

Homework on Data-Driven Systems

The problems selected for assignment 1 are P1 and P3, all the relevant Matlab code is available at: <https://github.com/FilippoGuarda/Sidra-2024---Data-Driven-Systems-Homeworks/tree/main>

Assignment 1:

In both exercises P1 and P3, we first run a simulation with bounded random input and initial state, for P1 we also add a disturbance less than plus minus 0.1.

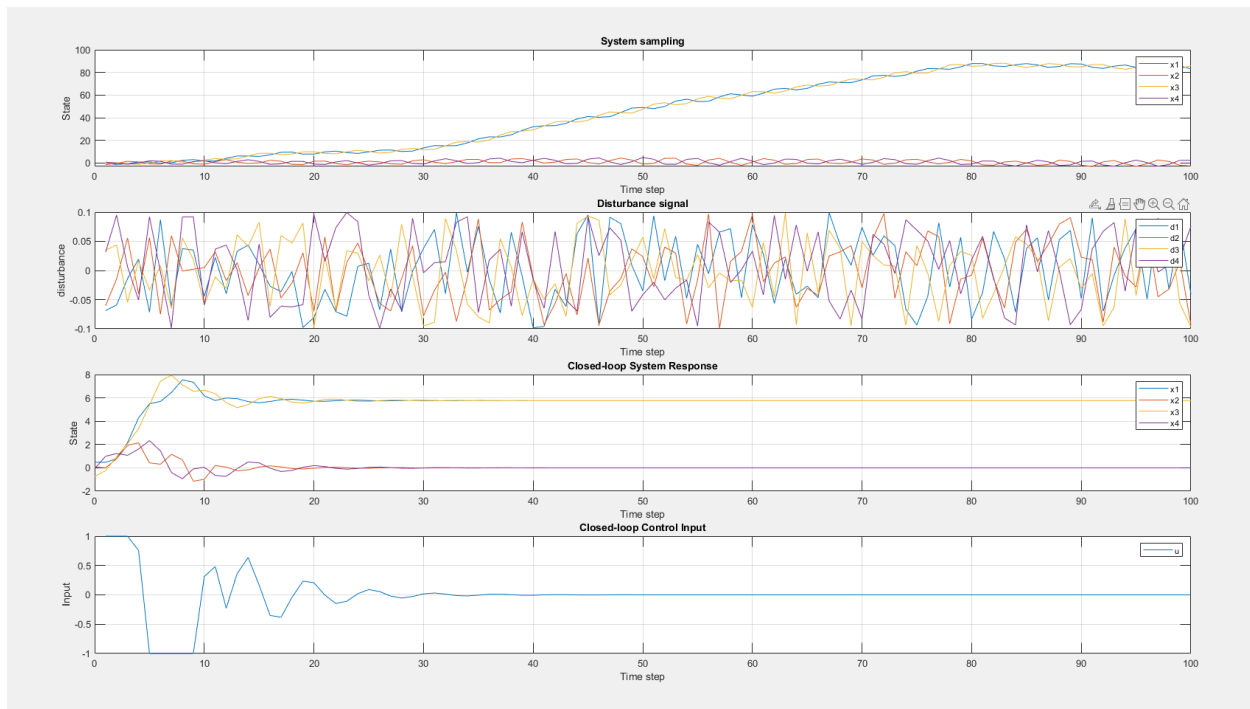
After obtaining U_0 , X_1 , X_0 in P1 we solve for Y and S using cvx to obtain the gain $K = U_0^*Y*S^{(-1)}$
In the case of P3 we add a C matrix to extract $y = X_3$ from the simulated state evolution. We build Φ from U and Y vectors.

As for P1, we solve for Q and P to obtain $K = U_0^*Q^*P^{(-1)}$.

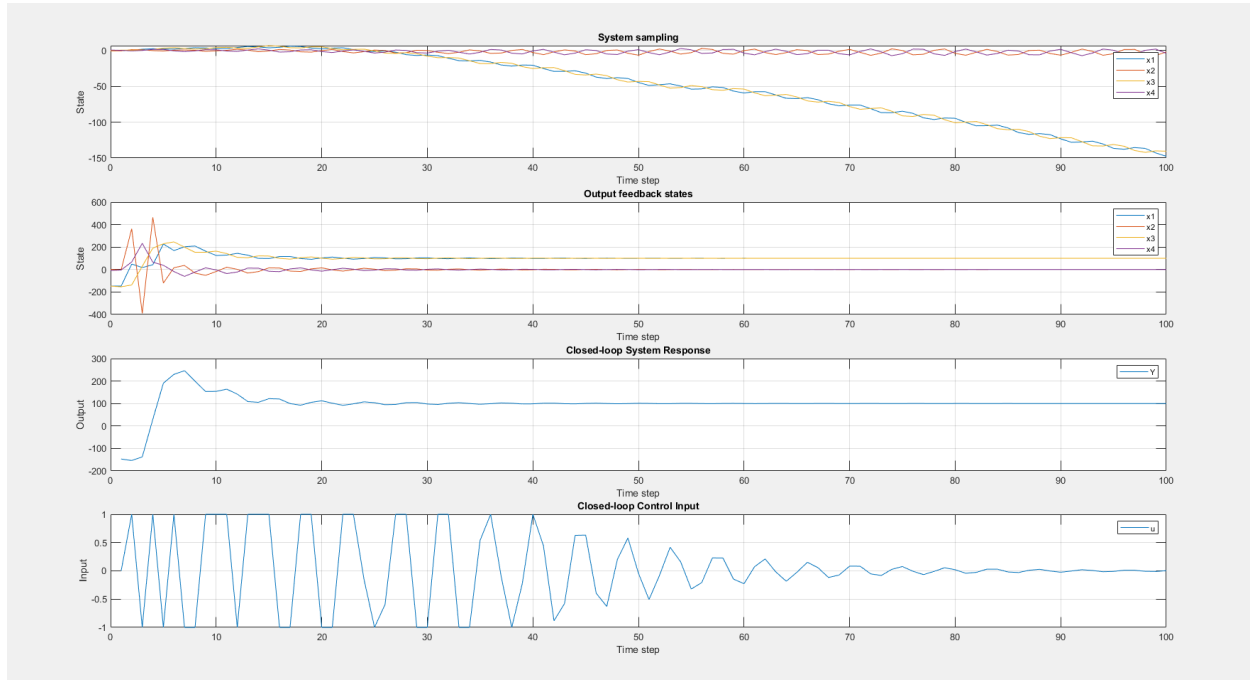
To account the impossibility of controlling both x_1 , x_2 to zero in P1 and P3 a fixed value X_e was added to separate the two equilibrium positions while computing u .

Here are the results for P1, P3.

State Feedback:



Output Feedback:



Assignment 2.

Similarly as what was done in assignment 1, we start by collecting the system state evolution from a random PE input signal, in this case though, we add an R matrix defined in such a way that it bounds all possible values of the nonlinear function $Q = [\sin(x) \ 0 \ 0 \ 0; \dots; 0 \ 0 \ 0 \ 0]$.

For example, $R = [1 \ 0 \ 0 \ 0; \dots; 0 \ 0 \ 0 \ 0] \succeq QQ^T$ for all values of x .

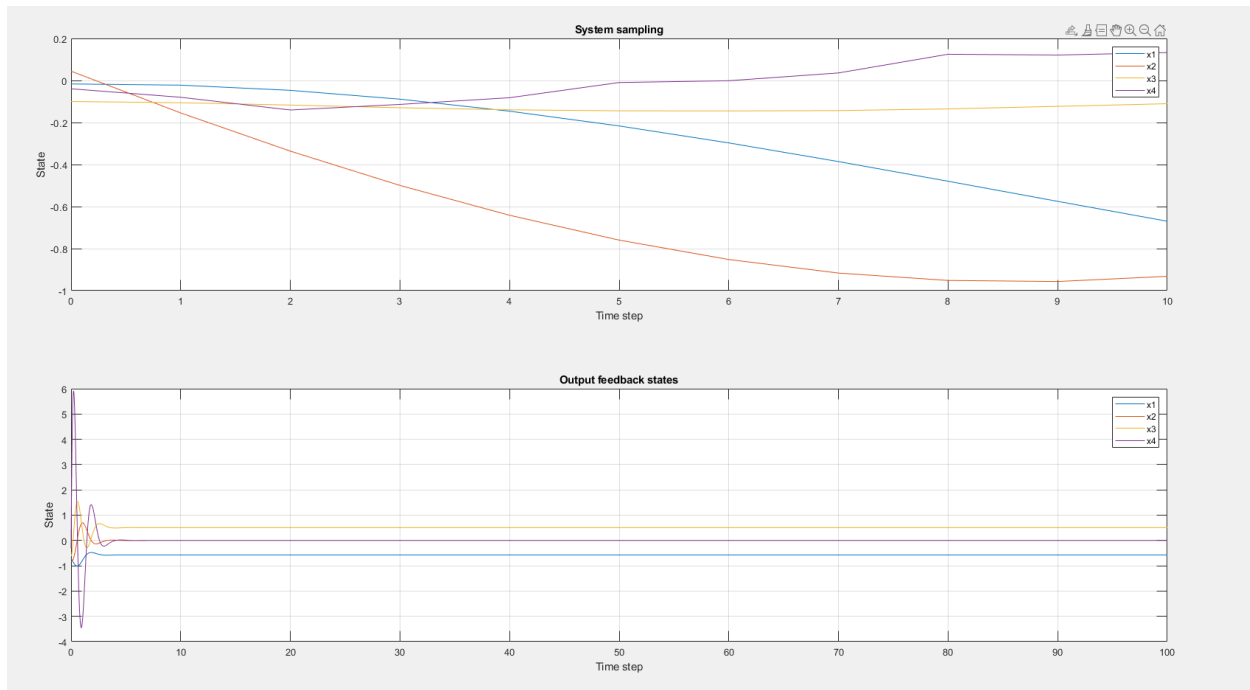
We also define a vector Z_0 which contains the linear evolution of the states prepended to the nonlinear part of the function.

As before we use cvx to solve for P , Y , G_2 . We define $G = [Y^*P(-1) \ G_2]$. Finally, $K = U_0^*G$.

For the second example we take into account the regulation error with respect to a desired equilibrium setting the target at $\pi/3$ like in the example and subsequently $x_5 = x_1 - \text{target}$.

The application of cvx is similar to previous times with the addition of the constraint $M^*[Y_1 \ G_2] = 0$.

State feedback control of robot arm:



PI control of robot arm:

