

Basics II - Data Structures

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Resources:

- *Python for Finance (2nd ed.)*: Sec. 3.Basic Data Structures (Section 3.Excursus: Functional Programming is optional)
- *The Python Tutorial*: Sec. 3.1.3 (Lists), 4.2 (for Statements), 4.3 (The `range()` Function), 4.4 (break and continue Statements, and else Clauses on Loops), 5.1 (More on Lists), 5.3 (Tuples and Sequences), 5.4 (Sets), 5.5 (Dictionaries)

Executive Summary

Intuitively, a *data structure* is an object containing other objects, not necessarily of the same *data type*.

Standard Python provides four basic data structures, which can be differentiated at high level by being: - *ordered* or *not ordered*: that is, whether they preserve the order in which entries are added or not; - *mutable* or *immutable*: that is, whether - once defined - they can be modified or not.

These data-structures are:

data-structure	ordered (or not)	mutable (or not)
Tuples	ordered	immutable
Lists	ordered	mutable
Dicts	not ordered	mutable
Sets	not ordered	mutable

The function `type()` can be called over any defined data-structure and returns its type: `tuple` for Tuples, `list` for Lists, `dict` for Dicts and `set` for Sets.

The following sections are organized as follows:

- In Section 1 Tuples (`tuple`) are introduced as the Python data-structure for *ordered* sequence-like objects that *cannot be* modified once defined.
- In Section 2 Lists (`list`) are introduced as the Python data-structure for *ordered* sequence-like objects that *can be* modified once defined. In this context `for` loops are introduced in Sec. Section 2.7.
- In Section 3 Dicts (`dict`) are introduced as the Python data-structure for *not ordered* collection-like objects that *can be* modified once defined and that implement a *key-to-value* map.
- In Section 4 Sets (`set`) are introduced as the Python data-structure for *not ordered* collection-like objects that *can be* modified once defined and that contain unique elements (that is, every elements appears only once).

1 Tuples

Tuples consists of a number of values - of heterogeneous data-type, in general - packed together in an immutable sequence and separated by commas.

In my experience, I didn't use tuple that often, probably because their *immutability* goes against the dynamism of trial-n-error phases of a typical quantitative analysis. In fact, for the same reason, tuples may be a good asset as they guarantee the safety of data stored in them.

1.1 Definition

Tuples can be defined with or without parenthesis () surrounding the ,-separated sequence.

```
[1]: tup = (1, 0.35, "GBP")

print(tup)
type(tup)
```

```
[2]: tup = 1, 0.35, "GBP"

print(tup)
type(tup)
```

The number of elements is easily retrieved by the `len()` function:

```
[3]: len(tup)
```

```
[3]: 3
```

1.2 Indexing and Slicing

Tuples share a lot of properties with other sequence-like data-structure. For details take a look at [Sequence Types — list, tuple, range](#) page of the Python standard library.

In particular, tuples share indexing features with strings (see [Basics_I_Data_Types.ipynb](#)) and lists (see Sec. 2). In particular, elements of a tuple can be accessed by *zero-based* indexes:

```
[4]: # 0 is the index of the first element of the tuple
print(tup[0])
type(tup[0])
```

```
1
```

```
[4]: int
```

```
[5]: # -1 is the index of the last element of the tuple
print(tup[-1])
type(tup[-1])

tup[len(tup)-1]
```

```
GBP
```

```
[5]: 'GBP'
```

and tuples can be sliced. That is, you can select few elements only of the tuple if you want to

```
[6]: tup_slice = tup[0:2] # elements from position 0 (included) to 2 (excluded)

print(tup_slice)
type(tup_slice)
```

```
(1, 0.35)
```

```
[6]: tuple
```

```
[7]: tup[2:5] # elements from position 2 (included) to 5 (excluded)
```

```
[7]: ('GBP',)
```

```
[8]: tup[:2] # elements from the beginning to position 2 (excluded) --- equivalent
      ↪ to tup[0:2]
```

```
[8]: (1, 0.35)
```

```
[9]: tup[-2:] # elements from the second-last (included) to the end
```

```
[9]: (0.35, 'GBP')
```

1.3 Changing Values (and why you shouldn't do that)

Analogously to strings - but differently from lists - tuples are *immutable* objects. That is, if you try to change one of its elements, you get

TypeError: 'tuple' object does **not** support item assignment

```
[10]: # p[0] = 17
```

In particular, you cannot simply use the + operator as you would do with a string to concatenate characters. That is, something like

```
17 + tup[1:]
```

would cause the following error

TypeError: unsupported operand type(s) for +: 'int' and 'tuple'

that simply tells you that you cannot *add* int objects (like 17) with tuple objects (like the slice `tup[1:]`).

```
[11]: # 17 + tup[1:]
```

Workaround to modify a tuple: of course there is a workaround (and it will be clear once you have covered Sec. 2 on Lists). You can: - convert the tuple into a list using `list()` casting function, - change the list (which is a mutable object) - convert the list back into a tuple using the `tuple()` casting function.

```
[12]: list_tup = list(tup) # cast tup as a list

print(list_tup)
type(list_tup)
```

```
[1, 0.35, 'GBP']
```

```
[12]: list
```

```
[13]: list_tup[0] = 17 # change the element
```

```
[14]: tup = tuple(list_tup) # cast-back as a tuple

print(tup)
type(tup)
```

```
(17, 0.35, 'GBP')
```

```
[14]: tuple
```

Nevertheless, if you need to modify a tuple, the real question is why did you pack your data into a tuple? So, the take-home message is: if you need to modify a tuple, re-think your code... you're likely to need a list instead of a tuple.

1.4 Nested Tuples

Read this section once you have covered Section 2 on Lists

Notice that even if the tuple itself is not mutable, its elements can consist of *mutable* objects (such as lists) and/or *immutable* objects (such as tuple themselves).

```
[15]: l = [87, 100, 99]           # a list
      t = ("ACT/365", "ACT/360") # a tuple

      nested_tup = (l, t, 100)

print(nested_tup)
type(nested_tup)
```

```
([87, 100, 99], ('ACT/365', 'ACT/360'), 100)
```

```
[15]: tuple
```

As we have seen, elements of `nested_tup` can be accessed through indexing:

```
[16]: print(nested_tup[0])
      type(nested_tup[0])
```

```
[87, 100, 99]
```

[16]: list

```
[17]: print(nested_tup[1])
      type(nested_tup[1])
```

('ACT/365', 'ACT/360')

[17]: tuple

```
[18]: print(nested_tup[2])
      type(nested_tup[2])
```

100

[18]: int

In the same way as we have seen in Section 2.3 for nested lists, you can as well access nested elements of list `l` and tuple `s` using nested-indexing of `nested_tup`:

```
[19]: # [0][0] is the index of the first element
      # of (list 'l' which is) the first element of the tuple 'nested_tup'
      print(nested_tup[0][0])
      type(nested_tup[0][0])
```

87

[19]: int

```
[20]: # [0][2] is the index of the third element
      # of (list 'l' which is) the first element of the tuple 'nested_tup'
      print(nested_tup[0][2])
      type(nested_tup[0][2])
```

99

[20]: int

```
[21]: # [1][0] is the index of the first element
      # of (tuple 't' which is) the second element of the tuple 'nested_tup'
      print(nested_tup[1][0])
      type(nested_tup[1][0])
```

ACT/365

[21]: str

```
[22]: # [1][1] is the index of the second element
      # of (tuple 't' which is) the second element of the tuple 'nested_tup'
      print(nested_tup[1][1])
```

```
type(nested_tup[1][1])
```

ACT/360

[22]: str

Warning: in the same way as they apply to nested-indexing of lists, indexing of tuples may raise (*repetita iuvant*):

- *out of range* **IndexError**: if you try to refer to an index that does not correspond to any element of the data structure (or of its nested data-structures, if any)

```
[23]: # produces: IndexError: tuple index out of range
# because index 3 would refer to the 4th element of nested_tup, that does not
      ↪ exist.

# nested_tup[3]
```

```
[24]: # produces: IndexError: list index out of range
# because index 3 would refer to the 4th element of nested_tup[0] (i.e. list
      ↪ 'l'), that does not exist

# nested_tup[0][3]
```

```
[25]: # produces: IndexError: tuple index out of range
# because index 2 would refer to the 3rd element of nested_tup[1] (i.e. tuple
      ↪ 't'), that does not exist

# nested_tup[1][2]
```

- *object is not subscriptable* **TypeError**: if you try to refer with an index to an element that is not indexable (like Integers, Floats,...)

```
[26]: nested_tup[2]
```

[26]: 100

```
[27]: # produces: TypeError: 'int' object is not subscriptable
# because we are trying to refer to the first element of nested_tup[2] (i.e.
      ↪ integer 100),
# that, in poor words, does not have any element inside and thus doesn't admit
      ↪ indexing.

# nested_tup[2][0]
```

Keeping in mind that if you need to modify a tuple, you're likely to have chosen the wrong data structure to pack together your data (why not opting for a `list` in the first place?), still for completeness let's briefly discuss what you can modify in a nested tuple.

Getting back to our nested tuple, you can modify only its mutable nested elements (if any):

```
[28]: nested_tup
```

```
[28]: ([87, 100, 99], ('ACT/365', 'ACT/360'), 100)
```

```
[29]: nested_tup[0][1] = 98
      nested_tup
```

```
[29]: ([87, 98, 99], ('ACT/365', 'ACT/360'), 100)
```

```
[30]: nested_tup[0].append(75)  # integer 75 is appended at the end of list [87, 98, 99]
      nested_tup
```

```
[30]: ([87, 98, 99, 75], ('ACT/365', 'ACT/360'), 100)
```

but you cannot explicitly re-define elements of the tuple `nested_tup` because this would contrast with the immutability of the (nested) tuple itself.

To make an example: an explicit redefinition of the element `nested_tup[0]` of `nested_tup` like this one

```
nested_tup[0] = [67, 89]
```

would produce

```
TypeError: 'tuple' object does not support item assignment
```

If you find strange that you can change values of the tuple's element `nested_tup[0]` or even adding values to it, as above, but you cannot re-define it as a whole... well, I'm with you. Let's go ahead, you can live with this :)

2 Lists

[Lists](#) consists of a number of values - in general, of heterogeneous data-type - packed together in a mutable sequence and separated by commas between square brackets.

Lists are very versatile data structures, since they offer flexibility (since they are mutable) and feature several built-in methods that can speed up coding.

2.1 Definition

Lists are defined with square brackets `[]` surrounding the ,-separated sequence.

```
[31]: lis = [1, 0.35, "GBP"]

      print(lis)
      type(lis)
```

```
[1, 0.35, 'GBP']
```



```
[31]: list
```

The number of elements is easily retrieved by the `len()` function:

```
[32]: len(lis)
```

```
[32]: 3
```

2.2 Indexing and Slicing

Lists share a lot of properties with other sequence-like data-structures. In particular, they share *zero-based* indexing and slicing with Strings and Tuples.

```
[33]: # 0 is the index of the first element of the list
      print(lis[0])
      type(lis[0])
```

```
1
```

```
[33]: int
```

```
[34]: # -1 is the index of the last element of the list
      print(lis[-1])
      type(lis[-1])
```

```
GBP
```

```
[34]: str
```

Here is how to slice a list (yes, always the same way):

```
[35]: lis_slice = lis[0:2] # elements from position 0 (included) to 2 (excluded)

      print(lis_slice)
      type(lis_slice)
```

```
[1, 0.35]
```

```
[35]: list
```

```
[36]: lis[2:5] # elements from position 2 (included) to 5 (excluded)
```

```
[36]: ['GBP']
```

```
[37]: lis[:2] # elements from the beginning to position 2 (excluded) --- equivalent_
      ↪ to lis[0:2]
```

```
[37]: [1, 0.35]
```

```
[38]: lis[-2:] # elements from the second-last (included) to the end
```

```
[38]: [0.35, 'GBP']
```

2.3 Nested Lists

Lists can nest other data structures, both *mutable* objects (such as other lists) and/or *immutable* objects (such as tuples).

```
[39]: l = [87, 100, 99]          # a list
      t = ("ACT/365", "ACT/360") # a tuple

      nested_lis = [l, t, 100]

      print(nested_lis)
      type(nested_lis)
```

```
[[87, 100, 99], ('ACT/365', 'ACT/360'), 100]
```

```
[39]: list
```

As we have seen, elements of `nested_lis` can be accessed through indexing:

```
[40]: print(nested_lis[0])
      type(nested_lis[0])
```

```
[87, 100, 99]
```

```
[40]: list
```

```
[41]: print(nested_lis[1])
      type(nested_lis[1])
```

```
('ACT/365', 'ACT/360')
```

```
[41]: tuple
```

```
[42]: print(nested_lis[2])
      type(nested_lis[2])
```

```
100
```

```
[42]: int
```

You can as well access elements of list `l` and tuple `s` using a nested-indexing of `nested_lis`:

```
[43]: nested_lis
```

```
[43]: [[87, 100, 99], ('ACT/365', 'ACT/360'), 100]
```

```
[44]: # [0][0] is the index of the first element
      # of (list 'l' which is) the first element of the list 'nested_lis'
      print(nested_lis[0][0])
      type(nested_lis[0][0])
```

87

[44]: int

```
[45]: # [0][2] is the index of the third element
      # of (list 'l' which is) the first element of the list 'nested_lis'
      print(nested_lis[0][2])
      type(nested_lis[0][2])
```

99

[45]: int

```
[46]: # [1][0] is the index of the first element
      # of (list 't' which is) the second element of the list 'nested_lis'
      print(nested_lis[1][0])
      type(nested_lis[1][0])
```

ACT/365

[46]: str

```
[47]: # [1][1] is the index of the second element
      # of (tuple 't' which is) the second element of the list 'nested_lis'
      print(nested_lis[1][1])
      type(nested_lis[1][1])
```

ACT/360

[47]: str

2.4 Indexing of Nested Sequences

Ok you have understood how it works... This is actually a general rule, that applies to all the sequence-like data structures: Tuples (**tuple**), Lists (**list**) but also Numpy arrays (**numpy.ndarray**, with the slightly changed syntax `[i,j]` instead of `[i][j]`, as we'll show in a future lesson) that will be introduced in a future notebook.

If a sequence-like data structure, say **seq**, has nested sequence-like elements, then

`seq[i][j]`

is the element of index `j` of the element of index `i`, `seq[i]`, of `seq`. That is, `seq[i][j]` is the $(j + 1)$ -th element of the $(i + 1)$ -th element, `seq[i]`, of `seq`.

Warning: nested-indexing of lists may raise:

- *out of range* **IndexError**: if you try to refer to an index that does not correspond to any element of the data structure (or of its nested data-structures, if any)

```
[48]: nested_lis
```

```
[48]: [[87, 100, 99], ('ACT/365', 'ACT/360'), 100]
```

```
[49]: # produces: IndexError: list index out of range
# because index 3 would refer to the 4th element of nested_lis, that does not
      ↪ exist.

nested_lis[len(nested_lis)-1]
```

```
[49]: 100
```

```
[50]: # produces: IndexError: list index out of range
# because index 3 would refer to the 4th element of nested_lis[0] (i.e. list
      ↪ 'l'), that does not exist

# nested_lis[0][3]
```

```
[51]: # produces: IndexError: tuple index out of range
# because index 2 would refer to the 3rd element of nested_lis[1] (i.e. tuple
      ↪ 't'), that does not exist

nested_lis[1][-1]
```

```
[51]: 'ACT/360'
```

- *object is not subscriptable* **TypeError**: if you try to refer with an index to an element that is not indexable (like Integers, Floats,...)

```
[52]: nested_lis[2]
```

```
[52]: 100
```

```
[53]: # produces: TypeError: 'int' object is not subscriptable
# because we are trying to refer to the first element of nested_lis[2] (i.e.
      ↪ integer 100),
# that, in poor words, does not have any element inside and thus doesn't admit
      ↪ indexing.

# nested_lis[2][0]
```

2.5 Changing Values

Differently from strings and tuples, lists are *mutable* objects and their elements can be changed in a straightforward way.

```
[54]: lis
```

```
[54]: [1, 0.35, 'GBP']
```

```
[55]: lis[0] = 17
lis
```

```
[55]: [17, 0.35, 'GBP']
```

Being a mutable object, you can modify both mutable and immutable (tuples) objects of a nested list, but of course you cannot change elements inside a nested immutable object (e.g. a tuple inside the list).

Let's go back to our `nested_lis` and suppose you want to change the first day count convention from "ACT/365" to "ACT/360"

```
[56]: nested_lis
```

```
[56]: [[87, 100, 99], ('ACT/365', 'ACT/360'), 100]
```

you cannot explicitly modify the element "ACT/365" of the tuple

```
("ACT/365", "ACT/360")
```

because this would result in a

```
TypeError: 'tuple' object does not support item assignment
```

```
[57]: # produced TypeError

# nested_lis[1][0] = "ACT/360"
```

but you could directly re-define the whole tuple `nested_lis[1]` as it is an element of the `nested_lis` list, which is a mutable object.

```
[58]: nested_lis[1] = 0.345
nested_lis
```

```
[58]: [[87, 100, 99], 0.345, 100]
```

Other - mutable - elements can be modified as you want:

```
[59]: nested_lis[0][1] = 98
nested_lis
```

```
[59]: [[87, 98, 99], 0.345, 100]
```

```
[60]: nested_lis[0].append(75)  # integer 75 is appended at the end of list [87, 98, 99]
      nested_lis
```

```
[60]: [[87, 98, 99, 75], 0.345, 100]
```

```
[61]: nested_lis[2] -= 10 # x -= 1 is a short-cut for x = x-1. Other are +=, *= and /=
      nested_lis
```

```
[61]: [[87, 98, 99, 75], 0.345, 90]
```

2.6 Built-in methods

For details on built-in methods see [5.1. More on Lists](#) of the Python tutorial. In particular, two particularly useful built-in methods are worth of mention: - `list.append(x)`: which appends element `x` to the end of the list, extending it

```
[62]: lis
```

```
[62]: [17, 0.35, 'GBP']
```

```
[63]: lis.append('EUR')
      lis
```

```
[63]: [17, 0.35, 'GBP', 'EUR']
```

- `list.sort()`: that sorts in ascending order a list.

Notice that the list to be sorted must have elements of homogenous data-type, otherwise the interpreter will complain, as in this case:

`TypeError: '<' not supported between instances of 'str' and 'float'`

```
[64]: # lis.sort()
```

```
[65]: lis[:2]
```

```
[65]: [17, 0.35]
```

but, for our list `lis`, the sorting will work if we define a new string as the `[17, 0.35]` slice of the original one

```
[66]: lis_slice = lis[:2]  # [17, 0.35] slice
      lis_slice.sort()
      lis_slice
```

```
[66]: [0.35, 17]
```

```
[67]: lis_slice2 = lis[-2:]  
lis_slice2
```

```
[67]: ['GBP', 'EUR']
```

```
[68]: lis_slice2.sort()  
lis_slice2
```

```
[68]: ['EUR', 'GBP']
```

2.7 for loop

A **for loop** in Python is declared as follows:

```
for variable in sequence:  
    statement(s) possibly using variable
```

A **sequence** can be a Python **list**, a Numpy `numpy.ndarray` or other sequence-like data structures. The Python interpreter *loops* from one element to the next one of the **sequence** assigning each time that element to the **variable**. With this value of **variable**, the **statement(s)** are executed. The loop ends when all the elements of the sequence have been considered.

2.7.1 for loop over a list

To make an example, we can print elements of a list:

```
[69]: x = [10, 20, 30]  
  
for xi in x:  
    print(xi)
```

```
10  
20  
30
```

Notice how this **for loop** is not *counter-based*, that is is the Python interpreter that loops into the sequence, returning us the current element of the sequence at each iteration.

2.7.2 Counter-based looping and `range()` function

In some occasions it could be good to loop over a sequence being able to access to its elements through their indexes. This can be achieved using the [range\(\) function](#) which generates a sequence of numbers as an object of the (strange) type **range**.

```
[70]: x = range(10)  
  
print(x)  
type(x)
```

```
range(0, 10)
```

[70]: range

range() is mostly used in for loops as follows:

```
[71]: # a loop over the first 5 numbers from zero
      for i in range(5):
          print(i)
```

0
1
2
3
4

```
[72]: # a loop over numbers from 1 to 9
      for i in range(1,10):
          print(i)
```

1
2
3
4
5
6
7
8
9

But it can be used also to loop over a list, accessing its indexes:

```
[73]: # a loop over the elements of list `lis`
      for i in range(len(x)):
          print(x[i])
```

0
1
2
3
4
5
6
7
8
9

```
[74]: x = [10, 20, 30]

      for i in range(3):
          print(i)
```



```
print(x[i])
```

```
0
10
1
20
2
30
```

where we have used the fact that `range(len(x))` returns numbers from 0 to `len(x)-1`, which are first and last indexes of list `x`.

Example: let's get back to our Fibonacci numbers (see Sec. 3.1 while loop of [Basics_I_Data_Types.ipynb](#) for a refresh) and let's suppose we want to compute the n -th number F_n

```
[75]: def fib_nth(n):
      """
      This function computes the n-th Fibonacci number using inline assignments.

      Parameters:
          n (int): which number to compute.

      Returns:
          F_n2 (int): n-th Fibonacci number.
      """

      if n <= 2:
          return n-1

      # inline initialization
      F_n2, F_n1 = 0, 1 # F_{n-2}, F_{n-1}

      for k in range(n-1):

          # uncomment this line below if you want to print to screen the current_
          ↪number
          print(F_n2)

          # inline update of the last two numbers
          F_n2, F_n1 = F_n1, F_n1 + F_n2

      return F_n2
```

```
[76]: N = 10
```

```
fib_nth(N)
```

```
0
1
1
2
3
5
8
13
21
```

[76]: 34

2.7.3 break Statement in loops

The `break` statement interrupts a `while` or `for` loop that wouldn't be concluded yet otherwise. It is typically used in combination with an `if` statement to break the loop once the condition triggered by the `if` is met.

To make a practical example, let's check whether an item is in a list looping over the list.

```
[77]: lis = [1, "A", 0.35, 1/4, "@"]

item = 0.35

for element in lis:

    print("Checking element {}".format(element))

    if element == item:
        print("Item {} found".format(item))
        break
```

```
Checking element 1
Checking element A
Checking element 0.35
Item 0.35 found
```

As you can see, elements `1/4` and `@` are not checked, because the `element == item` condition of the `if` statement is triggered for element `0.35`.

Just for your knowledge, this was just a pedantic example. If you really want to check whether an item is in a list, well it's super-easy: you have to use the general syntax: `'python object in sequence'` where is the `in` operator that manages the checking operations and returns `True` or `False` depending on the fact that the `object` is really found in the `sequence` or not. Therefore `in` is typically used in the `condition` part of an `if` statement.

```
[78]: if (item in lis):
        print("Item {} found".format(item))
    else:
        print("Item {} not found".format(item))
```

Item 0.35 found

2.7.4. enumerate() looping There is one more way to loop over a list, which allows us to access both indexes and values of a sequence. It's the built-in function `enumerate()`.

```
[79]: x = [10, 20, 30]

for i, xi in enumerate(x):
    print("index i={}; value xi={}".format(i, xi)) # xi is equivalent to do_
    ↪ x[i]
```

```
index i=0; value xi=10
index i=1; value xi=20
index i=2; value xi=30
```

2.8 8. List comprehension

Let's suppose we want to create a list of the squares of the first `n` numbers: 0, 1, 4, 9,... We could do this way with a for loop

```
[80]: def create_squares_list(n):

        lis = [] # an empty list

        for i in range(n):
            print(lis)
            lis += [i**2] # equivalent to lis.append(i**2)

        return lis
```

```
[81]: n = 10
```

```
[82]: x = create_squares_list(n)
x
```

```
[]
[0]
[0, 1]
[0, 1, 4]
[0, 1, 4, 9]
[0, 1, 4, 9, 16]
[0, 1, 4, 9, 16, 25]
[0, 1, 4, 9, 16, 25, 36]
```

```
[0, 1, 4, 9, 16, 25, 36, 49]
[0, 1, 4, 9, 16, 25, 36, 49, 64]
```

```
[82]: [0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

Timing the code (let's re-define `create_squares_list(n)` function without the print, which would consumes a lot of computing time otherwise)

```
[83]: def create_squares_list(n):

    lis = [] # an empty list

    for i in range(n):
        lis += [i**2] # equivalent to lis.append(i**2)

    return lis
```

```
[84]: %timeit create_squares_list(n)
```

3.46 μ s \pm 40.9 ns per loop (mean \pm std. dev. of 7 runs, 100000 loops each)

Alternatively we can create a list through a list comprehension feature (see [section 5.1.3. List Comprehensions](#)), which is an elegant and fast way to generate lists:

```
[85]: x = [i**2 for i in range(n)]
x
```

```
[85]: [0, 1, 4, 9, 16, 25, 36, 49, 64, 81]
```

```
[86]: y = [pippo**3 for pippo in range(n)]
y
```

```
[86]: [0, 1, 8, 27, 64, 125, 216, 343, 512, 729]
```

```
[87]: 9**3
```

```
[87]: 729
```

as you can see, the result is the same. For small dimensions like `n=10`, also the time is comparable

```
[88]: %timeit [i**2 for i in range(n)]
```

2.98 μ s \pm 38.4 ns per loop (mean \pm std. dev. of 7 runs, 100000 loops each)

but let's see what happen for bigger dimensions:

```
[89]: n = int(1e6)
n
```

```
[89]: 1000000
```

```
[90]: %timeit create_squares_list(n)
```

368 ms \pm 3.51 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)

```
[91]: %timeit [i**2 for i in range(n)]
```

334 ms \pm 30.2 ms per loop (mean \pm std. dev. of 7 runs, 1 loop each)

For such an easy definition (we are only computing squares) the improvement is marginal, but for more complex list definitions, the speed-improvement can be significant. Plus, what the entire `create_squares_list(n)` does has been replaced by the one-line of code `[i**2 for i in range(n)]`. Nice, isn't it?

3 Dicts

Dicts consists of collection of *key: value* pairs where *keys* are a *unique* set of any immutable data-type.

Dictionaries are very good to implement mapping-tables or any kind of logic association between a given set of unique indexers (the keys) and data (the values).

3.1 Definition

Dicts are defined with curly brackets `{}` surrounding the ,-separated list of **key: value** pairs.

```
[92]: d = {"AAA": 5, "A+": 20, "BBB": 50, "D": 100}
      d
```

```
[92]: {'AAA': 5, 'A+': 20, 'BBB': 50, 'D': 100}
```

So, differently from lists, that are indexed by a range of numbers, dictionaries are indexed by (unique) keys.

Notice that keys must be of immutable data-type: so ok `str`, `int`, `float`... but not `list` (because they can be modified in place)

```
[93]: d1 = {
      10: 1,
      20: 2,
      30: 3
      }
      d1
```

```
[93]: {10: 1, 20: 2, 30: 3}
```

If you try to use lists as keys of a dictionary you get

```
TypeError: unhashable type: 'list'
```

```
[94]: # d2 = {  
#     ["AAA"]: 5,  
#     ['A+']: 20,  
#     ['BBB']: 50,  
#     ['D']: 100  
# }
```

Another difference from lists is that dicts are not ordered (don't have memory of the order in which the list of key: value pairs has been inputted) and, in general, cannot be sorted. In particular, there is not such indexing like `dictName[0]`, `dictName[1]`, or so, simply because there is no guarantee that the first pair that we put in input is actually stored in the first position (whatever *first-position* could mean) and that could be retrieved accordingly.

3.2 key-based indexing

Indexing in dictionaries is implemented through their keys. Once you know the key, you can retrieve the corresponding value as `dictName[key]`. Like this:

```
[95]: d
```

```
[95]: {'AAA': 5, 'A+': 20, 'BBB': 50, 'D': 100}
```

```
[96]: d["AAA"]
```

```
[96]: 5
```

Once we have a dict, representing a map key-to-value, we typically want to look whether a key is in the dictionary:

```
[97]: key_list = ["AAA", "AA", "B+", "D"]  
  
for key in key_list:  
    if key in d:  
        print("key {} found".format(key))  
    else:  
        print("key {} not found".format(key))
```

```
key AAA found  
key AA not found  
key B+ not found  
key D found
```

Notice that if you try to access a dictionary with a key it does not have, you are going to receive a `KeyError` simply stating that that key is not part of the dictionary's keys.

```
[98]: d
```

```
[98]: {'AAA': 5, 'A+': 20, 'BBB': 50, 'D': 100}
```

```
[99]: # raises KeyError
      # d["B+"]
```

3.3 Changing Values

If you want to change a value corresponding to a given key, you just assign to it a new value:

```
dictName[key] = newValue
```

```
[100]: d["AAA"] = 1
      d
```

```
[100]: {'AAA': 1, 'A+': 20, 'BBB': 50, 'D': 100}
```

3.4 Built-in methods

Some useful methods: - `dict.keys()` returns a sequence of dict keys; - `dict.values()` returns a sequence of dict values; - `dict.items()` returns a sequence of key: value pairs packed as tuples

```
[101]: d.keys()
```

```
[101]: dict_keys(['AAA', 'A+', 'BBB', 'D'])
```

```
[102]: d.values()
```

```
[102]: dict_values([1, 20, 50, 100])
```

```
[103]: d.items()
```

```
[103]: dict_items([('AAA', 1), ('A+', 20), ('BBB', 50), ('D', 100)])
```

3.5 Looping over dicts

Looping can be done in several ways. The basic one is looping over the keys of the dictionary, which can be done in this way:

```
[104]: for key in d:
      print("key: {} - value: {}".format(key, d[key]))
```

```
key: AAA - value: 1
key: A+ - value: 20
key: BBB - value: 50
key: D - value: 100
```

The interpreter finds out that `d` is a dictionary and understands that it has to look for its keys and loop over them, assigning each time to `key` variable.

4 Sets

`Sets` consists of an unordered collection with no duplicate elements.

Sets are typically used to store unique values and to check whether a value is in there. Plus basic sets operations like union, intersection, etc...

4.1 Definition

Sets are defined with curly brackets `{}` surrounding a `,`-separated list

```
[105]: my_set = {1, 2, 2, 4, 6, 6}
my_set
```

```
[105]: {1, 2, 4, 6}
```

Alternatively you can use the key-word `set()`

```
[106]: my_set = set([1, 2, 2, 4, 6, 6])
my_set
```

```
[106]: {1, 2, 4, 6}
```

Notice how repeated values are automatically counted only one.

4.2 Test for membership

Checking whether an element is in the set can be done easily:

```
[107]: element_list = [i for i in range(10)]
element_list
for element in element_list:
    if element in my_set:
        print("element {} found".format(element))
    else:
        print("element {} not found".format(element))
```

```
element 0 not found
element 1 found
element 2 found
element 3 not found
element 4 found
element 5 not found
element 6 found
element 7 not found
element 8 not found
element 9 not found
```

```
[108]: element_list
```



```
[108]: [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

4.3 Set operations

Let's review basic set operations:

```
[109]: set1 = set([i for i in range(10)])    # yes, you can use list comprehension here
      set2 = {i**2 for i in range(10)}      # yes, this is another way to create a set
      ↪ set: "set-comprehension"
```

```
[110]: set1
```

```
[110]: {0, 1, 2, 3, 4, 5, 6, 7, 8, 9}
```

```
[111]: set2
```

```
[111]: {0, 1, 4, 9, 16, 25, 36, 49, 64, 81}
```

4.3.1. .union() The union of two sets is the set of elements in `set1`, `set2`, or both

```
[112]: set1.union(set2)
```

```
[112]: {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 16, 25, 36, 49, 64, 81}
```

or alternatively

```
[113]: set1 | set2
```

```
[113]: {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 16, 25, 36, 49, 64, 81}
```

4.3.2. .intersection() The intersection of two sets is the set of elements in common between `set1` and `set2`

```
[114]: set1.intersection(set2)
```

```
[114]: {0, 1, 4, 9}
```

or alternatively

```
[115]: set1 & set2
```

```
[115]: {0, 1, 4, 9}
```

4.3.3. .difference() The difference of two sets is the set of elements in `set1` but not in `set2`

```
[116]: set1.difference(set2) # notice that is different from set2.difference(set1)
```

```
[116]: {2, 3, 5, 6, 7, 8}
```

or alternatively

```
[117]: set1 - set2
```

```
[117]: {2, 3, 5, 6, 7, 8}
```

4.4 Getting rid of duplicates from a list

To conclude, often sets are used to get rid of duplicates in a list:

```
[118]: lis = [(-1)**n for n in range(10)]  
lis
```

```
[118]: [1, -1, 1, -1, 1, -1, 1, -1, 1, -1]
```

```
[119]: set(lis)
```

```
[119]: {-1, 1}
```