self-overlap)

positive cage weights

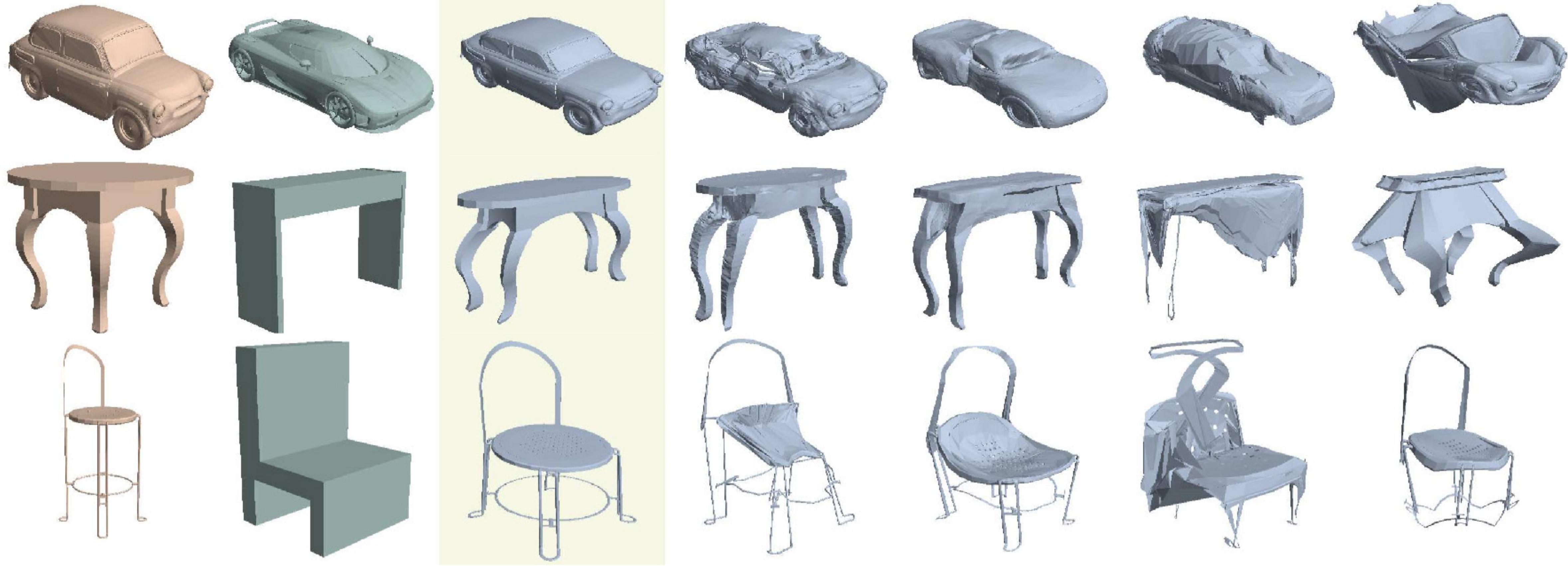
align with target

Chamfer

preserve input shapes

e.g., preserve normals

# Detail-Preserving Deformation



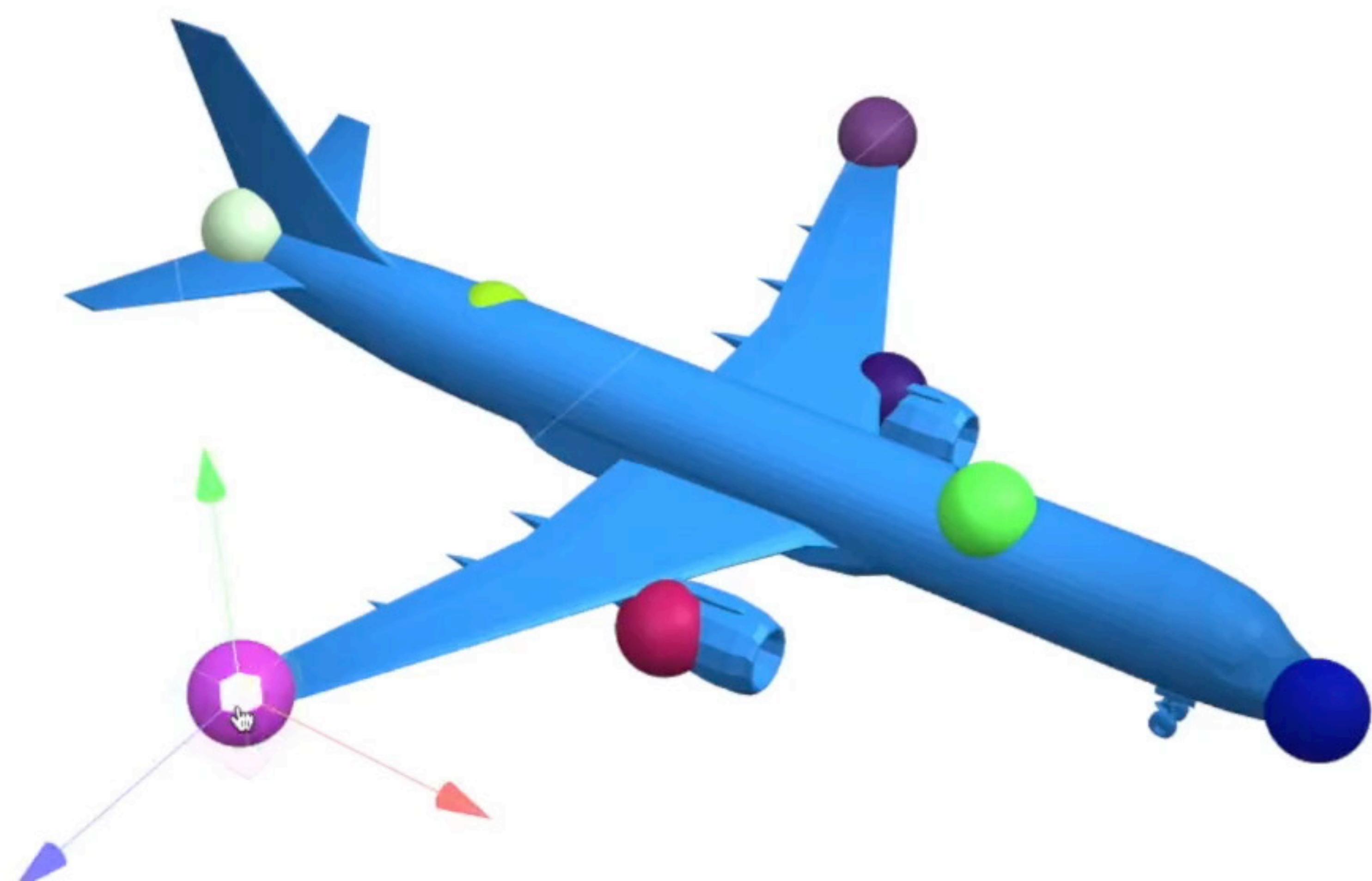
input

target

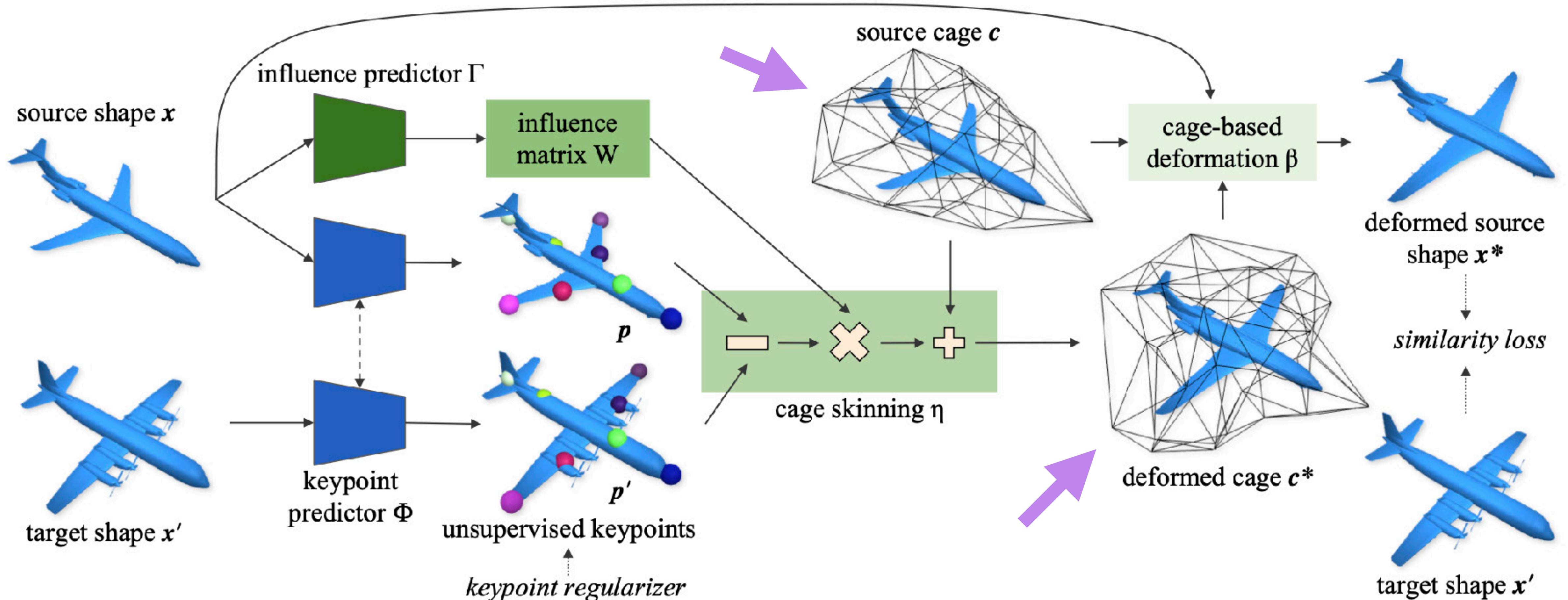
output

previous methods

# Keypoint Deformer



# Keypoint Deformer



# Key Takeaways

preserve details

not global shape aware

manual efforts

Classic

not preserve details

global shape aware

less manual efforts

lower quality

Deep

preserve details

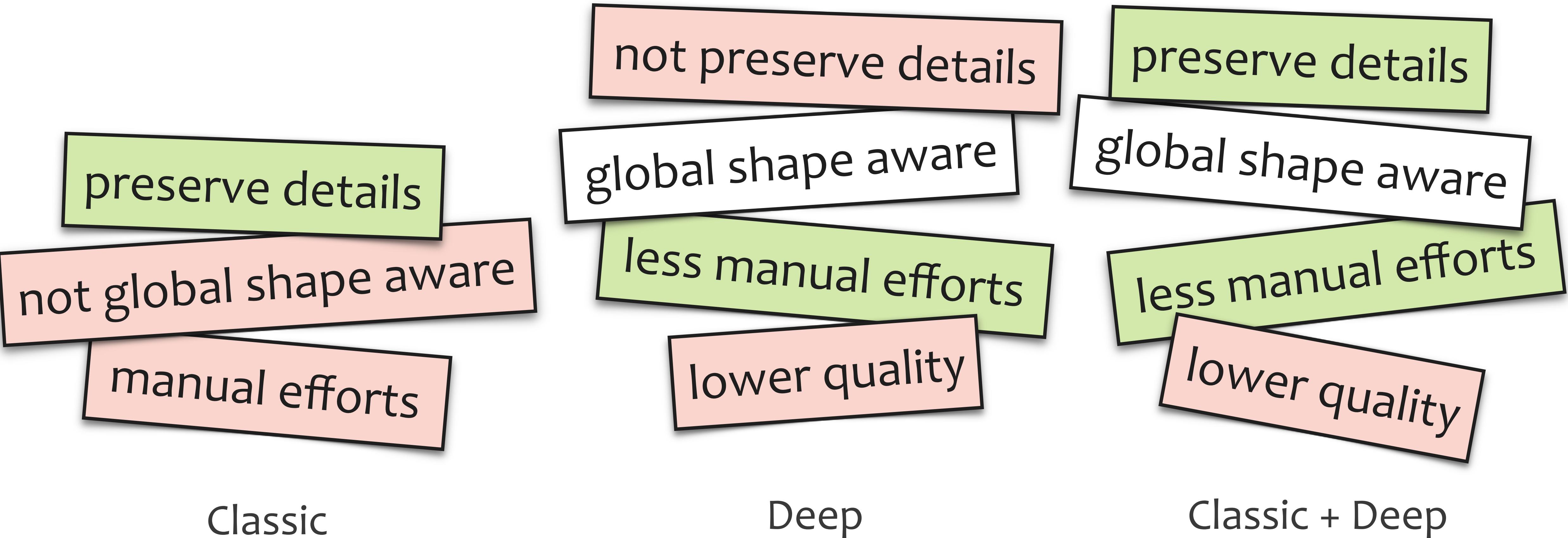
global shape aware

less manual efforts

lower quality

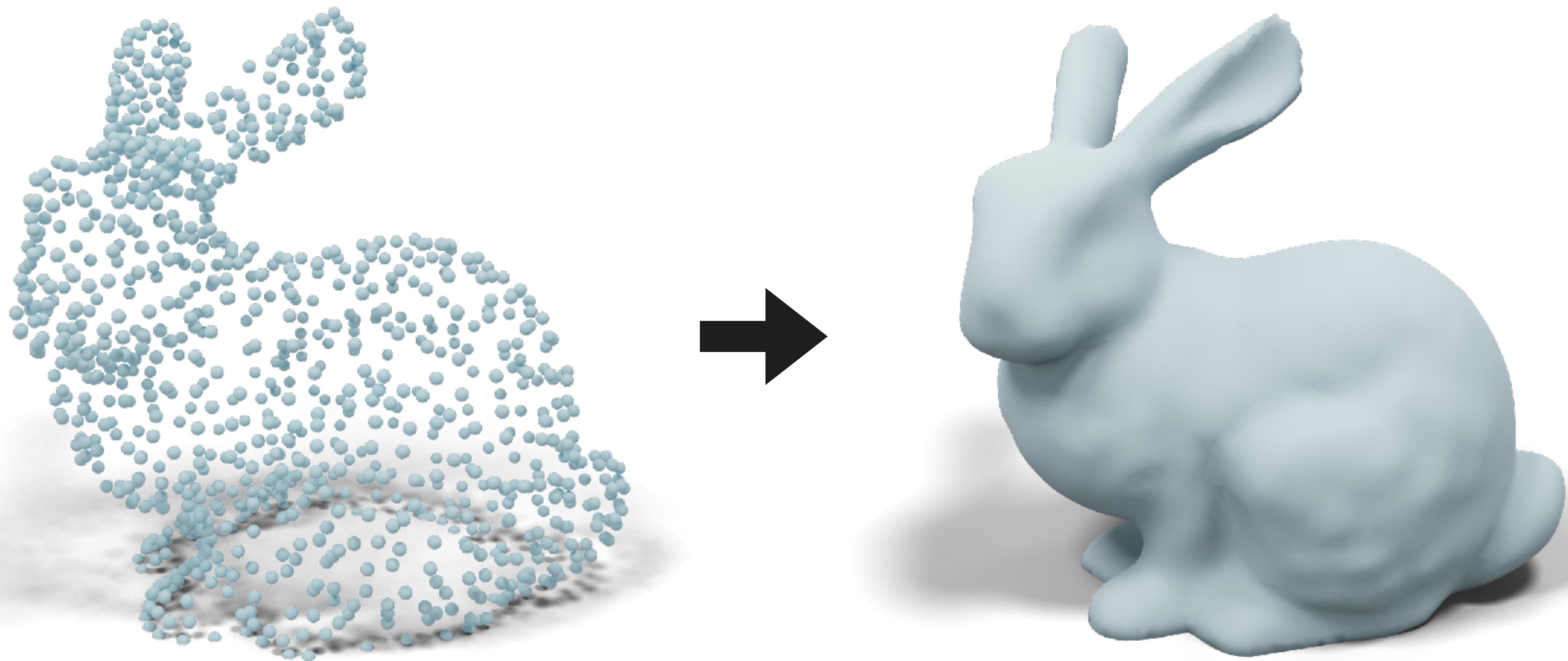
Classic + Deep

# Key Takeaways

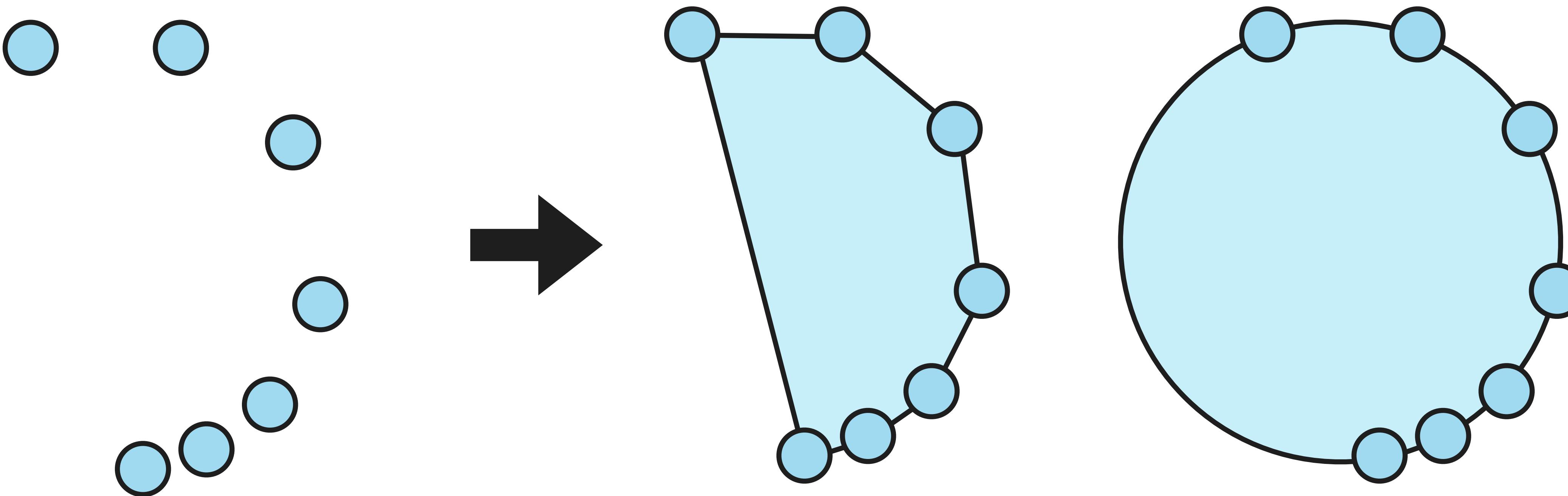


Machine learning as geometric prior

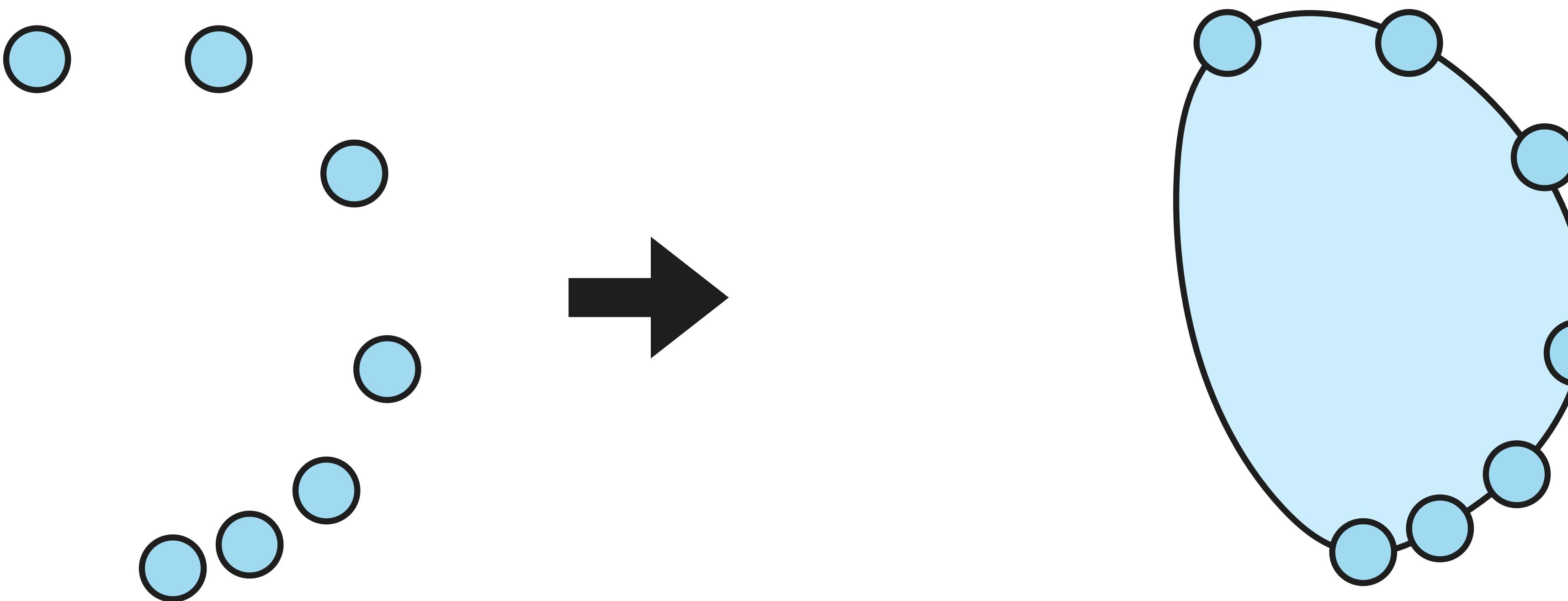
# Surface Reconstruction



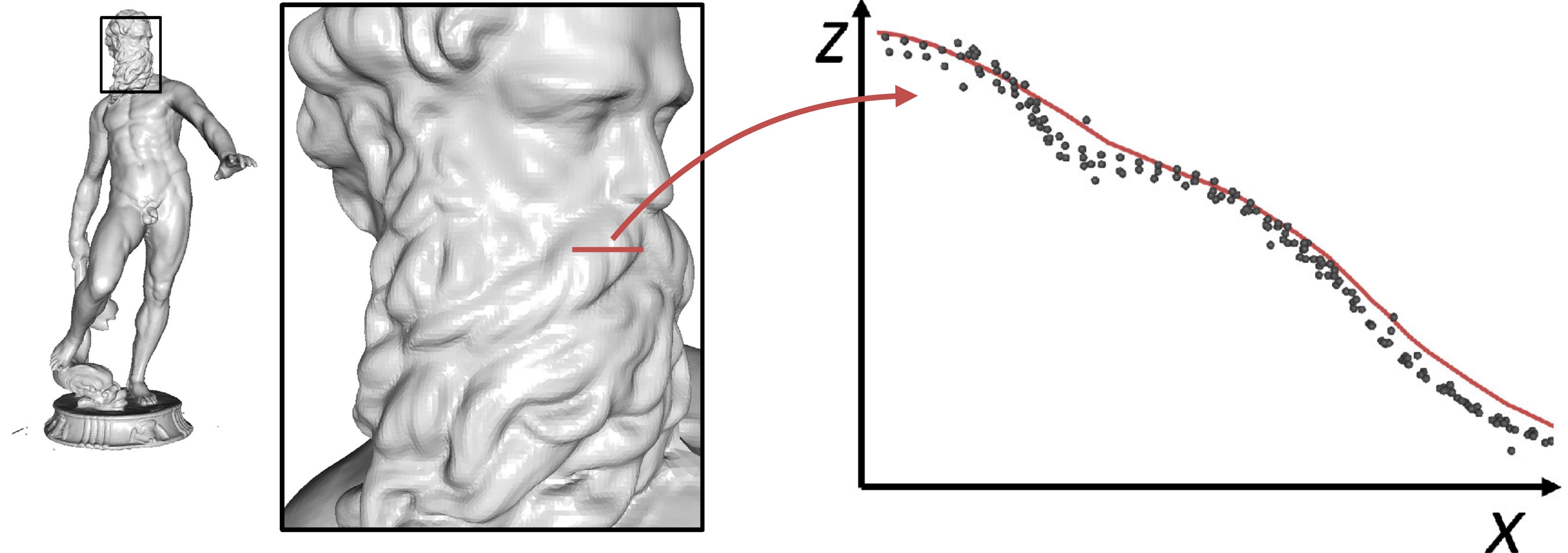
# An ill-posed problem



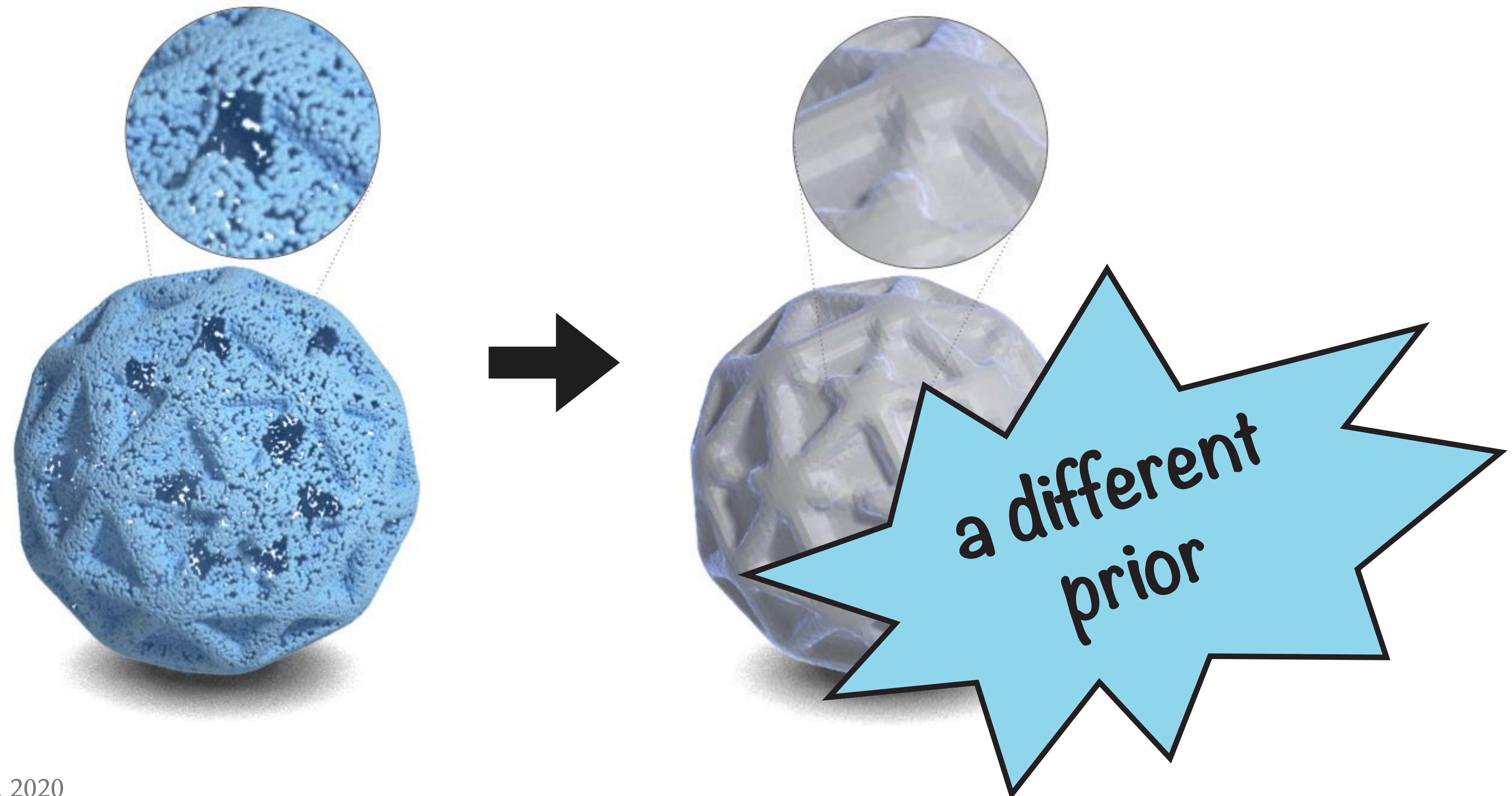
# A Smooth Solution



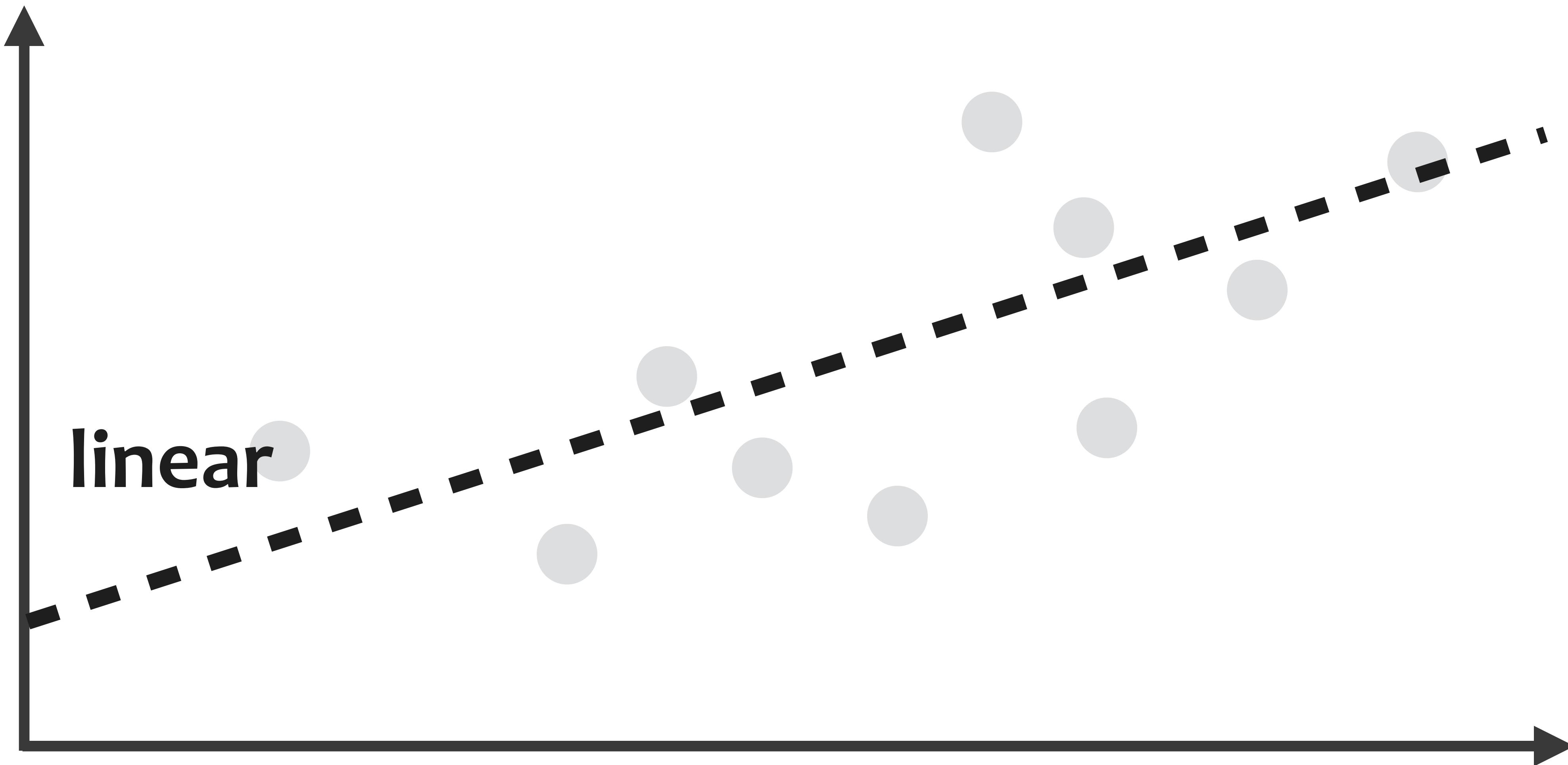
# Classic Smoothness Prior



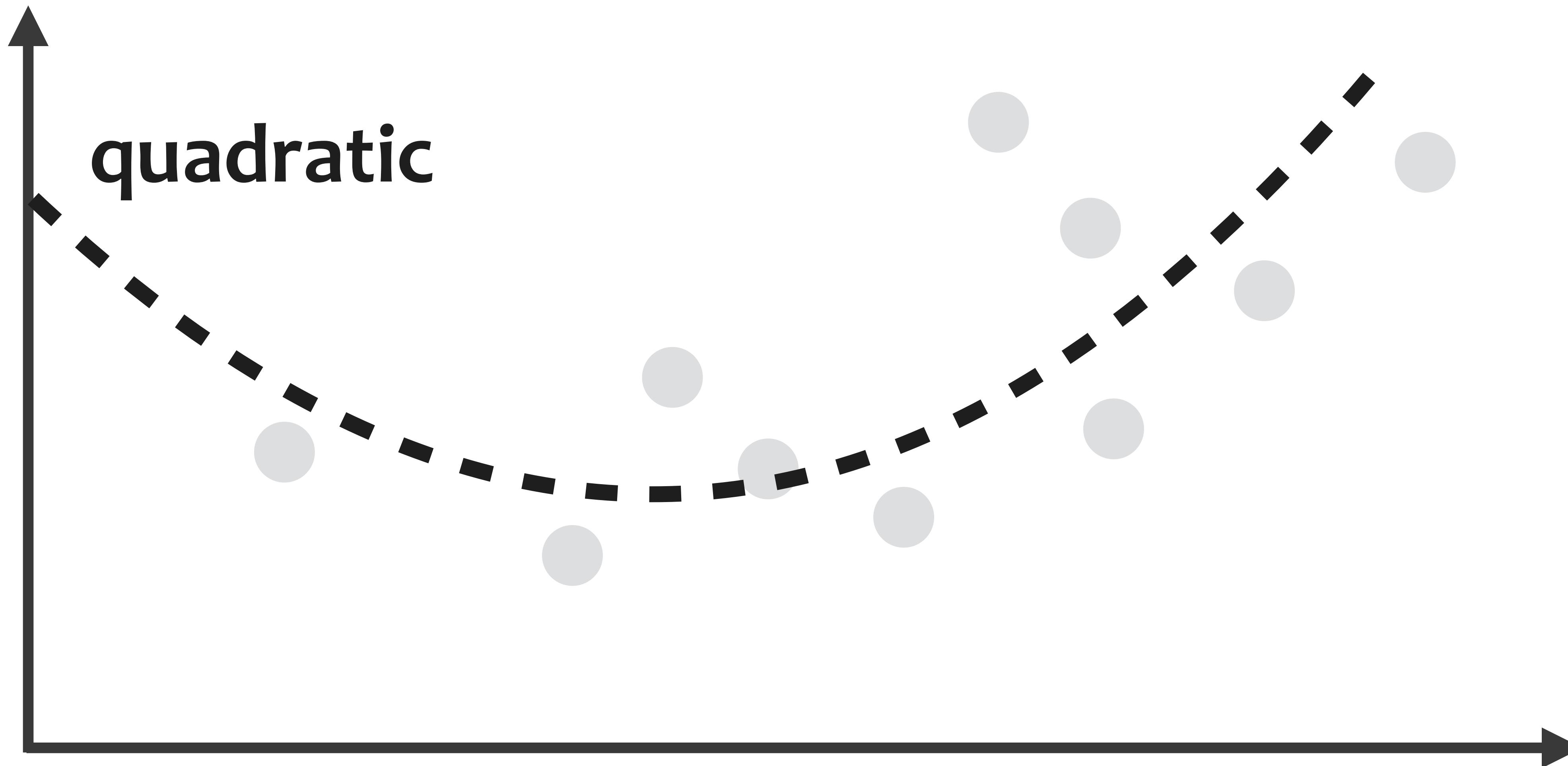
# Smoothness is not always good



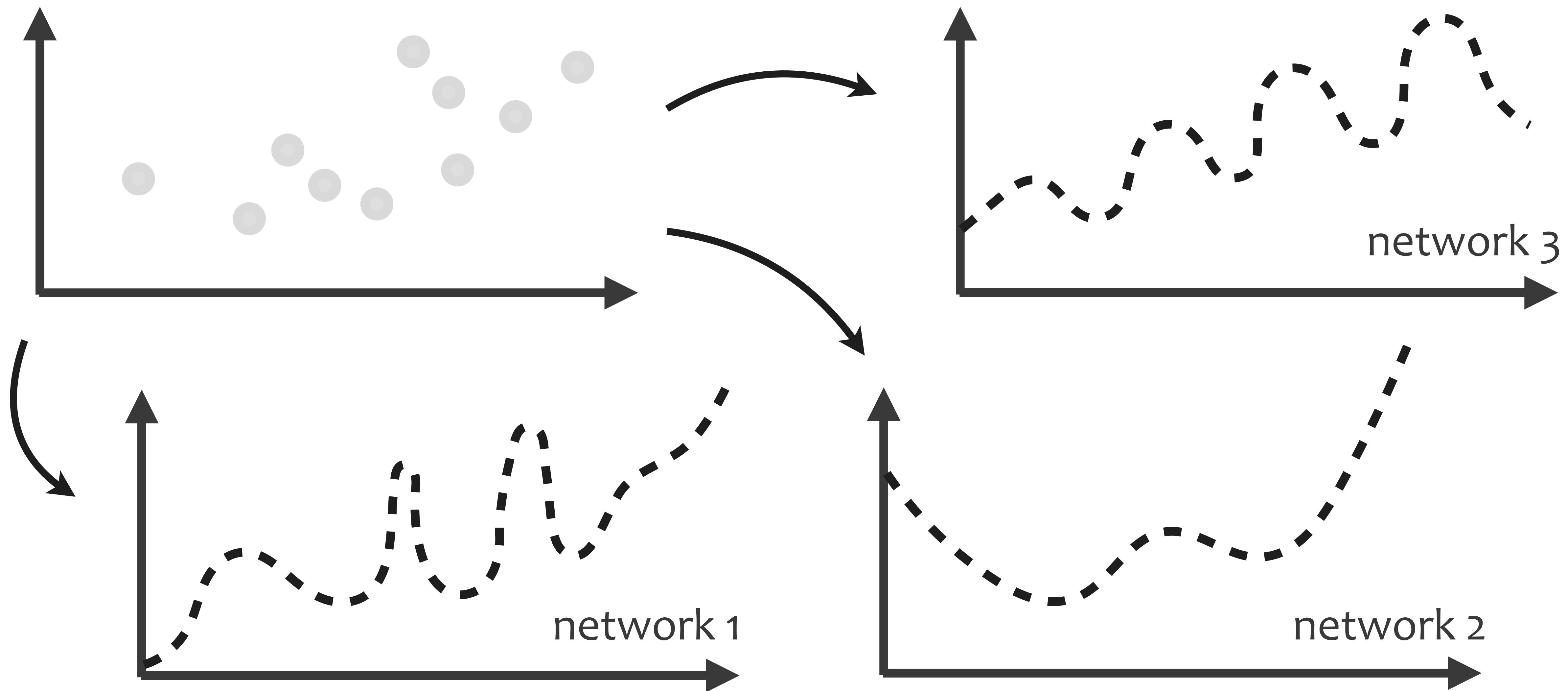
# Inductive Bias as Prior



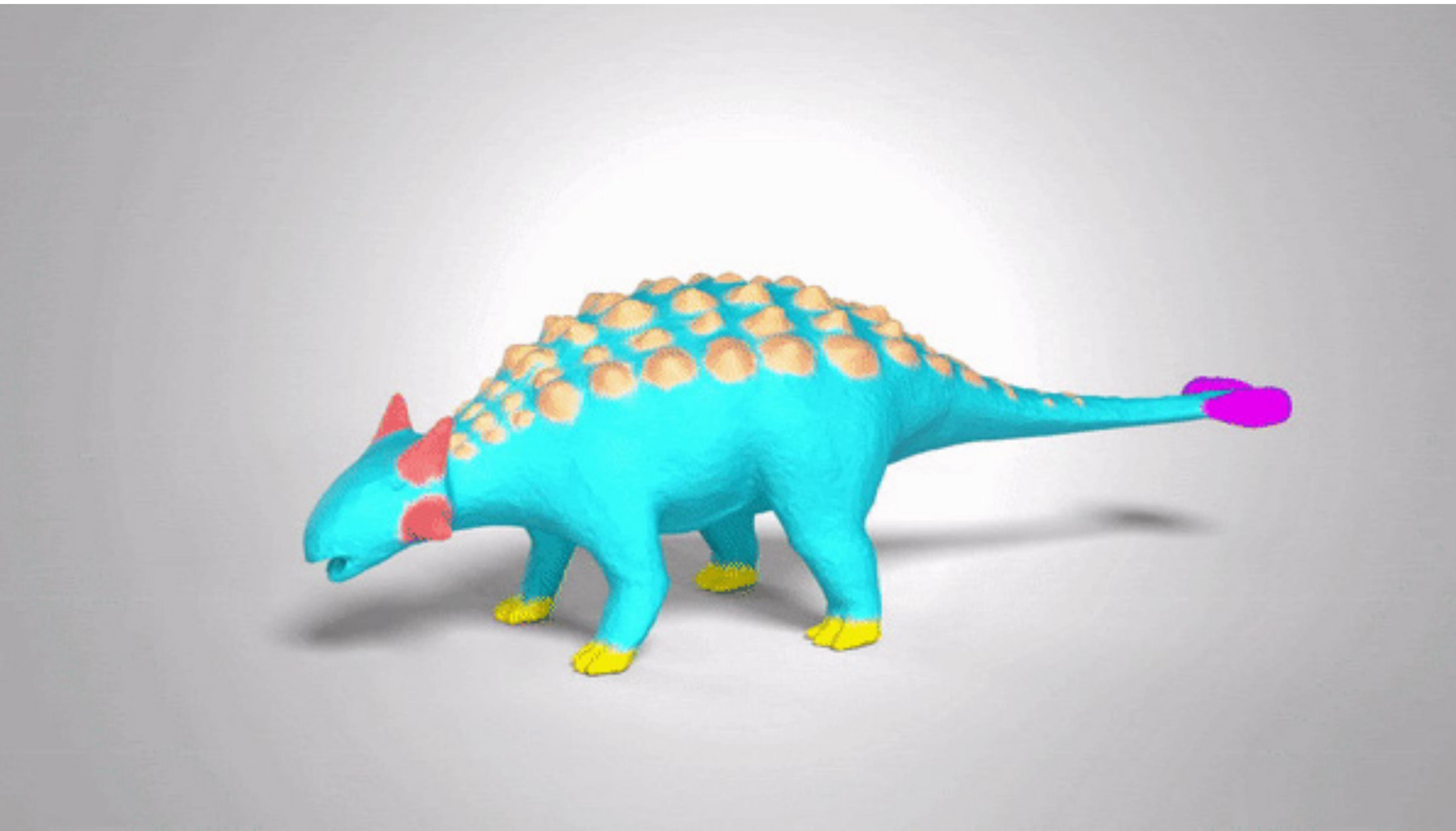
# Inductive Bias as Prior



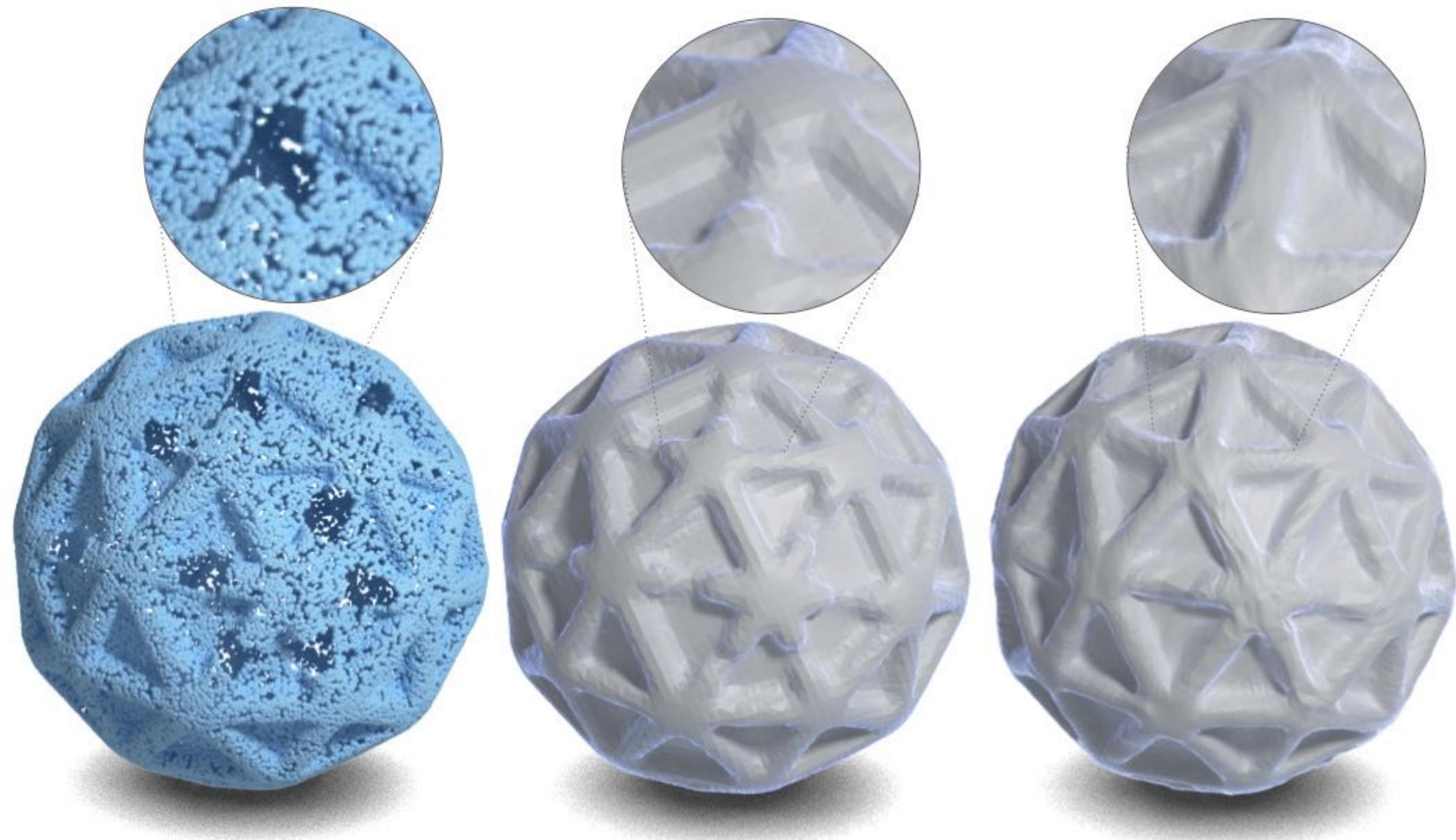
# Deep Network Biases



# New Possibilities : Self-Prior



# Results of Self-Prior



input

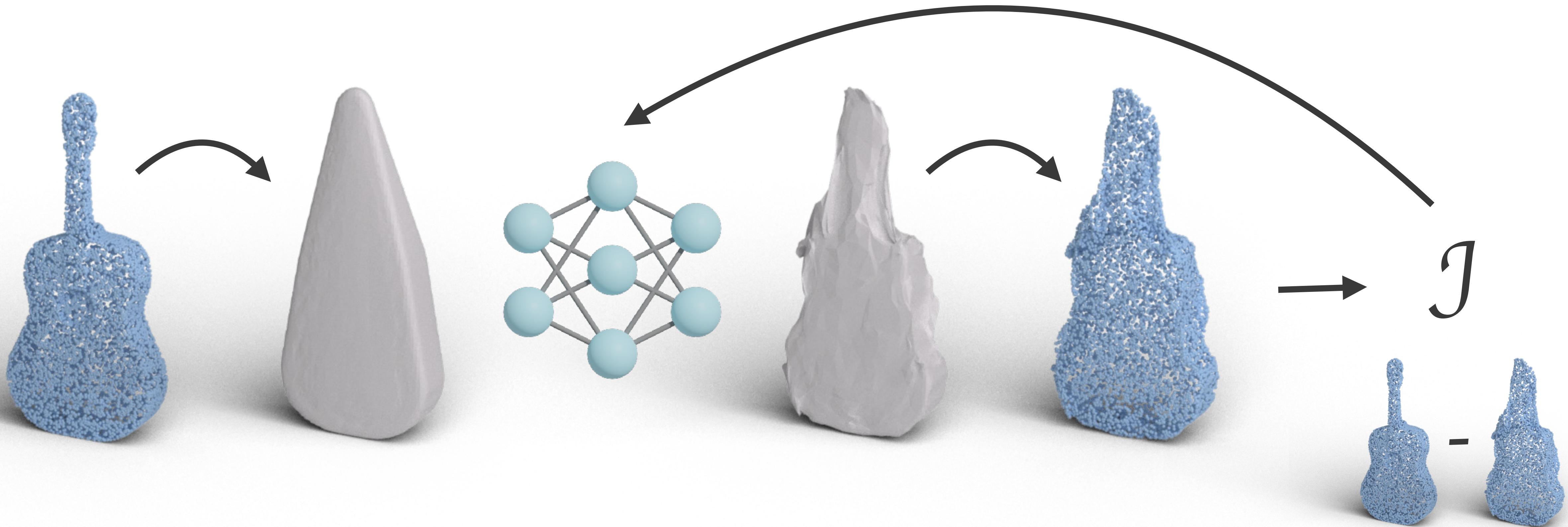
Smoothness

[Kazhdan et al. 2006]

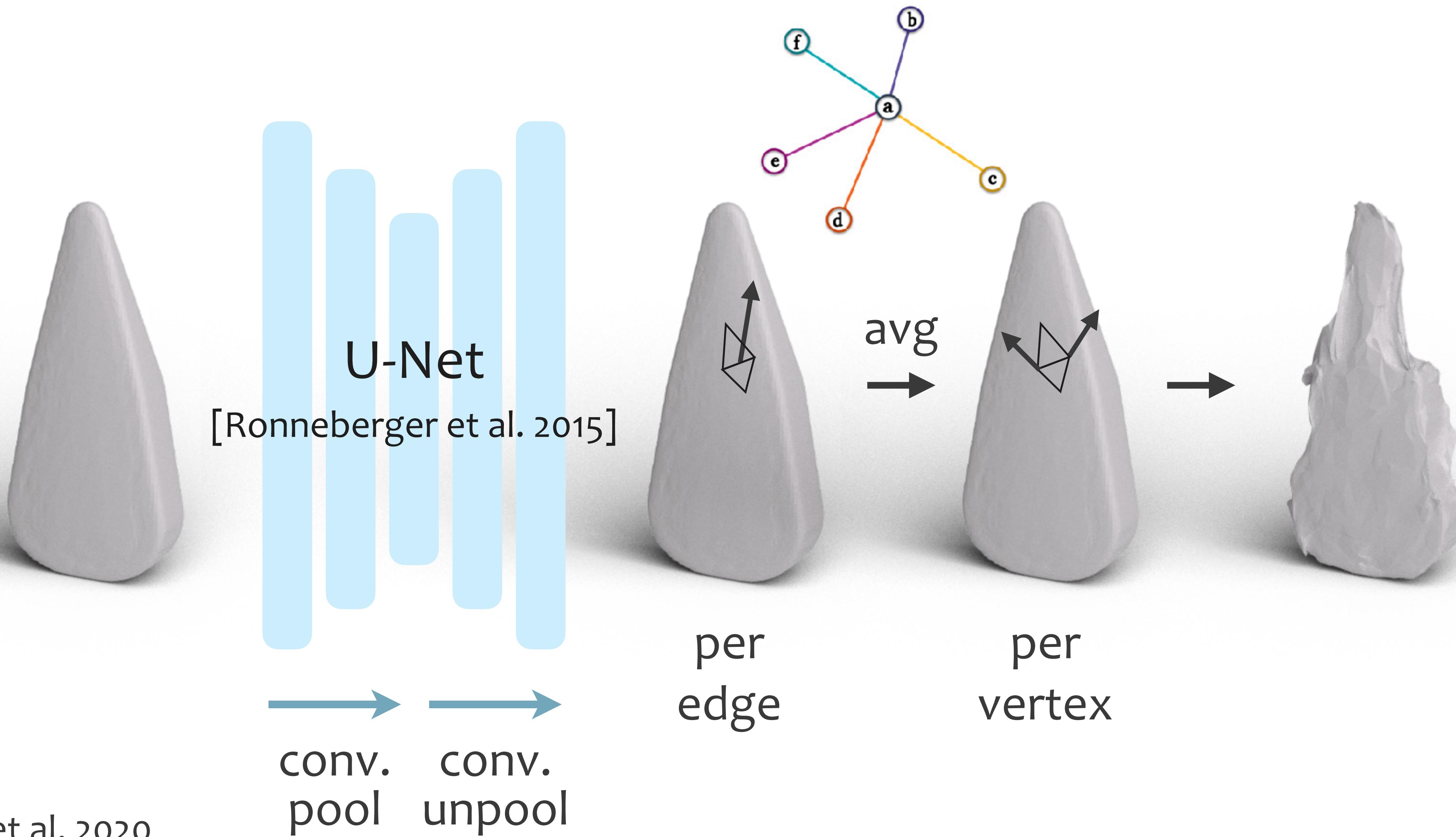
Self-prior

[Hanocka et al. 2020]

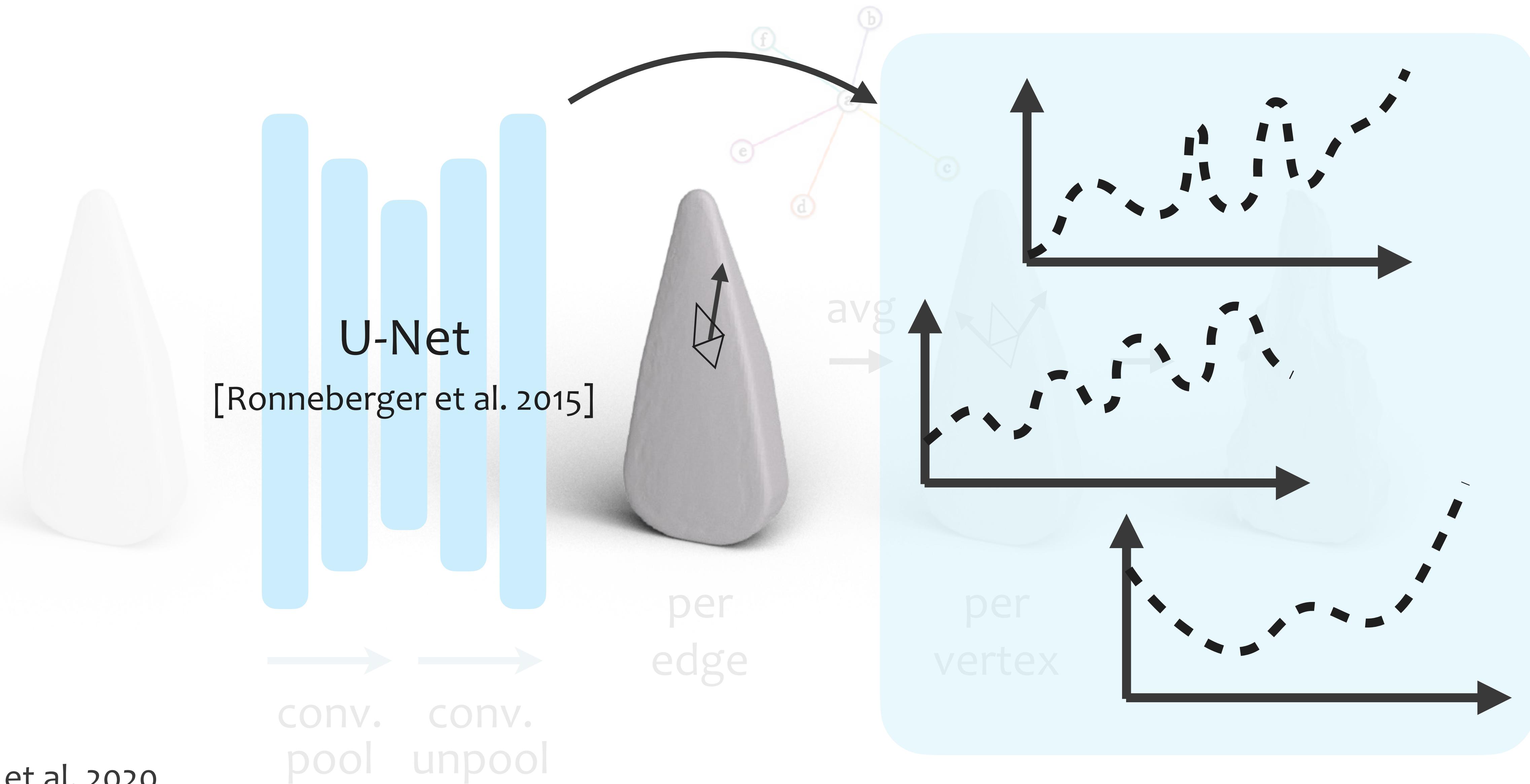
# Point2Mesh Overview



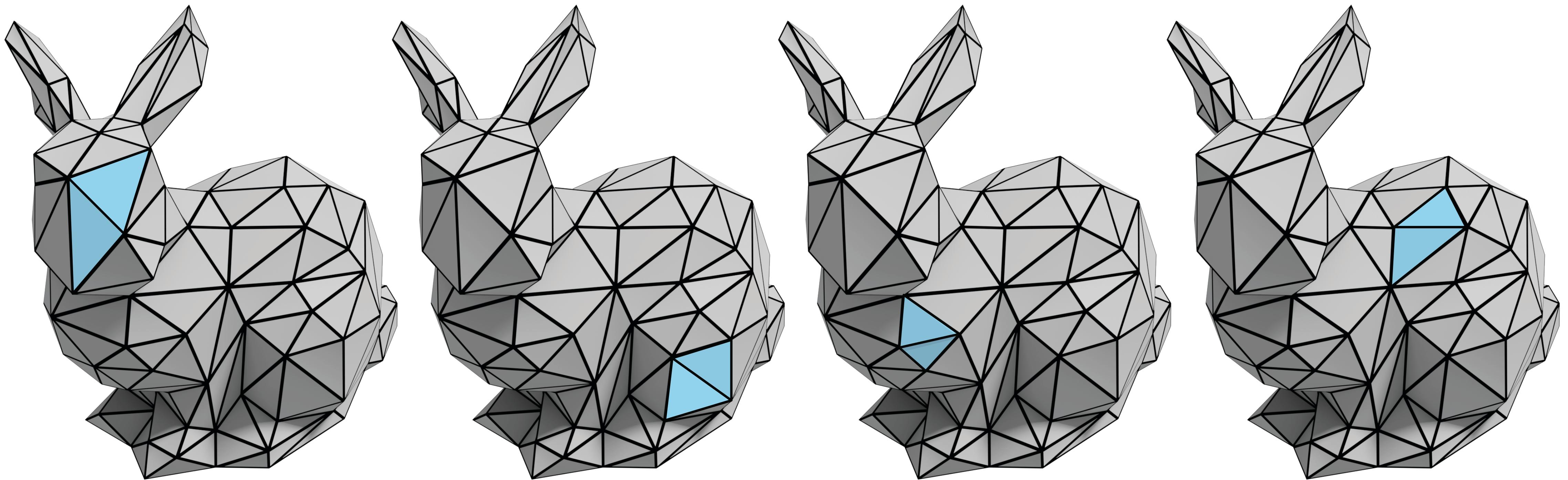
# Point2Mesh Overview



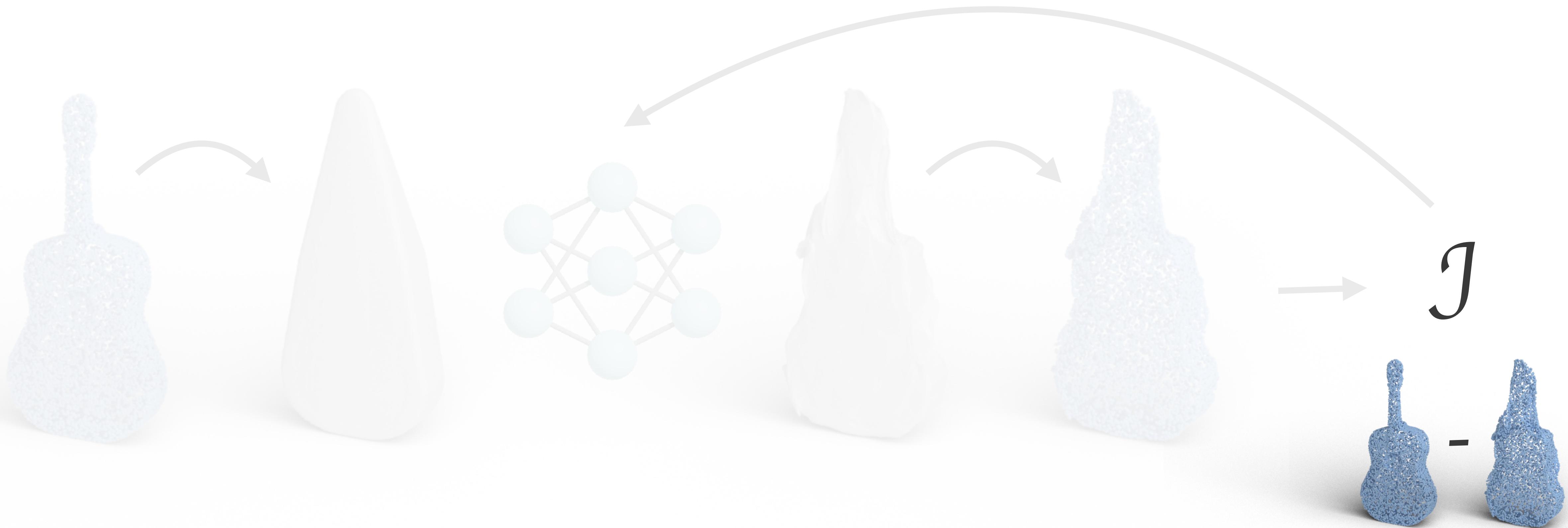
# Point2Mesh Overview



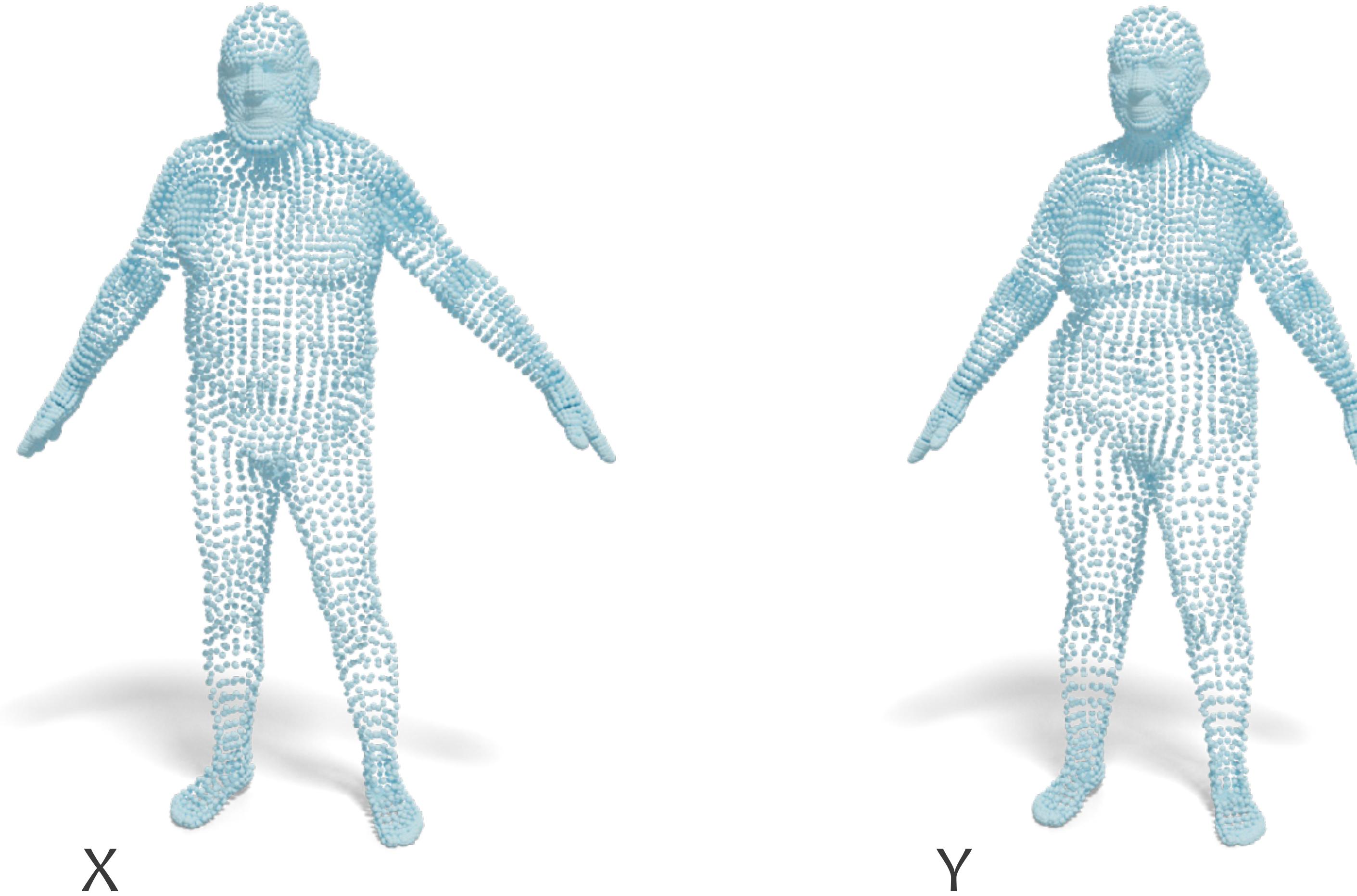
# CNN filters are shared



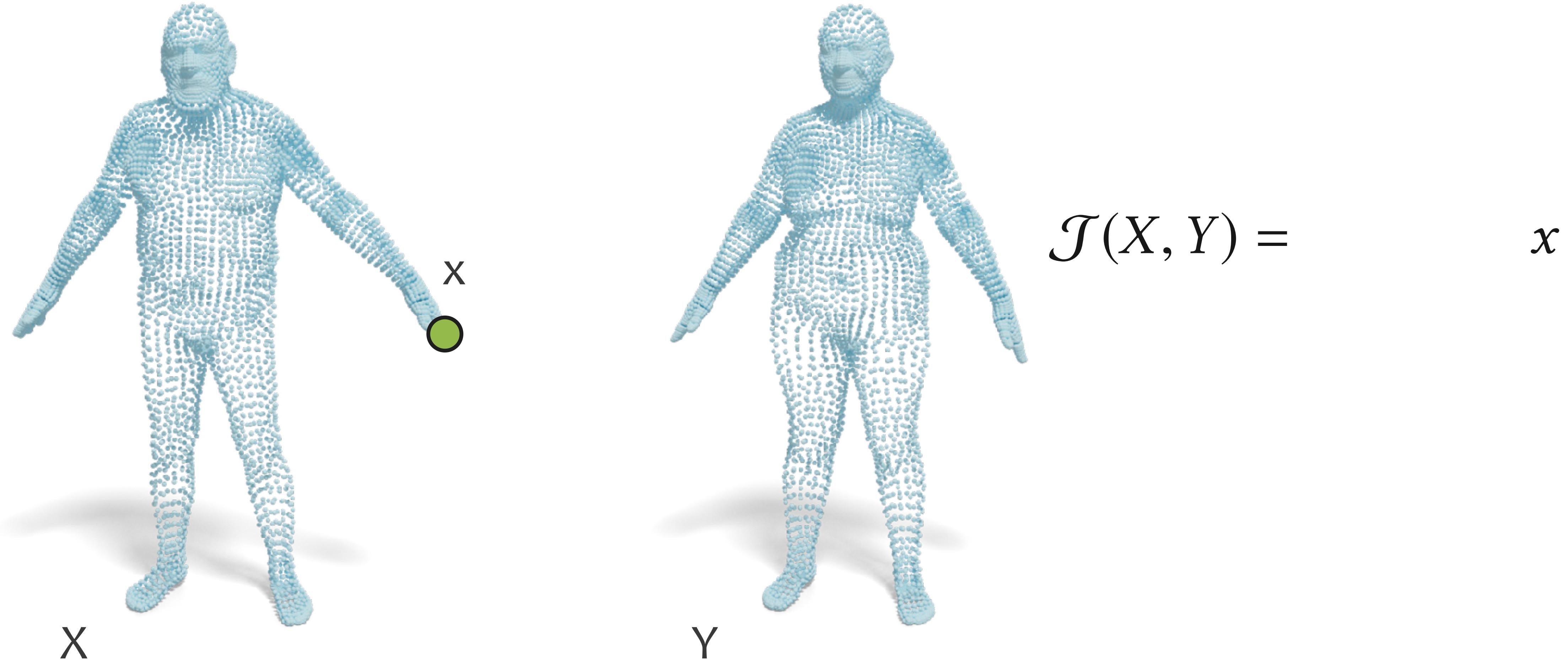
# Point2Mesh Overview



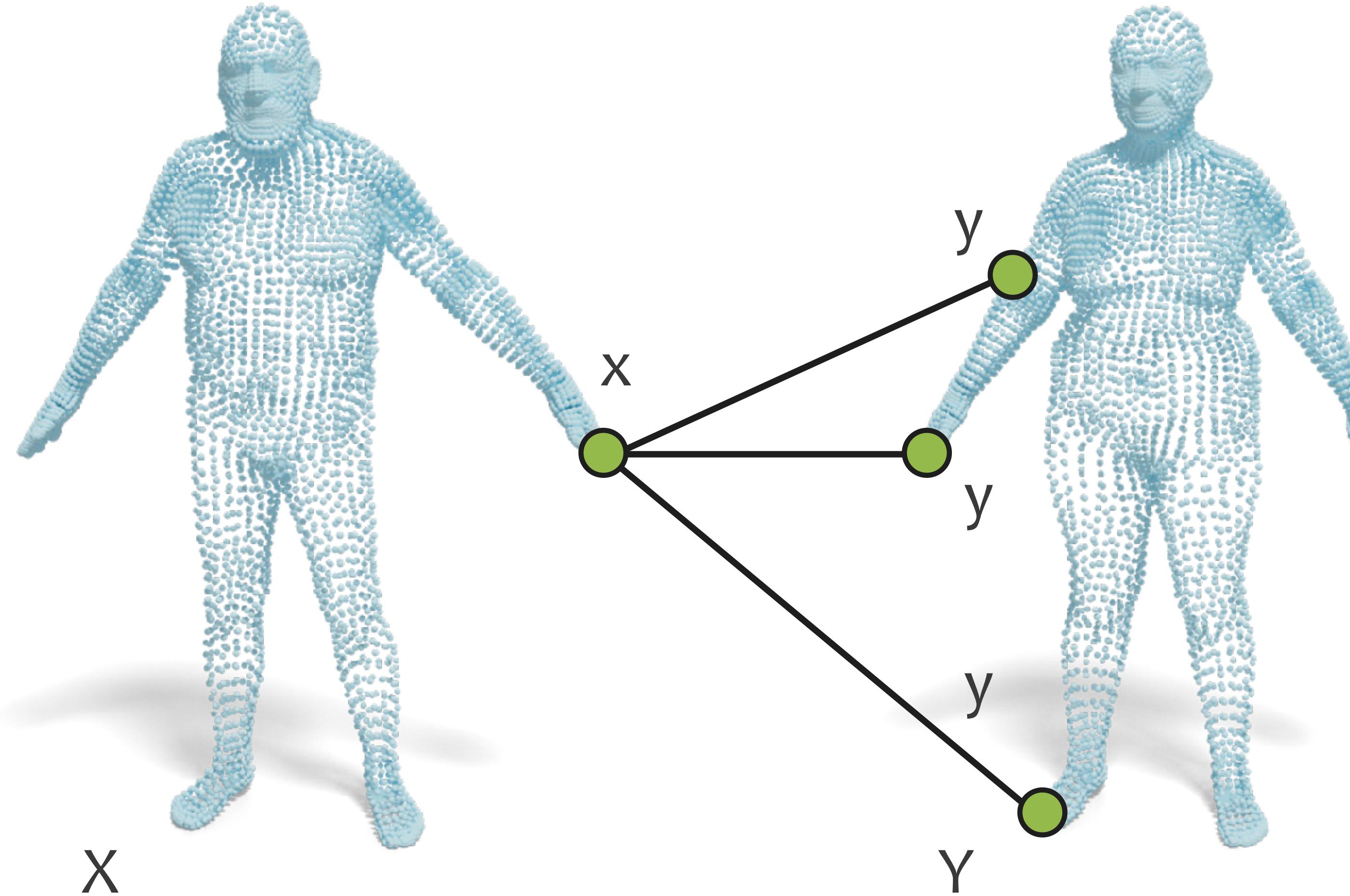
# Loss Function: Chamfer Distance



# Loss Function: Chamfer Distance



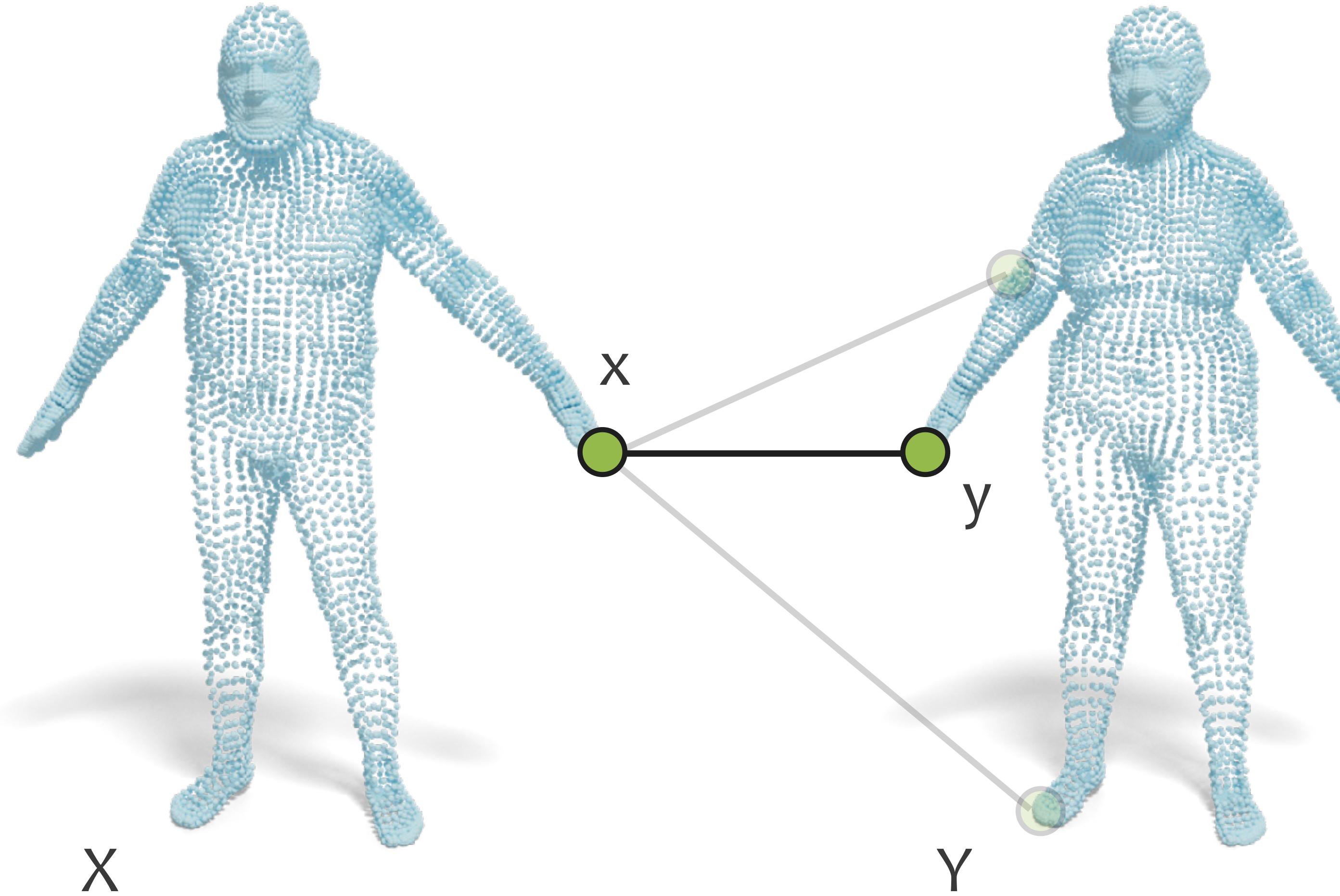
# Loss Function: Chamfer Distance



$$\mathcal{J}(X, Y) =$$

$$\|x - y\|^2$$

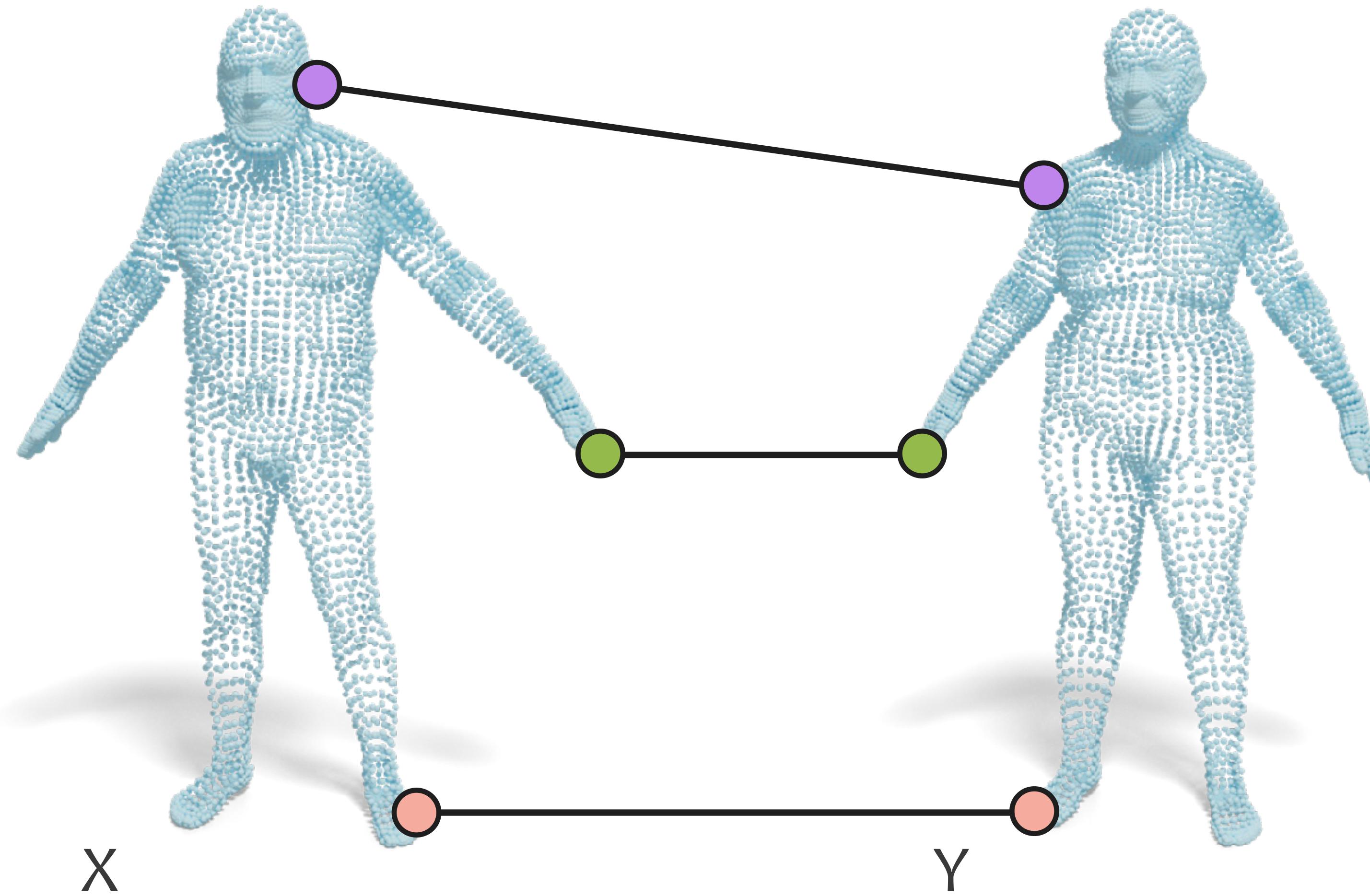
# Loss Function: Chamfer Distance



$$\mathcal{J}(X, Y) =$$

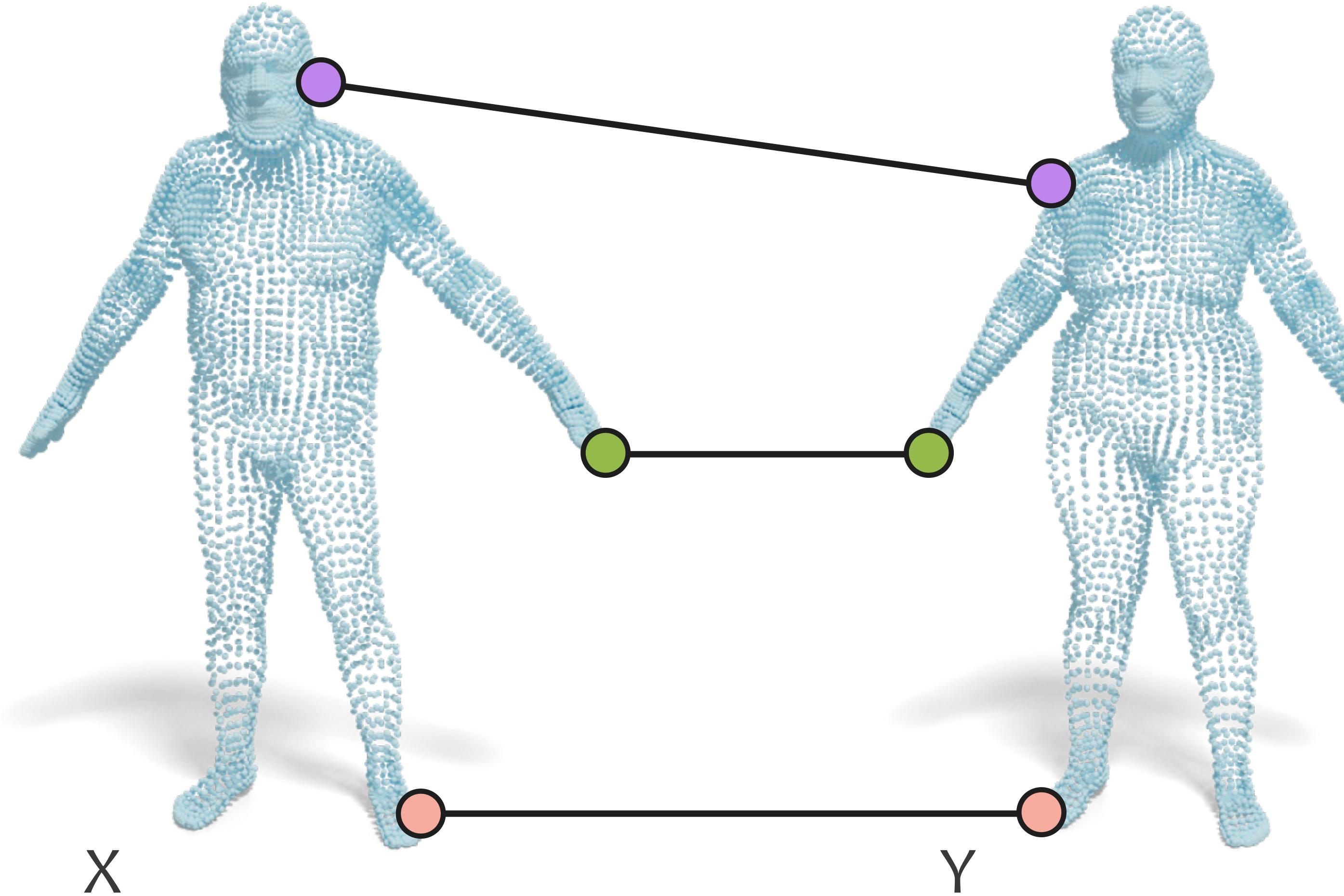
$$\min_{y \in Y} \|x - y\|^2$$

# Loss Function: Chamfer Distance



$$\mathcal{J}(X, Y) = \sum_{x \in X} \min_{y \in Y} \|x - y\|^2$$

# Loss Function: Chamfer Distance



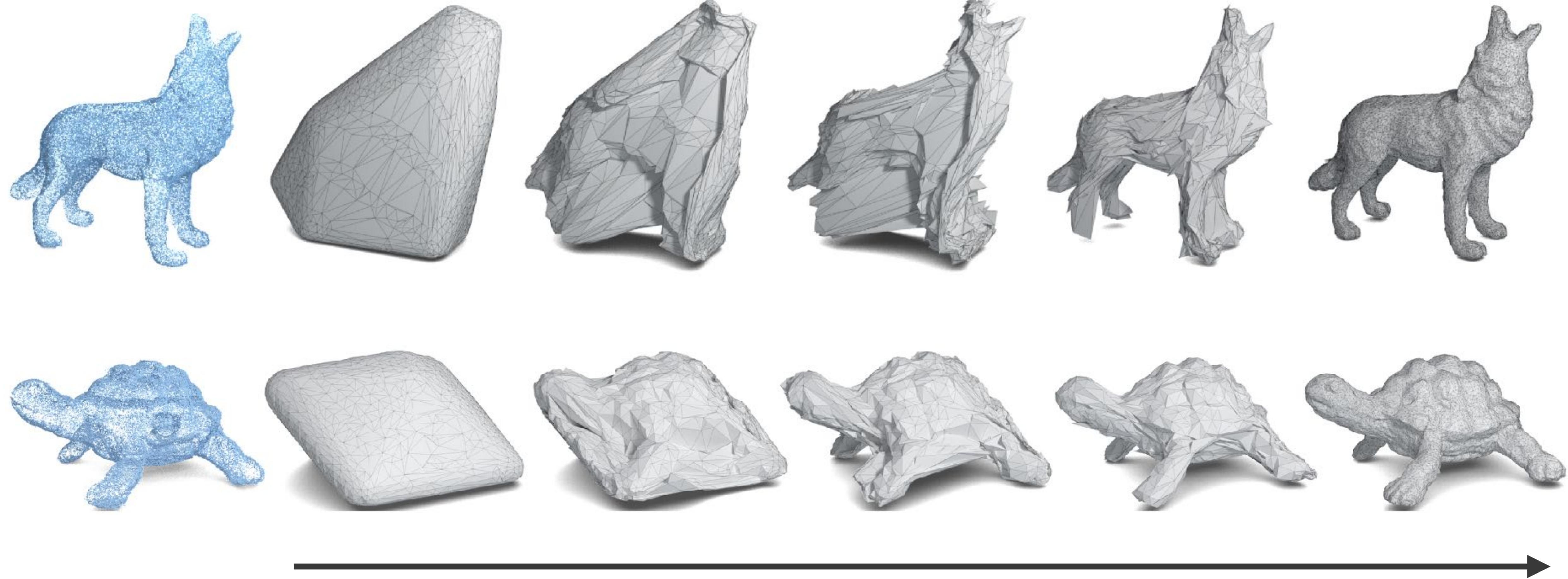
$$\begin{aligned}\mathcal{J}(X, Y) = & \sum_{x \in X} \min_{y \in Y} \|x - y\|^2 \\ & + \sum_{y \in Y} \min_{x \in X} \|y - x\|^2\end{aligned}$$

bidirectional Chamfer

# Optimization

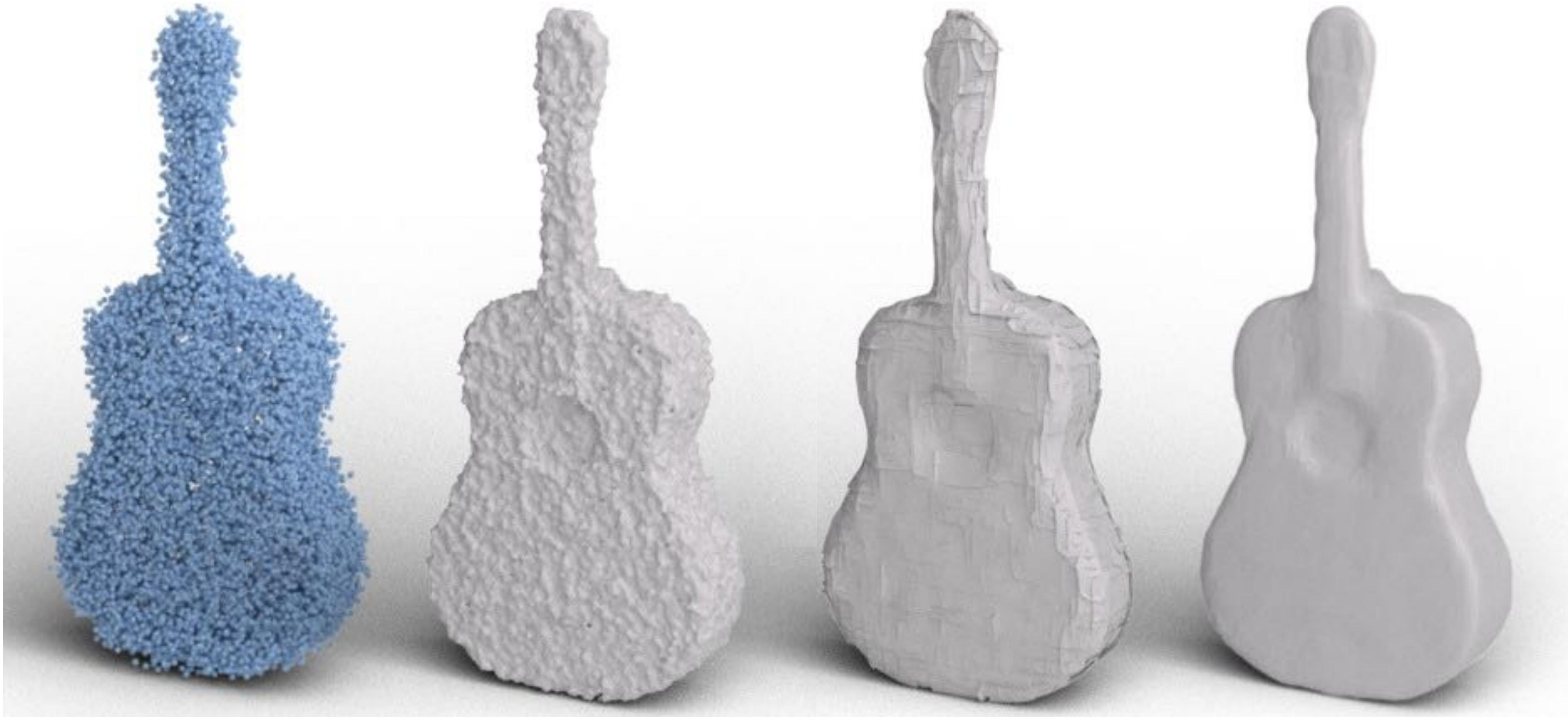


# Results



iterations

# Denosing

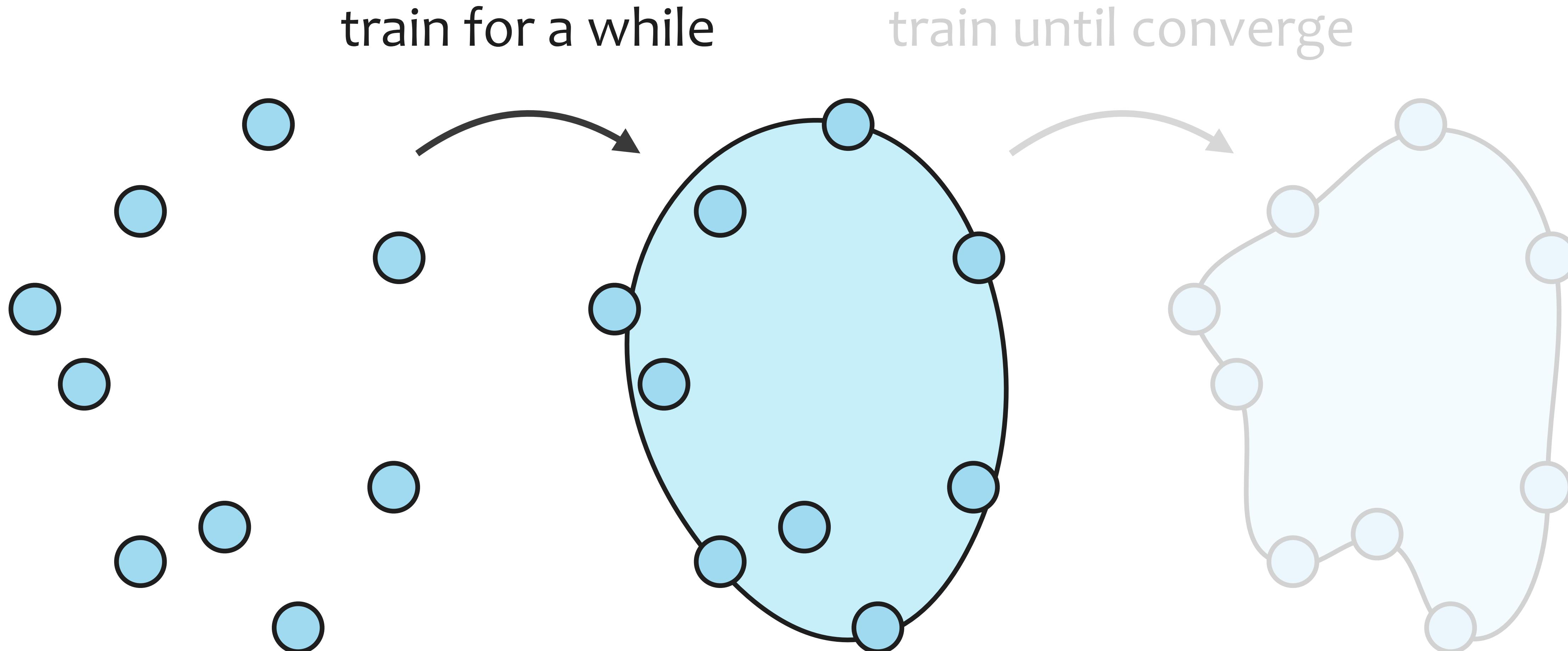


smoothness  
prior

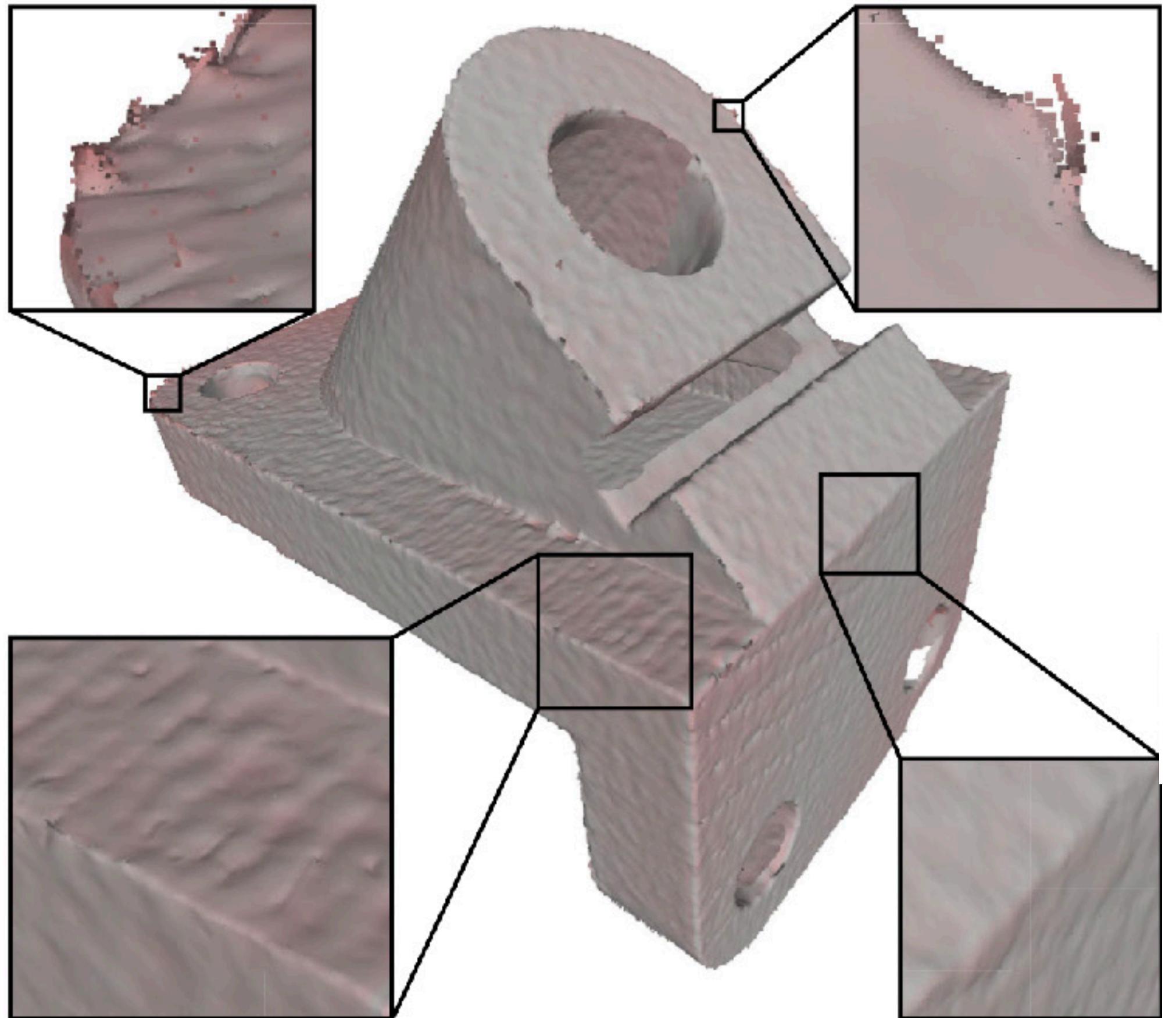
deep  
geometric prior

self-prior

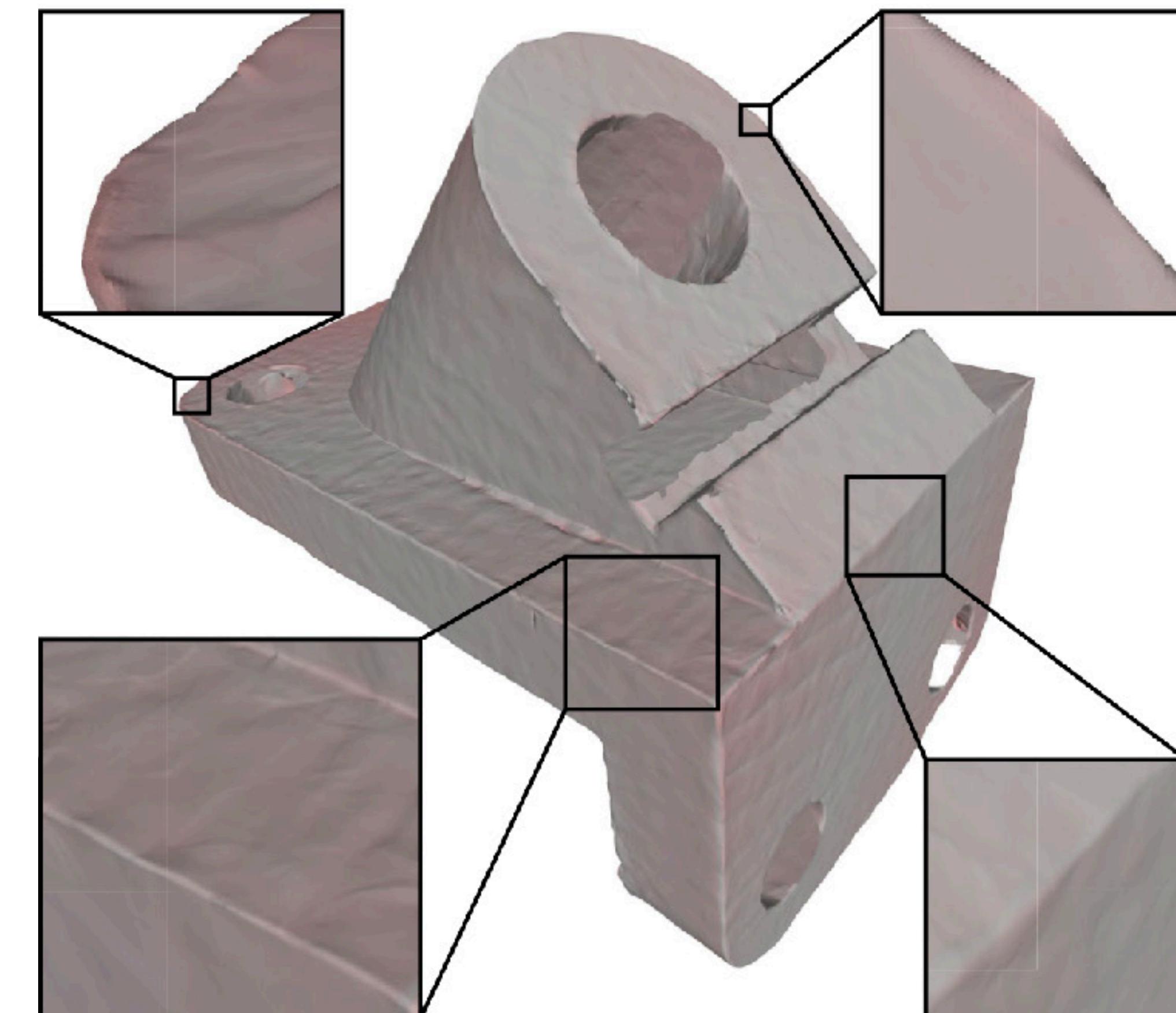
# Early-stop as a regularization



# Early-Stop Regularization

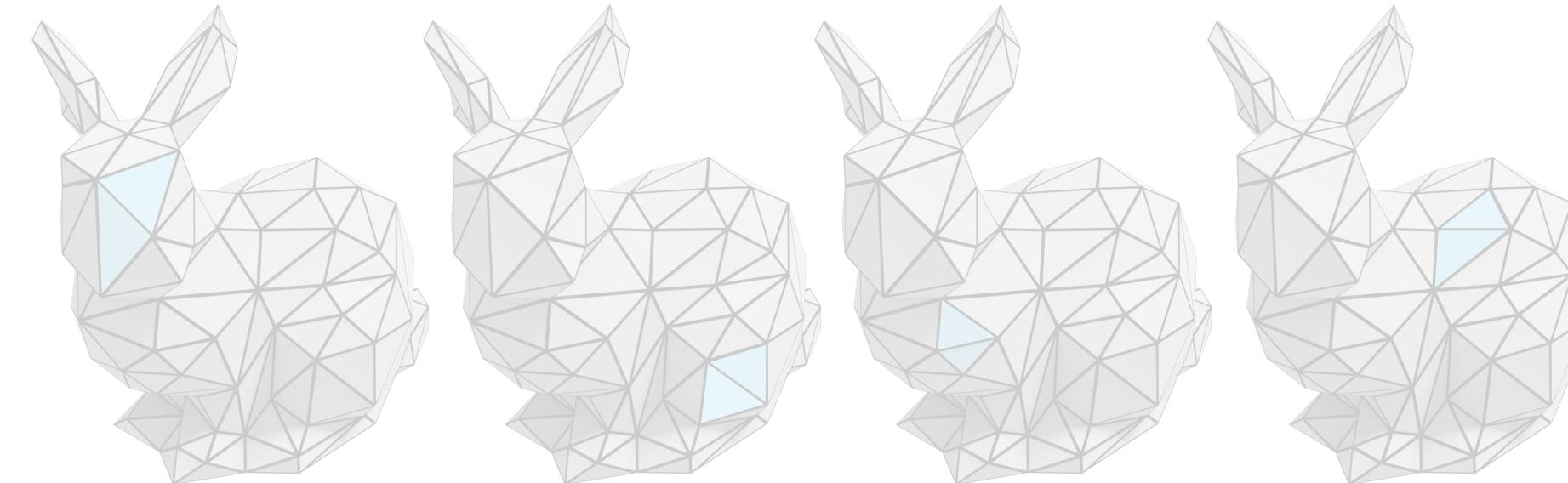


Classic



deep geometric prior

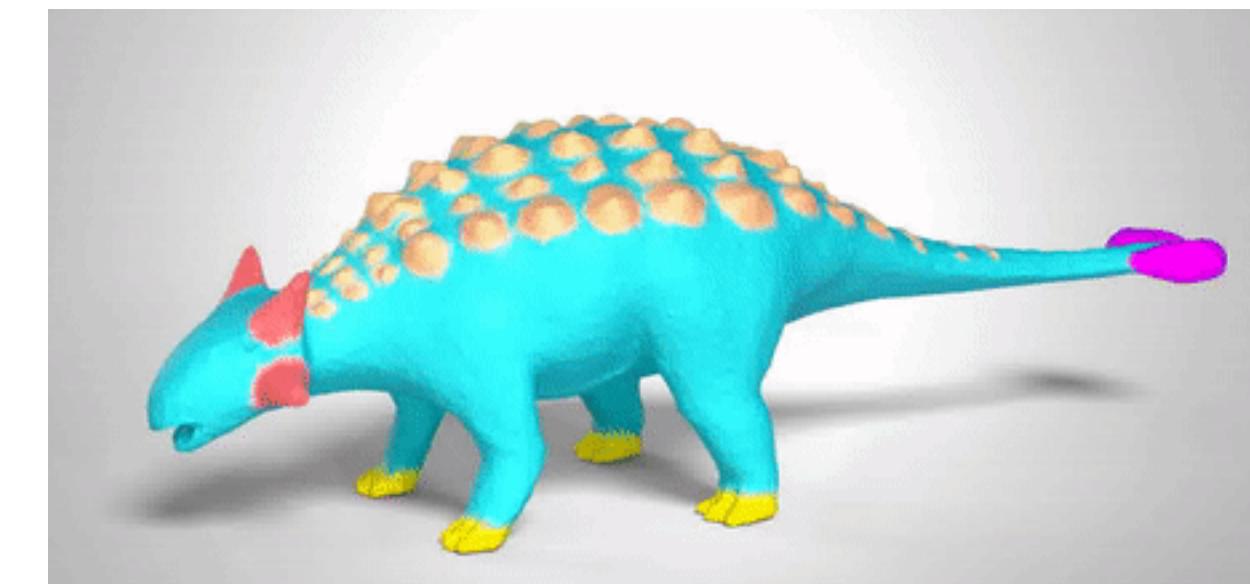
# Mesh Convolutional Neural Networks



## Machine Learning & Geometry Processing



## Learning from a Single Mesh

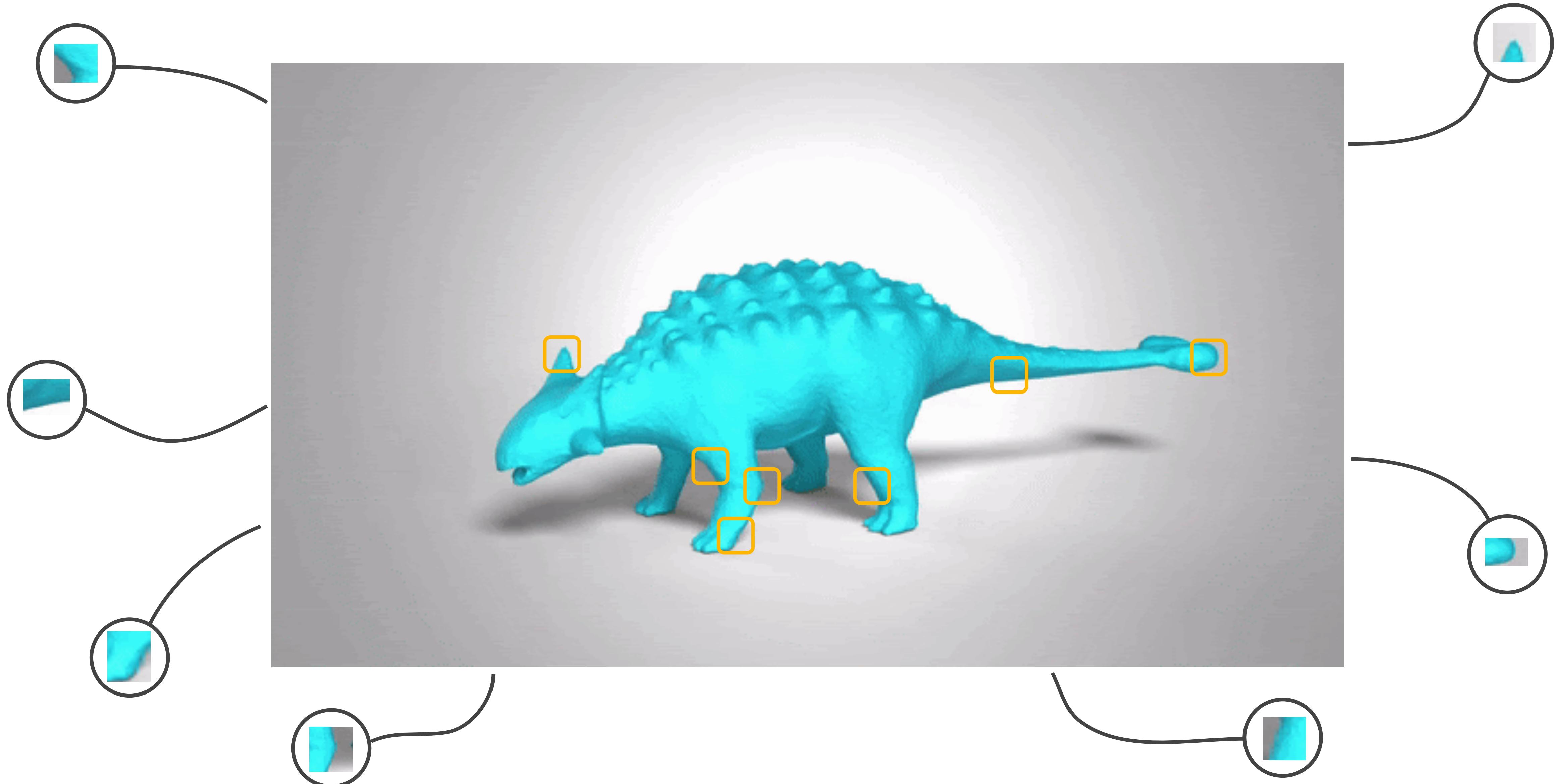


# Learning from external data

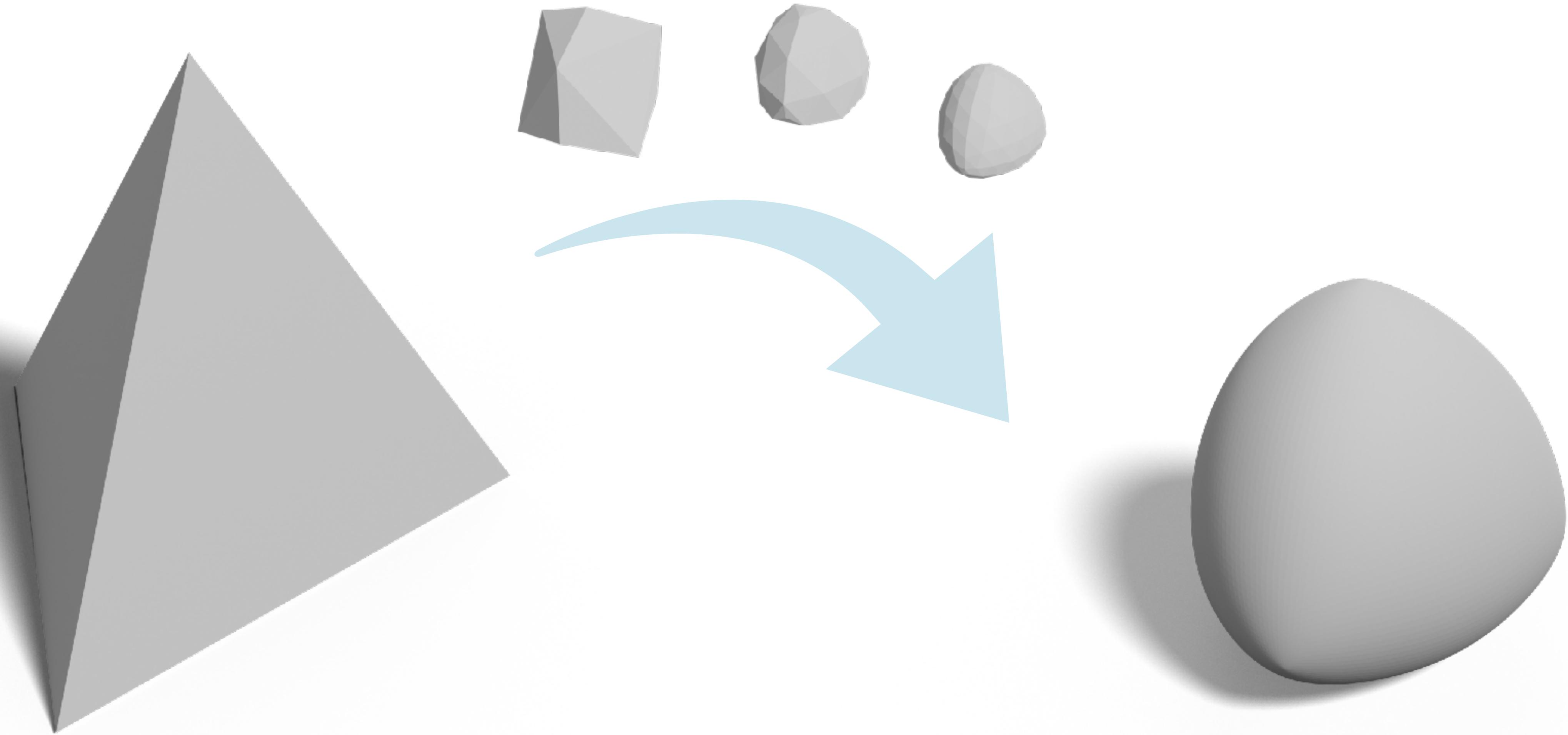


source: NVIDIA kaolin

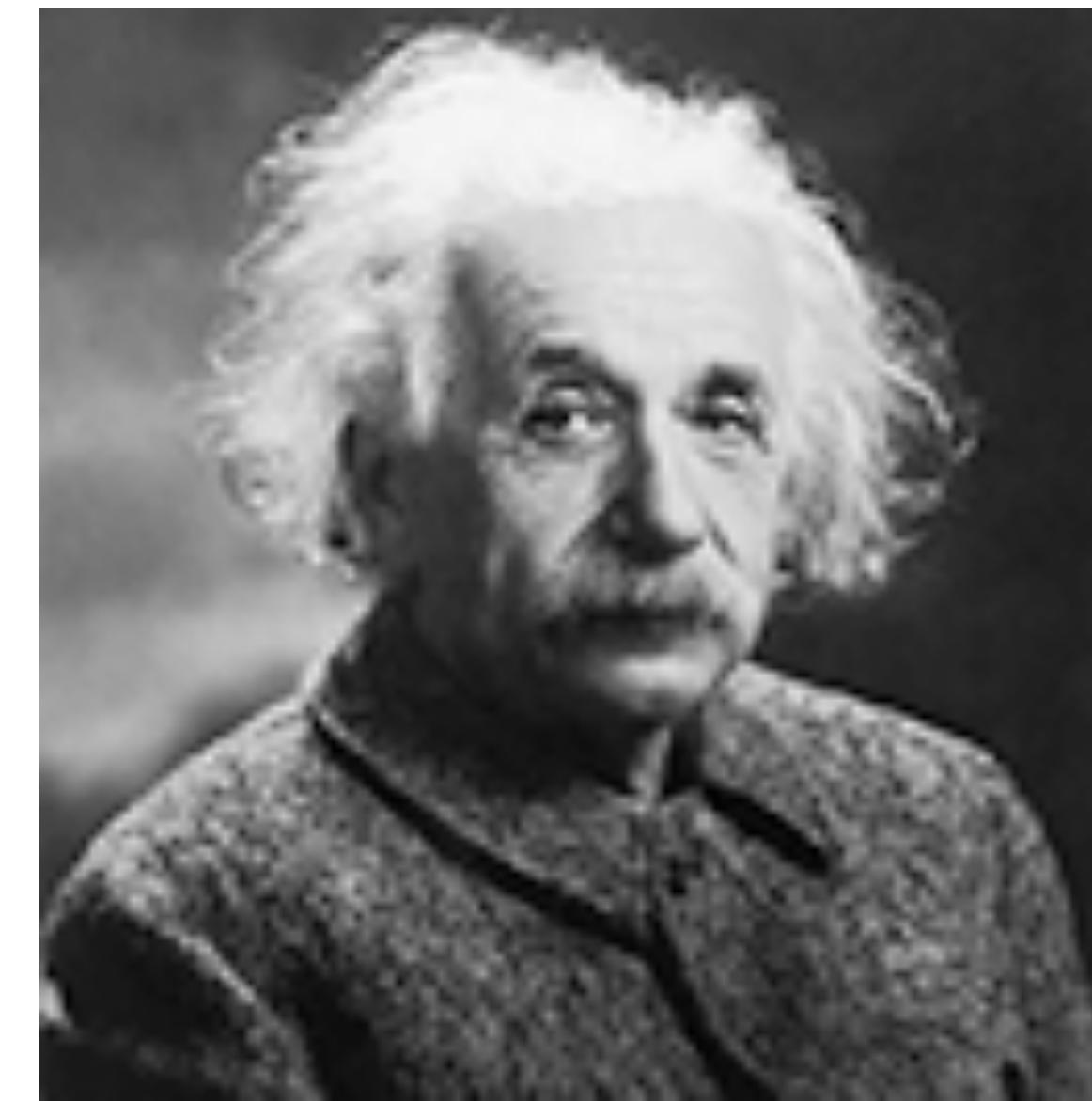
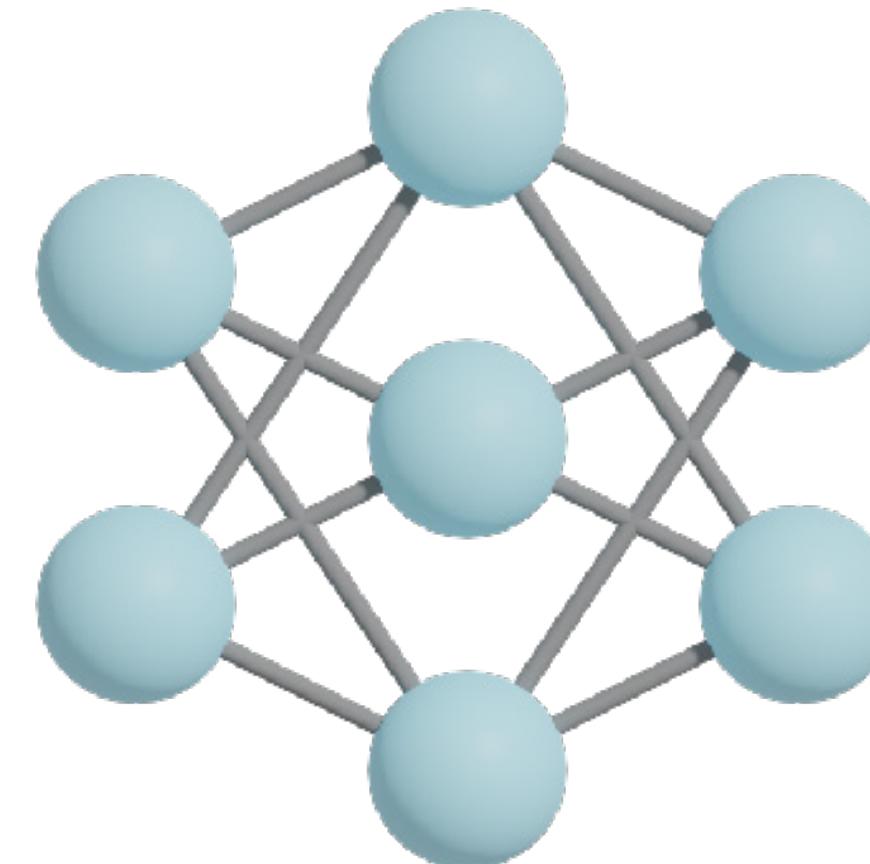
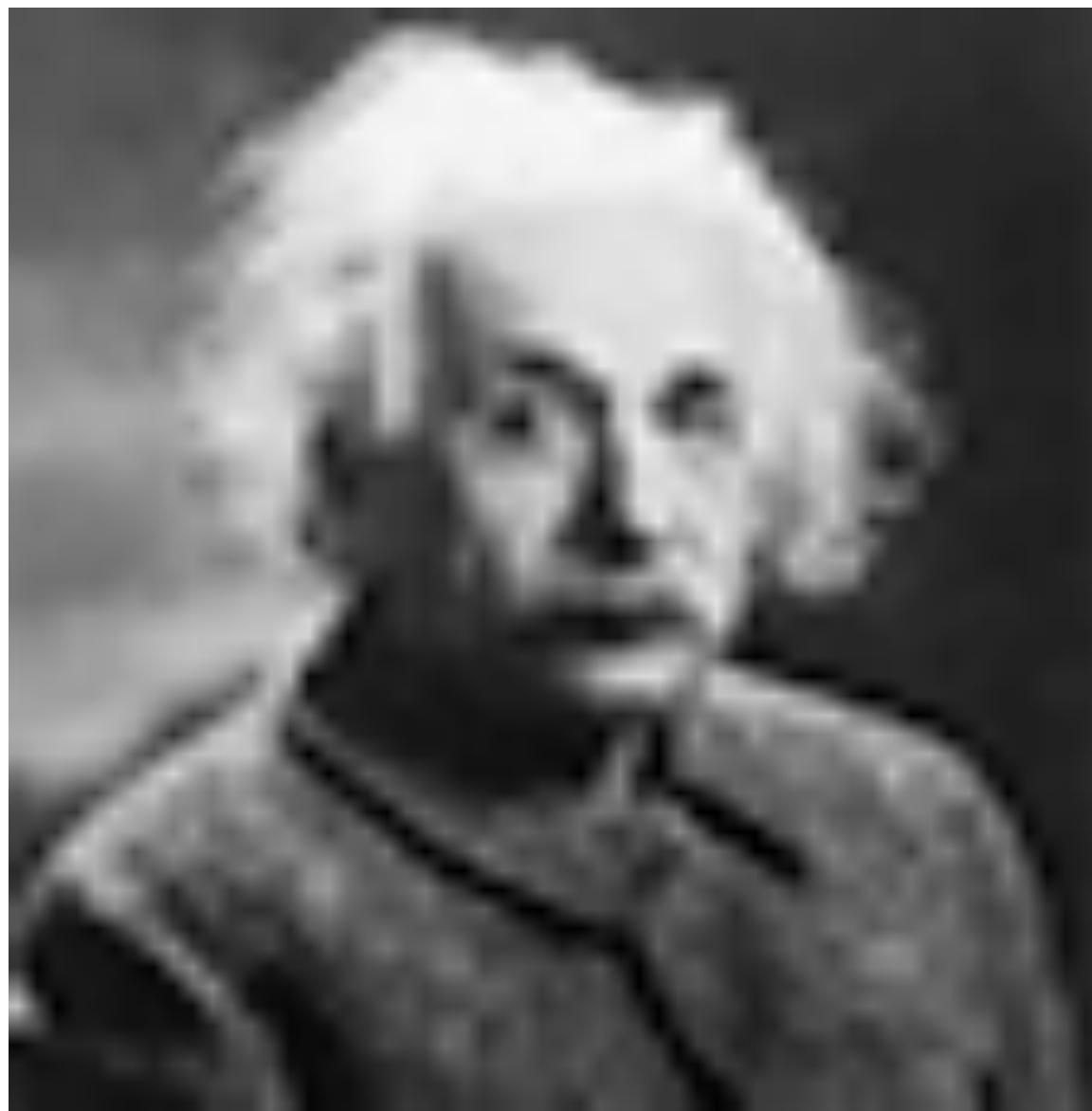
# Learning from internal data



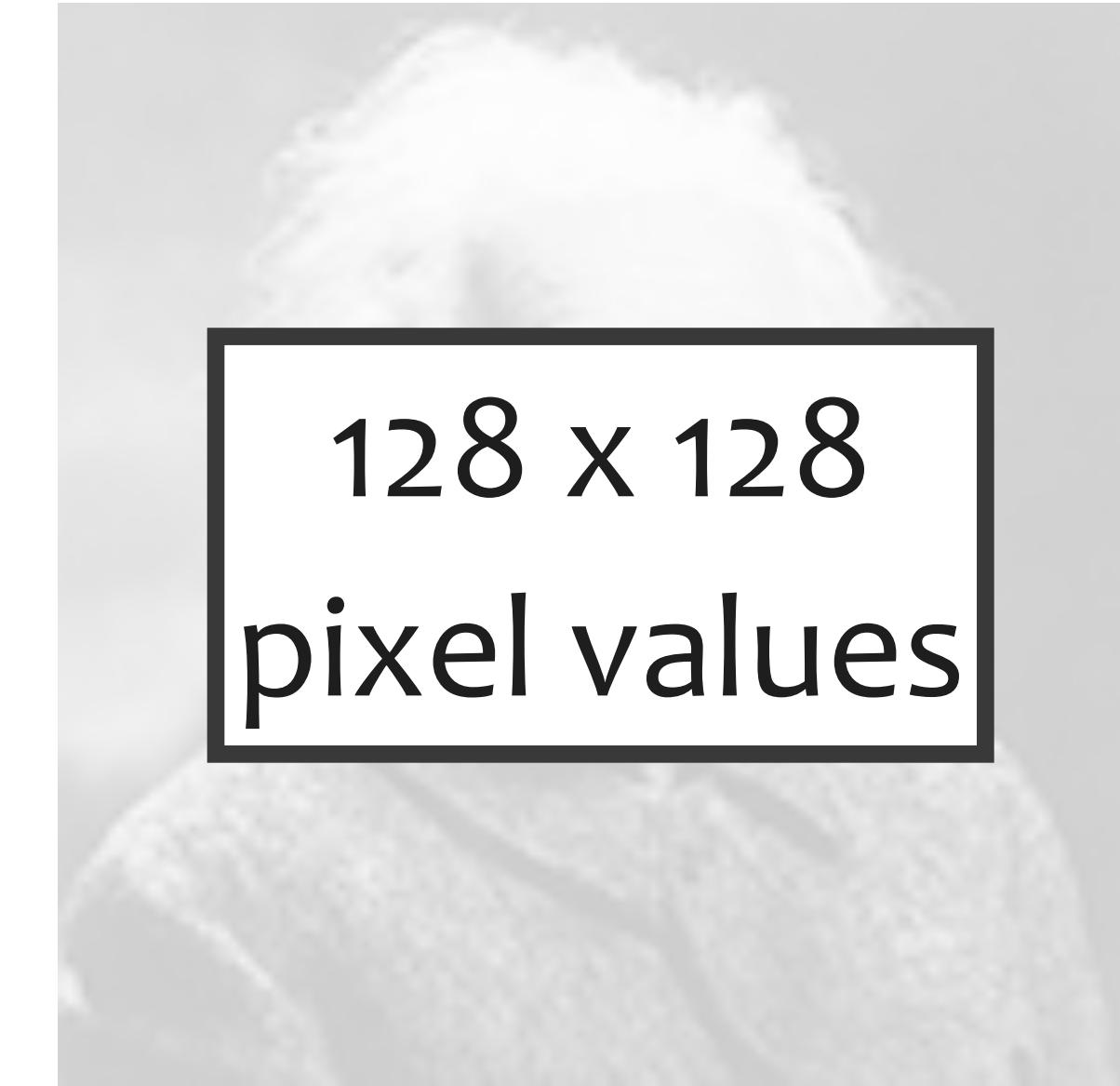
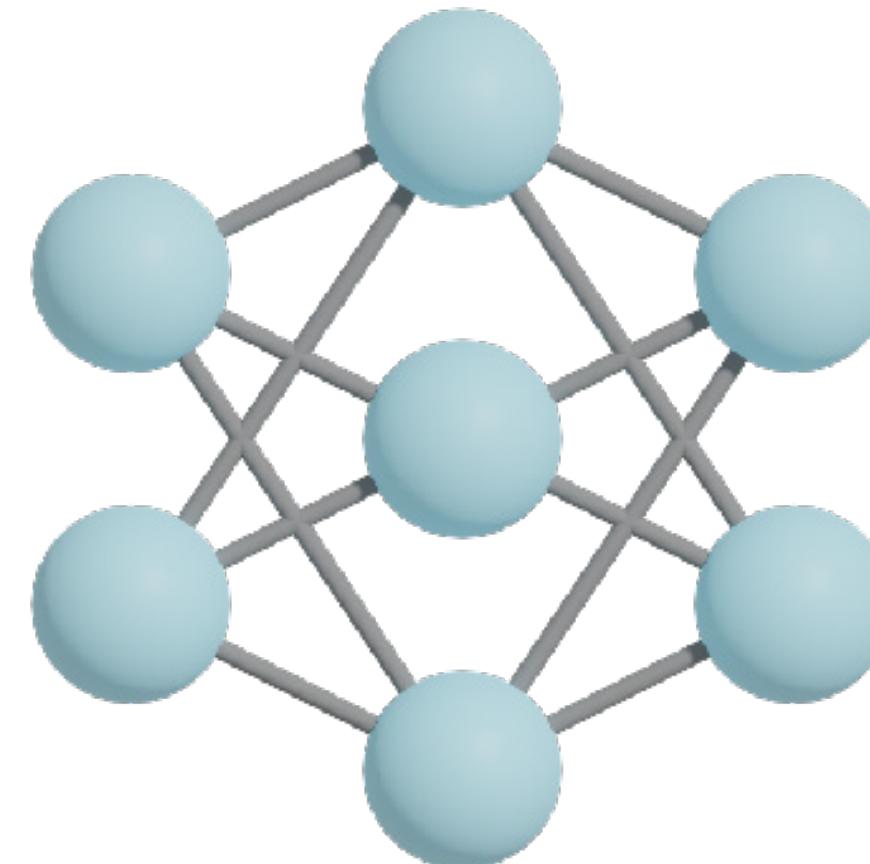
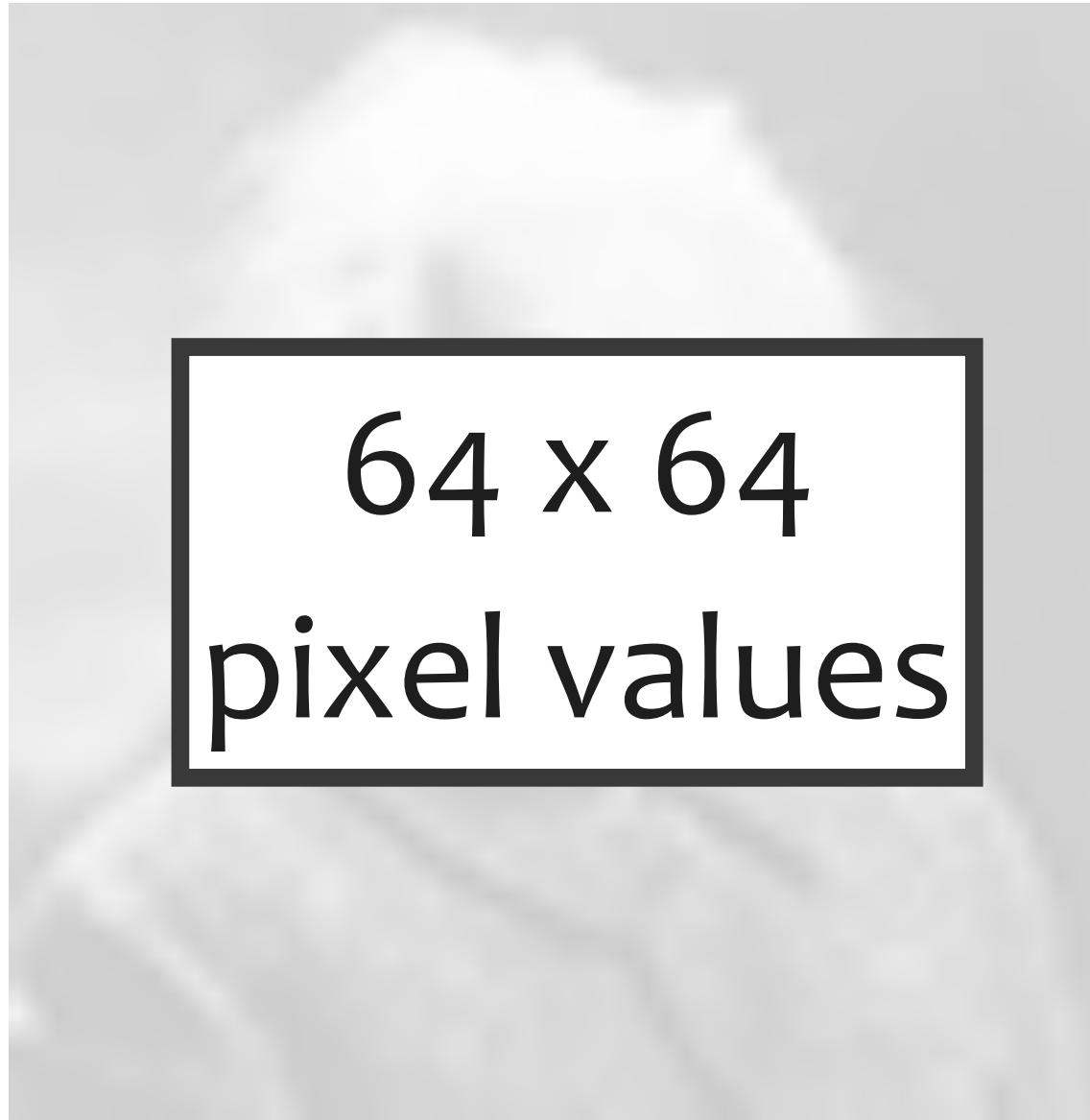
# Example: Mesh Upsampling



# Image Upsampling



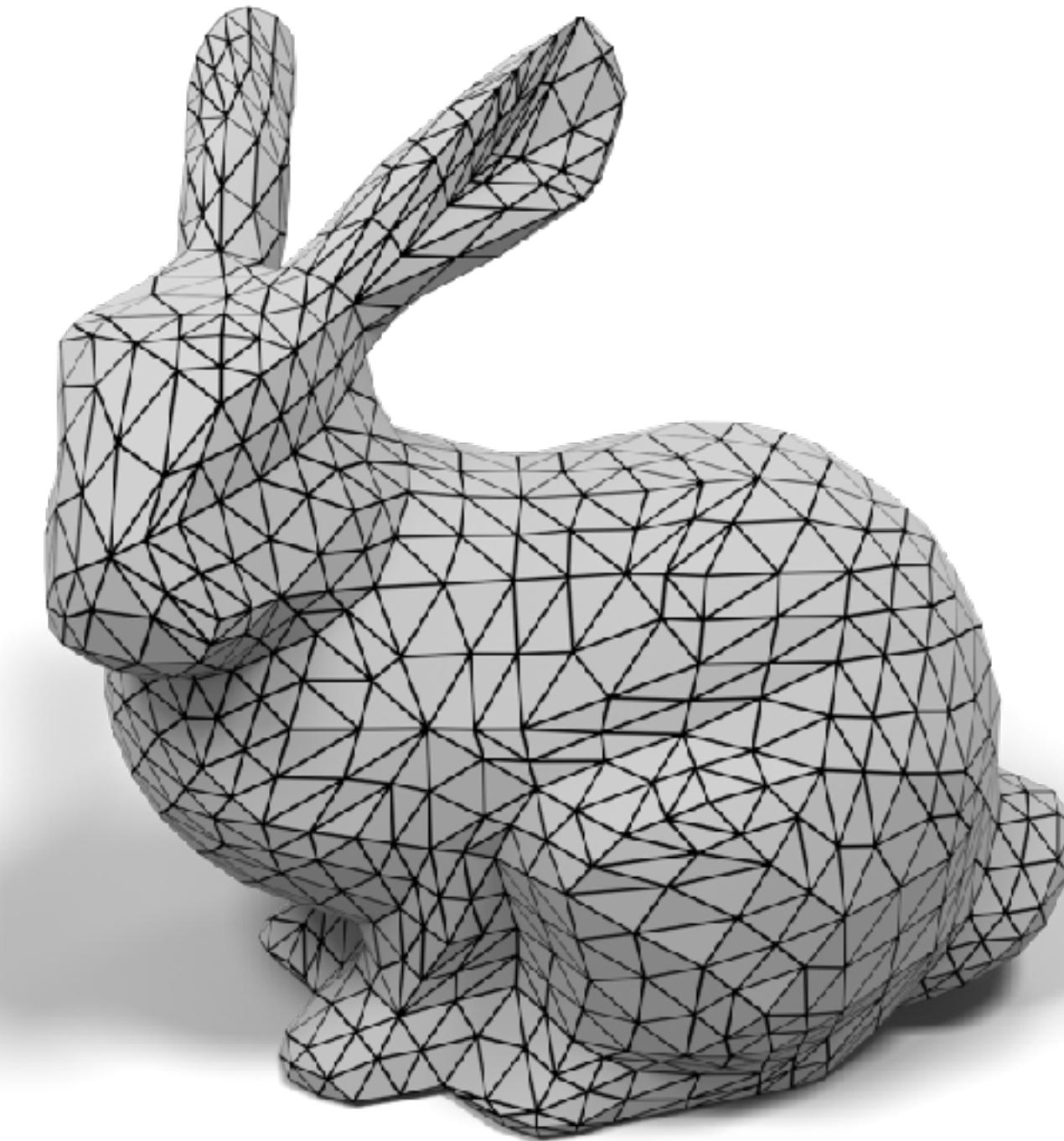
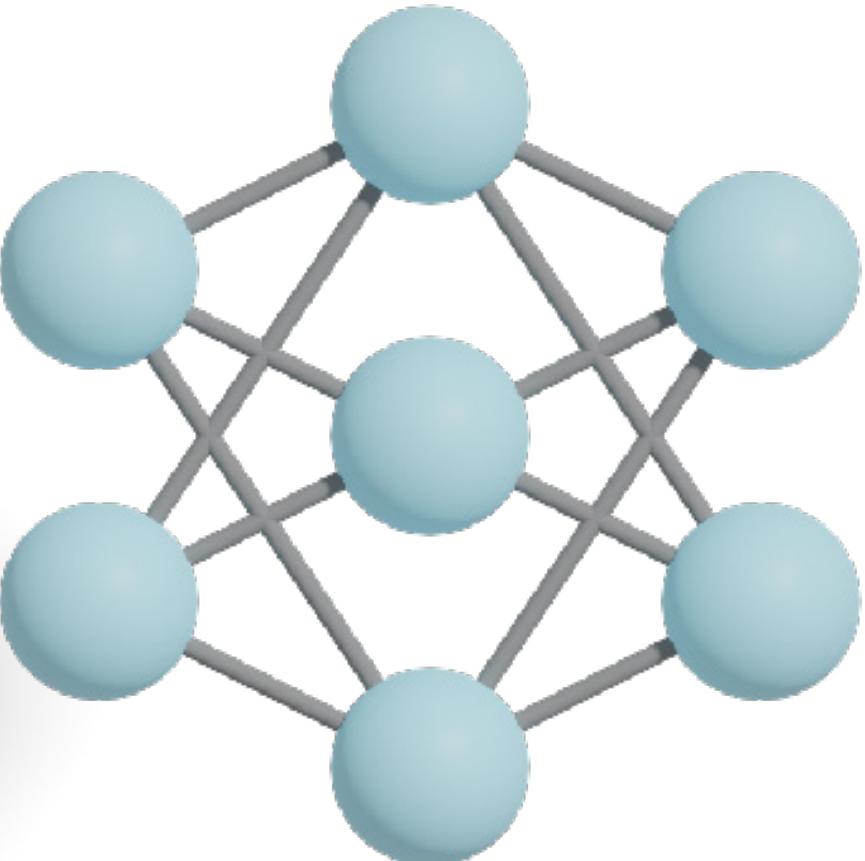
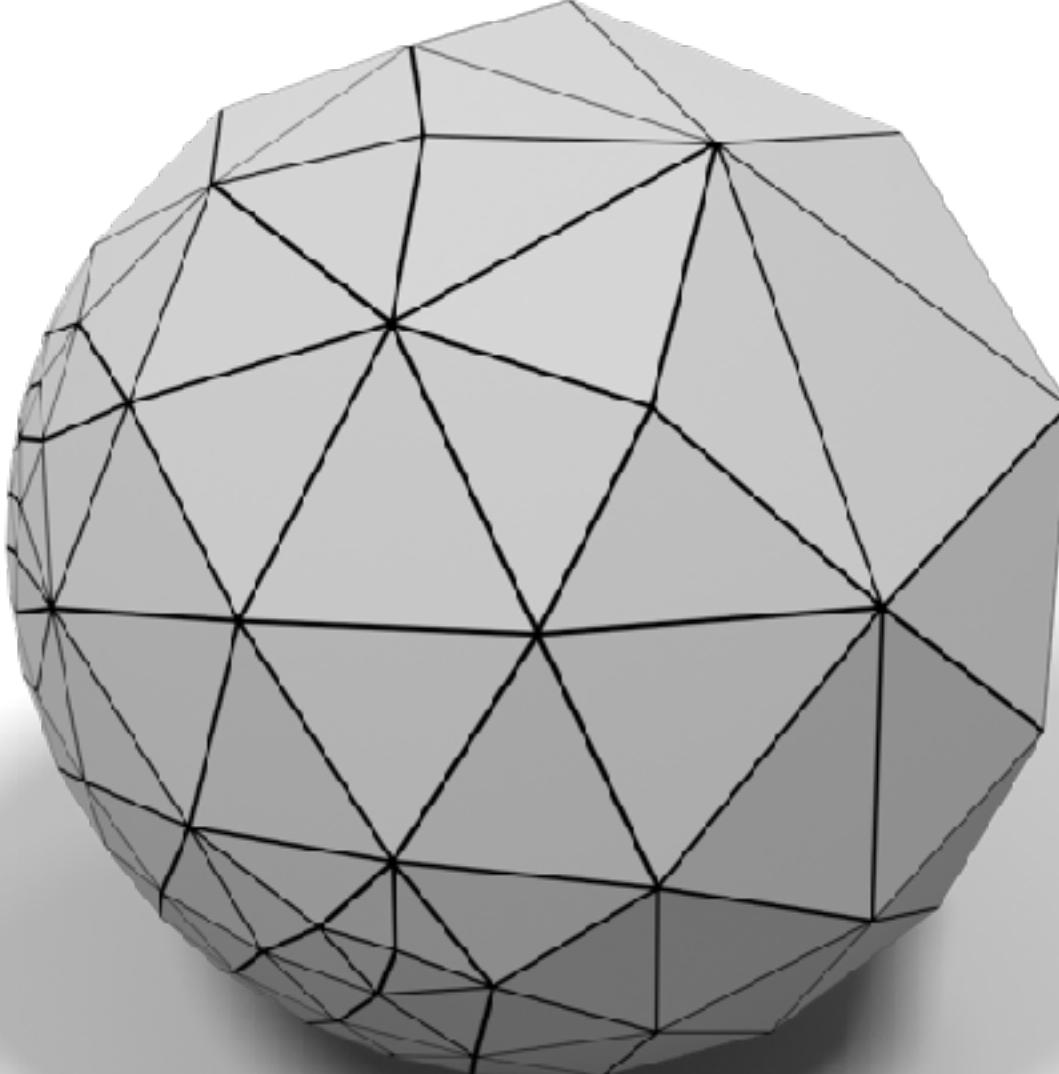
# Image Upsampling



- assume image size 64
- assume grid structure
- assume top-left to bottom-right
- assume upright position

- assume image size 128
- assume grid structure
- assume top-left to bottom-right
- assume upright position

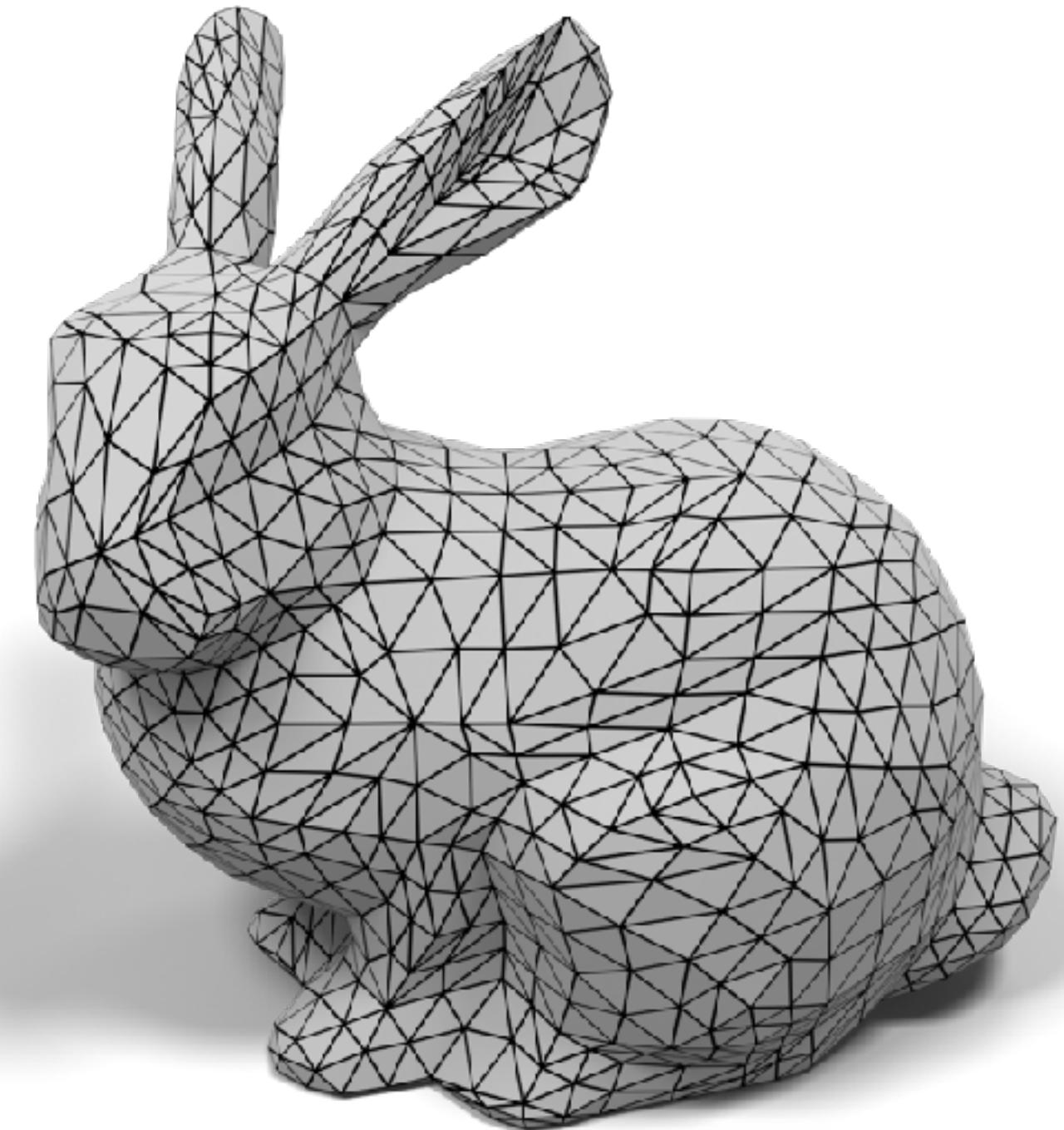
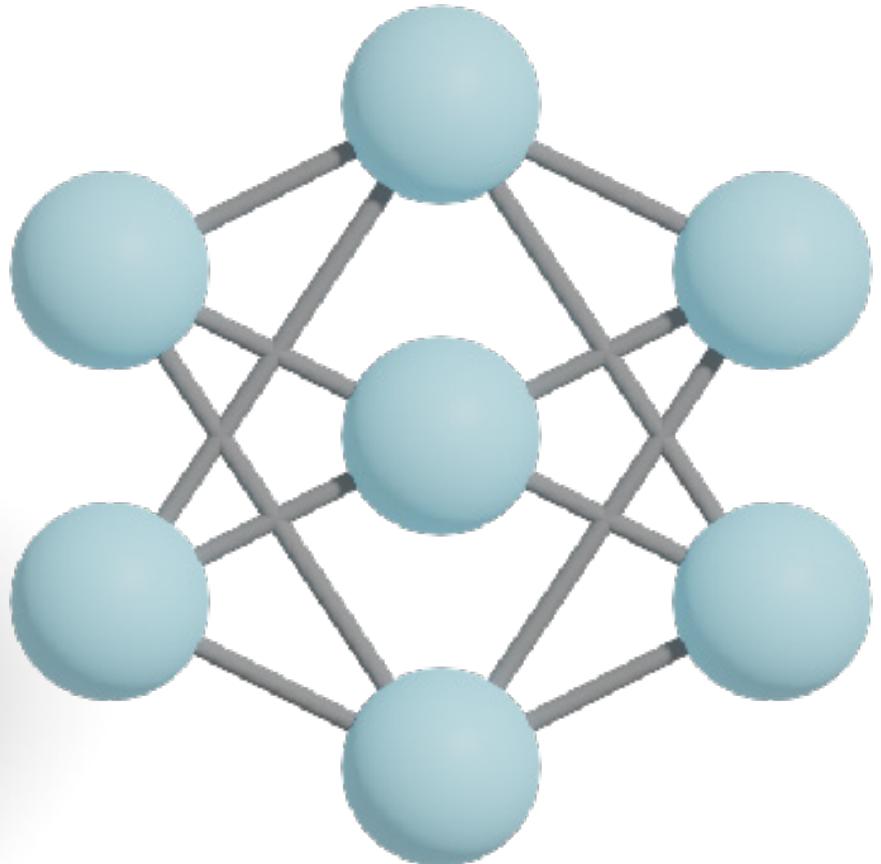
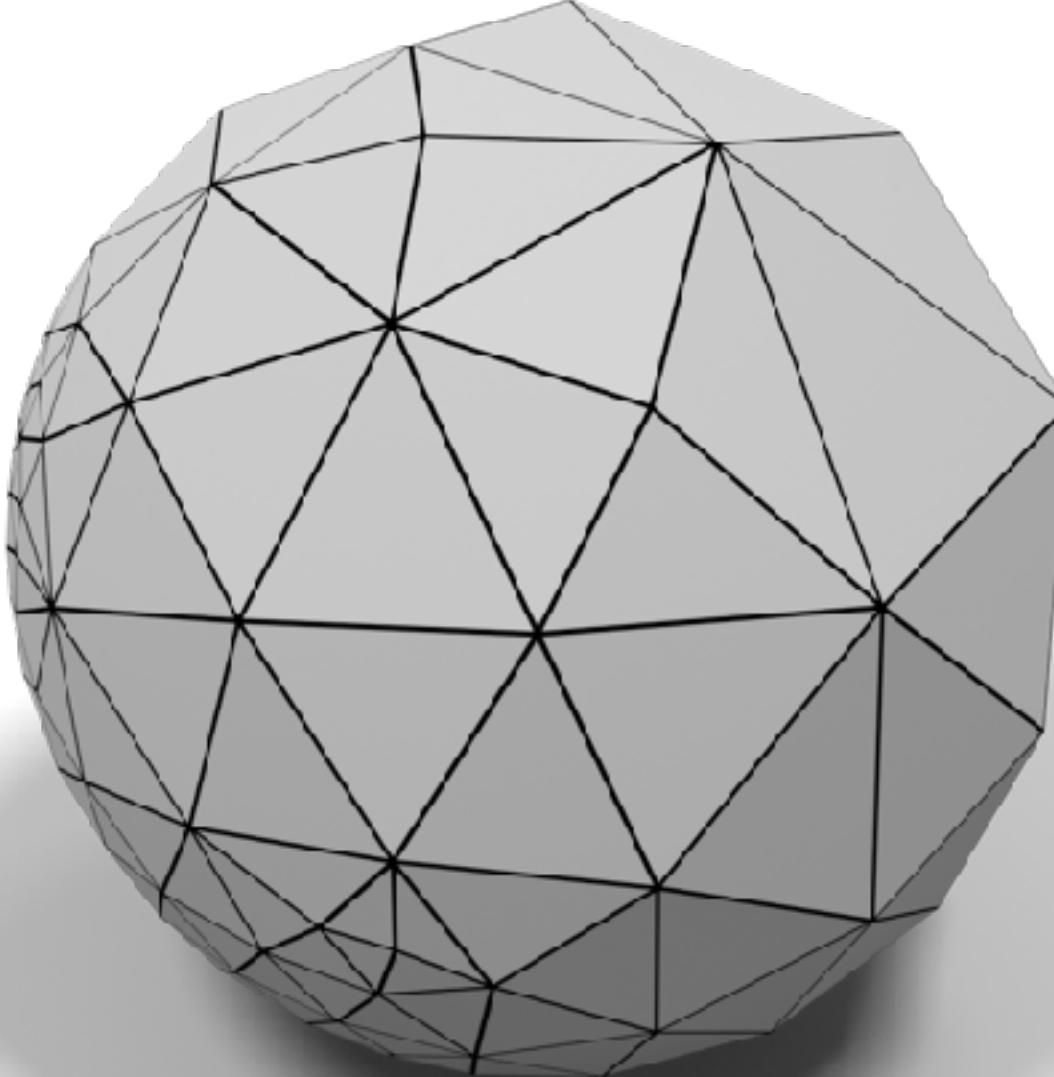
# Draw inspiration from images



- assume image size 64
- assume grid structure
- assume top-left to bottom-right
- assume upright position

- assume image size 128
- assume grid structure
- assume top-left to bottom-right
- assume upright position

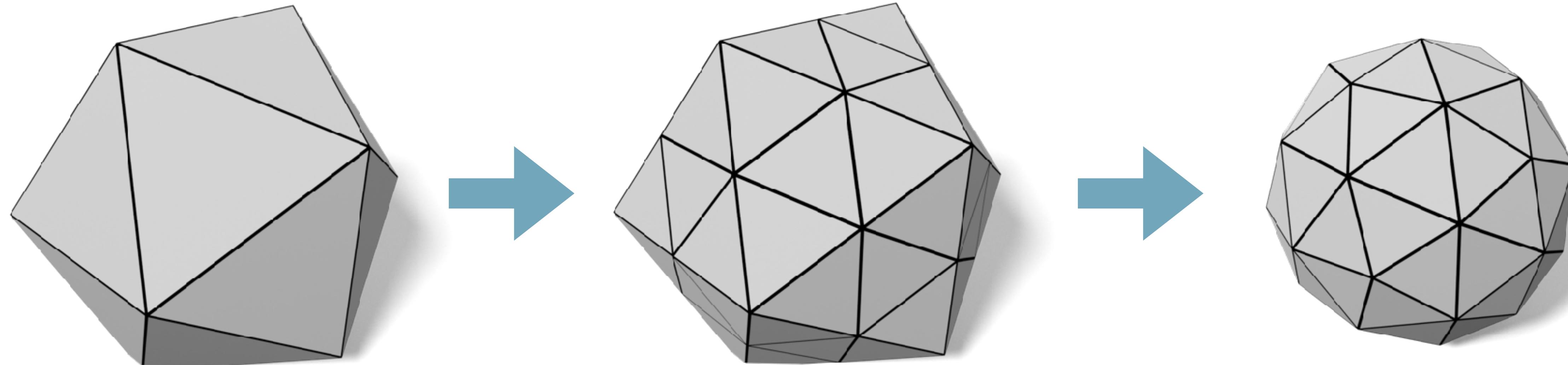
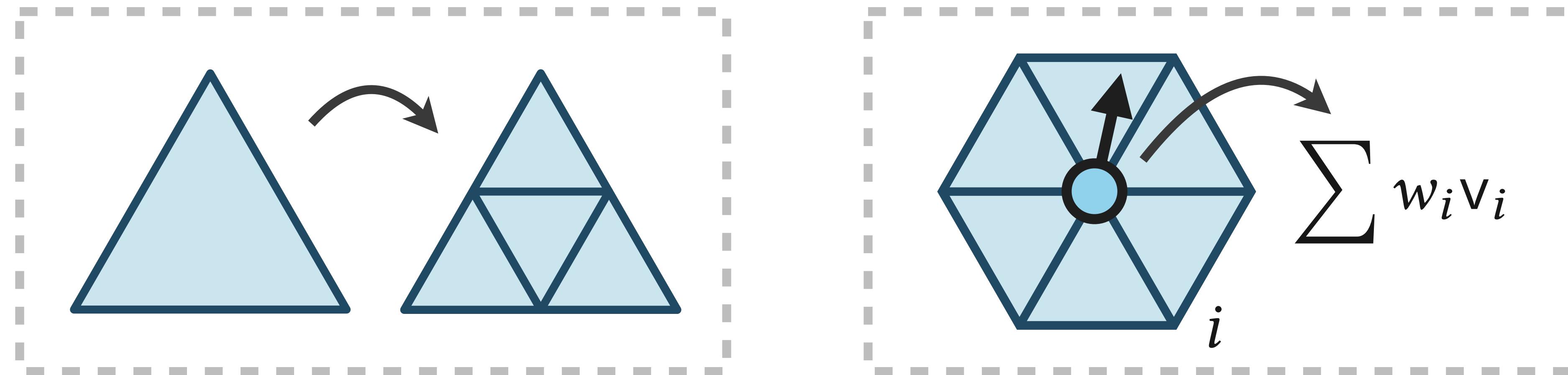
# Draw inspiration from images



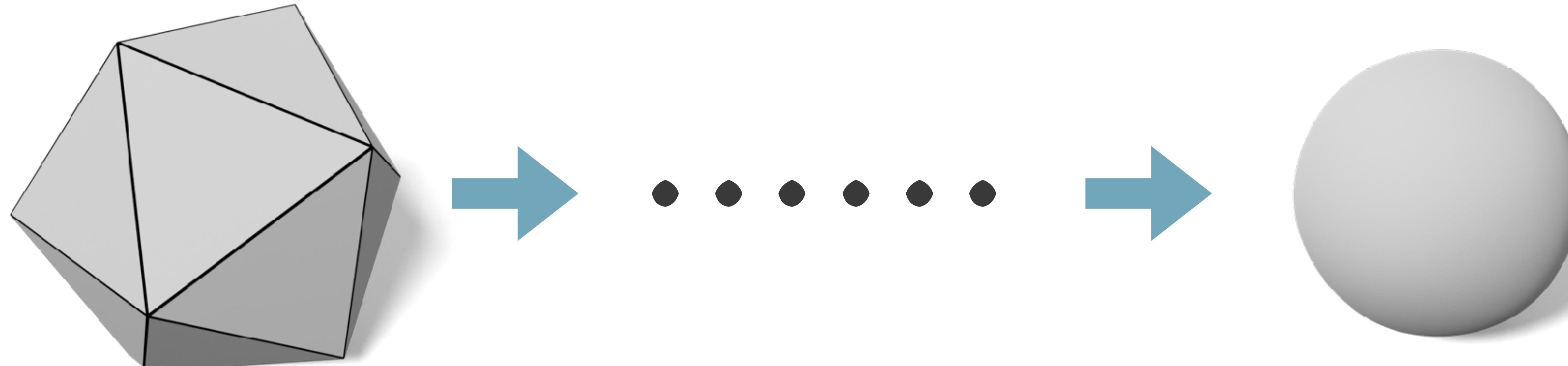
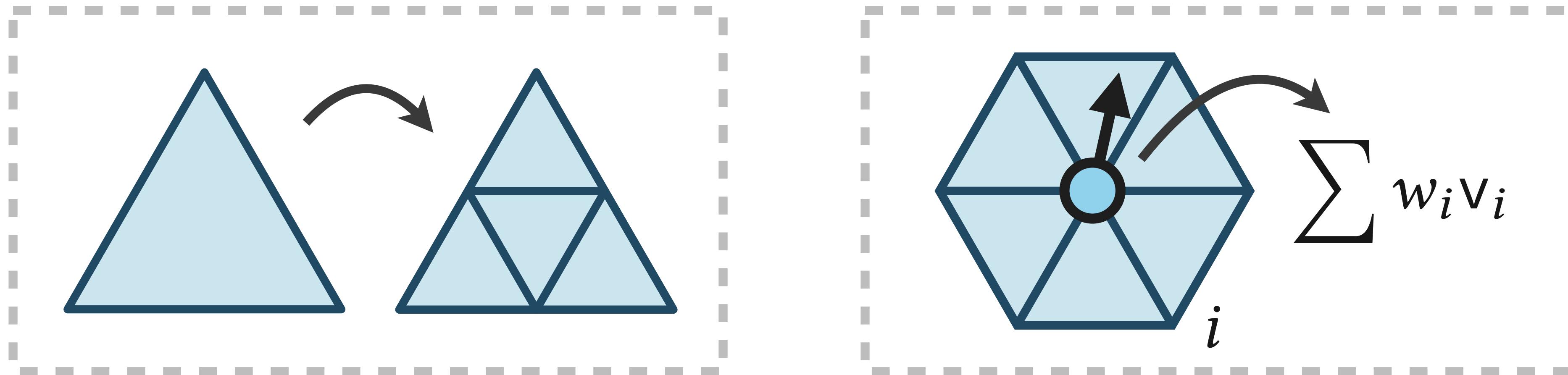
- assume 269 vertices
- assume a specific connectivity
- assume a specific ordering
- assume a specific orientation

- assume 1070 vertices
- assume a specific connectivity
- assume a specific ordering
- assume a specific orientation

# Classic Subdivision



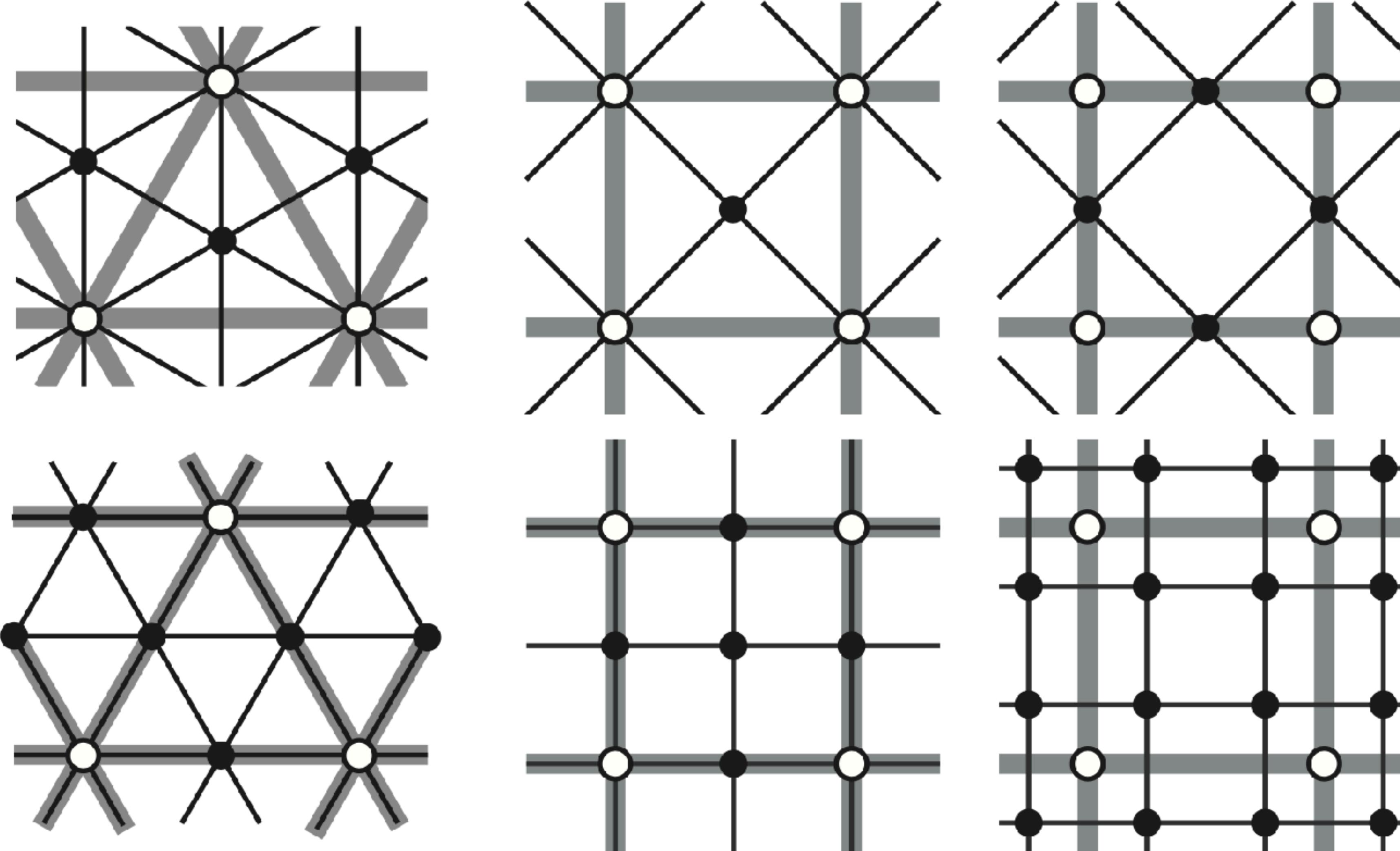
# Classic Subdivision



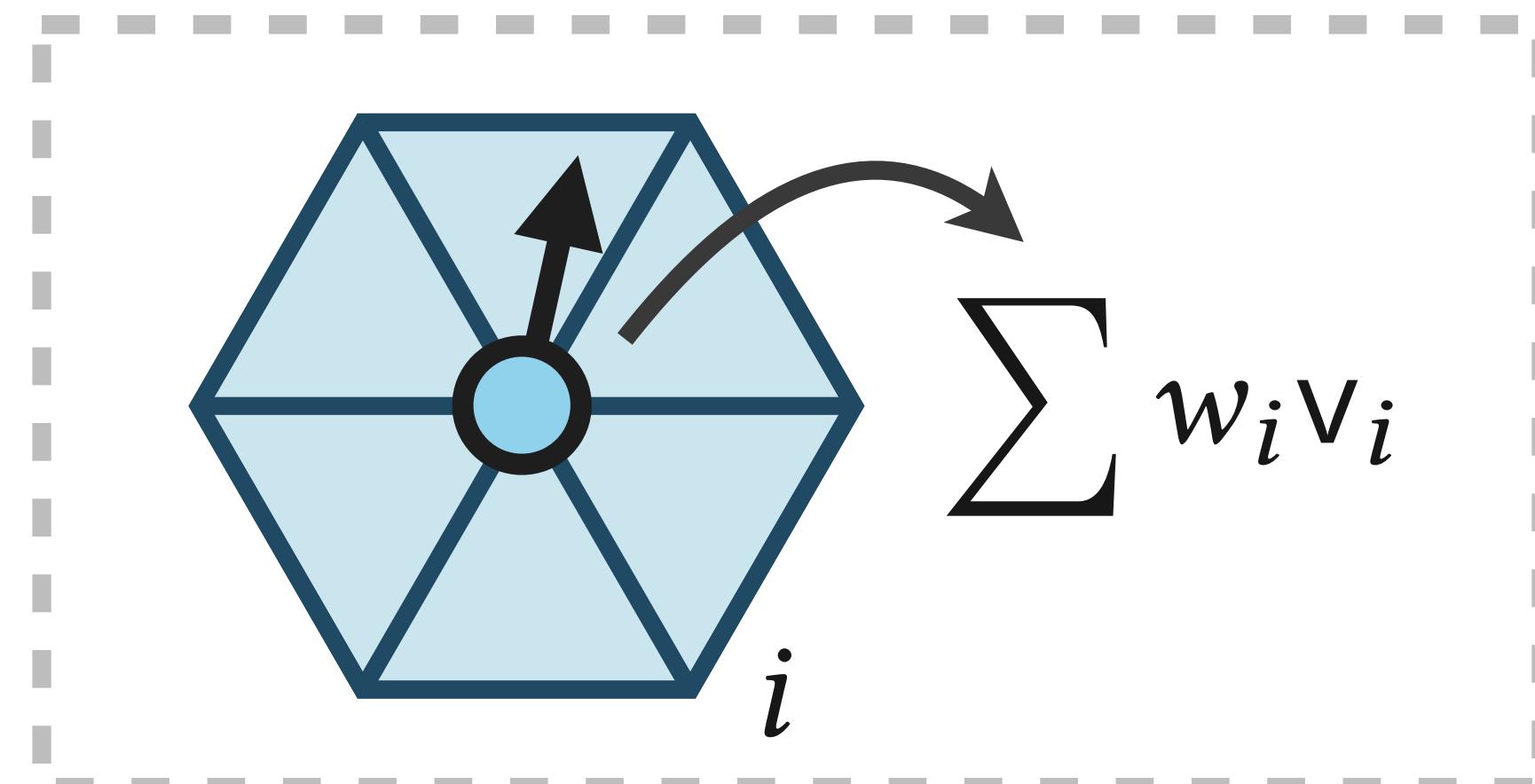
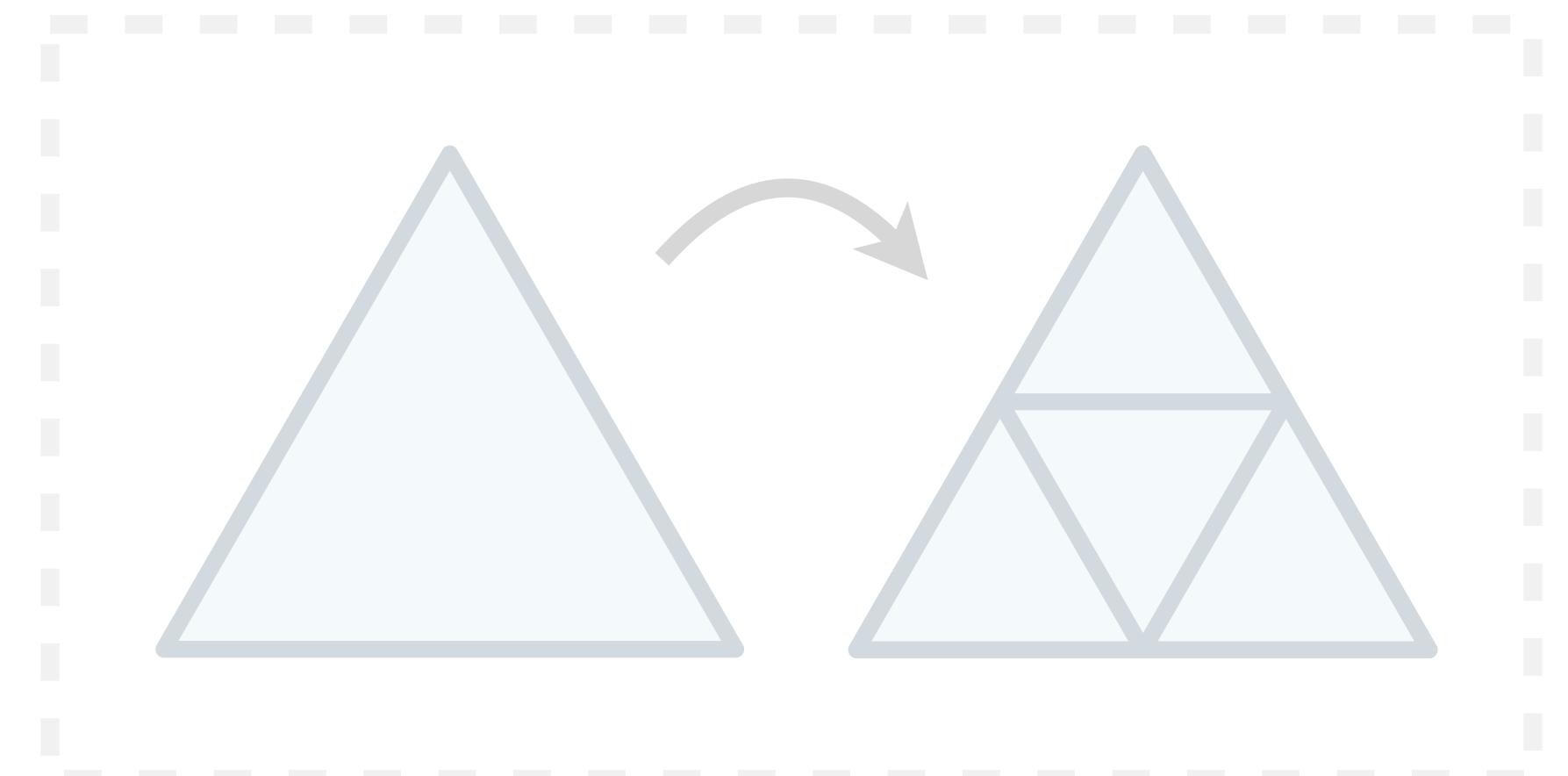
# Where we should put the network?



# Discrete Variables

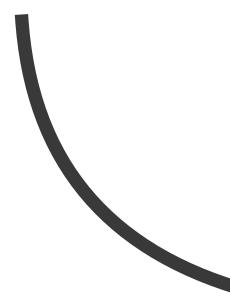
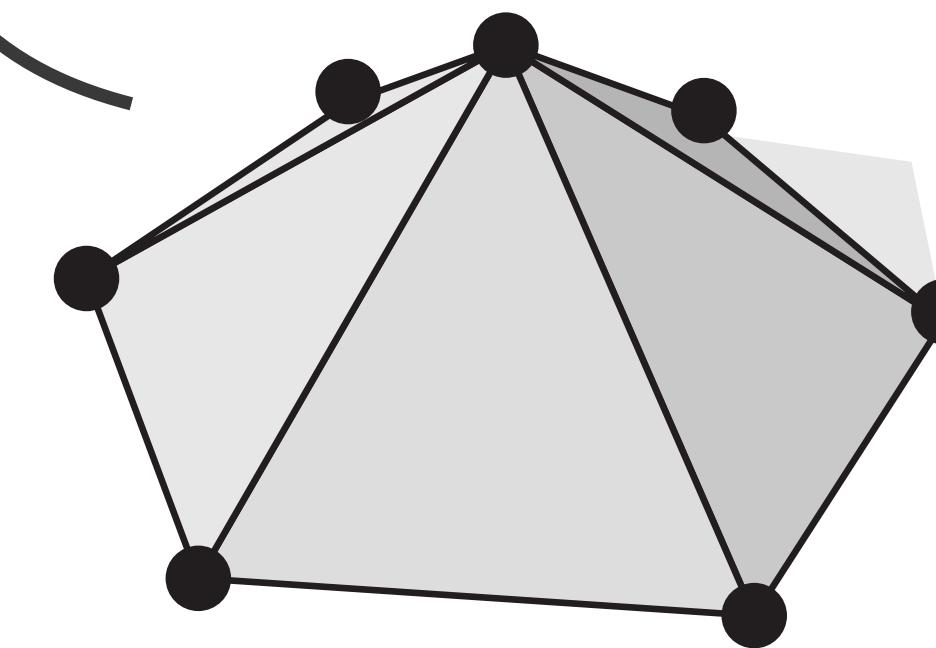
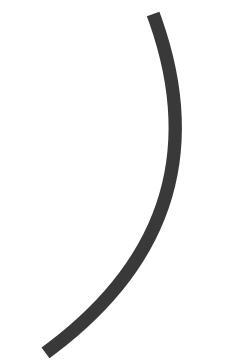
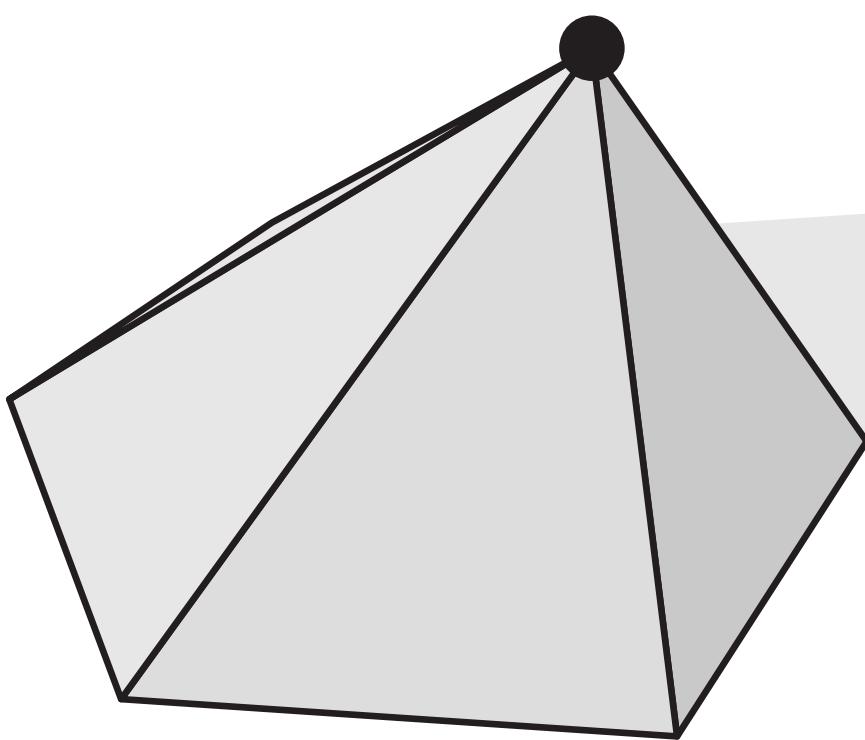


# Where we should put the network?



# From features to locations

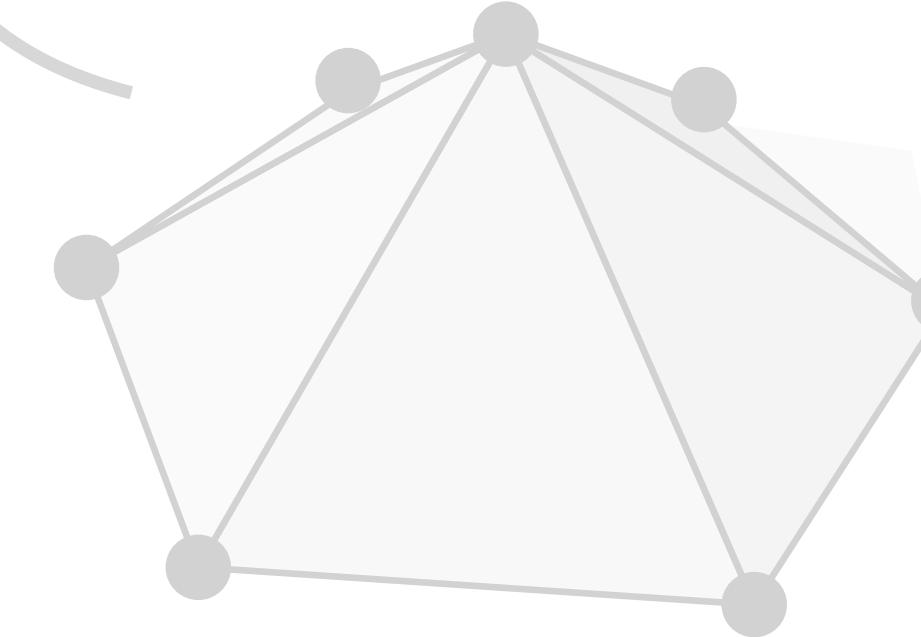
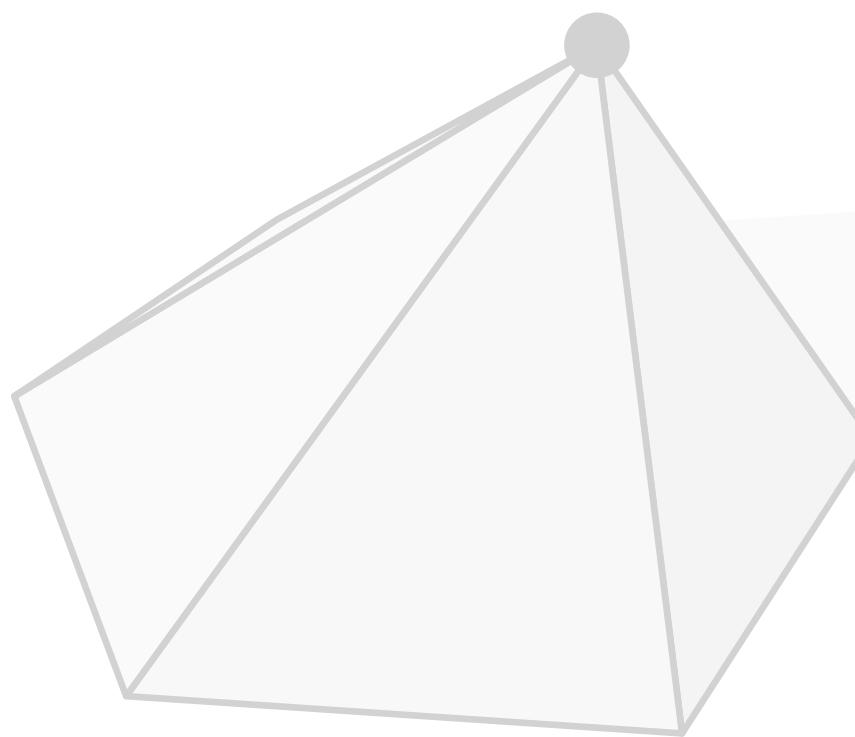
$$y = f_{\theta}(x)$$



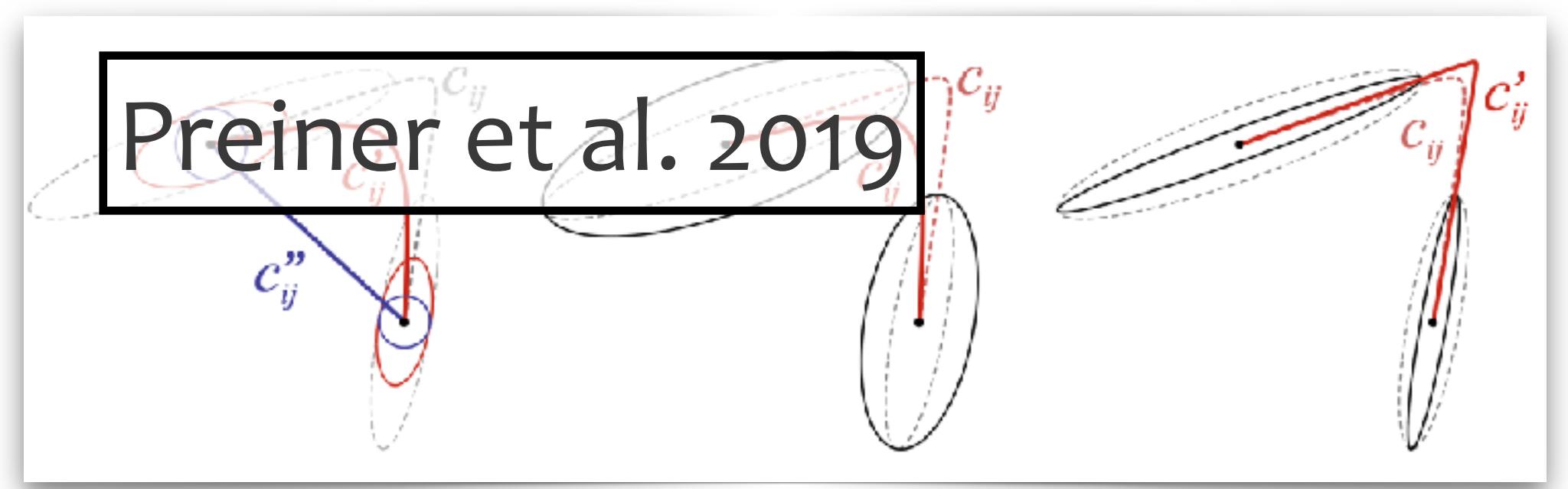
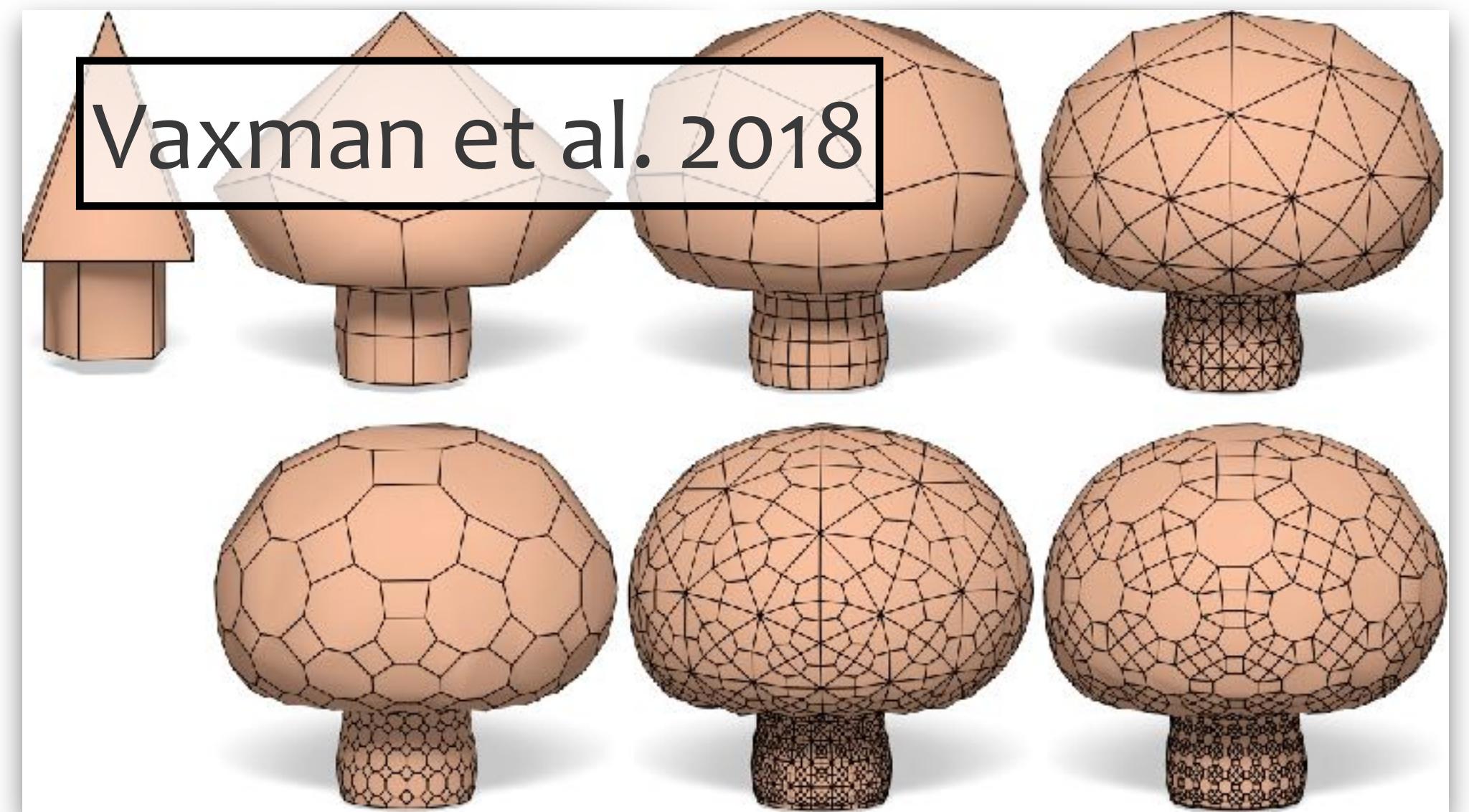
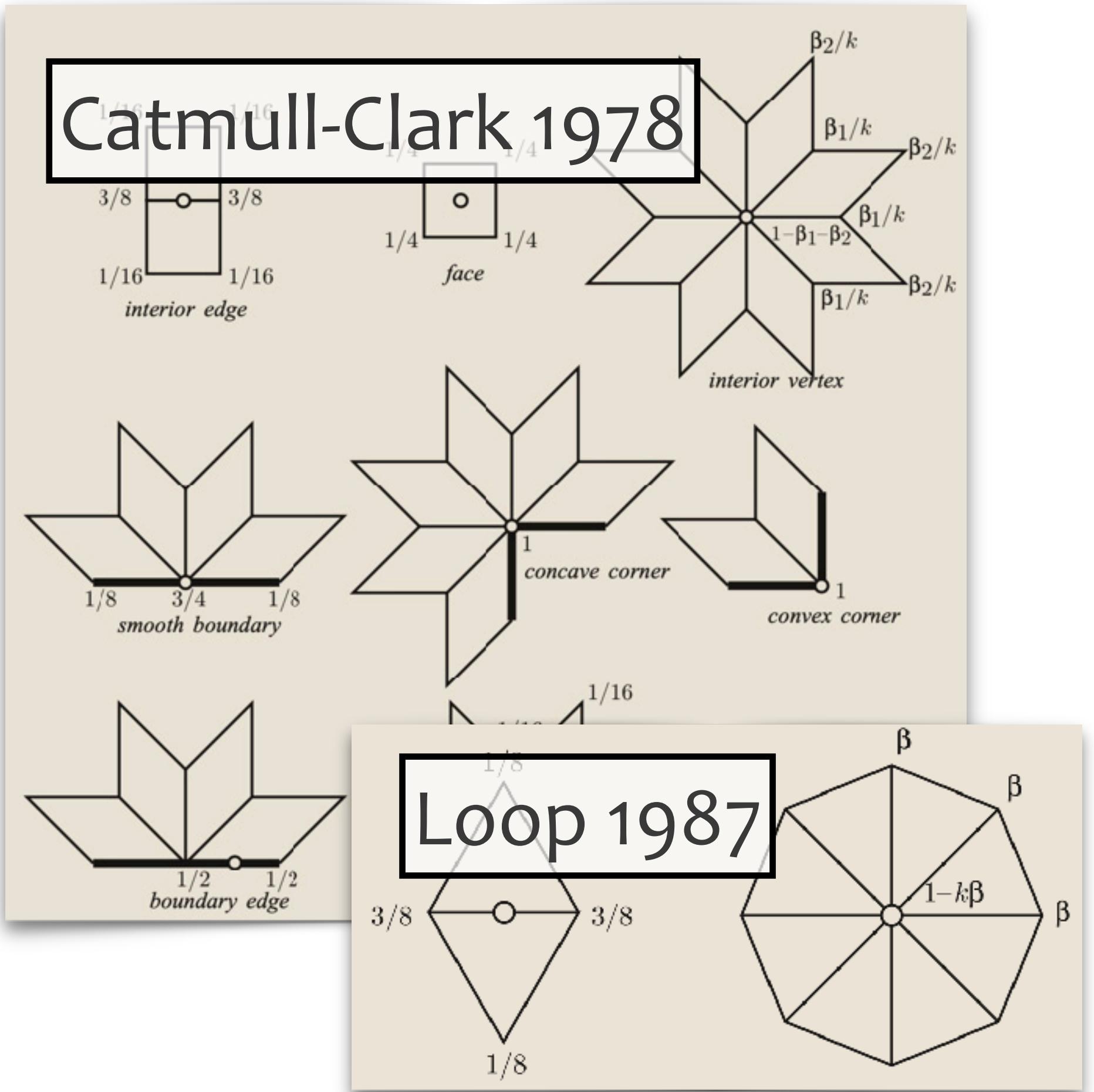
# From features to locations

difficult to define

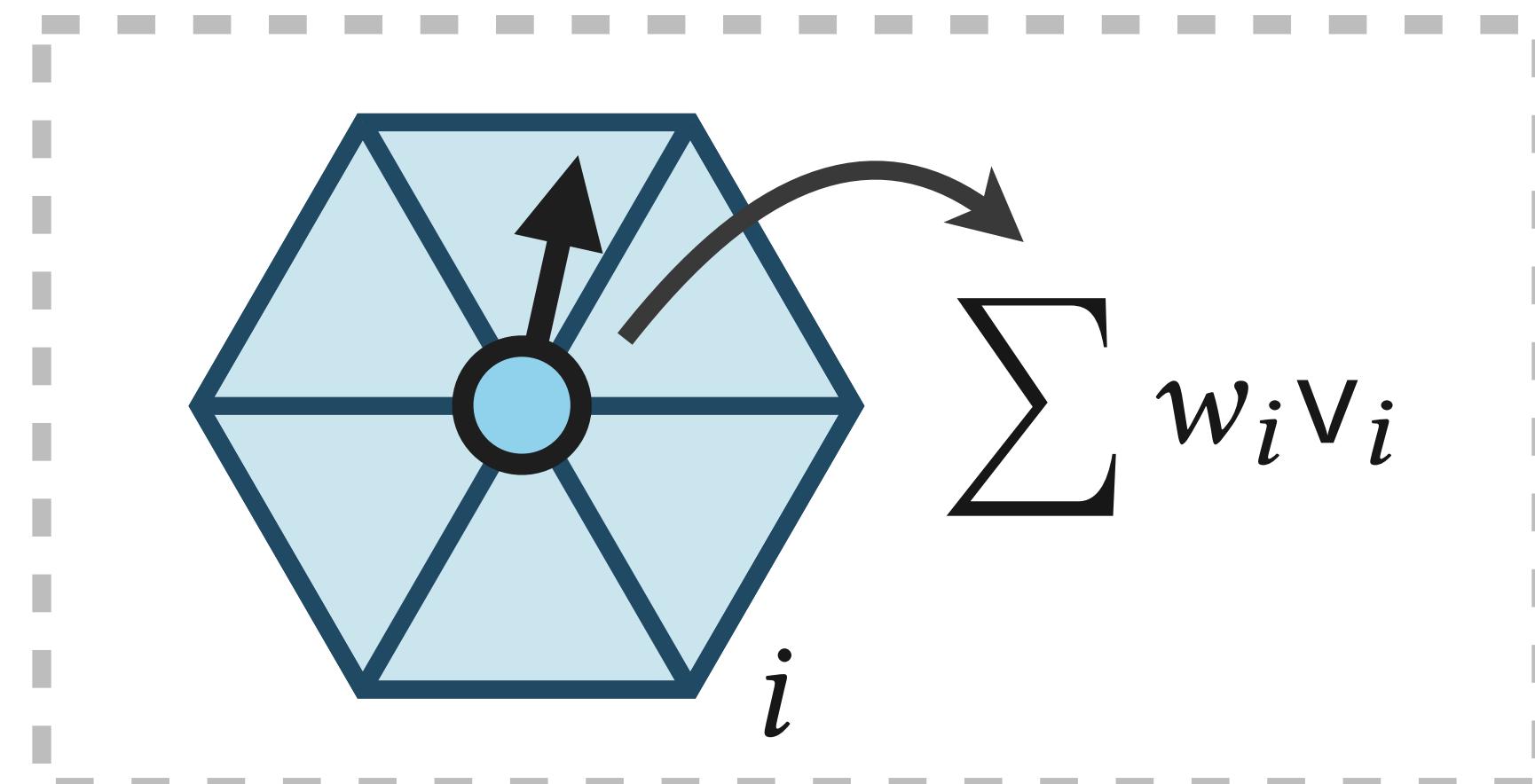
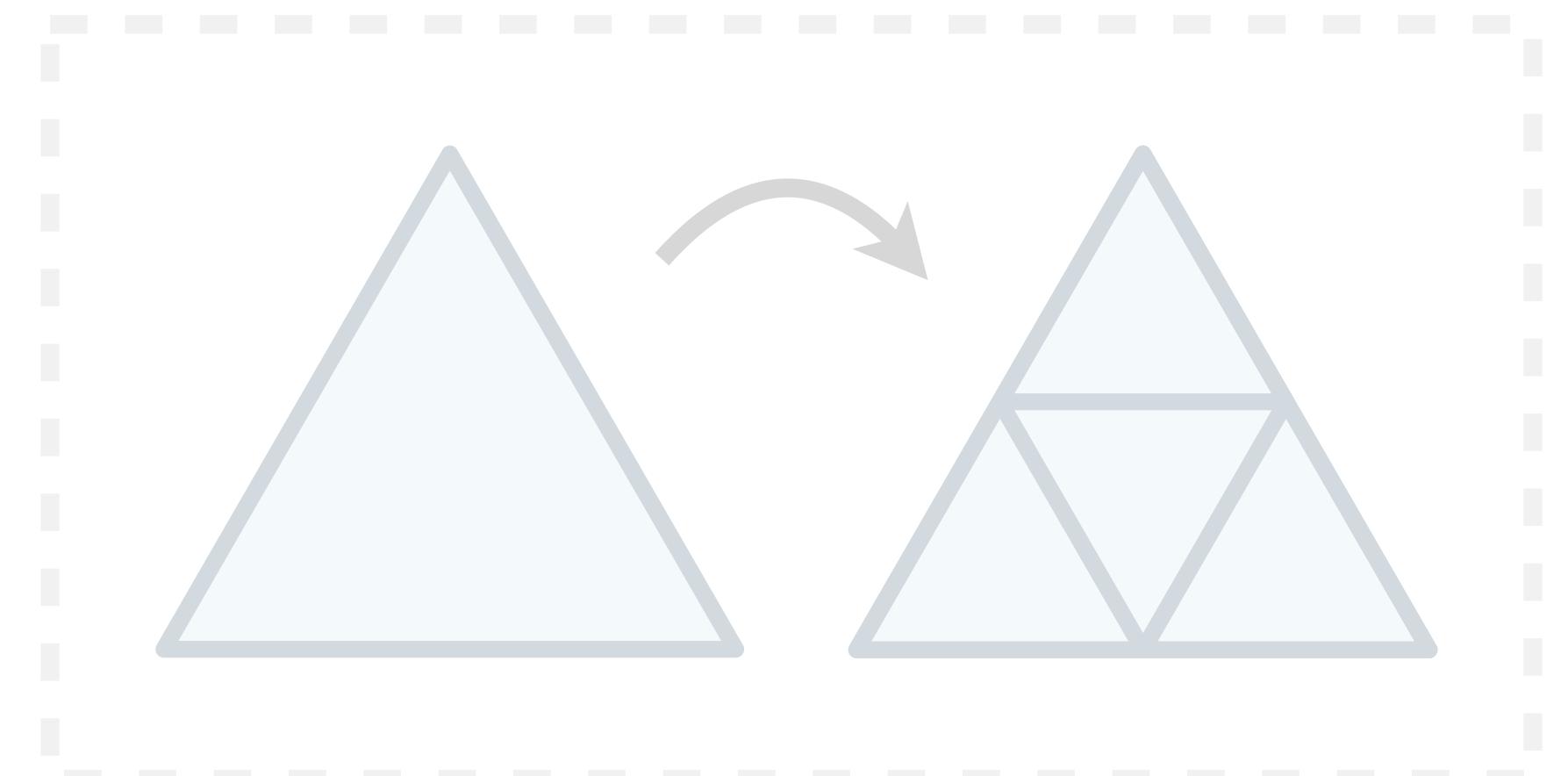
$$y = f_{\theta}(x)$$



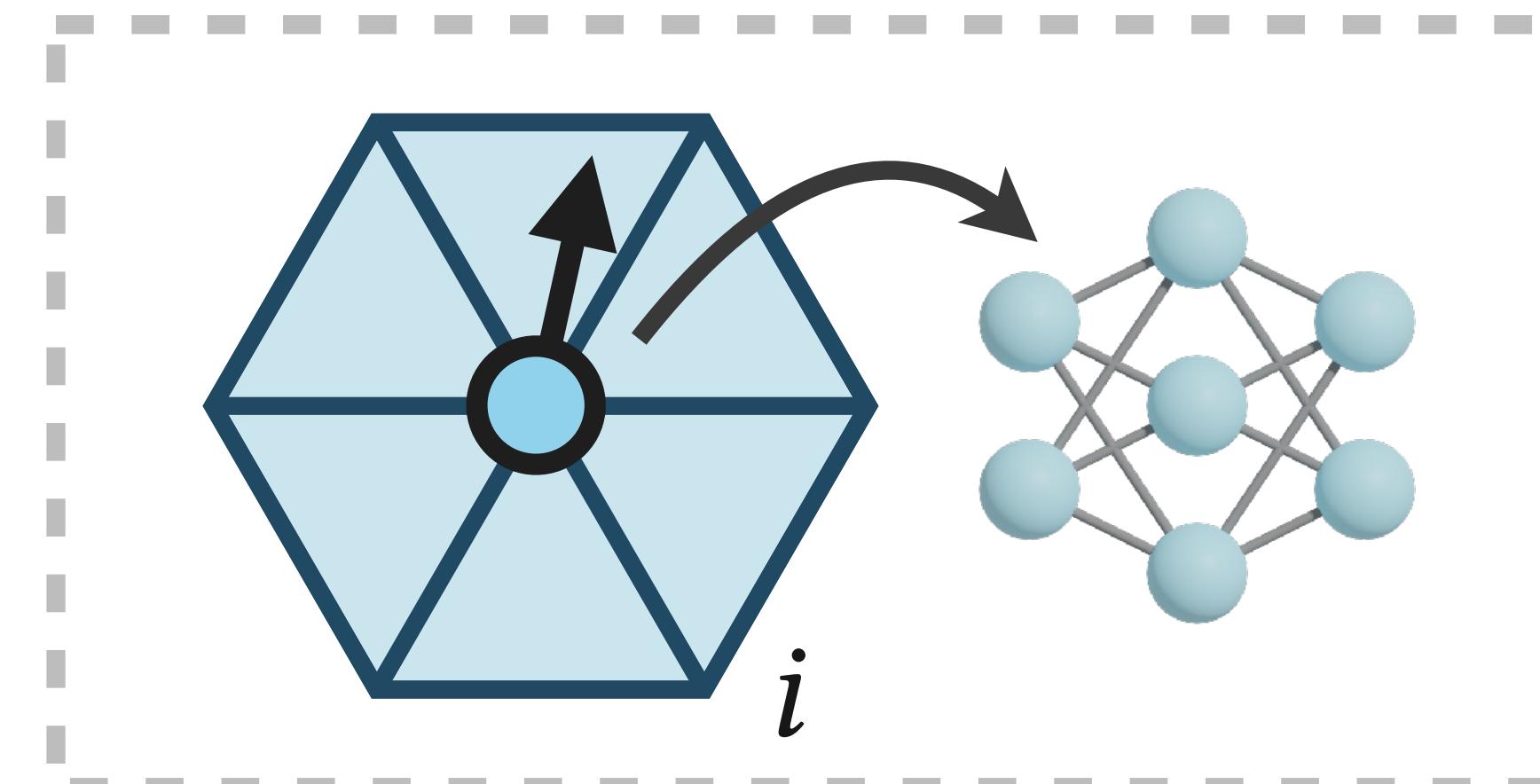
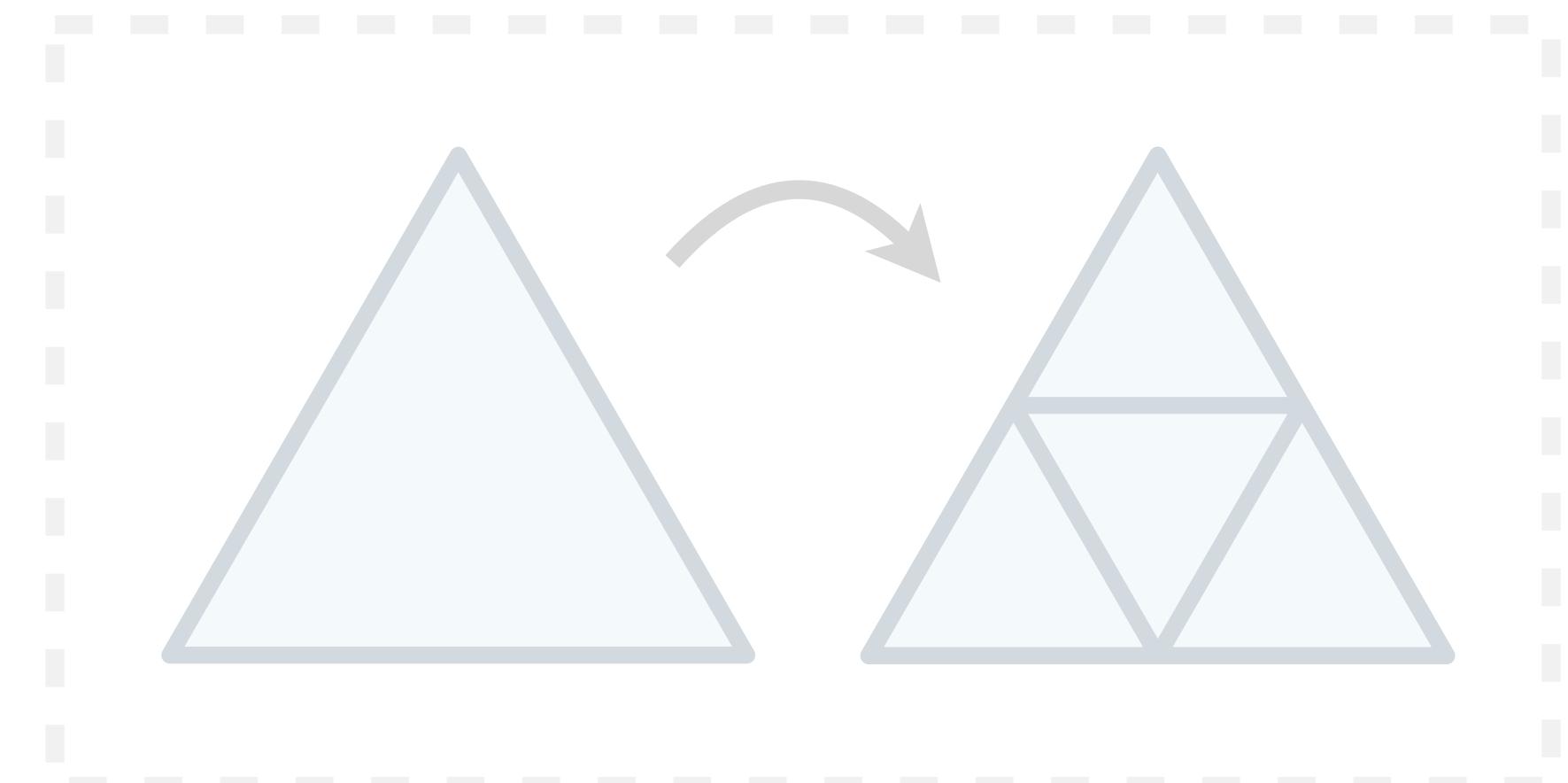
# Still an ongoing research



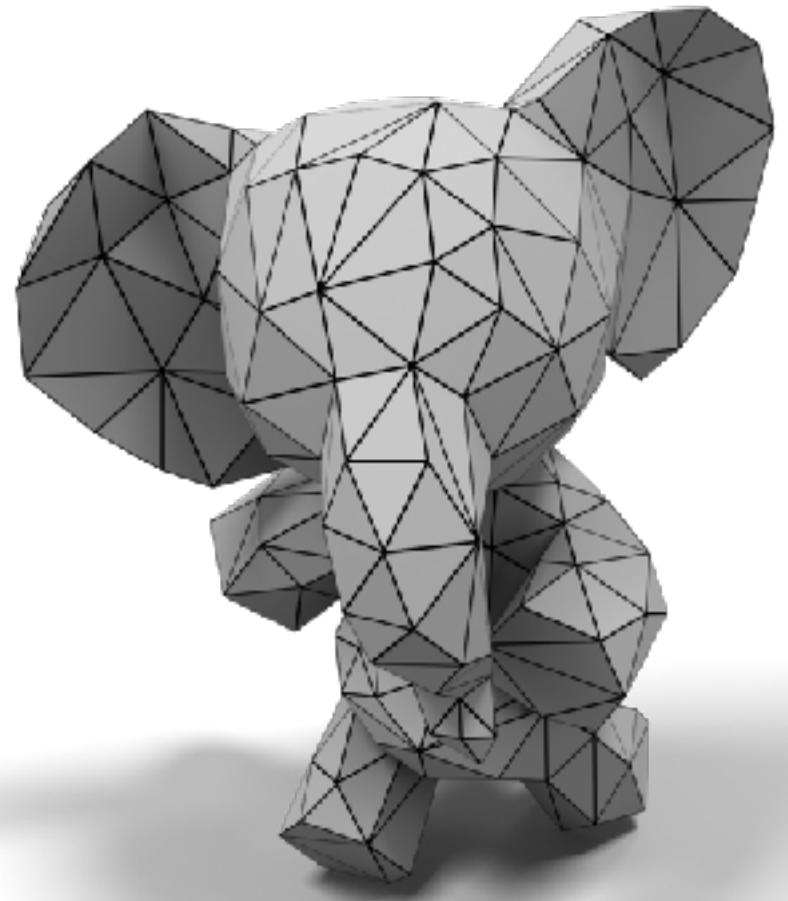
# Where we should put the network?



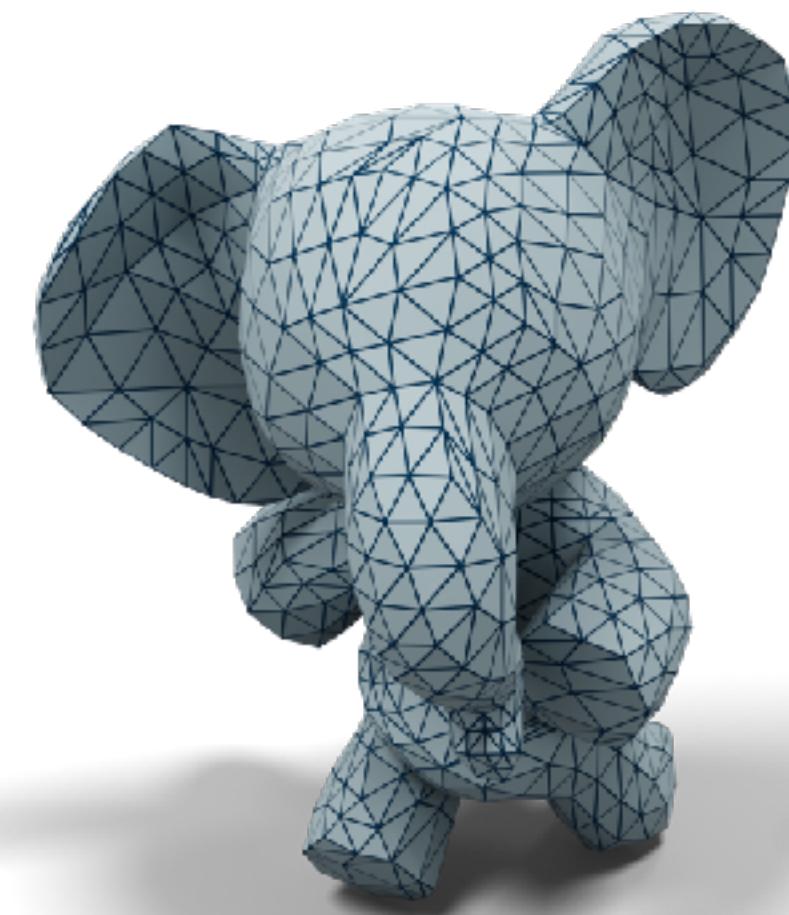
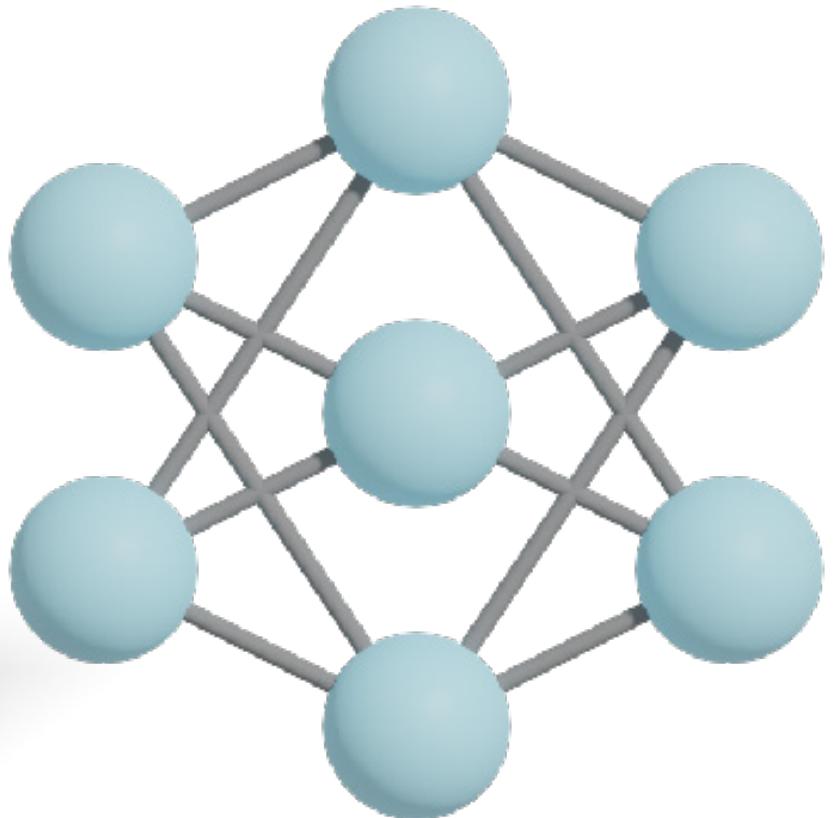
# Where we should put the network?



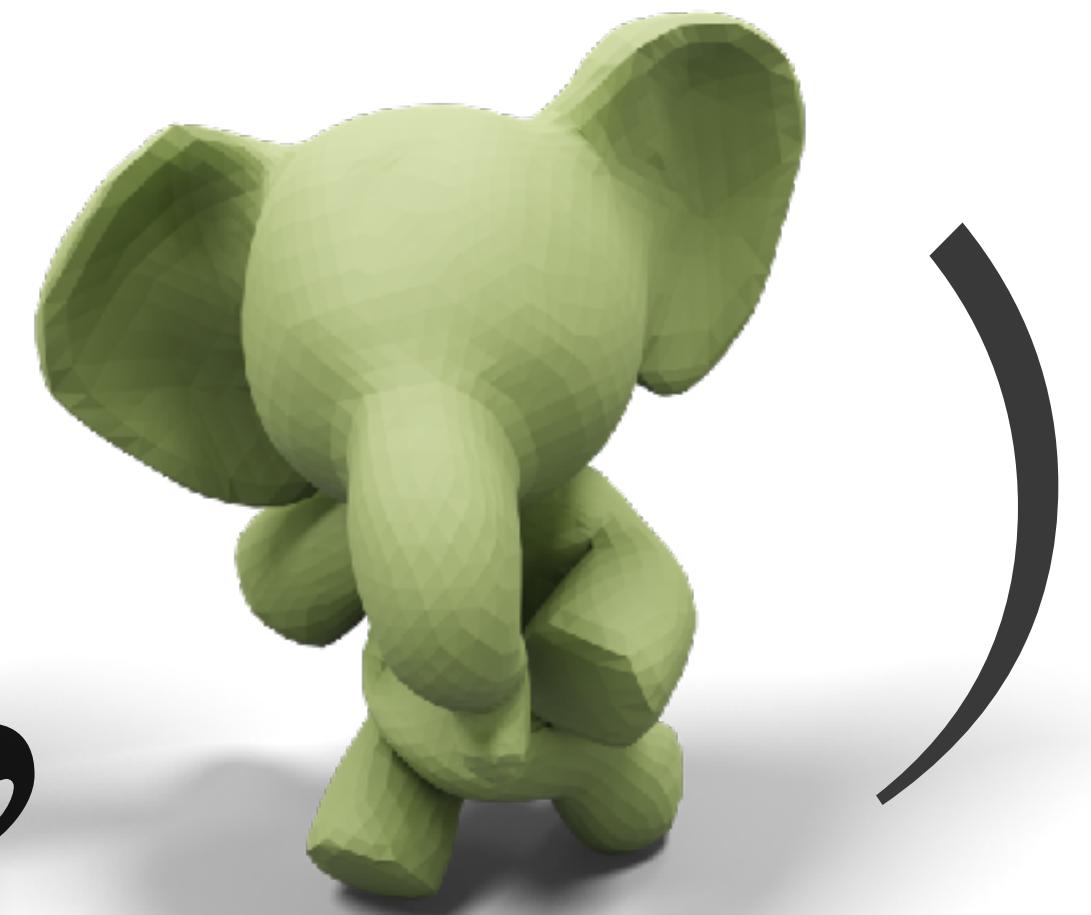
# Neural Subdivision Training



input

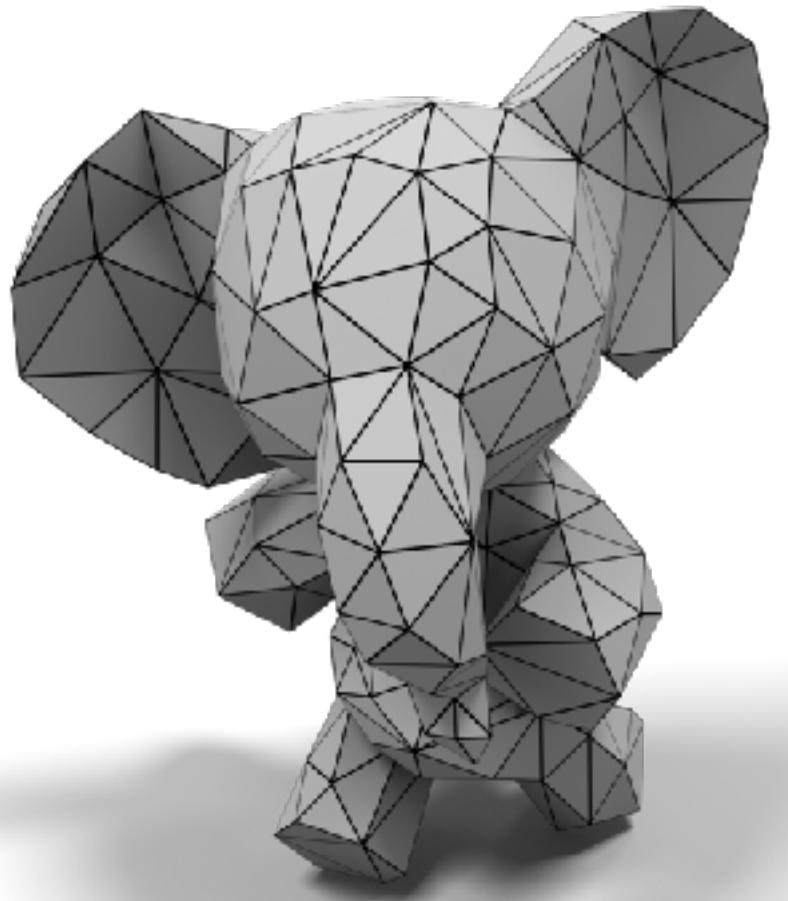


output

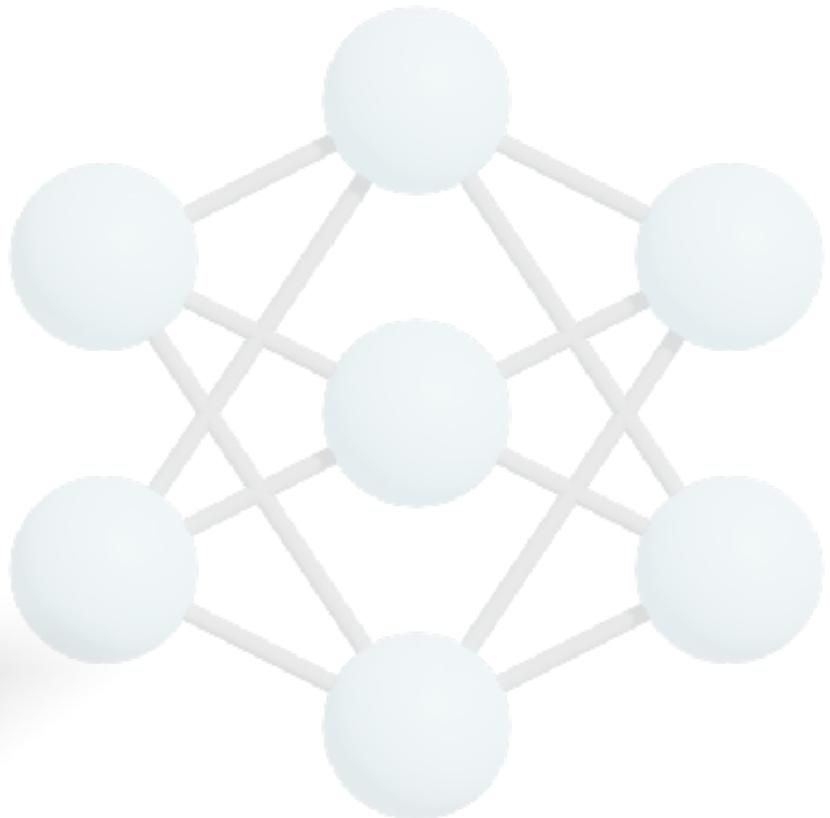


ground truth

# Neural Subdivision Training



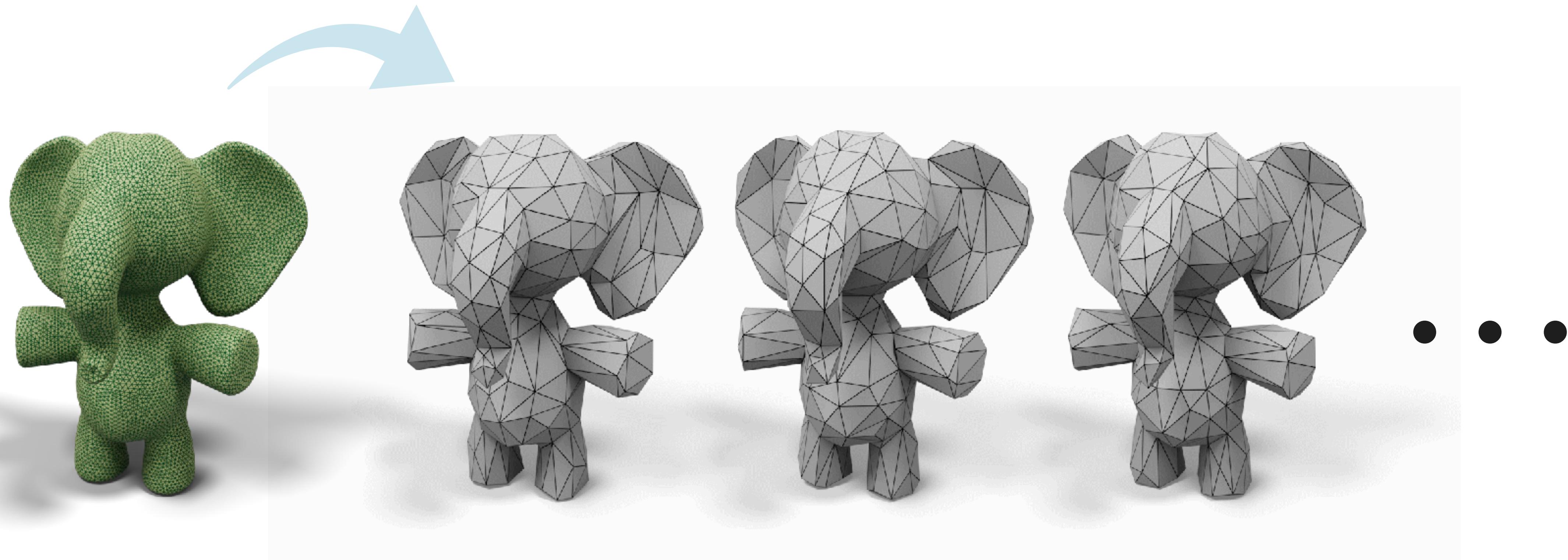
input



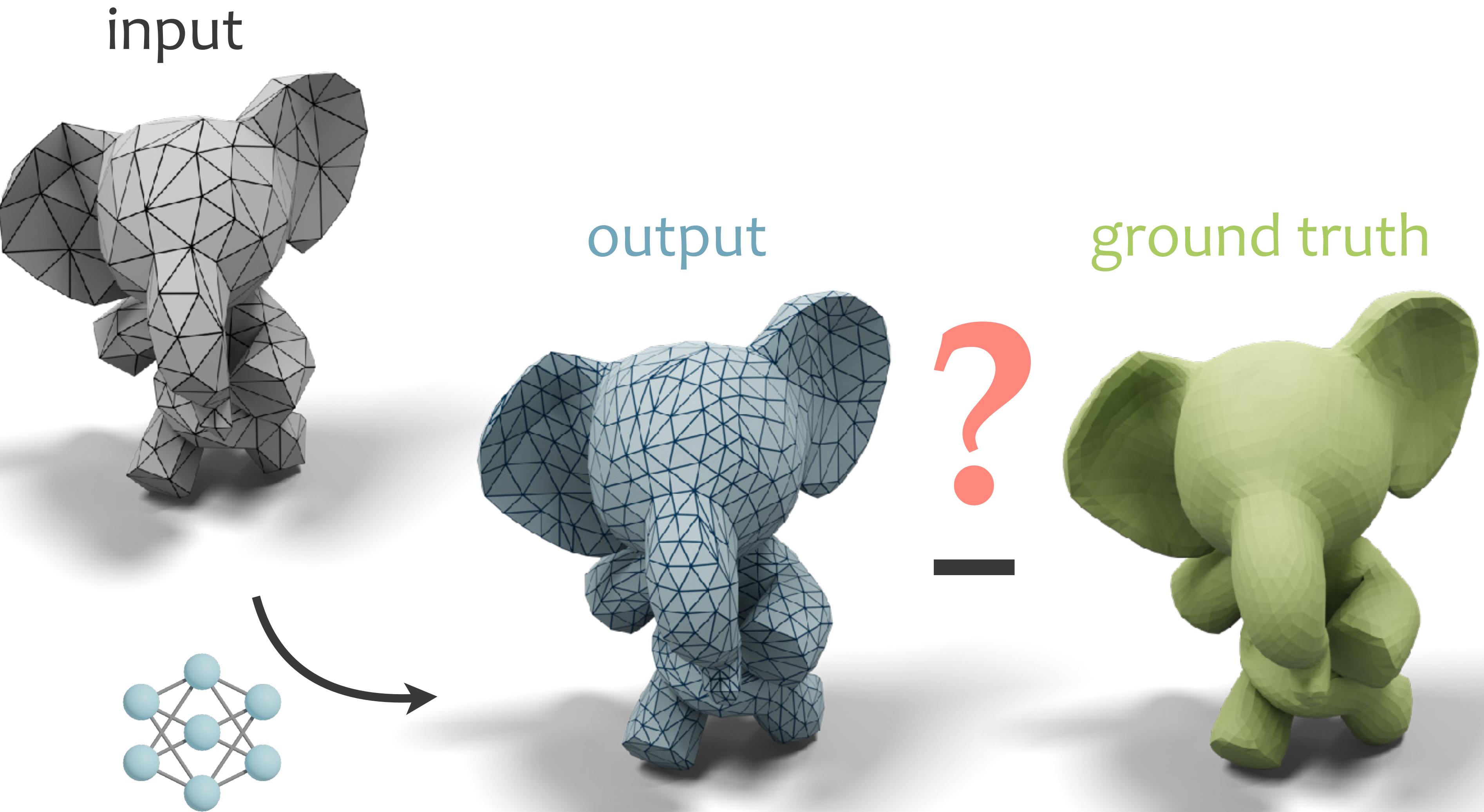
output

ground truth

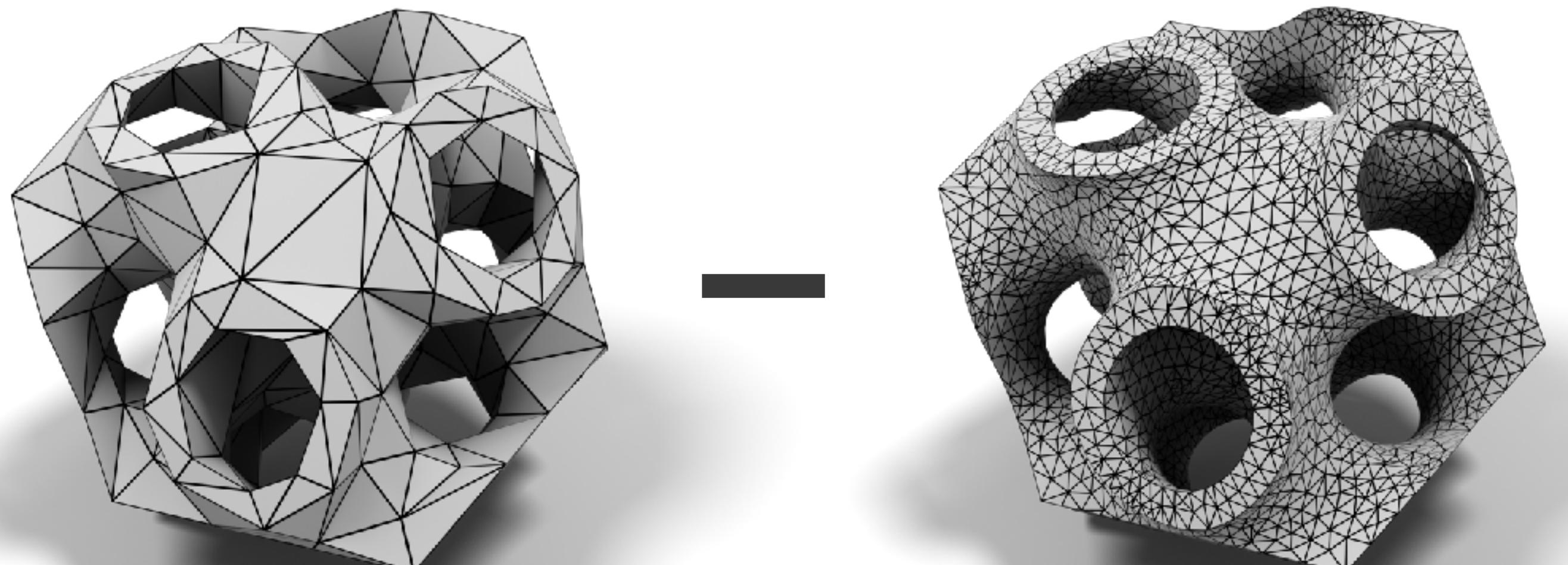
# Training Data



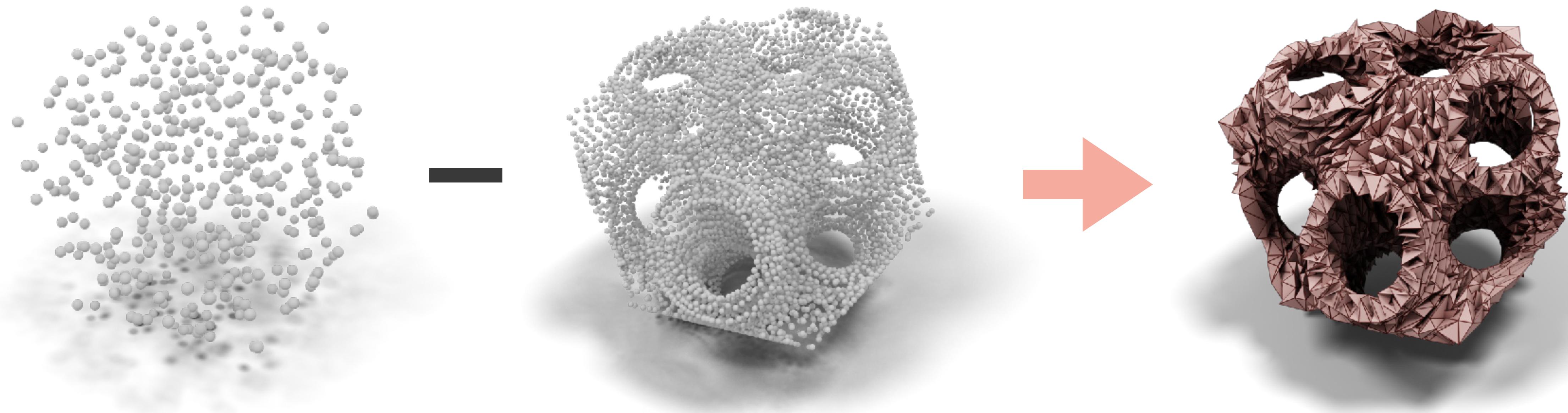
# Neural Subdivision Training



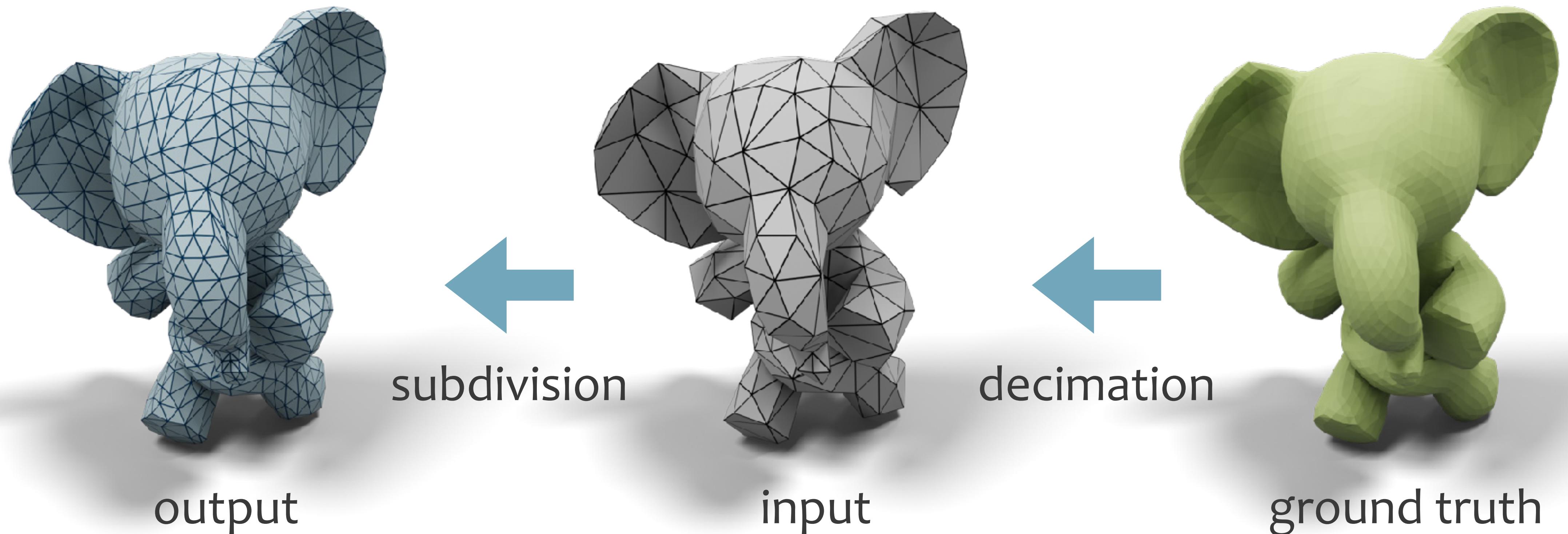
# Chamfer Distance



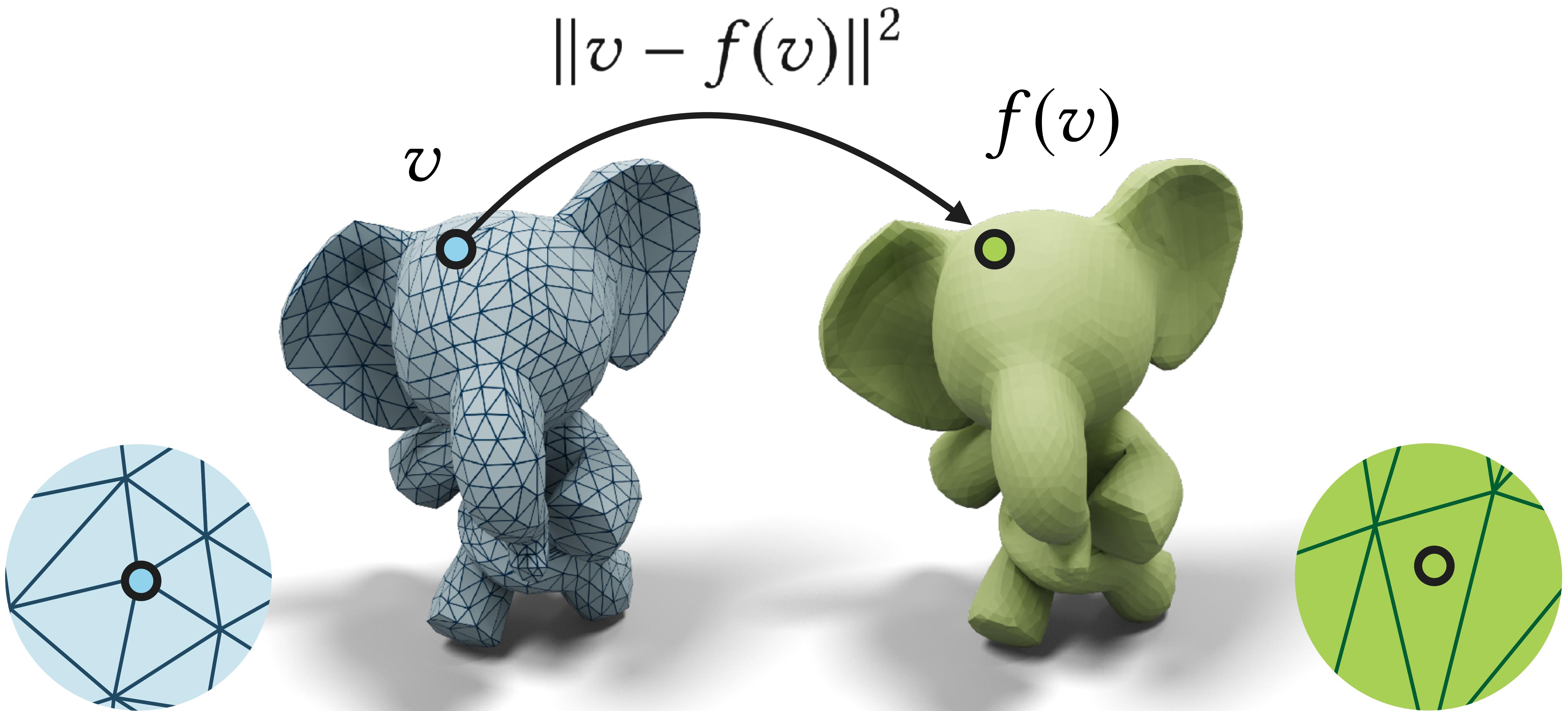
# Chamfer Distance



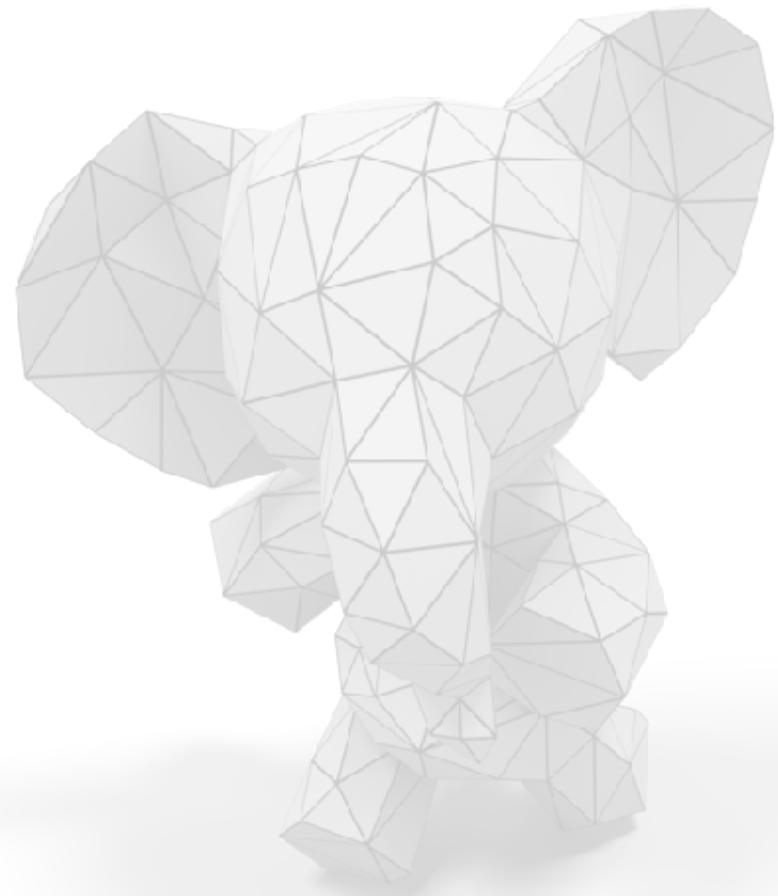
# Leverage the Structure



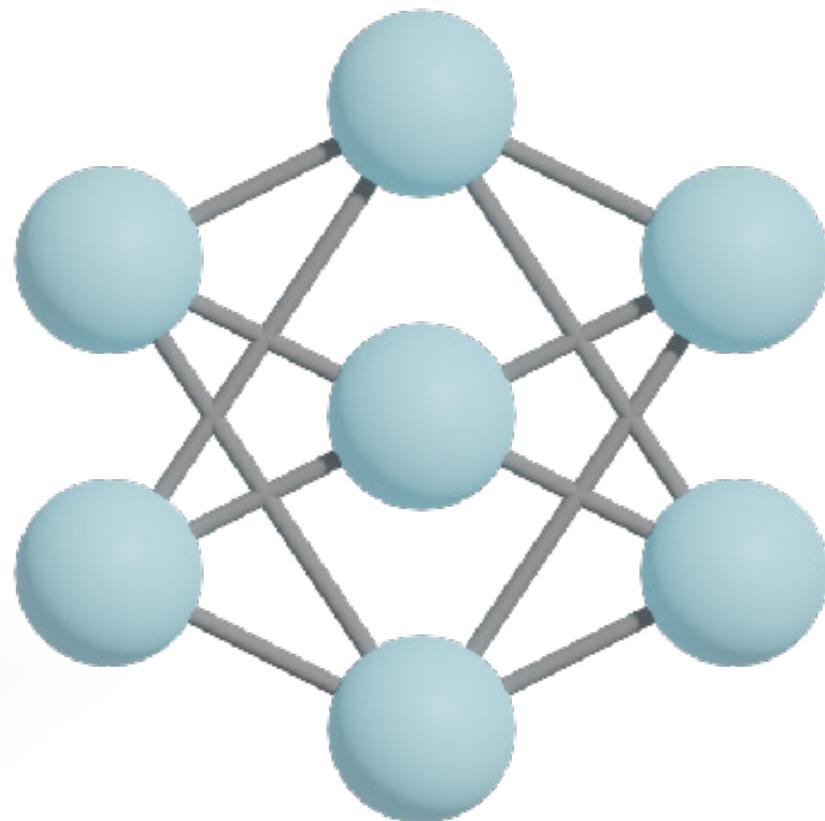
# Bijective Mapping



# Neural Subdivision Training



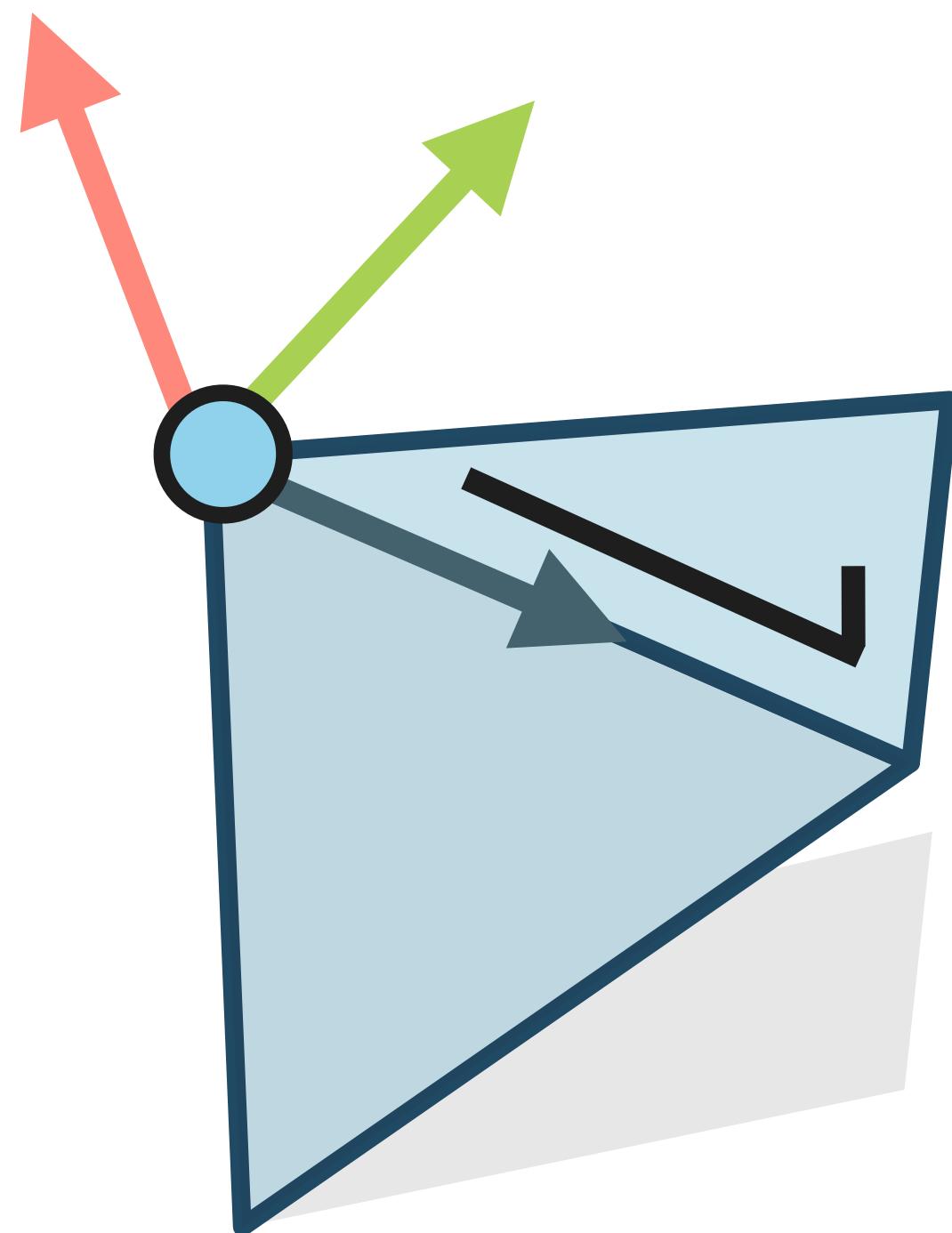
input



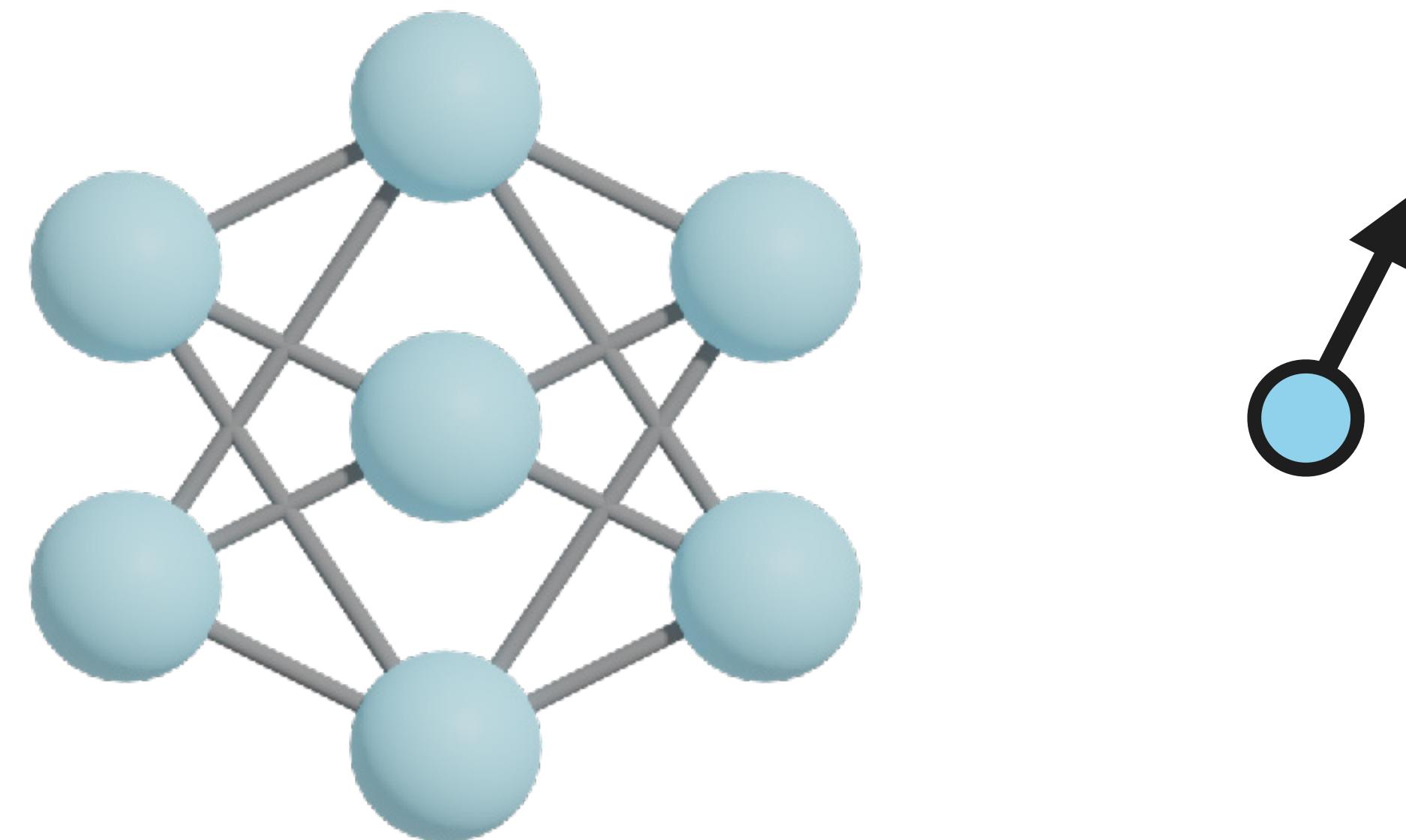
output

ground truth

# Subdivision Network

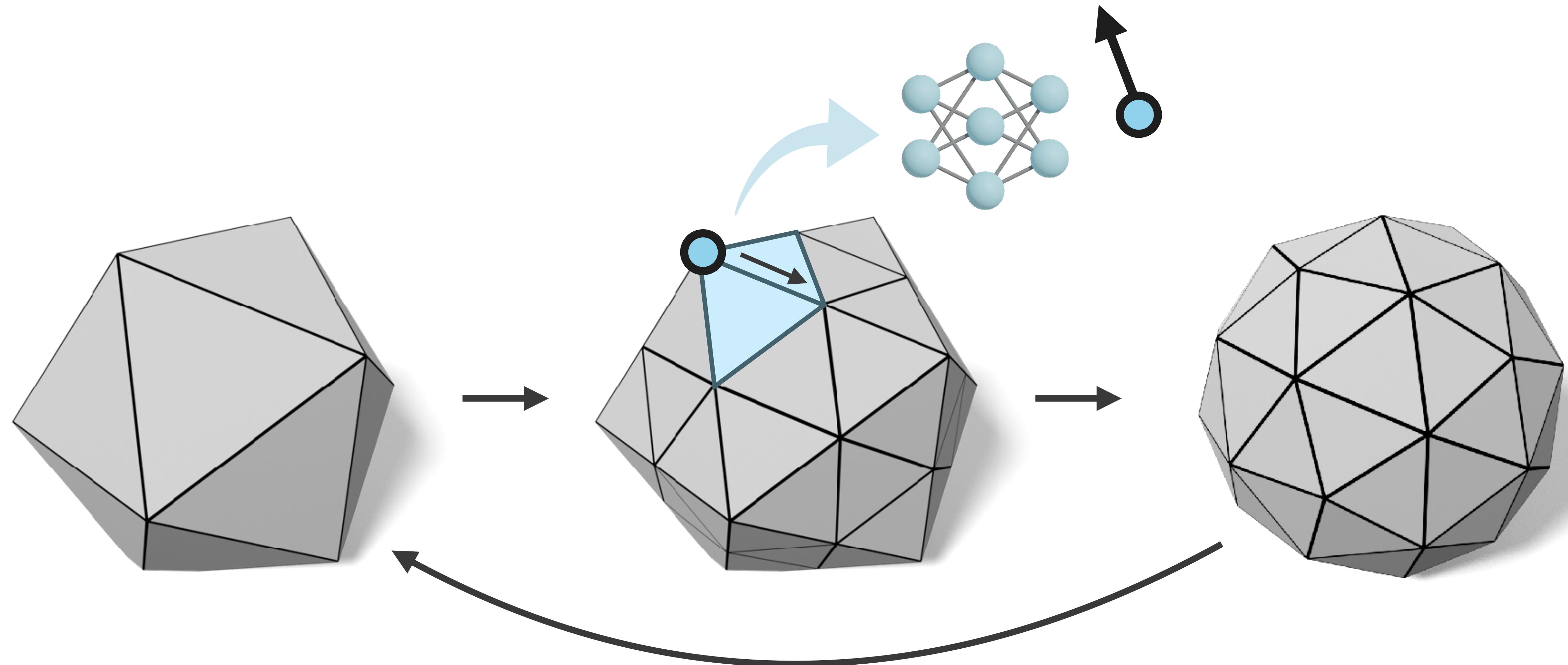


half-flap

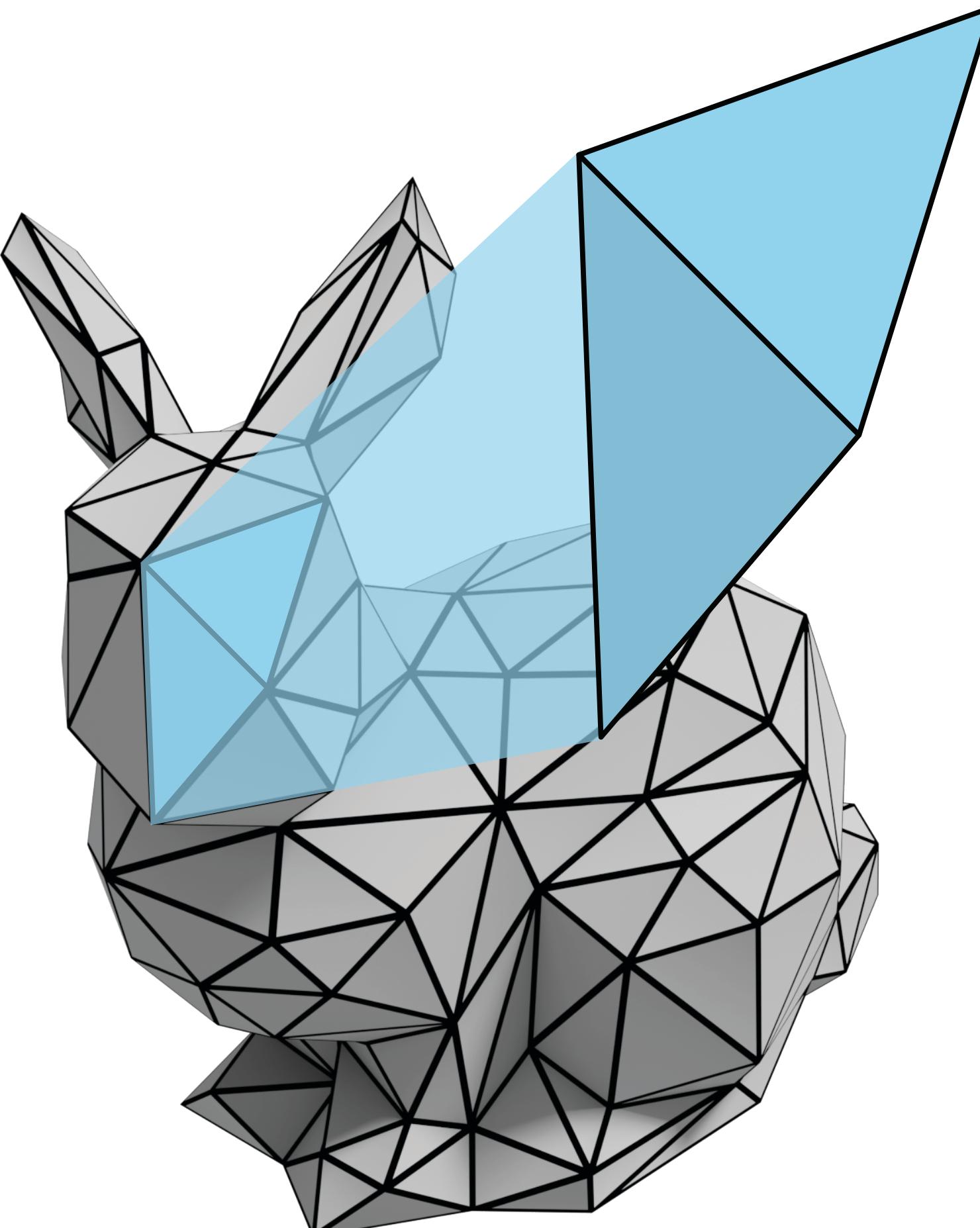


displacement

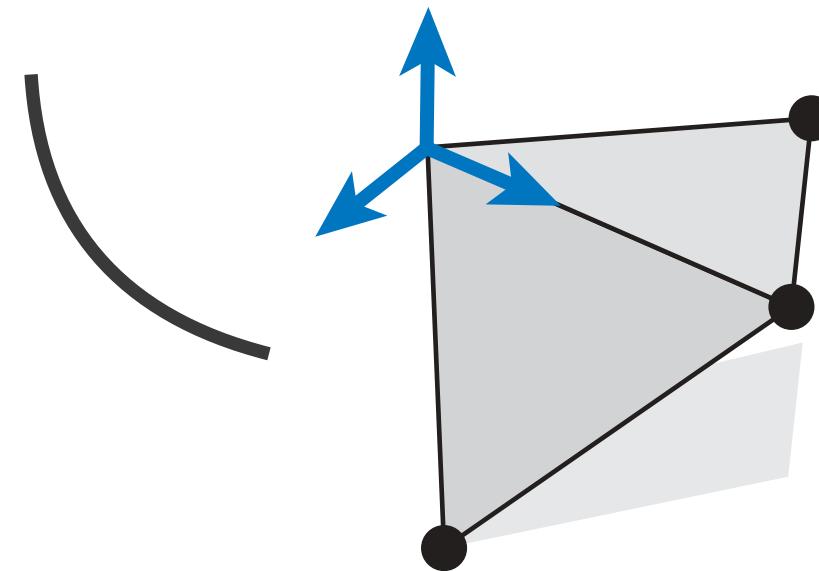
# Subdivision Network



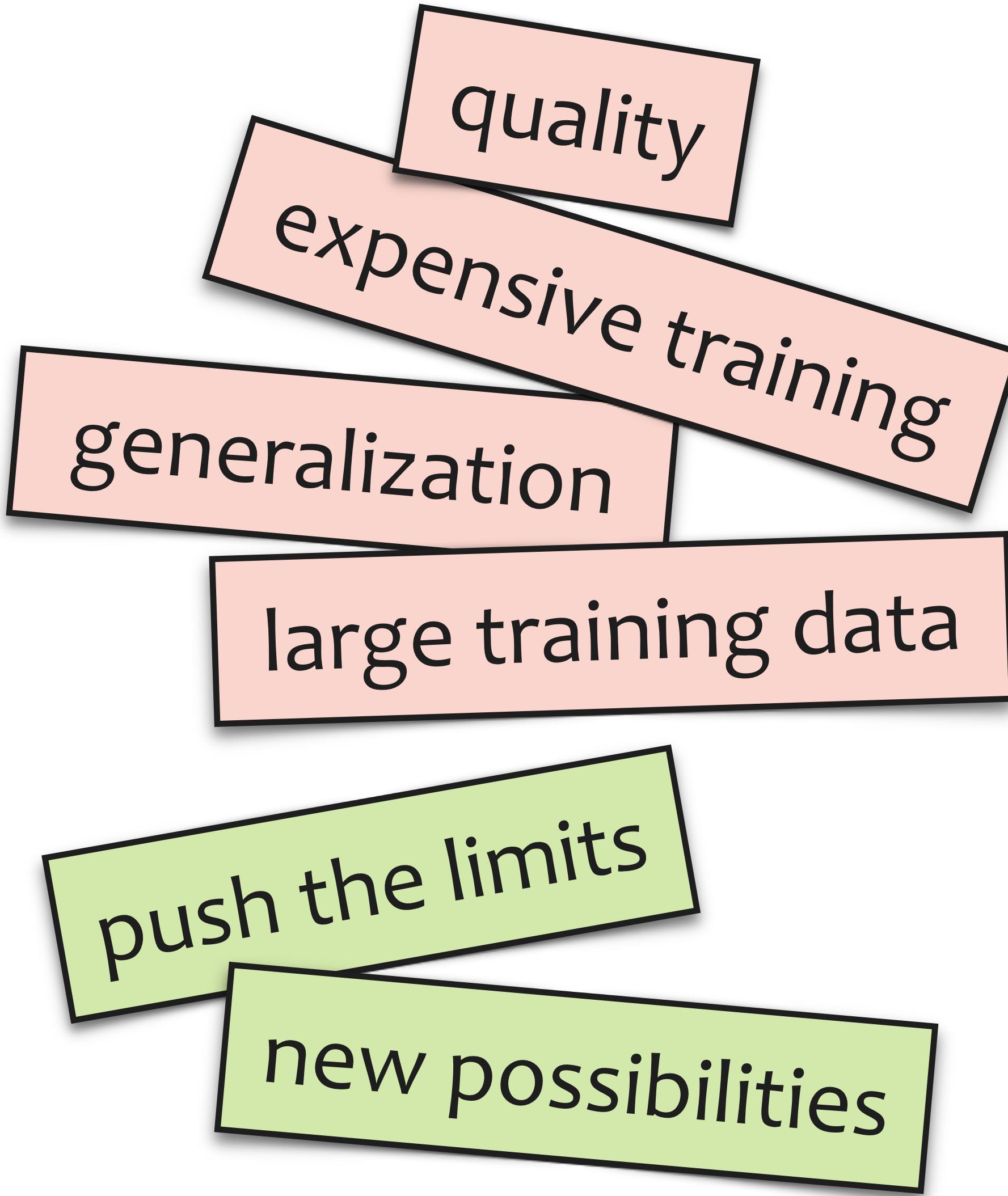
# Key Takeaways



- ~~assume 1070 vertices~~
- ~~assume a specific connectivity~~
- ~~assume a specific ordering~~
- ~~assume a specific orientation~~



# Alleviate limitations



# Alleviate limitations



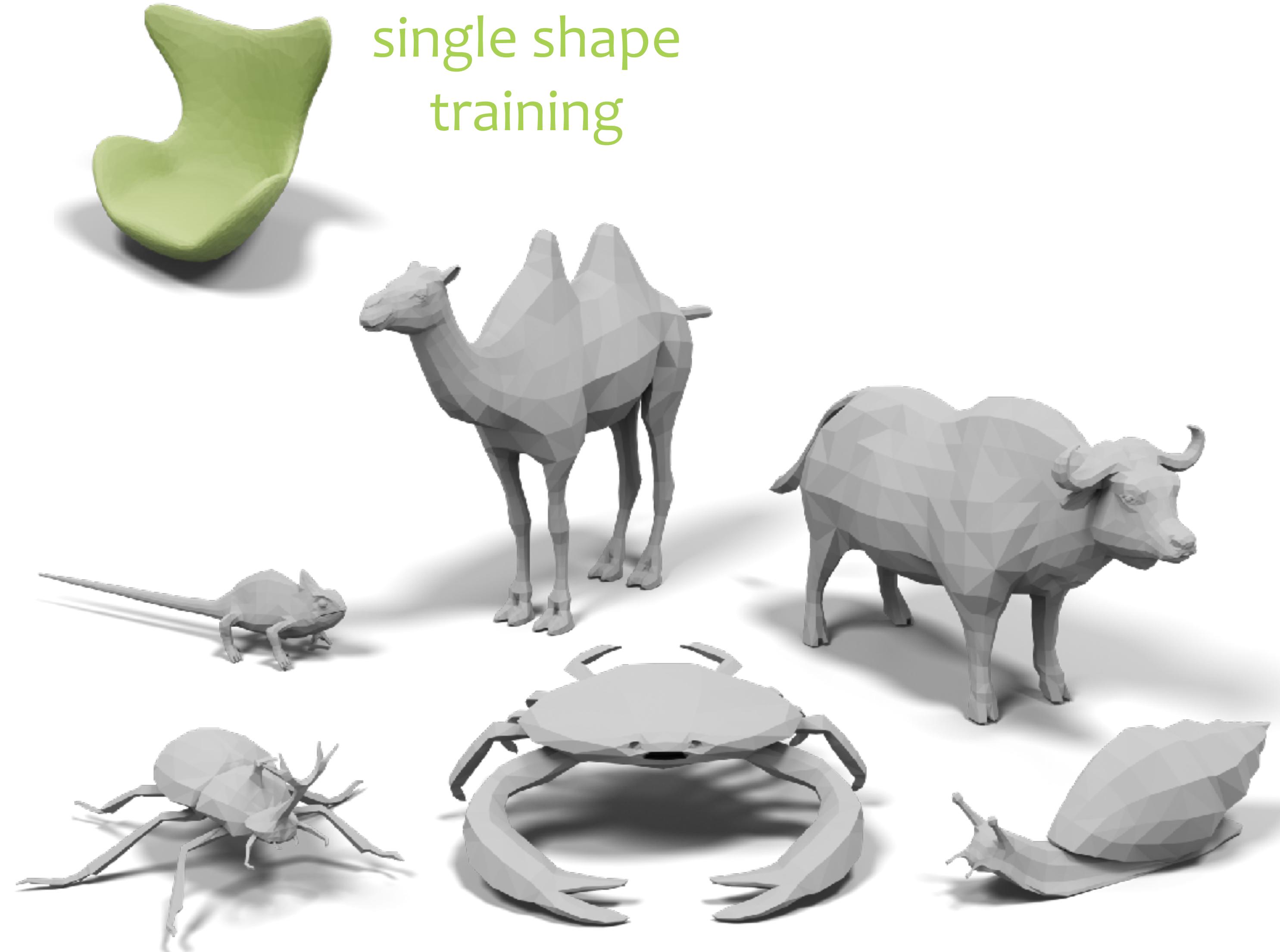
single shape  
training

# Alleviate limitations

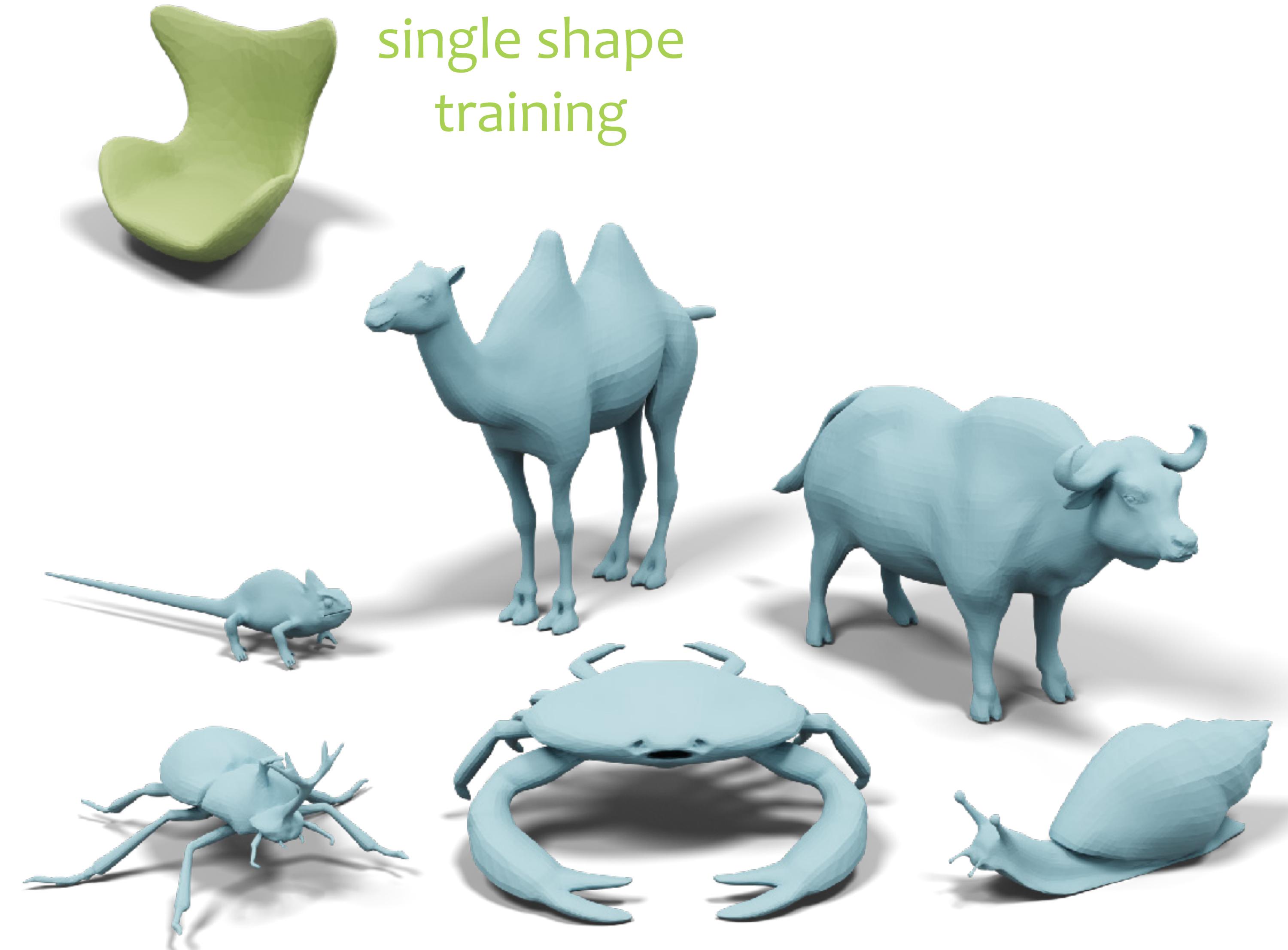


single shape  
training

# Alleviate limitations



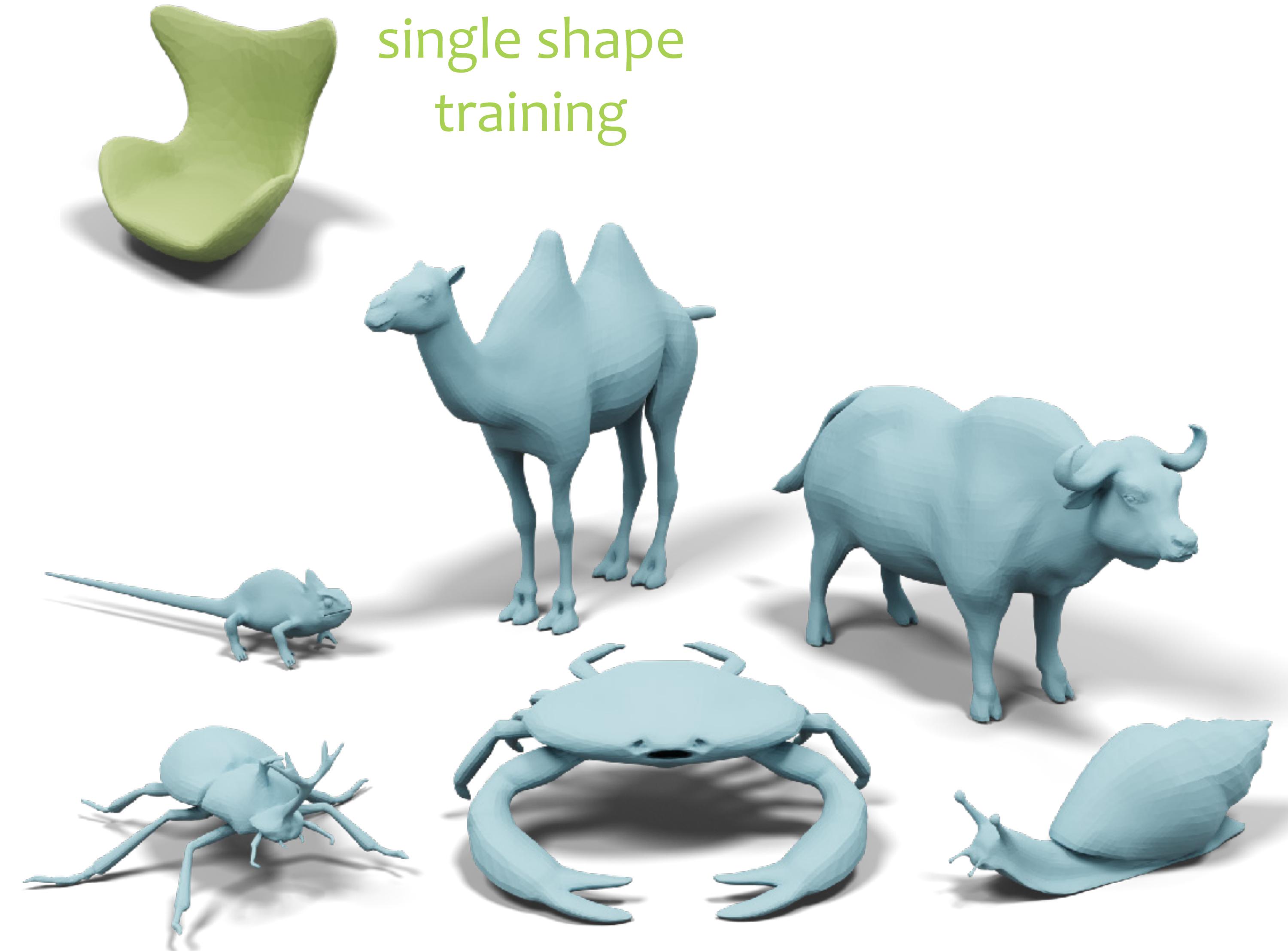
# Alleviate limitations



# Alleviate limitations

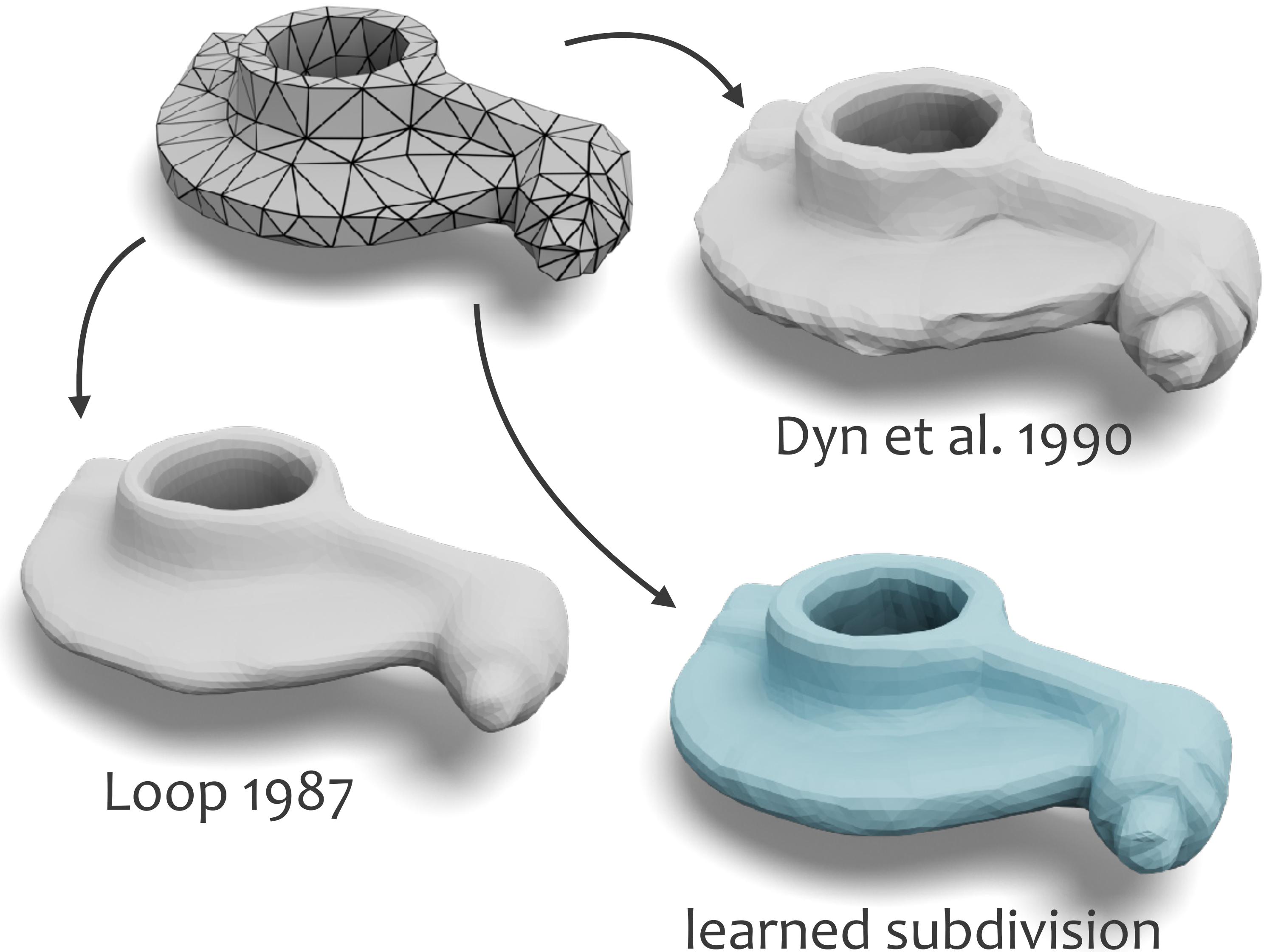
quality  
expensive training  
generalization  
large training data

push the limits  
new possibilities



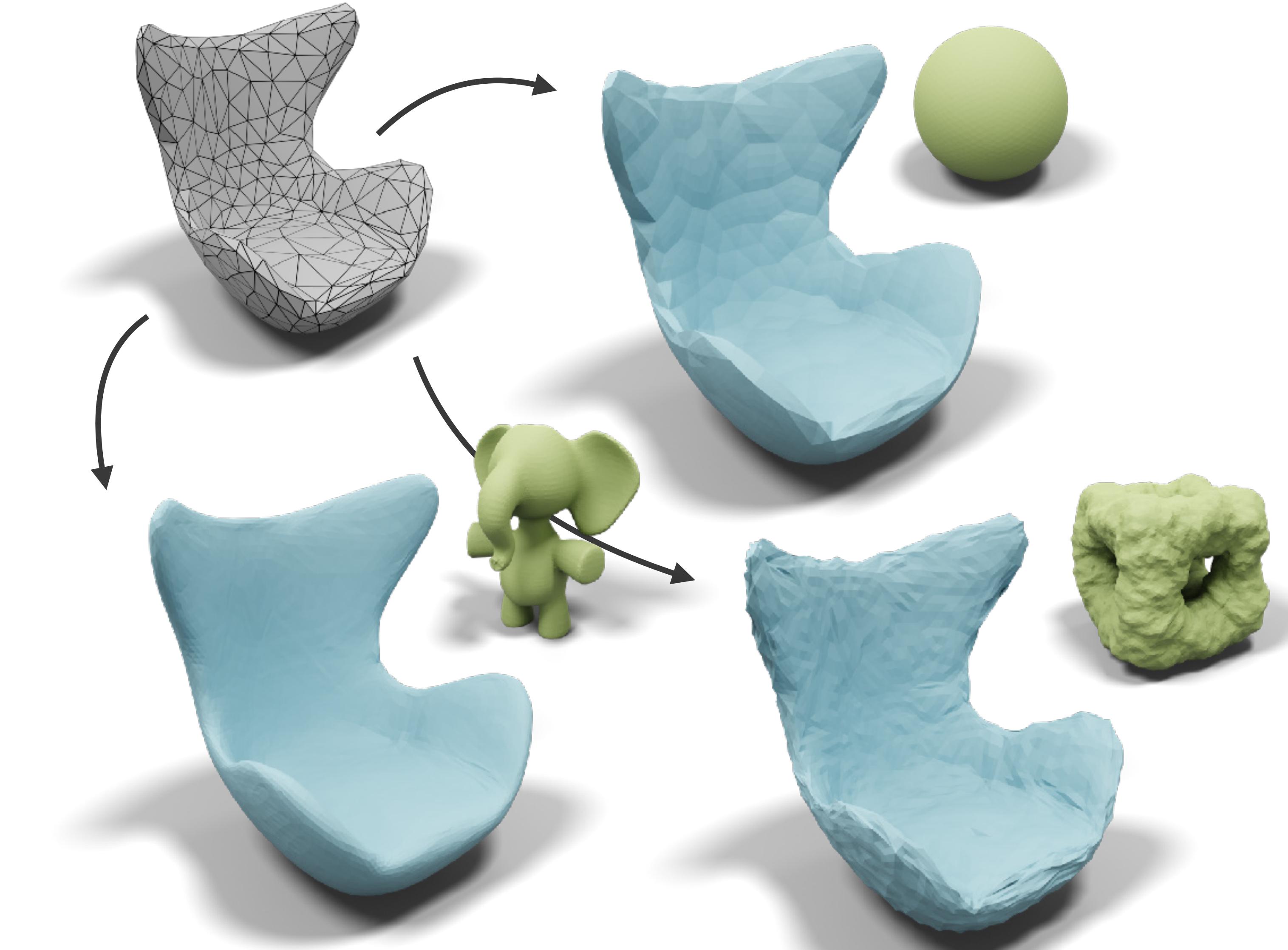
# Enjoy Advantages

quality  
expensive training  
generalization  
large training data  
push the limits  
new possibilities

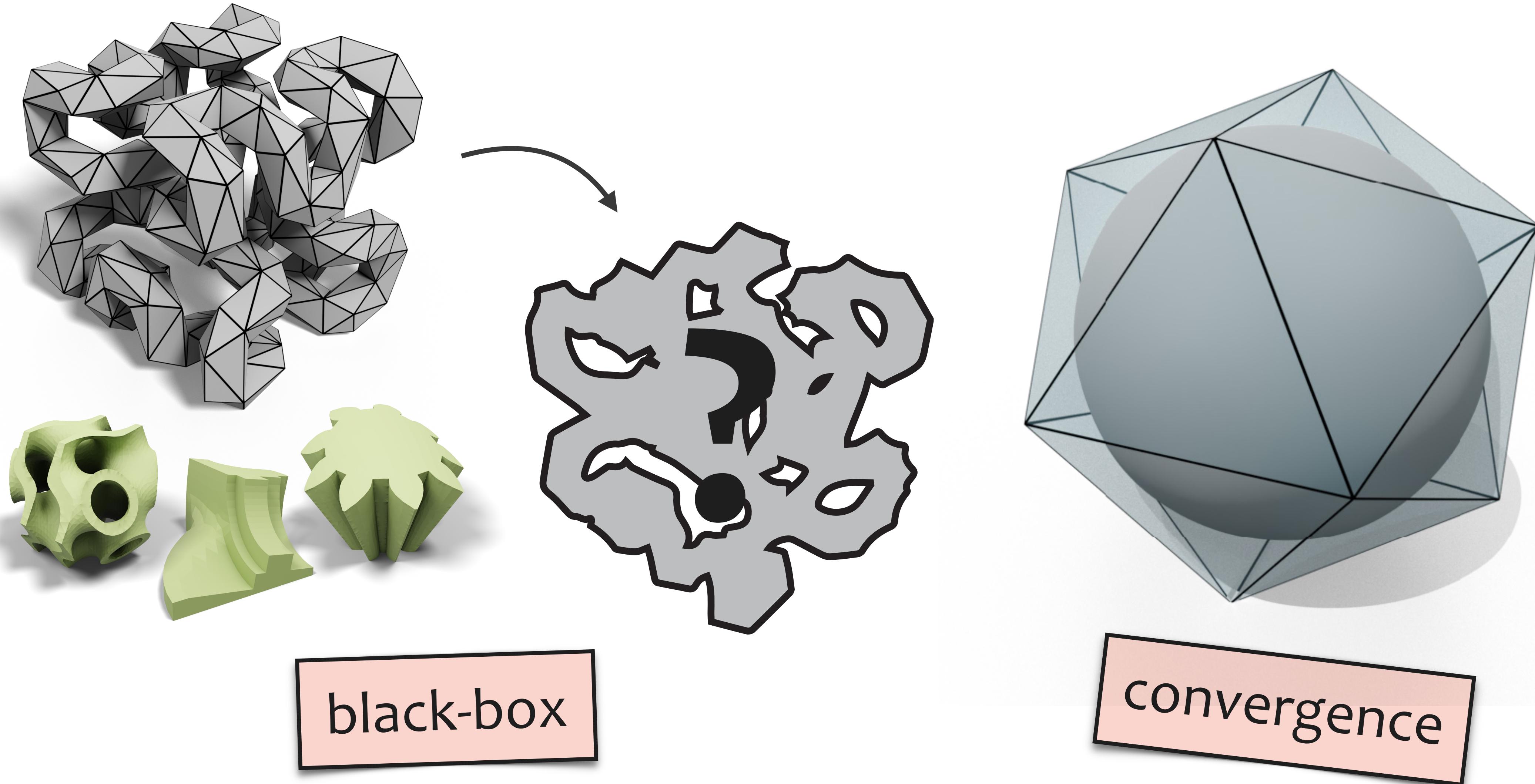


# Enjoy Advantages

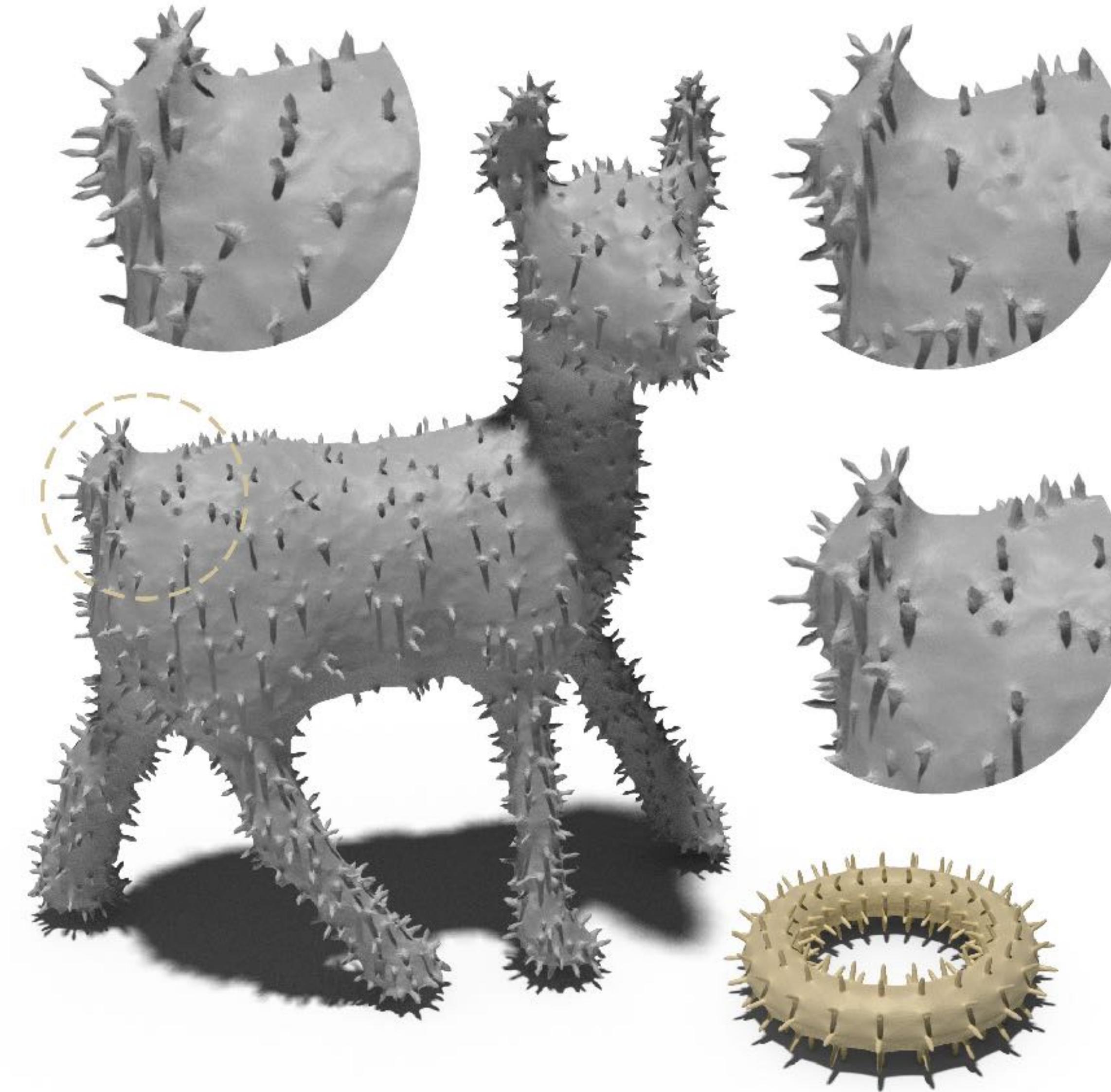
quality  
expensive training  
generalization  
large training data  
push the limits  
new possibilities



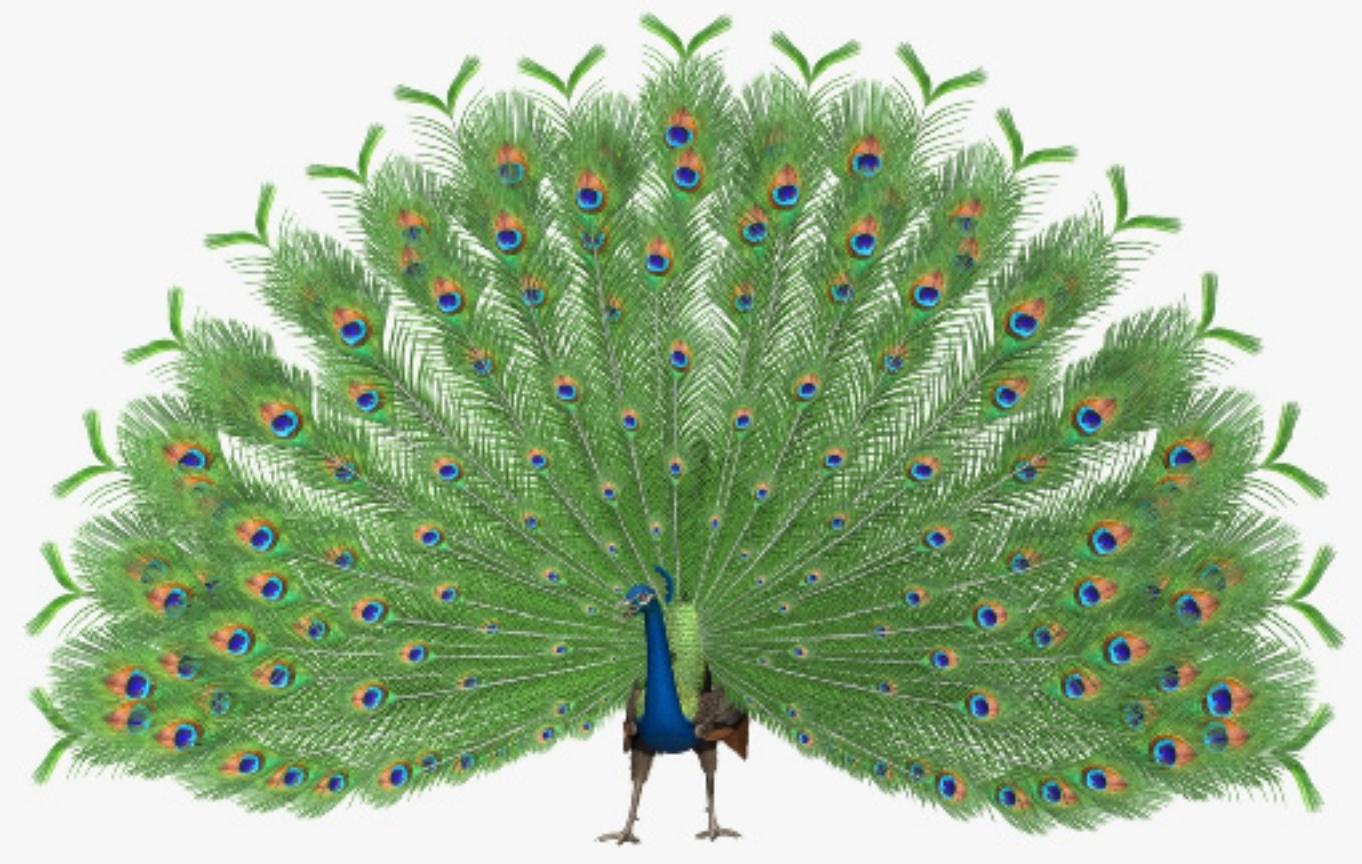
# Ongoing Research



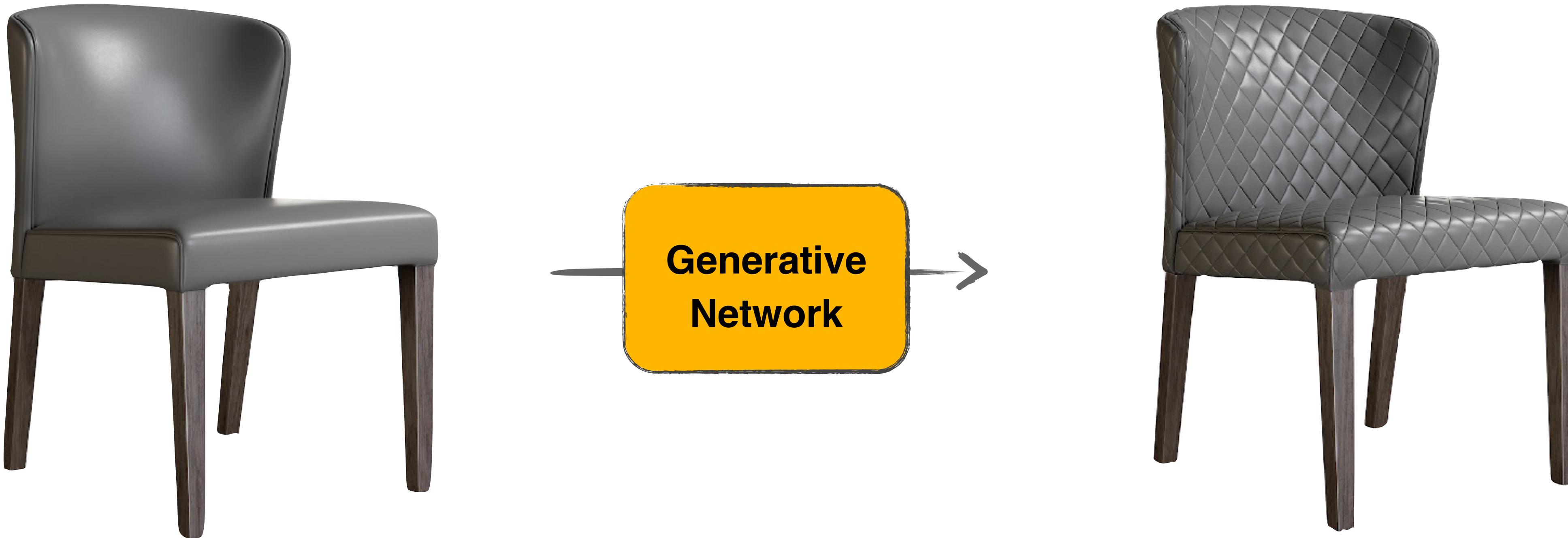
# Deep Geometric Texture Synthesis



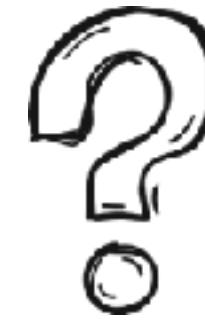
# Geometric Textures



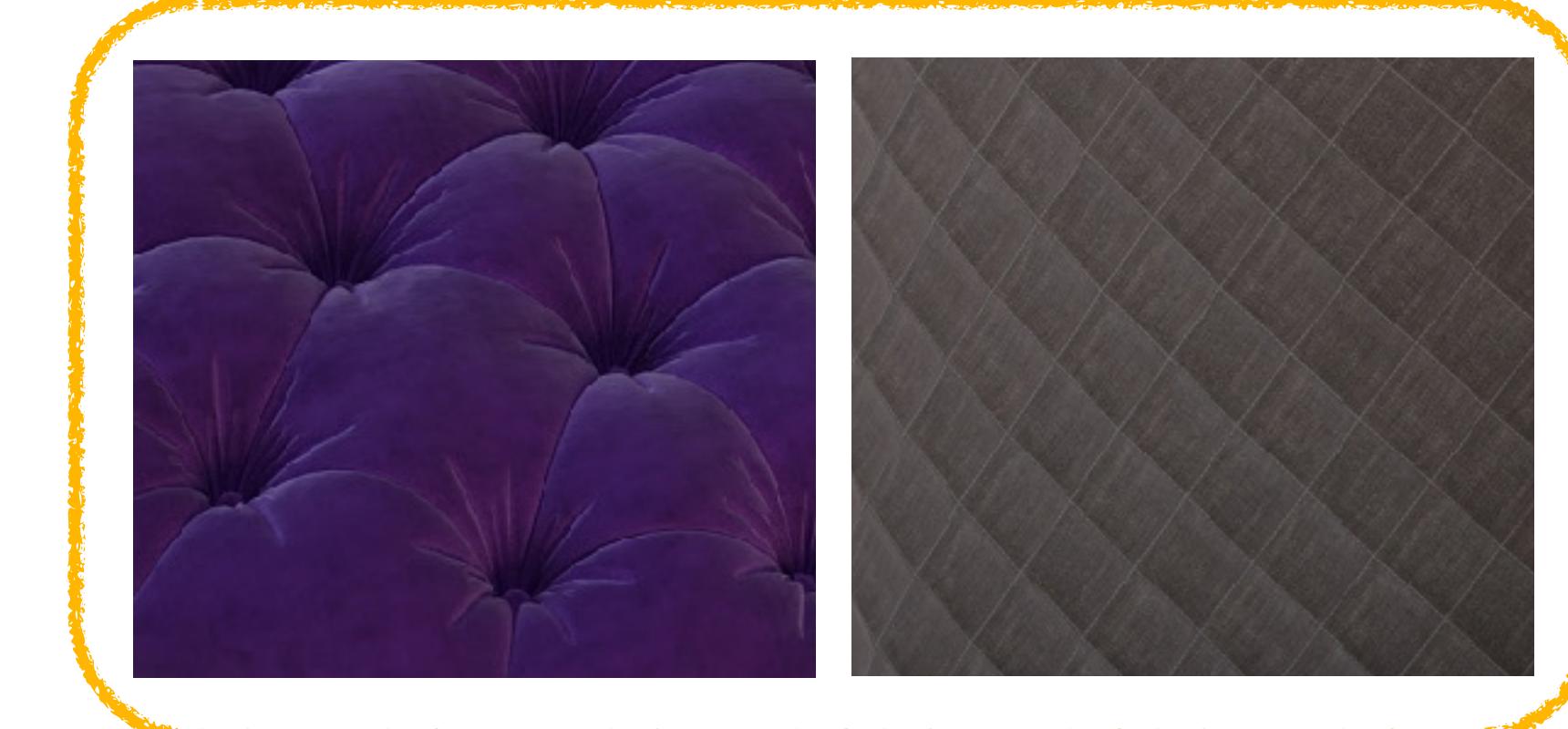
# Objective: Generative Texture Model



# External Dataset



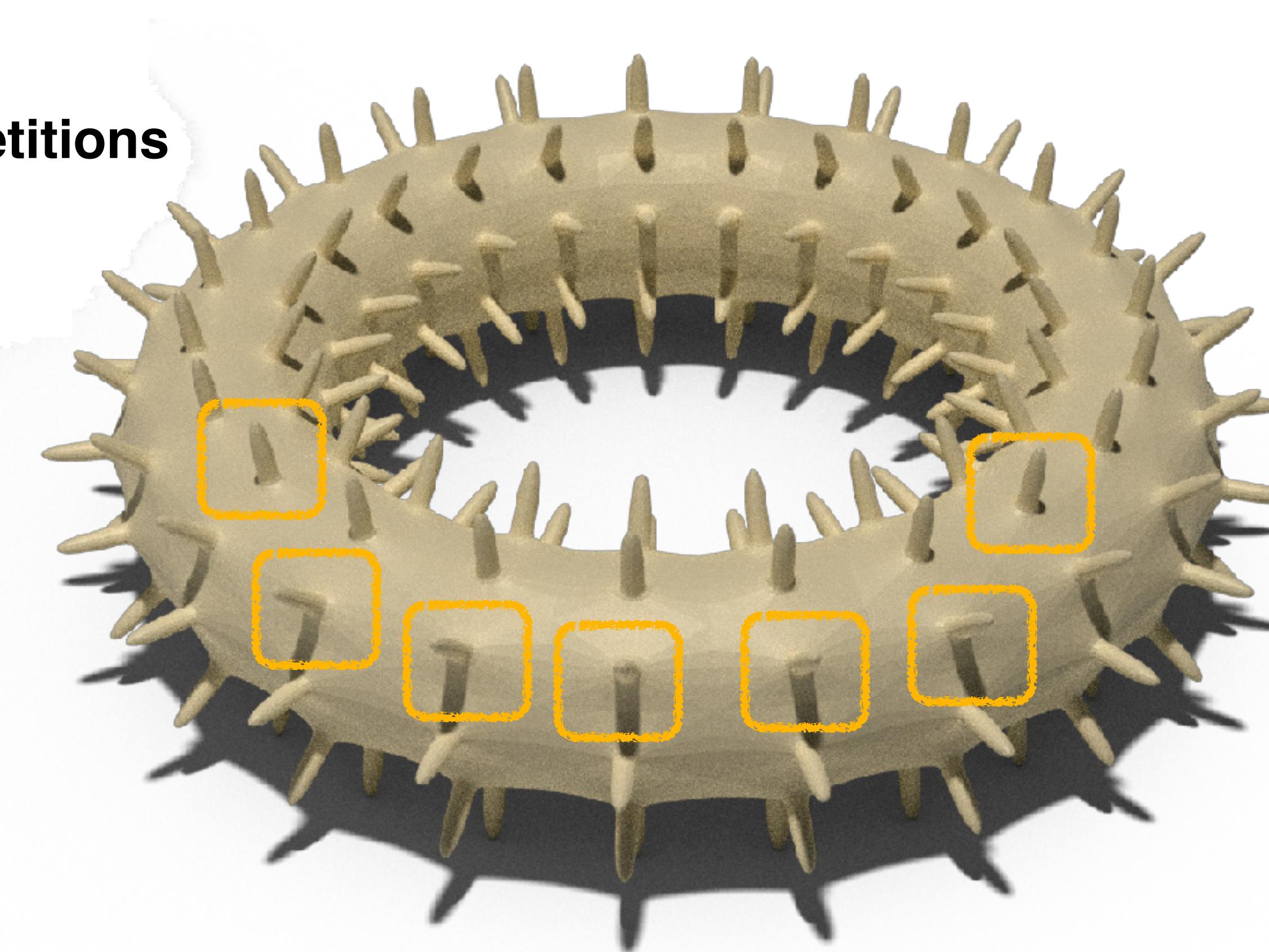
**Difficult to obtain collections  
with same geometric textures**



# Learn from a Single Shape

Patches are training data

Textures contain self-repetitions

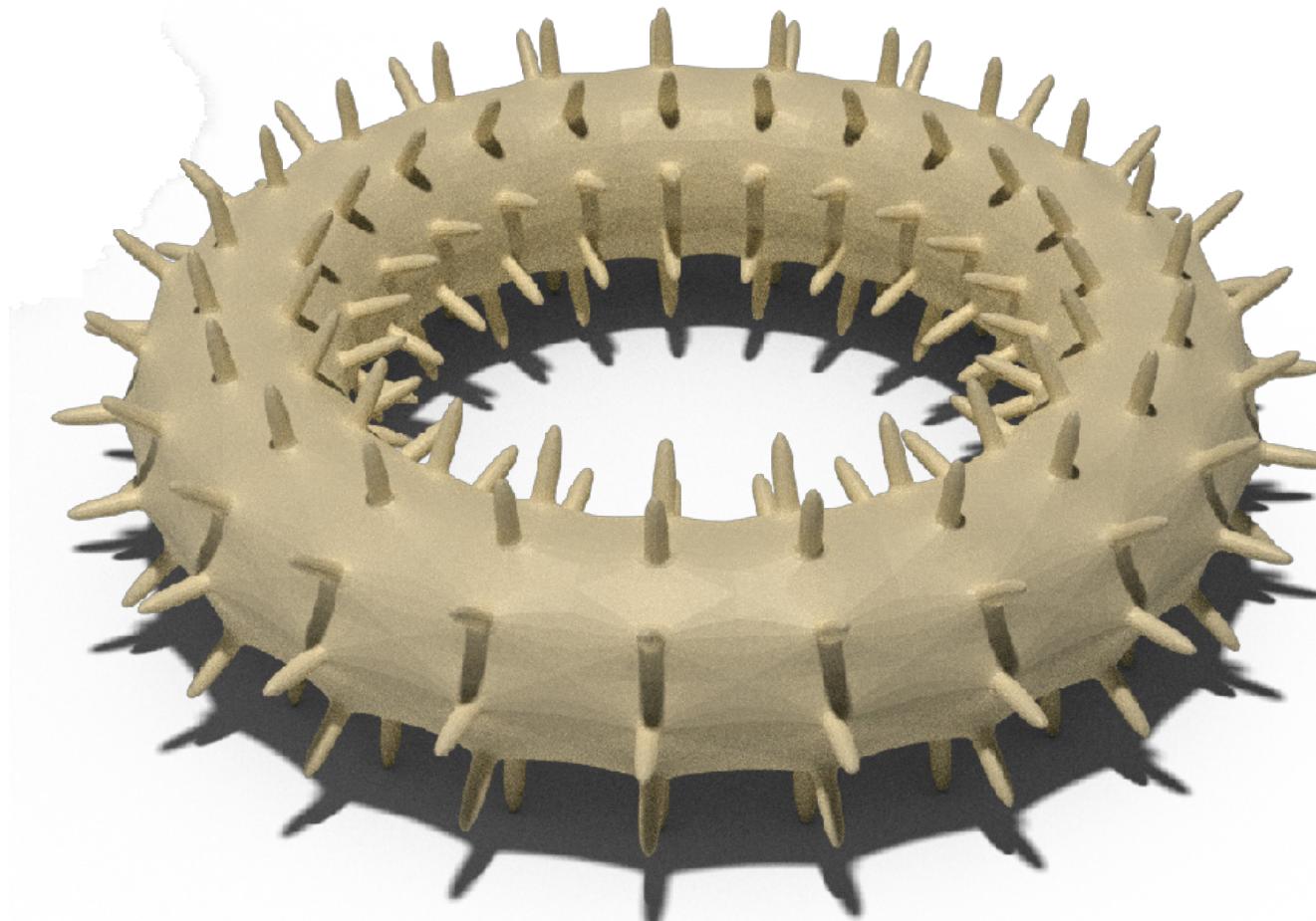


# Learn from a Single Shape

**Patches are training data**

**Textures contain self-repetitions**

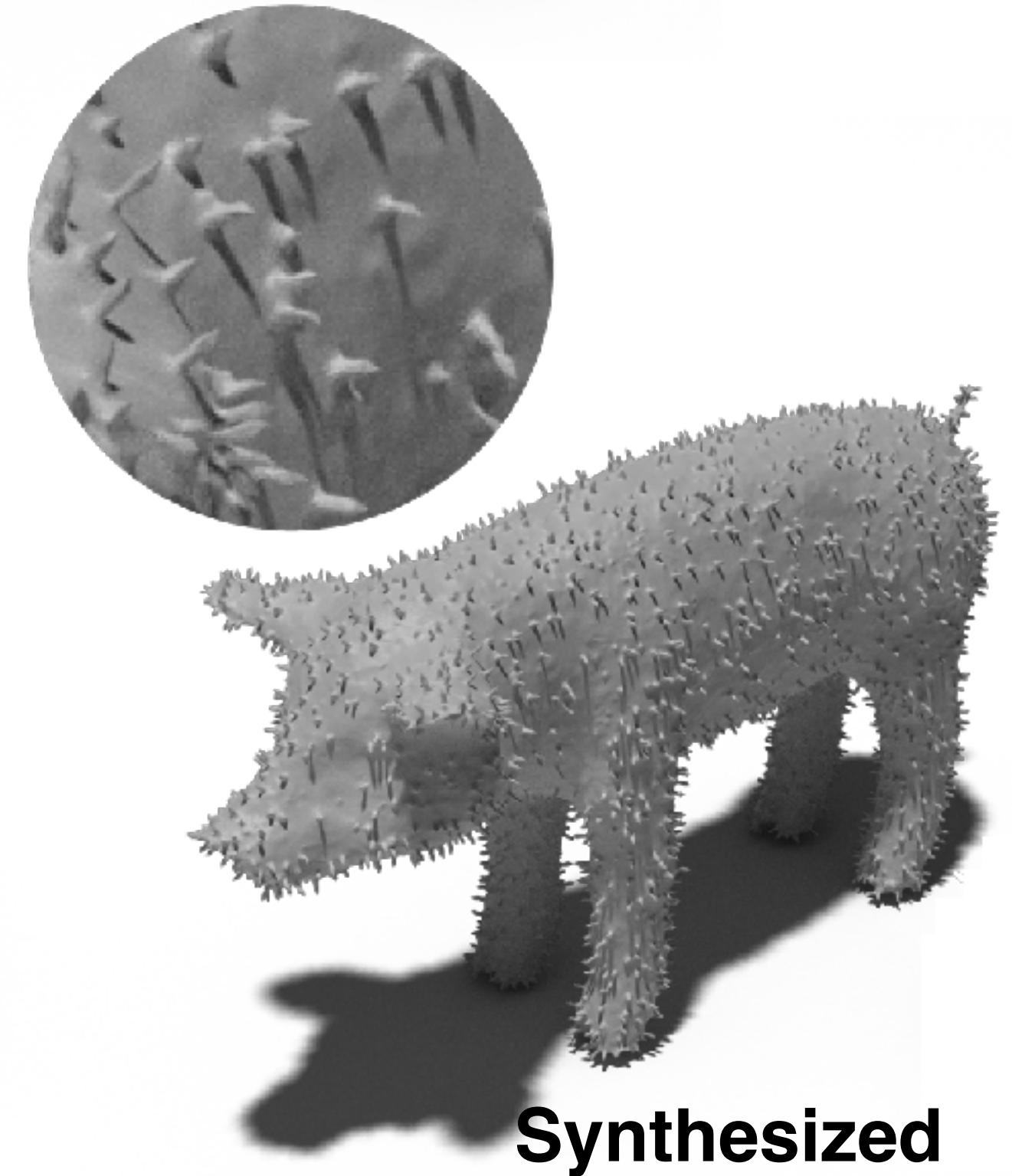
**Local patches are similar for different shapes!**



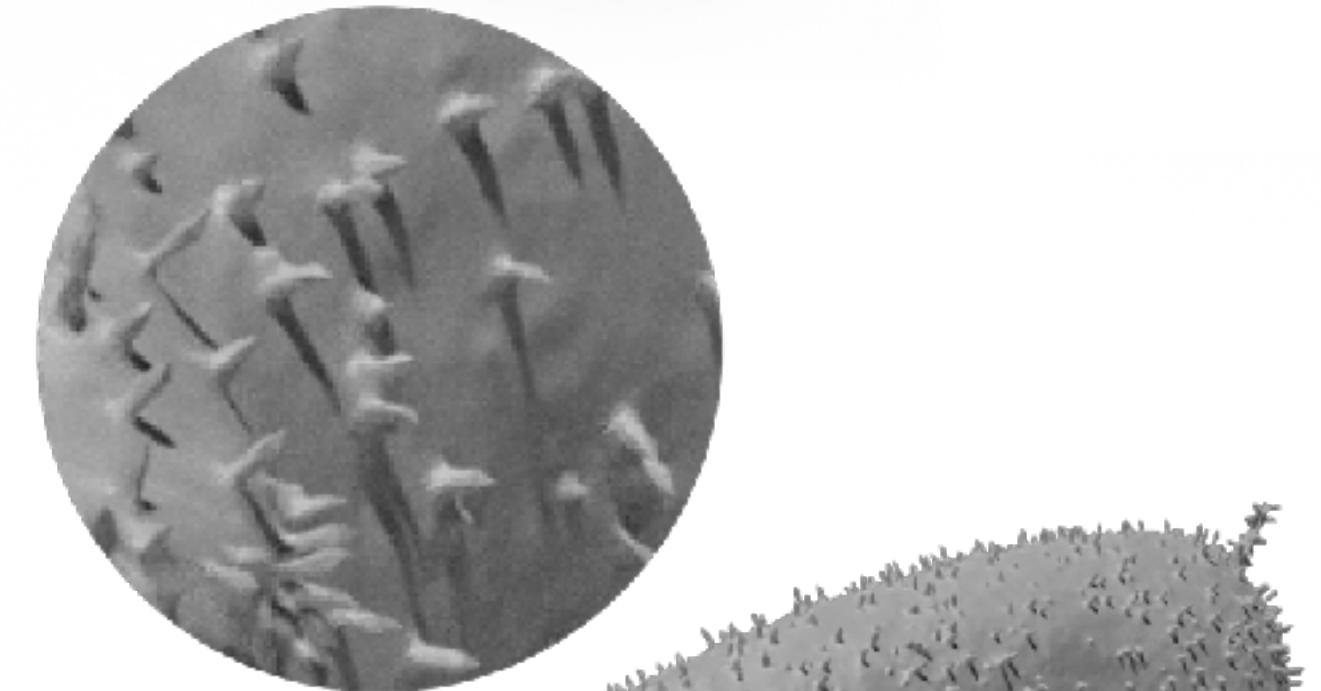
**Exemplar**



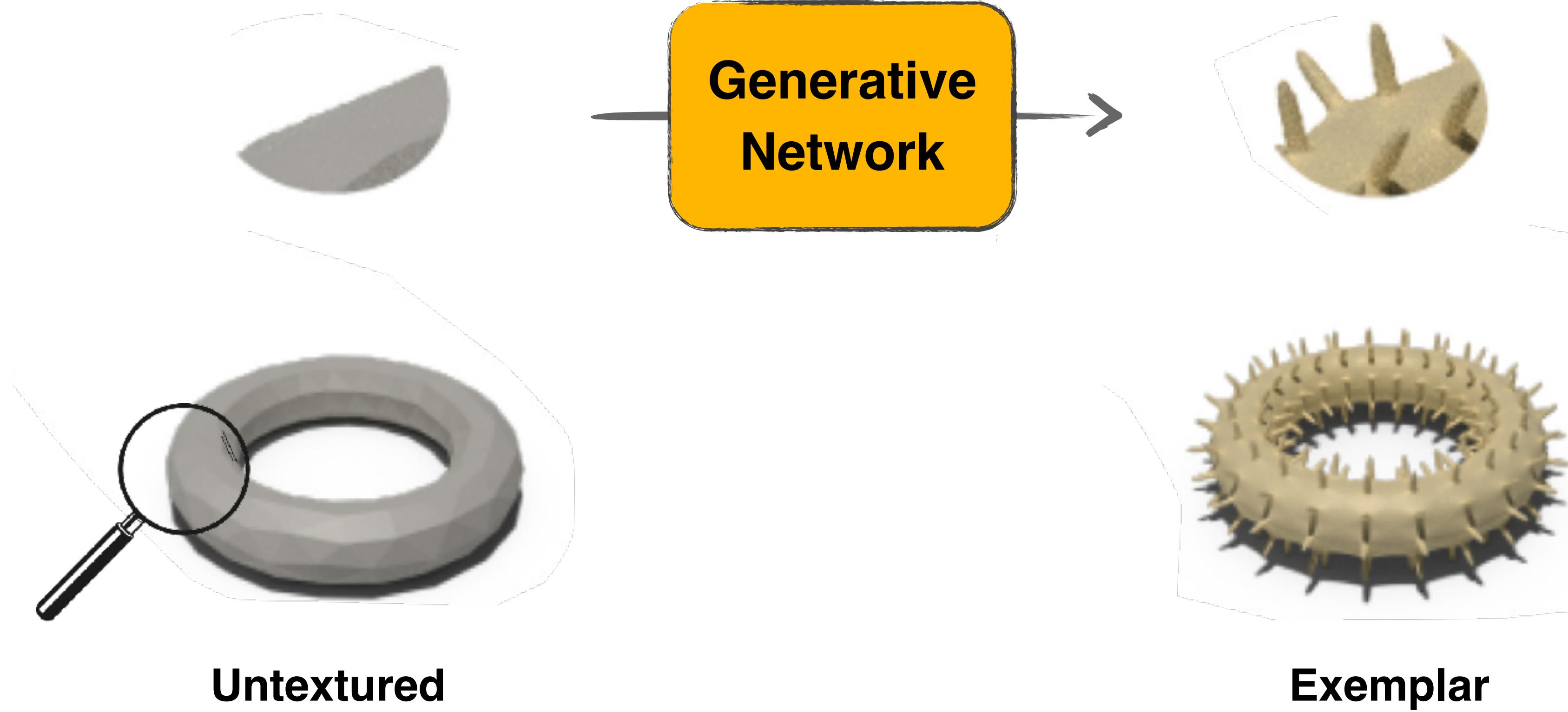
**New Object**



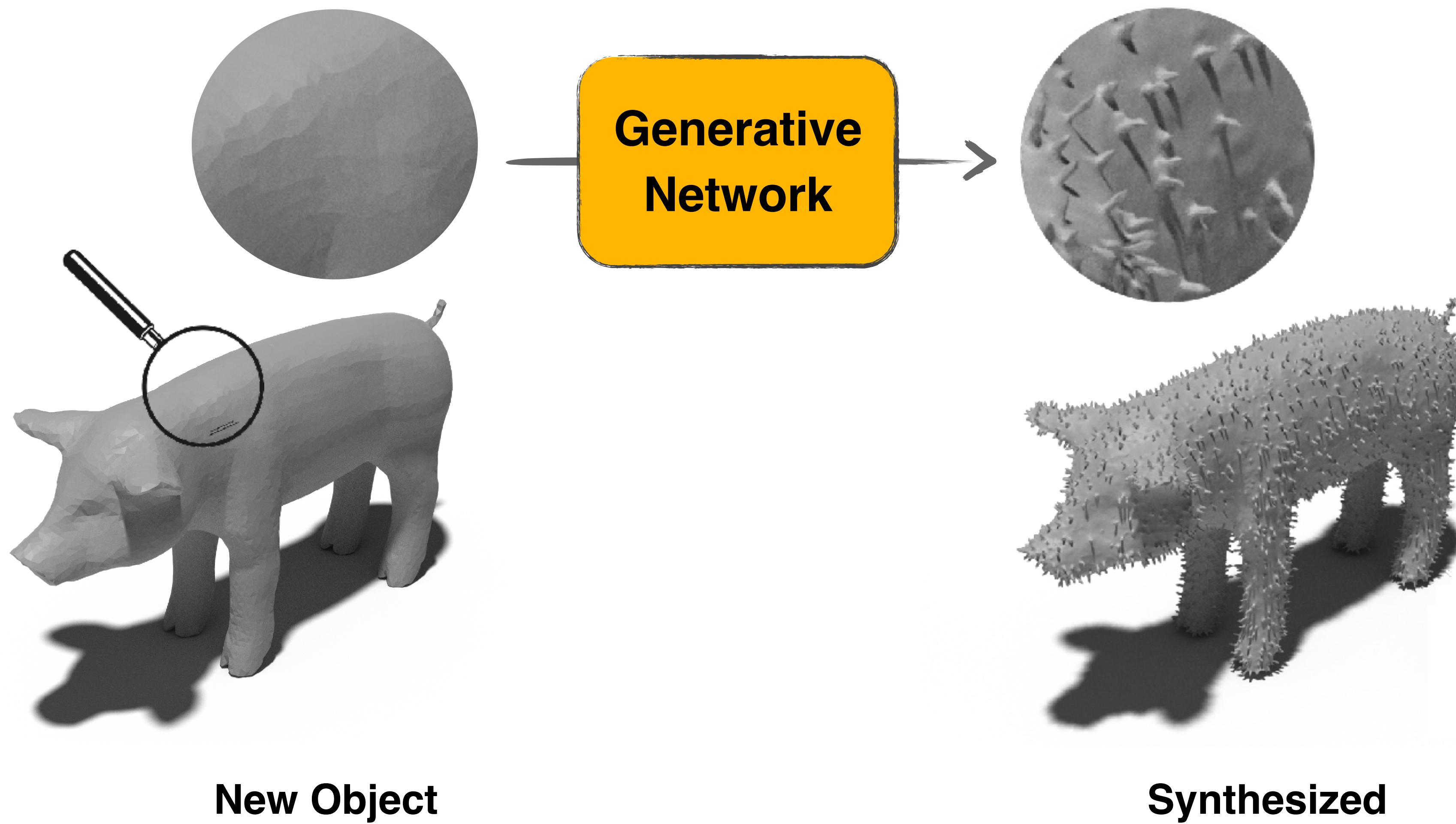
**Synthesized  
Textures**



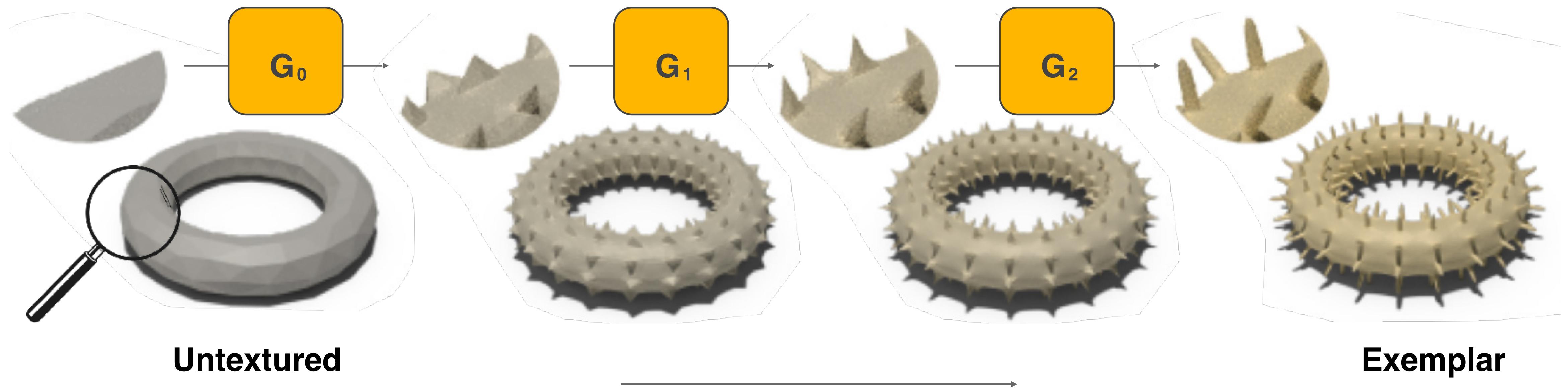
# Train on local patches



# Generalization from local patches

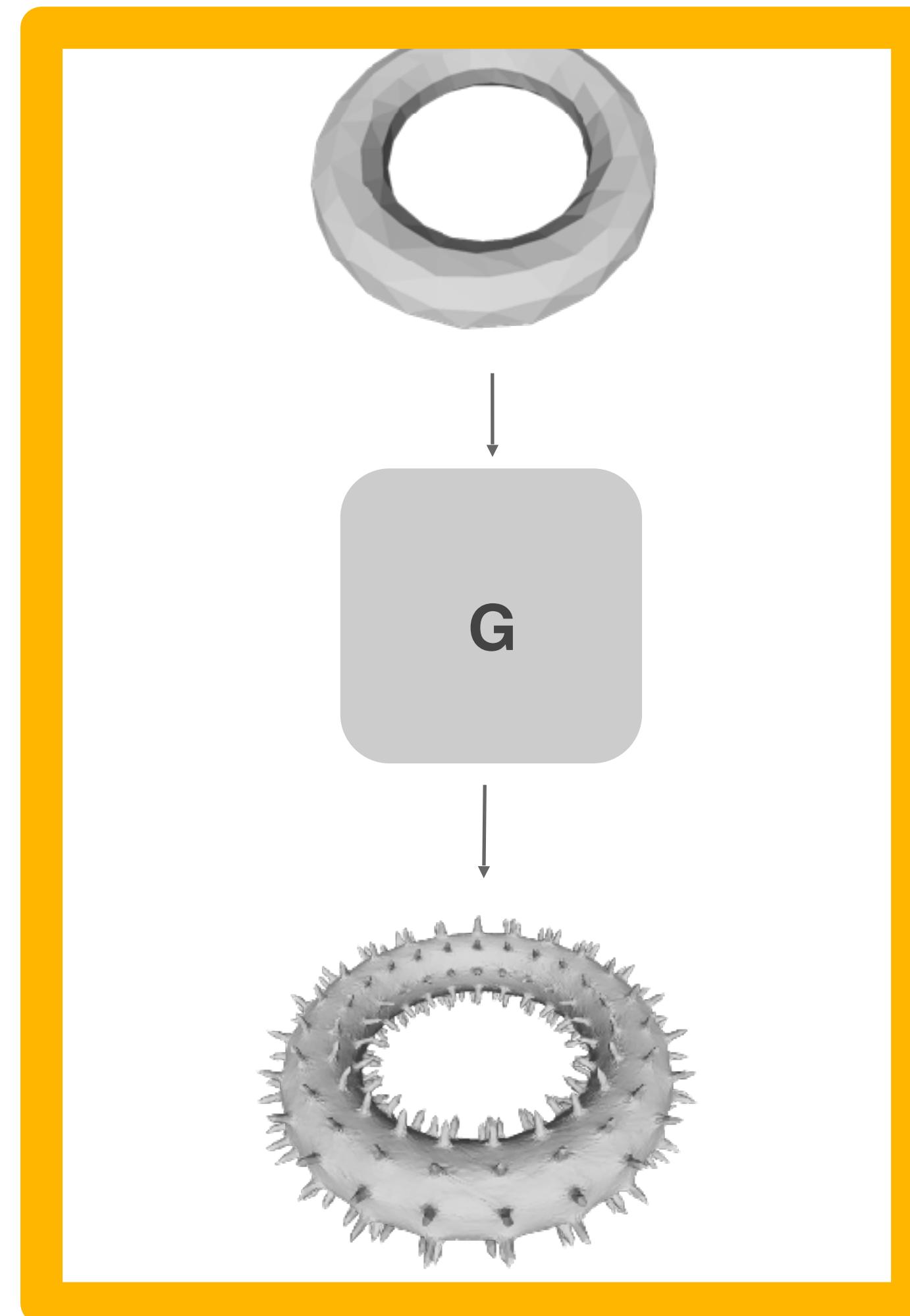


# Progressive Texture Synthesis





**Multi-Scale Training Inputs**

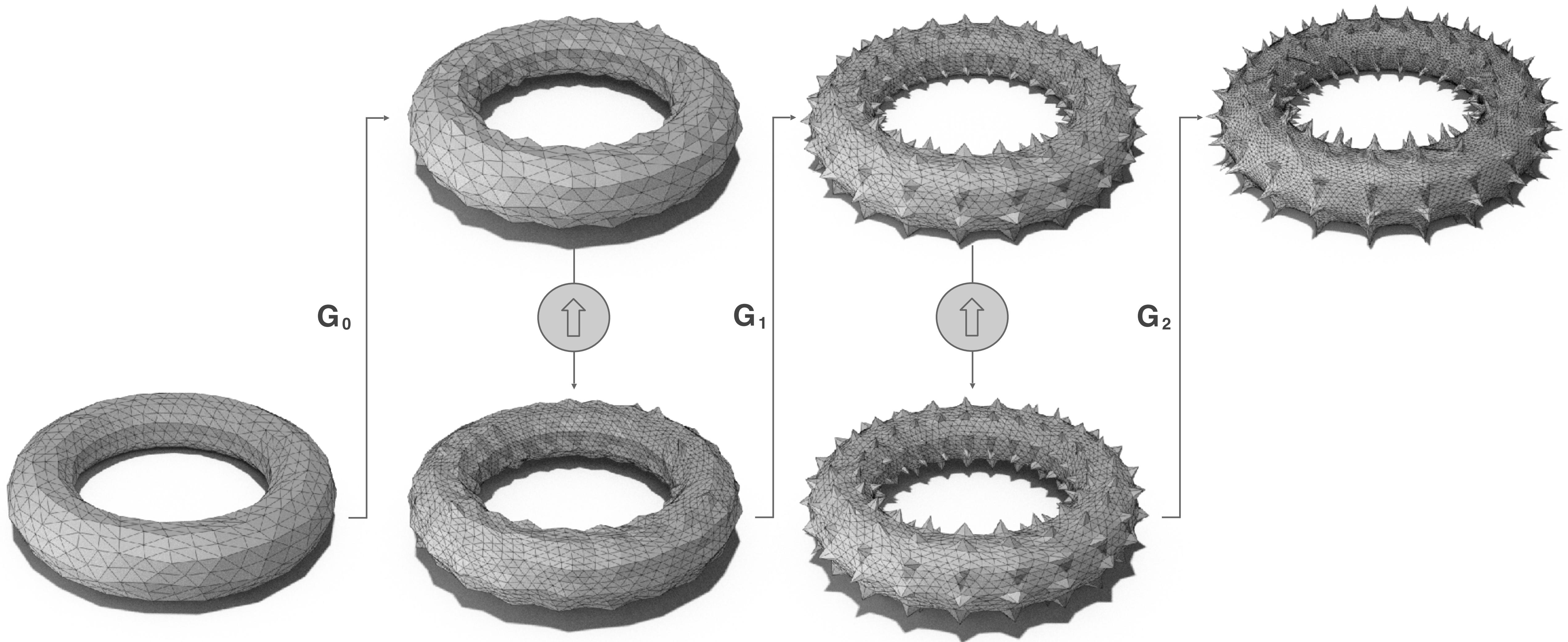


**Progressive Training**

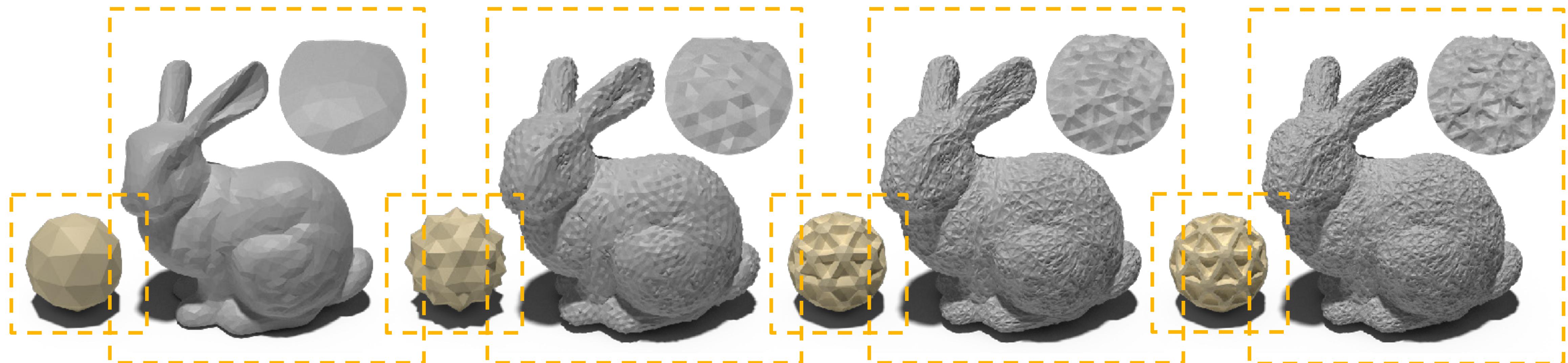


**Inference**

# Progressive Texture Synthesis



# Multi-Scale Textures



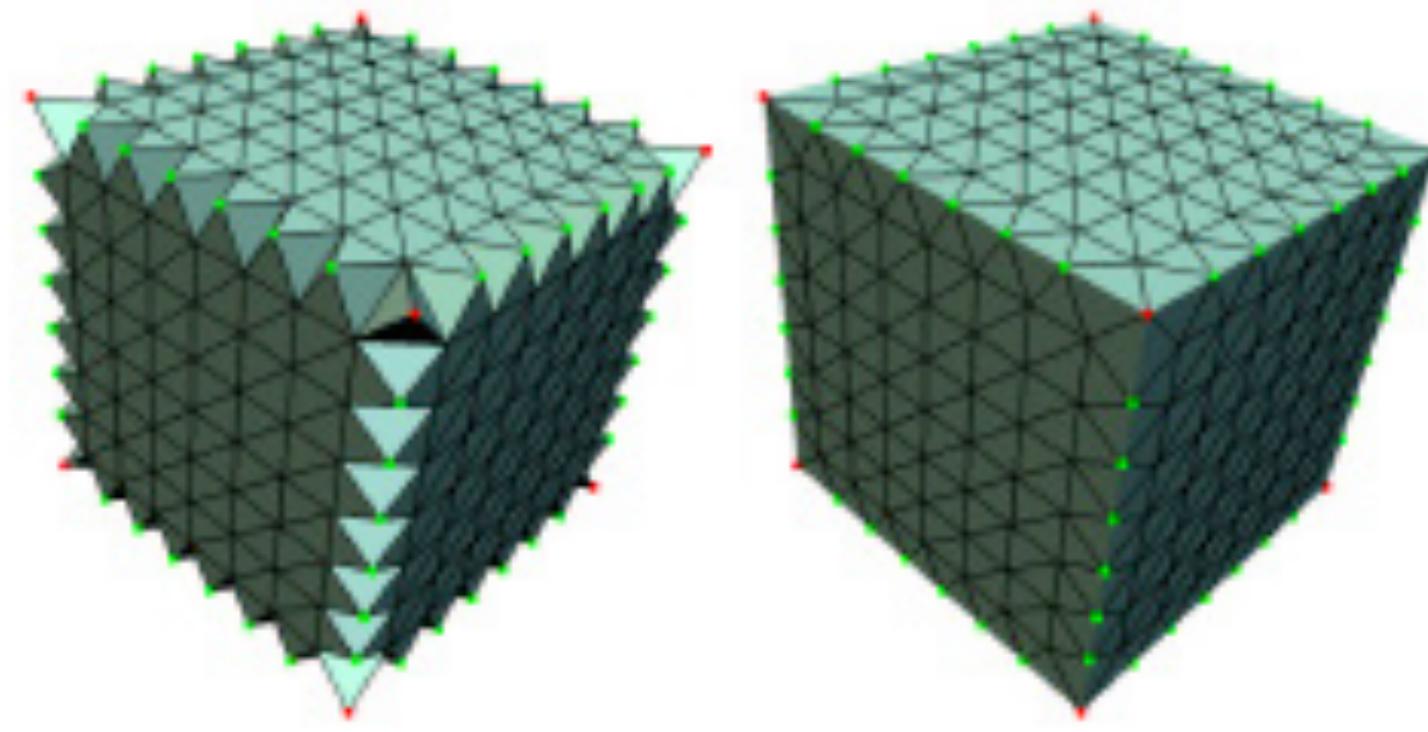
# Texture Interpolation



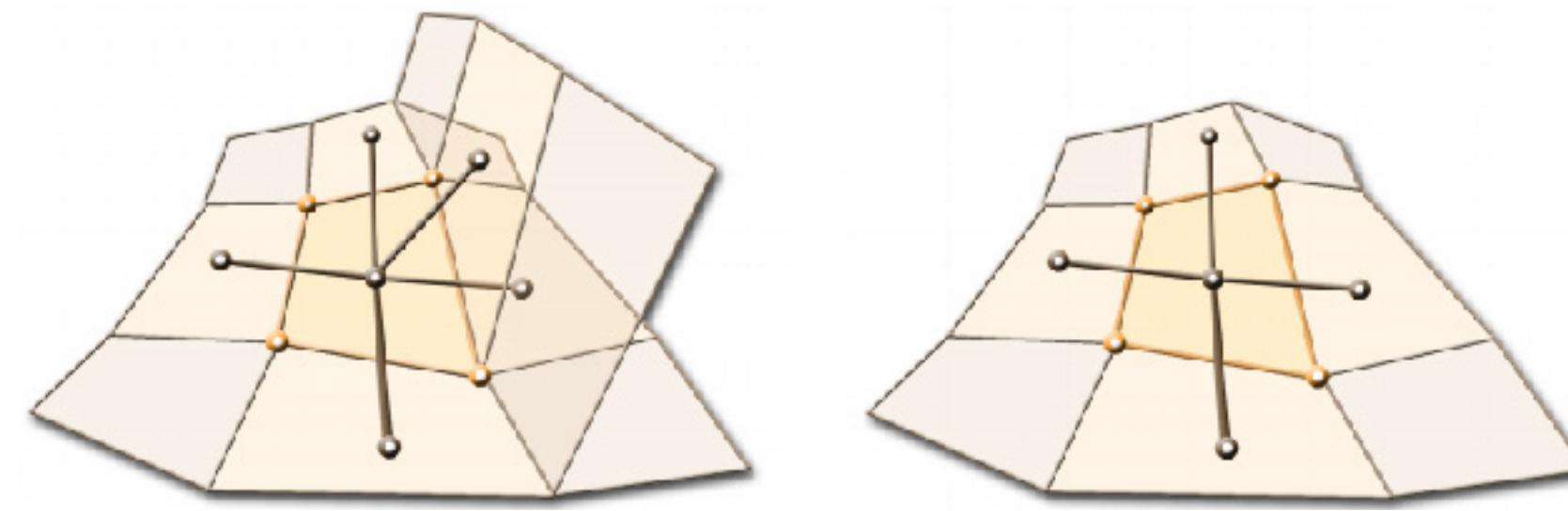
# SUMMARY



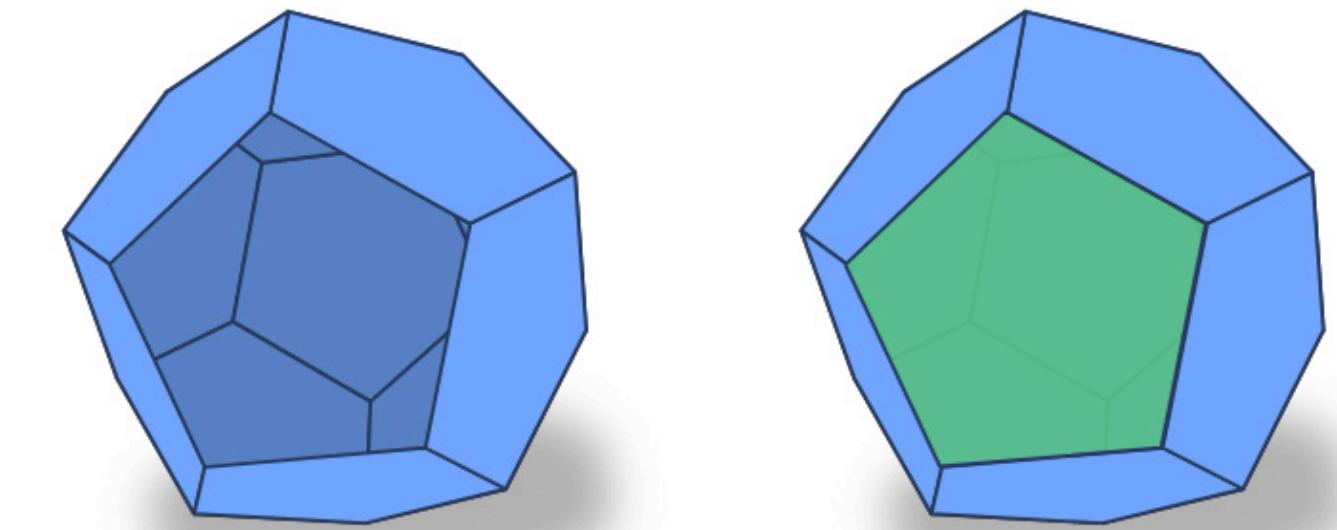
# Connectivity based Mesh Learning



sharp features

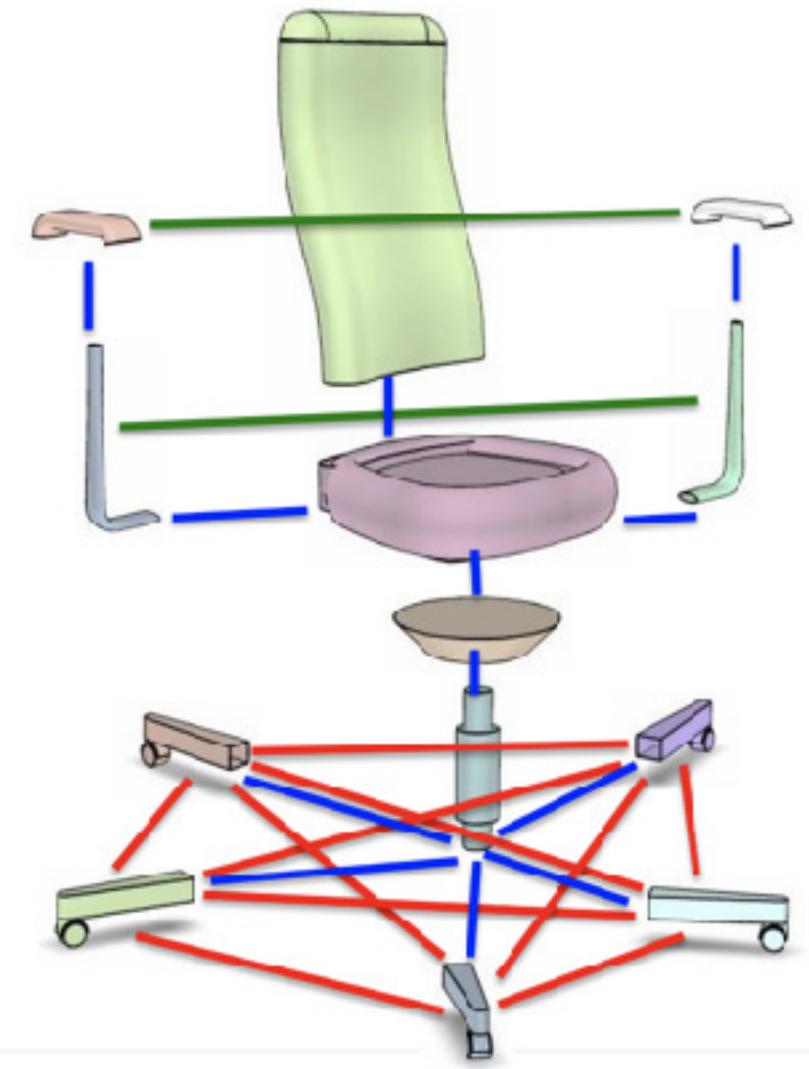


fix non-manifold

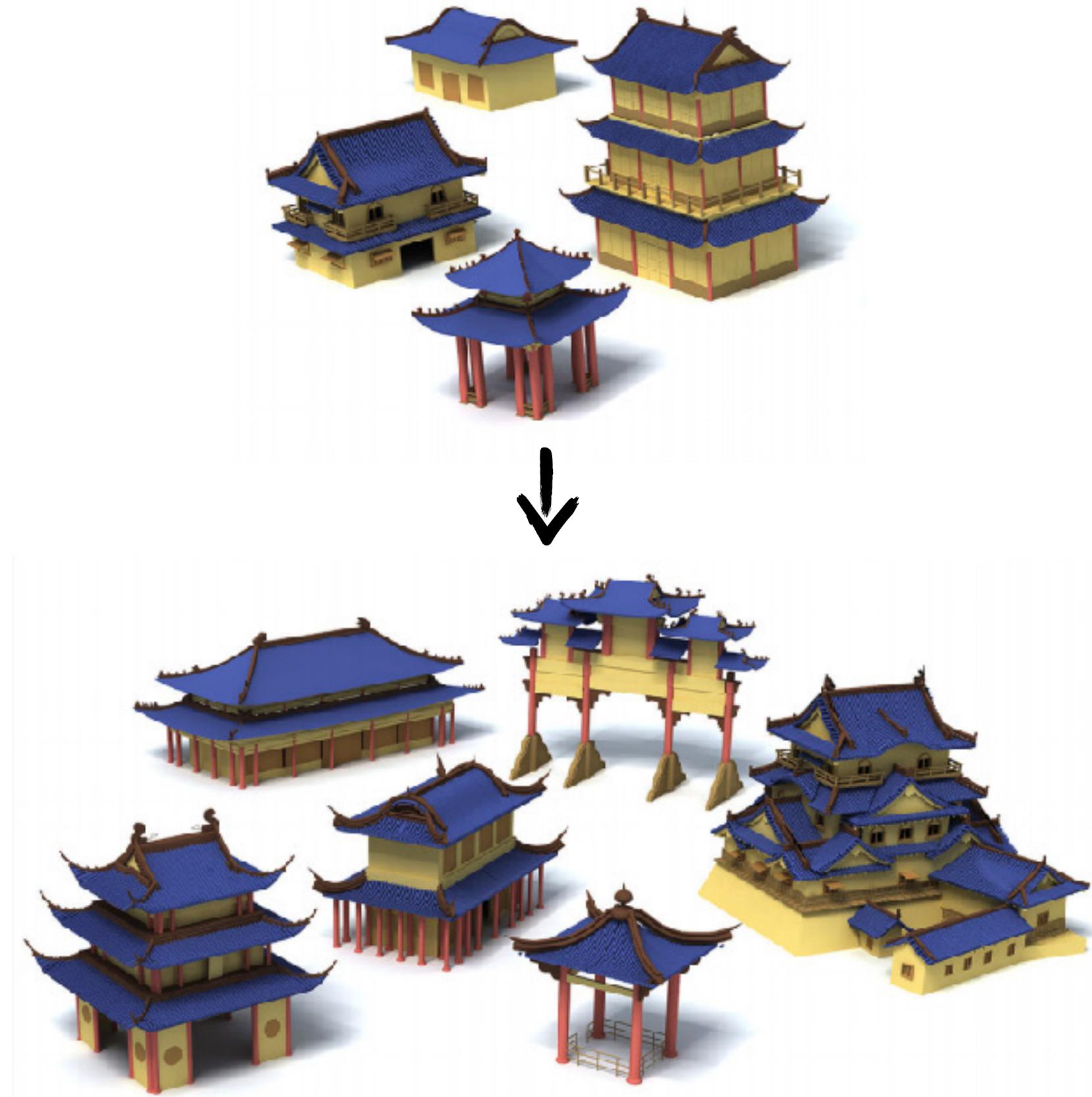


hole filling

# Mesh Generative Models



structural learning



structural shape synthesis



mesh boolean

# Shape Perception



input

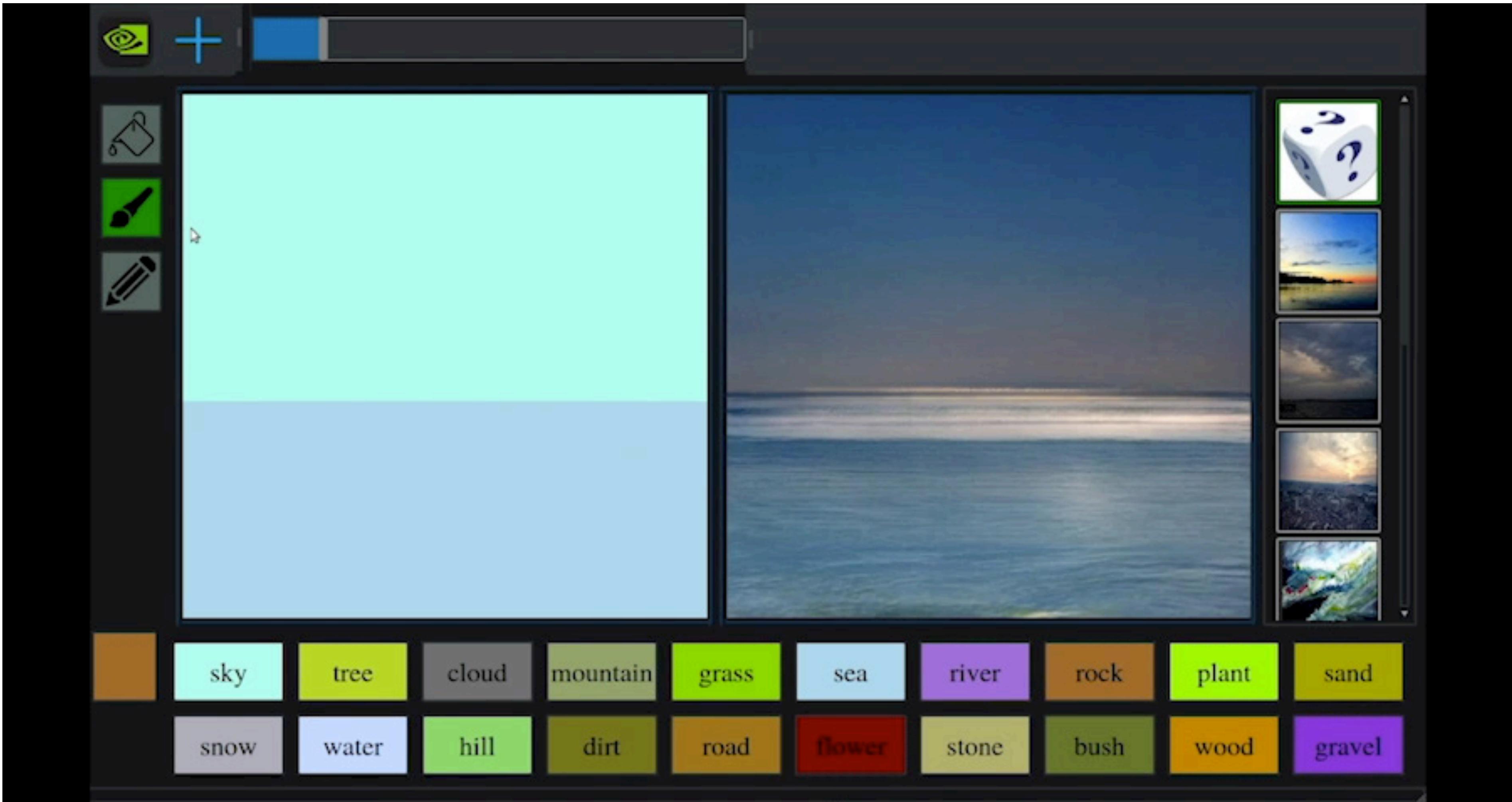


style



output

# Futuristic 3D Modeling Tools



# Draw Inspiration from Classic Methods

