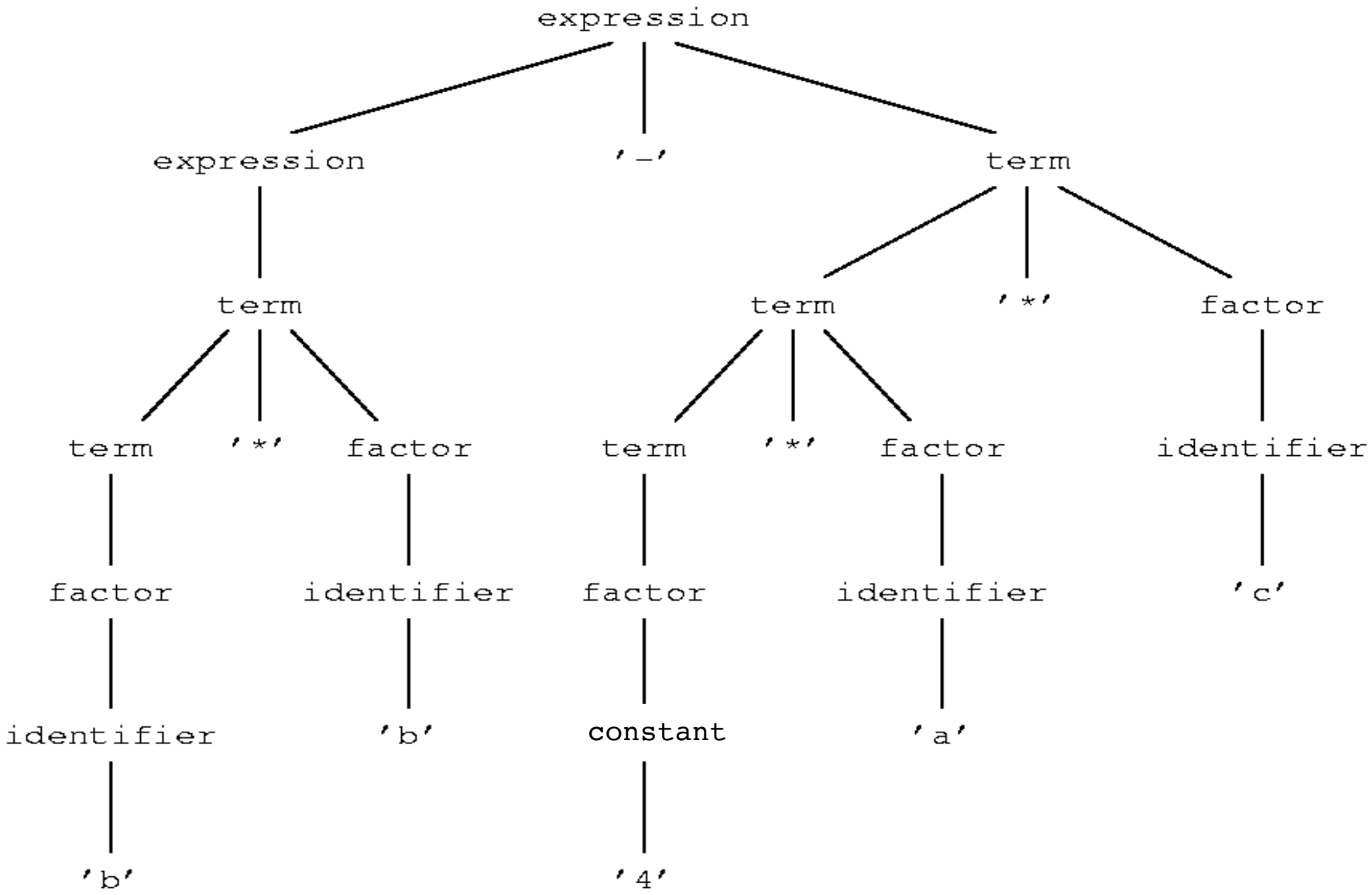
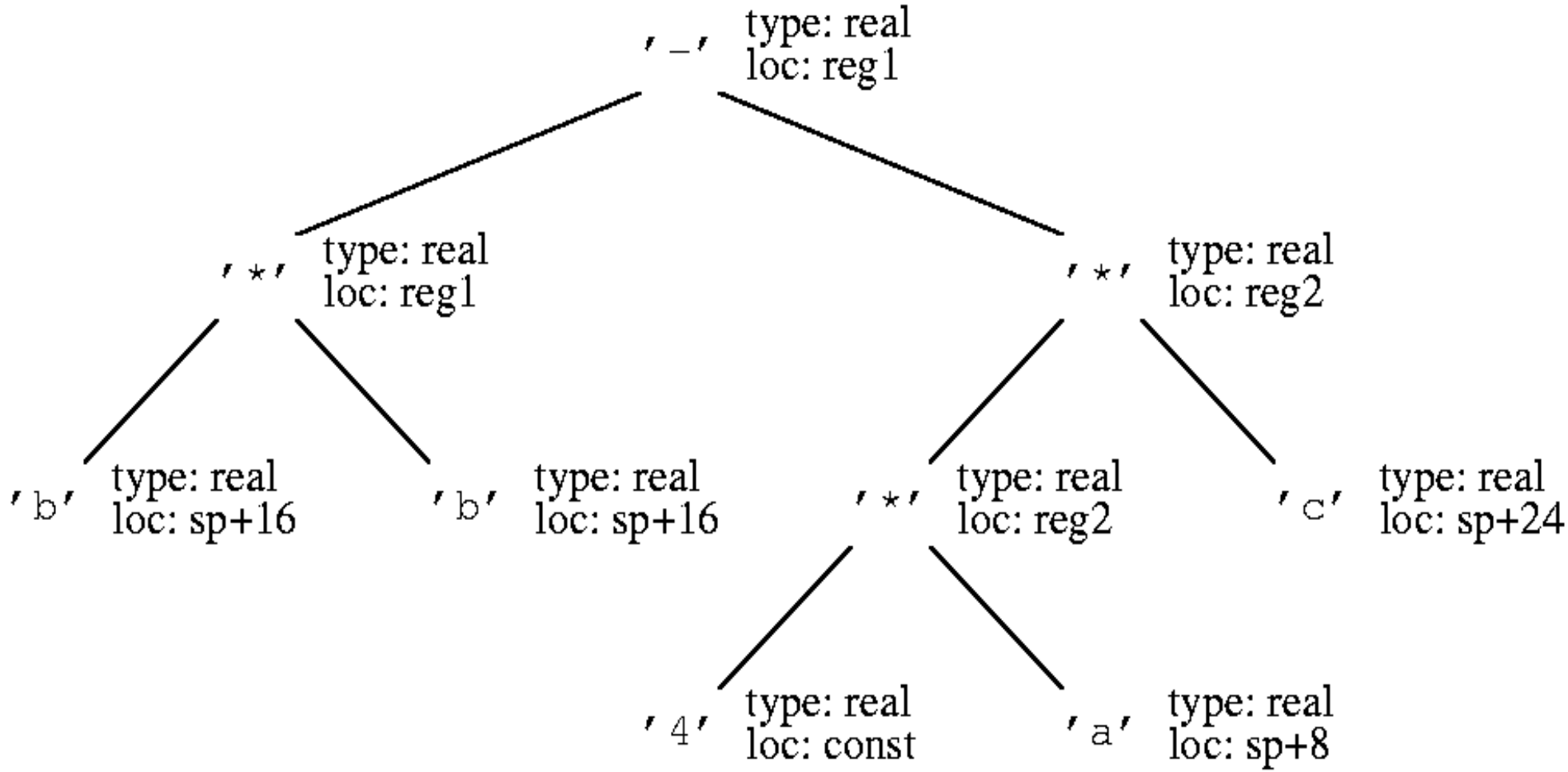
Parse tree for b*b-4*a*c



Annotated abstract syntax tree for b*b-4*a*c



```
<exp>        ::= <exp> + <term>
             | <exp> - <term>
             | <term>
<term>       ::= <term> * <factor>
```



```
             | <term> / <factor>
             | <factor>
<factor>     ::= ( <exp> )
             | <identifer>
```

- There are four operators (+, -, * and /), with two levels of precedence.
- The grammar imposes a ***phrase structure*** on expressions. In `a * b + c` the subexpression `a * b` is a phrase because it corresponds to a subtree of the derivation tree. This phrase structure gives effect to the precedence of the operators.
- The derivation of `a * (b + c)` the parentheses indicate a <factor>, so its derivation tree would be different.

Backus-Naur Form

Here is an example of a grammar:

```
<identifier> ::=  <letter>
                | <identifier> <digit>
                | <identifier> <letter>
<letter>     ::= a|b|c|d| ... x|y|z
<digit>      ::= 0|1|2|3|4|5|6|7|8|9
```

The essential features of the BNF formalism are:

1. Angle brackets. These signify non-terminal symbols.
2. The symbol ::= which is read `is defined as'.
3. The symbol | which means ‘or'.
4. The idea of a production rule.
5. A terminal symbol : anything not enclosed in angle brackets.

Ambiguous Grammar Example

```
<statement>          ::=   <conditional statement>
                         | . . .
                         | . . .

<conditional statement> ::=
     if <condition> then <statement>
   | if <condition> then <statement> else <statement>
```

Ambiguity

(from the exercises)

```
<exp>       ::= <exp> + <exp>
              | <exp> * <exp>
              | <ident>
<ident>     ::= x | y | z
```

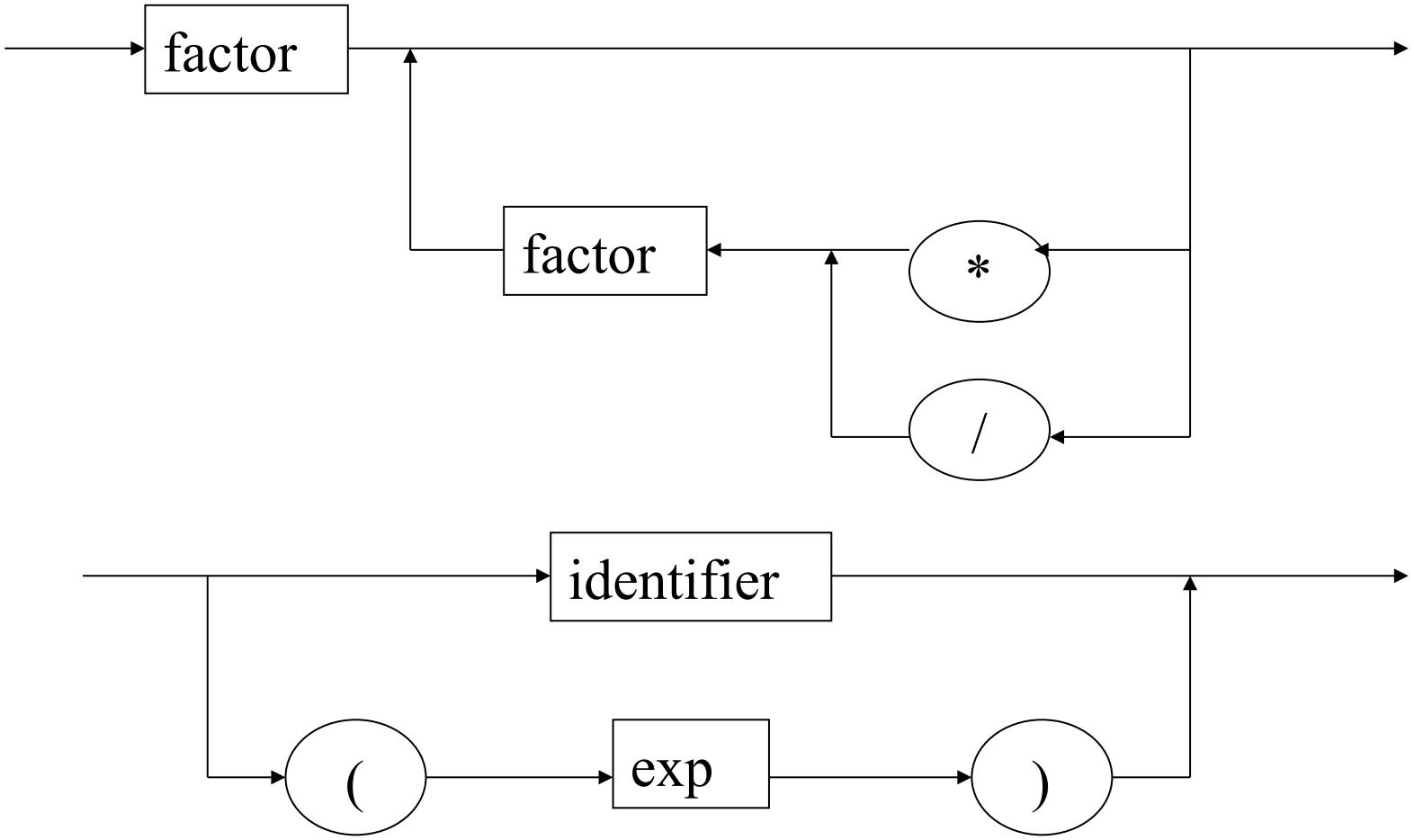
Legality and EBNF conversion

(from the exercises)

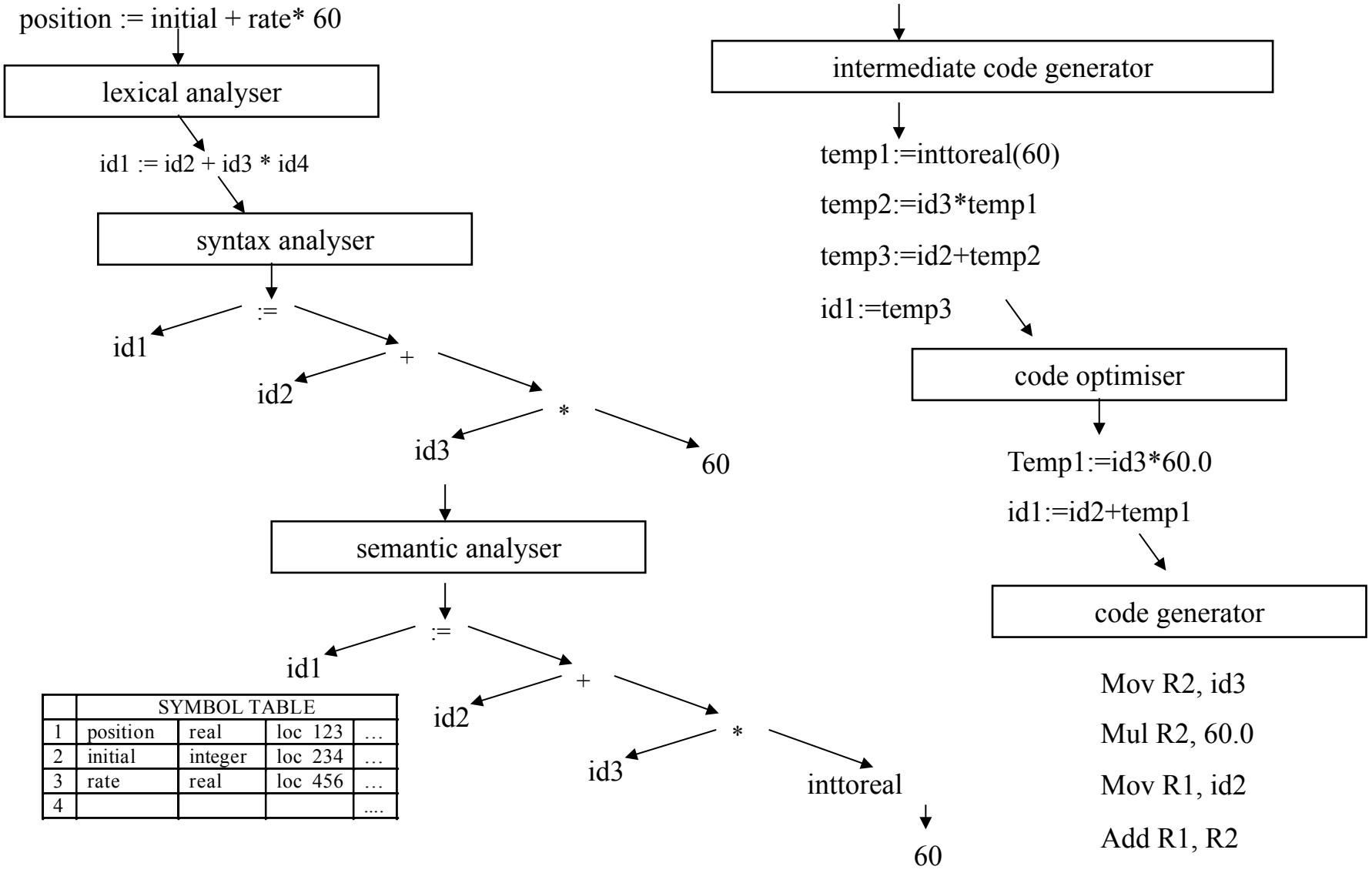
```
<rule1> ::= <rule1> Y   | <rule2>
<rule2> ::= Z <rule3>   | Z
<rule3> ::= X
```

Syntax Diagrams and Extended BNF (EBNF)

```
term -> factor { (‘*’ | ‘/’) factor }
factor -> ‘(‘ exp ‘)’ ‘ | identifier
```



position := initial + rate * 60



Operational Semantics

- Assignment Statements

$$\frac{E \vdash \langle exp \rangle \Rightarrow v}{E \vdash \langle identifer \rangle = \langle exp \rangle \Rightarrow E[\langle identifer \rangle \mapsto v]}$$

$$\frac{E \vdash \langle statement \rangle \Rightarrow E' \quad E' \vdash \langle prog \rangle \Rightarrow E''}{E \vdash \langle statement \rangle ; \langle prog \rangle \Rightarrow E''}$$

Axiomatic Semantics

{P} S {Q}

- assignment statements (axiom)

  {R(e)} x := e {R(x)}

- sequencing program statements (rule of inference)

$$\frac{\{P\}\ S1\ \{R\}\quad \{R\}\ S2\ \{Q\}}{\{P\}\ S1;S2\ \{Q\}}$$