

1. Create a DFA M1 for the language $\{w \mid w \text{ is a binary string with even number of 1's, starts with a 0, and when}$

interpreted as a number is divisible by 3 $\}, \Sigma = \{0,1\}$

2. Consider $r1 = (ab + cd)^* (c\epsilon + d\emptyset)$, $\Sigma = \{a,b,c,d\}$

(a) Draw an ϵ -NFA M2 which accepts $L(r1)$

(b) Draw the corresponding DFA M3 for M2

3. Write a regular expression denoting the language of all strings over the alphabet $\{a,b\}$ whose length is not

a multiple of 3.

4. Provide an algorithm for converting any ϵ -NFA to a corresponding NFA without epsilon transitions

5. Provide proof to Theorem 1

Theorem 1. If L is a regular language, then for some constant p and for each string $w \in L$, $|w| \geq p$ we can rewrite w as $w = xyz$ such that:

1. $|y| > 0$

2. $|xy| \geq p$

3. for each $k = 0, 1, \dots$ the string $xy^kz \in L$