## Variational Question-Answer Pair Generation for Machine Reading Comprehension

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## **Abstract**

We present a deep generative model of question-answer (QA) pairs for machine reading comprehension. We introduce two independent latent random variables into our model in order to diversify answers and questions separately. We also study the effect of explicitly controlling the KL term in the variational lower bound in order to avoid the "posterior collapse" issue, where the model ignores latent variables and generates QA pairs that are almost the same. Our experiments on SQuAD v1.1 showed that variational methods can aid OA pair modeling capacity, and that the controlled KL term can significantly improve diversity while generating high-quality questions and answers comparable to those of the existing systems.

#### 1 Introduction

Machine reading comprehension has gained much attention in the NLP community, whose goal is to devise systems that can answer questions about given documents (Rajpurkar et al., 2016; Trischler et al., 2017; Joshi et al., 2017). To build such systems, a substantial number of question-answer (QA) pairs are needed to train neural network based models. However, the creation of QA pairs from unlabeled documents requires considerable manual effort. To alleviate this problem, there has been a resurgence of work on automatic QA pair generation for data augmentation (Yang et al., 2017a; Du and Cardie, 2018; Subramanian et al., 2018; Alberti et al., 2019; Wang et al., 2019).

When the answers are text spans in a given paragraph, QA pair generation systems have generally used a pipeline of answer extraction (AE) and question generation (QG) models. QG aims to generate questions from each paragraph or sentence. Du et al. (2017) first used sequence-to-sequence models for QG and improved the quality, replacing

#### Context:

... Their hiatus saw the release of Beyoncé's debut album, Dangerously in Love (2003), which established her as a solo artist worldwide, earned <u>five</u> Grammy Awards and featured the Billboard Hot 100 number-one singles "Crazy in Love" and "Baby Boy".

#### Question-answer pairs:

What album made her a worldwide known artist?

— Dangerously in Love

What was the first album Beyoncé released as a solo artist?

— Dangerously in Love

What was the name of Beyonce's first solo album?

— Dangerously in Love

Table 1: Example of QA pairs with context in SQuAD v1.1 (Rajpurkar et al., 2016). Underlined text spans in the context are used as the gold answers. The listed QA pairs show the case in which multiple questions can be created from a single context-answer pair.

a rule-based method (Heilman and Smith, 2010). Following works used answers as additional input and showed that answers aid quality of QG (Zhou et al., 2018; Kim et al., 2018; Zhao et al., 2018). Since answers are not available in the real case, AE has been studied in addition to QG. AE aims to extract from documents question-worthy phrases, which are defined by Subramanian et al. (2018) and Wang et al. (2019) as phrases that are worth being asked about. Subramanian et al. (2018) and Kumar et al. (2018) proposed to extract answer candidates from documents and to generate questions from documents and the extracted answers. Similarly, Du and Cardie (2018) proposed to generate OA pairs such that requires coreference resolution. Moreover, Alberti et al. (2019) presented QA pair generation with roundtrip consistency that filters out unanswerable QA pairs using BERT (Devlin et al., 2019).

However, to the best of our knowledge, the diversity of QA pairs has been less studied. For QG,

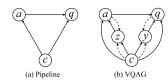


Figure 1: Graphical models of a pipeline model (a) and our Variational Question-Answer Pair Generative model (VQAG) (b). (c: context, a: answer, q: question, z and y: latent variables, **solid**: generative model, **dashed**: inference model)

a few studies focused on diversity (Yao et al., 2018; Bahuleyan et al., 2018). Namely, existing QA pair generation systems can only extract a fixed set of answer spans from each document. Since answers are important features for QG, the lack of diversity in answers should lead to the lack of diversity in questions. Here, we specifically focus on QA pair generation where AE and QG are distinctive stochastic processes that generate diverse outputs. For example, as shown in Table 1, multiple answer candidates such as "2003" and "Dangerously in Love" can be extracted from the context about Beyoncé, and multiple questions can be created from the answer "Dangerously in Love".

It is known that using a variational autoencoder (VAE) (Kingma and Welling, 2013) can diversify the generated text and generate unseen sentences from latent space (Bowman et al., 2016). Moreover, a conditional VAE (CVAE) can generate not only diverse sentences but also condition them on additional variables (Zhao et al., 2017). Here, we conjecture that the CVAE framework may be suitable for QA pair generation conditioned on context. Therefore, we propose a variational QA pair generative model (VQAG). As shown in Figure 1, we introduce two independent latent random variables into our VQAG to model the two one-to-many problems, AE and QG, enabling us to diversify AE and QG separately. We also study the effect of controlling the KL term in the variational lowerbound by introducing hyperparameters to mitigate the posterior collapse issue, where the model ignores latent variables and generate outputs that are almost the same.

We conducted experiments on three tasks, i.e., QA pair modeling, answer extraction, and answeraware question generation, using SQuAD v1.1. QA pair modeling is our newly developed task that enables us to assess the distribution modeling capacity of QA pair generative models. Our qualitative anal-

ysis reveals that our model can generate reasonable QA pairs that are not close to the ground truths.

Contributions Our main contributions are threefold: (1) We propose a Variational Question-Answer Pair Generative model including two independent latent random variables for modeling the diversity of AE and QG separately. To the best of our knowledge, our work is the first to introduce variational methods for both AE and QG jointly. (2) We develop the QA pair modeling task and show that our variational model achieves better modeling capacity than a non-stochastic model in terms of the negative log likelihood. (3) We show that explicitly controlling the KL term in the variational lowerbound objective can avoid the posterior collapse issue. Our model with the controlled KL value significantly improve diversity while generating high-quality questions and answers comparable or superior to those of the existing systems for AE and QG.

#### 2 Related Work

#### 2.1 Answer Extraction

Answer extraction (AE) can be performed in mainly three ways, i.e., 1) using linguistic knowledge, 2) sequence labeling, and 3) using a pointer network.

Yang et al. (2017a) extracted candidate phrases using rule-based methods such as part-of-speech tagger, a simple constituency parser, and named entity recognizer (NER). However, in the SQuAD dataset, not all the named entities, noun phrases, verb phrases, adjectives, or clauses, are used as gold answer spans. So, these rule-based methods are likely to extract many trivial phrases.

Therefore, there have been studies on training neural models to identify question-worthy phrases. Subramanian et al. (2018) treated the positions of answers as a sequence and used a pointer network (Vinyals et al., 2015). Du and Cardie (2018) framed the AE problem as a sequence labeling task and used BiLSTM-CRF (Huang et al., 2015) with NER features as additional inputs. Wang et al. (2019) used a pointer network and Match-LSTM (Wang and Jiang, 2016, 2017) to interact with the question generation module. Alberti et al. (2019) made use of pretrained BERT (Devlin et al., 2019) for AE.

Note that these current AE models are deterministic, i.e., their output is static when the input is fixed. As far as we know, our work is the first

to introduce a pointer network incorporating a latent random variable. In this paper, we assume that the answer spans used in the SQuAD dataset are question-worthy, but there should be question-worthy phrases not used as the gold answer spans in the dataset.

#### 2.2 **Question Generation**

Traditionally, Question Generation (QG) was studied using rule-based methods (Mostow and Chen, 2009; Heilman and Smith, 2010; Lindberg et al., 2013; Labutov et al., 2015) These rule-based methods use only the syntactic roles of words.

Since Du et al. (2017) proposed a neural sequence-to-sequence model (Sutskever et al., 2014) for QG and improved its BLEU scores compared to rule-based methods, neural models that take context and answer as inputs has started to be used to improve question quality with attention (Bahdanau et al., 2014) and copying (Gulcehre et al., 2016; Gu et al., 2016) mechanisms. Most works focused on generating relevant questions from answer-context pairs (Zhou et al., 2018; Song et al., 2018; Zhao et al., 2018; Sun et al., 2018; Kim et al., 2018; Harrison and Walker, 2018; Liu et al., 2019; Qiu and Xiong, 2019; Zhang and Bansal, 2019; Scialom et al., 2019). These works showed the importance of answers as input features for question generation. Other works studied predicting question types (Zhou et al., 2019; Kang et al., 2019), modeling structured answer-relevent relation (Li et al., 2019), and refining generated questions (Nema et al., 2019). To further improve question quality, policy gradient techniques have been used (Yuan et al., 2017; Yang et al., 2017a; Yao et al., 2018; Kumar et al., 2018). Dong et al. (2019) used a pretrained language model. While the above QG models do not handle cases in which multiple questions can be created from a single context-answer pair, the diversity of questions has been tackled using variational attention (Bahuleyan et al., 2018) or the CVAE (Yao et al., 2018).

Our work is different from these works in that we study QA pair generation by introducing variational methods into both AE and QG and that we evaluate diversity and modeling capacity of our model.

Further, constructing better QA pair generative models need to be constructed for not only data augmentation but also directly applying them to question answering. Lewis and Fan (2019) proposed to perform question answering tasks by re-

formulating them as  $a = \operatorname{argmax}_a p(q, a|c) = \operatorname{argmax}_a p(q|a, c)p(a|c)$ , and showed that the reformulation helped to mitigate the superficial understanding problems of machine reading comprehension (Weissenborn et al., 2017).

## 3 VQAG: Variational Question-Answer Pair Generative model

# 3.1 Background: Conditional Variational Autoencoder

The VAE (Kingma and Welling, 2013) is a popular deep generative model. It consists of a neural encoder (inference model) and a decoder (generative model). The encoder learns to map from an observed variable, x, to a latent variable, z, and the decoder works vice versa. *Neural approximation* and *reparameterization* techniques of VAE have been applied to NLP tasks such as text generation (Bowman et al., 2016), machine translation (Zhang et al., 2016), and sequence labeling (Chen et al., 2018).

The CVAE is an extension of the VAE, in which the prior distribution of a latent variable is explicitly conditioned on certain variables and enables generation processes to be more diverse than a VAE (Li et al., 2018; Zhao et al., 2017; Shen et al., 2017). The CVAE is trained by maximizing the following variational lower bound:

$$\log p_{\theta}(x|c) \ge \mathbb{E}_{z \sim q_{\phi}(z|x,c)}[\log p_{\theta}(x|z,c)] - D_{\text{KL}}(q_{\phi}(z|x,c)||p_{\theta}(z|c))$$
(1)

where  $D_{\rm KL}$  means the Kullback-Leibler divergence, c is the condition, and  $\theta$  ( $\phi$ ) is parameters of the generative (inference) model parameterized by neural networks.

#### 3.2 Problem Definition

Here, the problem is to generate QA pairs from contexts (documents). We focus on the case in which an answer is a text span in the context. We use c, q, and a to represent the context, question, and answer, respectively.

We assume that every QA pair is sampled independently given a context. Thus, the problem is defined as maximizing the following conditional log likelihood:

$$\log \prod_{k=1}^{N} p(q^k, a^k | c^k) = \sum_{k=1}^{N} \log p(q^k, a^k | c^k)$$

where N is the size of the training, development, or test set. For simplicity, we remove superscript k in the following sections.

#### 3.3 Variational Lower Bound

Because questions and answers are different types of observed variables, embedding QA pairs into different latent spaces may be suitable. For example, different questions can correspond to the same answer (Table 1). Thus, we introduce two independent latent random variables to assign the role of diversifying AE and QG to z and y, respectively (see Figure 1 (b)). The variational lower bound of our VQAG is as follows:

$$\log p_{\theta}(q, a|c) \ge \mathbb{E}_{z, y \sim q_{\phi}(z, y|q, a, c)} [\log p_{\theta}(q|y, a, c) + \log p_{\theta}(a|z, c)] - D_{\text{KL}}(q_{\phi}(z|a, c)||p_{\theta}(z|c)) - D_{\text{KL}}(q_{\phi}(y|q, c)||p_{\theta}(y|c)).$$
(2)

See Appendix A for the derivation of Eq. 2.

#### 3.4 Explicit KL control

VAEs often suffer from "posterior collapse", where the model learns to ignore latent variables and generates outputs that are almost the same. This problem occurs especially when VAEs are used for modeling discrete data and implemented with strong decoders such as LSTM (Bowman et al., 2016). Many approaches have been proposed to mitigate this issue, such as weakening the generators (Bowman et al., 2016; Yang et al., 2017b; Semeniuta et al., 2017), or modifying the objective functions to control the KL term (Tolstikhin et al., 2018; Zhao et al., 2017; Higgins et al., 2017).

We also observe that this issue happens when implementing our model according to the Ineq. 2. To mitigate this problem, inspired by Prokhorov et al. (2019), we use modified  $\beta$ -VAE (Higgins et al., 2017) proposed by Burgess et al. (2018), which uses two hyperparameters to control the KL terms. Our modified variational lower bound is as follows:

$$\log p_{\theta}(q, a|c) \geq \mathbb{E}_{z, y \sim q_{\phi}(z, y|q, a, c)} [\log p_{\theta}(q|y, a, c) + \log p_{\theta}(a|z, c)] - \beta |D_{\text{KL}}(q_{\phi}(z|a, c)||p_{\theta}(z|c)) - C| - \beta |D_{\text{KL}}(q_{\phi}(y|q, c)||p_{\theta}(y|c)) - C|,$$
(3)

where  $\beta > 0$  and  $C \ge 0$ . We use the same  $\beta$  and C for the two KL terms for simplicity. In this paper, we set  $\beta = 1$  and change only C because C was enough to regularize the KL terms in our case (see Table 2).

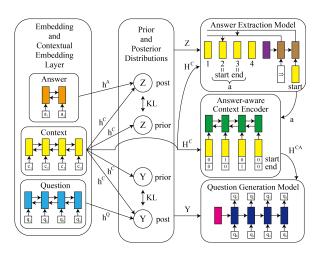


Figure 2: Overview of the model architecture. Each module with its input and output is shown. Note that the latent variables z and y are sampled from the posteriors when computing the variational lower bound and from the priors during generation. See  $\S 3.5$  for detailed computation in each module.

#### 3.5 Model Architecture

An overview of our VQAG is given in Figure 2. We describe the details of each module below. Here, we denote  $c = \{c_t\}_{t=1}^{L_C}$ ,  $q = \{q_t\}_{t=1}^{L_Q}$ , and  $a = \{a_t\}_{t=1}^{L_A} = \{c_t\}_{t=start}^{end}$ , where each element represents one word, and  $L_C$ ,  $L_Q$ , and  $L_A$  are, respectively, the lengths of the context, question, and answer span.

#### **Embedding and Contextual Embedding Layer**

First, in the embedding layer, the ith word,  $w_i$ , of a sequence of length L is simultaneously converted into word- and character-level embedding vectors,  $e_i^w$  and  $e_i^c$ , by using a convolutional neural network (CNN) based on Kim (2014). Then,  $e_i^w$  and  $e_i^c$  are concatenated across columns and  $e_i = [e_i^w; e_i^c]$  is obtained.

After that, we pass the embedding vectors to the contextual embedding layer as follows:

$$H, h = \text{BiLSTM}([e_1^T; e_2^T; ...; e_L^T])$$
 (4)

where  $H \in \mathbb{R}^{L \times 2d}$  is the concatenated outputs of LSTMs (Hochreiter and Schmidhuber, 1997) in each direction at each time step,  $e^T$  denotes the transpose of e, and  $h \in \mathbb{R}^{2d}$  is the concatenated last hidden state vectors of LSTMs in each direction. This bidirectional LSTM (BiLSTM) encoder is shared by the AE and QG tasks. The outputs have superscripts,  $H^C$ ,  $h^C$ ,  $H^Q$ ,  $h^Q$ ,  $H^A$ , and  $h^A$  to indicate where they come from; i.e., C, Q, and

A denote the context, question, and answer, respectively.

#### **Prior and Posterior Distributions**

Following Zhao et al. (2017), we hypothesized that the prior and posterior distributions of the latent variables follow multivariate Gaussian distributions with diagonal covariance. The distributions are described as follows:

$$\begin{split} z|a,c &\sim \mathcal{N}(\mu_{post_Z}, diag(\sigma_{post_Z}^2)) \\ z|c &\sim \mathcal{N}(\mu_{prior_Z}, diag(\sigma_{prior_Z}^2)) \\ y|q,c &\sim \mathcal{N}(\mu_{post_Y}, diag(\sigma_{post_Y}^2)) \\ y|c &\sim \mathcal{N}(\mu_{prior_Y}, diag(\sigma_{prior_Y}^2)). \end{split}$$

The prior and posterior distributions of the latent variables, z and y, are computed as follows:

$$\begin{bmatrix} \mu_{post_Z} \\ \log(\sigma_{post_Z}^2) \end{bmatrix} = W_{post_Z} \begin{bmatrix} h^C \\ h^A \end{bmatrix} + b_{post_Z}$$
$$\begin{bmatrix} \mu_{prior_Z} \\ \log(\sigma_{prior_Z}^2) \end{bmatrix} = W_{prior_Z} h^C + b_{prior_Z}$$
$$\begin{bmatrix} \mu_{post_Y} \\ \log(\sigma_{post_Y}^2) \end{bmatrix} = W_{post_Y} \begin{bmatrix} h^C \\ h^Q \end{bmatrix} + b_{post_Y}$$
$$\begin{bmatrix} \mu_{prior_Y} \\ \log(\sigma_{prior_Y}^2) \end{bmatrix} = W_{prior_Y} h^C + b_{prior_Y}.$$

Then, latent variable z (and y) is obtained using the reparameterization trick (Kingma and Welling, 2013):  $z = \mu + \sigma \odot \epsilon$ , where  $\odot$  represents the Hadamard product, and  $\epsilon \sim \mathcal{N}(0, I)$ . Then, z and y is passed to the AE and QG models, respectively.

#### **Answer Extraction Model**

We regard answer extraction as two-step sequential decoding, i.e.,

$$p(a|c) = p(c_{end}|c_{start}, c)p(c_{start}|c),$$
 (5)

that predicts the start and end positions of an answer span in this order. For AE, we modify a pointer network (Vinyals et al., 2015) to take into account the initial hidden state  $h_0^{AE} = W_1 z + b_1$ , which in the end diversify AE by enabling the mappings from z to a to be learned. The decoding process is as follows:

$$h_i^{IN} = \begin{cases} e(\Rightarrow) & \text{if } i = 1\\ H_{t_{i-1}}^C & \text{if } i = 2 \end{cases}$$

$$h_i^{AE} = \text{LSTM}(h_{i-1}^{AE}, h_i^{IN})$$

$$u_{ij}^{AE} = (v^{AE})^T \tanh(W_2 H_j^C + W_3 h_i^{AE} + b_2)$$

$$p(c_{t_i}|c_{t_{i-1}}, c) = \text{softmax}(u_i)$$

where  $1 \le i \le 2$ ,  $1 \le j \le L_C$ ,  $h_i^{AE}$  is the hidden state vector of the LSTM,  $h_i^{IN}$  is the *i*th input,  $t_i$  denotes the start (i=1) or end (i=2) positions in c, and v,  $W_n$  and  $b_n$  are learnable parameters. We learn the embedding of the special token " $\Rightarrow$ " as the initial input  $h_1^{IN}$ .

When we used the embedding vector  $e_{t_i}$  as  $h_{i+1}^{IN}$ , instead of  $H_{t_i}^C$ , following Subramanian et al. (2018), we observed that the extracted spans tended to be long and unreasonable. We assume that this is because the decoder cannot get the positional information from the input in each step.

#### **Answer-aware Context Encoder**

To compute answer-aware context information for QG, we use another BiLSTM as follows:

$$H^{CA}, h^{CA} = \text{BiLSTM}([H^C, o_{start}, o_{end}])$$
 (6)

where  $o_{start}$  and  $o_{end} \in \mathbb{R}^{L_C}$  are the one-hot vectors of the start and end positions of an answer span.  $H^{CA} \in \mathbb{R}^{L_C \times 2d}$  is used as the source for attention and copying in question generation.  $(h^{CA} \in \mathbb{R}^{2d})$ 

#### **Question Generation Model**

For QG, we modify an LSTM decoder with attention and copying mechanisms to take the initial hidden state  $h_0^{QG} = W_4 y + b_3$  as input to diversify QG. In detail, at each time step, the probability distribution of generating words from vocabulary using attention (Bahdanau et al., 2014) is computed as:

$$\begin{split} h_i^{QG} &= \text{LSTM}(h_{i-1}^{QG}, q_{t-1}) \\ u_{ij}^{att} &= (v^{att})^T \text{tanh}(W_5 h_i^{QG} + W_6 H_j^{CA} + b_4) \\ a_i^{att} &= \text{softmax}(u_i^{att}) \\ \hat{h}_i &= \sum_j a_{ij}^{att} H_j^{CA} \\ \tilde{h}_i &= \text{tanh}(W_7([\hat{h}_i; h_i^{QG}] + b_5)) \\ P_{vocab} &= \text{softmax}(W_8(\tilde{h}_i) + b_6), \end{split}$$

and the probability distributions of copying (Gulcehre et al., 2016; Gu et al., 2016) from context are computed as:

$$u_{ij}^{copy} = (v^{copy})^T \tanh(W_9 h_i^{QG} + W_{10} H_j^{CA} + b_7)$$
  
$$a_i^{copy} = \operatorname{softmax}(u_i^{copy})$$

Accordingly, the probability of outputting  $q_i$  is:

$$p_g = \sigma(W_{11}h_i^{QG})$$

$$p(q_i|q_{1:i-1}, a, c)$$

$$= p_g P_{vocab}(q_i) + (1 - p_g) \sum_{j:c_i = q_i} a_{ij}^{copy}$$

where  $\sigma$  is the sigmoid function.

## 4 Experiments & Results

See Appendix B for the training details.

#### 4.1 Dataset

We used SQuAD v1.1 (Rajpurkar et al., 2016), a large QA pair dataset consisting of documents collected from Wikipedia and 100k QA pairs created by crowdworkers. Each question in SQuAD can be answered by a text span in a context. Since the SQuAD test set has not been released, we split the dataset following Du et al. (2017), where the original training set is split into training and development sets and the original development set is used as a test set. In so doing, the sizes of the training, development and test sets amounted to 70,484, 10,570, and 11,877, respectively.

	NLL	$NLL_a$	$\mathrm{NLL}_q$	$D_{\mathrm{KL}_z}$	$D_{\mathrm{KL}_y}$
Pipeline VQAG	36.26	3.99	32.50	-	-
C = 0	34.46	4.46	30.00	0.027	0.036
C = 5	37.00	5.15	31.51	4.862	4.745
C = 20	59.66	14.38	43.56	17.821	17.038
C = 100	199.43	81.01	112.37	92.342	91.635

Table 2: QA pair modeling capacity measured on the test set. NLL: negative log likelihood  $(-\log p(q,a|c))$ . NLL $_a=-\log p(a|c),$  NLL $_q=-\log p(q|a,c).$   $D_{\mathrm{KL}_z}$  and  $D_{\mathrm{KL}_y}$  are Kullback–Leibler divergence between the approximate posterior and the prior of the latent variable z and y. The lower NLL is, the higher the probability is that the model assigns to the test set. NLL for our models are estimated with importance sampling using 300 samples.

## 4.2 QA Pair Modeling

We originally developed a QA pair modeling to evaluate QA pair generative models. We compared models based on the bases of the probability they assigned to the ground truth QA pairs. We chose the negative log likelihood (NLL) of QA pairs as the metric, namely,  $-\frac{1}{N}\sum_{k=1}^N \log p(q^k,a^k|c^k)$ . Since variational models can not directly compute NLL, we estimate NLL with importance sampling. We also estimate each term in decomposed NLL, i.e., NLL = NLL<sub>a</sub> + NLL<sub>q</sub> =  $-\log p(a|c)$  - $\log p(q|a,c)$ . The better a model performs in this task, the better it fit the test set. As a baseline, to assess the effect of incorporating latent random variables, we implemented a pipeline model similar to Subramanian et al. (2018), eliminating all the architectures related to latent random variables in our models and treating a sequence of the start and

		Diversity				
	Precision		Re	call	Dist	
	Prop.	Exact	Prop.	Exact	2131	
NER BiLSTM-CRF	34.44	19.61	64.60	45.39	30.0k	
w/ char w/ NER (2018)	45.96	33.90	41.05	28.37	-	
VQAG						
C = 0	58.39	47.15	21.82	16.38	3.1k	
C = 5	30.16	13.41	83.13	60.88	71.2k	
C = 20	21.95	5.75	72.26	42.15	103.3k	
C = 100	23.32	7.48	71.74	39.70	84.6k	

Table 3: Results for answer extraction on the test set. For all the metrics, higher is better.

end positions of all the possible answers in context as the output of AE.

**Result** Table 2 shows the result of QA pair modeling. First, our models with C = 0 are superior to the pipeline model, which means that introducing latent random variables aid QA pair modeling capacity. However, the KL terms converge to zero with C = 0. In other tasks, it is shown that our model with C = 0 collapses into a deterministic model. The fact that NLLa is consistently lower than NLLq is due to the decomposition of probability  $p(a|c) = p(c_{end}|c_{start}, c)p(c_{start}|c)$  and  $p(q|a,c) = \prod_i p(q_i|q_{1:i-1},a,c)$ , which is sensitive to the sequence length. Also, we observe that the hyperparameter C can control the KL values, showing the potential to avoid the posterior collapse issue in our case. When we set C > 0, KL values are greater than 0, which implies that latent variables have non-trivial information about questions and answers.

#### 4.3 Answer Extraction

Inputs were the contexts and outputs were a set of multiple answer spans. Following Du and Cardie (2018), to measure the accuracy of multiple phrases, we computed *Proportional Overlap* and *Exact Match* metrics (Breck et al., 2007; Johansson and Moschitti, 2010) for each pair of a predicted answer and a ground truth. *Proportional Overlap* returns scores proportional to the amount of overlap. We report the precision and recall with respect to the above metrics.

Our models are different from existing models in

<sup>&</sup>lt;sup>1</sup>We exclude *Binary Overlap* because, as Breck et al. (2007) discussed, *Binary Overlap* assigns high scores on systems that extract the entire input context, and therefore is not a reliable metric.

	Relevance						Diversity				
	B1	B2	В3	B4	ME	RL	Token	D1	D2	E4	SB4
ELMo+QPP&QAP(2019)											
w/Beam10	48.39	32.71	24.13	18.34	24.82	46.66	133.2k	10.1k	45.8k	15.75	-
w/DivBeam50	48.59	32.83	24.21	18.40	24.86	46.66	133.8k	10.2k	46.4k	15.78	-
	B1-R	B2-R	B3-R	B4-R	ME-R	RL-R	Token	D1	D2	E4	SB4
ELMo+QPP&QAP(2019) w/DivBeam50	62.32	47.77	37.96	30.05	36.77	62.87	7.0M	15.8k	218.9k	18.28	91.44
VQAG											
C = 0	35.57	18.75	10.79	6.35	18.31	33.92	7.6M	14.4k	155.3k	17.33	97.61
C = 5	44.19	27.09	16.33	9.71	25.84	45.18	11.5M	19.0k	481.1k	19.71	82.59
C = 20	48.19	32.87	22.96	14.94	25.29	48.26	4.9M	22.4k	549.2k	19.72	44.41
C = 100	35.22	19.88	13.25	9.20	22.27	37.55	8.2M	22.1k	508.8k	19.74	44.22

Table 4: Results for answer-aware question generation on the test set of Du et al. (2017)'s split of SQuAD. Paragraph-level contexts and answer spans are used as input. Bn: BLEU-n, ME: METEOR, RL: ROUGE-L, Token: the total number of the generated words, Dn: Dist-n, E4: Ent-4 (entropy of 4-grams), SB4: Self-BLEU-4. "-R" represents recall. (e.g. B1-R is the recall of BLEU-1.) One question per answer-context pair is evaluated in the upper part, while 50 questions per answer-context pair is evaluated in the lower part to assess their diversity.

that they can generate an arbitrary number of samples and improve diversity. For comparison, we had our models extract a total of 50 answer spans from each context to assess their diversity and quality, while the existing models can extract only a fixed set of answer spans. To measure the diversity of the predicted answer spans, we calculated the Dist score as the total number of distinct spans.

For AE, we adopted two baselines, named entity recognition (NER) and BiLSTM-CRF w/ char w/NER (Du and Cardie, 2018) For NER, we used spaCy. For BiLSTM-CRF w/ char w/ NER, we directly copied the scores from Du and Cardie (2018). **Result** Table 3 shows the result. Our model with the condition C = 5 performed the best in terms of the recall scores, while surpassing NER in terms of diversity. From the viewpoint of diversity, C = 20is the best setting. However, high Dist scores do not occur together with high recall scores. This observation shows the trade-off between diversity and quality. In this task, we show that our model with C = 5 can cover most of the human-created answers and also extract more diverse answers than baselines. However, when C = 0, the Dist score is fairly low. This implies the posterior collapse issue, though the precision scores are the best.

While our models with  $C \geq 5$  had low precision, it was due to the diversity of extracted answers. If diversity is improved, answer spans that are not treated as ground truths would be extracted. Since even the test set do not cover all the possible answer spans, we assert that low precision scores do not

necessarily mean poor performance.

### 4.4 Question Generation

The inputs were the contexts and gold answer spans. To see how well our models could generate diverse questions, we had them generate a total of 50 questions from each context-answer pair.

We calculated the BLEU (Papineni et al., 2002), METEOR (Denkowski and Lavie, 2014), and ROUGE-L (Lin, 2004) scores, and report the recall scores per reference question. Since our motivation is to improve diversity, precision metrics are not appropriate in our setting. Thus, we do not report precision scores here. To measure diversity, we computed Dist-n, Ent-n (Serban et al., 2017; Zhang et al., 2018), and Self-BLEU (Zhu et al., 2018). Ent-n is the entropy (in bits) of n-grams, and it reflects how evenly n-grams are generated. Self-BLEU evaluates the degree to which sentences generated by a system resemble each other. We calculated Self-BLEU scores for 50 questions generated from each context-answer pair and averaged them. We computed Dist-n following the definition of Xu et al. (2018), wherein Dist-n is the number of distinct n-grams.<sup>2</sup> We also reported the total number of generated words as reference.

For QG, we compared our models with the ELMo+QAP&QPP model (Zhang and Bansal, 2019), which achieved the state-of-the-art in

<sup>&</sup>lt;sup>2</sup>Dist-n is often defined as the ratio of distinct n-grams (Li et al., 2016) but this is not fair when the number of generated sentences differs among models, so we did not use this.

beyonc 's vocal range spans [our octaves]. jody rosen highlights her tone and timbre as particularly distinctive, describing her voice as "one of the most compelling instruments in popular music". while another critic says she is a "vocal acrobat, being able to sing long and complex melismas and vocal runs effortlessly, and in key. her vocal abilities mean she is identified as the centerpiece of destiny 's child. (the daily mail calls beyonc 's voice" versatile", capable of exploring power ballads, soul, rock belting, operatic flourishes, and hip hop. jon pareles of the new york times commented that her voice is "velvety yet [tart], with an insistent flutter and reserves of soul belting". rosen notes that the hip hop era highly influenced beyonc 's strange rhythmic vocal style, but also finds her quite traditionalist in her use of balladry, gospel and falsetto, other critics praise her range and power), with chris richards of the washington post saying she was "capable of punctuating any beat with goose - bump - inducing whispers or full - bore diva - roars."

Table 5: Heatmap of 250 answer spans extracted using our VQAG (C = 5), the best performing model in terms of recall of Exact match (see Table 3). The darker the color is, the more often the word is extracted. The phrases surrounded by  $\bigcap$  are the ground truth answers of SQuAD.

C=0	C=5	C=20	C=100
beyonc range spans spans spans spans or four octaves spans? —four	how can one find her vocal abilities in key music? — she is identified as the centerpiece of destiny 's child	how does her voice as her voice? —one of the most compelling instruments in popular music".	leptines polybolos ? —four
beyonc range spans spans spans spans spans and which vocal range?—four	how many octaves is beyonc 's vocal range spans four oc- taves? —spans four	how many power ballads are used by chris richards? — the daily mail calls beyonc 's voice" versatile"	j.n. ? —four octaves

Table 6: Examples of QA pairs generated with our model. The input context is the same as the one in Table 5.

SQuAD QG. Since diversity metrics were not reported in that paper, we reran the model, which is publicly available <sup>3</sup>. In addition, to compare our models with the baseline under an equivalent condition, we also reran the ELMo+QAP&QPP model with diverse beam search (Li et al., 2016), kept top 50 questions per answer, and used them to calculate the metrics.

**Result** Table 4 shows the result of QG. The recall scores of our model with C=20 were comparable to the scores of ELMo+QAP&QPP w/Beam10 and w/DivBeam50. Though ELMo+QAP&QPP w/DivBeam50 is superior in terms of the recall of relevance scores, our models perform significantly better in terms of the diversity scores. This shows that our model can improve diversity while generating high-quality questions. Among the various settings of C, 20 is suitable based on this result.

#### 5 Analysis

Since it is hard to evaluate generated QA pairs that are valid but not close to the ground truths, we analyze the generated questions and answers qualitatively.

Table 5 shows the example answers extracted by our model and the gold answers of SQuAD. Our

model extracts every gold answer of SQuAD at least once. Moreover, there are answers extracted by our model that are not used in SQuAD but question-worthy. For example, "jon pareles" and "one of the most compelling instruments in popular mucis" are question-worthy because these are related to the main topic, Beyoncé. Note that our model can extract not only named entities but also phrases of other types like this example.

Table 6 shows some examples of generated QA pairs from the various settings of C. The examples with C=5 seems the most reasonable and diverse. When C=0, the generated QA pairs are reasonable but lack diversity, suffering from posterior collapse. When C=100, the generated QA paris are diverse but not reasonable. From this result, finding an appropriate value of C is necessary.

#### 6 Conclusion

We designed a variational QA pair generative model, consisting of two independent latent random variables. We showed explicitly controlling the KL term could either enable our model to perform well in distribution modeling (C=0) or avoid posterior collapse and improve diversity and recall-oriented relevance scores (C>0). However, it is not trivial how to find the optimal C.

<sup>&</sup>lt;sup>3</sup>https://github.com/ZhangShiyue/QGforQA

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## A Derivations of the Variational Lower Bound

The equation 2 is derived as follows:

$$\begin{split} \log p_{\theta}(q, a | c) \\ &= \mathbb{E}_{z, y \sim q_{\phi}(z, y | q, a, c)} \left[ \log p_{\theta}(q, a | c) \right] \\ &= \mathbb{E}_{z, y} \left[ \log \frac{p_{\theta}(q, a | z, y, c) p_{\theta}(z, y | c)}{p_{\theta}(z, y | q, a, c)} \right] \\ &= \mathbb{E}_{z, y} \left[ \log \frac{p_{\theta}(q, a | z, y, c) p_{\theta}(z, y | c)}{p_{\theta}(z, y | q, a, c)} \right] \\ &= \mathbb{E}_{z, y} \left[ \log \frac{p_{\theta}(q, a | z, y, c) p_{\theta}(z, y | c)}{p_{\theta}(z, y | q, a, c)} \right] \\ &= \mathbb{E}_{z, y} \left[ \log \frac{p_{\theta}(q | y, a, c) p_{\theta}(y | c)}{p_{\theta}(y | q, c)} \right. \\ &+ \log \frac{p_{\theta}(a | z, c) p_{\theta}(z | c)}{p_{\theta}(z | a, c)} \\ &+ \log \frac{q_{\phi}(y | q, c)}{q_{\phi}(y | q, c)} + \log \frac{q_{\phi}(z | a, c)}{q_{\phi}(z | a, c)} \right] \\ &= \mathbb{E}_{z, y} \left[ \log p_{\theta}(q | y, a, c) + \log p_{\theta}(a | z, c) \right. \\ &+ \log \frac{p_{\theta}(y | c)}{q_{\phi}(z | a, c)} + \log \frac{q_{\phi}(y | q, c)}{p_{\theta}(z | a, c)} \right] \\ &= \mathbb{E}_{z, y} \left[ \log p_{\theta}(q | y, a, c) + \log p_{\theta}(a | z, c) \right] \\ &- D_{KL}(q_{\phi}(y | q, c) | | p_{\theta}(y | c)) \\ &+ D_{KL}(q_{\phi}(z | a, c) | | p_{\theta}(z | a, c)) \\ &\geq \mathbb{E}_{z, y} \left[ \log p_{\theta}(q | y, a, c) + \log p_{\theta}(a | z, c) \right] \\ &- D_{KL}(q_{\phi}(y | q, c) | | p_{\theta}(y | c)) \\ &- D_{KL}(q_{\phi}(y | q, c) | | p_{\theta}(y | c)) \\ &- D_{KL}(q_{\phi}(y | q, c) | | p_{\theta}(y | c)) \\ &- D_{KL}(q_{\phi}(z | a, c) | | p_{\theta}(y | c)) \right. \\ \end{array}$$

#### **B** Training Details

We use pretrained GloVe (Pennington et al., 2014) vectors with 300 dimensions and freeze them during training. The pretrained word embeddings were shared by the input layer of the context encoder, the input and output layers of the question decoder. The vocabulary have most frequent 50k words in our training set. The dimension of character-level embedding vectors is 32. The number of windows are 100. The dimension of hidden vectors are 300. The dimension of latent variables are 200. Any LSTMs used in this paper has one layer. We used Adam (Kingma and Ba, 2014) for optimization

with initial learning rate 0.001. All the parameters was initialized with Xavier Initialization (Glorot and Bengio, 2010). Models were trained for 20 epochs with a batch size of 16. We used a dropout (Srivastava et al., 2014) rate of 0.2 for all the LSTM layers and attention modules.