## 1 Multiple comparisons between groups

If an ANOVA test has identified that not all groups belong to the same population, then methods may be used to identify which groups are significantly different to each other.

Below are two commonly used methods: Tukey's and Holm-Bonferroni.

These two methods assuming data that is approximately normally distributed.

## 1.1 Setting up the data, and running an ANOVA

```
import numpy as np
import scipy.stats as stats
# Create four random groups of data with a mean difference of 1
mu, sigma = 10, 3 # mean and standard deviation
group1 = np.random.normal(mu, sigma, 50)
mu, sigma = 11, 3 # mean and standard deviation
group2 = np.random.normal(mu, sigma, 50)
mu, sigma = 12, 3 # mean and standard deviation
group3 = np.random.normal(mu, sigma, 50)
mu, sigma = 13, 3 # mean and standard deviation
group4 = np.random.normal(mu, sigma, 50)
# Show the results for Anova
F_statistic, pVal = stats.f_oneway(group1, group2, group3, group4)
print ('P value:')
print (pVal)
OUT:
P value:
1.6462001201818463e-08
For the multicomparison tests we will put the data into a dataframe. And then reshape it to a stacked
dataframe
# Put into dataframe
df = pd.DataFrame()
df['treatment1'] = group1
df['treatment2'] = group2
df['treatment3'] = group3
df['treatment4'] = group4
# Stack the data (and rename columns):
stacked_data = df.stack().reset_index()
stacked_data = stacked_data.rename(columns={'level_0': 'id',
                                             'level_1': 'treatment',
                                             0:'result'})
# Show the first 8 rows:
```

```
print (stacked_data.head(8))
OUT:
   id
       treatment
                    result
   0 treatment1 12.980445
1
   0 treatment2 8.444603
   0 treatment3 10.713692
   0 treatment4 10.777762
3
   1 treatment1 14.350560
5
   1 treatment2 9.436072
6
  1 treatment3 12.715509
7
   1 treatment4 15.016419
```

## 1.2 Tukey's multi-comparison method

See https://en.wikipedia.org/wiki/Tukey's\_range\_test

This method tests at  $P_i$ 0.05 (correcting for the fact that multiple comparisons are being made which would normally increase the probability of a significant difference being identified). A results of 'reject = True' means that a significant difference has been observed.

```
from statsmodels.stats.multicomp import (pairwise_tukeyhsd,
                                     MultiComparison)
# Set up the data for comparison (creates a specialised object)
MultiComp = MultiComparison(stacked_data['result'],
                         stacked_data['treatment'])
# Show all pair-wise comparisons:
# Print the comparisons
print(MultiComp.tukeyhsd().summary())
OUT:
Multiple Comparison of Means - Tukey HSD, FWER=0.05
_____
        group2 meandiff lower upper reject
  group1
treatment1 treatment2 1.5021 -0.0392 3.0435 False
treatment1 treatment3 1.47
                            -0.0714 3.0113 False
treatment1 treatment4 3.8572
                            2.3159 5.3985 True
treatment2 treatment3 -0.0322 -1.5735 1.5091 False
treatment2 treatment4 2.355 0.8137 3.8963 True
```

## 1.3 Holm-Bonferroni Method

treatment3 treatment4 2.3872 0.8459 3.9285 True

```
See: https://en.wikipedia.org/wiki/Holm%E2%80%93Bonferroni_method
The Holm-Bonferroni method is an alterantive method.

comp = MultiComp.allpairtest(stats.ttest_rel, method='Holm')
print (comp[0])

OUT:
```

Test Multiple Comparison ttest\_rel FWER=0.05 method=Holm alphacSidak=0.01, alphacBonf=0.008

group1	group2	stat	pval	<pre>pval_corr</pre>	reject
treatment1	treatment2	-2.1234	0.0388	0.0776	False
treatment1	${\tt treatment3}$	-2.4304	0.0188	0.0564	False
treatment1	${\tt treatment4}$	-6.4443	0.0	0.0	True
${\tt treatment2}$	${\tt treatment3}$	0.0457	0.9637	0.9637	False
${\tt treatment2}$	${\tt treatment4}$	-3.7878	0.0004	0.0017	True
treatment3	treatment4	-5.0246	0.0	0.0	True