量子物理练习答案

1, C 2, B 3, A 4, D 5, 0.268 (=
$$2 - \sqrt{3}$$
) 6, 2.55, 4

7.
$$\sqrt{\frac{h}{2m(v-v_0)}}$$
 8. 1.51 9. 1:1 4:1 10. $hc(\frac{1}{\lambda_0} - \frac{1}{\lambda})$

11、解: 根据维恩位移定律: $T\lambda_m = b$ \implies

太阳:
$$T_1 = \frac{b}{\lambda_{m1}} = 5.27 \times 10^3 \text{ K}$$

北极星:
$$T_2 = \frac{b}{\lambda_{m2}} = 8.28 \times 10^3 \,\mathrm{K}$$

天狼星:
$$T_3 = \frac{b}{\lambda_{m^3}} = 9.99 \times 10^3 \,\mathrm{K}$$

12、解:
$$\begin{cases} M_B = \sigma T^4 \\ \lambda_m T = b \end{cases} \Rightarrow \frac{M_{B2}}{M_{B1}} = (\frac{T_2}{T_1})^4 = (\frac{\lambda_{m1}}{\lambda_{m2}})^4 = 3.63$$

13、解: 爱因斯坦光电效应方程:
$$hv = \frac{1}{2}mv^2 + w$$

(1)
$$w = \frac{hc}{\lambda_0} = 3.2 \times 10^{-19} (J)$$

(2)
$$eU_a = \frac{1}{2}mv^2 = hv - w = h\frac{c}{\lambda} - w \implies U_a = \frac{h\frac{c}{\lambda} - w}{e} = 3.65 \text{ (V)}$$

14、解: 求解本题只需理解康普顿效应公式的意义就可代公式得结果

(1)
$$\Delta \lambda = \lambda - \lambda_0 = \frac{2h}{m_0 c} \sin^2 \frac{\theta}{2} = 0.012 \times 10^{-10} \text{ m}$$
 $\lambda = \lambda_0 + \Delta \lambda = 1.012 \times 10^{-10} \text{ m}$

(2) 由于散射能量守恒,光子的能量损失就是电子获得的动能,得

$$E_k = h v_0 - h v = hc(\frac{1}{\lambda_0} - \frac{1}{\lambda}) = 2.36 \times 10^{-17} \text{ J} = 148 \text{ eV}$$

(1)
$$\frac{1}{2}mv^2 = hv - w = h\frac{c}{\lambda} - w = 3.2 \times 10^{-19} \text{ (J)}$$

(2)
$$eU_a = \frac{1}{2}mv^2 \implies U_a = 2.0(V)$$

(3)
$$\frac{hc}{\lambda_0} = w \implies \lambda_0 = 2.96 \times 10^{-7} \text{ (m)}$$

16.
$$Mathebox{ } M: \ dP = |\psi|^2 dx = \frac{2}{a} \sin^2 \frac{\pi x}{a} dx$$

粒子位于 0-a/4内的概率为:

$$P = \int_{0}^{a/4} \frac{2}{a} \sin^2 \frac{\pi x}{a} dx = \frac{2}{\pi} \left[\frac{\pi x}{2a} - \frac{1}{4} \sin \frac{2\pi x}{a} \right] \Big|_{0}^{a/4} = \frac{1}{4} - \frac{1}{2\pi} = 0.091$$