

## Standard Integration formulas

$$(1) \quad \int x^k dx = \frac{1}{k+1} x^{k+1} \quad (k \neq -1);$$

$$(2) \quad \int \frac{1}{x} dx = \ln |x|;$$

$$(3) \quad \int e^{ax} dx = \frac{1}{a} e^{ax};$$

$$(4) \quad \int \sin x dx = -\cos x$$

$$(5) \quad \int \cos x dx = \sin x;$$

$$(6) \quad \int \sec x dx = \ln |\sec x + \tan x|;$$

$$(7) \quad \int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \left( \frac{x}{a} \right);$$

$$(8) \quad \int \frac{x}{a^2 + x^2} dx = \frac{1}{2} \ln(a^2 + x^2);$$

$$(9) \quad \int \frac{1}{a^2 - x^2} dx = \frac{1}{2a} \ln \left| \frac{a+x}{a-x} \right|;$$

$$(10) \quad \int \frac{1}{\sqrt{x^2 + a^2}} dx = \ln \left| x + \sqrt{x^2 + a^2} \right|;$$

$$(11) \quad \int \frac{1}{\sqrt{x^2 - a^2}} dx = \ln \left| x + \sqrt{x^2 - a^2} \right|;$$

$$(12) \quad \int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \left( \frac{x}{a} \right);$$

$$(13) \quad \int \sqrt{x^2 + a^2} dx = \frac{1}{2} x \sqrt{x^2 + a^2} + \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 + a^2} \right|;$$

$$(14) \quad \int \sqrt{x^2 - a^2} dx = \frac{1}{2} x \sqrt{x^2 - a^2} - \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 - a^2} \right|;$$

$$(15) \quad \int \sqrt{a^2 - x^2} dx = \frac{1}{2} x \sqrt{a^2 - x^2} + \frac{1}{2} a^2 \sin^{-1} \left( \frac{x}{a} \right);$$

$$(16) \quad \int \ln x dx = x \ln x - x;$$

$$(17) \quad \int e^{ax} \cos bx dx = e^{ax} \left[ \frac{a \cos bx + b \sin bx}{a^2 + b^2} \right];$$

$$(18) \quad \int e^{ax} \sin bx dx = e^{ax} \left[ \frac{a \sin bx - b \cos bx}{a^2 + b^2} \right].$$

## Some reduction formulas

- (1)  $\int \sin^n x \, dx = -\frac{\cos x \sin^{n-1} x}{n} + \frac{n-1}{n} \int \sin^{n-2} x \, dx;$
- (2)  $\int \cos^n x \, dx = \frac{\sin x \cos^{n-1} x}{n} + \frac{n-1}{n} \int \cos^{n-2} x \, dx;$
- (3)  $\int \tan^n x \, dx = \frac{\tan^{n-1} x}{n-1} - \int \tan^{n-2} x \, dx, (n > 1);$
- (4)  $\int \sec^n x \, dx = \frac{\sec^{n-2} x \tan x}{n-1} + \frac{n-2}{n-1} \int \sec^{n-2} x \, dx, (n > 1);$
- (5)  $\int e^{ax} x^n \, dx = \frac{e^{ax} x^n}{a} - \frac{n}{a} \int e^{ax} x^{n-1} \, dx;$
- (6)  $\int \frac{a^2}{(x^2 + a^2)^n} dx = \frac{1}{(2n-2)} \frac{x}{(x^2 + a^2)^{n-1}} + \frac{2n-3}{(2n-2)} \int \frac{1}{(x^2 + a^2)^{n-1}} dx, (n > 1).$

## Some trigonometric identities

- (1)  $\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y;$
- (2)  $\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y;$
- (3)  $\tan(x \pm y) = \frac{\tan x \pm \tan y}{1 \mp \tan x \tan y};$
- (4)  $\sin x \cos y = \frac{1}{2} [\sin(x+y) + \sin(x-y)];$
- (5)  $\cos x \cos y = \frac{1}{2} [\cos(x+y) + \cos(x-y)];$
- (6)  $\sin x \sin y = \frac{1}{2} [\cos(x-y) - \cos(x+y)].$

## Area, Arc Length, Volume

1. Area between two curves:  $\int_a^b |f(x) - g(x)| dx$
2. Arc length:  $\int_a^b \sqrt{1 + [f'(x)]^2} dx$
3. Volume, revolution about the  $x$ -axis:  $\pi \int_a^b [R(x)^2 - r(x)^2] dx,$   
 revolution about the  $y$ -axis:  $2\pi \int_a^b x|f(x) - g(x)| dx$
4. Surface area, revolution about the  $x$ -axis:  $2\pi \int_a^b f(x) \sqrt{1 + [f'(x)]^2} dx$