

We have pre-calculated the order in which the flight arrive in each node  $x \in V$ , and we say that, if there is a conflict, then  $x_{i,j} = 0$  means that  $x_{j,i} = 1$  and then that the flight  $i$  pass before flight  $j$ , if there are no conflict  $x_{i,j} = x_{j,i} = 1$

**Require:** graph  $G = (V, E)$ , set of flight  $F$ , path of each flight  $P_i \forall i \in F$ , conflict variable  $x_{i,j}$  (see above),  $t(s, i) \forall i \in F, \forall s(P_i)$  starting time for the initial node of the path

**Ensure:** earliest time an arc can come to a node  $v \in V$

{calculate the number number of conflict between two flights}

$Mc \leftarrow 0$

**for all**  $i \in F$  **do**

**for all**  $j \in F$  **do**

$tmp \leftarrow |P_i \cap P_j|$

**if**  $tmp > Mc$  **then**

$Mc \leftarrow tmp$

**end if**

**end for**

**end for**

{define t}

**for all**  $i \in F$  **do**

**for all**  $x \in V : x \notin s(P_i)$  **do**

$t(x, i) = -1$

**end for**

**end for**

{propagation of time}

**for**  $|F|^{Mc}$  **do**

**for all**  $i \in F$  **do**

**for**  $(x, y) \in P_i$  **do**

**if**  $\exists j \in F : y_{i,j} = 0$  **then**

**if**  $t(y, j) = -1$  **then**

**break**

**else**

                propagate time s.t. it's far enough from the conflict {}

**end if**

**else**

            propagate time  $\{t(y, i) \leftarrow t(x, i) + \frac{d}{v_{\min}}\}$

**end if**

**end for**

**end for**

**end for**

TODO: check if the next function it's working, with  $d$  the distance,  $s$  the maximum percentage change,  $v_{i,j,z}$  the speed of the arc  $(i, j) \in A$  and flight  $z$ ,  $D$  the safety distance ( $\underline{t}, \bar{t}$  are the min and max safaty time)

$$\forall i \in F, \forall (x, y) \in A$$

$$\begin{aligned} \bar{t}_{i,y} &= \begin{cases} \bar{t}_{i,x} + \dots \frac{d}{\max\{\underline{v}_{i,y}, (1-s)*v_{x,y,i}\}} & \text{if } \nexists j \in F : y_{i,j} \neq 1 \\ \bar{t}_{j,y} + \dots & \text{if } \exists j \in F : y_{i,j} = 1 \end{cases} \\ \underline{t}_{i,y} &= \begin{cases} \underline{t}_{i,x} + \frac{d}{\min\{\bar{v}_{i,y}, (1+s)*v_{x,y,i}\}} & \text{if } \nexists j \in F : y_{i,j} \neq 1 \\ \underline{t}_{j,y} + \dots & \text{if } \exists j \in F : y_{i,j} = 1 \end{cases} \end{aligned}$$

Possibili miglorie da inserire:

Per ogni volo, mettere in un buffer l'arco/l'ultimo nodo definito

Idee propagazione:

usare range permesso, quindi impostare nei nodi di conflitto le velocità e trattare negli altri posti tramite propagazione raggiungere gli altri, per i successivi non è un problema dato che dobbiamo attendere quelli che vengono prima.

For latest time, just use inverse the order of the path and some other small differences.