COMP1917: Computing 1

16. Binary Search Trees

Reading: Moffat, Section 10.3, 10.5

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Binary Tree Structure

We define a self-referential structure similar to a Linked List, but with two pointers, to the "left" and "right" branch:

```
typedef struct tnode Tnode;
struct tnode {
    int data;
    Tnode *left;
    Tnode *right;
};
```

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Binary Search Trees - Motivation

- a Linked List is a one-dimensional recursive structure each node has one pointer to the next node
 - ▶ Problem: finding, deleting or inserting items takes a long time because of the need to linearly search for the item of interest
- a Binary Tree is constructed from nodes, where each node contains:
 - ▶ a "left" pointer (which could be NULL)
 - ▶ a "right" pointer (which could be NULL)
 - ▶ a "data" value
- this leads to a multi-branching recursive structure which can speed up finding, deleting and inserting of items considerably

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Binary Trees

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- a "root" pointer points to the topmost node in the tree
- the left and right pointers recursively point to smaller "subtrees" on either side
- a NULL pointer represents a binary tree with no elements an empty tree (or subtree)

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Binary Search Tree

- a Binary Search Tree is a binary tree in which the items are ordered from left to right across the tree.
- To ensure the items remain ordered, new items must be inserted according to these rules:
 - if the new item has a data value less than the data value at this node, it is recursively inserted into the left subtree
 - if the new item has a data value greater than the data value at this node, it is recursively inserted into the right subtree

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Binary Search Tree Operations

```
Tnode * makeTnode( int data ); // create new node
Tnode * findTnode( int data, Tnode *root );
Tnode * insertTnode( Tnode *new_node, Tnode *root );
void printTree( Tnode *root ); // print all items
void freeTree ( Tnode *root ); // free entire tree
int treeSize ( Tnode *root ); // number of items
int treeHeight( Tnode *root ); // max depth of an item
```

Building a Binary Search Tree

The shape of the tree depends on the order in which the nodes are inserted:

8,12,5,15,2,10

```
10
                    5
                                      8
                  2 10
     15
                                    5 12
2 8 12
                    8 15
                                      10 15
                      12
```

5,2,10,8,15,12

Question: what if the order is 2, 5, 8, 10, 12, 15?

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Making a New Node

10,5,15,2,8,12

```
Create a new Tnode with the specified data value.
Tnode * makeTnode( int data )
   Tnode *new_node =(Tnode *)malloc( sizeof( Tnode ));
   if( new_node == NULL ) {
     fprintf(stderr, "Error: memory allocation failed.\n");
      exit( 1 );
   new_node->data = data;
   new_node->left = NULL;
  new_node->right = NULL;
   return( new_node );
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```

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Finding a Node in the Tree

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Search Trees

Insert New Node into Binary Search Tree

```
Tnode * insertTnode( Tnode *new_node, Tnode *root )
   Tnode *child = root, *parent = NULL;
   while( child != NULL ) { // find parent for new node
       parent = child;
       if( new_node->data < parent->data )
           child = parent->left;
       else
           child = parent->right;
   if( parent == NULL )
                                  // tree was empty
       root = new_node;
   else if( new_node->data < parent->data )
       parent->left = new_node; // insert to the left
   else
       parent->right = new_node; // insert to the right
   return( root );
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```

Recursive version of findTnode()

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Recursive version of insertTnode()

```
Tnode * insertTnode( Tnode *new_node, Tnode *root )
{
   if( root == NULL ) { // we have reached the insertion point
      root = new_node;
   }
   else if( new_node->data < root->data ) {
        // insert new node into (and update) left subtree
      root->left = insertTnode(new_node, root->left);
   }
   else { // insert new node into (and update) right subtree
      root->right = insertTnode(new_node, root->right);
   }
   return( root );
}
```

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Printing a Binary Search Tree

```
/*
*/
Print all items of the tree in order

void printTree( Tnode *root )
{
   if( root != NULL ) {
      printTree( root->left ); // recursively print smaller items
      printf("%c",root->data ); // print current item
      printTree( root->right ); // recursively print larger items
   }
}
```

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Computing the Size of a Tree

Freeing all items from a Tree

```
/*
     */
     Recursively free all the items from a Binary Tree
void freeTree( Tnode *root )
{
     if( root != NULL ) {
        freeTree( root->left );
        freeTree( root->right );
        free( root );
     }
}
```

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Computing the Height of a Tree

```
int treeHeight( Tnode *root )

{
   int leftHeight, rightHeight;
   if( root == NULL ) {
      return( 0 );
   }

   else {
      leftHeight = treeHeight( root->left );
      rightHeight = treeHeight( root->right );
      if( leftHeight > rightHeight )
           return( 1 + leftHeight );
      else
           return( 1 + rightHeight );
   }
}

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```

Questions

- what is the maximum number of items that could be stored in a BST with height H?
- if the number of items in a BST is N, what is the minimum height such a tree could have?
- how would you delete an item from a BST (so that the BST structure is preserved)?

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