Quiz (Week 3)

Properties for Functions

Question 1

The ROT13 Cipher is a simple substitution cipher which rotates the alphabet by thirteen places, that is, A becomes N and Z becomes M. Here is a simple (rather inefficient) Haskell implementation:

Select all the properties that this function satisfies (assuming ASCII strings).

Question 2

Here is a function that fairly merges ordered lists, e.g. merge [2,4,6,7] [1,2,3,4] == [1,2,2,3,4,4,6,7].

```
merge xs [] = xs
merge [] ys = ys
```

Select all the properties that this function satisfies.

Question 3

The following code converts Haskell Int values to and from strings containing their binary representation (as a sequences of '1' and '0' characters).

Select all properties that these functions satisfy.

```
    i >= 0 ==> fromBinary (toBinary i) == i
    all (`elem` "01") s ==> toBinary (fromBinary s) == s
    all (`elem` "01") s ==> read s >= fromBinary s
    i > 0 ==> length (toBinary i) >= length (show i)
    all (`elem` "01") s ==> fromBinary s == fromBinary ('0':s)
```

Question 4

The following function removes adjacent duplicates from a list.

Assume the presence of the following sorted predicate:

```
sorted :: (Ord a) => [a] -> Bool
sorted (x:y:xs) = x <= y && sorted (y:xs)
sorted xs = True</pre>
```

Select all properties that dedup satisfies.

```
    sorted xs ==> sorted (dedup xs)
    sorted xs ==> dedup xs == nub xs
    sorted xs ==> dedup (dedup xs) == dedup xs
    sorted xs && sorted ys ==> dedup xs ++ dedup ys == dedup (xs ++ ys)
    sorted xs ==> length (dedup xs) < length xs</li>
    (x `elem` xs) == (x `elem` dedup xs)
```

Functions for Properties

Question 5

Here are a set of properties that the function foo must satisfy:

```
foo :: [a] -> (a -> b) -> [b]
foo = undefined -- see below

prop_1 :: [Int] -> Bool
prop_1 xs = foo xs id == xs

prop_2 :: [Int] -> (Int -> Int) -> (Int -> Int) -> Bool
prop_2 xs f g = foo (foo xs f) g == foo xs (g . f)
```

Choose an implementation for foo that satisfies the above properties, and typechecks:

2. \bigcirc

```
foo [] f = []
foo (x:xs) f = x : foo xs f
```

foo [] f = []
foo (x:xs) f = f x : foo xs f

```
foo [] f = []
foo (x:xs) f = foo xs f
```

Question 6

foo xs f = xs

```
bar :: [Int] -> [Int]
bar = undefined

prop_1 :: [Int] -> Bool
prop_1 xs = bar (bar xs) == xs

prop_2 :: [Int] -> Bool
prop_2 xs = length xs == length (bar xs)

prop_3 :: [Int] -> (Int -> Int) -> Bool
prop_3 xs f = bar (map f xs) == map f (bar xs)
```

Choose all implementations for bar that satisfy the above properties, and type-check:

```
bar xs = go xs []
where go [] acc = acc
go (x:xs) acc = go xs (x:acc)
```

```
bar [] = []
bar (x:xs) = xs ++ [x]
```

4. \Box bar = id

```
5. 
bar xs = nub xs
```

bar xs = replicate (length xs) (maximum xs)

Question 7

```
baz :: [Integer] -> Integer
baz = undefined

prop_1 :: [Integer] -> [Integer] -> Bool
prop_1 xs ys = baz xs + baz ys == baz (xs ++ ys)

prop_2 :: [Integer] -> Bool
prop_2 xs = baz xs == baz (reverse xs)

prop_3 :: Integer -> [Integer] -> Bool
prop_3 x xs = baz (x:xs) - x == baz xs
```

Choose a law-abiding definition for baz, that type checks:

3. \bigcirc

```
baz [] = 1
baz (x:xs) = x + baz xs
```

4.

```
baz xs = 0
```

Question 8

Here is a definition of a function fun, and properties for another function nuf:

```
fun :: [Integer] -> [Integer]
fun [] = []
fun [x] = []
fun (x:y:xs) = (y-x):fun (y:xs)

nuf :: [Integer] -> Integer -> [Integer]
nuf = undefined

prop_1 :: [Integer] -> Integer -> Bool
prop_1 xs x = nuf (fun (x:xs)) x == (x:xs)

prop_2 :: [Integer] -> Integer -> Bool
prop_2 xs x = fun (nuf xs x) == xs
```

Choose a definition for nuf that type checks and satisfies the given properties:

```
1. ○
    nuf [] i = []
    nuf (x:xs) i = (i + x) : nuf xs (i + x)
```

```
2. 
    nuf [] i = [i]
    nuf (x:xs) i = (i + x) : nuf xs (i + x)
```

```
3. \bigcirc

nuf xs i = scanl (\v x -> v + x) i xs
```

```
nuf [] i = []
nuf (x:xs) i = (i + x) : nuf xs i
```

5. \bigcirc

nuf xs
$$i = i$$
: scanl ($\forall x \rightarrow \forall + x$) $i xs$

Due: Friday, June 28, 11:59:59 pm

Upon clicking submit, you will be prompted for your zID and zPass. Please make sure that your answers are final and that you have answered every question.

If there is a problem, please contact the course administrator.

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