

# ECONOMETRIC ANALYSIS OF NETWORK DATA

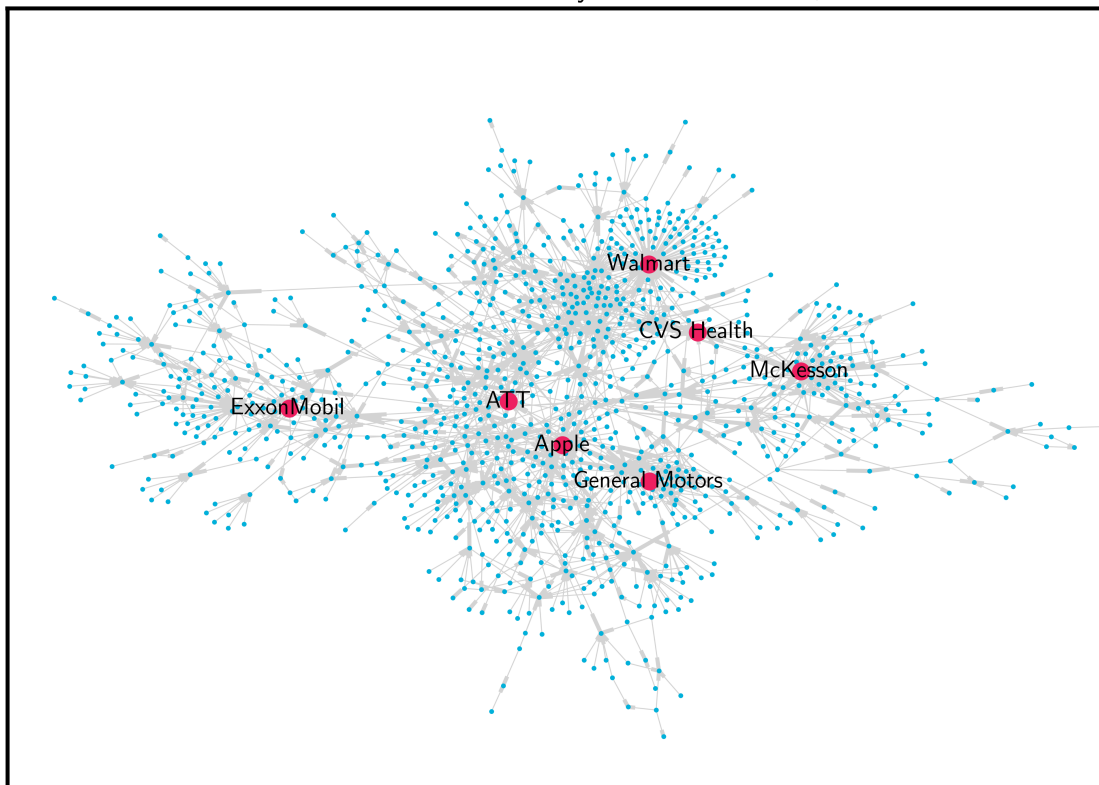
*University of Oslo*

*September, 2017*

## Course Description

This course will provide an overview of econometric methods appropriate for the analysis of social and economic networks. Many social and economic activities are embedded in networks. Furthermore, datasets with natural graph theoretic (i.e., network) structure are increasingly available to researchers. We will review (i) how to describe, summarize and visually present network data and (ii) formal econometric models of network formation that admit heterogeneity, strategic behavior, and/or dynamics. The focus will be on the formal development of methods, but selected empirical examples will also be covered, as will methods of practical computation.

United States Inter-Firm Buyer-Seller Network, 2015



Source: Compustat - Capital IQ and author's calculations.  
Raw data available at <https://wrds-web.wharton.upenn.edu/wrds/> (Accessed January 2017)

## COURSE LOGISTICS

**Instructor:** Bryan Graham, Department of Economics, University of California – Berkeley

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**Time:** To be determined.

**Prerequisites:** The equivalent of a first year Ph.D. level sequence in econometrics. Specifically an understanding of probability and statistical inference at the level of Casella and Berger (1990, *Statistical Inference*), linear regression analysis at the level of Goldberger (1991, *A Course in Econometrics*) and some exposure to non-linear models (e.g., maximum likelihood, M-estimation). I will also assume a basic knowledge of applied matrix algebra.

**Textbook:** Readings preceded by a [r] in the course outline are “required” (i.e., should ideally be read prior to class), while those preceded by a [b] are for “background” (i.e., may be useful for students interested in additional material). Students should consider purchasing the textbooks by Jackson (2006) and Newman (2010), but doing so is not necessary. The survey by Goldenberg et al. (2009) covers much of the technical literature in statistics and machine learning, but is now somewhat dated.

**Computation:** The bulk of class will be devoted to the formal development of the material, albeit with empirical illustrations as well as ample discussions of the various practicalities of implementation. However I do intend to reserve some class time for actual practice with computation. Computational examples will be done using Python. Python is a widely used general purpose programming language with good functionality for scientific computing. I highly recommend the Anaconda distribution, which is available for download at <http://continuum.io/downloads>. Some basic tutorials on installing and using Python, with a focus on economic applications, can be found online at <http://quant-econ.net>. You may also wish to install Rodeo, which is an integrated development environment (IDE) tailored to statistics or “data science” applications. Rodeo makes working in Python look and feel similar to working in Stata or MATLAB. Rodeo is also free and available at <https://www.yhat.com/>.

Good books for learning Python, with some coverage of statistical applications, are:

1. Guttag, John V. (2013). *Introduction to Computation and Programming Using Python*. Cambridge, MA: MIT Press.
2. VanderPlas, Jake. (2016). *Python Data Science Handbook: Essential Tools for Working with Data*. Cambridge: O'Reilly Media, Inc.

The former is an excellent introduction to computer science as well as Python, the latter covers core Data Science packages available in Python.

The code I will provide will execute properly in Python 2.7. Nevertheless I recommend installing Python 3.5. This is the latest Python release. Graphviz is a free graph visualization program that is also useful (<http://www.graphviz.org/>).

## COURSE OUTLINE

DATE	TOPIC	READINGS
<b>Lec 1</b> (90 min)	<b>DESCRIBING NETWORKS</b>	[r] de Paula (2016); Graham (2015); Jackson (2008, Ch. 2) [b] Goldenberg et al. (2009)
	Examples of networks	[b] Atalay et al. (2011); Mizuno et al. (2014)
	Small worlds	[b] Apicella et al. (2012); Acemoglu et al. (2012)
	Degree distributions	[b] Milgram (1967)
	Homophily	[b] Mitzenmacher (2004)
	Triads	[b] McPherson et al. (2001)
		[b] Granovetter (1973); Jackson et al. (2012)
<b>Lec 2</b> (90 min)	<b>SHOCK PROPOGATION ON NETWORKS</b>	[r] Carvalho (2014)
		[b] Acemoglu et al. (2012)
		[b] Acemoglu et al. (2016)
<b>Lec 3</b> (90 min)	<b>NONPARAMETRICS: GRAPHONS</b>	[r] Bickel & Chen (2009); Diaconis & Janson (2008)
	Estimation	[r] Chatterjee (2015); Zhang et al. (2015)
	Stochastic Block Model	[b] Daudin et al. (2000)
<b>Lec 4</b> (90 min)	<b>NONPARAMETRICS: NETWORK MOMENTS</b>	[r] Holland & Leinhardt (1976)
	Theory	[r] Bickel et al. (2011)
	Computation	[r] Bhattacharya & Bickel (2015)
		[r] Blitzstein & Diaconis (2011); Chatterjee et al. (2011)
<b>Lec 5</b> (90 min)	<b>MODELS OF NETWORK FORMATION</b>	
	Dyadic Link Formation	[r] Graham (2014)
	Dynamic Models	[r] Graham (2016)
	Strategic models	[r] de Paula et al. (2015)
<b>Lec 6</b> (90 min)	<b>PEER EFFECTS</b>	[r] Manski (1993)
		[r] Bramoullé et al. (2009)
		[b] Blume et al. (2015)

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