

# MATU9D2: Practical Statistics

## Practical 4: Hand Calculations: Solutions

Spring 2017

### Question 1.

- a.)  $H_0$ : there is NO relationship  
 $H_1$ : there IS a relationship

b.)

#### Observed

	Africa	Asia	South America	Totals
Malaria A	14	31	45	90
Malaria B	5	2	53	60
Malaria C	45	53	2	100
<b>column totals</b>	<b>64</b>	<b>86</b>	<b>100</b>	
N	250			

#### Expected

	Africa	Asia	South America	Totals
Malaria A	23.04	30.96	36	90
Malaria B	15.36	20.64	24	60
Malaria C	25.6	34.4	40	100
<b>column totals</b>	<b>64</b>	<b>86</b>	<b>100</b>	
N	250			

Observed	Expected	(O-E)^2	(O-E)^2/E
14	23.04	81.7216	3.546944444
31	30.96	0.0016	5.16796E-05
45	36	81	2.25
5	15.36	107.3296	6.987604167
2	20.64	347.4496	16.83379845
53	24	841	35.04166667
45	25.6	376.36	14.7015625
53	34.4	345.96	10.05697674
2	40	1444	36.1

Statistic = Sum = 125.5186047

Degree of Freedom = (num Rows - 1)(num column - 1)  
= (3-1)(3-1)  
= 4

$$\chi^2 = 125.5186$$

$\alpha = 0.05$ , one-tailed chi-squared (4)

Rejection Region Critical value of  $\chi^2(4;0.05) = 9.49$ .

p-value:  $P(\chi^2(4) > 125.519) \ll 0.001$

Conclusion:

Observed test statistic (125.519) is in the rejection region so can reject  $H_0$  in favour of  $H_1$  at the 5% significance level, i.e. there is a relationship between region and malaria type (but we don't know what it is!)

## Question 2.

$H_0$ : the distribution is uniform

$H_1$ : the distribution is not uniform

	<b>Observed</b>	<b>Expected</b>	<b>(O-E)<sup>2</sup></b>	<b>(O-E)<sup>2</sup>/E</b>
1	24	20	16	0.8
2	15	20	25	1.25
3	27	20	49	2.45
4	17	20	9	0.45
5	22	20	4	0.2
6	15	20	25	1.25
Total	120	120	Sum =	6.4

Note Expected frequency =  $N/6 = 120/6 = 20$

Degrees of freedom =  $(k-1) = (6-1) = 5$

$P(\chi^2(5) > 6.4) = 0.269218$

The rejection region for  $\chi^2(5; 0.01)$  is approximately 15.09 which is greater than our observed statistic.

Conclusion: The calculated p-value is greater than the significance level so we cannot reject the null hypothesis in favour of the alternative at this significance level.