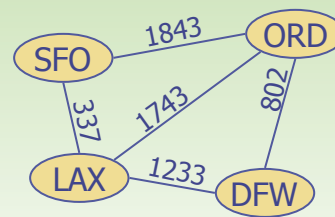


Graphs



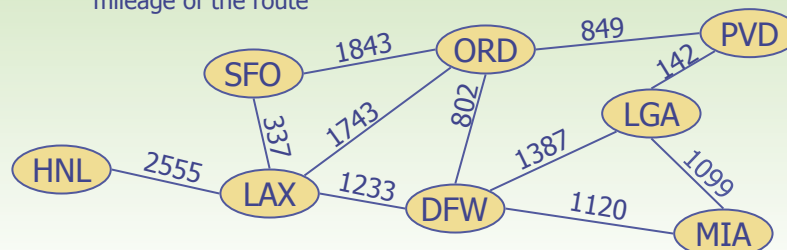
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Graphs

1

Graphs

- A graph is a pair (V, E) , where
 - V is a set of nodes, called **vertices**
 - E is a collection of pairs of vertices, called **edges**
 - Vertices and edges are positions and store elements
- Example:
 - A vertex represents an airport and stores the three-letter airport code
 - An edge represents a flight route between two airports and stores the mileage of the route



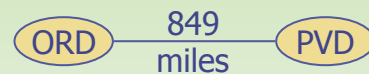
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Graphs

2

Edge Types

- Directed edge
 - ordered pair of vertices (u, v)
 - first vertex u is the origin
 - second vertex v is the destination
 - e.g., a flight
- Undirected edge
 - unordered pair of vertices (u, v)
 - e.g., a flight route
- Directed graph
 - all the edges are directed
 - e.g., route network
- Undirected graph
 - all the edges are undirected
 - e.g., flight network



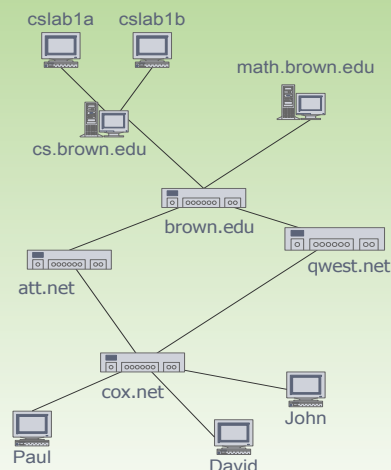
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Graphs

3

Applications

- Electronic circuits
 - Printed circuit board
 - Integrated circuit
- Transportation networks
 - Highway network
 - Flight network
- Computer networks
 - Local area network
 - Internet
 - Web
- Databases
 - Entity-relationship diagram



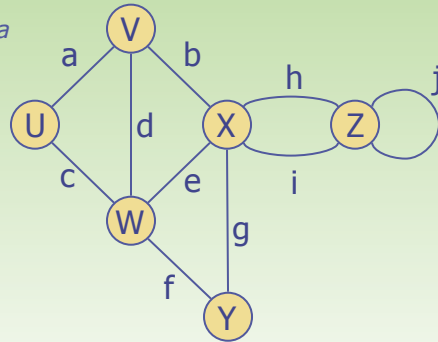
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Graphs

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Terminology

- End vertices (or endpoints) of an edge
 - U and V are the endpoints of a
- Edges incident on a vertex
 - a , d , and b are incident on V
- Adjacent vertices
 - U and V are adjacent
- Degree of a vertex
 - X has degree 5
- Parallel edges
 - h and i are parallel edges
- Self-loop
 - j is a self-loop



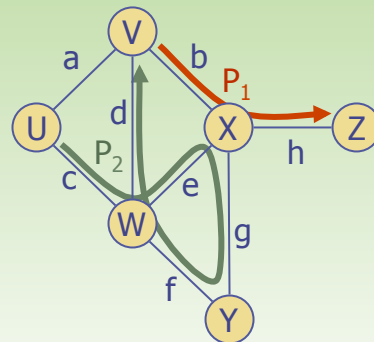
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Graphs

5

Terminology (cont.)

- Path
 - sequence of alternating vertices and edges
 - begins with a vertex
 - ends with a vertex
 - each edge is preceded and followed by its endpoints
- Simple path
 - path such that all its vertices and edges are distinct
- Examples
 - $P_1 = (V, b, X, h, Z)$ is a simple path
 - $P_2 = (U, c, W, e, X, g, Y, f, W, d, V)$ is a path that is not simple



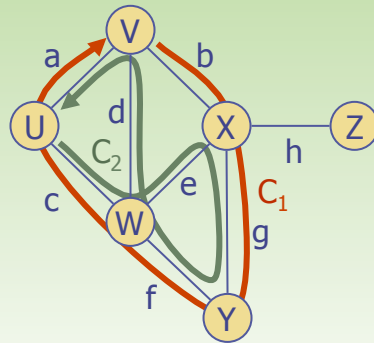
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Graphs

6

Terminology (cont.)

- Cycle
 - circular sequence of alternating vertices and edges
 - each edge is preceded and followed by its endpoints
- Simple cycle
 - cycle such that all its vertices and edges are distinct
- Examples
 - $C_1 = (V, b, X, g, Y, f, W, c, U, a, \hookleftarrow)$ is a simple cycle
 - $C_2 = (U, c, W, e, X, g, Y, f, W, d, V, a, \hookleftarrow)$ is a cycle that is not simple



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Graphs

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Main Methods of the Graph ADT

- Vertices and edges
 - are positions
 - store elements
- Accessor methods
 - **endVertices**(e): an array of the two endvertices of e
 - **opposite**(v, e): the vertex opposite of v on e
 - **areAdjacent**(v, w): true iff v and w are adjacent
 - **replace**(v, x): replace element at vertex v with x
 - **replace**(e, x): replace element at edge e with x
- Update methods
 - **insertVertex**(o): insert a vertex storing element o
 - **insertEdge**(v, w, o): insert an edge (v,w) storing element o
 - **removeVertex**(v): remove vertex v (and its incident edges)
 - **removeEdge**(e): remove edge e
- Iterable collection methods
 - **incidentEdges**(v): edges incident to v
 - **vertices**(): all vertices in the graph
 - **edges**(): all edges in the graph

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Graphs

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