

CENG466, Fall 2022, THE 1

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Abstract—We implemented affine transformation using both bilinear and bicubic interpolation as well as histogram extraction, equalization, and adaptive equalization for the first Take Home Exam of Fall 2022 semester.

Index Terms—image processing, affine transformation, histogram equalization

I. INTRODUCTION

II. AFFINE TRANSFORMATION

A. Rotation

B. Bilinear Interpolation

C. Bicubic Interpolation

Bicubic interpolation is defined as

$$p(x, y) = \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} x^i y^j, \quad (1)$$

calculated by finding the values of 16 coefficients in $[a_{ij}]$, whose values are informed by the 16 closest pixel. By only using the 4 closest pixel $(0, 0)$, $(0, 1)$, $(1, 0)$, and $(1, 1)$ and derivatives of them in horizontal, vertical, and diagonal directions, we can calculate the values of $[a_{ij}]$ as

$$A = \begin{bmatrix} a_{00} & a_{01} & a_{02} & a_{03} \\ a_{10} & a_{11} & a_{12} & a_{13} \\ a_{20} & a_{21} & a_{22} & a_{23} \\ a_{30} & a_{31} & a_{32} & a_{33} \end{bmatrix} \quad (2)$$

$$B = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -3 & 3 & -2 & -1 \\ 2 & -2 & 1 & 1 \end{bmatrix} \quad (3)$$

$$F = \begin{bmatrix} f(0, 0) & f(0, 1) & f_y(0, 0) & f_y(0, 1) \\ f(1, 0) & f(1, 1) & f_y(1, 0) & f_y(1, 1) \\ f_x(0, 0) & f_x(0, 1) & f_{xy}(0, 0) & f_{xy}(0, 1) \\ f_x(1, 0) & f_x(1, 1) & f_{xy}(1, 0) & f_{xy}(1, 1) \end{bmatrix} \quad (4)$$

$$A = BFB^{-1}. \quad (5)$$

As most of the available libraries in our disposal does not calculate the values of A for each given image, instead assigning them predetermined values (such as `opencv`), we decided to implement it by ourselves. To achieve this, we used a 3 step process.

- **Precomputation** We started by calculated the values of $f_x(x, y)$, $f_y(x, y)$, and $f_{xy}(x, y)$ for every pixel of the original input image where

$$f_x(x, y) = \frac{f(x+1, y) - f(x-1, y)}{2} \quad (6)$$

$$f_y(x, y) = \frac{f(x, y+1) - f(x, y-1)}{2} \quad (7)$$

$$f_{xy}(x, y) = \frac{f_x(x, y) + f_y(x, y)}{2} \quad (8)$$

using 0 padding.

- **Interpolation** We calculated the brightness value of every pixel of the output image using Equations 1 and 5.
- **Normalization** We normalized the brightness values of the output image to $[0, 255]$, then rounded them to nearest integer value.

III. HISTOGRAM EQUALIZATION

A. Histogram Extraction

B. Histogram Equalization

C. Adaptive Histogram Equalization

IV. DEPENDENCIES

We used following libraries for the described reasons.

- **os**: Handling non-existent input or output paths.
- **PIL**: Reading images and converting them arrays.
- **numpy**: Executing array and matrix operations.
- **math**: Performing trigonometric operations.
- **matplotlib**: Creating histograms as graphics and writing arrays as image files.

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