KIOUPRESS

Multivariate Data Analysis

R과 Python을 이용한

다변량분석

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; 3강

Ch3. 인자분석 (Factor Analysis)

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Ch4. 군집분석 (Cluster Analysis)

;6,7 강

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;8강

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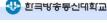
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;13,14강

총정리: 15강

1강. 다변량 시각화(1)

- 파이썬 기초
- 기술통계량 및 분할표



1. 파이썬 기초

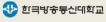


파이썬 기초

- import libraries
- comment
- pip
- if
- for
- Functions
- class
- Read text(excel) files
- Numpy
- Pandas

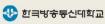
참고문헌

- (1) Statistics and Machine Learning in Python, E. Duchesnay, T. Lofstedt ftp://ftp.cea.fr/pub/unati/people/educhesnay/pystatml/StatisticsMachineLearningPythonDraft.pdf
- (2) Practical Machine Learning with R and Python, Tinniam V Ganesh https://github.com/tvganesh/PracticalMachineLearningWithRandPython



import libraries

```
# 'generic import' of math module
import math
math.sqrt(25)
# import a function from math
from math import sqrt
sqrt(25)
# import multiple functions at once from math
from math import cos, floor
import os
os.getcwd()
                                # in R, getwd()
os.chdir("c:/data/pydata")
                               # in R, setwd("c:/data/rdata")
import pandas as pd
bmi = pd.read_csv("bmi.csv")
```



주석(Comments)

comments in line

6699 99

Comments in sentences

Brian Heinold, A Practical Introduction to Python Programming, 2012. Edouard Duchesnay, Tommy Löfstedt. Statistics and Machine Learning in Python, 2018.

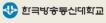
6699 99

help("modules"): 설치된 모듈 목록 보기

•••

```
_functools
                                      tabnanny
              CSV
                         numpy
                                       tarfile
_hashlib
             ctypes
                        numpydoc
                                      tblib
_heapq
              curl
                        odbc
_imp
                         odo
                                      telnetlib
            curses
brain_typing
               marshal
                           snowballstemmer zict
brain_uuid
               math
                           socket
                                           zipapp
bs4
            matplotlib
                                           zipfile
                           socketserver
builtins
             mccabe
                           socks
                                           zipimport
bz2
                           sockshandler
                                            zlib
             menuinst
cProfile
                           sortedcollections zmq
            mglearn
```

•••



pip

```
pip : Python 패키지를 설치하고 관리하는 프로그램
```

예) 패키지 mglearn, graphviz 설치하기 (Graphviz: 구글 검색 참조) Dos 창에서

pip install mglearn pip install graphviz

참고1: python - m pip install - upgrade pip

참고2: Path 설정하기

Windows 시스템 - 제어판 - 시스템 및 보완 - 시스템 - 고급 시스템 설정

- 환경변수- 시스템 변수에서 Path 편집-새로만들기에서

C:₩anaconda3₩Scripts

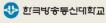
```
Microsoft Windows [Version 10.0.17134.523]
(c) 2018 Microsoft Corporation. All rights reserved.

C:#Users#HP>cd.,

C:#Users>cd.,

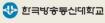
C:#Vod anaconda3

C:#wanaconda3>pip install mglearn
Requirement already satisfied: mglearn in c:#wanaconda3#lib#site-packages (0.1.7)
Requirement already satisfied: pandas in c:#wanaconda3#lib#site-packages (from mglearn) (0.23.0)
Requirement already satisfied: scikit-learn in c:#wanaconda3#lib#site-packages (from mglearn) (0.19.1)
Requirement already satisfied: matplotlib in c:#wanaconda3#lib#site-packages (from mglearn) (2.2.2)
Requirement already satisfied: pillow in c:#wanaconda3#lib#site-packages (from mglearn) (5.1.0)
Requirement already satisfied: cycler in c:#wanaconda3#lib#site-packages (from mglearn) (2.3.0)
Requirement already satisfied: imageio in c:#wanaconda3#lib#site-packages (from mglearn) (2.3.0)
Requirement already satisfied: numby in c:#wanaconda3#lib#site-packages (from mglearn) (2.3.0)
Requirement already satisfied: numby in c:#wanaconda3#lib#site-packages (from mglearn) (1.14.3)
```



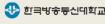
basic operations

```
# Number
10**3 # 1,000
      # 2.5
10/4
10 / float(4) # 2.5
5 % 4 # modulo 1 - remainder
10 // 4 # floor division 2
# Boolean operations
# comparisons (these return True)
5 \ 3
5 >= 3
5!=3
5 == 5
# boolean operations (these return True)
5 \ 3 and 6 \ 35 \ 3 or 5 \ 3 not False
False or not False and True
```



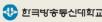
data types

```
# determine the type of an object
type(2)
               # returns 'int'
type(2.0) # returns 'float'
type('two')
                  # returns 'str'
type(True)
                  # returns 'bool'
type(None)
                  # returns 'NoneType'
# check if an object is of a given type
isinstance(2.0, int)
                           # returns False
isinstance(2.0, (int, float)) # returns True
# convert an object to a given type
float(2)
int(2.9)
str(2.9)
# zero, None, and empty containers are converted to False
bool(0)
bool(None)
bool(") # empty string
bool([]) # empty list
bool({}) # empty dictionary
```



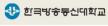
Tuples, lists and dictionaries

```
The 3 basic data types in Python are: - Tuples - List - Dictionary
**Tuples**: Tuples are immutable python objects which are enclosed with paranthesis. Immutability implies
that objects cannot be added or removed to tuples. Hence we cannot
add or remove elements from tuples. However a tuple can be removed using the del() commands
**List**: List are a sequence of disimilar objects enclosed within square brackets. Objects
can be added to lists using append() and deleted using remove()
**Dictionary**: Dictionaries are a name(key)-value pair enclosed within curly braces. The name-value
pairs are separated using a ':'. The keys must be unique in the dictionary
The length of tuples, lists and dictionaries can be obtained with the len()
# Tuples are enclosed in paranthesis
mytuple=(1,3,7,6,"test")
print(mytuple)
# Lists are enclosed in square bracket
mylist = [1, 2, 7, 4, 12]
#Dictionary - These are similar to name-value pairs
mydict={'Name':'Ganesh','Age':54,'Occupation':'Engineer'}
print(mydict)
print(mydict['Age'])
# No of elements in tuples, lists and dictionaries can be got with len()
print("Length of tuple=",len(mytuple))
print("Length of list =", len(mylist))
print("Length of dictionary =",len(mydict))
```



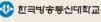
Lists

```
# empty list
empty = []
# empty = list()
empty.append(23)
empty.append(45)
empty
Out[20]: [23, 45]
```



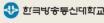
Lists

```
# list slicing [start:end:stride]
weekdays = ['mon','tues','wed','thurs','fri']
weekdays[0] # element 0
weekdays [0:3] # elements 0, 1, 2
weekdays[:3] # elements 0, 1, 2
weekdays[3:] # elements 3, 4
weekdays[-1] # last element (element 4)
weekdays[::2] # every 2nd element (0, 2, 4)
weekdays[::-1] # backwards (4, 3, 2, 1, 0)
# sort a list
simpsons.sort()
simpsons.sort(reverse=True) # sort in reverse
simpsons.sort(key=len) # sort by a key
# conatenate +, replicate *
[1, 2, 3] + [4, 5, 6]
["a"] * 2 + ["b"] * 3
```



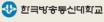
Tuples

```
# create a tuple
digits = (0, 1, 'two') # create a tuple directly
digits = tuple([0, 1, 'two']) # create a tuple from a list
# examine a tuple
digits [2] # returns 'two'
len(digits) # returns 3
digits.count(0) # counts the number of instances of that value (1)
digits.index(1) # returns the index of the first instance of that value (1)
```



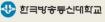
Dictionaries

```
# create a dictionary (two ways)
family = {'dad':'homer', 'mom':'marge', 'size':6}
family = dict(dad='homer', mom='marge', size=6)
# examine a dictionary
family['dad'] # returns 'homer'
len(family) # returns 3
family.keys() # returns list: ['dad', 'mom', 'size']
family.values() # returns list: ['homer', 'marge', 6]
family.items() # returns list of tuples:
               # [('dad', 'homer'), ('mom', 'marge'), ('size', 6)]
'mom' in family # returns True
'marge' in family # returns False (only checks keys)
```



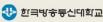
Set: 집합 - list 와 달리 중복과 순서가 없음

```
# create a set
languages = {'python', 'r', 'java'} # create a set directly
snakes = set(['cobra', 'viper', 'python']) # create a set from a list
# examine a set
len (languages) # returns 3
'python' in languages # returns True
# set operations 1
languages & snakes # returns intersection: {'python'}
languages | snakes # returns union: {'cobra', 'r', 'java', 'viper', 'python'}
languages - snakes # returns set difference: {'r', 'java'}
snakes - languages # returns set difference: {'cobra', 'viper'}
# set operations 2
s1 = \{1,2,3,4,5\}
s2 = \{2,4,6\}
print(s1.intersection(s2)) #교집합 {2, 4}
                                               print(s1.difference(s2))
                                                                           # 차집합
print(s1.union(s2))
                           # 합집합
                                               {1, 3, 5}
{1, 2, 3, 4, 5, 6}
```



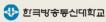
Conditional statements (조건문)

```
x = 3
# if statement
if x > 0:
  print('positive')
# if/else statement
if x > 0:
  print('positive')
else:
  print('zero or negative')
# if/elif/else statement
if x > 0:
  print('positive')
elif x == 0:
 print('zero)
else:
 print('negative')
```



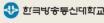
Loops (반복문)

```
# range returns a list of integers
range(0, 3) # returns [0, 1, 2]: includes first value but excludes second value
range(0, 5, 2) # returns [0, 2, 4]: third argument specifies the 'stride'
fruits = ['apple', 'banana', 'cherry']
for fruit in fruits:
  print(fruit.upper())
for fruit in fruits:
  if fruit == 'banana':
    print("Found the banana!")
    break # exit the loop and skip the 'else' block
  else:
    # this block executes ONLY if the for loop completes without hitting 'break'
    print("Can't find the banana")
count = 0
while count < 5:
  print("This will print 5 times")
  count += 1 # equivalent to 'count = count + 1'
```



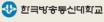
Functions

```
# define a function with no arguments and no return values
def print_text():
  print('this is text')
# call the function
print_text()
# define a function with one argument and no return values
def print_this(x):
  print(x)
# call the function
print_this(3) # prints 3
n = print_this(3) # prints 3, but doesn't assign 3 to n
                 # because the function has no return statement
# define a function with one argument and one return value
def square_this(x):
  return x ** 2
# call the function
square_this(3) # prints 9
var = square_this(3) # assigns 9 to var, but does not print 9
```



Functions - 계속

```
# default arguments
def power_this(x, power=2):
  return x ** power
power_this(2) # 4
power_this(2, 3) # 8
# return two values from a single function
def min_max(nums):
  return min(nums), max(nums)
# return values can be assigned to a single variable as a tuple
nums = [1, 2, 3]
min_max_num = min_max(nums) # min_max_num = (1, 3)
```

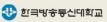


Functions - lambda

 Lambda operations all you to create small anonymous function which computes something

```
# operations on list
a = [5,2,3,1,7]
b = [1,5,4,6,8]
# Create a lambda function to add 2 numbers
add_fct = lambda x,y:x+y
add_fct(a,b)
Out[12]: [5, 2, 3, 1, 7, 1, 5, 4, 6, 8]
# Add all elements of lists a and b
print(list(map(add_fct, a,b)))
[6, 7, 7, 7, 15]
```

Ref: Practical machine learning with R and Python: 3rd ed., Tinniam V Ganesh

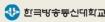


Object oriented programming (OOP)

```
import math
# Inheritance + Encapsulation
class Square():
  def __init__(self, width):
          self.width = width
  def area (self):
     return self.width ** 2
class Disk():
  def init (self, radius):
    self.radius = radius
  def area (self):
    return math.pi * self.radius ** 2
shapes = [Square(2), Disk(3)]
# Polymorphism
print([s.area() for s in shapes])
수행결과
 [4, 28.274333882308138]
```

```
1 import math
                                         In [45]: runfile('F:/□
                                         [4, 28.274333882308138]
 3# __init__ is a special method callea
 4# Inheritance + Encapsulation
                                         In [46]:
 5class Square():
      def __init__(self, width):
          self.width = width
      def area(self):
          return self.width ** 2
10 class Disk():
      def __init__(self, radius):
          self.radius = radius
      def area(self):
          return math.pi * self.radius
16 shapes = [Square(2), Disk(3)]
17# Polymorphism
18print([s.area() for s in shapes])
```

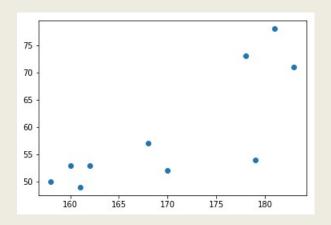
```
a= Square(2)
a.area()
Out[12]: 4
```

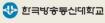


Read text file using pandas

```
import os
import pandas as pd
import matplotlib.pyplot as plt
# Set the current working directory
os.chdir("c:/data/pydata")
os.getcwd() #'c:₩₩data₩₩pydata'
# data = pd_read.csv('c:/data/pydata/bmi.csv')
data = pd.read_csv("bmi.csv")
data.head()
Out[13]:
height weight
0 181 78
  161
       49
 170 52
  160 53
4 158
       50
weig = data ['weight']
heig = data ['height']
bmi = weig/(heig/100)**2
plt.scatter(heig, weig)
plt.show()
```

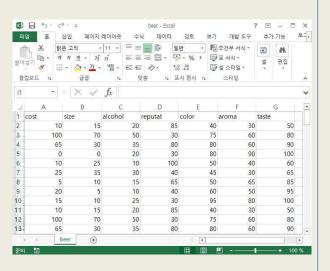
```
파일(F) 편집(F) 서식(O) 보기(V) 도움말
height,weight
181, 78
161, 49
170,52
160,53
158,50
168,57
162,53
179,54
183,71
178,73
```



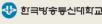


Read Excel file using pandas

```
import os
import pandas as pd
import matplotlib.pyplot as plt
# Set the current working directory
os.chdir("c:/data/pydata")
os.getcwd() #'c:₩₩data₩₩pydata'
beer = pd.read_excel("beer.xlsx, sheet_name='Beer')
beer.head()
Out[9]:
  cost size alcohol reputat color aroma taste
   10
   100 70
               50
                                       80
               35
                                       90
               20
                                      100
                      100
                                       60
beer['cost'] # beer.cost
Out[12]:
0 10
  100
  65
   0
   10
   25
```



beer.xlsx



Numpy

NumPy is one of the most fundamental package for scientific computing with Python. Numpy includes the support for handling large, multi-dimensional arrays and matrices, along with a large collection of high-level mathematical functions to operate on these arrays.

import numpy as np #Create a 1d numpy array data1 = [6, 7.5, 8, 0, 1]

arr1 = np.array(data1)
print(arr1)

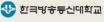
Python의 기본 자료구조

- list / tuple / dictionary / set

: The Python languge was not initially designed for numerical computing

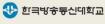
: 1995 matrix-sig group

: 2006 numpy

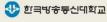


Numpy

```
# Create numpy array in a single line
import numpy as np
arr1= np.array([6, 7.5, 8, 0, 1])
#Print the array
print(arr1)
### 2D array
#Create a 2d numpy array
import numpy as np
data2 = [[1, 2, 3, 4], [5, 6, 7, 8]]
arr2 = np.array(data2)
# Print the 2d array
print(arr2)
```



2. 기술통계량 및 분할표



기술통계량 및 분할표

예제) 한설문조사에서 다음 6개 문항에 대하여 표본 추출된 40명을 대상으로 조사한 자료가 다음과 같이 정리되어 있다.

예제

문항 1.귀하의 성별은?

1)남자 2)여자

문항 2. 결혼하셨습니까?

1) 미혼 2) 기혼 3) 이혼

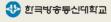
문항 3.귀하의 나이는?(단위:세)

문항 4. 귀하의 직업은?

1)회사원 2)공무원 3)노무자 4)정치가

5)학생 6)기업가 7)주부 8)기타

문항 6.가족의 월수입은?(단위: 만원)

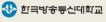


◆ csv 파일 읽기

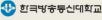
> survey = read.csv("c:/data/mva/survey.csv")

🧻 survey - Windows 메모장
파일(F) 편집(E) 서식(O) 보기(V) 도움말
seq, sex, marriage, age, job, edu, salary
1,1,1,21,1,4,60
2,1,1,22,5,5,100
3,1,1,33,1,4,200
4,2,2,33,7,4,120
5,1,2,28,1,4,70
6,1,1,21,5,5,80
7,2,2,39,7,4,190
8,1,1,32,1,4,100
9,1,2,44,3,1,120
10,1,2,55,4,4,110
11,2,2,46,7,5,150
12,1,1,20,1,4,50
13,1,2,31,6,4,210
14,1,1,27,1,4,60
15,2,1,21,5,5,80
16,2,1,22,5,5,70

1	A	В	C	D	E	F	G	Н	-
1	seq	sex	marriage	age	job	edu	salary		
2	1	1		21	1	4	60		
3	2	1	1	22	5	5	100		
4	3	1	1	33	1	4	200		
5	4	2	2	33	7	4	120		
6	5	1	2	28	1	4	70		
7	6	1	1	21	5	5	80		
8	7	2	2	39	7	4	190		
9	8	1	1	32	1	4	100		
10	9	1	2	44	3	1	120		
11	10	1	2	55	4	4	110		
12	11	2	2	46	7	5	150		
13	12	1	1	20	1	4	50		
14	13	1	2	31	6	4	210		
15	14	1	1	27	1	4	60		
16	15	2	1	21	5	5	80		
◆ ◆ ▶ ■ survey / ② /					1	4	88		▶ []



```
> survey = read.csv("c:/data/mva/survey.csv")
> head(survey,3)
  seq sex marriage age job edu salary
                    21 1
                                   60
2 2 1
                 1 22 5 5 100
                  1 33 1 4
                                  200
> mean(survey$age)
[1] 34.275
> sd(survey$age)
[1] 11.60236
> survey$sex = factor(survey$sex, levels=c(1:2), labels=c("Male", "Female"))
> survey$marriage = factor(survey$marriage, levels=c(1:3),
                          labels=c("Unmarried"."Married"."Divorced"))
> survey$job = factor(survey$job, levels=c(1:8),
                     labels=c('a','b','c','d','e','f','g','other'))
> survey$edu = ordered(survey$edu, levels=c(1:5),
                       labels=c('none','elem','med','high','college'))
```



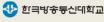
```
> summary(survey[,-1])
                         marriage
                                                                   job
                                                                                    edu
         sex
                                        age
Male :27 Unmarried:15 Min. :20.00 a :12
Female:13 Married :23 1st Qu.:24.75 f : 7
Divorced: 2 Median:32.00 g : 6
Mean :34.27 c : 5
3rd Qu.:42.50 e : 5
                                                                          none
                                                                           elem
                                                                           med
                                                                           high :19
                                                                           college: 16
                                    Max. :59.00
                                                          (Other): 2
          salary
 Min. : 50.0
 1st Qu.: 77.5
 Median : 105.0
 Mean : 130.2
 3rd Qu.: 175.0
 Max. :349.0
```



R을 이용한 그룹별 기술통계량 구하기

◎ 나이에 대한 (성별, 결혼상태, 성별x결혼상태) 평균 및 표준편차

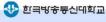
```
> tapply(survey$age, survey$sex, mean)
    Male Female
33.96296 34.92308
> with(survey, tapply(age, sex, sd))
   Male Female
11.96945 11.24323
> with(survey, tapply(age, marriage, mean))
Unmarried Married Divorced
24.66667 39.13043 50.50000
> with(survey, tapply(age, marriage, sd))
Unmarried Married Divorced
4.151879 10.467718 12.020815
```



R을 이용한 그룹별 기술통계량 구하기

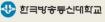
◎ 나이에 대한 (성별, 결혼상태, 성별x결혼상태) 평균 및 표준편차

```
> sex_ma = list(survey$sex, survey$marriage)
> table(sex_ma)
    sex ma.2
sex ma.1 Unmarried Married Divorced
 Male 10 15
 Female 5 8
> with(survey, tapply(age, sex_ma, mean))
      Unmarried Married Divorced
      24.8 37.86667 50.5
Male
Female 24.4 41.50000 NA
> with(survey, tapply(age, sex_ma, sd))
   Unmarried Married Divorced
Male 4.709329 11.230486 12.02082
Female 3.209361 9.071147
```



◎ 빈도표 및 분할표(성별, 교육)

```
> table(survey$sex)
 Male Female
   27
      13
> table(survey$edu)
  none elem
                  med high college
                                  16
> table(survey$sex, survey$edu)
        none elem med high college
      1 1 1 13
 Male
 Female 0 0 2 6
> sex_edu = table(survey$sex, survey$edu)
> summary(sex_edu)
Number of cases in table: 40
Number of factors: 2
Test for independence of all factors:
     Chisq = 2.5781, df = 4, p-value = 0.6307
     Chi-squared approximation may be incorrect
```



파이썬을 이용한 기술통계량 구하기

```
import numpy as np
import pandas as pd
# 데이터 읽기
survey = pd.read_csv("c:/data/mva/survey.csv")
survey.head(3)
Out[4]:
  seq sex marriage age job edu salary
                  1 21 1
                                      60
0
                  1 22 5 5 100
1 33 1 4 200
                                      200
# 평균 구하기
survey["age"].mean()
Out[5]: 34.275
# 표준편차 구하기
survey["age"].std()
Out[6]: 11.602359397542536
```



파이썬을 이용한 기술통계량 구하기

```
# 범주형 변수로 변환하기
survey["sex"] = survey["sex"].astype("category")
survey["job"] = survey["job"].astype("category")
survey["edu"] = survey["edu"].astype("category")
survey.marriage = survey.marriage.astype("category")
# 연속인 변수의 기술통계량 구하기
survey.iloc[:, 1:].describe()
Out [7]:
                    salary
            age
      40.000000 40.00000
count
      34.275000
                 130.22500
mean
std
      11.602359
                72.19258
min
      20.000000 50.00000
25%
      24.750000 77.50000
50%
      32.000000
                105.00000
75%
      42.500000
                 175.00000
      59.000000
                 349,00000
max
```



파이썬을 이용한 그룹별 기술통계량 구하기

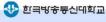
◎ 나이에 대한 (성별, 결혼상태, 성별x결혼상태) 평균 및 표준편차



파이썬을 이용한 그룹별 기술통계량 구하기

◎ 나이에 대한 (성별, 결혼상태, 성별x결혼상태) 평균 및 표준편차

```
# (sex, marriage)를 그룹으로 age의 기술통계량 구하기
agestat_by_sex_marriage = survey.groupby(["sex","marriage"])["age"].describe()
agestat_by_sex_marriage
Out[19]:
            count
                                std
                                      min 25% 50%
                                                       75%
                                                            max
                      mean
sex marriage
            10.0 24.800000 4.709329 20.0 21.00 23.5 26.75 33.0
            15.0 37.866667 11.230486 22.0 31.00 34.0 46.50 56.0
             2.0 50.500000 12.020815 42.0 46.25 50.5 54.75 59.0
             5.0 24.400000 3.209361 21.0 22.00 24.0 26.00 29.0
             8.0 41.500000 9.071147 27.0 37.50 41.0 46.75 56.0
agestat_by_sex_marriage["mean"] # 표준편차: std
Out[21]:
sex marriage
              24.800000
              37.866667
              50.500000
              24,400000
              41.500000
Name: mean. dtype: float64
```



파이썬을 이용한 기술통계량 구하기

◎ 빈도표 및 분할표(성별, 교육)

```
sex_freq = pd.crosstab(index=survey.sex, columns='count')
sex_freq
Out[31]:
col 0 count
sex
1 27
2 13
# (sex, edu)의 분할표 구하기
sex_edu_table = pd.crosstab(index=survey.sex, columns=survey.edu)
sex edu table
Out [35]:
edu 123 4 5
sex
    1 1 1 13 11
  00265
```



파이썬을 이용한 기술통계량 구하기

◎ 빈도표 및 분할표(성별, 교육)



다음시간에는

2강 다변량 시각화(2)

