

Regarding AR(1) models, which of the following statements are true?

- (a) For a positive value of  $\phi$ , the ACF exponentially decrease to zero as the lag  $h$  increases.
- (b) (c) For a positive value of  $\phi$ , the ACF exponentially converges to zero as the lag  $h$  increases.
- (c) (d)  $\phi$  is the slope in the AR(1) model and the lag 1 autocorrelation.

The Ljung-Box statistic,  $Q(m)$ , is a function of the accumulated sample autocorrelations,  $r_j$ ,  $j = 1, 2, \dots, m$ , up to any specified time lag  $m$ . Which of the following sentence(s) is(are) true?

- a. When applied to  $x_t$ , the sample raw data, the null distribution of  $Q(m)$  is approximately a  $\chi^2$  distribution with  $df = m$ .
- b. When applied to  $w_t$ , the residuals of a time series model, under the null hypothesis, the distribution of  $Q(m)$  is approximately a  $\chi^2$  distribution with  $df = m - p$ ,  $m > p$ , where  $p$  is the number of coefficients in the model.

Please consider the following ARIMA model, ARIMA(1,0,1)(1,0,0)<sub>12</sub>. Which of the polynomials below is correct?

- (a)  $(1 - \phi B)(1 - \Phi B^{12})(x_t - \mu) = (1 + \theta B)w_t$

Consider the following model:  $(1 - \phi B)(1 - B)x_t = w_t$ ,

- (a) ARIMA(1,1,0)

The  $\Psi$ -weights are needed to calculate the confidence intervals of a forecast. From the sentences below choose the one(s) that is(are) true.

- (a) The  $\Psi$ -weight  $\Psi_0$ , is used to determine the standard error of the one-step ahead prediction.
- (b) If our forecast is for periods very far out the end of the time series the total variance of the time series will be incorporated in the forecast.

For a time series the partial autocorrelation function, or PACF, between  $x_t$  and  $x_{t-h}$  is defined as:

- (c) the conditional correlation between  $x_t$  and  $x_{t-h}$ , conditional on  $x_{t-h+1}, \dots, x_{t-1}$ , the set of observations between the time points  $t$  and  $t - h$ ,  $h = 0, \pm 1, \pm 2, \dots$

Which of the following is the one that better allows you to determine if the residuals of a model are normally distributed?

- (a) The q-q plot of the time series.

Consider the usual algebraic representation of the AR(1) process:

- a. An interesting property of a weak stationary time series is that theoretically it has the same structure forward as it does backwards.
- b. A requirement for a stationary AR(1) is that the absolute value of  $\phi$  is: below 1