Exercise (Week 4)



DUE: Tue 2 July 14:00:00

Getting Started

CSE

Stack

Download the exercise tarball and extract it to a directory on your local machine. This tarball contains a file, called Ex03.hs, wherein you will do all of your programming.

To test your code, run the following shell commands to open a GHCi session:

```
$ stack repl
Configuring GHCi with the following packages: Ex03
Using main module: 1. Package 'Ex03' component exe:Ex03 ...
GHCi, version 8.2.2: http://www.haskell.org/ghc/ :? for help
[1 of 1] Compiling Ex03 (Ex03.hs, interpreted)
Ok, one module loaded.
*Ex03> quickCheck prop_mysteryPred_1
...
```

Calling quickCheck in the above way will run the given QuickCheck property with 100 random test cases.

Note that you will only need to submit <code>Ex03.hs</code> , so only make changes to that file.

QuickCheck and Search Trees

The file Ex03.hs includes the support code described in the following as well as stubs for the three functions that you must implement. The QuickCheck properties discussed below are also included.

We include a binary tree implementation, plus a predicate, <code>isBST</code>, which returns if a tree is a binary *search* tree (that is, an infix traversal of the tree is sorted). This is a *data invariant* for our BST operations.

We also include insert and deleteAll functions for binary search trees:

```
-- Add an integer to a BinaryTree, preserving BST property.
insert :: Integer -> BinaryTree

-- Remove all instances of an integer in a binary tree,
-- preserving BST property
deleteAll :: Integer -> BinaryTree -> BinaryTree
```

An arbitrary generator that generates binary search trees:

```
searchTrees :: Gen BinaryTree
```

If we wanted to check that our generator always generates wellformed inputs, we can check it by running the additional property:

```
prop_searchTrees = forAll searchTrees isBST
```

We use the arbitrary search tree generator rather than prefix our properties with a guard like isBST tree ==> to prevent QuickCheck generating lots of spurious test cases.

Implementing A Mystery Function (Part 1a, 2 Mark)

Write a predicate function | mysteryPred |, which has the following type signature:

```
mysteryPred :: Integer -> BinaryTree -> Bool
```

It must satisfy the following QuickCheck properties:

You can test your mysteryPred implementation by simply running quickCheck prop_mysteryPred_[1-2] in the playground or GHCi.

Even more mysterious (Part 1b, 3 Marks)

Write a function mysterious, with the following type signature:

```
mysterious :: BinaryTree -> [Integer]
```

It must satisfy the following QuickCheck properties:

You can test your mysterious implementation by simply running quickCheck prop_mysterious_[1-2] in a playground or GHCi.

Depending on your exact definition, this could be an abstraction function for binary search trees. Consider how our binary tree operations like insert and deleteAll

could be specified using data refinement.

Balancing Act (Part 2, 4 Marks)

First, we have the generator:

```
sortedListsWithoutDuplicates :: Gen [Integer]
```

We use a generator to produce | sortedListsWithoutDuplicates | because guarding our properties with | isSorted list ==> | etc. means that QuickCheck will waste a lot of time randomly generating lists and checking if they satisfy the guard. We can check if our generator works with the following properties:

Write a function astonishing, of type [Integer] -> BinaryTree that satisfies these properties:

Where isBalanced is a predicate that returns true if a tree is height-balanced:

Note: This definition of isBalanced is a rather generous definition of balanced trees. Can you find an example of a tree that is not very balanced for which this function would still return True? What would a stricter predicate look like?

Submission instructions

You can submit your exercise by typing:

\$ give cs3141 Ex03 Ex03.hs

on a CSE terminal, or by using the give web interface. Your file *must* be named Ex03.hs (case-sensitive!). A dry-run test will *partially* autotest your solution at submission time. To get full marks, you will need to perform further testing yourself.