

Optimal Dynamic Economic Dispatch Including Renewable Energy Source using Artificial Bee Colony Algorithm

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Abstract— Power utilities strive for optimal economic operation of their electric networks while considering the challenges of escalating fuel costs and increasing demand for electricity. The dynamic economic dispatch (DED) occupies a prominent place in a power system's operation and control. It aims to determine the optimal power outputs of on-line generating units in order to meet the load demand subject to satisfying various operational constraints over finite dispatch periods. Similar to most real-world complex engineering optimization problems, the nonlinear and nonconvex characteristics are more prevalent in the DED problem. Therefore, obtaining a truly optimal solution presents a challenge. In this paper, the artificial bee colony (ABC) algorithm – a recently introduced population-based technique – is utilized to solve the DED problem. Integrating a renewable-energy source and analyzing its impact is considered as well. A sample test system with a dispatch period of 24-hour is designated to validate the outcomes. The promising results prove that the ABC algorithm has a great potential to be applied in different electric power system optimization areas.

Keywords—component; Artificial Bee Colony (ABC) Algorithm; Dynamic Economic Dispatch (DED) Problem; Renewable Energy Sources.

I. INTRODUCTION

The ultimate goal of power plants is to meet the required load demand with the lowest operating costs possible while taking into consideration practical equality and inequality constraints algorithms. Optimal operation of electric power system networks is a challenging real-world engineering problem. Indeed, the optimal operation of these networks is the result of multiple optimization problems that interact with each other sufficiently and efficiently. Those – linked – optimization problems are the unit commitment, optimal power flow, and economic dispatch scheduling.

The dynamic economic dispatch (DED) occupies a prominent place in a power system's operation and control. The goal of DED is to determine the optimal power outputs of on-line generating units in order to meet the load demand subject to satisfying various operational constraints over finite dispatch periods. In practice, there are static economic dispatch (SED) and DED problems. The latter considers additional practical constraints such as upper and lower bounds on the units' ramping-rates. In reality, units will not respond to steep

or instantaneous load variations. Early research works responding to this aspect were published in the 1970s [1, 2]. Most of the early methods proposed to solve the DED problem used deterministic techniques such as non-linear programming (NLP) [3], dynamic programming (DP) [4], and variational techniques based on Lagrange multipliers [5].

Optimization based on swarm intelligence, known as meta-heuristic algorithms, gained popularity in solving complex and real-world optimization problems years ago. Because the performance of most of the meta-heuristic methods are independent of the initial solutions and are derivative-free, they overcome the main limitations of deterministic optimization methods, e.g., getting trapped in local extrema and divergence situations. An example of the recently introduced meta-heuristic methods is the artificial bee colony (ABC) algorithm. It is a population-based technique proposed late in 2005 [6], and inspired by the intelligent foraging behaviour of the honeybee swarm. The DED problem was one of the real-world optimization problems that has benefited from the development of the meta-heuristic algorithms. Based on the genetic algorithm (GA), the authors in [7] and [8] suggested a GA-based method to solve the DED problem. The particle swarm optimization (PSO) method is also utilized in [9] and [10] to solve the DED problem. An evolutionary programming (EP) technique in [11] and [12] is adopted to solve the DED problem. Simulating annealing method (SA), quantum evolutionary algorithm (QEA), and Tabu search approach (TS) have been also designated to solve the DED problem in [13], [14], and [15], respectively.

Although renewable sources, e.g., wind, tidal, and photovoltaic, are environmentally-friendly practices, the intermittent nature of the renewable sources choices degrades their applicability as dispatchable options [16]. Despite that, according to the Global Wind Energy Council (GWEC) [17], the installed capacity of wind power farms in Canada is increasing exponentially, as Fig. 1 indicates.

In this paper, the ABC algorithm is proposed to solve the DED problem. In addition, the ABC algorithm is utilized to verify the efficiency of a previously introduced – by the same authors – constrained search-tactic [18] in solving high dimensional dynamic problems. An attempt to integrate a

renewable resource and analyze its impact is considered. A sample system with a 24-hour dispatch period is adopted to validate the proposed algorithm competence.

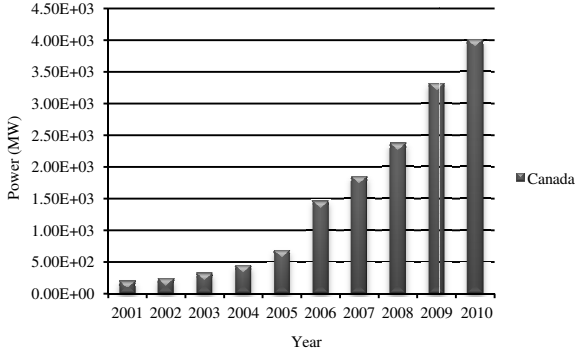


Figure 1. Total installed capacity of wind power in Canada.

This paper is organized as follows: Section II offers the mathematical formulations of the DED problem. Section III presents a brief description of the ABC optimization algorithm. Computational results and comparative study are demonstrated in sections IV. Section V contains the conclusion.

II. MATHEMATICAL FORMULATIONS

A. Objective Function

Since the objective function of the DED problem is to minimize the operating fuel's costs of committed generating units to meet the load demand, subject to equality and inequality constraints over a predetermined dispatch period, the result's practical usefulness will be degraded if the units' valve-point effects are neglected. Consequently, there are two models to represent the units' valve-point effects in the literature [19]. The first represents the units' valve-point effects in terms of prohibited operating zones which are included as inequality constraints. The second form represents the units' valve-point effects as a rectified sinusoid term which is superimposed on the approximate quadratic fuel cost function. The general mathematical form of the DED problem is as follows:

$$F = \min \sum_{t=1}^T \sum_{i=1}^N f_i(P_i^t)$$

$$f_i(P_i) = a_i + b_i P_i + c_i P_i^2 + \left| d_i \times \sin \left(g_i \times (P_{i,min} - P_i) \right) \right| \quad (1)$$

where, $f_i(P_i)$ is the fuel cost function of i^{th} generator; P_i^t is the output power of i^{th} generator at a time t , $\forall i \in \{1, 2, \dots, N\}$ and $\forall t \in \{1, 2, \dots, T\}$; a_i , b_i , c_i , d_i , and g_i are the i^{th} generator's coefficients, and $P_{i,min}$ is the minimum limit of i^{th} generator.

B. Equality Constraints

It is impractical to neglect the system's transmission losses so the B -coefficient formula is commonly used to express it. Thus, the real power balance equation representing equality constraints of the problem considered is as follows:

$$\sum_{t=1}^T \sum_{i=1}^N P_i^t = \sum_{t=1}^T P_D^t + P_L^t \quad (2)$$

Integration of a renewable source (RS) modifies the equality constraints function [16] to be as follows:

$$\sum_{t=1}^T \sum_{i=1}^N P_i^t = \sum_{t=1}^T \left(P_D^t + P_L^t - \sum_{RS=1}^M \mu_{RS} P_{RS}^t \right) \quad (3)$$

where, P_D^t and P_L^t are the load demand and system's loss at a time t respectively. The multiplier μ_{RS} is set to a permissible amount of active power injected by RS , P_{RS}^t is the forecasted real power from RS at time t $\forall RS \in \{1, 2, \dots, M\}$. In this paper, μ_{RS} is set to one.

The system's active power loss can be calculated using George's loss expression [20] as follows:

$$\sum_{t=1}^T P_L^t = \sum_{t=1}^T \sum_{j=1}^N \sum_{i=1}^N P_i^t B_{ij} P_j^t \quad (4)$$

where, B_{ij} is the ij^{th} element of the loss coefficient square matrix.

C. Inequality Constraints

The inequality constraints of the DED problem are the units' ramp-rate limits, i.e., upper rate (UR_i) and down rate (DR_i), are considered as follows:

$$\begin{aligned} P_i^t - P_i^{t-1} &\leq UR_i \\ P_i^{t-1} - P_i^t &\leq DR_i \end{aligned} \quad (5)$$

Additional inequality constraints are the minimum and maximum power output of each unit:

$$P_{i,min} \leq P_i \leq P_{i,max} \quad (6)$$

Therefore, to incorporate the constraints of units' ramp-rate limits (5) in the real power output limit constraints (6), the modified units' real power outputs are evaluated [21] as follows:

$$\begin{aligned} P_{i,min}^t &= \max(P_{i,min}, P_i^{t-1} - DR_i) \\ P_{i,max}^t &= \min(P_{i,max}, P_i^{t-1} + UR_i) \end{aligned} \quad (7)$$

The following inequality constraints describe the case when units have prohibited operating zones [9] defined by:

$$\begin{cases} P_{i,min} \leq P_i^t \leq P_{i,1}^l \\ P_{i,j-1}^u \leq P_i^t \leq P_{i,j}^l \\ P_{i,n_i}^u \leq P_i^t \leq P_{i,max} \end{cases}, j \in \{2, 3, \dots, n_i\} \quad (8)$$

where, $P_{i,1}^l$ is the lower limit of the first prohibited zone of the i^{th} generator; $P_{i,j-1}^u$ is the upper limit of the $(j-1)^{th}$ prohibited zone of the i^{th} generator; P_{i,n_i}^u is the upper limit of the n_i^{th} prohibited zone of the i^{th} generator; n_i is the number of prohibited zones in the i^{th} generator.

III. ARTIFICIAL BEE COLONY ALGORITHM

Inspired by the intelligent foraging behaviour of honeybee swarms, the ABC algorithm was introduced [6] and [22]. The colony of artificial bees consists of three groups: employed,

onlookers, and scout bees. The employed bees (E_b) randomly search for food-source positions (solutions.) By dancing they share information (communicate) about that food source, such as nectar amounts (solutions qualities), with the onlooker bees (O_b) waiting in the dance area at the hive. The duration of a dance is proportional to the nectar's content (fitness value) of the food source being exploited by the employed bee. Onlooker bees watch various dances before choosing a food-source position, according to the probability proportional to the quality of that food source. Consequently, a good food-source position attracts more bees than a bad one. Onlookers and scout bees, once they discover a new food-source position, may change their status to become employed bees. When the food-source position has been visited (tested) fully, the employed bee associated with it abandons it and may once more become a scout or onlooker bee.

It is clear that the ABC algorithm has the following control parameters: 1) the *CS* that consists of employed bees (E_b) plus onlooker bees (O_b), 2) the *limit* value, which is the number of trials for a food-source position to be abandoned, and 3) the maximum cycle number (*MCN*.) Although the ABC algorithm has three parameters to be tuned, once the *CS* parameter has been determined by the practitioner, the *limit* value can be calculated easily as half of the *CS* multiplied by the problem's dimension. Therefore, technically speaking, the ABC algorithm has only two parameters to be adjusted: *CS* and the *MCN* values. Updating these two parameters towards the most effective values has a higher likelihood of success than in other competing meta-heuristic methods. The pseudo-code of the ABC algorithm is as follows:

1. Initialize the population.
2. Modify positions.
3. Apply selection criterion.
4. **Repeat** (cycle.)
5. Allow the employed bees to share the food information with onlooker bees.
6. Allow the onlooker bees to choose the best food source based on the probability calculation.
7. Apply selection criterion.
8. Check for an abundant solution, and (if exists) initiate a new food-source position. Otherwise, follow the next step.
9. Retain best solution so far.
10. **Until** stopping rule.

IV. RESULTS AND DISCUSSION

The five units system is selected to verify the validity of the proposed algorithm. The acceptable violation of equality constraints is adjusted to be $\leq 10^{-4}$. The control parameters of selected techniques are tuned after trial-and-error experiments. The proposed search-tactic is implemented in C, and executed on an Intel® core™ 2 duo PC with 2.66-GHz speed and 4GB RAM. The results are obtained after carrying out 30 independent runs for each system, and are compared with those obtained using other well-known algorithms. It is important to mention that the constraints of the DED are handled using the penalty factor method. The performance of the ABC algorithm without and with the integration of the constrained search-

tactic reported in [18] is analyzed as well. Two test cases are examined, and the results are compared with those of other well-known methods. The integration of a renewable energy source is considered in the second test case. Details of test cases are highlighted in the following sub-sections.

A. Case 1

The aim of this system is to operate its five generating units economically to meet the 24-hour load demand subject to satisfying various equality and inequality constraints. Table I records the five units' coefficients and characteristics. This system's constraints are the transmission losses using George's loss expression, units' bound limits, and unit's ramp-rate limits. The operating fuel cost's function superimposes the unit's prohibited operating zones by a rectify sinusoid term. The system's load demand and *B*-loss coefficient matrix are reported in Table II and Table III respectively. The ABC algorithm is designated to solve this system with, and without the integration of the constrained search-tactic reported in [18].

TABLE I. GENERATING UNITS' COEFFICIENTS AND CHARACTERISTICS FOR THE 5-UNIT SYSTEM.

| Units | 1 | 2 | 3 | 4 | 5 |
|---------------------------|---------|----------|----------|----------|----------|
| P^0 (MW) | 50.7118 | 40.9004 | 100.0930 | 116.8943 | 161.0431 |
| P_{min} (MW) | 10.0000 | 20.0000 | 30.0000 | 40.0000 | 50.0000 |
| P_{max} (MW) | 75.0000 | 125.0000 | 175.0000 | 250.0000 | 300.0000 |
| a (\$) | 25.0000 | 60.0000 | 100.0000 | 120.0000 | 40.0000 |
| b (\$/MW) | 2.0000 | 1.8000 | 2.1000 | 2.0000 | 1.8000 |
| c (\$/MW ²) | 0.0080 | 0.0030 | 0.00120 | 0.0010 | 0.0015 |
| d (\$) | 100.000 | 140.0000 | 160.0000 | 180.0000 | 200.0000 |
| UR (MW/h) | 30.0000 | 30.0000 | 40.0000 | 50.0000 | 50.0000 |
| DR (MW/h) | 30.0000 | 30.0000 | 40.0000 | 50.0000 | 50.0000 |

TABLE II. LOAD DEMAND FOR THE 5-UNIT SYSTEM.

| Hour (h) | P_D (MW) | Hour (h) | P_D (MW) |
|----------|------------|----------|------------|
| 1 | 410 | 13 | 704 |
| 2 | 435 | 14 | 690 |
| 3 | 475 | 15 | 654 |
| 4 | 530 | 16 | 580 |
| 5 | 558 | 17 | 558 |
| 6 | 608 | 18 | 608 |
| 7 | 626 | 19 | 654 |
| 8 | 654 | 20 | 704 |
| 9 | 690 | 21 | 680 |
| 10 | 704 | 22 | 605 |
| 11 | 720 | 23 | 527 |
| 12 | 740 | 24 | 463 |

TABLE III. *B*-LOSS COEFFICIENTS' MATRIX FOR THE 5-UNIT SYSTEM.

| $i \backslash j$ | 1 | 2 | 3 | 4 | 5 |
|------------------|----------|----------|----------|----------|----------|
| 1 | 0.000049 | 0.000014 | 0.000015 | 0.000015 | 0.000020 |
| 2 | 0.000014 | 0.000045 | 0.000016 | 0.000020 | 0.000018 |
| 3 | 0.000015 | 0.000016 | 0.000039 | 0.000010 | 0.000012 |
| 4 | 0.000015 | 0.000020 | 0.000010 | 0.000040 | 0.000014 |
| 5 | 0.000020 | 0.000018 | 0.000012 | 0.000014 | 0.000035 |

After trail-and-error experiments, the ABC parameters: *CS*, *limit*, and *MCN* were tuned as 300, 18×10^3 , and 30×10^3 respectively. Utilizing the constrained search-tactic [18] will alter the main objective function for the first 3×10^3 (φ) iterations.

As presented in Table IV, the integration of the constrained search-tactic [18] enhanced the ABC algorithm's performance resulting in a significant reduction (4.41%) in the operating fuel's cost. The cost saving (\$2,254.60 daily) is shown in Fig. 2. An average 21% reduction in the required CPU time was obtained as well. The load demand curve, each committed unit's output power, and the total system's input power are exemplified in Fig. 3. The optimal dispatched power for this system guaranteed that the system's constraints were satisfied during the 24-hour dispatch period, as shown in Table V and Fig. 3. In other words, the output power of each unit in every time interval was consistent with the output power of adjacent units. The ABC algorithm's performance for this system is in Fig. 4.

TABLE IV. COMPARISON OF RESULTS OF THE PROPOSED ABC ALGORITHM FOR CASE 1; MAX: MAXIMUM; AVG.: AVERAGE; MIN: MINIMUM; STD.DEV.: STANDARD DEVIATION.

| Method | Max. (\$) | Avg. (\$) | Min. (\$) | Std.Dev. | CPU (s) |
|--------|-----------|-----------|------------------|----------|---------|
| ABC | 51,868.90 | 51,462.82 | 51,102.80 | 229.191 | 280.440 |
| ABC* | 50,195.90 | 49,814.28 | 48,848.20 | 288.168 | 221.520 |

* With the integration of the constrained search-tactic offered in [18].

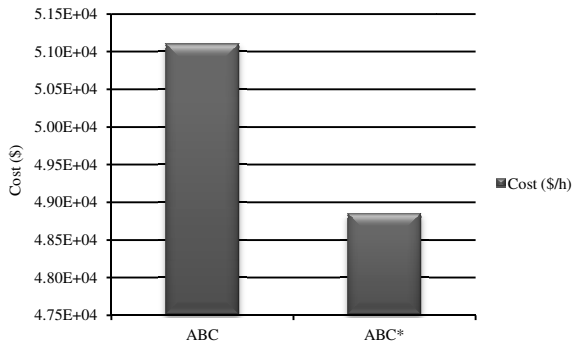


Figure 2. Operating fuel costs for case 1 due to ABC algorithm with and without the integration of the constrained search-tactic.

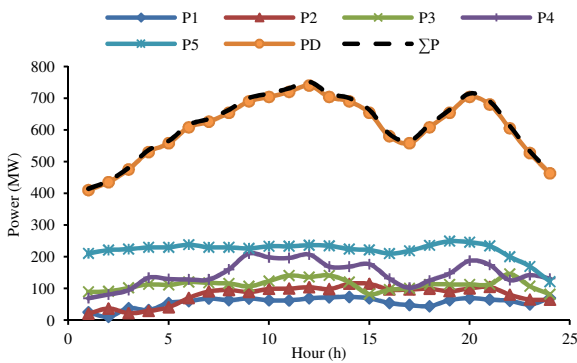


Figure 3. Optimal units' dispatch schedule, load demand curve, and total power supply for case 1.

TABLE V. OPTIMAL DISPATCH POWER FOR CASE 1 USING ABC ALGORITHM WITH THE INTEGRATION OF THE CONSTRAINED SEARCH-TACTIC.

| Time (h) | Units' optimal output power and total power supply, both in (MW) | | | | | |
|--------------------------------|--|----------------|----------------|----------------|----------------|------------------|
| | P ₁ | P ₂ | P ₃ | P ₄ | P ₅ | ΣP |
| 1 | 24.90640 | 20.44230 | 89.00000 | 69.00000 | 210.33820 | 413.68690 |
| 2 | 10.12730 | 36.44830 | 90.92960 | 80.64500 | 221.00020 | 439.15040 |
| 3 | 37.63000 | 22.00010 | 101.70000 | 94.48800 | 224.03600 | 479.85410 |
| 4 | 31.17770 | 28.85390 | 112.65200 | 133.75600 | 229.52000 | 535.95960 |
| 5 | 53.67679 | 40.35030 | 111.01879 | 130.01300 | 229.52000 | 564.57888 |
| 6 | 59.46100 | 70.00000 | 120.16420 | 128.20410 | 237.96910 | 615.79840 |
| 7 | 68.10929 | 90.79000 | 117.64000 | 128.21195 | 229.52000 | 634.27124 |
| 8 | 62.99900 | 95.05200 | 115.43330 | 160.03000 | 229.52000 | 663.03430 |
| 9 | 68.00000 | 89.09100 | 106.90000 | 210.00000 | 226.16150 | 700.15250 |
| 10 | 62.15450 | 98.54000 | 123.00350 | 198.01000 | 232.78100 | 714.48900 |
| 11 | 61.80400 | 99.54000 | 140.59600 | 195.87000 | 233.08070 | 730.89070 |
| 12 | 68.58800 | 103.76350 | 135.92940 | 206.97000 | 236.30170 | 751.55260 |
| 13 | 72.12000 | 98.00810 | 141.00000 | 168.87110 | 234.38000 | 714.37920 |
| 14 | 73.03300 | 114.53950 | 120.01190 | 168.60430 | 223.87860 | 700.06730 |
| 15 | 68.43499 | 114.54150 | 82.20120 | 176.48584 | 221.58730 | 663.25083 |
| 16 | 53.50430 | 96.40200 | 96.12900 | 131.11160 | 210.00000 | 587.14690 |
| 17 | 47.31110 | 96.45100 | 100.02000 | 102.10090 | 218.77329 | 564.65629 |
| 18 | 43.57430 | 98.89896 | 112.67330 | 124.91000 | 235.81870 | 615.87526 |
| 19 | 62.43000 | 91.54000 | 112.66000 | 147.31700 | 249.14970 | 663.09670 |
| 20 | 68.80430 | 100.02940 | 112.67330 | 187.32000 | 245.72590 | 714.55290 |
| 21 | 64.42430 | 104.60303 | 112.67310 | 174.06160 | 234.05680 | 689.81883 |
| 22 | 60.60000 | 80.30000 | 145.66000 | 126.01700 | 200.00000 | 612.57700 |
| 23 | 49.38430 | 65.02312 | 107.03100 | 142.02000 | 169.30200 | 532.76042 |
| 24 | 69.36430 | 64.35970 | 81.67300 | 131.06820 | 121.00143 | 467.46663 |
| Total operating fuel cost (\$) | | | | | | 48,848.20 |
| Total system's power loss (%) | | | | | | 1.300 |

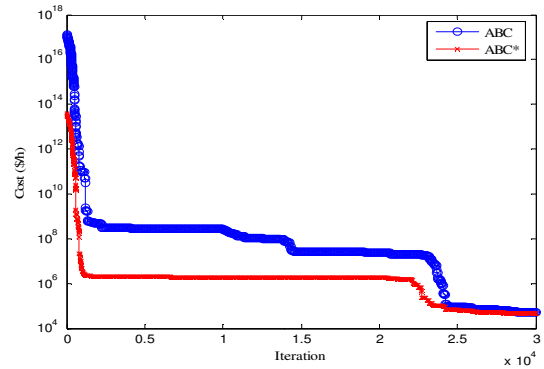


Figure 4. The ABC algorithm's performance for case 1.

B. Case 2

In this test case, the impact of integrating renewable energy resources is examined on the five units system used previously. A wind-power farm is designated to share a 10% of the system's load demand. In addition, the ABC algorithm's parameters are tuned as in case 1. The ABC algorithm with the utilization of that designated tactic [18] is employed in this test case.

As shown in Table VI, and with respect to Table V, the integration of RS decreased the operating fuel cost and the system's transmission losses. The 10% contribution of a RS led to 2.71% reduction in the fuel cost for this system with regard to non-RS integration scenario. The total system's loss is decreased by 20.15% due to the 10% sharing of RS practice. The average CPU time required to attain a solution in this case was approximately 200.000 seconds, which was less than that of the previous test case.

TABLE VI. OPTIMAL DISPATCH POWER FOR CASE 2 USING ABC ALGORITHM WITH THE INTEGRATION OF THE CONSTRAINED SEARCH-TACTIC.

| Time (h) | Units' optimal output power and total power supply, both in (MW) | | | | | |
|--------------------------------|--|----------------|----------------|----------------|----------------|-----------|
| | P ₁ | P ₂ | P ₃ | P ₄ | P ₅ | ΣP |
| 1 | 53.00000 | 35.00000 | 80.00000 | 78.00000 | 125.80800 | 371.80800 |
| 2 | 39.65957 | 64.10482 | 71.87489 | 65.53363 | 153.57705 | 394.74996 |
| 3 | 49.28233 | 75.67546 | 92.35823 | 76.70595 | 137.27795 | 431.29992 |
| 4 | 36.48119 | 52.14938 | 105.57053 | 126.68860 | 160.80950 | 481.69920 |
| 5 | 64.99354 | 56.50897 | 93.86012 | 127.53065 | 164.55193 | 507.44521 |
| 6 | 57.86589 | 73.92488 | 99.40114 | 163.08726 | 159.18274 | 553.46191 |
| 7 | 40.10564 | 89.02398 | 121.97463 | 130.52654 | 188.38893 | 570.01972 |
| 8 | 56.10172 | 106.55467 | 108.33142 | 136.19100 | 188.71398 | 595.89279 |
| 9 | 74.25326 | 97.08604 | 134.72116 | 108.27100 | 214.76170 | 629.09316 |
| 10 | 70.18770 | 83.05224 | 114.33486 | 155.00623 | 219.45800 | 642.03903 |
| 11 | 73.72856 | 88.30782 | 126.53435 | 154.95246 | 213.25231 | 656.77550 |
| 12 | 69.25282 | 86.51000 | 133.90429 | 159.17164 | 226.43400 | 675.27275 |
| 13 | 72.22919 | 87.69308 | 131.92719 | 125.81428 | 224.34800 | 642.01174 |
| 14 | 72.99018 | 76.38711 | 142.32171 | 132.32986 | 204.96343 | 628.99229 |
| 15 | 74.89765 | 101.73754 | 136.14901 | 121.46363 | 161.53230 | 595.78013 |
| 16 | 65.13230 | 82.07555 | 103.00153 | 131.25100 | 146.19226 | 527.65264 |
| 17 | 74.94059 | 63.48749 | 90.45637 | 133.72639 | 144.83885 | 507.44969 |
| 18 | 73.54776 | 54.90115 | 112.07866 | 119.61939 | 193.29377 | 553.44073 |
| 19 | 74.95189 | 67.99570 | 105.63626 | 145.87981 | 201.39886 | 595.86252 |
| 20 | 74.33483 | 92.85957 | 145.63517 | 118.09636 | 211.04199 | 641.96792 |
| 21 | 58.96502 | 87.17871 | 111.22778 | 122.22385 | 240.37016 | 619.96552 |
| 22 | 65.75197 | 69.17475 | 84.66006 | 140.12104 | 191.06119 | 550.76901 |
| 23 | 71.44790 | 45.01166 | 99.43192 | 121.81690 | 141.23045 | 478.93883 |
| 24 | 42.89456 | 43.22525 | 88.81553 | 104.58387 | 140.75652 | 420.27573 |
| Total operating fuel cost (\$) | | | | | | 47,522.60 |
| Total system's power loss (%) | | | | | | 1.155 |

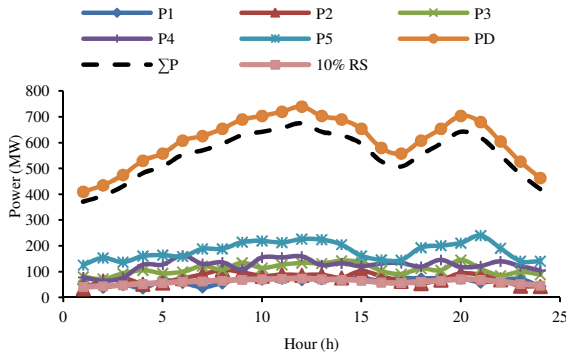


Figure 5. Optimal units' dispatch schedule, load demand curve, and total power supply for case 2.

The improvement in the operating fuel cost is demonstrated in Fig. 6. Clearly, significant daily cost saving of \$1,325.60 is the result of the 10% RS's sharing with respect to case 1.

C. Comparative Study

The result of the proposed ABC* algorithm was compared with those obtained by hybrid harmony search (HHS) [23] and adaptive particle swarm optimization (APSO) [24]. Although both HHS and APSO methods attained "less" operating fuel costs than that of the ABC* algorithm, they disregarded the P^0 scheduling values, and relaxed the accepted value for violating the equality constraints. Moreover, the outcomes of the APSO approach claimed in [24] violated the units' ramp-rate constraints of unit-1 at hours 4, 14, and 19; unit-3 at hour 13; unit-4 at hour 6; unit-5 at hour 18. The dispatch schedule with a high power output mismatch degraded the practicality of the

attainable solutions by these methods. Clearly, as shown in Fig. 7, the dispatch schedule of on-line units in every time interval was more consistent using the ABC* algorithm than the compared methods. The proposed ABC* algorithm provided the least absolute value of violating the system's equality constraints and, therefore, represented the minimum total system's power loss.

Although relaxing the equality constraints' violation plays a significant role (in addition to other factors such as the utilized algorithm and PC's features) in achieving a faster solution, the offered ABC* algorithm outperformed that of HHS method with respect to the CPU time requirement (~28%) as seen in Table VII.

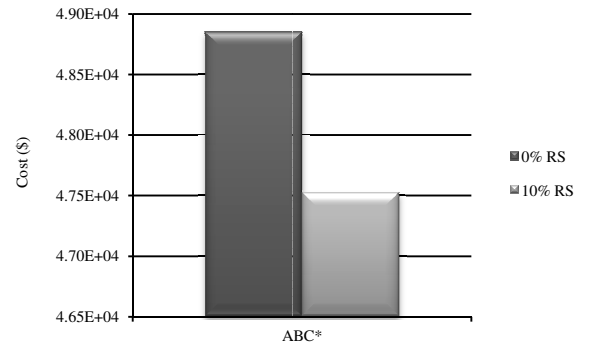


Figure 6. Operating fuel cost reduction due to the 10% RS contribution obtained by the ABC algorithm with the integration of the constrained search-tactic.

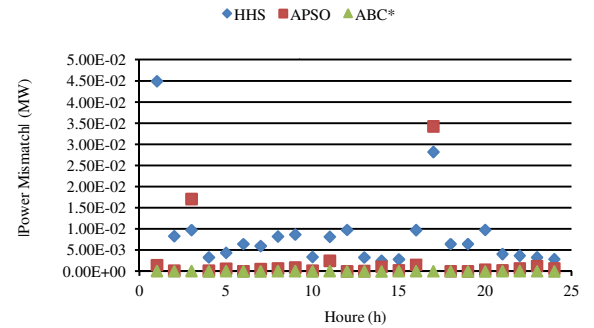


Figure 7. Violation of equality constraints due to different algorithms for case 1.

TABLE VII. COMPARISON OF RESULTS FOR CASE 1.

| Time (h) | HHS [23] | | APSO [24] | | Proposed ABC* | |
|--------------------------------|------------------------|--------------------|------------------------|--------------------|------------------------|--------------------|
| | $P_{mismatch}$ (MW) | P_{loss} (MW) | $P_{mismatch}$ (MW) | P_{loss} (MW) | $P_{mismatch}$ (MW) | P_{loss} (MW) |
| 1 | 0.04497 | 3.98993 | 0.00149 | 3.68599 | 0.00009 | 3.68681 |
| 2 | 0.00833 | 4.44333 | 0.00016 | 4.05636 | 0.00003 | 4.15043 |
| 3 | 0.00976 | 5.36546 | 0.01713 | 4.79507 | 0.00008 | 4.85418 |
| 4 | 0.00331 | 6.35801 | 0.00016 | 5.90654 | 0.00002 | 5.95962 |
| 5 | 0.00438 | 6.84172 | 0.00065 | 6.68515 | 0.00009 | 6.57897 |
| 6 | 0.00647 | 7.95917 | 0.00006 | 7.88534 | 0.00001 | 7.79841 |
| 7 | 0.00601 | 8.45969 | 0.00055 | 8.44065 | 0.00002 | 8.27126 |
| 8 | 0.00825 | 9.25765 | 0.00068 | 9.18548 | 0.00005 | 9.03425 |
| 9 | 0.00870 | 10.19960 | 0.00090 | 10.17370 | 0.00010 | 10.15240 |
| 10 | 0.00340 | 10.55940 | 0.00020 | 10.55940 | 0.00000 | 10.48900 |
| 11 | 0.00820 | 11.04460 | 0.00250 | 10.93730 | 0.00010 | 10.89080 |
| 12 | 0.00980 | 11.71960 | 0.00000 | 11.45470 | 0.00000 | 11.55260 |
| 13 | 0.00330 | 10.55940 | 0.00010 | 10.48940 | 0.00000 | 10.37920 |
| 14 | 0.00250 | 10.16830 | 0.00110 | 10.16810 | 0.00000 | 10.06730 |
| 15 | 0.00285 | 9.08335 | 0.00023 | 9.23697 | 0.00005 | 9.25088 |
| 16 | 0.00979 | 7.20059 | 0.00157 | 7.22987 | 0.00010 | 7.14700 |
| 17 | 0.02842 | 6.68326 | 0.03427 | 6.87957 | 0.00006 | 6.65635 |
| 18 | 0.00647 | 7.95057 | 0.00005 | 7.93155 | 0.00004 | 7.87530 |
| 19 | 0.00648 | 9.25758 | 0.00002 | 9.21798 | 0.00001 | 9.09669 |
| 20 | 0.00980 | 10.65710 | 0.00040 | 10.59840 | 0.00000 | 10.55290 |
| 21 | 0.00409 | 9.90149 | 0.00027 | 9.89417 | 0.00009 | 9.81892 |
| 22 | 0.00373 | 7.87063 | 0.00068 | 7.87302 | 0.00007 | 7.57693 |
| 23 | 0.00331 | 6.15349 | 0.00127 | 5.91707 | 0.00003 | 5.76039 |
| 24 | 0.00288 | 4.97762 | 0.00069 | 4.69031 | 0.00002 | 4.46665 |
| ΣP_{loss} (MW) | 196.6615 | | 193.8921 | | 192.0672 | |
| Total operating fuel cost (\$) | 44677.30 | | 43154.90 | | 48,848.20 | |
| CPU (s) | -- | | 308.400 | | 221.520 | |

* With the integration of the constrained search-tactic offered in [18].

V. CONCLUSION

This paper has employed the ABC algorithm with the constrained search-tactic previously offered by the same authors in solving the DED problem. Different test cases as well as a comparative analysis verified the effectiveness of the proposed algorithm. An attempt of integrating renewable energy source and analyzing its impact on the objective function has been addressed in this paper. A fraction contribution of RS led to a significant reduction in the operating fuel cost. From the promising outcomes, the ABC method has a potential to be applied in the dynamic economic and emission dispatch problems in future publications.

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