

# Feature Structures and Unification Grammars

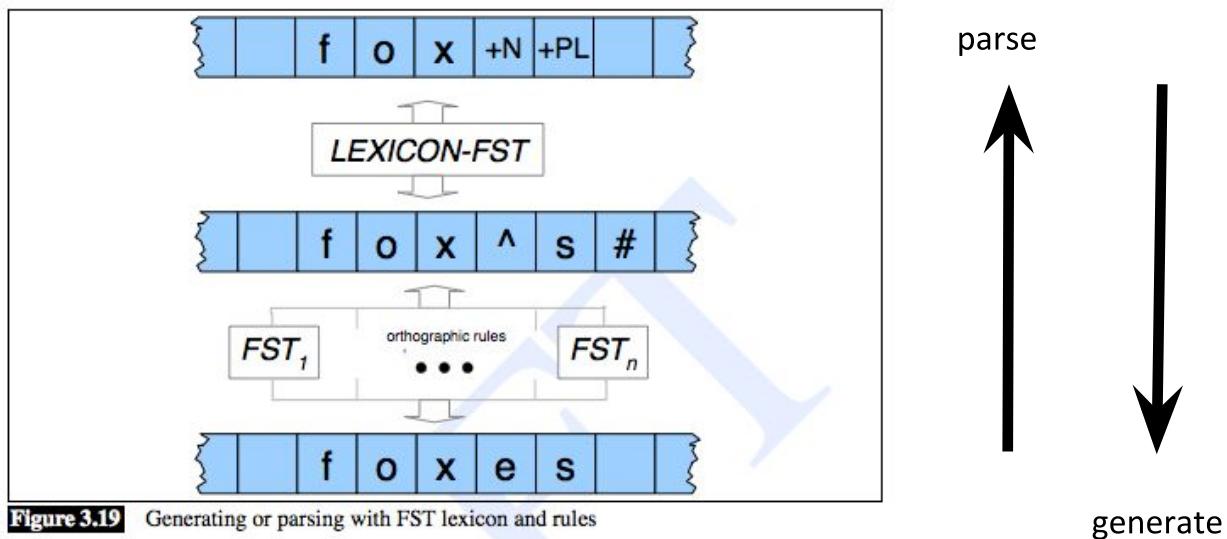
11-711 Algorithms for NLP

October 2020 – Part II

# Review: Inflectional Morphology and syntactic agreement

- Morphology is the study of the internal structure of words.
  - **Derivational morphology.** How new words are created from existing words.
    - [grace]
    - [[grace]ful]
    - [un[grace]ful]]
  - **Inflectional morphology.** How features relevant to the **syntactic context** of a word are marked on that word.
    - This example illustrates number (singular and plural) and tense (present and past).
    - Green indicates irregular. Blue indicates zero marking of inflection. Red indicates regular inflection.
    - **This student walks.**
    - **These students walk.**
    - **These students walked.**
  - **Compounding.** Creating new words by combining existing words
    - With or without spaces: surfboard, golf ball, blackboard

# Review: Features, morphology, FSTs:



# Linguistic features

- (Linguistic “features” vs. ML “features”.)
- Human languages usually include *agreement* constraints; in English, e.g., subject/verb
  - I often swim
  - **He** often swims
  - They often swim
- *Could* have a separate category for each minor type: N1s, N1p, ..., N3s, N3p, ...
  - *Each* with its own set of grammar rules!

# A day without features...

- $\text{NP1s} \rightarrow \text{Det-s N1s}$
- $\text{NP1p} \rightarrow \text{Det-p N1p}$   
...
- $\text{NP3s} \rightarrow \text{Det-s N3s}$
- $\text{NP3p} \rightarrow \text{Det-p N3p}$   
...
- $\text{S1s} \rightarrow \text{NP1s VP1s}$
- $\text{S1p} \rightarrow \text{NP1p VP1p}$
- $\text{S3s} \rightarrow \text{NP3s VP3s}$
- $\text{S3p} \rightarrow \text{NP3p VP3p}$

# Linguistic features

- *Could* have a separate category for each minor type: N1s, N1p, ..., N3s, N3p, ...
  - *Each* with its own set of grammar rules!
- Much better: represent these regularities using independent ***features***: number, gender, person, ...
- Features are typically introduced by lexicon; checked and propagated by constraint equations attached to grammar rules

# Feature Structures (FSs)

Having multiple orthogonal features with values leads naturally to ***Feature Structures***:

```
[Det  
  [root: a]  
  [number: sg ]]
```

A feature structure's values can in turn be FSs:

```
[NP  
  [agreement: [[number: sg]  
    [person: 3rd]]]]
```

Feature Path: <NP agreement person>

# Adding constraints to CFG rules

- $S \rightarrow NP\ VP$   
 $<NP\ number> = <VP\ number>$
- $NP \rightarrow Det\ Nominal$   
 $<NP\ head> = <Nominal\ head>$   
 $<Det\ head\ agree> = <Nominal\ head\ agree>$

# F<sub>S</sub>s from lexicon, constrs. from rules

Lexicon entry:

[Det  
[root: *a*]  
[number: sg ]]

Rule with constraints:

NP → Det Nominal  
 $\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$   
 $\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

- Combine to get result:

[NP [Det  
[root: *a*]  
[number: sg ]]  
[Nominal [number: sg] ...]  
[number: sg]]

# Similar issue with VP types

Another place where grammar rules could explode:

Jack laughed

VP → Verb *for many specific verbs*

Jack found a key

VP → Verb NP *for many specific verbs*

Jack gave Sue the paper

VP → Verb NP NP *for many specific verbs*

# Verb Subcategorization

Verbs have sets of allowed args. Could have many sets of VP rules. Instead, have a SUBCAT feature, marking sets of allowed arguments:

- +none -- Jack laughed
- +np -- Jack found a key
- +np+np -- Jack gave Sue the paper
- +vp:inf -- Jack wants to fly
- +np+vp:inf -- Jack told the man to go
- +vp:ing -- Jack keeps hoping for the best
- +np+vp:ing -- Jack caught Sam looking at his desk
- +np+vp:base -- Jack watched Sam look at his desk
- +np+pp:to -- Jack gave the key to the man

- +pp:loc -- Jack is at the store
- +np+pp:loc -- Jack put the box in the corner
- +pp:mot -- Jack went to the store
- +np+pp:mot -- Jack took the hat to the party
- +adjp -- Jack is happy
- +np+adjp -- Jack kept the dinner hot
- +sthat -- Jack believed that the world was flat
- +sfor -- Jack hoped for the man to win a prize

**50-100** possible *frames* for English; a single verb can have several.

(Notation from James Allen “Natural Lanauaage Understanding”)

# Verb frames are *not* totally semantic

- It does seem to be partly lexical:

John wants to fly

John likes to fly

John likes flying

\*John wants flying

- Can vary with dialect:

??The car needs washed (*only in Pittsburghese?*)

# Frames for “ask”

(in J+M notation)

Subcat	Example
<i>Quo</i>	asked [ <i>Quo</i> “What was it like?”]
<i>NP</i>	asking [ <i>NP</i> a question]
<i>Swh</i>	asked [ <i>Swh</i> what trades you’re interested in]
<i>Sto</i>	ask [ <i>Sto</i> him to tell you]
<i>PP</i>	that means asking [ <i>PP</i> at home]
<i>Vto</i>	asked [ <i>Vto</i> to see a girl called Evelyn]
<i>NP Sif</i>	asked [ <i>NP</i> him] [ <i>Sif</i> whether he could make]
<i>NP NP</i>	asked [ <i>NP</i> myself] [ <i>NP</i> a question]
<i>NP Swh</i>	asked [ <i>NP</i> him] [ <i>Swh</i> why he took time off]

# Adding transitivity constraint

- $S \rightarrow NP\ VP$   
 $<NP\ number> = <VP\ number>$
- $NP \rightarrow Det\ Nominal$   
 $<NP\ head> = <Nominal\ head>$   
 $<Det\ head\ agree> = <Nominal\ head\ agree>$
- $VP \rightarrow \text{Verb}\ NP$   
 $<VP\ head> = <\text{Verb}\ head>$   
 $<VP\ head\ subcat> = +np \quad (\text{which means transitive})$

# Applying a verb subcat feature

Lexicon entry:

[Verb  
[root: *found*]  
[head: find]  
[subcat: +np ]]

Rule with constraints:

VP → Verb      NP  
<VP head> = <Verb head>  
<VP head subcat> = +np

- Combine to get result:

[VP [Verb  
[root: *found*]  
[head: find]  
[subcat: +np ]]  
[NP ...]  
[head: find [subcat: +np]]]]

# Relation to LFG constraint notation

- $\text{VP} \rightarrow \text{Verb} \quad \text{NP}$   
 $\langle \text{VP head} \rangle = \langle \text{Verb head} \rangle$   
 $\langle \text{VP head subcat} \rangle = +\text{np}$

*from JM book is the same as the LFG expression*

- $\text{VP} \rightarrow \text{Verb} \quad \text{NP}$   
 $(\uparrow \text{head}) = (\downarrow \text{head})$   
 $(\uparrow \text{head subcat}) = +\text{np}$

# Unification

- Merging FSs (and failing if not possible) is called ***Unification***
- Simple FS examples:

[number sg]  $\sqcup$  [number sg] = [number sg]

[number sg]  $\sqcup$  [number pl] FAILS

[number sg]  $\sqcup$  [number []] = [number sg]

[number sg]  $\sqcup$  [person 3rd] = [number sg,  
person 3rd]

# New kind of “=” sign

- Already had two meanings in programming:
  - “:=” means “**make** the left be equal to the right”
  - “==” means “the left and right **happen to be** equal”
- Now, a third meaning:
  - □ “=” means “make the left and the right **be the same thing** (from now on)”

# Recap: applying constraints

Lexicon entry:

[Det  
[root: *a*]  
[number: sg ]]

Rule with constraints:

$\text{NP} \rightarrow \text{Det Nominal}$   
 $\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$   
 $\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

- Combine to get result:

[NP [Det  
[root: *a*]  
[number: sg ]]  
[Nominal [number: sg] ...]  
[number: sg]]

# Unifying constraints (1)

Lexicon entries:

[Det  
[root: *a*]  
[number: sg ]]

[Nominal  
[root: *dog*]  
[number: sg ]]

- Rule with constraints:  
 $\text{NP} \rightarrow \text{Det Nominal}$   
 $\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$   
 $\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

- Combine to get result:  
[NP [Det  
[root: *a*]  
[number: sg ]]  
[Nominal  
[root: *dog*]  
[number: sg ] ...]  
[number: sg]]]

# Unifying constraints (2)

Lexicon entries:

[Det  
[root: *a*]  
[number: sg ]]

[Nominal  
[root: *dogs*]  
[number: pl ]]

- Rule with constraints:  
 $\text{NP} \rightarrow \text{Det Nominal}$   
 $\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$   
 $\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

- Combine to get result:  
FAIL

# Unifying constraints (3)

Lexicon entries:

[Det  
[root: *a*]  
[number: sg ]]

[Nominal  
[root: *deer*]  
[number: {sg pl} ]]

- Rule with constraints:  
 $\text{NP} \rightarrow \text{Det Nominal}$   
 $\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$   
 $\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

- Combine to get result:  
[NP [Det  
[root: *a*]  
[number: sg ]]  
[Nominal  
[root: *deer*]  
[number: sg] ...]  
[number: sg]]]

# Turning constraint eqns. into FS

FS1: Lexicon entry:

```
[Det  
  [root: a]  
  [number: sg ]]
```

- Combine FS1 and FS2 to get result:

```
[NP [Det  
  [root: a]  
  [number: sg ]]  
  [Nominal [number: sg ]  
   ...]  
  [number: sg ]]
```

Rule with constraints:

$\text{NP} \rightarrow \text{Det Nominal}$

$\langle \text{NP number} \rangle = \langle \text{Det number} \rangle$

$\langle \text{NP number} \rangle = \langle \text{Nominal number} \rangle$

*becomes* FS2:

```
[NP [Det [number: (1) ]]  
  [Nominal  
   [number: (1) ]  
   ...]  
  [number: (1) ]]
```

# Another example

This (oversimplified) rule:

$$S \rightarrow NP\ VP$$

$$\langle S \text{ subject} \rangle = NP$$

$$\langle S \text{ agreement} \rangle = \langle S \text{ subject agreement} \rangle$$

turns into this DAG:

```
[S [subject (1)
    [agreement (2) ]]
  [agreement (2) ]
  [NP (1) ]
  [VP ]]
```

# “Unification” example without “EQ”

[agreement [number sg],  
subject [agreement [number sg]]]  
↳[subject [agreement [person 3rd,  
number sg]]]  
= [agreement [number sg],  
subject [agreement [person 3rd,  
number sg]]]

- <agreement> is (initially) equal to <subject agreement>, but **not** EQ
- So **not** equal anymore **after** the operation:  
*<agreement person> is still null*

# Unification example with “EQ”

[•agreement (1), subject [agreement (1)]]

□[subject [agreement [person 3rd, number sg]

= [agreement (1),

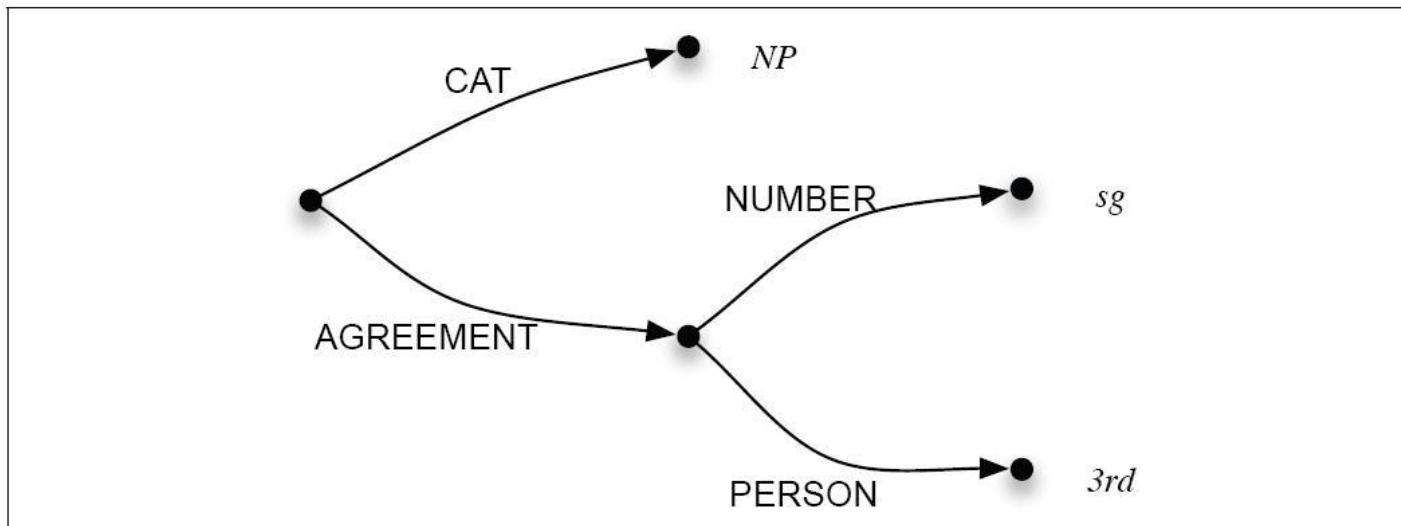
subject [agreement (1) [person 3rd,

number sg]]]

- <agreement> *is* <subject agreement> (EQ), so they are equal
- and **stay** equal, **always**, in the future:  
*<agreement person> is 3rd afterwards!*

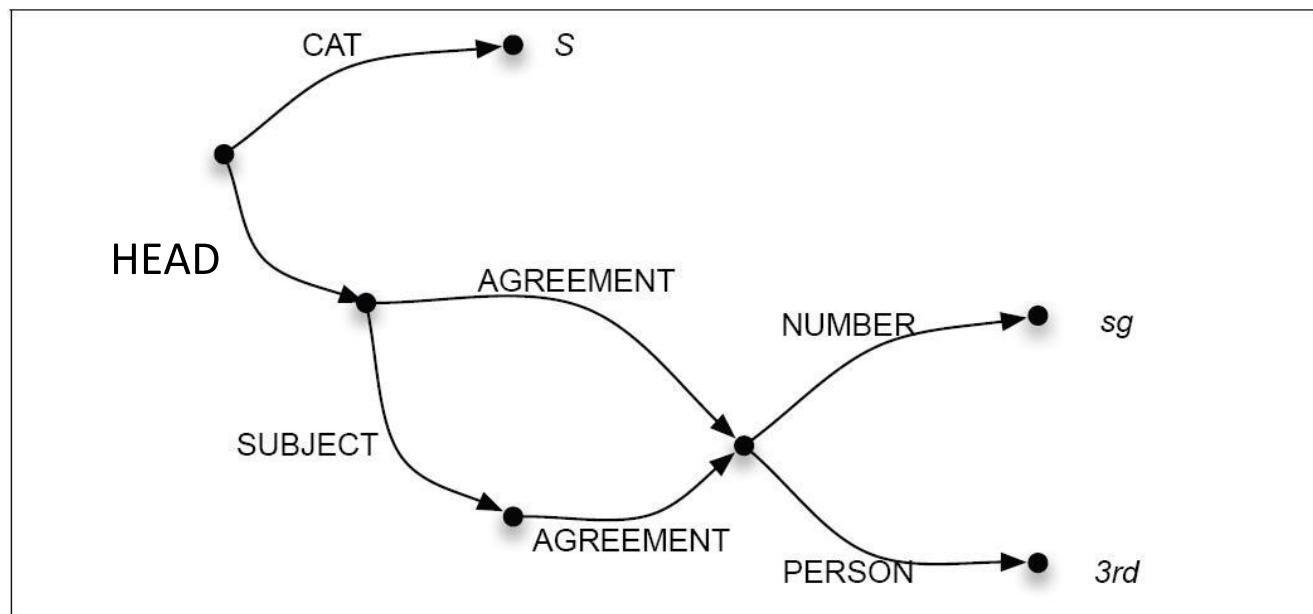
# Ordinary FSs as DAGs

- Taking feature paths seriously
- May be easier to think about than numbered cross-references in text
- [cat NP, agreement [number sg, person 3rd]]



# Re-entrant FS as DAGs

- [cat S, head [agreement (1) [number sg, person 3rd], subject [agreement (1)]]]



# Seems tricky. Why bother?

- Unification allows the systems that use it to handle many complex phenomena in “simple” elegant ways:
  - There seems to be a dog in the yard.
  - There seem to be dogs in the yard
- Unification makes this work smoothly.
  - Make the Subjects of the clauses EQ:  
 $\langle \text{VP subj} \rangle = \langle \text{VP COMP subj} \rangle$   
 $[\text{VP } [\text{subj: (1)}] \ [ \text{COMP } [\text{subj: (1)}] ]]$
  - (Ask Lori Levin for LFG details.)

# *Real* Unification-Based Parsing

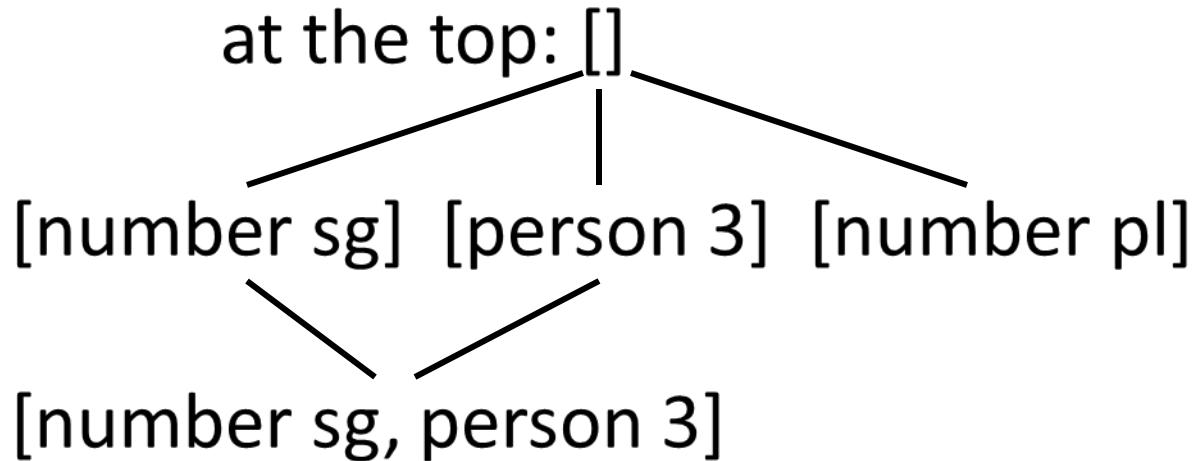
- $X_0 \rightarrow X_1 X_2$   
 $\langle X_0 \text{ cat} \rangle = \mathbf{S}$ ,  $\langle X_1 \text{ cat} \rangle = \mathbf{NP}$ ,  $\langle X_2 \text{ cat} \rangle = \mathbf{VP}$   
 $\langle X_1 \text{ head agree} \rangle = \langle X_2 \text{ head agree} \rangle$   
 $\langle X_0 \text{ head} \rangle = \langle X_2 \text{ head} \rangle$
- $X_0 \rightarrow X_1 \text{ and } X_2$   
 $\langle X_1 \text{ cat} \rangle = \langle X_2 \text{ cat} \rangle$ ,  $\langle X_0 \text{ cat} \rangle = \langle X_1 \text{ cat} \rangle$
- $X_0 \rightarrow X_1 X_2$   
 $\langle X_1 \text{ orth} \rangle = \text{how}$ ,  $\langle X_2 \text{ sem} \rangle = \langle \text{SCALAR} \rangle$

# Complexity

- J&M II: “search the chart for states whose DAGs *unify* with the DAG of the completed state”. Plus a lot of copying.
- Unification parsing is “quite expensive”.
  - NP-Complete in some versions.
  - Early AWB paper on Turing Equivalence(!)
- So maybe *too* powerful?
  - (like GoTo or Call-by-Name?)
  - Add restrictions to make it tractable:
    - Tomita’s Pseudo-unification (Tomabechi too)
    - Gerald Penn work on tractable HPSG: ALE

# Formalities: subsumption

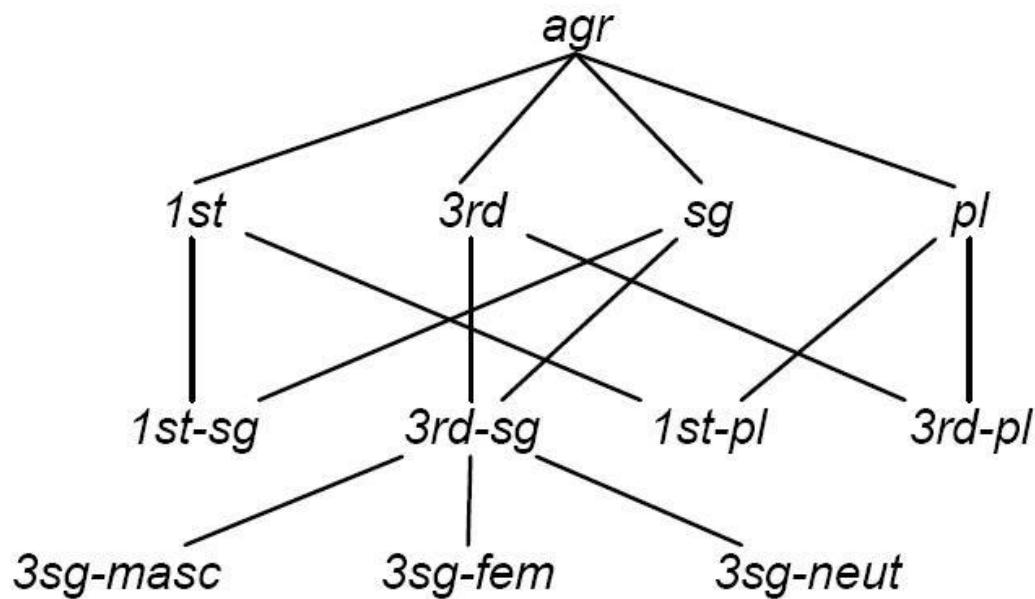
- Less specific FS1 ***subsumes*** more specific FS2  
 $\text{FS1} \sqsubseteq \text{FS2}$  (Inverse is FS2 ***extends*** FS1)
- Subsumption relation forms a ***semilattice***,



- Unification defined wrt semilattice:  
 $F \sqcup G = H$  s.t.  $F \sqsubseteq H$  and  $G \sqsubseteq H$   
H is the Most General Unifier (MGU)

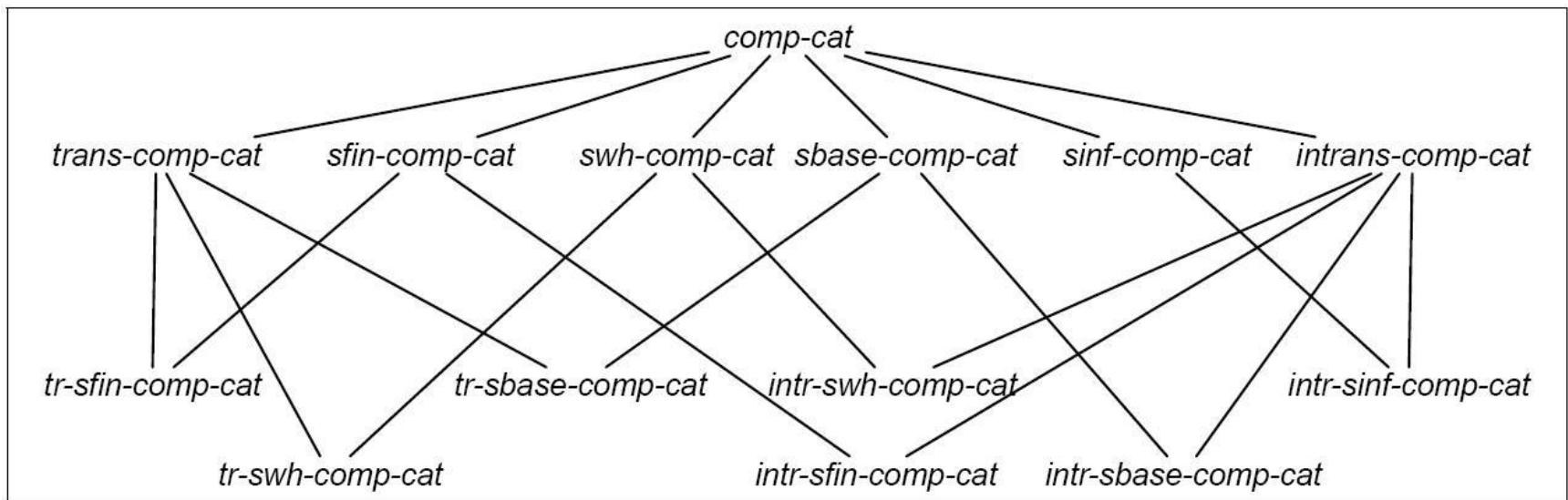
# Hierarchical Types

Hierarchical types allow *values* to unify too (or not):



# Hierarchical subcat frames

Many verbs share *subcat* frames, some with more arguments specified than others:



# Questions?

# Subcategorization

## Noun Phrase Types

<b>There</b>	nonreferential there
<b>It</b>	nonreferential it
<b>NP</b>	noun phrase

**There** *is still much to learn*  
**It** *was evident that my ideas*  
*As he was relating his story*

## Preposition Phrase Types

<b>PP</b>	preposition phrase
<b>PPing</b>	gerundive PP
<b>PPpart</b>	particle

*couch their message in terms*  
*censured him for not having intervened*  
*turn it off*

## Verb Phrase Types

<b>VPbrst</b>	bare stem VP
<b>VPto</b>	to-marked infin. VP
<b>VPwh</b>	wh-VP
<b>VPing</b>	gerundive VP

*she could discuss it*  
*Why do you want to know?*  
*it is worth considering how to write*  
*I would consider using it*

## Complement Clause types

<b>Sfin</b>	finite clause
<b>Swh</b>	wh-clause
<b>Sif</b>	whether/if clause
<b>Sing</b>	gerundive clause
<b>Sto</b>	to-marked clause
<b>Sferto</b>	for-to clause
<b>Sbrst</b>	bare stem clause

*Maintain that the situation was unsatisfactory*  
*it tells us where we are*  
*ask whether Aristophanes is depicting a*  
*see some attention being given*  
*know themselves to be relatively unhealthy*  
*She was waiting for him to make some reply*  
*commanded that his sermons be published*

## Other Types

<b>AjP</b>	adjective phrase
<b>Quo</b>	quotes

*thought it possible*  
*asked "What was it like?"*