Lab Work 3

André Pedrosa [85098], Filipe Pires [85122], João Alegria [85048]

Algorithmic Information Theory

Department of Electronics, Telecommunications and Informatics

University of Aveiro

December 30, 2019

1 Introduction

This report aims to describe the work developed for the third and final assignment of the course of 'Algorithmic Information Theory', explaining all scripts developed by us and presenting the results we considered most relevant regarding the quality of the solutions.

The programs implemented in Shell have the purpose of measuring similarity of images using a compression-based strategy and automatically identify human faces. Along with the description of the solutions, we also discuss the characteristics and the preprocessing done to the available dataset, the data compression algorithms used and the tests executed. All code developed is publicly accessible in our GitHub repository:

https://github.com/joao-alegria/TAI.

2 Image Classification

When dealing with image processing problems that require object identification, the usual environment calls for a classification approach, as the objects to be identified belong to specific classes with clear and separable characteristics. The challenge we are faced with (I) is a special approach for the image classification problem of facial recognition or identification. It is special in the sense that it does not aim to explore the usual strategies based on feature extraction, rather it is meant to rely on data compression methods and the notion of algorithmic information. Algorithmic information, also known as algorithmic entropy or Kolmogorov complexity, is the measure of information in a given data portion based on the theoretical algorithm that would be required to recreate that same data portion.

As this is an abstract definition, an example can clarify the concept: considering strings A="0101010101" and B="0010100110", for instance, one can easily reach the conclusion that string A is far easier to define than string B, since for A we can simply define it as the smaller string "01" repeated 5 times; string B, on the other hand, the process is not as simple and we probably will require the entire string to describe it. What this means is that A has less information than B. To achieve the so called algorithmic information of each one, the thought process is the same but now the string descriptions are achieved through algorithms; for our examples, the algorithms that define strings A and B are the following:

By a quick analysis, it is obvious that stringA() is less complex than stringB(), iterating only 5 times, contrasting with the 10 iterations of the second; hence confirming that string B has more information than string A. This can be directly correlated with data compression, since compressors take advantage of the data repetition to reduce space usage, and thereby compress the information by storing the data that appears frequently and the indicators of the places where those repetitions occur.

With this in mind, one can proceed to understand how the image classification will be done. Using the Normalized Information Distance defined by equation 1, where K(x) and K(x-y) define the Kolmogorov complexity of the string x and of the string x given string y.

$$NID(x,y) = \frac{max\{K(x|y), K(y|x)\}}{max\{K(x), K(y)\}}$$
(1)

Unfortunately, because the Kolmogorov complexity is non-computable, this formula is only theoretical and we are sure there is no algorithm that can compute any string complexity. Nevertheless, compressors approximate the formula's results very closely, if used correctly. So we used two of the most frequently used approximations of NID to determine the compression distance between images and, with these distances, calculate the closest images, i.e. the most similar ones, and hopefully classify them as belonging to the group of images that represent the same face.

2.1 NCD Approximation

By using known general purpose compressors, such as gzip, lzma or tar, the Kolmogorov complexity can be estimated by the number of bits the resulting compressed file has. This approximation is called Normalized Compression Distance (NCD) and is expressed by equation 2, where C(x) and C(x,y) represent the number of bits the compression of x and of x and y concatenated contain, respectively. The xy concatenation can be performed in several ways, the most common being to simply perform an union on both; other more complex operations can also be done, such as interlacing the two data sources.

$$NCD(x,y) = \frac{C(x,y) - min\{C(x), C(y)\}}{max\{C(x), C(y)\}}$$
(2)

Following the formula, results close to 0 indicate similarity and close to 1 dissimilarity. The only restriction to this approach is that the compressor used must follow the condition $C(x,x) \simeq C(x)$. If this is not verified, the results of NCD are not reliable.

2.2 NCCD Approximation

The second approximation is called Normalized Conditional Compression Distance, expressed by equation 3. The difference between NCD and NCCD is that the later uses conditional compressors to achieve its estimations. Conditional compressors are normally implemented with finite-context models and take in consideration the previous occurring terms to compress the new term. This is a more direct approximation of the NID and, in general, generates better results than the NCD.

$$NCCD(x,y) = \frac{max\{C(x|y), C(y|x)\}}{max\{C(x), C(y)\}}$$
(3)

C(x) has the same meaning as before and C(x-y) represents the number of bits the compression of x needs given that y occurred (C(y|x)) follows the same logic). Due to the conditional aspect of this approach, C(x) can be a special case of C(x-y) were y is equal to the empty string, making true the statement $C(x) = C(x|\epsilon)$.

3 Dataset

Like in all experimental work, specially in image processing, a considerably large dataset is required for any results to be significant and any conclusions to be solid. Also, when benchmarking an algorithm, it is recommended that standard test datasets are used for researchers to be able to directly compare the results. Taking this in consideration, we downloaded AT&T "The Database of Faces" (formerly "The ORL Database of Faces") and used it to test our code.

The image database contains 10 different images of each of the 40 distinct subjects. For some subjects the images were taken at different times, between April 1992 and April 1994, with varying lighting conditions and different facial expressions. Most faces are in an upright position in frontal view, with a slight left-right rotation. All 400 images were taken in black & white at the Olivetti Research Laboratory in Cambridge, UK.



Figure 1: Image taken from the assignment description (1). Examples from the ORL face dataset. In the first row, ten face images corresponding to the same subject (s01). In the second row, the first face image of subjects s02 to s11.

To speedup the processing of each image, we applied 2 transformations to each element of the dataset. The first consisted in a simple image reduction from 112×92 px to 56×46 px, ensuring that proportions remained the same. The second was a quantization process from 8 bits per pixel gray level to 4 bits only. These modifications were accomplished using ImageMagick (2), a command-line program to create, edit, compose, or convert bitmap images.



Figure 2: Example from subject s01 of the ORL face dataset, before and after preprocessing.

4 Experiment

Once the dataset was ready, we composed an experiment to determine which commonly used compressors provided the best results for our intents. The conducted study had 2 phases: the first where we tested several data compressors using NCD and compared the precisions of the face identification program using each of the compressors; the second where we tested a conditional compressor using NCCD and compared the best results of the first phase with those of this test.

4.1 Compressor Validation

Before conducting our experiment, we needed to make sure the compressor candidates were valid. This was done by verifying for each compressor C if condition $C(x,x) \simeq C(x)$ was true. The concatenation used in this verification uses the only valid operation for this situation, the "append" operation, which is explained in section 4.3.

The script checkCompressor.sh was a script developed to help us manually verifying each compressor. For each candidate, we compressed an example image and the concatenation of itself, and then ran this script. What it does is collect the outcomes of the compressions and print them to the console side by side for us to quickly detect which break the condition.

From the compressors put to test, the ones we considered invalid were pax and shar, with a difference between C(x) and C(x,x) of over 50% for an example image as x, while the others were less than 40%. Although 40% is still a very significant difference, we decided to keep most of the standard compressors as reaching a difference close to 0% was already known to be really difficult to find.

4.2 Tested Compressors

Zip is a compression and file packaging utility for many operating systems, like Unix, VMS, MSDOS, etc.. It is analogous to a combination of the Unix commands tar and compress and is compatible with PKZIP (Phil Katz's ZIP for MSDOS systems). It performs a lossless compression that can achieve 3:1/2:1 ratios in text files. The standard compression method is deflate, which uses a combination of LZSS and Huffman coding.

Gzip is a single-file/stream lossless data compression utility. This compression algorithm uses Lempel-Ziv coding (LZ77) to achieve its reduction factors. Gzip will only attempt to compress regular files. In particular, it will ignore symbolic links. Typically, text such as source code or English is reduced by 60-70%. Compression is generally much better than that achieved by LZW, Huffman coding, or adaptive Huffman coding.

The Lempel–Ziv–Markov chain algorithm, aslo known as LZMA, is an algorithm used to perform lossless data compression. Developed by Igor Pavlov, was first used in the 7z format of

the 7-Zip archiver. This algorithm uses a dictionary compression scheme somewhat similar to the LZ77 algorithm published by Abraham Lempel and Jacob Ziv in 1977 and features a high compression ratio (generally higher than bzip2).

Bzip2 is a free and open-source file compression program that uses the Burrows–Wheeler algorithm. It only compresses single files and is not a file archiver. This algorithm compresses most files more effectively than the older LZW and Deflate compression algorithms, but is considerably slower. LZMA is generally more space-efficient than bzip2 at the expense of even slower compression speed, while having much faster decompression.

ZPAQ is an open source command line archiver for Windows and Linux. It uses an appendonly format which can be rolled back to an earlier state to retrieve older versions. It supports fast incremental update by adding only files whose last-modified date has changed since the previous update. It compresses using deduplication and several algorithms (LZ77, BWT, and context mixing) depending on the data type and the selected compression level.

Ppmd, or Prediction by partial matching is an adaptive statistical data compression technique based on context modeling and prediction. PPM models use a set of previous symbols in the uncompressed symbol stream to predict the next symbol in the stream. PPM algorithms can also be used to cluster data into predicted groupings in cluster analysis.

The conditional compressor used to test NCCD was given *a priori* for this assignment. It is based on finite context modeling and it is implemented in C++ and specialized to compress images with the help of OpenCV.

4.3 Study Pipeline

The experiment's pipeline is structured as an iterative process, built in testCompressor.sh. This script receives as its only parameter the operation to be used to concatenate images. As the concatenation can be done in more than one way, we executed the experiment for 3 different types of concatenations:

- Append this operation unites the two images one above the other (duplicating the height of the resulting image).
- Interlace interpolated horizontal stripes of both images are stacked together (in this operation half of the data of each image is not used).
- Average for each pixel position, the average of the gray value of both images at that position is calculated and added to the new image in the same position.

These image manipulations were also done with the help of ImageMagick. Examples of these operations can be seen in Figure 3, where the first 2 faces correspond to the first images of subjects s01 and s02, and the 3 remaining images correspond to the concatenation using append, interlace and average respectively. Note that, to verify the condition discussed in section 4.1, the concatenation is done for the same image, so using either the average or the interlace operations will result in the exact same image as the original; this is why we used the append operation in that context.



Figure 3: Concatenation examples applied to subjects s01 and s02 using different operations.

Back to the experiment's script, its execution workflow follows the pseudo-code presented next, where concat corresponds to the chosen operation passed to the script and compress corresponds to the compression action executed by the current compressor of the first loop.

```
for each compressor, do:
    for each subject, do:
        minNCD = 1
        for each testImg, do:
            for each goldStdImg, do:
                tmp = concat(testImg,goldStdImg)
                cTmp = compress(tmp)
                cT = compress(testImg)
                cGS = compress(goldStdImg)
                maxS = getMaxSize(cTmp,cT,cGS)
                minS = getMinSize(cTmp,cT,cGS)
                NCD = (size(cTmp) - minS) / maxS
                if NCD < minNCD:
                      minNCD = NCD</pre>
```

The output of each script execution was written to disk in different files. Then, to determine the accuracy of each compressor using each of the concatenation alternatives, we executed a second script that reads the output files, computes the performance metrics and writes them on the console for analysis.

5 Results & Discussion

Lorem ipsum ...

6 Conclusions

In terms of code organization and readability, we made sure our repository was as well structured as possible and our code properly commented and documented. The base folder contains a *README* file for basic instructions. All code is in the *src* folder.

References

- 1. Armando J. Pinho, AIT: Lab Work no.3, University of Aveiro, 2019/20.
- 2. ImageMagick Studio LLC, ImageMagick, https://imagemagick.org/index.php, accessed in December 2019.