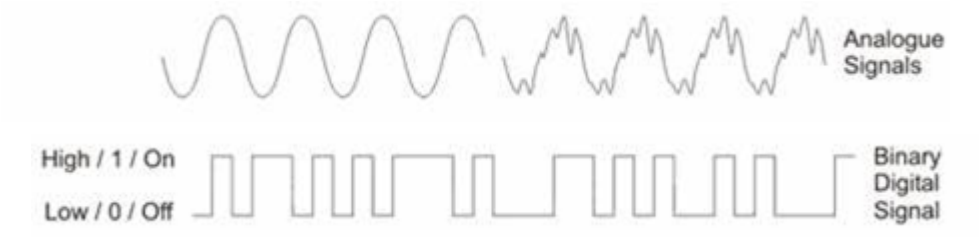
Binary Representations

Bits and Bytes

- Bit - **B**inary dig**IT** (either 0 or 1)
  - 0 (low voltage) and 1 (high voltage)
  - 0 (off) and 1 (on)
  - 0 (false) and 1 (true)



- Byte - 8 bits
- Data sizes are measured in terms of bytes
  - Kilobyte (KB) - 1024 bytes
  - Megabyte (MB) - 1024 KB
  - Gigabyte (GB) -1024 MB
  - Terabyte (TB) - 1024 GB

Types of information

- Computer processors must work with different kinds of information:
  - Numbers: integers and decimal numbers
  - Letters: characters from the alphabet, punctuation, anything you can type on a keyboard
  - Instructions: add, subtract, compare
  - Images, videos
- Each type of information must be represented using bits (using only 1’s and 0’s). We usually just refer to this as the data’s binary representation.

Positional Number Systems

- Decimal Numbers: What does 253 mean?

- We call our number system “decimal” because it uses a base of 10.
  - There are ten symbols used to represent ten values: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9
  - The position of the symbol determines its “weight”: 10^0, 10^1, 10^2, ...
- The binary number system uses a base of 2.
  - There are two symbols used to represent two values: 0, 1
  - The position of the symbol determines its “weight”: 2^0, 2^1, 2^2, …
- The decimal system that we are used to and the binary system are positional number systems because the position determines the weight (place value).

Binary Numbers (Positive Integers)

- Convert the following binary numbers into base-10 (decimal) numbers:

  1001

  1101101

  100010010

Positive Decimal Integers → Binary

- Convert the decimal numbers to binary:

5	23
87	135

Representing Characters

- ASCII - **A**merican **S**tandard **C**ode for **I**nformation **I**nterchange

Hex	Value	Hex	Value	Hex	Value	Hex	Value	Hex	Value	Hex	Value	Hex	Value	Hex	Value
00	NUL	10	DLE	20	SP	30	0	40	@	50	P	60	`	70	p
01	SOH	11	DC1	21	!	31	1	41	A	51	Q	61	a	71	q
02	STX	12	DC2	22	"	32	2	42	B	52	R	62	b	72	r
03	ETX	13	DC3	23	#	33	3	43	C	53	S	63	c	73	s
04	EOT	14	DC4	24	$	34	4	44	D	54	T	64	d	74	t
05	ENQ	15	NAK	25	%	35	5	45	E	55	U	65	e	75	u
06	ACK	16	SYN	26	&	36	6	46	F	56	V	66	f	76	v
07	BEL	17	ETB	27	'	37	7	47	G	57	W	67	g	77	w
08	BS	18	CAN	28	(	38	8	48	H	58	X	68	h	78	x
09	HT	19	EM	29	)	39	9	49	I	59	Y	69	i	79	y
0A	LF	1A	SUB	2A	*	3A	:	4A	J	5A	Z	6A	j	7A	z
0B	VT	1B	ESC	2B	+	3B	;	4B	K	5B	[	6B	k	7B	{
0C	FF	1C	FS	2C	,	3C	<	4C	L	5C	\	6C	l	7C	|
0D	CR	1D	GS	2D	-	3D	=	4D	M	5D	]	6D	m	7D	}
0E	SO	1E	RS	2E	.	3E	>	4E	N	5E	^	6E	n	7E	~
0F	SI	1F	US	2F	/	3F	?	4F	O	5F	_	6F	o	7F	DEL

ASCII control characters

00	NULL	(Null character)
01	SOH	(Start of Header)
02	STX	(Start of Text)
03	ETX	(End of Text)
04	EOT	(End of Trans.)
05	ENQ	(Enquiry)
06	ACK	(Acknowledgement)
07	BEL	(Bell)
08	BS	(Backspace)
09	HT	(Horizontal Tab)
10	LF	(Line feed)
11	VT	(Vertical Tab)
12	FF	(Form feed)
13	CR	(Carriage return)
14	SO	(Shift Out)
15	SI	(Shift In)
16	DLE	(Data link escape)
17	DC1	(Device control 1)
18	DC2	(Device control 2)
19	DC3	(Device control 3)
20	DC4	(Device control 4)
21	NAK	(Negative acknowl.)
22	SYN	(Synchronous idle)
23	ETB	(End of trans. block)
24	CAN	(Cancel)
25	EM	(End of medium)
26	SUB	(Substitute)
27	ESC	(Escape)
28	FS	(File separator)
29	GS	(Group separator)
30	RS	(Record separator)
31	US	(Unit separator)
127	DEL	(Delete)

ASCII printable characters

32	space	64	@	96	`
33	!	65	A	97	a
34	"	66	B	98	b
35	#	67	C	99	c
36	$	68	D	100	d
37	%	69	E	101	e
38	&	70	F	102	f
39	'	71	G	103	g
40	(	72	H	104	h
41	)	73	I	105	i
42	*	74	J	106	j
43	+	75	K	107	k
44	,	76	L	108	l
45	-	77	M	109	m
46	.	78	N	110	n
47	/	79	O	111	o
48	0	80	P	112	p
49	1	81	Q	113	q
50	2	82	R	114	r
51	3	83	S	115	s
52	4	84	T	116	t
53	5	85	U	117	u
54	6	86	V	118	v
55	7	87	W	119	w
56	8	88	X	120	x
57	9	89	Y	121	y
58	:	90	Z	122	z
59	;	91	[	123	{
60	<	92	\	124	|
61	=	93	]	125	}
62	>	94	^	126	~
63	?	95	_		

Extended ASCII characters

128	Ç	160	á	192	└	224	Ó
129	ü	161	í	193	┴	225	ß
130	é	162	ó	194	┬	226	Ô
131	â	163	ú	195	├	227	Ò
132	ä	164	ñ	196	─	228	õ
133	à	165	Ñ	197	┼	229	Õ
134	å	166	ª	198	ã	230	µ
135	ç	167	º	199	Ã	231	þ
136	ê	168	¿	200	╚	232	Þ
137	ë	169	®	201	╔	233	Ú
138	è	170	¬	202	╩	234	Û
139	ï	171	½	203	╦	235	Ù
140	î	172	¼	204	╠	236	ý
141	ì	173	¡	205	═	237	Ý
142	Ä	174	«	206	╬	238	¯
143	Å	175	»	207	¤	239	´
144	É	176	░	208	ð	240	≡
145	æ	177	▒	209	Ð	241	±
146	Æ	178	▓	210	Ê	242	‗
147	ô	179	│	211	Ë	243	¾
148	ö	180	┤	212	È	244	¶
149	ò	181	Á	213	ı	245	§
150	û	182	Â	214	Í	246	÷
151	ù	183	À	215	Î	247	¸
152	ÿ	184	©	216	Ï	248	°
153	Ö	185	╣	217	┘	249	¨
154	Ü	186	║	218	┌	250	·
155	ø	187	╗	219	█	251	¹
156	£	188	╝	220	▄	252	³
157	Ø	189	¢	221	¦	253	²
158	×	190	¥	222	Ì	254	■
159	ƒ	191	┐	223	▀	255	nbsp

Hexadecimal Number System

- Hexadecimal is a positional number system that uses base 16
  - There are 16 symbols: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F
  - The position determines the weight: 16^0, 16^1, 16^2, …
- Find the binary representation of “A”

- Simple conversion from hex → binary and binary → hex

https://byjus.com/maths/hex-to-decimal/

Convert hex 4C to binary

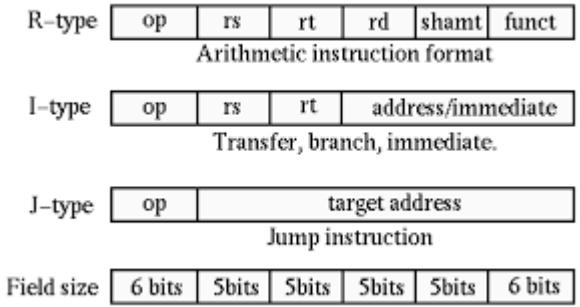
Convert binary 10110110 to hex

Representing Strings of Characters

- Find the binary representations of: “code”, “CODE”, “12”, “#Wow!”

Representing Instructions

- Example: MIPS assembly language



op: the opcode (operation) of the instruction

rs, rt, rd: source and destination registers

Shamt: shift amount

Funct: selects the variant of the operation

address/immediate address offset or immediate (constant) value

Target address: target address of the jump instruction

MIPS assembly language

Category	Instruction	Example	Meaning	Comments
Arithmetic	add	add $1,$2,$3	$1 = $2 + $3	3 operands; exception possible
	subtract	sub $1,$2,$3	$1 = $2 – $3	3 operands; exception possible
	add immediate	addi $1,$2,100	$1 = $2 + 100	+ constant; exception possible
	add unsigned	addu $1,$2,$3	$1 = $2 + $3	3 operands; no exceptions
	subtract unsigned	subu $1,$2,$3	$1 = $2 – $3	3 operands; no exceptions
	add imm. unsign.	addiu $1,$2,100	$1 = $2 + 100	+ constant; no exceptions
	Move fr. copr. reg.	mfc0 $1,$epc	$1 = $epc	Used to get exception PC
	multiply	mult $2,$3	Hi, Lo = $2 ¥ $3	64-bit signed product in Hi, Lo
	multiply unsigned	multu $2,$3	Hi, Lo = $2 ¥ $3	64-bit unsigned product in Hi, Lo
	divide	div $2,$3	Lo = $2 ÷ $3, Hi = $2 mod $3	Lo = quotient, Hi = remainder
	divide unsigned	divu $2,$3	Lo = $2 ÷ $3, Hi = $2 mod $3	Unsigned quotient and remainder
	Move from Hi	mfhi $1	$1 = Hi	Used to get copy of Hi
	Move from Lo	mflo $1	$1 = Lo	Use to get copy of Lo
Logical	and	and $1,$2,$3	$1 = $2 & $3	3 register operands; logical AND
	or	or $1,$2,$3	$1 = $2 | $3	3 register operands; logical OR
	and immediate	andi $1,$2,100	$1 = $2 & 100	Logical AND register, constant
	or immediate	ori $1,$2,100	$1 = $2 | 100	Logical OR register, constant
	shift left logical	sll $1,$2,10	$1 = $2 << 10	Shift left by constant
	shift right logical	srl $1,$2,10	$1 = $2 >> 10	Shift right by constant
Data transfer	load word	lw $1,100($2)	$1 = Memory[$2+100]	Data from memory to register
	store word	sw $1,100($2)	Memory[$2+100] = $1	Data from register to memory
	load upper imm.	lui $1,100	$1 = 100 x 2^{16}	Loads constant in upper 16 bits
Conditional branch	branch on equal	beq $1,$2,100	if ($1 == $2) go to PC+4+100	Equal test; PC relative branch
	branch on not eq.	bne $1,$2,100	if ($1!= $2) go to PC+4+100	Not equal test; PC relative
	set on less than	slt $1,$2,$3	if ($2 < $3) $1=1; else $1=0	Compare less than; 2's complement
	set less than imm.	slti $1,$2,100	if ($2 < 100) $1=1; else $1=0	Compare < constant; 2's comp.
	set less than uns.	sltu $1,$2,$3	if ($2 < $3) $1=1; else $1=0	Compare less than; natural number
	set l.t. imm. uns.	sltiu $1,$2,100	if ($2 < 100) $1=1; else $1=0	Compare < constant; natural
Unconditional jump	jump	j 10000	go to 10000	Jump to target address
	jump register	jr $31	go to $31	For switch, procedure return
	jump and link	jal 10000	$31 = PC + 4; go to 10000	For procedure call

MIPS opcodes

OPCODE map

Table of opcodes for all instructions:

	000	001	010	011	100	101	110	111
000	R-type		j	jal	beq	bne	blez	bgtz
001	addi	addiu	slti	sltiu	andi	ori	xori	
010								
011	llo	lhi	trap					
100	lb	lh		lw	lbu	lhu		
101	sb	sh		sw				
110								
111								

FUNC map of R-type instructions

Table of function codes for register-format instructions:

	000	001	010	011	100	101	110	111
000	sll		srl	sra	sllv		srlv	srav
001	jr	jalr						
010	mfhi	mthi	mflo	mtlo				
011	mult	multu	div	divu				
100	add	addu	sub	subu	and	or	xor	nor
101			slt	sltu				
110								
111								

Find binary representation for:

add $1, $2, $3

addi $4, $5, 10

j 0xA40C