US Macro Data Forecasting Report

[View on TensorFlow.org] [Run in Google Colab] [View source on GitHub] [Download notebook]

This is a report on analyzing and forecasting the US macro data using **Recurrent Neural N** **Convolutional Neural Network (CNNs)** and **Generative Adversarial Net** report is:

Part I. Statistical analysis

- Basic manipulation
- Correlation analysis
- Time series analysis with `ARIMA`

Part II. Deep learning models

- Basic model: single-step, single-feature forecasting with LSTM
- Generalized model: multi-step, multi-feature forcasting with LSTM
- Advanced model: Generative Adversarial Network (GAN) with RNN and CNN.

Part III. Conclusions and Next steps

- Conclusions
- Next steps

Introduction

1. The Notebook

Follow the notebook, we can recreate all the results, notice that

- Upload the `USMacroData.xls` file to the root folder on google colab.
- To navigate better, use the table of contents bottom on the upper-left sidebar.
- **For clarity, all code cells are hiden, double click on the cell to get the**
- Change the parameters as indicated in the comments to create more custom outputs.
- All source code can also be found in the project file folder

2. The US Macro dataset

This report uses a US Macro Dataset provided by the ADP.

Before analyzing the data with codes, we have the following observations.

- This dataset contains **6** different features (the **Inflation, Wage, Unemployment,** **InterstRate**) about the macro economy of the US.

- Data were collected every $\mathbf{1}$ month, beginning in $\mathbf{1965\text{-}01\text{-}01\ to\ 2015\text{-}12\text{-}01}$.
- In total, we have $\mathbf{612\ rows\ (month)}$ and $\mathbf{6\ columns\ (features)}$.

Part I.1 Basic manipulation

Code and examples

```
basic.py
```

read the file and show the head

	Month	Inflation	Wage	Unemployment	Consumption	Investment	InterestRa
0	1965-01-01	1.557632	3.200000	4.9	6.972061	12.3	3.9
1	1965-02-01	1.557632	3.600000	5.1	7.811330	13.2	3.9
2	1965-03-01	1.242236	4.000000	4.7	7.828032	18.7	4.(
3	1965-04-01	1.552795	3.585657	4.8	8.477938	9.8	4.(
4	1965-05-01	1.552795	3.968254	4.6	7.139364	10.2	4.

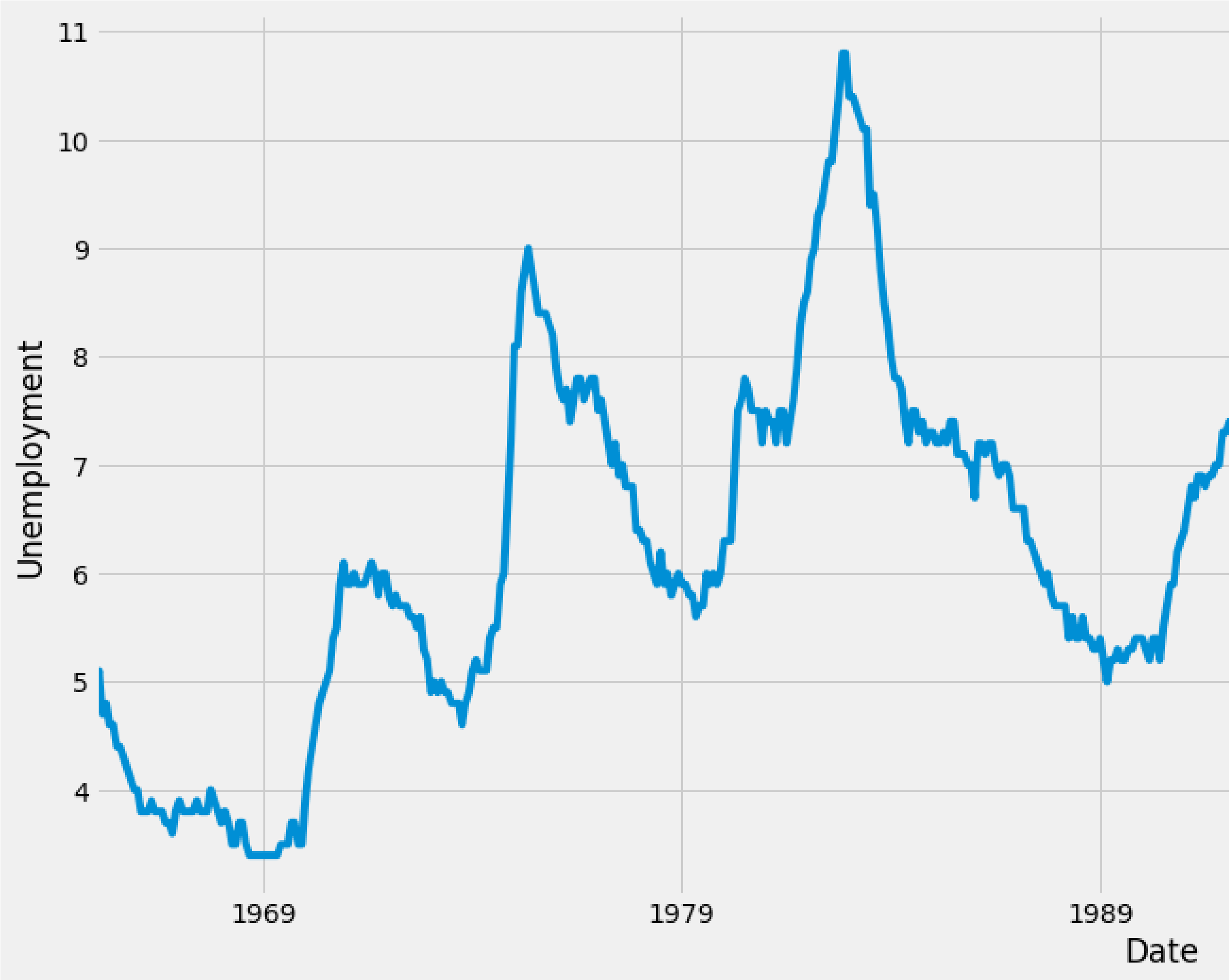
Basic checks: find null values and fill, set index, etc.

```
Null values summary:

Inflation       0
Wage            0
Unemployment    0
Consumption     0
Investment      0
InterestRate    0
dtype: int64
```

Month	Inflation	Wage	Unemployment	Consumption	Investment	InterestRate
1965-01-01	1.557632	3.200000	4.9	6.972061	12.3	3.90
1965-02-01	1.557632	3.600000	5.1	7.811330	13.2	3.98
1965-03-01	1.242236	4.000000	4.7	7.828032	18.7	4.04
1965-04-01	1.552795	3.585657	4.8	8.477938	9.8	4.09
1965-05-01	1.552795	3.968254	4.6	7.139364	10.2	4.10

Example: plot the "Inflation" column



Data Analysis

As a high level overview, some distinguishable patterns appear when we plot the data:

- **In the 80's (1979-1989), all features experienced some drastic chang**
- The time-series has **seasonality pattern**, for example, **Unemployment** has **long** goes through 1 or 2 major up and downs. We will examine the seasonality more carefully in

Part I.2 Correlation analysis

Though it's indicated that there's no obvious correlation among the 6 features, we compute severa **Naive correlation, Pearson correlation, local Pearson correlation, instan** and related statistics in order to

- Test the validity of the assumption (i.e. no two features are apprantly correlated).
- Chose source and target features for later model builds.

By doing so, we can get more understanding about the 'quality' and 'inner relations' of the data. If explanatory power to the feature that we want to predict (e.g. "Inflation"), then there is no need for learning models. On the other hand, if one feature has higher-than-random correlations to another the feature and the other as the target. In this case, **to determine which feature leads,** the **Dynamic time wrapping**.

Code and Examples

correlation.py

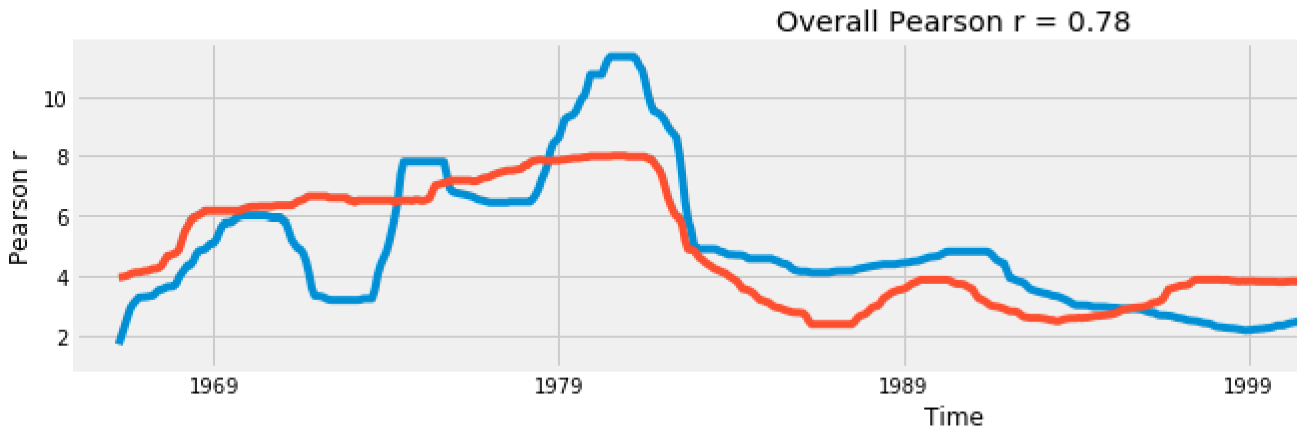
```
Requirement already satisfied: dtw in /usr/local/lib/python3.6/dist-packages (1.4.0)
Requirement already satisfied: scipy in /usr/local/lib/python3.6/dist-packages (from
Requirement already satisfied: numpy in /usr/local/lib/python3.6/dist-packages (from
```

Example: Naive correlation.

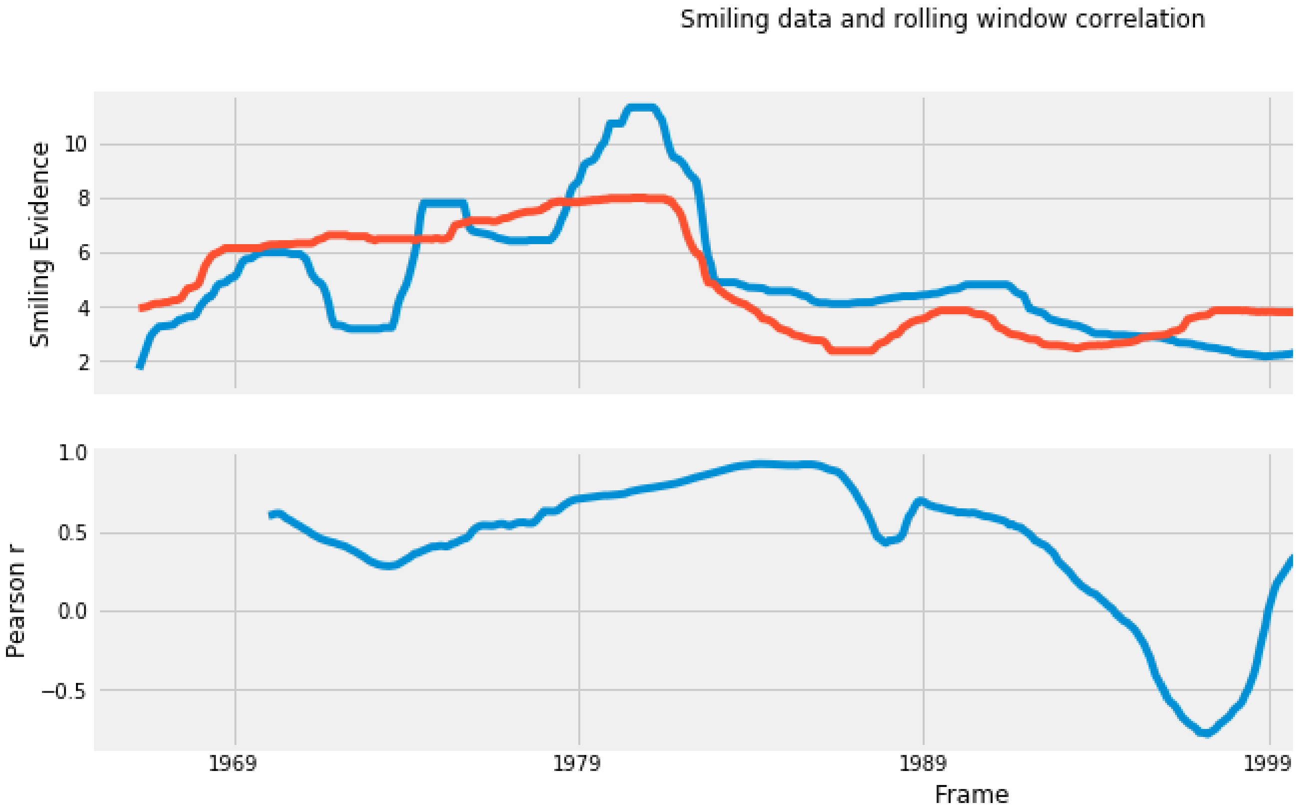
	Inflation	Wage	Unemployment	Consumption	Investment	InterestR
Inflation	1.000000	0.778155	0.191886	0.617820	-0.341421	0.773
Wage	0.778155	1.000000	-0.068529	0.703745	-0.125412	0.647
Unemployment	0.191886	-0.068529	1.000000	-0.097183	-0.038286	-0.027
Consumption	0.617820	0.703745	-0.097183	1.000000	0.203165	0.655
Investment	-0.341421	-0.125412	-0.038286	0.203165	1.000000	-0.234
InterestRate	0.773616	0.647482	-0.027809	0.655305	-0.234573	1.000

Example: Pearson correlation

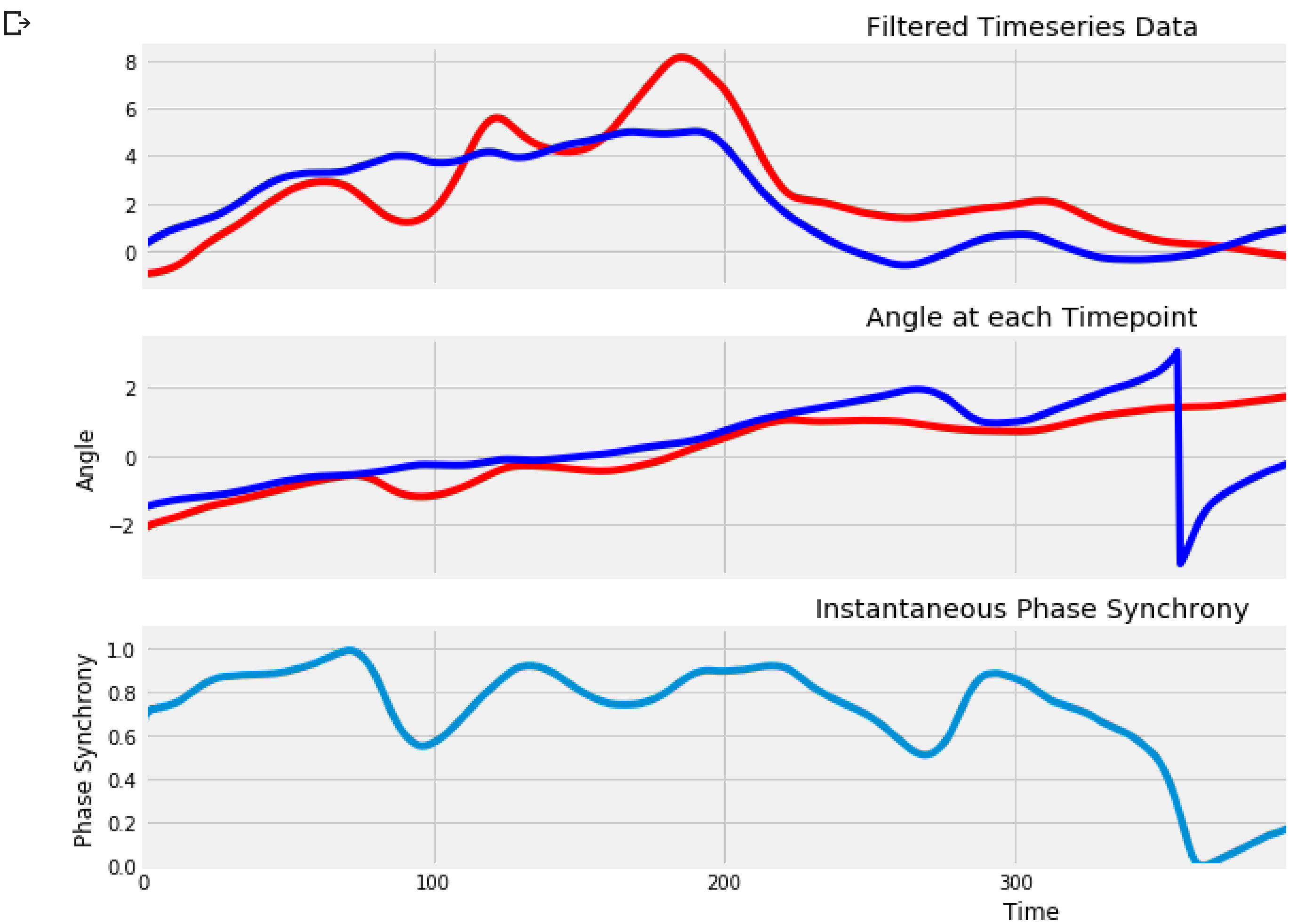
```
Pandas computed Pearson r: 0.7781551675438367
Scipy computed Pearson r: 0.7781551675438365 and p-value: 2.53137614903759e-125
```



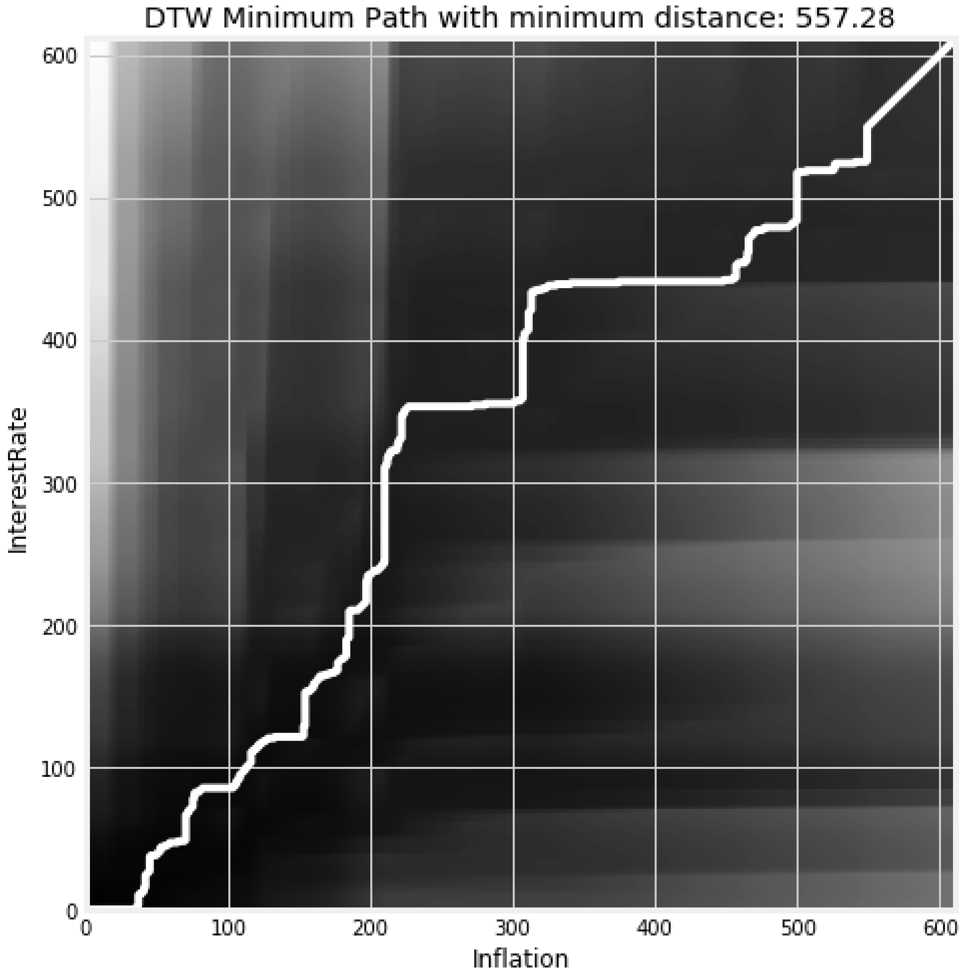
Example: local Pearson correlation



Example: instantaneous phase synchronization



Example: dynamic time wraping



Data analysis

Inspecting the correlations from different angles, we find

- **Inflation and Wage have the highest correlation, 0.778155,** among all tl
- Inflation, Wage, Consumption and IntestRate show quite high positive correlation, and low n Unemployment and Investment.
- **Most features slightly leads the Inflation feature**.
- For the first 30 years, certain feature pairs show **high instantaneous phase synchı**

We conclude that

- **The assumption that no two features have apparent correlation is w**
- It's reasonable to **use Inflation as target and the other 5 features as source for forcastiı** .

Part I.3 Time series analysis with ARIMA

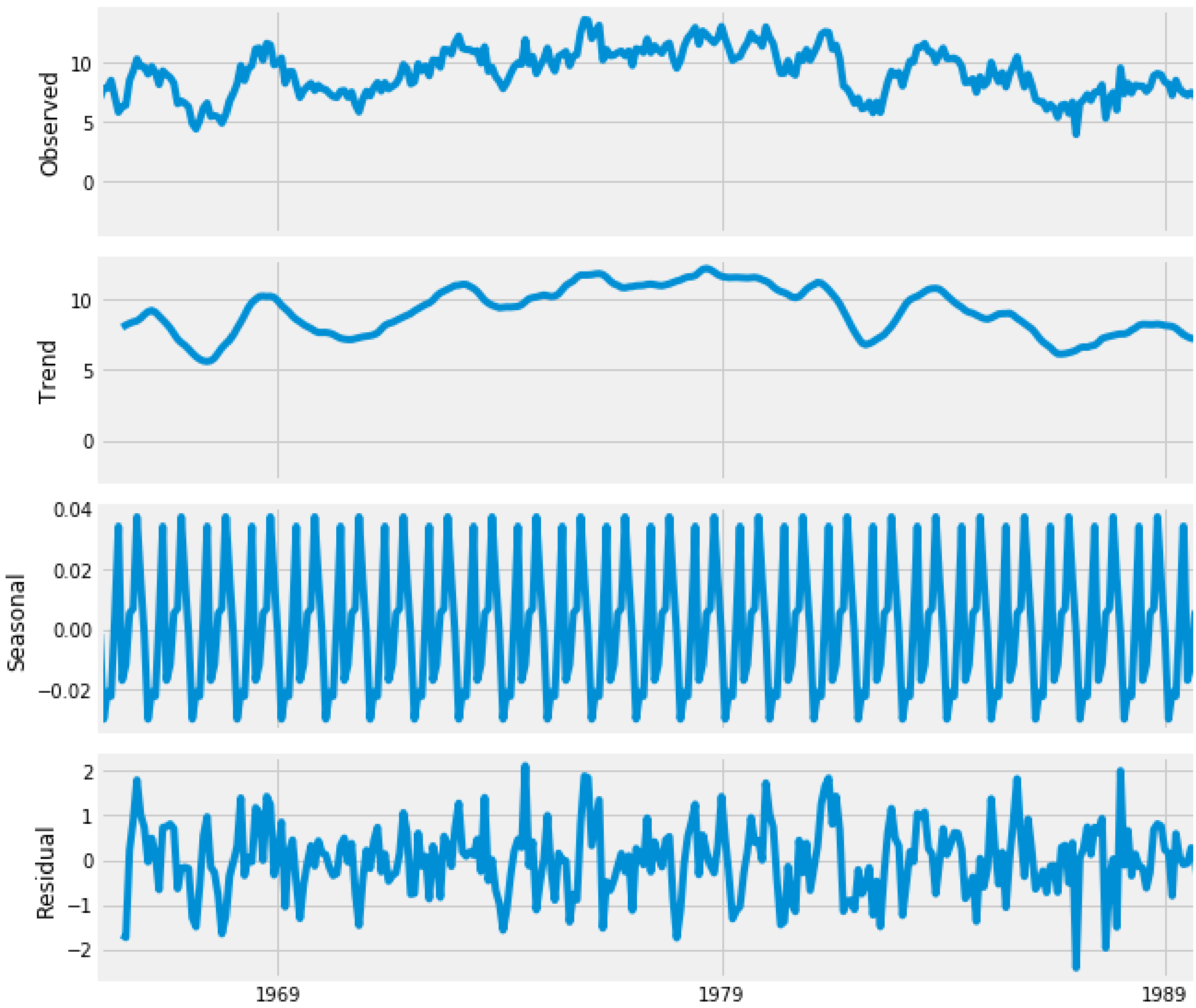
As we mentioned above, some remarkable patterns (e.g. seasonality pattern) naturally appear in c

- We visualize our data using **time-series decomposition** that allows us to decompos trend, seasonality, and noise.
- We **train an ARIMA (Autoregressive Integrated Moving Average) m** Inflation values. To get optimal output, we first
- Use **grid search** to get the optimal parameters for the ARIMA mode.
- We use **ARIMA diagnostics** to investigate any unusual behavior.

Code and examples

`time_series.py`

Example: decompose "Consumption" column into trend, seasonal and residua

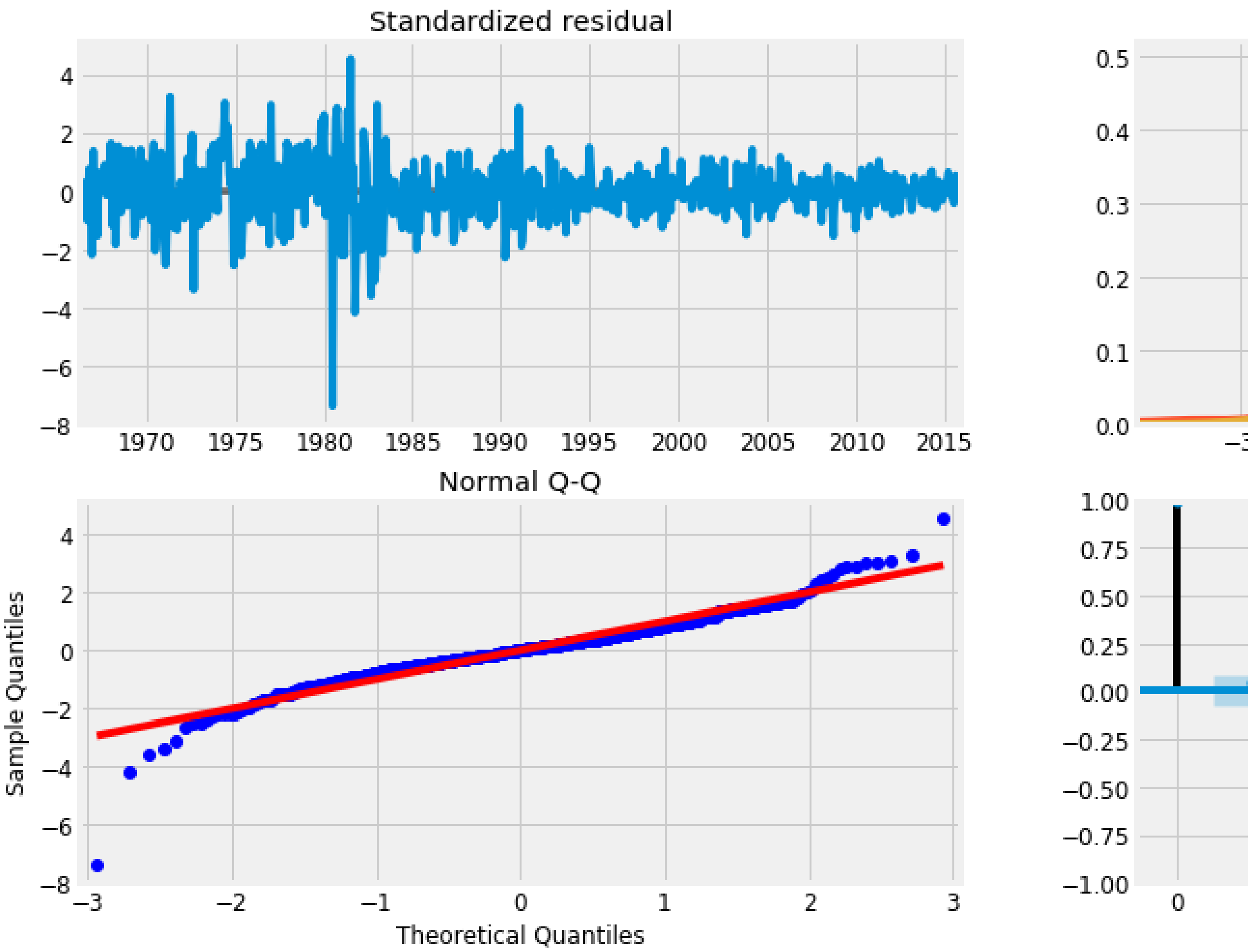


Time series analysis with `ARIMA`

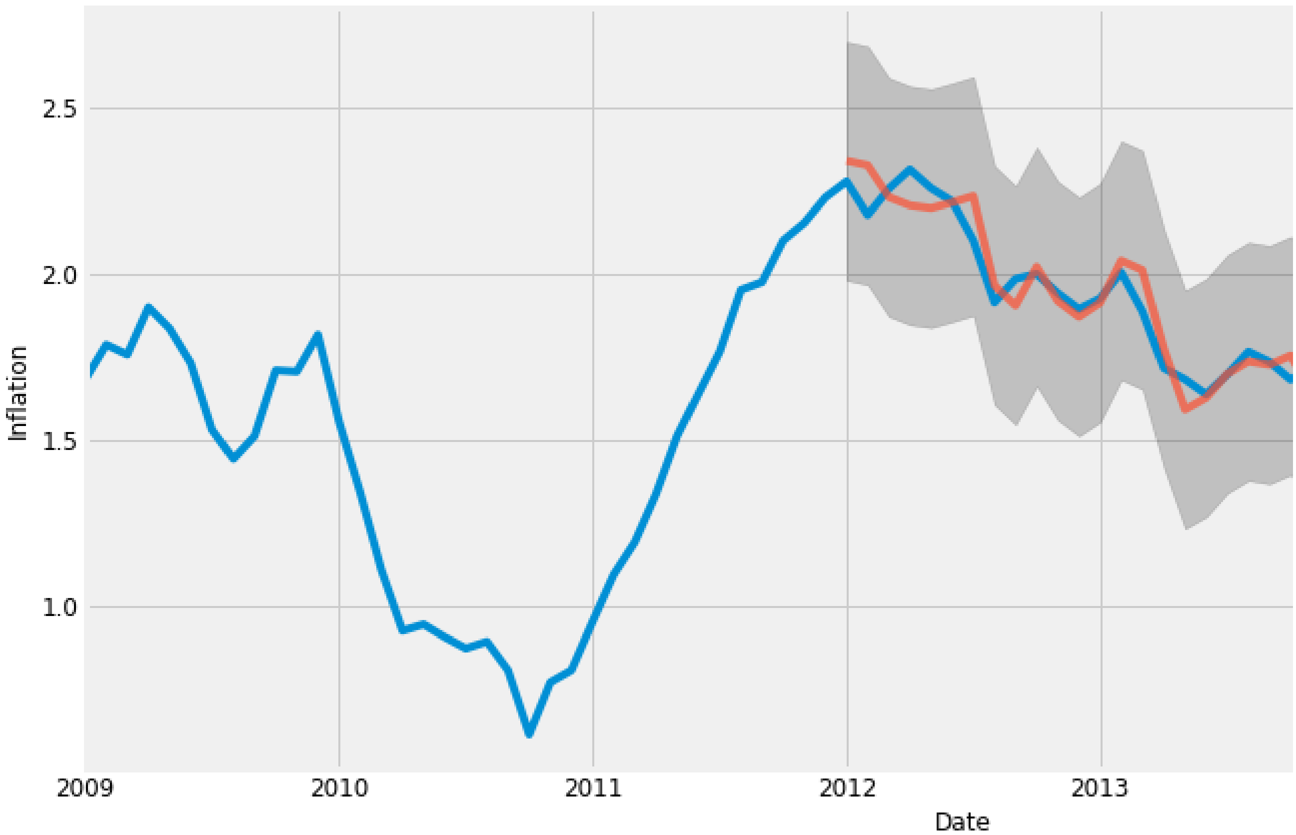
Grid search for optimal `ARIMA` parameters

`ARIMA` training

`ARIMA` diadonostics



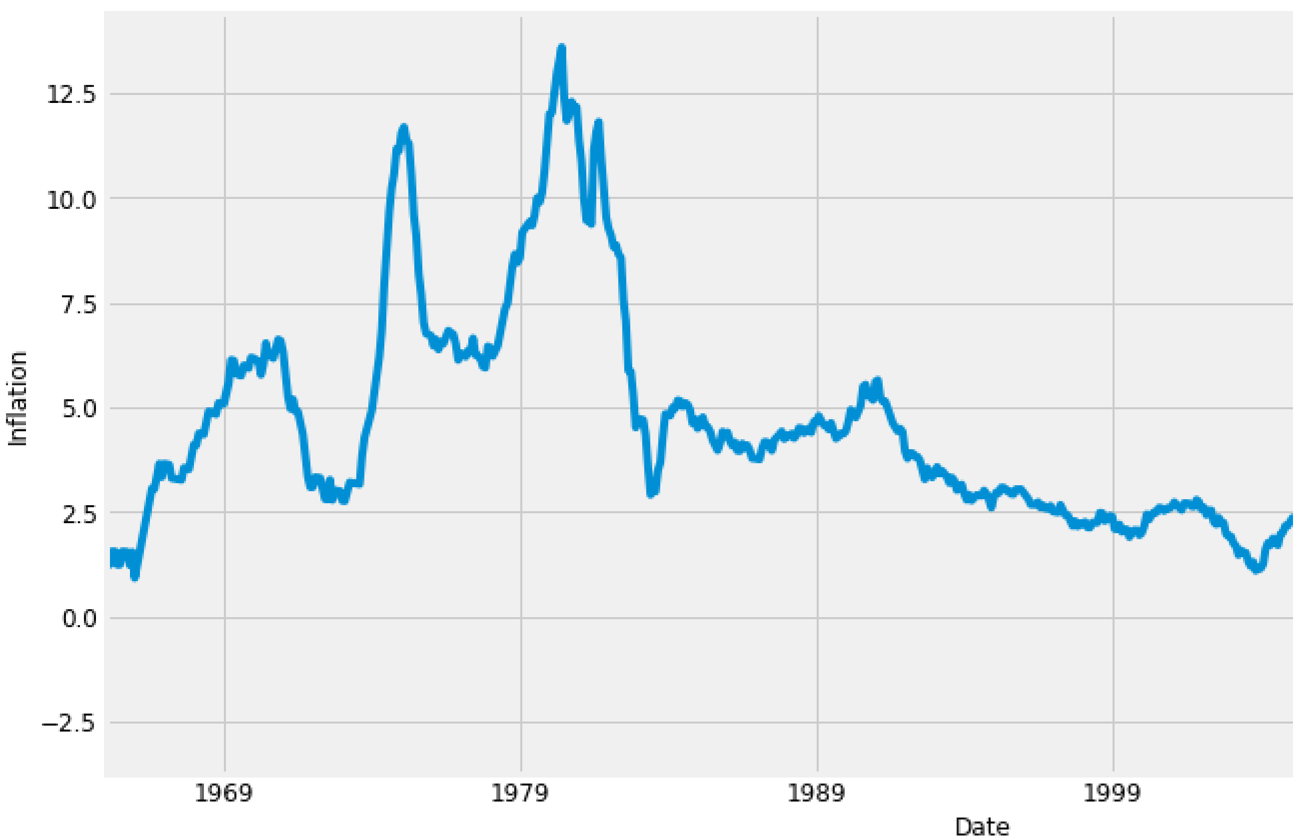
`ARIMA` predictions




```
The Mean Squared Error of our forecasts is 0.004963826636415743

The Root Mean Squared Error of our forecasts is 0.07
```

`ARIMA` forcasts



Data Analysis

- Components plot show the obvious seasonality, for example, in every 10 years, the "**Inflati** a **half-year seasonality**.
- The optimal ARIMA parameters for "Inflation" are `(1, 1, 1)x(0, 0, 1, 12)`
- The ARIMA diagonostics show that the **noise distribution is narrower than the**
- **The one-step ahead forcast captures the overall trend well**.
- As we forecast further out into the future, we becomes less confident in our values. This is r by our model, which grow larger as we move further out into the future.

Part II.1 Basic model: single-step, single-feature fo

Recurrent Neural Networks (RNNs) are good fits for time-series analysis because R designed to capture patterns developing through time.

However, vanilla RNNs have a major disadvantage---the vanishing gradient problem---"the changes so small, making the network unable to converge to a optimal solution.

LSTM (Long-Short Term Memory) is a variation of vanilla RNNS,it overcomes the va problem by clipping gradients if they exceed some constant bounds.

In this section, we will

- Process the data to fit the LSTM model
- **Build and train the LSTM model for single-step, single-feature pred** tomorrow value with only today's values of the other 5 features).

imports

Data preparation

Build and train the LSTM model

Make sure data forms are correct

```
(427, 1, 5)
(427, 1)
(184, 1, 5)
(184, 1)
```

LSTM with SGD, RMSprop, Adam optimizers, epochs = 100

```
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/optimizers.py:79

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow_core/pythor
Instructions for updating:
Use tf.where in 2.0, which has the same broadcast rule as np.where
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

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WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

Train on 427 samples, validate on 184 samples
Epoch 1/100
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

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427/427 [==============================] - 2s 6ms/step - loss: 6.8603 - acc: 0.0000e+
Epoch 2/100
427/427 [==============================] - 1s 3ms/step - loss: 2.4877 - acc: 0.0000e+
Epoch 3/100
427/427 [==============================] - 1s 3ms/step - loss: 1.8379 - acc: 0.0000e+
Epoch 4/100
427/427 [==============================] - 1s 3ms/step - loss: 1.4932 - acc: 0.0000e+
Epoch 5/100
427/427 [==============================] - 1s 3ms/step - loss: 1.2980 - acc: 0.0000e+
Epoch 6/100
427/427 [==============================] - 1s 3ms/step - loss: 1.2265 - acc: 0.0000e+
Epoch 7/100
427/427 [==============================] - 1s 3ms/step - loss: 1.0970 - acc: 0.0000e+
Epoch 8/100
427/427 [==============================] - 1s 3ms/step - loss: 1.0660 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 1.0541 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 1.0670 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 1.0103 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.9960 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.9544 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.9127 - acc: 0.0000e+
Epoch 17/100
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427/427 [==============================] - 1s 3ms/step - loss: 0.9417 - acc: 0.0000e+
Epoch 18/100
427/427 [==============================] - 1s 3ms/step - loss: 0.9365 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.8785 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.8879 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.8620 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.8465 - acc: 0.0000e+
Epoch 27/100
427/427 [==============================] - 1s 3ms/step - loss: 0.8588 - acc: 0.0000e+
Epoch 28/100
427/427 [==============================] - 1s 3ms/step - loss: 0.8365 - acc: 0.0000e+
Epoch 29/100
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427/427 [==============================] - 1s 3ms/step - loss: 0.8323 - acc: 0.0000e+
Epoch 31/100
427/427 [==============================] - 1s 3ms/step - loss: 0.7964 - acc: 0.0000e+
Epoch 32/100
427/427 [==============================] - 1s 3ms/step - loss: 0.8261 - acc: 0.0000e+
Epoch 33/100
427/427 [==============================] - 1s 3ms/step - loss: 0.8114 - acc: 0.0000e+
Epoch 34/100
427/427 [==============================] - 1s 3ms/step - loss: 0.8281 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.8105 - acc: 0.0000e+
Epoch 37/100
427/427 [==============================] - 1s 3ms/step - loss: 0.7924 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.7719 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.7406 - acc: 0.0000e+
Epoch 41/100
427/427 [==============================] - 1s 3ms/step - loss: 0.7874 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.7825 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.7498 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.7355 - acc: 0.0000e+
Epoch 47/100
427/427 [==============================] - 1s 3ms/step - loss: 0.7383 - acc: 0.0000e+
Epoch 48/100
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Epoch 48/100
427/427 [==============================] - 1s 3ms/step - loss: 0.7791 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.6951 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.6459 - acc: 0.0000e+
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Epoch 79/100
427/427 [==============================] - 1s 3ms/step - loss: 0.6751 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.6266 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.6240 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.6331 - acc: 0.0000e+
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427/427 [==============================] - 1s 3ms/step - loss: 0.5983 - acc: 0.0000e+
Epoch 98/100
427/427 [==============================] - 1s 3ms/step - loss: 0.5794 - acc: 0.0000e+
Epoch 99/100
427/427 [==============================] - 1s 3ms/step - loss: 0.5872 - acc: 0.0000e+
Epoch 100/100
```
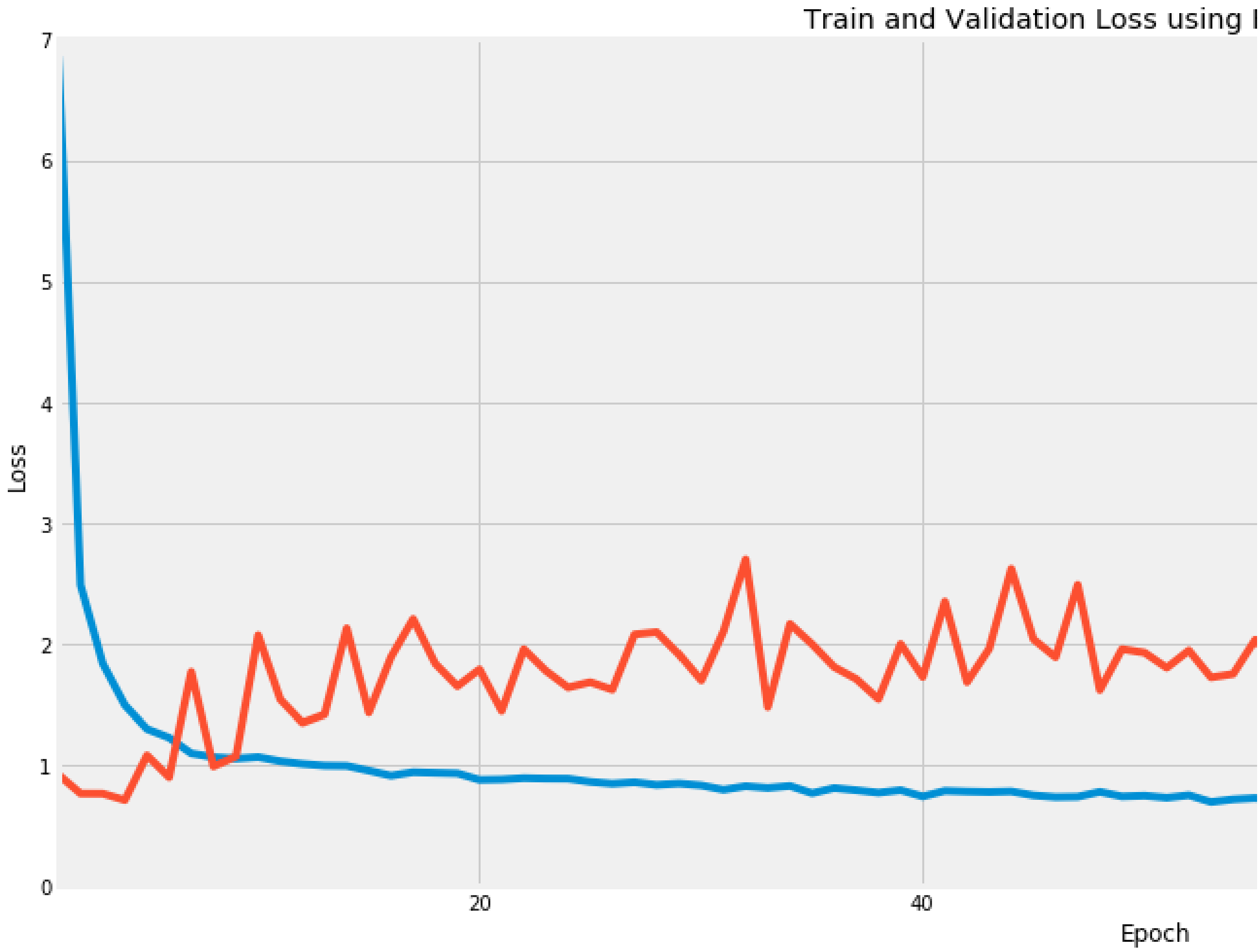

Plot result

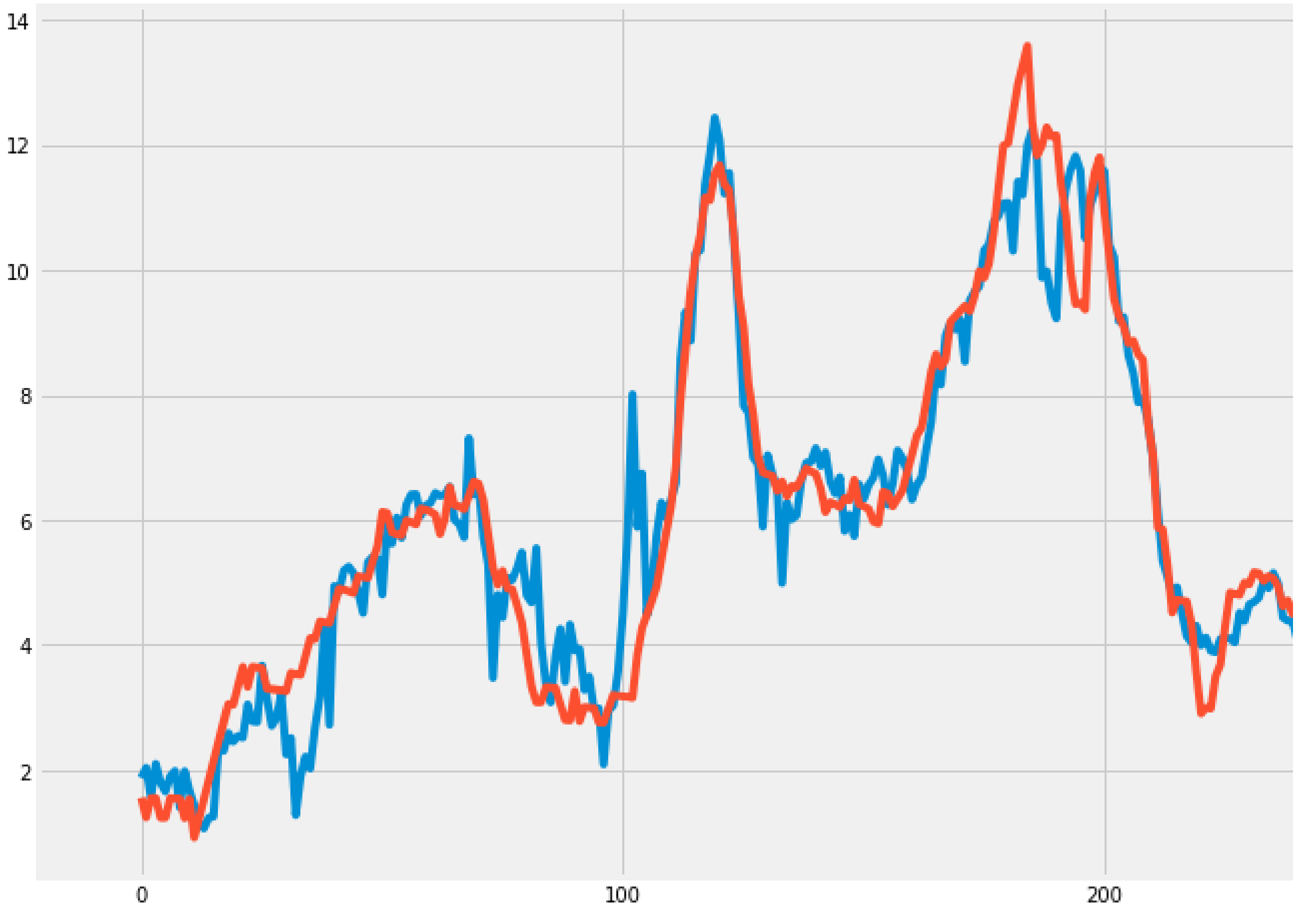
Plot result

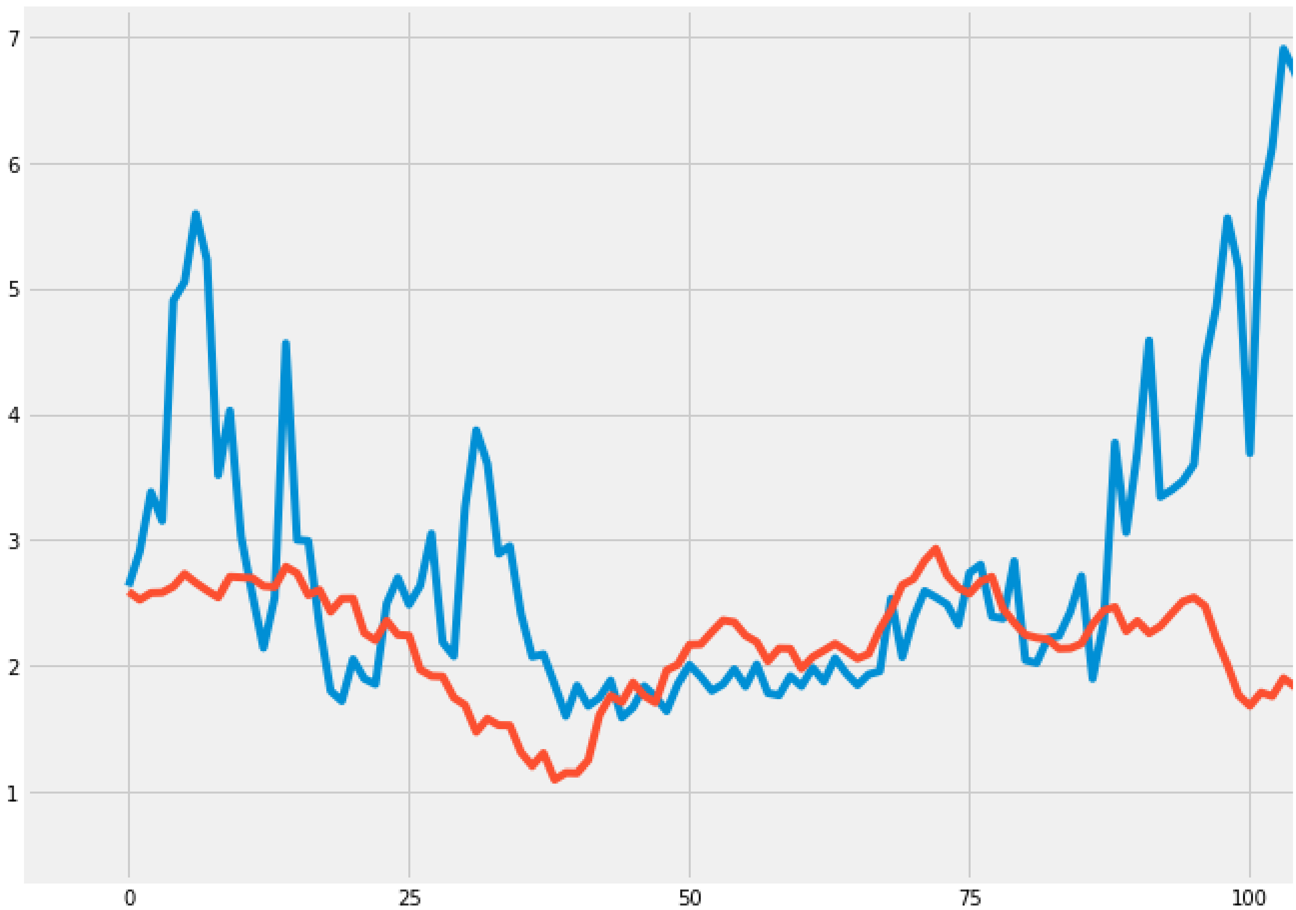


Plot predictions

Plot predictions

```
Train Score: 0.71 RMSE
Test Score: 1.53 RMSE
```





Data Analysis

We only trained the model for 100 epochs, feel free to modify it to any number as long as we have
results we find during the experiments

- LSTM with Adam or RMSprop optimizers work better than the SGD optimizer in this project.
- Each model fits the training dataset very well.
- **The prediction captures the range and characteristics of the real dat**
- **The model doesn't predict the rapid increasing near the 100th test d**

Part II.2 Generalized model: multi-step, multi-fea

We build a multi-step, multi-feature LSTM model in this section. That means we can use several-d
features in the future.
For example, we can use last 12-month's data of Wage, Consumption, In
. In this section, we

- Process the data to fit the requirements of all possible multi-step, multi-feature prediction ta
- We modify the LSTM model accordingly.
- Plot the 3-month prediction for Inflation and Unemployment with last 12-month's data of Wa
  InterestRate.

Data preparation

Make the data forms are all correct

```
(418, 12, 4)
(418, 6)
(180, 12, 4)
(418, 6)
```

Scaling, vectorize and de_vectorize

Multi-step LSTM model, change the input_shape and Dense layer parameter to

Train the model. Change the optimizer parameter to use other optimizers, e.g.

```
Train on 418 samples, validate on 180 samples
Epoch 1/200
418/418 [==============================] - 5s 12ms/step - loss: 5.9280 - acc: 0.2895
Epoch 2/200
418/418 [==============================] - 5s 11ms/step - loss: 1.9184 - acc: 0.4043
Epoch 3/200
418/418 [==============================] - 4s 11ms/step - loss: 1.4018 - acc: 0.3541
Epoch 4/200
418/418 [==============================] - 4s 11ms/step - loss: 1.1442 - acc: 0.3373
Epoch 5/200
418/418 [==============================] - 4s 11ms/step - loss: 0.9653 - acc: 0.3493
Epoch 6/200
418/418 [==============================] - 4s 10ms/step - loss: 0.8703 - acc: 0.3876
Epoch 7/200
418/418 [==============================] - 4s 11ms/step - loss: 0.7075 - acc: 0.3684
Epoch 8/200
418/418 [==============================] - 4s 10ms/step - loss: 0.6512 - acc: 0.3923
Epoch 9/200
418/418 [==============================] - 4s 10ms/step - loss: 0.5565 - acc: 0.4163
Epoch 10/200
418/418 [==============================] - 4s 11ms/step - loss: 0.4753 - acc: 0.4354
Epoch 11/200
418/418 [==============================] - 4s 11ms/step - loss: 0.4950 - acc: 0.4139
Epoch 12/200
418/418 [==============================] - 5s 11ms/step - loss: 0.4238 - acc: 0.4474
Epoch 13/200
418/418 [==============================] - 5s 11ms/step - loss: 0.4073 - acc: 0.4234
Epoch 14/200
418/418 [==============================] - 5s 11ms/step - loss: 0.3882 - acc: 0.4665
Epoch 15/200
418/418 [==============================] - 5s 11ms/step - loss: 0.3522 - acc: 0.4354
Epoch 16/200
418/418 [==============================] - 5s 12ms/step - loss: 0.3426 - acc: 0.4354
Epoch 17/200
418/418 [==============================] - 5s 11ms/step - loss: 0.3134 - acc: 0.4617
Epoch 18/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2790 - acc: 0.4665
Epoch 19/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2807 - acc: 0.4545
Epoch 20/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2760 - acc: 0.4809
Epoch 21/200
418/418 [==============================] - 4s 11ms/step - loss: 0.2589 - acc: 0.5048
Epoch 22/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2368 - acc: 0.4809
Epoch 23/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2378 - acc: 0.4737
Epoch 24/200
418/418 [==============================] - 4s 11ms/step - loss: 0.2329 - acc: 0.4761
Epoch 25/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2324 - acc: 0.5191
Epoch 26/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1927 - acc: 0.4904
Epoch 27/200
418/418 [==============================] - 5s 11ms/step - loss: 0.2153 - acc: 0.5096
Epoch 28/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1898 - acc: 0.5120
Epoch 29/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1831 - acc: 0.4976
Epoch 30/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1925 - acc: 0.5144
```

```
Epoch 31/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1713 - acc: 0.5167
Epoch 32/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1675 - acc: 0.5024
Epoch 33/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1622 - acc: 0.5000
Epoch 34/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1885 - acc: 0.4928
Epoch 35/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1623 - acc: 0.4689
Epoch 36/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1560 - acc: 0.5167
Epoch 37/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1556 - acc: 0.5431
Epoch 38/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1548 - acc: 0.5072
Epoch 39/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1414 - acc: 0.5431
Epoch 40/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1353 - acc: 0.5191
Epoch 41/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1457 - acc: 0.5072
Epoch 42/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1308 - acc: 0.5191
Epoch 43/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1170 - acc: 0.5048
Epoch 44/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1353 - acc: 0.5024
Epoch 45/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1350 - acc: 0.5287
Epoch 46/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1127 - acc: 0.5215
Epoch 47/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1181 - acc: 0.5311
Epoch 48/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1288 - acc: 0.5239
Epoch 49/200
418/418 [==============================] - 4s 10ms/step - loss: 0.1176 - acc: 0.5239
Epoch 50/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1106 - acc: 0.5215
Epoch 51/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1047 - acc: 0.5144
Epoch 52/200
418/418 [==============================] - 5s 11ms/step - loss: 0.1037 - acc: 0.5502
Epoch 53/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0972 - acc: 0.5096
Epoch 54/200
418/418 [==============================] - 4s 11ms/step - loss: 0.1043 - acc: 0.5550
Epoch 55/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0986 - acc: 0.5287
Epoch 56/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0971 - acc: 0.5694
Epoch 57/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0981 - acc: 0.5335
Epoch 58/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0982 - acc: 0.5335
Epoch 59/200
418/418 [==============================] - 5s 12ms/step - loss: 0.0952 - acc: 0.5431
Epoch 60/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0990 - acc: 0.5263
Epoch 61/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0919 - acc: 0.5335
```

```
418/418 [==============================] - 5s 11ms/step - loss: 0.0919 - acc: 0.5359
Epoch 62/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0878 - acc: 0.5311
Epoch 63/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0898 - acc: 0.5502
Epoch 64/200
418/418 [==============================] - 5s 12ms/step - loss: 0.1000 - acc: 0.5167
Epoch 65/200
418/418 [==============================] - 5s 12ms/step - loss: 0.0819 - acc: 0.5526
Epoch 66/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0896 - acc: 0.5718
Epoch 67/200
418/418 [==============================] - 5s 12ms/step - loss: 0.0902 - acc: 0.5431
Epoch 68/200
418/418 [==============================] - 5s 12ms/step - loss: 0.0774 - acc: 0.5024
Epoch 69/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0836 - acc: 0.5311
Epoch 70/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0901 - acc: 0.5526
Epoch 71/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0884 - acc: 0.5407
Epoch 72/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0970 - acc: 0.5359
Epoch 73/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0739 - acc: 0.5694
Epoch 74/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0730 - acc: 0.5598
Epoch 75/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0807 - acc: 0.5335
Epoch 76/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0757 - acc: 0.5502
Epoch 77/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0856 - acc: 0.5478
Epoch 78/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0697 - acc: 0.5526
Epoch 79/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0659 - acc: 0.5574
Epoch 80/200
418/418 [==============================] - 5s 12ms/step - loss: 0.0819 - acc: 0.5766
Epoch 81/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0737 - acc: 0.5191
Epoch 82/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0670 - acc: 0.5718
Epoch 83/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0702 - acc: 0.5574
Epoch 84/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0733 - acc: 0.5766
Epoch 85/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0701 - acc: 0.5718
Epoch 86/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0653 - acc: 0.5598
Epoch 87/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0727 - acc: 0.5431
Epoch 88/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0714 - acc: 0.5383
Epoch 89/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0722 - acc: 0.5478
Epoch 90/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0660 - acc: 0.5766
Epoch 91/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0625 - acc: 0.5718
Epoch 92/200
```

```
418/418 [==============================] - 5s 11ms/step - loss: 0.0623 - acc: 0.5813
Epoch 93/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0697 - acc: 0.5646
Epoch 94/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0656 - acc: 0.5335
Epoch 95/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0573 - acc: 0.5335
Epoch 96/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0591 - acc: 0.5191
Epoch 97/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0596 - acc: 0.5837
Epoch 98/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0561 - acc: 0.5598
Epoch 99/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0662 - acc: 0.5311
Epoch 100/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0594 - acc: 0.5383
Epoch 101/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0598 - acc: 0.5670
Epoch 102/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0594 - acc: 0.5191
Epoch 103/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0539 - acc: 0.5718
Epoch 104/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0580 - acc: 0.5550
Epoch 105/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0601 - acc: 0.5574
Epoch 106/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0552 - acc: 0.5502
Epoch 107/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0651 - acc: 0.5550
Epoch 108/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0549 - acc: 0.5598
Epoch 109/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0488 - acc: 0.5478
Epoch 110/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0501 - acc: 0.5431
Epoch 111/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0506 - acc: 0.5478
Epoch 112/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0516 - acc: 0.5335
Epoch 113/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0528 - acc: 0.5694
Epoch 114/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0548 - acc: 0.5574
Epoch 115/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0476 - acc: 0.5694
Epoch 116/200
418/418 [==============================] - 5s 13ms/step - loss: 0.0497 - acc: 0.5957
Epoch 117/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0511 - acc: 0.5478
Epoch 118/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0545 - acc: 0.5455
Epoch 119/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0605 - acc: 0.5646
Epoch 120/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0538 - acc: 0.5670
Epoch 121/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0523 - acc: 0.5455
Epoch 122/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0517 - acc: 0.5742
Epoch 123/200
```

```
Epoch 123/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0463 - acc: 0.5670
Epoch 124/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0461 - acc: 0.5813
Epoch 125/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0423 - acc: 0.5550
Epoch 126/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0479 - acc: 0.5550
Epoch 127/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0486 - acc: 0.5837
Epoch 128/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0541 - acc: 0.5407
Epoch 129/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0455 - acc: 0.5478
Epoch 130/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0582 - acc: 0.5670
Epoch 131/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0479 - acc: 0.5622
Epoch 132/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0408 - acc: 0.5622
Epoch 133/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0622 - acc: 0.5526
Epoch 134/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0443 - acc: 0.5383
Epoch 135/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0419 - acc: 0.5598
Epoch 136/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0398 - acc: 0.5431
Epoch 137/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0430 - acc: 0.5526
Epoch 138/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0430 - acc: 0.5646
Epoch 139/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0418 - acc: 0.5694
Epoch 140/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0429 - acc: 0.5813
Epoch 141/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0384 - acc: 0.5837
Epoch 142/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0419 - acc: 0.5670
Epoch 143/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0383 - acc: 0.5646
Epoch 144/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0431 - acc: 0.5909
Epoch 145/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0404 - acc: 0.5646
Epoch 146/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0421 - acc: 0.5502
Epoch 147/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0400 - acc: 0.5455
Epoch 148/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0397 - acc: 0.5550
Epoch 149/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0367 - acc: 0.5574
Epoch 150/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0366 - acc: 0.5359
Epoch 151/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0400 - acc: 0.5813
Epoch 152/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0369 - acc: 0.5455
Epoch 153/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0363 - acc: 0.5718
```

```
Epoch 154/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0405 - acc: 0.5455
Epoch 155/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0373 - acc: 0.5478
Epoch 156/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0429 - acc: 0.5455
Epoch 157/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0392 - acc: 0.5909
Epoch 158/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0395 - acc: 0.5646
Epoch 159/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0454 - acc: 0.5526
Epoch 160/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0428 - acc: 0.5335
Epoch 161/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0389 - acc: 0.5718
Epoch 162/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0451 - acc: 0.5574
Epoch 163/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0364 - acc: 0.5742
Epoch 164/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0412 - acc: 0.5598
Epoch 165/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0393 - acc: 0.5359
Epoch 166/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0408 - acc: 0.5646
Epoch 167/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0359 - acc: 0.5789
Epoch 168/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0431 - acc: 0.5742
Epoch 169/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0365 - acc: 0.5742
Epoch 170/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0400 - acc: 0.5646
Epoch 171/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0396 - acc: 0.5789
Epoch 172/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0393 - acc: 0.5718
Epoch 173/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0373 - acc: 0.5789
Epoch 174/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0394 - acc: 0.5909
Epoch 175/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0359 - acc: 0.5478
Epoch 176/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0361 - acc: 0.5670
Epoch 177/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0336 - acc: 0.5718
Epoch 178/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0420 - acc: 0.5766
Epoch 179/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0380 - acc: 0.5622
Epoch 180/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0358 - acc: 0.5502
Epoch 181/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0352 - acc: 0.5407
Epoch 182/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0404 - acc: 0.5885
Epoch 183/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0381 - acc: 0.6077
Epoch 184/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0359 - acc: 0.5718
```

```
Epoch 185/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0364 - acc: 0.5526
Epoch 186/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0351 - acc: 0.5742
Epoch 187/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0344 - acc: 0.5646
Epoch 188/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0348 - acc: 0.5598
Epoch 189/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0348 - acc: 0.5789
Epoch 190/200
418/418 [==============================] - 4s 10ms/step - loss: 0.0370 - acc: 0.5742
Epoch 191/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0361 - acc: 0.5622
Epoch 192/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0327 - acc: 0.5550
Epoch 193/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0346 - acc: 0.5837
Epoch 194/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0342 - acc: 0.5718
Epoch 195/200
418/418 [==============================] - 4s 11ms/step - loss: 0.0324 - acc: 0.5670
Epoch 196/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0328 - acc: 0.5646
Epoch 197/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0396 - acc: 0.5789
Epoch 198/200
418/418 [==============================] - 5s 11ms/step - loss: 0.0418 - acc: 0.5957
```

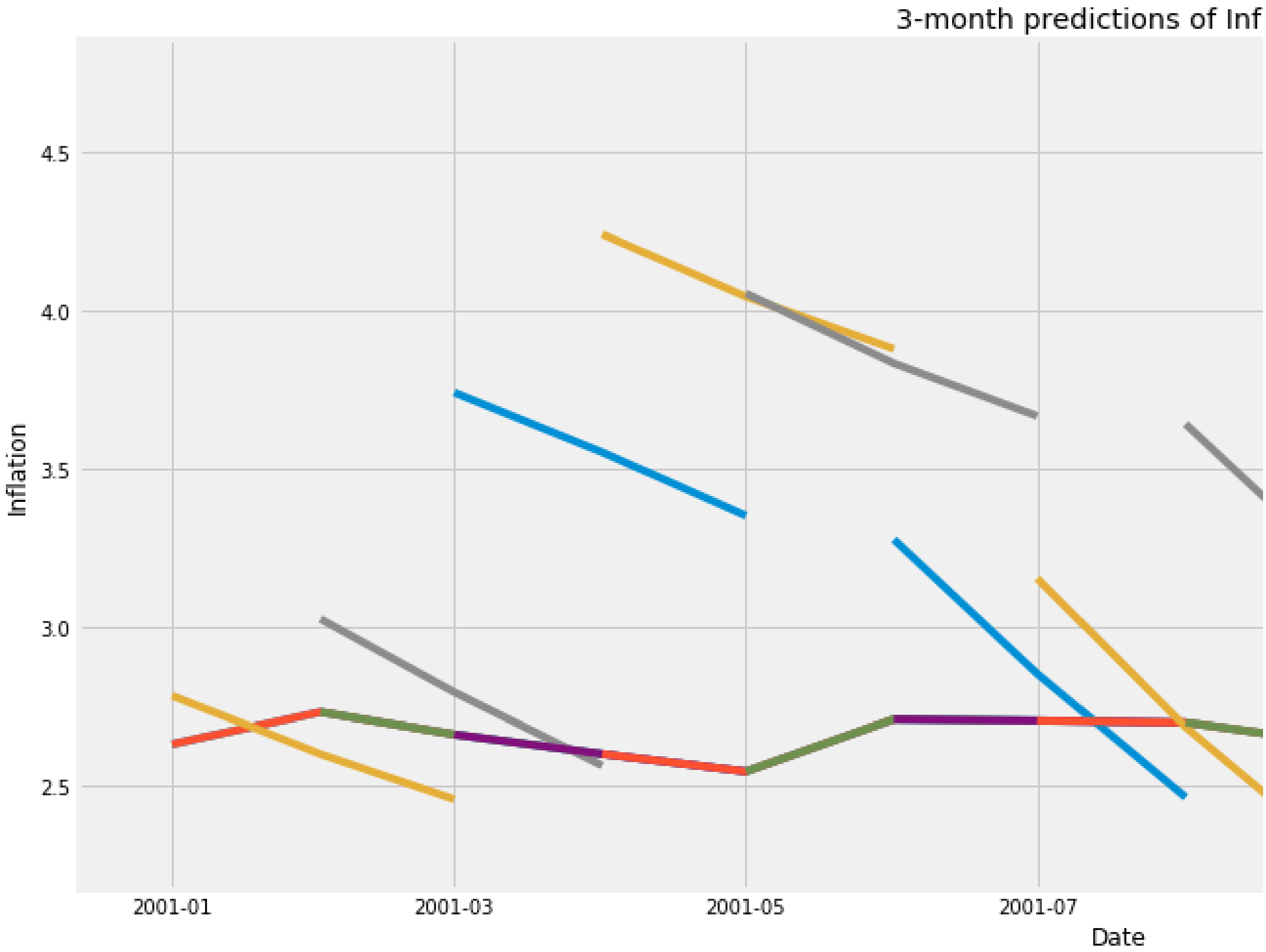
Make predictions with the trained model

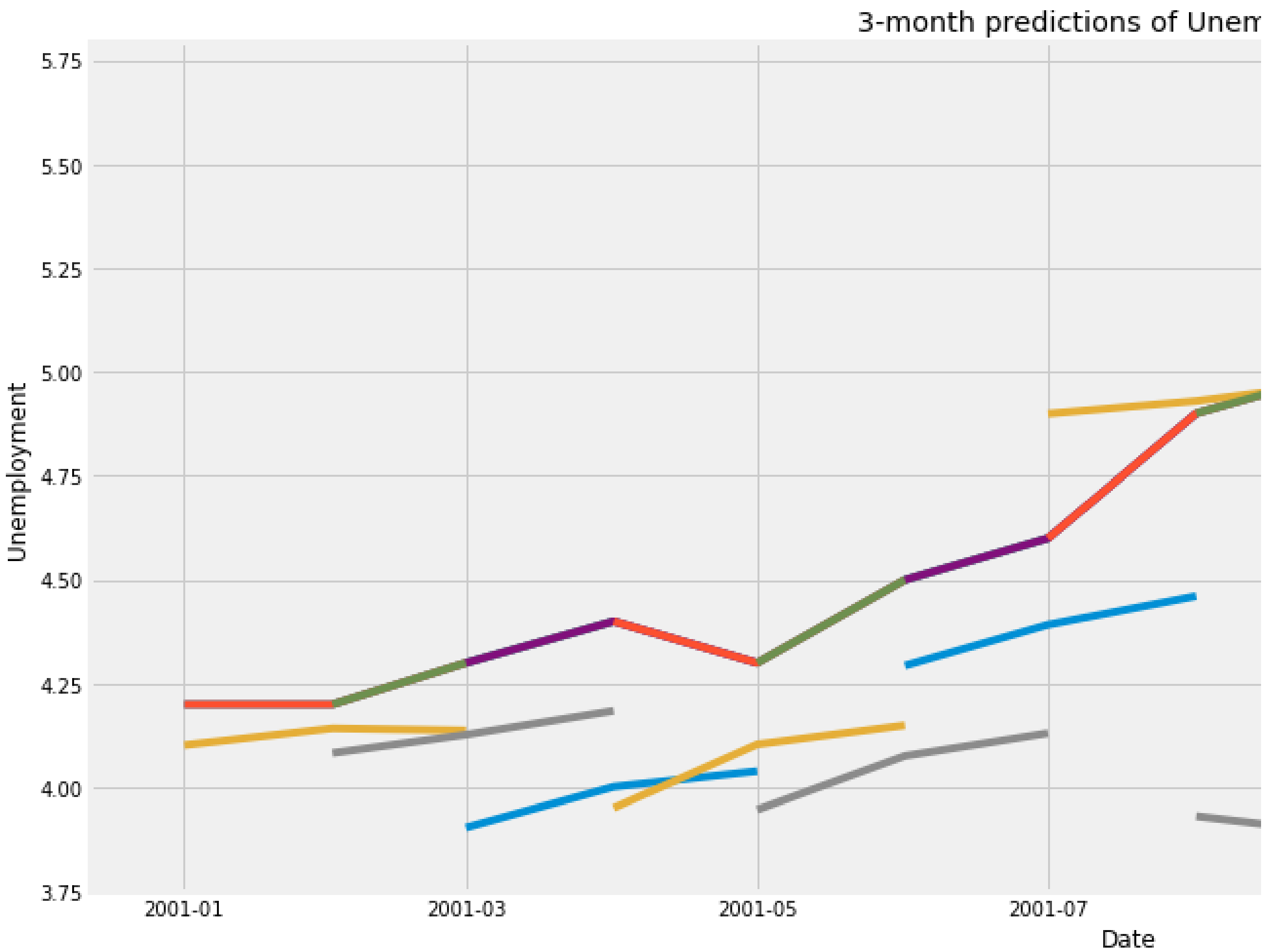
Plot Multi-step, Multi-feature predictions.

To read to graph below

- Each short line segment is a 3-month prediction: start, middle, end point of the line segment month's data respectively.
- X axies is the data.
- The long line is the real data.
- We plot the prediction for year 2001, change the parameter as you want to get prediction for

We show the first 12 month's data and corresponding 3-month predictions for


3-month predictions of Inf
Inflation
4.5
4.0
3.5
3.0
2.5
2001-01
2001-03
2001-05
2001-07
Date


3-month predictions of Unem
Unemployment
5.75
5.50
5.25
5.00
4.75
4.50
4.25
4.00
3.75
2001-01
2001-03
2001-05
2001-07
Date

Data Analysis

Though the dataset is not big enough, we still successfully capture several features in the predicti

- **Model predictions shows similar trend as the real data**, e.g. from the prec predicted values are more or less in the most correct range and goes in the same direction a
- **The model captures the range of the real data very precisely**.
- **All 3-month predictions are continuous**, which means the modell successfully

Part II.3 Advanced model: Generative Adversaria

Generative Adversarial Networks (GAN) have been a successful model in genera **The idea that GANs can to used to predict time-series data is new and e:** in learning characteristics of data, our model is based on the **assumptions**.

- Values of a **feature has certain patterns** and behavior (characteristics).
- **The future values of a feature should follow more or less the same pa** operating in a totally different way, or the economy drastically changes).

Our **goal** is that

- Generate future data that has similar (surely not exactly the same) distribution as the histori

In our model, we use

- **LSTM as a time-series generator**.
- **1-dimensional CNN as a discriminator**.

imports

Data preparation

Make sure all data forms are as what we want

```
(418, 12, 4)
(418, 6)
(180, 12, 4)
(180, 6)
```

Model architecture: LSTM generator

It's a 1-layer LSTM model.

- 50 hidden layers of LSTM cells
- 1 dense layer with 6 (2*3) dimensional output, since we have 2 features and 3 months to pre

Create generator

```
Model: "sequential_6"
_________________________________________________________________
Layer (type)                 Output Shape              Param #   
=================================================================
lstm_5 (LSTM)                (None, 50)                11000     
_________________________________________________________________
dense_5 (Dense)              (None, 6)                 306       
=================================================================
Total params: 11,306
Trainable params: 11,306
Non-trainable params: 0
_________________________________________________________________
```

Model architecture: CNN discriminator

The structure of the discriminator is given by

- Reshape layer. Each row in y_train is acturally 1-dimensional (6,), which is different from (6,1
- 1-dimensional Convolutional layer with 32, 3×1 filters to capture the characteristics of 3-mc
- LeakyReLU layer
- Dropout layer. Random reconfigurate 10% of the weights to zero to prevent overfitting.
- 1-dimensional Convolutional layer with 64, 3×1 filters to capture more characteristics of the
- Batchnormalization layer. To normalize the data.
- 1 Dense layer with 50 hidden nets.
- Dropout layer.
- 1 Dense layer with 1 net.

Create discriminator

```
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl

WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorfl
Instructions for updating:
Please use `rate` instead of `keep_prob`. Rate should be set to `rate = 1 - keep_prob
Model: "sequential_7"
_________________________________________________________________
Layer (type)                 Output Shape              Param #
=================================================================
reshape_1 (Reshape)          (None, 6, 1)              0
_________________________________________________________________
conv1d_1 (Conv1D)            (None, 4, 32)             128
_________________________________________________________________
leaky_re_lu_1 (LeakyReLU)    (None, 4, 32)             0
_________________________________________________________________
dropout_1 (Dropout)          (None, 4, 32)             0
_________________________________________________________________
conv1d_2 (Conv1D)            (None, 2, 64)             6208
_________________________________________________________________
batch_normalization_1 (Batch (None, 2, 64)             256
_________________________________________________________________
dense_6 (Dense)              (None, 2, 50)             3250
_________________________________________________________________
dropout_2 (Dropout)          (None, 2, 50)             0
_________________________________________________________________
flatten_1 (Flatten)          (None, 100)               0
_________________________________________________________________
dense_7 (Dense)              (None, 1)                 101
=================================================================
Total params: 9,943
Trainable params: 9,815
Non-trainable params: 128
_________________________________________________________________
```

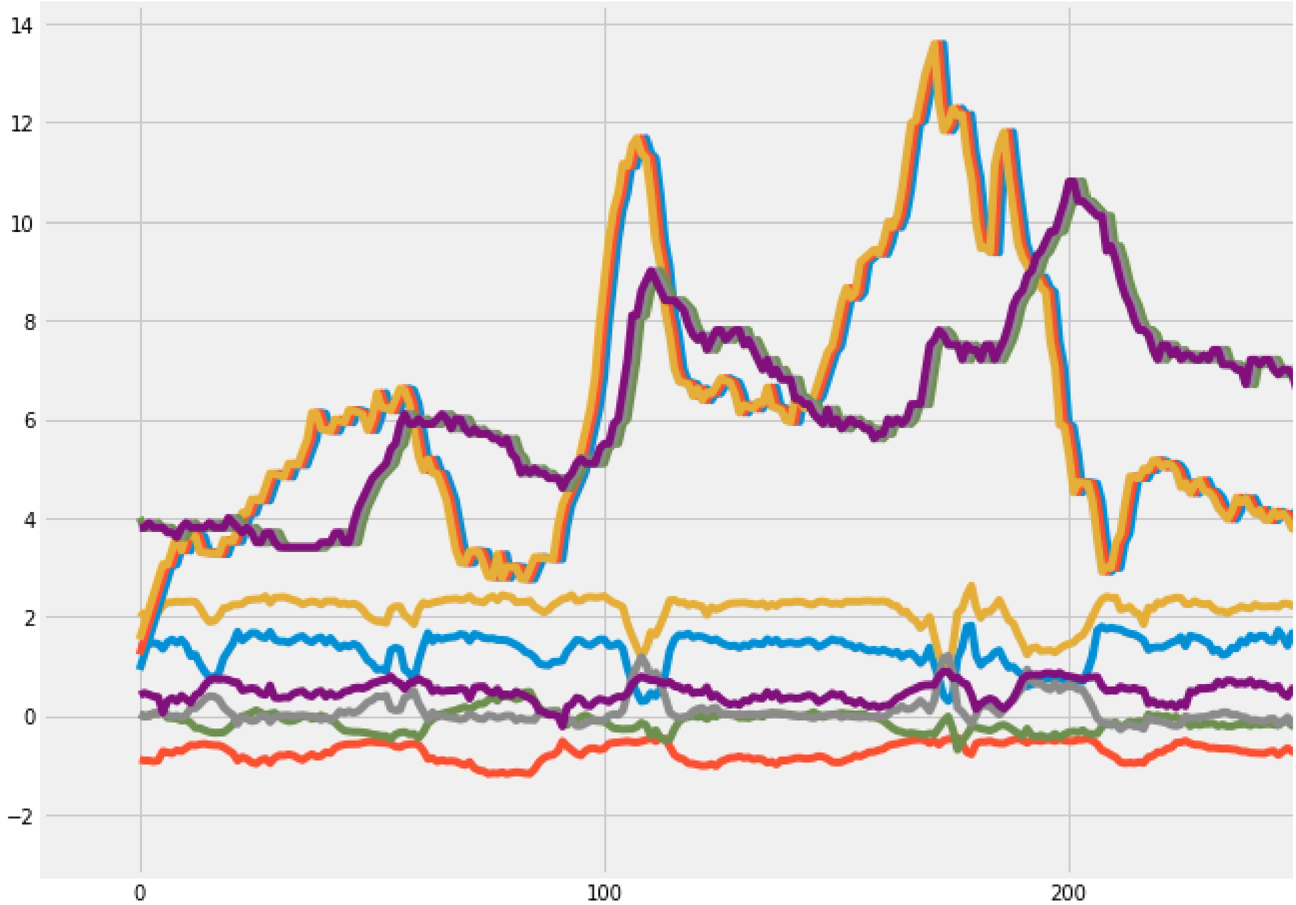
Create a GAN model with LSTM as the generator and CNN as the discriminato

```
Model: "model_1"
_________________________________________________________________
Layer (type)                 Output Shape              Param #
=================================================================
input_1 (InputLayer)         (None, 12, 4)             0
_________________________________________________________________
sequential_6 (Sequential)    (None, 6)                 11306
_________________________________________________________________
sequential_7 (Sequential)    (None, 1)                 9943
=================================================================
Total params: 21,249
Trainable params: 11,306
Non-trainable params: 9,943
_________________________________________________________________
```

Training function for the entangled GAN model

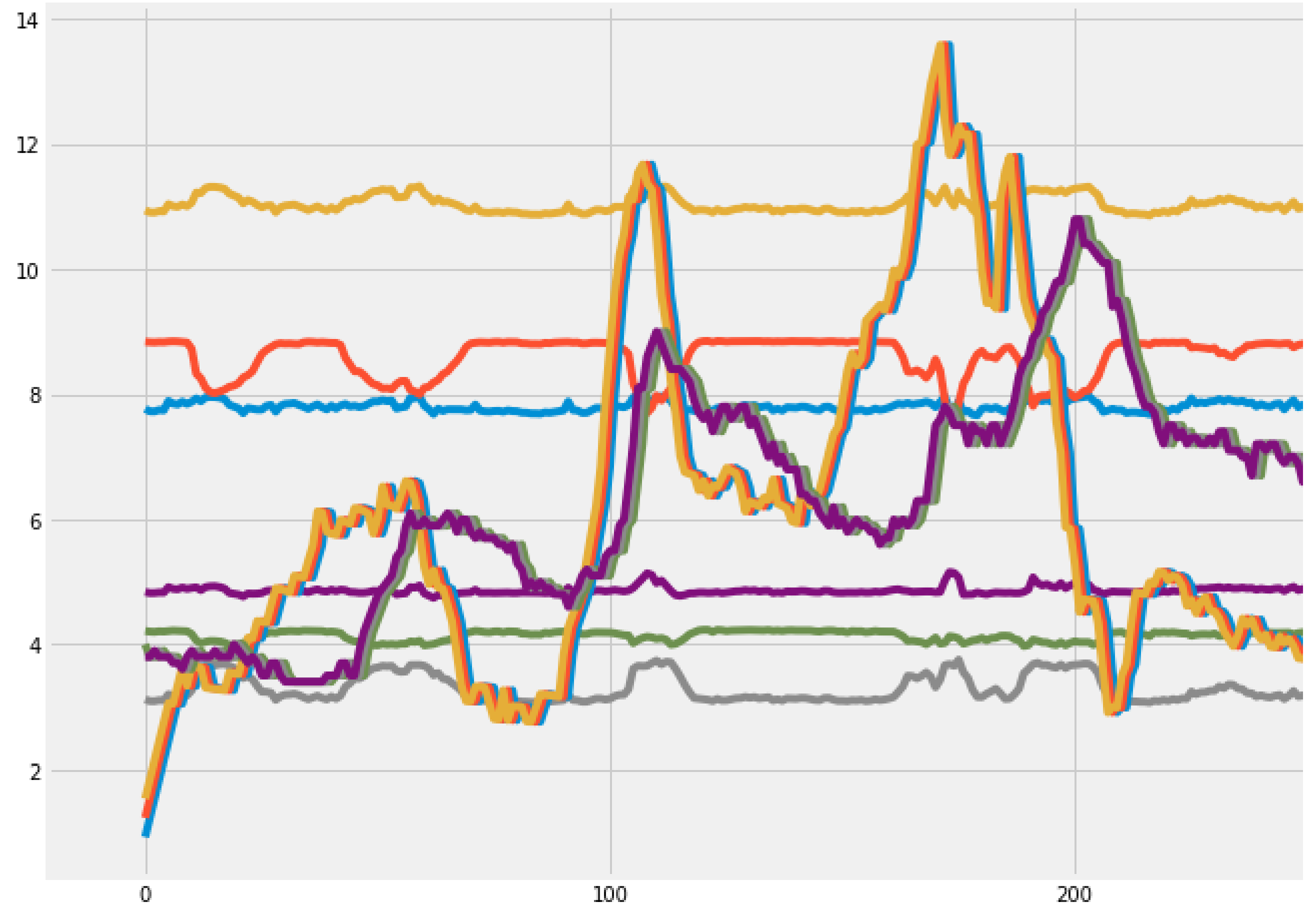
```
training(x_train, y_train, x_test, y_test, epochs=100, random_size=128)
```

```
  0%|          | 0/128 [00:00<?, ?it/s]Epoch 1
100%|██████████| 128/128 [00:08<00:00, 15.65it/s]
```



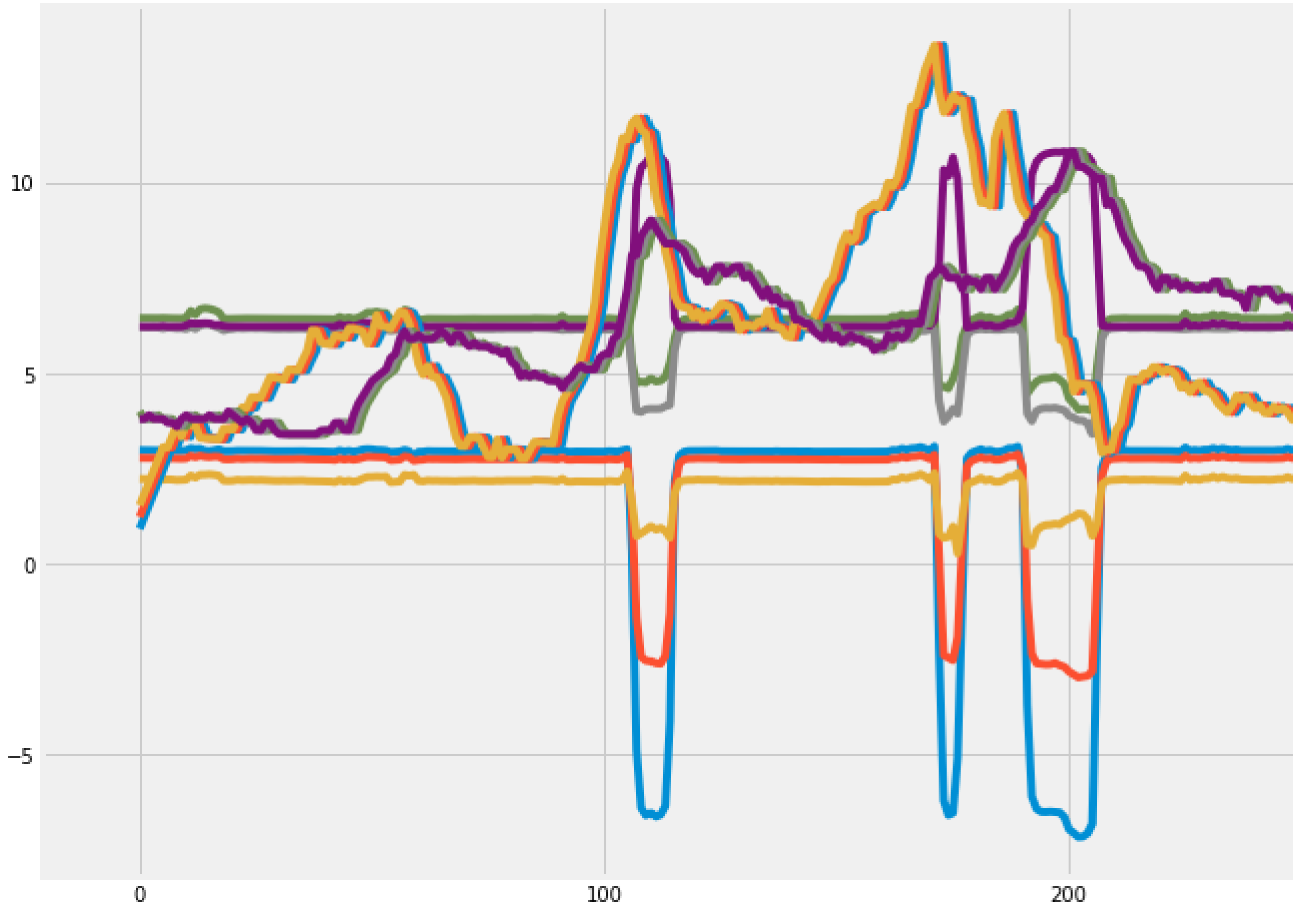

```
  2%|▏         | 2/128 [00:00<00:06, 19.94it/s]Epoch 2
100%|██████████| 128/128 [00:04<00:00, 29.42it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.94it/s]Epoch 3
100%|██████████| 128/128 [00:04<00:00, 29.58it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.07it/s]Epoch 4
100%|██████████| 128/128 [00:04<00:00, 29.35it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.72it/s]Epoch 5
100%|██████████| 128/128 [00:04<00:00, 29.83it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.50it/s]Epoch 6
100%|██████████| 128/128 [00:04<00:00, 30.25it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.87it/s]Epoch 7
100%|██████████| 128/128 [00:04<00:00, 30.41it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.67it/s]Epoch 8
100%|██████████| 128/128 [00:04<00:00, 30.37it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.97it/s]Epoch 9
100%|██████████| 128/128 [00:04<00:00, 30.58it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.65it/s]Epoch 10
100%|██████████| 128/128 [00:04<00:00, 30.07it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.40it/s]Epoch 11
100%|██████████| 128/128 [00:04<00:00, 30.25it/s]
  2%|▏         | 3/128 [00:00<00:04, 26.66it/s]Epoch 12
100%|██████████| 128/128 [00:04<00:00, 30.41it/s]
  3%|▎         | 4/128 [00:00<00:04, 29.75it/s]Epoch 13
100%|██████████| 128/128 [00:04<00:00, 29.22it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.95it/s]Epoch 14
100%|██████████| 128/128 [00:04<00:00, 30.80it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.43it/s]Epoch 15
100%|██████████| 128/128 [00:04<00:00, 31.35it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.34it/s]Epoch 16
100%|██████████| 128/128 [00:04<00:00, 30.07it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.40it/s]Epoch 17
100%|██████████| 128/128 [00:04<00:00, 31.02it/s]
```

```
  3%|▎         | 4/128 [00:00<00:04, 30.01it/s]Epoch 18
100%|██████████| 128/128 [00:04<00:00, 30.52it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.46it/s]Epoch 19
100%|██████████| 128/128 [00:04<00:00, 31.62it/s]
  3%|▎         | 4/128 [00:00<00:03, 34.89it/s]Epoch 20
100%|██████████| 128/128 [00:04<00:00, 31.69it/s]
```



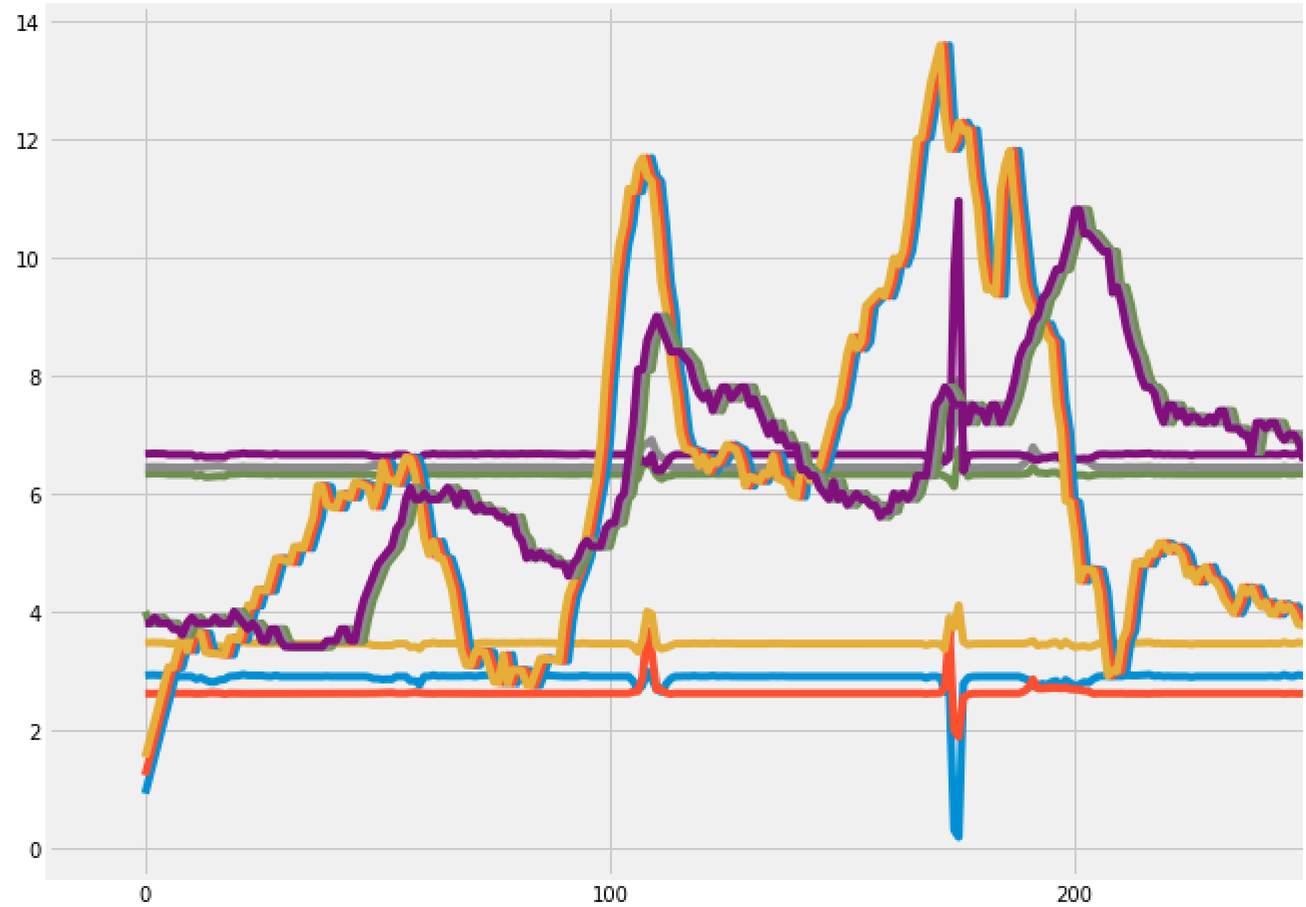

```
  2%|▏         | 2/128 [00:00<00:06, 19.48it/s]Epoch 21
100%|██████████| 128/128 [00:04<00:00, 29.86it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.29it/s]Epoch 22
100%|██████████| 128/128 [00:04<00:00, 29.05it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.60it/s]Epoch 23
100%|██████████| 128/128 [00:04<00:00, 29.78it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.10it/s]Epoch 24
100%|██████████| 128/128 [00:04<00:00, 29.62it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.07it/s]Epoch 25
100%|██████████| 128/128 [00:04<00:00, 29.27it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.76it/s]Epoch 26
100%|██████████| 128/128 [00:04<00:00, 29.74it/s]
  2%|▏         | 3/128 [00:00<00:04, 26.23it/s]Epoch 27
100%|██████████| 128/128 [00:04<00:00, 28.71it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.21it/s]Epoch 28
100%|██████████| 128/128 [00:04<00:00, 29.99it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.93it/s]Epoch 29
100%|██████████| 128/128 [00:04<00:00, 30.66it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.86it/s]Epoch 30
100%|██████████| 128/128 [00:04<00:00, 29.74it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.26it/s]Epoch 31
100%|██████████| 128/128 [00:04<00:00, 30.43it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.09it/s]Epoch 32
100%|██████████| 128/128 [00:04<00:00, 30.46it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.95it/s]Epoch 33
100%|██████████| 128/128 [00:04<00:00, 29.99it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.55it/s]Epoch 34
100%|██████████| 128/128 [00:04<00:00, 29.70it/s]
```

```
  2%|▌         | 3/128 [00:00<00:04, 28.76it/s]Epoch 35
100%|██████████| 128/128 [00:04<00:00, 29.75it/s]
  2%|▌         | 3/128 [00:00<00:04, 28.67it/s]Epoch 36
100%|██████████| 128/128 [00:04<00:00, 29.09it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.19it/s]Epoch 37
100%|██████████| 128/128 [00:04<00:00, 29.67it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.92it/s]Epoch 38
100%|██████████| 128/128 [00:04<00:00, 28.88it/s]
  2%|▌         | 3/128 [00:00<00:04, 28.82it/s]Epoch 39
100%|██████████| 128/128 [00:04<00:00, 29.19it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.61it/s]Epoch 40
100%|██████████| 128/128 [00:04<00:00, 29.19it/s]
```



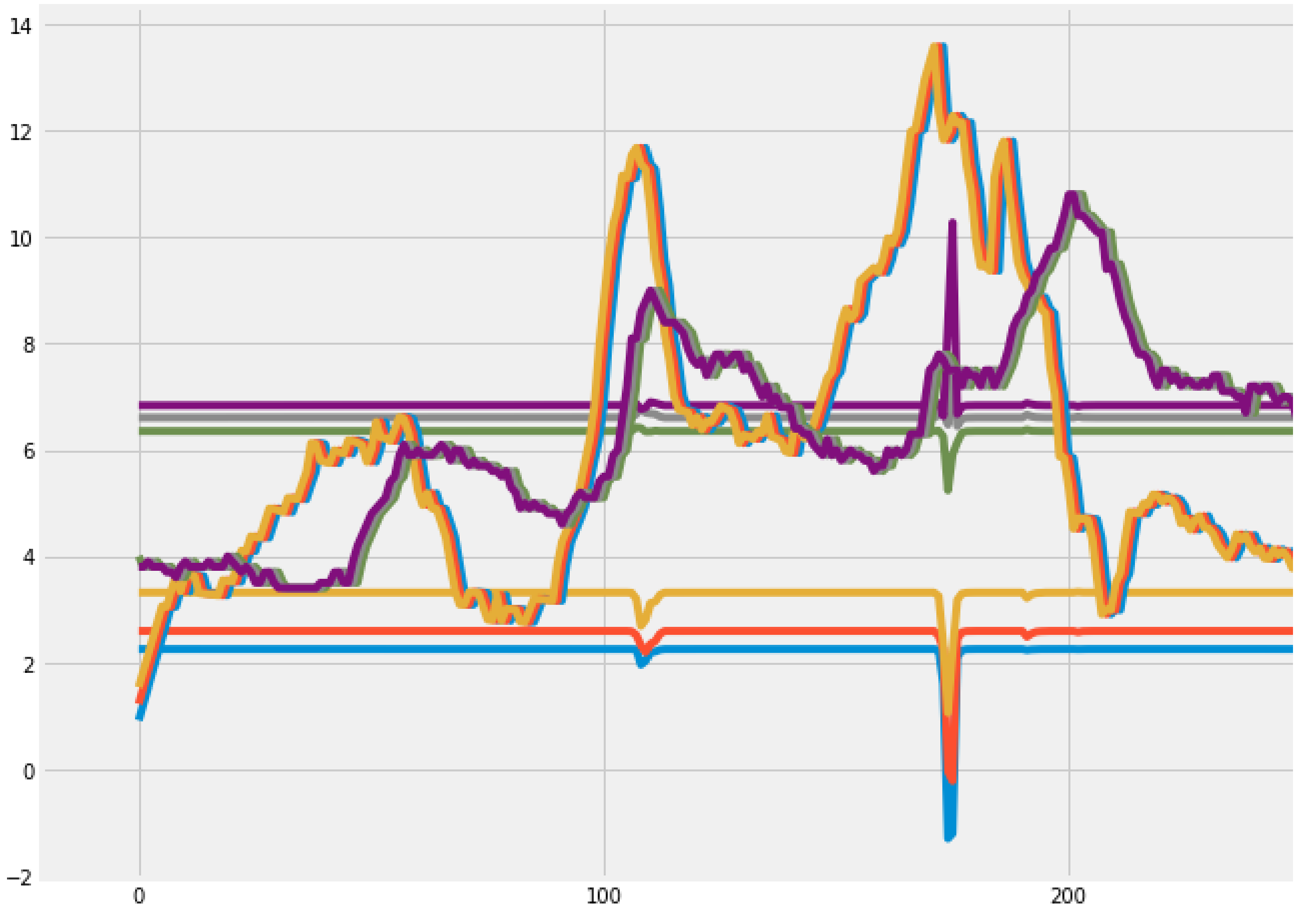

```
  2%|▌         | 2/128 [00:00<00:06, 19.26it/s]Epoch 41
100%|██████████| 128/128 [00:04<00:00, 29.63it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.59it/s]Epoch 42
100%|██████████| 128/128 [00:04<00:00, 30.28it/s]
  3%|▎         | 4/128 [00:00<00:03, 32.75it/s]Epoch 43
100%|██████████| 128/128 [00:04<00:00, 30.83it/s]
  3%|▎         | 4/128 [00:00<00:03, 32.29it/s]Epoch 44
100%|██████████| 128/128 [00:04<00:00, 32.71it/s]
  3%|▎         | 4/128 [00:00<00:03, 32.79it/s]Epoch 45
100%|██████████| 128/128 [00:04<00:00, 28.47it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.92it/s]Epoch 46
100%|██████████| 128/128 [00:04<00:00, 30.41it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.85it/s]Epoch 47
100%|██████████| 128/128 [00:04<00:00, 29.80it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.54it/s]Epoch 48
100%|██████████| 128/128 [00:04<00:00, 30.91it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.64it/s]Epoch 49
100%|██████████| 128/128 [00:04<00:00, 29.83it/s]
  2%|▌         | 3/128 [00:00<00:04, 29.82it/s]Epoch 50
100%|██████████| 128/128 [00:04<00:00, 29.02it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.06it/s]Epoch 51
100%|██████████| 128/128 [00:04<00:00, 28.55it/s]
  2%|▌         | 3/128 [00:00<00:04, 28.80it/s]Epoch 52
```

```
  2%|▏         | 3/128 [00:00<00:04, 28.80it/s]Epoch 52
100%|██████████| 128/128 [00:04<00:00, 29.09it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.35it/s]Epoch 53
100%|██████████| 128/128 [00:04<00:00, 29.70it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.59it/s]Epoch 54
100%|██████████| 128/128 [00:04<00:00, 30.46it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.65it/s]Epoch 55
100%|██████████| 128/128 [00:04<00:00, 30.19it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.88it/s]Epoch 56
100%|██████████| 128/128 [00:04<00:00, 29.89it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.61it/s]Epoch 57
100%|██████████| 128/128 [00:04<00:00, 30.19it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.45it/s]Epoch 58
100%|██████████| 128/128 [00:04<00:00, 30.63it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.55it/s]Epoch 59
100%|██████████| 128/128 [00:04<00:00, 30.14it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.68it/s]Epoch 60
100%|██████████| 128/128 [00:04<00:00, 29.85it/s]
```



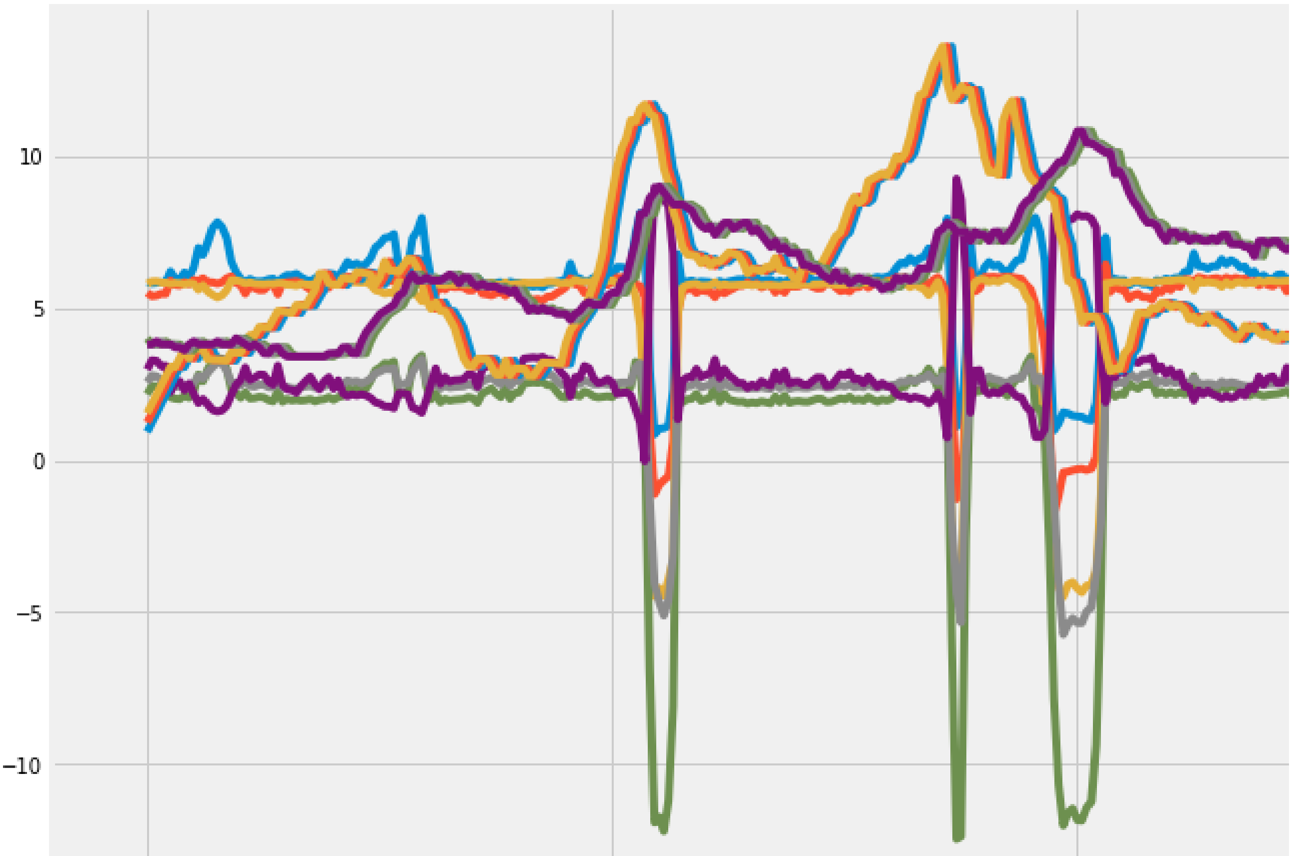

```
  2%|▏         | 2/128 [00:00<00:06, 19.16it/s]Epoch 61
100%|██████████| 128/128 [00:04<00:00, 30.38it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.39it/s]Epoch 62
100%|██████████| 128/128 [00:04<00:00, 29.60it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.60it/s]Epoch 63
100%|██████████| 128/128 [00:04<00:00, 29.58it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.27it/s]Epoch 64
100%|██████████| 128/128 [00:04<00:00, 30.06it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.11it/s]Epoch 65
100%|██████████| 128/128 [00:04<00:00, 30.36it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.81it/s]Epoch 66
100%|██████████| 128/128 [00:04<00:00, 30.15it/s]
  3%|▎         | 4/128 [00:00<00:03, 32.00it/s]Epoch 67
100%|██████████| 128/128 [00:04<00:00, 30.40it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.03it/s]Epoch 68
100%|██████████| 128/128 [00:04<00:00, 29.16it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.40it/s]Epoch 69
```

```
100%|██████████| 128/128 [00:04<00:00, 28.71it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.61it/s]Epoch 70
100%|██████████| 128/128 [00:04<00:00, 30.25it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.97it/s]Epoch 71
100%|██████████| 128/128 [00:04<00:00, 29.77it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.25it/s]Epoch 72
100%|██████████| 128/128 [00:04<00:00, 29.83it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.63it/s]Epoch 73
100%|██████████| 128/128 [00:04<00:00, 29.61it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.55it/s]Epoch 74
100%|██████████| 128/128 [00:04<00:00, 29.75it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.34it/s]Epoch 75
100%|██████████| 128/128 [00:04<00:00, 28.44it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.63it/s]Epoch 76
100%|██████████| 128/128 [00:04<00:00, 29.48it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.93it/s]Epoch 77
100%|██████████| 128/128 [00:04<00:00, 29.92it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.83it/s]Epoch 78
100%|██████████| 128/128 [00:04<00:00, 29.52it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.81it/s]Epoch 79
100%|██████████| 128/128 [00:04<00:00, 29.02it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.71it/s]Epoch 80
100%|██████████| 128/128 [00:04<00:00, 28.87it/s]
```




```
  2%|▏         | 3/128 [00:00<00:05, 24.81it/s]Epoch 81
100%|██████████| 128/128 [00:04<00:00, 29.22it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.41it/s]Epoch 82
100%|██████████| 128/128 [00:04<00:00, 29.89it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.14it/s]Epoch 83
100%|██████████| 128/128 [00:04<00:00, 29.72it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.89it/s]Epoch 84
100%|██████████| 128/128 [00:04<00:00, 30.30it/s]
  3%|▎         | 4/128 [00:00<00:03, 33.79it/s]Epoch 85
100%|██████████| 128/128 [00:04<00:00, 29.43it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.43it/s]Epoch 86
```

```
100%|██████████| 128/128 [00:04<00:00, 30.24it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.16it/s]Epoch 87
100%|██████████| 128/128 [00:04<00:00, 29.39it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.31it/s]Epoch 88
100%|██████████| 128/128 [00:04<00:00, 30.50it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.11it/s]Epoch 89
100%|██████████| 128/128 [00:04<00:00, 31.16it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.89it/s]Epoch 90
100%|██████████| 128/128 [00:04<00:00, 30.44it/s]
  3%|▎         | 4/128 [00:00<00:04, 29.90it/s]Epoch 91
100%|██████████| 128/128 [00:04<00:00, 30.20it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.57it/s]Epoch 92
100%|██████████| 128/128 [00:04<00:00, 29.56it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.85it/s]Epoch 93
100%|██████████| 128/128 [00:04<00:00, 30.54it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.71it/s]Epoch 94
100%|██████████| 128/128 [00:04<00:00, 29.20it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.58it/s]Epoch 95
100%|██████████| 128/128 [00:04<00:00, 29.72it/s]
  2%|▏         | 3/128 [00:00<00:04, 27.01it/s]Epoch 96
100%|██████████| 128/128 [00:04<00:00, 29.18it/s]
  3%|▎         | 4/128 [00:00<00:04, 30.88it/s]Epoch 97
100%|██████████| 128/128 [00:04<00:00, 30.39it/s]
  3%|▎         | 4/128 [00:00<00:03, 31.04it/s]Epoch 98
100%|██████████| 128/128 [00:04<00:00, 30.20it/s]
  2%|▏         | 3/128 [00:00<00:04, 29.26it/s]Epoch 99
100%|██████████| 128/128 [00:04<00:00, 30.30it/s]
  2%|▏         | 3/128 [00:00<00:04, 28.76it/s]Epoch 100
100%|██████████| 128/128 [00:04<00:00, 30.81it/s]
```



Data Analysis

- **Our LSTM generator is not pre-trained**, which means **The GAN model** get results as good as the previous models, but **this experimental model shows p**

- The GAN model successfully learned the correct range.
- **The GAN model learns the most drastic characteristics of the data**. I

Part III Conclusions and Next steps

Conclusions

In this project on analyzing and forecasting the US macro data we managed to accomplish the fol

- **Statistical analysis in Part I**
  - Basic manipulation: read the file, find null values and set index and some column plott
  - Correlation analysis: compute different correlations and use to to validate our choice c
  - Time series analysis with `ARIMA`: grid search for optimal parameters and train the ARII
- **Build 3 Deep learning models from basic one to advanced one in Par**
  - Basic model: single-step, single-feature forecasting with LSTM
  - Generalized model: multi-step, multi-feature forcasting with LSTM
  - Advanced model: Generative Adversarial Network (GAN) with LSTM and CNN.

Along the way, we find several remarkable patterns and features of our data

- Features show **long-period seasonality**.
- **Several features show apparent correlations**.
- **Most features slightly leads the Inflation feature**.
- The GAN model successfully learned the correct range.
- **The GAN model learns the most drastic characteristics of the data**.

Next steps

The USMacroData is not a big dataset, the following are a few furthur steps that we have done bu directions we can try to investigate:

- It's natural to **include the target feature itself into consideration**, because i most relevant to the future value of the feature itself. It can be easily achieved by modifying
- Investigate the difference between the first thirty years and the last twenty years.
- **Pre-train the LSTM model in the GAN model. In this way, the mod**
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