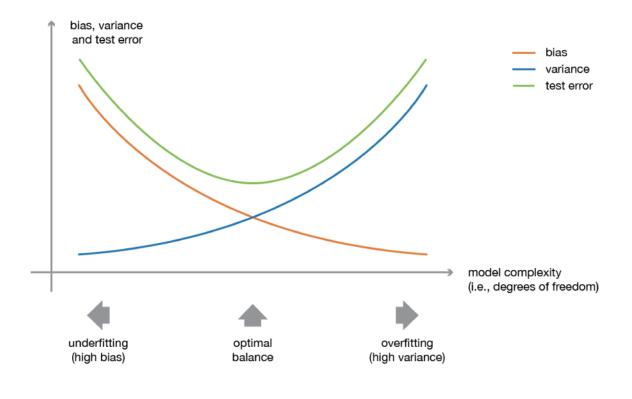
# Ensemble learning: bagging, boosting and stacking

These methods are **Ensemble learning** techniques. These models are machine learning paradigms where multiple models (often called "weak learners") are trained to **solve the same problem** and **combined** to get **better** results. The main hypothesis is that when **weak models** are **correctly combined** we can obtain **more accurate and/or robust models**.

# Single weak learner

In machine learning, no matter if we are facing a classification or a regression problem, the choice of the model is extremely important to have any chance to obtain good results. This choice can depend on many variables of the problem: quantity of data, dimensionality of the space, distribution hypothesis...

A **low bias and a low variance**, although they most often vary in opposite directions, are the **two most fundamental features** expected for a model. Indeed, to be able to "solve" a problem, we want our model to have **enough degrees of freedom** to resolve the underlying complexity of the data we are working with, but we also want it to have **not too much degrees of freedom** to avoid **high variance** and be **more robust**. This is the well known **bias-variance tradeoff**.



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Illustration of the bias-variance tradeoff.

In ensemble learning theory, we call **weak learners** (or **base models**) models that can be used as building blocks for designing more complex models by **combining several of them**. Most of the time, these basics models **perform not so well** by themselves either because they have a **high bias** (low

degree of freedom models, for example) **or** because they have **too much variance** to be robust (high degree of freedom models, for example). Then, the idea of ensemble methods is to combining several of them together in order to create a **strong learner** (or **ensemble model**) that achieves better performances.

Usually, ensemble models are used in order to:

- decrease the variance for bagging (Bootstrap Aggregating) technique
- reduce bias for the boosting technique
- improving the predictive force for stacking technique.

To understand these techniques, first, we will explore what is boostrapping and its different **hypothesis**.

## **Bagging**

In **parallel methods** we fit the different considered learners independently from each others and, so, it is possible to train them concurrently. The most famous such approach is "bagging" (standing for "bootstrap **agg**regating") that aims at producing an ensemble model that is **more robust** than the individual models composing it.

When training a model, no matter if we are dealing with a classification or a regression problem, we obtain a function that takes an input, returns an output and that is defined with respect to the training dataset.

The idea of bagging is then simple: we want to fit several independent models and "average" their predictions in order to obtain a model with a lower variance. However, we can't, in practice, fit fully independent models because it would require too much data. So, we rely on the good "approximate properties" of bootstrap samples (representativity and independence) to fit models that are almost independent.

First, we create **multiple bootstrap samples** so that each new bootstrap sample will act as another (almost) independent dataset drawn from true distribution. Then, we can **fit a weak learner for each of these samples and finally aggregate them such that we kind of "average" their outputs** and, so, obtain an ensemble model with **less variance** that its components. Roughly speaking, as the bootstrap samples are approximatively **independent and identically distributed (i.i.d.)**, so are the learned base models. Then, **"averaging" weak learners outputs** do not change the expected answer but reduce its variance.

So, assuming that we have L bootstrap samples (approximations of L independent datasets) of size B denoted

$$\{z_1^1, z_2^1, ..., z_B^1\}, \{z_1^2, z_2^2, ..., z_B^2\}, ..., \{z_1^L, z_2^L, ..., z_B^L\} \\ \qquad z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\ z_b^l \equiv b \text{-th observation of the $l$-th bootstrap sample } \\$$

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Each {....} is a bootstrap sample of B observation

we can fit L almost independent weak learners (one on each dataset)

$$w_1(.), w_2(.), ..., w_L(.)$$

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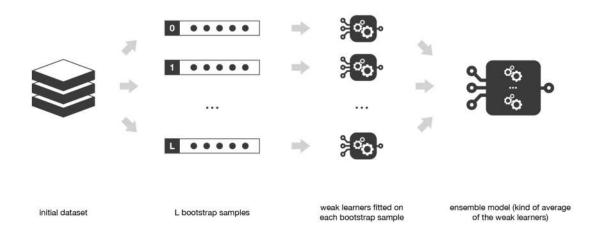
and then aggregate them into some kind of averaging process in order to get an ensemble model with a lower variance. For example, we can define our strong model such that

$$s_L(.) = \frac{1}{L} \sum_{l=1}^{L} w_l(.)$$
 (simple average, for regression problem)  
 $s_L(.) = \underset{k}{\operatorname{arg max}} [\operatorname{card}(l|w_l(.) = k)]$  (simple majority vote, for classification problem)

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There are several possible ways to aggregate the multiple models fitted in parallel. - For a **regression problem**, the outputs of individual models can literally be **averaged** to obtain the output of the ensemble model. - For **classification problem** the class outputted by each model can be seen as a **vote** and the class that receives the **majority of the votes** is returned by the ensemble model (this is called **hard-voting**). Still for a classification problem, we can **also** consider the **probabilities of each classes** returned by all the models, **average these probabilities** and keep the class with the **highest average probability** (this is called **soft-voting**). -> Averages or votes can either be simple or weighted if any relevant weights can be used.

Finally, we can mention that one of the big advantages of bagging is that **it can be parallelised**. As the different models are fitted independently from each others, intensive parallelisation techniques can be used if required.



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Bagging consists in fitting several base models on different bootstrap samples and build an ensemble model that "average" the results of these weak learners.

Question: - Can you name an algorithms based on Bagging technique, Hint: leaf

##### Examples

Here, we are trying some example of **stacking** 

Bagged Decision Trees for Classification

```
import pandas
from sklearn import model selection
from sklearn.ensemble import BaggingClassifier
from sklearn.tree import DecisionTreeClassifier
names = ['preg', 'plas', 'pres', 'skin', 'test', 'mass', 'pedi', 'age', 'class']
dataframe = pandas.read_csv("https://raw.githubusercontent.com/jbrownlee/Datasets/master/pin
array = dataframe.values
x = array[:,0:8]
y = array[:,8]
max_features = 3
kfold = model selection.KFold(n splits=10, random state=2020)
rf = DecisionTreeClassifier(max_features=max_features)
num_trees = 100
model = BaggingClassifier(base_estimator=rf, n_estimators=num_trees, random_state=2020)
results = model selection.cross val score(model, x, y, cv=kfold)
print("Accuracy: \%0.2f (+/- \%0.2f)" % (results.mean(), results.std()))
```

Random Forest Classification

```
import pandas
from sklearn import model_selection
from sklearn.ensemble import RandomForestClassifier
names = ['preg', 'plas', 'pres', 'skin', 'test', 'mass', 'pedi', 'age', 'class']
dataframe = pandas.read_csv("https://raw.githubusercontent.com/jbrownlee/Datasets/master/pin
array = dataframe.values
x = array[:,0:8]
y = array[:,8]
kfold = model_selection.KFold(n_splits=10, random_state=2020)
rf = DecisionTreeClassifier()
num_trees = 100
max features = 3
kfold = model selection.KFold(n splits=10, random state=2020)
model = RandomForestClassifier(n_estimators=num_trees, max_features=max_features)
results = model_selection.cross_val_score(model, x, y, cv=kfold)
\label{eq:print("Accuracy: $\%0.2f (+/- \%0.2f)" % (results.mean(), results.std()))} \\
```

Both of these algorithms will print, Accuracy: 0.77 (+/- 0.07). They are equivalent.

# **Boosting**

In **sequential methods** the different combined weak models are **no longer** fitted **independently** from each others. The idea is to fit models **iteratively** such that the training of model at a given step depends on the models fitted at the previous steps. "Boosting" is the most famous of these approaches and it produces an ensemble model that is in general **less biased** than the weak learners that compose it.

**Boosting** methods work in the same **spirit** as **bagging** methods: we build a **family of models** that are **aggregated** to obtain a strong learner that performs better.

However, unlike bagging that mainly aims at reducing variance, boosting is a technique that consists in fitting sequentially multiple weak learners in a very adaptative way: each model in the sequence is fitted giving more importance to observations in the dataset that were badly handled by the previous models in the sequence. Intuitively, each new model focus its efforts on the most difficult observations to fit up to now, so that we obtain, at the end of the process, a strong learner with lower bias (even if we can notice that boosting can also have the effect of reducing variance).

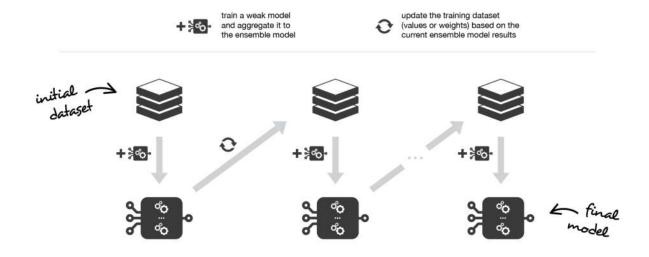
-> Boosting, like bagging, can be used for regression as well as for classification problems.

Being mainly focused at reducing bias, the base models that are often considered for boosting are\*
\*models with low variance but high bias. For example, if we want to usetreesas our base models,
we will choose most of the time shallow decision trees with only a few depths.\*\*

Another important reason that motivates the use of low variance but high bias models as weak learners for boosting is that these models are in general less computationally expensive to fit (few degrees of freedom when parametrised). Indeed, as computations to fit the different models **can't be done in parallel** (unlike bagging), it could become too expensive to fit sequentially several complex models.

Once the weak learners have been chosen, we still need to define **how** they will be sequentially **fitted** and **how** they will be **aggregated**. We will discuss these questions in the two following subsections, describing more especially two important boosting algorithms: **adaboost** and **gradient boosting**.

In a nutshell, these two meta-algorithms **differ** on how they **create and aggregate** the weak learners during the sequential process. **Ada**ptive **boosting updates the weights attached to each of the training dataset observations** whereas **gradient boosting updates the value of these observations**. This main difference comes from the way both methods try to **solve the optimisation** problem of finding the best model that can be written as a weighted sum of weak learners.



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Boosting consists in, iteratively, fitting a weak learner, aggregate it to the ensemble model and "update" the training dataset to better take into account the strengths and weakness of the current ensemble model when fitting the next base model.

## 1/ Adaptative boosting

In adaptative boosting (often called "adaboost"), we try to define our ensemble model as a weighted sum of L weak learners

$$s_L(.) = \sum_{l=1}^{L} c_l \times w_l(.)$$
 where  $c_l$ 's are coefficients and  $w_l$ 's are weak learners

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Finding the best ensemble model with this form is a difficult optimisation problem. Then, **instead** of trying to **solve it in one single shot** (finding all the coefficients and weak learners that give the best overall additive model), we make use of an **iterative optimisation process** that is much more tractable, even if it can lead to a sub-optimal solution. More especially, we **add** the **weak learners one by one**, looking at each iteration for the **best possible pair** (**coefficient, weak learner**) to add to the current ensemble model. In other words, we define recurrently the (s\_1)'s such that

$$s_l(.) = s_{l-1}(.) + c_l \times w_l(.)$$

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where c\_l and w\_l are chosen such that s\_l is the model that fit the best the training data and, so, that is the **best possible improvement over s\_(l-1)**. We can then denote

$$(c_{l}, w_{l}(.)) = \underset{c, w(.)}{\operatorname{arg \, min}} E(s_{l-1}(.) + c \times w(.)) = \underset{c, w(.)}{\operatorname{arg \, min}} \sum_{n=1}^{N} e(y_{n}, s_{l-1}(x_{n}) + c \times w(x_{n}))$$

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where E(.) is the fitting error of the given model and e(.,.) is the loss/error function. Thus, instead of optimising "globally" over all the L models in the sum, we **approximate the optimum by optimising** "**locally**" building and adding the weak learners to the strong model one by one.

More especially, when considering a **binary classification**, we can show that the adaboost algorithm can be re-written into a process that proceeds as follow. First, it updates the **observations weights** in the dataset and train a new weak learner with a **special focus** given to the **observations misclassified** by the current ensemble model. Second, it adds the weak learner to the weighted sum according to an update coefficient that expresse the performances of this weak model: **the better a weak learner performs**, **the more it contributes to the strong learner**.

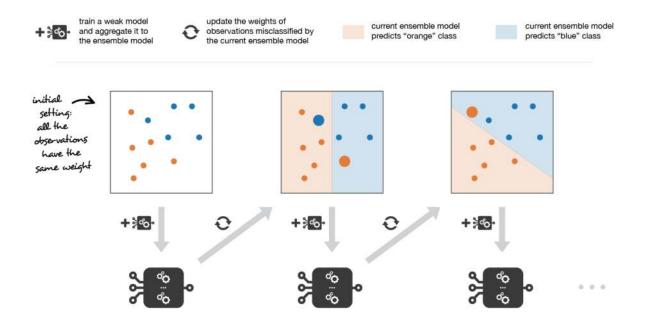
So, assume that we are facing a **binary classification** problem, with **N** observations in our dataset and we want to use **adaboost** algorithm with a given family of weak models. At the **very beginning** of the algorithm (first model of the sequence), **all the observations have the same weights 1/N**. Then, we **repeat L times (for the L learners in the sequence)** the following steps:

• fit the best possible weak model with the current observations weights

- compute the value of the update coefficient that is some kind of scalar evaluation metric of the weak learner that indicates how much this weak learner should be taken into account into the ensemble model
- · update the strong learner by adding the new weak learner multiplied by its update coefficient
- compute new observations weights that expresse which observations we would like to focus on at the next iteration (weights of observations wrongly predicted by the aggregated model increase and weights of the correctly predicted observations decrease)

Repeating these steps, we have then build **sequentially** our **L models** and **aggregate** them into a **simple linear combination weighted by coefficients expressing the performance of each learner.** 

**Notice** that there exists variants of the initial adaboost algorithm such that LogitBoost (classification) or L2Boost (regression) that mainly differ by their choice of loss function.



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Adaboost updates weights of the observations at each iteration. Weights of well classified observations decrease relatively to weights of misclassified observations. Models that perform better have higher weights in the final ensemble model.

## 2/ Gradient boosting

In gradient boosting, the ensemble model we try to build is also a weighted sum of weak learners

$$s_L(.) = \sum_{l=1}^{L} c_l \times w_l(.)$$
 where  $c_l$ 's are coefficients and  $w_l$ 's are weak learners

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Just as we mentioned for adaboost, finding the optimal model under this form is too difficult and an iterative approach is required. The main difference with adaptative boosting is in the definition of the sequential optimisation process. Indeed, gradient boosting casts the problem into a gradient descent one: at each iteration we fit a weak learner to the opposite of the gradient of the current fitting error with respect to the current ensemble model. Let's try to clarify this last point. First, theoretical gradient descent process over the ensemble model can be written

$$s_l(.) = s_{l-1}(.) - c_l \times \nabla_{s_{l-1}} E(s_{l-1})(.)$$

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where E(.) is the fitting error of the given model, c\_l is a coefficient corresponding to the step size and

$$-\nabla_{s_{l-1}}E(s_{l-1})(.)$$

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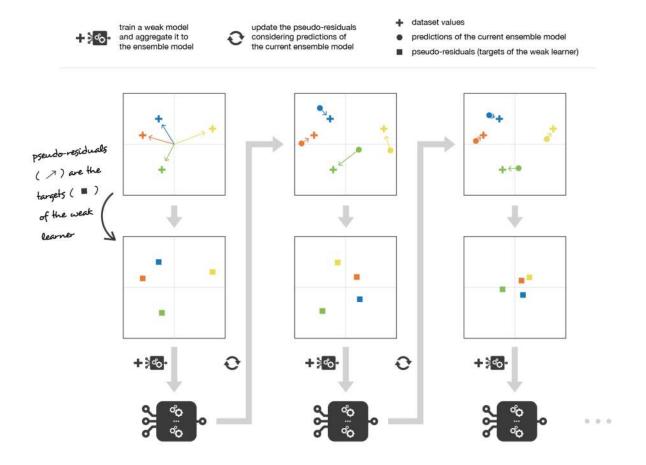
This entity is the **opposite of the gradient of the fitting error with respect to the ensemble model at step l-1**. This opposite of the gradient is a function that can, in practice, only be evaluated for observations in the training dataset (for which we know inputs and outputs): these evaluations are called pseudo-residuals attached to each observations. Moreover, even if we know for the observations the values of these pseudo-residuals, we don't want to add to our ensemble model any kind of function: we only want to add a new instance of weak model. So, the natural thing to do is to fit a weak learner to the pseudo-residuals computed for each observation. Finally, the coefficient c\_l is computed following a one dimensional optimisation process (line-search to obtain the best step size c\_l).

So, assume that we want to use gradient boosting technique with a given family of weak models. At the very beginning of the algorithm (first model of the sequence), the pseudo-residuals are set equal to the observation values. Then, we repeat L times (for the L models of the sequence) the following steps:

- fit the best possible weak model to pseudo-residuals (approximate the opposite of the gradient with respect to the current strong learner)
- compute the value of the optimal step size that defines by how much we update the ensemble model in the direction of the new weak learner
- update the ensemble model by adding the new weak learner multiplied by the step size (make a step of gradient descent)
- compute new pseudo-residuals that indicate, for each observation, in which direction we would like to
  update next the ensemble model predictions

Repeating these steps, we have then build sequentially our L models and aggregate them **following a** gradient descent approach. Notice that, while adaptative boosting tries to solve at each iteration exactly the "local" optimisation problem (find the best weak learner and its coefficient to add to the strong model), gradient boosting uses instead a gradient descent approach and can more easily be adapted to large number of loss functions. Thus, gradient boosting can be considered as a generalization of adaboost to arbitrary differentiable loss functions.

Note There is an algorithm which gained huge popularity after a **Kaggle's competitions**. It is **XGBoost** (Extreme Gradient Boosting). This is a gradient boosting algorithm which has more flexibility (varying number of terminal nodes and left weights) parameters to avoid sub-learners correlations. Having these important qualities, **XGBOOST** is one of the most used algorithm in data science. **LIGHTGBM** is a recent implementation of this algorithm. It was published by **Microsoft** and it gives us the same scores (if parameters are equivalents) but it runs **quicker** than a classic **XGBOOST**.



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Gradient boosting updates values of the observations at each iteration. Weak learners are trained to fit the pseudo-residuals that indicate in which direction to correct the current ensemble model predictions to lower the error.

#### **Examples**

Here, we are trying an example of **Boosting** and compare it to a **Bagging**. Both of algorithms take the same weak learners to build the macro-model

· Adaboost Classifier

```
from sklearn.ensemble import AdaBoostClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import load_breast_cancer
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
```

```
from sklearn.metrics import confusion matrix
from sklearn.preprocessing import LabelEncoder
from sklearn.metrics import accuracy score
from sklearn.metrics import f1_score
breast_cancer = load_breast_cancer()
x = pd.DataFrame(breast cancer.data, columns=breast cancer.feature names)
y = pd.Categorical.from_codes(breast_cancer.target, breast_cancer.target_names)
# Transforming string Target to an int
encoder = LabelEncoder()
binary_encoded_y = pd.Series(encoder.fit_transform(y))
#Train Test Split
train_x, test_x, train_y, test_y = train_test_split(x, binary_encoded_y, random_state=1)
clf_boosting = AdaBoostClassifier(
    DecisionTreeClassifier(max_depth=1),
    n estimators=200
)
clf boosting.fit(train x, train y)
predictions = clf_boosting.predict(test_x)
print("For Boosting : F1 Score {}, Accuracy {}".format(round(f1_score(test_y,predictions),2)
```

## • Random Forest as a bagging classifier

```
from sklearn.ensemble import AdaBoostClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import load_breast_cancer
import pandas as pd
import numpy as np
from sklearn.model_selection import train test_split
from sklearn.metrics import confusion_matrix
from sklearn.preprocessing import LabelEncoder
from sklearn.metrics import accuracy score
from sklearn.metrics import f1 score
from sklearn.ensemble import RandomForestClassifier
breast cancer = load breast cancer()
x = pd.DataFrame(breast_cancer.data, columns=breast_cancer.feature_names)
y = pd.Categorical.from_codes(breast_cancer.target, breast_cancer.target_names)
# Transforming string Target to an int
encoder = LabelEncoder()
binary encoded y = pd.Series(encoder.fit transform(y))
#Train Test Split
train_x, test_x, train_y, test_y = train_test_split(x, binary_encoded_y, random_state=1)
clf bagging = RandomForestClassifier(n estimators=200, max depth=1)
clf_bagging.fit(train_x, train_y)
predictions = clf bagging.predict(test x)
print("For Bagging : F1 Score {}, Accuracy {}".format(round(f1_score(test_y,predictions),2),
```

#### Comparaison

Metric	Bagging Boosting	
Accuracy	0.91	0.97
F1-Score	0.88	0.95

# Overview of stacking

**Stacking** mainly **differ** from **bagging and boosting** on two points: - First stacking often considers **heterogeneous weak learners** (different learning algorithms are combined) whereas bagging and boosting consider mainly homogeneous weak learners. - Second, stacking learns to combine the base models using a **meta-model** whereas bagging and boosting combine weak learners following deterministic algorithms.

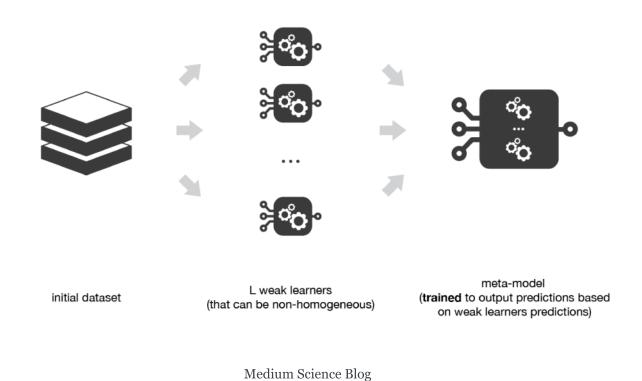
As we already mentioned, the idea of stacking is to learn several different weak learners and **combine them by training a meta-model** to output predictions based on the multiple predictions returned by these weak models. So, we need to define two things in order to build our stacking model: the L learners we want to fit and the meta-model that combines them.

For example, for a classification problem, we can choose as weak learners a KNN classifier, a logistic regression and a SVM, and decide to learn a neural network as meta-model. Then, the neural network will take as inputs the outputs of our three weak learners and will learn to return final predictions based on it.

So, assume that we want to fit a stacking ensemble composed of L weak learners. Then we have to follow the steps thereafter:

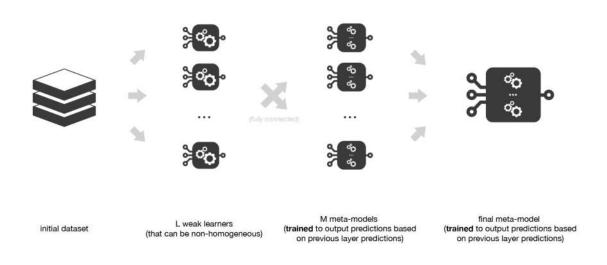
- split the training data in two folds
- choose L weak learners and fit them to data of the first fold
- for each of the L weak learners, make predictions for observations in the second fold
- fit the meta-model on the second fold, using predictions made by the weak learners as inputs

In the previous steps, we split the dataset in two folds because predictions on data that have been used for the training of the weak learners are **not relevant for the training of the meta-model**.



Stacking consists in training a meta-model to produce outputs based on the outputs returned by some lower layer weak learners.

A possible extension of stacking is multi-level stacking. It consists in doing **stacking with multiple layers**. As an example,



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Multi-level stacking considers several layers of stacking: some meta-models are trained on outputs returned by lower layer meta-models and so on. Here we have represented a 3-layers stacking model.

## **Examples**

Here, we are trying an example of **Stacking** and compare it to a **Bagging** & a **Boosting**. We note that, many other applications (datasets) would show more difference between these techniques.

```
from sklearn.ensemble import AdaBoostClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import load_breast_cancer
import pandas as pd
import numpy as np
from sklearn.model selection import train test split
from sklearn.metrics import confusion_matrix
from sklearn.preprocessing import LabelEncoder
from sklearn.metrics import accuracy score
from sklearn.metrics import f1_score
from sklearn.ensemble import RandomForestClassifier
from sklearn.linear_model import LogisticRegression
breast_cancer = load_breast_cancer()
x = pd.DataFrame(breast cancer.data, columns=breast cancer.feature names)
y = pd.Categorical.from_codes(breast_cancer.target, breast_cancer.target_names)
# Transforming string Target to an int
encoder = LabelEncoder()
binary_encoded_y = pd.Series(encoder.fit_transform(y))
#Train Test Split
train_x, test_x, train_y, test_y = train_test_split(x, binary_encoded_y, random_state=2020)
```

```
boosting clf ada boost= AdaBoostClassifier(
    DecisionTreeClassifier(max depth=1),
    n estimators=3
)
bagging clf rf = RandomForestClassifier(n estimators=200, max depth=1,random state=2020)
clf rf = RandomForestClassifier(n estimators=200, max depth=1,random state=2020)
clf ada boost = AdaBoostClassifier(
    DecisionTreeClassifier(max depth=1, random state=2020),
    n estimators=3
)
clf_logistic_reg = LogisticRegression(solver='liblinear',random_state=2020)
#Customizing and Exception message
class NumberOfClassifierException(Exception):
    pass
#Creating a stacking class
class Stacking():
    ...
        This is a test class for stacking !
        Please fill Free to change it to fit your needs
        We suppose that at least the First N-1 Classifiers have
        a predict proba function.
    def __init__(self,classifiers):
        if(len(classifiers) < 2):</pre>
            raise numberOfClassifierException("You must fit your classifier with 2 classifi€
        else:
            self._classifiers = classifiers
    def fit(self,data_x,data_y):
        stacked data x = data x.copy()
        for classfier in self. classifiers[:-1]:
            classfier.fit(data x,data y)
            stacked_data_x = np.column_stack((stacked_data_x,classfier.predict_proba(data_x)
        last classifier = self. classifiers[-1]
        last classifier.fit(stacked data x,data y)
    def predict(self,data x):
        stacked_data_x = data_x.copy()
        for classfier in self._classifiers[:-1]:
            prob predictions = classfier.predict proba(data x)
            stacked data x = np.column stack((stacked data x,prob predictions))
        last_classifier = self._classifiers[-1]
        return last classifier.predict(stacked data x)
bagging clf rf.fit(train x, train y)
boosting clf ada boost.fit(train x, train y)
```

```
classifers_list = [clf_rf,clf_ada_boost,clf_logistic_reg]
clf_stacking = Stacking(classifers_list)
clf_stacking.fit(train_x,train_y)

predictions_bagging = bagging_clf_rf.predict(test_x)
predictions_boosting = boosting_clf_ada_boost.predict(test_x)
predictions_stacking = clf_stacking.predict(test_x)

print("For Bagging : F1 Score {}, Accuracy {}".format(round(f1_score(test_y,predictions_bocprint("For Stacking : F1 Score {}, Accuracy {}".format(round(f1_score(test_y,predictions_bocprint("For Stacking : F1 Score {}, Accuracy {}".format(round(f1_score(test_y,predictions_stacking : F1 Score {}, Accuracy {})".format(round(f1_score(test_y,predictions_stacking : F1 Score {}, Accuracy {},
```

## Comparaison

Metric	Bagging	Boosting	Stacking
Accuracy	0.90	0.94	0.98
F1-Score	0.88	0.93	0.98