Hospital Readmission sample solution

This chunk reads in the data, relevels factors, and prints a summary.

```
# Loading data
readmission <- read.csv(file="readmission.csv")

vars <- colnames(readmission)[c(2,3,5,9)] #variables to relevel
for (i in vars){
  table <- as.data.frame(table(readmission[,i]))
  max <- which.max(table[,2])
  level.name <- as.character(table[max,1])
  readmission[,i] <- relevel(readmission[,i], ref = level.name)
}
summary(readmission)

## Readmission.Status Gender Race ER</pre>
```

```
F:38011
## Min.
          :0.0000
                                White
                                        :56124
                                                 Min.
                                                        :0.0000
## 1st Qu.:0.0000
                      M:28771
                                Black
                                        : 7099
                                                 1st Qu.:0.0000
## Median :0.0000
                                Hispanic: 1286
                                                 Median :0.0000
          :0.1259
## Mean
                                Others : 2273
                                                 Mean
                                                        :0.5083
## 3rd Qu.:0.0000
                                                 3rd Qu.:1.0000
## Max.
          :1.0000
                                                 Max.
                                                        :9.0000
##
     DRG.Class
                        LOS
                                                     HCC.Riskscore
                                         Age
##
  MED
          :35771
                   Min. : 1.000
                                    Min. : 24.00
                                                     Min.
                                                           : 0.079
   SURG
          :30447
                   1st Qu.: 3.000
                                    1st Qu.: 67.00
                                                     1st Qu.: 1.107
   UNGROUP: 564
                   Median : 5.000
                                    Median : 75.00
##
                                                     Median : 1.865
##
                   Mean
                          : 6.693
                                    Mean
                                          : 73.64
                                                     Mean
                                                           : 2.345
##
                   3rd Qu.: 8.000
                                    3rd Qu.: 83.00
                                                     3rd Qu.: 3.173
##
                          :36.000
                                    Max. :101.00
                   Max.
                                                     Max.
                                                            :12.307
##
        DRG.Complication
##
   MedicalMCC.CC:18110
## MedicalNoC
              :12310
## Other
                : 9345
## SurgMCC.CC
                :15468
##
   SurgNoC
                :11549
##
```

Task 1

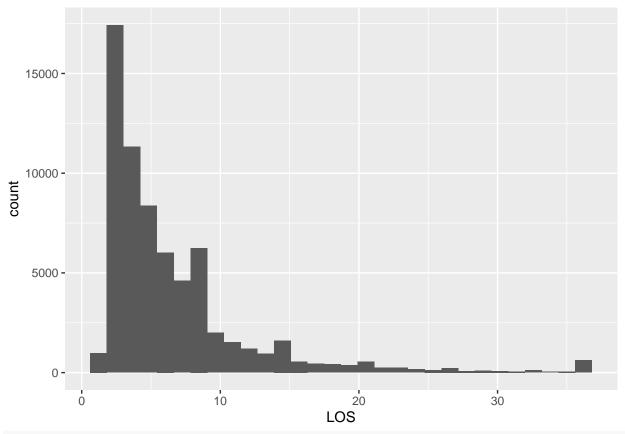
I have elected to make a table for ER and histograms for the other three variables.

```
library(ggplot2)
```

```
## Warning: replacing previous import by 'rlang:::=' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::.data' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::as_label' when loading
## 'dplyr'
## Warning: replacing previous import by 'rlang::as_name' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::dots_n' when loading 'dplyr'
```

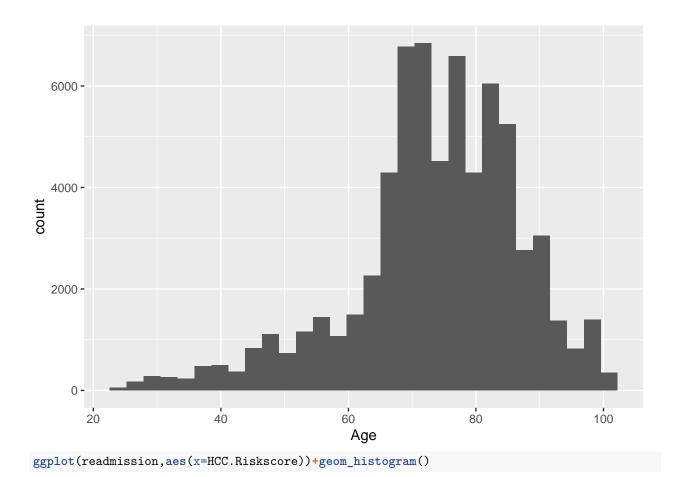
```
## Warning: replacing previous import by 'rlang::enquo' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::enquos' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::expr' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::sym' when loading 'dplyr'
## Warning: replacing previous import by 'rlang::syms' when loading 'dplyr'
table(readmission$ER)
##
                                     5
##
                         3
                               4
                                           6
                                                 7
                                                       9
## 43086 16280 5286 1572
                                   105
                                                       2
                             438
ggplot(readmission,aes(x=LOS))+geom_histogram()
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

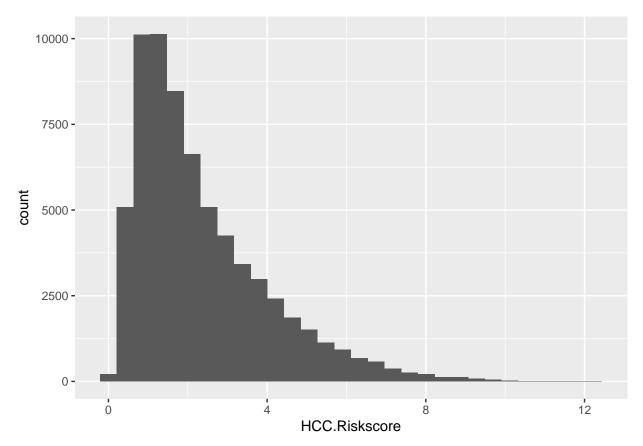


ggplot(readmission,aes(x=Age))+geom_histogram()

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



I will use log transformations of the LOS and HCC. Riskscore variables. I also create an indicator variables for those under age 65. The following chunk does these.

```
#two log transforms and removal of original variables
readmission$logLOS <- log(readmission$LOS)
readmission$logRiskscore <- log(readmission$HCC.Riskscore)
readmission$LOS <- NULL
readmission$HCC.Riskscore <- NULL
readmission$Under65 <- ifelse(readmission$Age < 65, 1, 0)
summary(readmission)</pre>
```

```
Readmission.Status Gender
                                          Race
                                                            ER
    Min.
            :0.0000
                        F:38011
                                                             :0.0000
##
                                   White
                                            :56124
                                                     Min.
##
    1st Qu.:0.0000
                        M:28771
                                   Black
                                            : 7099
                                                     1st Qu.:0.0000
    Median :0.0000
##
                                   Hispanic: 1286
                                                     Median :0.0000
##
            :0.1259
                                   Others : 2273
                                                             :0.5083
    Mean
                                                     Mean
##
    3rd Qu.:0.0000
                                                     3rd Qu.:1.0000
##
    Max.
            :1.0000
                                                     Max.
                                                             :9.0000
##
      DRG.Class
                                             DRG.Complication
                                                                   logLOS
                           Age
    MED
                                       MedicalMCC.CC:18110
##
            :35771
                             : 24.00
                                                                       :0.000
                     Min.
                                                               Min.
##
    SURG
            :30447
                     1st Qu.: 67.00
                                       MedicalNoC
                                                      :12310
                                                               1st Qu.:1.099
##
    UNGROUP: 564
                     Median : 75.00
                                       Other
                                                      : 9345
                                                               Median :1.609
##
                            : 73.64
                                       SurgMCC.CC
                                                      :15468
                                                                       :1.653
                     Mean
                                                               Mean
##
                     3rd Qu.: 83.00
                                       SurgNoC
                                                      :11549
                                                               3rd Qu.:2.079
##
                             :101.00
                     Max.
                                                               Max.
                                                                       :3.584
##
     logRiskscore
                          Under65
##
    Min.
            :-2.5383
                       Min.
                               :0.0000
    1st Qu.: 0.1017
                       1st Qu.:0.0000
```

```
## Median: 0.6235 Median: 0.0000
## Mean: 0.5999 Mean: 0.1684
## 3rd Qu:: 1.1547 3rd Qu:: 0.0000
## Max: 2.5102 Max: :1.0000
```

Readmission.Status Gender

:0.0000

F:38005

Min.

Task 2

This chunk creates a tabular view of the two variables.

```
table(readmission $DRG.Class, readmission $DRG.Complication)
##
##
             MedicalMCC.CC MedicalNoC Other SurgMCC.CC SurgNoC
##
     MED
                      18104
                                  12310
                                         5357
                                                        0
                                                                 0
##
     SURG
                          6
                                      0
                                         3424
                                                    15468
                                                             11549
     UNGROUP
                          0
                                      0
                                          564
                                                        0
                                                                 0
##
Six items will be deleted and the two existing variables recoded as a single factor variable. The following
code does that.
readmission.new <- readmission #preserve the original data until the work can be checked
readmission.new <- readmission.new[!(readmission.new$DRG.Complication=="MedicalMCC.CC" & readmission.ne
readmission.new DRG <- ifelse(readmission.new DRG.Complication == "Medical MCC.CC", "Med.C",
                        ifelse(readmission.new$DRG.Complication=="MedicalNoC","Med.NoC",
                                ifelse(readmission.new$DRG.Complication=="SurgMCC.CC", "Surg.C",
                                       ifelse(readmission.new$DRG.Complication=="SurgNoC", "Surg.NoC",
                                               ifelse(readmission.new$DRG.Class=="UNGROUP","UNGROUP",
                                                      ifelse(readmission.new$DRG.Complication=="Other"&rea
readmission.new$DRG <- as.factor(readmission.new$DRG)</pre>
table(readmission.new$DRG)
##
##
       Med.C
               Med.NoC
                         OtherMED OtherSURG
                                                 Surg.C
                                                         Surg.NoC
                                                                     UNGROUP
##
       18104
                  12310
                             5357
                                                  15468
                                        3424
                                                            11549
                                                                         564
readmission.new$DRG.Class <- NULL
readmission.new$DRG.Complication <- NULL
Relevel the new variable.
table <- as.data.frame(table(readmission.new[,"DRG"]))
  max <- which.max(table[,2])</pre>
  level.name <- as.character(table[max,1])</pre>
  readmission.new[,"DRG"] <- relevel(readmission.new[,"DRG"], ref = level.name)
table(readmission.new$DRG)
##
##
       Med.C
               Med.NoC OtherMED OtherSURG
                                                 Surg.C
                                                         Surg.NoC
                                                                     UNGROUP
##
       18104
                  12310
                             5357
                                        3424
                                                  15468
                                                             11549
                                                                         564
Accept the new dataframe by renaming it back to readmission.
readmission <- readmission.new
readmission.new <- NULL
summary(readmission)
```

:56120

FR

:0.0000

Min.

Race

White

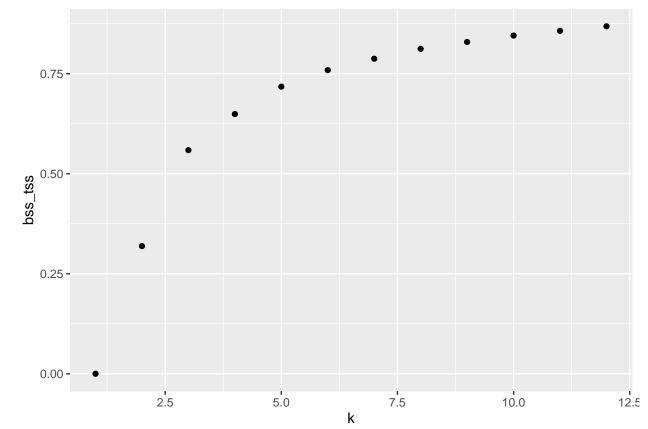
```
1st Qu.:0.0000
                        M:28771
                                  Black
                                          : 7097
                                                    1st Qu.:0.0000
    Median :0.0000
                                  Hispanic: 1286
##
                                                    Median :0.0000
                                  Others : 2273
    Mean
           :0.1259
                                                    Mean
                                                           :0.5083
   3rd Qu.:0.0000
                                                    3rd Qu.:1.0000
##
##
    Max.
           :1.0000
                                                    Max.
                                                            :9.0000
##
##
                          logLOS
                                       logRiskscore
                                                             Under65
         Age
##
    Min.
          : 24.00
                     Min.
                             :0.000
                                      Min.
                                              :-2.5383
                                                         Min.
                                                                 :0.0000
##
    1st Qu.: 67.00
                      1st Qu.:1.099
                                      1st Qu.: 0.1017
                                                         1st Qu.:0.0000
##
    Median : 75.00
                      Median :1.609
                                      Median : 0.6238
                                                         Median :0.0000
    Mean
          : 73.64
                      Mean
                             :1.653
                                      Mean
                                             : 0.6000
                                                         Mean
                                                                 :0.1684
    3rd Qu.: 83.00
                      3rd Qu.:2.079
                                      3rd Qu.: 1.1547
##
                                                         3rd Qu.:0.0000
                                      Max.
##
    Max.
           :101.00
                      Max.
                             :3.584
                                            : 2.5102
                                                                 :1.0000
                                                         Max.
##
##
           DRG
##
   {\tt Med.C}
             :18104
##
    Med.NoC :12310
    OtherMED: 5357
  OtherSURG: 3424
##
   Surg.C
            :15468
##
    Surg.NoC:11549
  UNGROUP: 564
```

Task 3

This code performs cluster analysis for from 1 to 12 clusters and constructs an elbow plot.

```
nstart.val <- 20
cluster_vars <- readmission[c('logLOS','Age')]</pre>
for(i in 1:ncol(cluster_vars)){
  cluster_vars[,i] <- scale(cluster_vars[,i])</pre>
}
km1 <- kmeans(cluster_vars,centers=1,nstart=nstart.val)</pre>
km2 <- kmeans(cluster_vars,centers=2,nstart=nstart.val)</pre>
km3 <- kmeans(cluster_vars,centers=3,nstart=nstart.val)</pre>
km4 <- kmeans(cluster_vars,centers=4,nstart=nstart.val)</pre>
km5 <- kmeans(cluster_vars,centers=5,nstart=nstart.val)</pre>
km6 <- kmeans(cluster_vars,centers=6,nstart=nstart.val)</pre>
km7 <- kmeans(cluster_vars,centers=7,nstart=nstart.val)</pre>
km8 <- kmeans(cluster vars,centers=8,nstart=nstart.val)
km9 <- kmeans(cluster_vars,centers=9,nstart=nstart.val)</pre>
km10 <- kmeans(cluster vars,centers=10,nstart=nstart.val)
km11 <- kmeans(cluster_vars,centers=11,nstart=nstart.val)</pre>
km12 <- kmeans(cluster_vars,centers=12,nstart=nstart.val)</pre>
var.exp \leftarrow data.frame(k = c(1:12),
                        bss_tss = c(km1$betweenss/km1$totss,
                                     km2$betweenss/km2$totss,
                                     km3$betweenss/km3$totss,
                                     km4$betweenss/km4$totss,
                                     km5$betweenss/km5$totss,
                                     km6$betweenss/km6$totss,
                                     km7$betweenss/km7$totss,
                                     km8$betweenss/km8$totss,
```

```
km9$betweenss/km9$totss,
km10$betweenss/km10$totss,
km11$betweenss/km11$totss,
km12$betweenss/km12$totss))
ggplot(var.exp,aes(x=k,y=bss_tss))+geom_point()
```

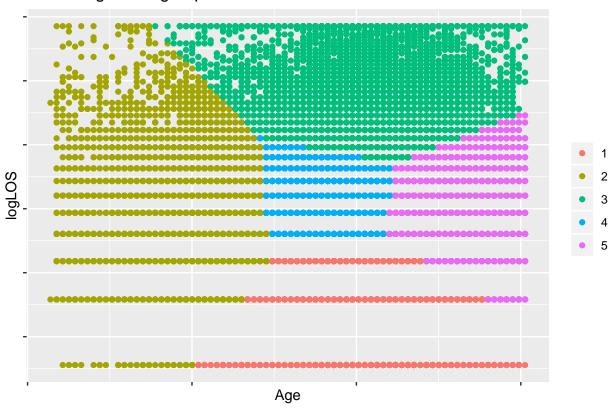


The following chunk creates the new variable based on 5 clusters.

```
LOS_Age_Clust <- as.factor(km5$cluster) #This creates a new variable based on having 5 clusters.

cluster_vars$LOS_Age_Clust <- LOS_Age_Clust
ggplot(data = cluster_vars, aes(x = Age, y = logLOS, col = LOS_Age_Clust)) + geom_point() + theme(axis.
```

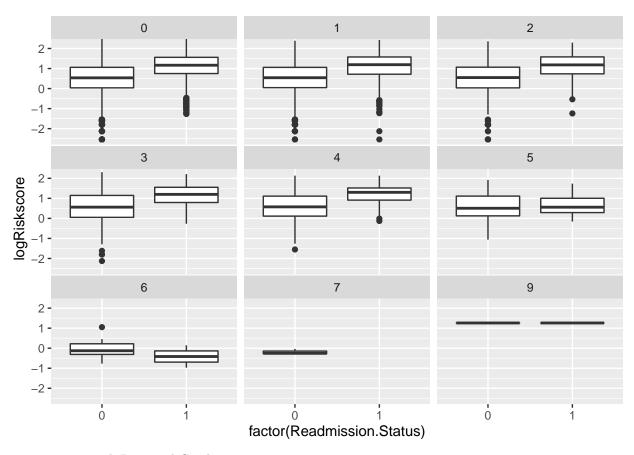
Clustering with 5 groups



Task 4

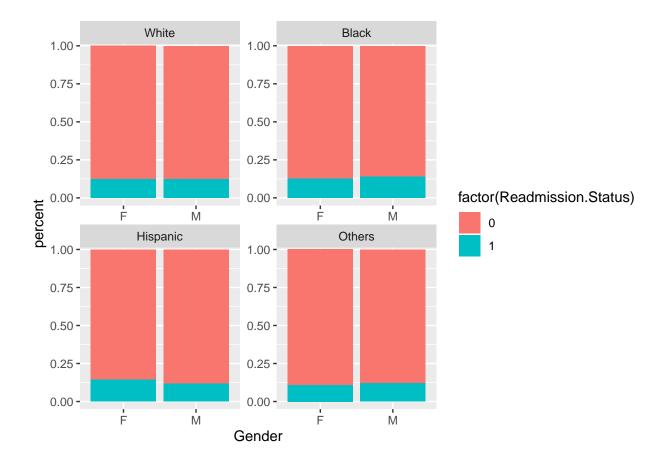
My first look is at ER and logRiskscore.

ggplot(readmission,aes(x=factor(Readmission.Status),y=logRiskscore)) + geom_boxplot() +facet_wrap(~fact



Trying again with Race and Gender.

```
ggplot(readmission,aes(Gender,fill=factor(Readmission.Status))) + geom_bar(position = "fill") +
  facet_wrap(~Race,ncol=2,scales="free")+scale_y_continuous()+ylab("percent")
```



Before fitting a GLM, I will split the data into training and test sets.

Task 5

```
#Create train and test sets
library(caret)
```

```
## Loading required package: lattice
## Warning: replacing previous import by 'rlang::!!' when loading 'recipes'
## Warning: replacing previous import by 'rlang::as_character' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::call2' when loading 'recipes'
## Warning: replacing previous import by 'rlang::exec' when loading 'recipes'
## Warning: replacing previous import by 'rlang::expr' when loading 'recipes'
## Warning: replacing previous import by 'rlang::f_lhs' when loading 'recipes'
## Warning: replacing previous import by 'rlang::f_rhs' when loading 'recipes'
## Warning: replacing previous import by 'rlang::is_empty' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::is_quosure' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::is_quosure' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::is_quosure' when loading
```

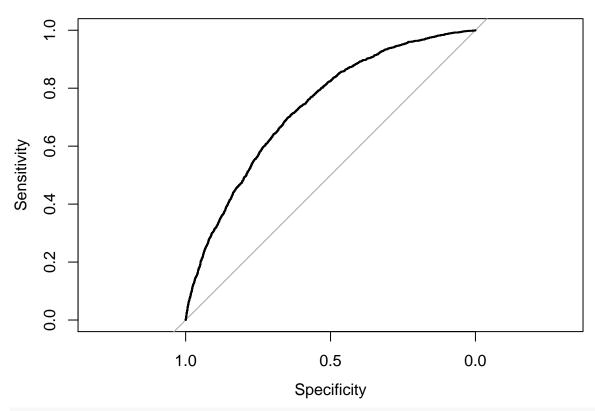
```
## 'recipes'
## Warning: replacing previous import by 'rlang::names2' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::quo' when loading 'recipes'
## Warning: replacing previous import by 'rlang::quo get expr' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::quo_squash' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::quo_text' when loading
## 'recipes'
## Warning: replacing previous import by 'rlang::quos' when loading 'recipes'
## Warning: replacing previous import by 'rlang::sym' when loading 'recipes'
## Warning: replacing previous import by 'rlang::syms' when loading 'recipes'
## Warning: replacing previous import by 'tibble::tibble' when loading
## 'recipes'
## Warning: replacing previous import by 'plyr::ddply' when loading 'caret'
## Warning: replacing previous import by 'recipes::all_outcomes' when loading
## 'caret'
## Warning: replacing previous import by 'recipes::all_predictors' when
## loading 'caret'
## Warning: replacing previous import by 'recipes::bake' when loading 'caret'
## Warning: replacing previous import by 'recipes::has_role' when loading
## 'caret'
## Warning: replacing previous import by 'recipes::juice' when loading 'caret'
## Warning: replacing previous import by 'recipes::prep' when loading 'caret'
set.seed(4321)
partition <- createDataPartition(readmission[,1], list = FALSE, p = .75) #The partition will stratify u
train <- readmission[partition, ]</pre>
test <- readmission[-partition, ]</pre>
print("TRAIN")
## [1] "TRAIN"
mean(train$Readmission.Status)
## [1] 0.1269518
print("TEST")
## [1] "TEST"
mean(test$Readmission.Status)
## [1] 0.1228585
```

I will now run a glm using the binomial distribution and logit link and add the desired interaction.

```
library(pROC)
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
      cov, smooth, var
glmlogit <- glm(Readmission.Status ~ . + Gender*Race, data=train, family = binomial(link="logit"))</pre>
summary(glmlogit)
##
## Call:
## glm(formula = Readmission.Status ~ . + Gender * Race, family = binomial(link = "logit"),
##
      data = train)
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -1.3460 -0.5643 -0.3911 -0.2544
                                       3.0541
##
## Coefficients:
##
                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                       -2.603997
                                   0.136923 -19.018 < 2e-16 ***
## GenderM
                                   0.031186 -0.697 0.48575
                       -0.021739
## RaceBlack
                        0.050490
                                   0.059038
                                             0.855 0.39244
## RaceHispanic
                        0.142477
                                   0.129136
                                            1.103 0.26989
## RaceOthers
                                   0.113611 -1.124 0.26112
                       -0.127669
## ER
                       -0.005826
                                   0.017218 -0.338 0.73508
                                   0.001617 -4.598 4.26e-06 ***
## Age
                       -0.007438
## logLOS
                                            3.214 0.00131 **
                       0.065528
                                   0.020390
## logRiskscore
                       1.330490
                                   0.023717 56.100 < 2e-16 ***
## Under65
                                   0.057945 -1.119 0.26314
                       -0.064840
## DRGMed.NoC
                       -0.040421
                                   0.042587 -0.949 0.34254
                                   0.054738 2.291 0.02195 *
## DRGOtherMED
                        0.125416
## DRGOtherSURG
                        0.103201
                                   0.065984
                                            1.564 0.11781
                                             0.187 0.85184
## DRGSurg.C
                        0.007461
                                   0.039946
## DRGSurg.NoC
                       -0.010876
                                   0.043732 -0.249 0.80360
## DRGUNGROUP
                        0.134489
                                   0.139704
                                            0.963 0.33571
                                             0.041 0.96706
## GenderM:RaceBlack
                        0.003736
                                   0.090470
## GenderM:RaceHispanic -0.321541
                                   0.213049 -1.509 0.13124
## GenderM:RaceOthers
                        0.237410
                                   0.158452
                                            1.498 0.13405
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33955 on 50063 degrees of freedom
## AIC: 33993
```

Number of Fisher Scoring iterations: 5

```
predslogit <- predict(glmlogit,newdat=test,type="response")</pre>
roclogit <- roc(test$Readmission.Status,predslogit)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
confusionMatrix(factor(1*(predslogit>.5)),factor(test$Readmission.Status))
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                  0
            0 14630 2042
##
##
            1
                 13
##
##
                  Accuracy : 0.8769
##
                    95% CI: (0.8718, 0.8818)
##
       No Information Rate: 0.8771
##
       P-Value [Acc > NIR] : 0.5434
##
##
                     Kappa : 0.0061
##
    Mcnemar's Test P-Value : <2e-16
##
##
##
               Sensitivity: 0.999112
##
               Specificity: 0.004388
            Pos Pred Value: 0.877519
##
            Neg Pred Value: 0.409091
##
                Prevalence : 0.877141
##
##
            Detection Rate: 0.876363
##
      Detection Prevalence: 0.998682
##
         Balanced Accuracy: 0.501750
##
          'Positive' Class : 0
##
##
plot(roclogit)
```



auc(roclogit)

library(pROC)

logLOS

logRiskscore

Area under the curve: 0.7324

The same code is now run with the probit link.

```
glmprobit <- glm(Readmission.Status ~ . + Gender*Race, data=train, family = binomial(link="probit"))</pre>
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ . + Gender * Race, family = binomial(link = "probit"),
##
       data = train)
##
## Deviance Residuals:
                 1Q
                      Median
                                    3Q
           -0.5756 -0.3944
##
  -1.2689
                              -0.2384
                                         3.2478
##
## Coefficients:
##
                          Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                    0.0741325 -19.387
                        -1.4371865
                                                       < 2e-16 ***
## GenderM
                        -0.0138744
                                    0.0168726
                                               -0.822
                                                        0.41090
## RaceBlack
                                                        0.46050
                         0.0237364
                                    0.0321619
                                                 0.738
## RaceHispanic
                         0.0763654
                                    0.0711823
                                                 1.073
                                                        0.28335
## RaceOthers
                        -0.0712955
                                    0.0606013 -1.176
                                                       0.23941
## ER
                        -0.0025486
                                    0.0093214
                                                -0.273 0.78454
## Age
                        -0.0045131
                                    0.0008786
                                                -5.137 2.79e-07 ***
```

3.060 0.00221 **

0.0124659 57.126 < 2e-16 ***

0.0112270

0.0343572

0.7121243

```
## Under65
                       -0.0408896 0.0314227 -1.301 0.19316
## DRGMed.NoC
                       ## DRGOtherMED
                        0.0679331 0.0298657
                                              2.275 0.02293 *
## DRGOtherSURG
                        0.0540437
                                   0.0362048
                                               1.493
                                                     0.13551
## DRGSurg.C
                        0.0086575
                                   0.0215849
                                              0.401
                                                     0.68835
## DRGSurg.NoC
                       -0.0045170 0.0236140 -0.191
                                                     0.84830
## DRGUNGROUP
                                              0.905
                        0.0704562 0.0778915
                                                     0.36571
## GenderM:RaceBlack
                        0.0159955
                                   0.0493390
                                              0.324
                                                     0.74579
## GenderM:RaceHispanic -0.1665655
                                   0.1147644 -1.451
                                                     0.14668
## GenderM:RaceOthers
                        0.1305341 0.0854834
                                               1.527 0.12676
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 38117
                            on 50081 degrees of freedom
## Residual deviance: 33928 on 50063 degrees of freedom
## AIC: 33966
## Number of Fisher Scoring iterations: 5
predsprobit <- predict(glmprobit,newdat=test,type="response")</pre>
rocprobit <- roc(test$Readmission.Status,predsprobit)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
confusionMatrix(factor(1*(predsprobit>.5)),factor(test$Readmission.Status))
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction
                 0
           0 14638 2048
##
##
           1
                 5
##
##
                 Accuracy: 0.877
##
                   95% CI : (0.8719, 0.882)
##
      No Information Rate: 0.8771
##
      P-Value [Acc > NIR] : 0.5247
##
##
                    Kappa : 0.002
##
##
   Mcnemar's Test P-Value : <2e-16
##
##
              Sensitivity: 0.999659
##
              Specificity: 0.001463
##
           Pos Pred Value: 0.877262
##
           Neg Pred Value: 0.375000
##
               Prevalence: 0.877141
##
           Detection Rate: 0.876842
##
     Detection Prevalence: 0.999521
##
        Balanced Accuracy: 0.500561
##
```

```
## 'Positive' Class: 0

Plot(rocprobit)

0.0

0.0

0.0

1.0

0.5

Specificity
```

Area under the curve: 0.7324

Task 6

auc(rocprobit)

A new dataframe is created that drops logLOS and Age and adds LOS_Age_Clust. It must then be partitioned.

```
readmission.cluster <- readmission</pre>
readmission.cluster$Age <- NULL</pre>
readmission.cluster$logLOS <- NULL</pre>
readmission.cluster$LOS_Age_Clust <- LOS_Age_Clust</pre>
table(readmission.cluster$LOS_Age_Clust)
##
##
              2
                     3
                            4
        1
                                   5
## 14231
          7640 10811 18296 15798
train.cluster <- readmission.cluster[partition, ]</pre>
test.cluster <- readmission.cluster[-partition, ]</pre>
```

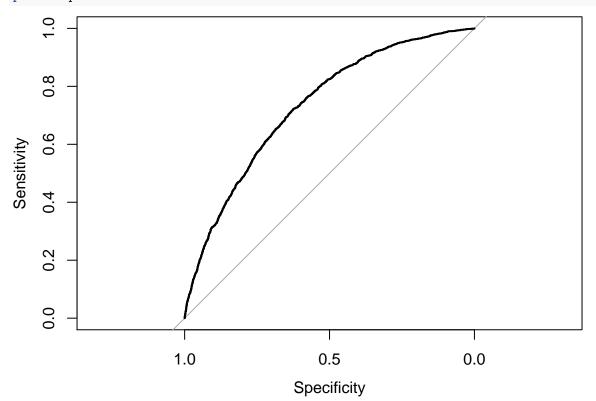
This code reruns the probit regression using the cluster variable.

```
library(pROC)
glmprobit.clust <- glm(Readmission.Status ~ . + Gender*Race, data=train.cluster, family = binomial(link)</pre>
```

```
summary(glmprobit.clust)
##
## Call:
  glm(formula = Readmission.Status ~ . + Gender * Race, family = binomial(link = "probit"),
##
       data = train.cluster)
##
## Deviance Residuals:
      Min
                 1Q
                      Median
                                   3Q
                                           Max
## -1.2352 -0.5764 -0.3958 -0.2390
                                        3.2774
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                        -1.764757
                                    0.025668 -68.754 < 2e-16 ***
## GenderM
                        -0.009280
                                    0.016857
                                             -0.551 0.581972
## RaceBlack
                         0.029904
                                    0.032122
                                               0.931 0.351880
                                               1.147 0.251238
## RaceHispanic
                         0.081615
                                    0.071134
## RaceOthers
                        -0.064763
                                    0.060541
                                             -1.070 0.284736
## ER
                        -0.002681
                                    0.009317 -0.288 0.773505
## logRiskscore
                         0.708164
                                    0.012367 57.262 < 2e-16 ***
## Under65
                         0.078550
                                    0.033476
                                               2.346 0.018954 *
## DRGMed.NoC
                        -0.021906
                                    0.023018 -0.952 0.341244
## DRGOtherMED
                         0.069296
                                    0.029842
                                              2.322 0.020229 *
## DRGOtherSURG
                         0.056222
                                    0.036180
                                              1.554 0.120192
## DRGSurg.C
                         0.007818
                                    0.021579
                                               0.362 0.717132
## DRGSurg.NoC
                        -0.004116
                                    0.023607 -0.174 0.861582
## DRGUNGROUP
                         0.072082
                                    0.077943
                                              0.925 0.355068
## LOS_Age_Clust2
                         0.030645
                                    0.042490
                                               0.721 0.470763
## LOS_Age_Clust3
                         0.083453
                                    0.025226
                                               3.308 0.000939 ***
## LOS_Age_Clust4
                                               2.150 0.031541 *
                         0.050077
                                    0.023290
## LOS_Age_Clust5
                         0.004006
                                    0.023922
                                               0.167 0.867013
## GenderM:RaceBlack
                         0.014296
                                    0.049321
                                               0.290 0.771932
## GenderM:RaceHispanic -0.164691
                                    0.114652 -1.436 0.150875
## GenderM:RaceOthers
                                    0.085419
                         0.128235
                                               1.501 0.133291
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33948 on 50061 degrees of freedom
## AIC: 33990
## Number of Fisher Scoring iterations: 5
predsprobit.clust <- predict(glmprobit.clust,newdat=test.cluster,type="response")</pre>
rocprobit.clust <- roc(test.cluster$Readmission.Status,predsprobit.clust)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
confusionMatrix(factor(1*(predsprobit.clust>.5)),factor(test.cluster$Readmission.Status))
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                  0
            0 14639
                     2049
##
##
            1
##
                  Accuracy: 0.877
##
##
                    95% CI : (0.8719, 0.882)
       No Information Rate : 0.8771
##
##
       P-Value [Acc > NIR] : 0.5247
##
##
                     Kappa : 0.0012
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.9997268
               Specificity: 0.0009751
##
##
            Pos Pred Value : 0.8772172
            Neg Pred Value: 0.3333333
##
##
                Prevalence : 0.8771415
##
            Detection Rate: 0.8769019
##
      Detection Prevalence: 0.9996406
##
         Balanced Accuracy: 0.5003510
##
##
          'Positive' Class: 0
##
```

plot(rocprobit.clust)



```
auc(rocprobit.clust)
```

Area under the curve: 0.7321

Task 7

1

```
The first step is to binarize the factor levels that have more than two levels. fullRank is set to FALSE so that
all levels get binarized. The interaction variable is also a factor variable and must be binarized as well. In
each case the base level will then need to be deleted. I do it this way becasue if fullRank is TRUE I can't be
sure about which level becomes the base.
#Add the interaction variable to the data frame
readmission $\fraceGender <- factor(paste0(readmission $\fraceRace, readmission $\fraceGender))
summary(readmission$RaceGender)
##
      BlackF
                  BlackM HispanicF HispanicM
                                                   OthersF
                                                               OthersM
                                                                            WhiteF
##
         4157
                    2940
                                 751
                                            535
                                                       1206
                                                                  1067
                                                                             31891
##
      WhiteM
        24229
##
factor_names <- c("Race", "DRG", "RaceGender")</pre>
factor_vars <- readmission[,factor_names]</pre>
for (var in factor_names) {
  factor_vars[, var] <- as.character(factor_vars[, var])</pre>
}
binarizer <- caret::dummyVars(paste("~", paste(factor_names, collapse = "+")) , data = factor_vars, ful
binarized_vars <- data.frame(predict(binarizer, newdata = factor_vars))</pre>
head(binarized_vars)
##
     RaceBlack RaceHispanic RaceOthers RaceWhite DRGMed.C DRGMed.NoC
## 1
              0
                              0
                                          0
                                                      1
                                                                0
## 2
              0
                              0
                                          0
                                                      1
                                                                0
                                                                             0
## 3
                              0
                                                                0
              0
                                          0
                                                      1
                                                                             0
## 4
              0
                              0
                                          0
                                                      1
                                                                0
                                                                             1
## 5
              0
                              0
                                          0
                                                      1
                                                                             1
## 6
              0
                              0
                                          0
                                                      1
                                                                0
                                                                             0
     DRGOtherMED DRGOtherSURG DRGSurg.C DRGSurg.NoC DRGUNGROUP
##
## 1
                                0
                                           0
                                                         0
                                                                      0
                 1
## 2
                 0
                                0
                                           0
                                                         1
                                                                      0
                 0
                                0
                                                                      0
## 3
                                           0
                                                         1
## 4
                 0
                                0
                                           0
                                                         0
                                                                      0
## 5
                 0
                                0
                                           Λ
                                                         0
                                                                      0
## 6
                 0
                                0
                                                                      0
##
     RaceGenderBlackF RaceGenderBlackM RaceGenderHispanicF
## 1
                      0
                                          0
## 2
                      0
                                          0
                                                                 0
                                          0
                                                                 0
## 3
                      0
## 4
                      0
                                          0
                                                                 0
## 5
                      0
                                          0
                                                                 0
## 6
                      0
                                          0
```

RaceGenderOthersF RaceGenderOthersM RaceGenderWhiteF

```
## 2
                          0
                                                0
                                                                     0
                                                                                         0
## 3
                          0
                                               0
                                                                     0
                                                                                         0
                                                                                         0
## 4
                           0
                                               0
                                                                     0
                          0
                                               0
                                                                     0
                                                                                         0
## 5
## 6
                                               0
                                                                     0
                                                                                         0
##
     RaceGenderWhiteM
## 1
## 2
## 3
                       1
## 4
                       1
## 5
                       1
## 6
                       1
```

Now delete the three base variables.

```
binarized_vars$RaceWhite <- NULL
binarized_vars$DRGMed.C <- NULL
binarized_vars$RaceGenderWhiteF <- NULL
head(binarized_vars)</pre>
```

```
RaceBlack RaceHispanic RaceOthers DRGMed.NoC DRGOtherMED DRGOtherSURG
##
## 1
              0
                             0
                                          0
                                                      0
                                                                                   0
                                                                    1
              0
                             0
                                          0
                                                      0
                                                                                   0
## 2
                                                                    0
## 3
              0
                             0
                                          0
                                                      0
                                                                                   0
                                                                    0
                             0
## 4
              0
                                          0
                                                      1
                                                                    0
                                                                                   0
## 5
                             0
                                          0
                                                                    0
                                                                                   0
              0
                                                      1
## 6
              0
                             0
                                          0
                                                      0
                                                                    0
##
     DRGSurg.C DRGSurg.NoC DRGUNGROUP RaceGenderBlackF RaceGenderBlackM
## 1
              0
                            0
                                         0
## 2
              0
                            1
                                         0
                                                            0
                                                                                0
## 3
              0
                            1
                                         0
                                                            0
                                                                                0
## 4
              0
                            0
                                         0
                                                            0
                                                                                0
## 5
              0
                            0
                                         0
                                                            0
                                                                                0
## 6
                            0
                                        0
                                                            0
                                                                                0
              1
     RaceGenderHispanicF RaceGenderHispanicM RaceGenderOthersF
## 1
                          0
                                                 0
                                                                     0
## 2
                          0
                                                 0
                                                                     0
                          0
                                                 0
                                                                     0
## 3
## 4
                          0
                                                 0
                                                                     0
                          0
## 5
                                                 0
                                                                     0
                          0
## 6
                                                                     0
##
     RaceGenderOthersM RaceGenderWhiteM
## 1
                       0
                                           1
## 2
                       0
                                           1
## 3
                       0
                                           1
                       0
## 4
                                           1
## 5
                       0
                                           1
## 6
                        0
                                           1
```

I now attach the binarized variables and remove the three original factor variables. A new dataframe is created so the old one is preserved.

```
readmission.bin <- cbind(readmission, binarized_vars)
readmission.bin$Race <- NULL
readmission.bin$RaceGender <- NULL</pre>
```

summary(readmission.bin)

```
##
    Readmission.Status Gender
                                          ER
                                                           Age
##
    Min.
           :0.0000
                        F:38005
                                           :0.0000
                                                             : 24.00
                                   Min.
                                                     Min.
##
    1st Qu.:0.0000
                        M:28771
                                   1st Qu.:0.0000
                                                     1st Qu.: 67.00
##
    Median :0.0000
                                   Median :0.0000
                                                     Median: 75.00
##
    Mean
            :0.1259
                                   Mean
                                           :0.5083
                                                     Mean
                                                             : 73.64
##
    3rd Qu.:0.0000
                                   3rd Qu.:1.0000
                                                     3rd Qu.: 83.00
                                           :9.0000
           :1.0000
                                   Max.
                                                             :101.00
##
    Max.
                                                     Max.
##
        logLOS
                      logRiskscore
                                            Under65
                                                             RaceBlack
##
    Min.
            :0.000
                     Min.
                             :-2.5383
                                        Min.
                                                :0.0000
                                                           Min.
                                                                  :0.0000
##
    1st Qu.:1.099
                     1st Qu.: 0.1017
                                         1st Qu.:0.0000
                                                           1st Qu.:0.0000
##
    Median :1.609
                     Median: 0.6238
                                         Median :0.0000
                                                           Median :0.0000
##
    Mean
            :1.653
                             : 0.6000
                                         Mean
                                                :0.1684
                                                           Mean
                                                                  :0.1063
                     Mean
                     3rd Qu.: 1.1547
##
    3rd Qu.:2.079
                                         3rd Qu.:0.0000
                                                           3rd Qu.:0.0000
##
    Max.
            :3.584
                     Max.
                             : 2.5102
                                         Max.
                                                :1.0000
                                                           Max.
                                                                  :1.0000
##
     RaceHispanic
                         RaceOthers
                                             DRGMed.NoC
                                                              DRGOtherMED
            :0.0000
                               :0.00000
##
    Min.
                       Min.
                                           Min.
                                                  :0.0000
                                                             Min.
                                                                     :0.00000
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.0000
                                                             1st Qu.:0.00000
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.0000
                                                             Median :0.00000
##
    Mean
            :0.01926
                       Mean
                               :0.03404
                                           Mean
                                                  :0.1843
                                                             Mean
                                                                     :0.08022
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.0000
                                                             3rd Qu.:0.00000
                               :1.00000
                                                                     :1.00000
##
    Max.
            :1.00000
                       Max.
                                           Max.
                                                  :1.0000
                                                             Max.
##
     DRGOtherSURG
                         DRGSurg.C
                                           DRGSurg.NoC
                                                             DRGUNGROUP
##
    Min.
            :0.00000
                       Min.
                               :0.0000
                                                 :0.000
                                                                   :0.00000
                                                           1st Qu.:0.000000
##
    1st Qu.:0.00000
                       1st Qu.:0.0000
                                          1st Qu.:0.000
##
    Median : 0.00000
                       Median : 0.0000
                                          Median : 0.000
                                                           Median :0.000000
##
    Mean
            :0.05128
                       Mean
                               :0.2316
                                          Mean
                                                 :0.173
                                                           Mean
                                                                   :0.008446
##
    3rd Qu.:0.00000
                       3rd Qu.:0.0000
                                          3rd Qu.:0.000
                                                           3rd Qu.:0.000000
##
                                                                   :1.000000
    Max.
            :1.00000
                               :1.0000
                                                 :1.000
                                                           Max.
                       Max.
                                          Max.
##
    RaceGenderBlackF
                       RaceGenderBlackM
                                           RaceGenderHispanicF
##
    Min.
            :0.00000
                       Min.
                               :0.00000
                                           Min.
                                                  :0.00000
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                           1st Qu.:0.00000
##
##
    Median :0.00000
                       Median :0.00000
                                           Median :0.00000
##
    Mean
            :0.06225
                       Mean
                               :0.04403
                                           Mean
                                                  :0.01125
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                           3rd Qu.:0.00000
##
    Max.
            :1.00000
                       Max.
                               :1.00000
                                           Max.
                                                  :1.00000
##
    RaceGenderHispanicM RaceGenderOthersF RaceGenderOthersM RaceGenderWhiteM
            :0.000000
##
    Min.
                         Min.
                                 :0.00000
                                             Min.
                                                     :0.00000
                                                                Min.
                                                                        :0.0000
                         1st Qu.:0.00000
##
    1st Qu.:0.000000
                                             1st Qu.:0.00000
                                                                1st Qu.:0.0000
##
    Median :0.000000
                         Median :0.00000
                                             Median :0.00000
                                                                Median :0.0000
##
    Mean
            :0.008012
                         Mean
                                 :0.01806
                                             Mean
                                                     :0.01598
                                                                Mean
                                                                        :0.3628
                                             3rd Qu.:0.00000
                                                                3rd Qu.:1.0000
##
    3rd Qu.:0.000000
                         3rd Qu.:0.00000
##
    Max.
            :1.000000
                         Max.
                                 :1.00000
                                             Max.
                                                     :1.00000
                                                                Max.
                                                                        :1.0000
```

I need to again split the data into train and test sets.

```
train.bin <- readmission.bin[partition, ]
test.bin <- readmission.bin[-partition, ]</pre>
```

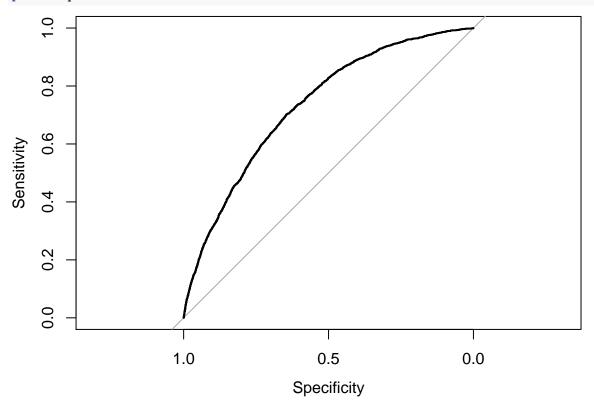
I next run the GLM on the binarized data. In doing so, I recognized that the interaction variable created combinations that were redundant. I need to remove all the interactions with male and then re-partition the data.

```
readmission.bin$RaceGenderOthersM <- NULL
readmission.bin$RaceGenderWhiteM <- NULL
readmission.bin$RaceGenderHispanicM <- NULL
readmission.bin$RaceGenderBlackM <- NULL
summary(readmission.bin)
##
    Readmission.Status Gender
                                         ER
                                                          Age
##
    Min.
           :0.0000
                        F:38005
                                   Min.
                                          :0.0000
                                                     Min.
                                                            : 24.00
                                   1st Qu.:0.0000
    1st Qu.:0.0000
                        M:28771
                                                     1st Qu.: 67.00
##
##
    Median :0.0000
                                   Median :0.0000
                                                     Median: 75.00
##
    Mean
           :0.1259
                                   Mean
                                          :0.5083
                                                     Mean
                                                            : 73.64
##
    3rd Qu.:0.0000
                                   3rd Qu.:1.0000
                                                     3rd Qu.: 83.00
##
    Max.
           :1.0000
                                   Max.
                                          :9.0000
                                                     Max.
                                                            :101.00
##
        logLOS
                                           Under65
                                                            RaceBlack
                      logRiskscore
                                                                 :0.0000
##
           :0.000
                            :-2.5383
                                               :0.0000
    Min.
                     Min.
                                        Min.
                                                          Min.
    1st Qu.:1.099
                     1st Qu.: 0.1017
                                        1st Qu.:0.0000
                                                          1st Qu.:0.0000
##
    Median :1.609
                     Median: 0.6238
                                        Median :0.0000
                                                          Median :0.0000
##
    Mean
           :1.653
                     Mean
                            : 0.6000
                                        Mean
                                               :0.1684
                                                          Mean
                                                                  :0.1063
                     3rd Qu.: 1.1547
                                                          3rd Qu.:0.0000
##
    3rd Qu.:2.079
                                        3rd Qu.:0.0000
##
    Max.
           :3.584
                     Max.
                            : 2.5102
                                        Max.
                                               :1.0000
                                                          Max.
                                                                  :1.0000
##
     RaceHispanic
                         RaceOthers
                                            DRGMed.NoC
                                                             DRGOtherMED
##
    Min.
           :0.00000
                       Min.
                              :0.00000
                                          Min.
                                                  :0.0000
                                                            Min.
                                                                    :0.00000
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                          1st Qu.:0.0000
                                                            1st Qu.:0.00000
    Median :0.00000
                       Median :0.00000
                                          Median :0.0000
                                                            Median :0.00000
##
    Mean
           :0.01926
                       Mean
                              :0.03404
                                          Mean
                                                  :0.1843
                                                            Mean
                                                                    :0.08022
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                          3rd Qu.:0.0000
                                                            3rd Qu.:0.00000
##
    Max.
           :1.00000
                       Max.
                              :1.00000
                                          Max.
                                                  :1.0000
                                                            Max.
                                                                    :1.00000
##
     DRGOtherSURG
                         DRGSurg.C
                                          DRGSurg.NoC
                                                            DRGUNGROUP
##
    Min.
           :0.00000
                       Min.
                              :0.0000
                                                 :0.000
                                                          Min.
                                                                  :0.000000
                                         1st Qu.:0.000
##
    1st Qu.:0.00000
                       1st Qu.:0.0000
                                                          1st Qu.:0.000000
    Median :0.00000
                       Median :0.0000
                                         Median :0.000
                                                          Median :0.000000
##
   Mean
           :0.05128
                       Mean
                              :0.2316
                                         Mean
                                                :0.173
                                                          Mean
                                                                  :0.008446
                       3rd Qu.:0.0000
                                         3rd Qu.:0.000
##
    3rd Qu.:0.00000
                                                          3rd Qu.:0.000000
##
    Max.
           :1.00000
                              :1.0000
                                                 :1.000
                                                                  :1.000000
                       Max.
                                         Max.
                                                          Max.
    RaceGenderBlackF
                       RaceGenderHispanicF RaceGenderOthersF
##
  Min.
           :0.00000
                       Min.
                              :0.00000
                                            Min.
                                                    :0.00000
##
    1st Qu.:0.00000
                       1st Qu.:0.00000
                                            1st Qu.:0.00000
##
   Median :0.00000
                       Median :0.00000
                                            Median :0.00000
    Mean
           :0.06225
                       Mean
                              :0.01125
                                            Mean
                                                    :0.01806
##
    3rd Qu.:0.00000
                       3rd Qu.:0.00000
                                            3rd Qu.:0.00000
   Max.
           :1.00000
                       Max.
                              :1.00000
                                                    :1.00000
                                            Max.
train.bin <- readmission.bin[partition, ]</pre>
test.bin <- readmission.bin[-partition, ]</pre>
glmprobit <- glm(Readmission.Status ~ . , data=train.bin, family = binomial(link="probit"))</pre>
summary(glmprobit)
##
## Call:
  glm(formula = Readmission.Status ~ ., family = binomial(link = "probit"),
##
       data = train.bin)
##
## Deviance Residuals:
```

```
Median
##
                 1Q
                                   3Q
                    -0.3944 -0.2384
## -1.2689 -0.5756
                                        3.2478
##
## Coefficients:
##
                         Estimate Std. Error z value Pr(>|z|)
                       -1.4371865 0.0741325 -19.387
                                                      < 2e-16 ***
## (Intercept)
## GenderM
                                             -0.822
                       -0.0138744 0.0168726
                                                      0.41090
## ER
                       -0.0025486 0.0093214
                                              -0.273
                                                     0.78454
## Age
                       -0.0045131 0.0008786
                                              -5.137 2.79e-07 ***
## logLOS
                        0.0343572 0.0112270
                                               3.060 0.00221 **
## logRiskscore
                        0.7121243 0.0124659
                                              57.126 < 2e-16 ***
## Under65
                       -0.0408896 0.0314227
                                             -1.301 0.19316
## RaceBlack
                        0.0397319 0.0378371
                                               1.050 0.29368
                                             -1.001 0.31698
## RaceHispanic
                       -0.0902001 0.0901389
## RaceOthers
                        0.0592385 0.0603545
                                               0.982
                                                     0.32634
## DRGMed.NoC
                       -0.0216338 0.0230263
                                              -0.940
                                                      0.34746
## DRGOtherMED
                                               2.275 0.02293 *
                        0.0679331 0.0298657
## DRGOtherSURG
                        0.0540437 0.0362048
                                               1.493 0.13551
## DRGSurg.C
                                               0.401 0.68835
                        0.0086575 0.0215849
## DRGSurg.NoC
                       -0.0045170 0.0236140
                                              -0.191
                                                      0.84830
## DRGUNGROUP
                        0.0704562 0.0778915
                                               0.905 0.36571
## RaceGenderBlackF
                                              -0.324 0.74579
                       -0.0159955 0.0493390
## RaceGenderHispanicF 0.1665655 0.1147644
                                               1.451
                                                      0.14668
## RaceGenderOthersF
                       -0.1305341 0.0854834
                                             -1.527 0.12676
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 38117
                             on 50081 degrees of freedom
## Residual deviance: 33928 on 50063 degrees of freedom
## AIC: 33966
##
## Number of Fisher Scoring iterations: 5
predsprobit <- predict(glmprobit,newdat=test.bin,type="response")</pre>
rocprobit <- roc(test.bin$Readmission.Status,predsprobit)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
confusionMatrix(factor(1*(predsprobit>.5)),factor(test.bin$Readmission.Status))
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction
                  0
                        1
##
            0 14638
                     2048
##
            1
                  5
                        3
##
##
                  Accuracy: 0.877
##
                    95% CI: (0.8719, 0.882)
##
      No Information Rate: 0.8771
##
       P-Value [Acc > NIR] : 0.5247
```

```
##
##
                     Kappa : 0.002
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.999659
##
##
               Specificity: 0.001463
            Pos Pred Value: 0.877262
##
##
            Neg Pred Value: 0.375000
                Prevalence: 0.877141
##
##
            Detection Rate: 0.876842
      Detection Prevalence: 0.999521
##
##
         Balanced Accuracy: 0.500561
##
##
          'Positive' Class : 0
##
```

plot(rocprobit)



auc(rocprobit)

```
## Area under the curve: 0.7324
```

The next step is to run stepAIC on this model.

```
library(MASS)
stepAIC(glmprobit)
```

```
## Start: AIC=33965.61
## Readmission.Status ~ Gender + ER + Age + logLOS + logRiskscore +
## Under65 + RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC +
```

```
##
      DRGOtherMED + DRGOtherSURG + DRGSurg.C + DRGSurg.NoC + DRGUNGROUP +
##
      RaceGenderBlackF + RaceGenderHispanicF + RaceGenderOthersF
##
                       Df Deviance
##
                                     AIC
## - DRGSurg.NoC
                        1
                             33928 33964
## - ER
                             33928 33964
                        1
## - RaceGenderBlackF
                           33928 33964
                        1
## - DRGSurg.C
                           33928 33964
                        1
## - Gender
                           33928 33964
                        1
## - DRGUNGROUP
                           33928 33964
                        1
## - DRGMed.NoC
                        1 33928 33964
                           33929 33965
## - RaceOthers
                        1
                           33929 33965
## - RaceHispanic
                        1
## - RaceBlack
                       1 33929 33965
## - Under65
                       1 33929 33965
## <none>
                             33928 33966
## - RaceGenderHispanicF 1
                           33930 33966
## - DRGOtherSURG
                           33930 33966
## - RaceGenderOthersF
                           33930 33966
                        1
                           33933 33969
## - DRGOtherMED
                        1
## - logLOS
                             33937 33973
                        1
## - Age
                           33954 33990
## - logRiskscore
                             37741 37777
                        1
## Step: AIC=33963.65
## Readmission.Status ~ Gender + ER + Age + logLOS + logRiskscore +
##
      Under65 + RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC +
      DRGOtherMED + DRGOtherSURG + DRGSurg.C + DRGUNGROUP + RaceGenderBlackF +
##
      RaceGenderHispanicF + RaceGenderOthersF
##
##
                       Df Deviance
## - ER
                        1
                             33928 33962
## - RaceGenderBlackF
                             33928 33962
## - DRGSurg.C
                             33928 33962
                        1
## - Gender
                        1
                             33928 33962
                           33929 33963
## - DRGUNGROUP
                        1
## - DRGMed.NoC
                        1 33929 33963
## - RaceOthers
                       1 33929 33963
                        1 33929 33963
## - RaceHispanic
## - RaceBlack
                       1 33929 33963
## - Under65
                       1 33929 33963
## <none>
                            33928 33964
## - RaceGenderHispanicF 1
                           33930 33964
## - RaceGenderOthersF 1
                           33930 33964
## - DRGOtherSURG
                        1 33930 33964
## - DRGOtherMED
                           33934 33968
                        1
## - logLOS
                        1
                             33937 33971
## - Age
                        1
                             33954 33988
## - logRiskscore
                             37742 37776
## Step: AIC=33961.73
## Readmission.Status ~ Gender + Age + logLOS + logRiskscore + Under65 +
      RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC + DRGOtherMED +
##
      DRGOtherSURG + DRGSurg.C + DRGUNGROUP + RaceGenderBlackF +
##
```

```
##
       RaceGenderHispanicF + RaceGenderOthersF
##
##
                         Df Deviance
                                       AIC
## - RaceGenderBlackF
                               33928 33960
                          1
## - DRGSurg.C
                               33928 33960
## - Gender
                               33928 33960
                          1
## - DRGUNGROUP
                          1
                            33929 33961
## - DRGMed.NoC
                          1
                              33929 33961
## - RaceOthers
                          1
                               33929 33961
## - RaceHispanic
                          1
                               33929 33961
## - RaceBlack
                          1
                               33929 33961
## - Under65
                               33929 33961
                          1
## <none>
                               33928 33962
## - RaceGenderHispanicF 1
                               33930 33962
## - RaceGenderOthersF
                               33930 33962
                          1
## - DRGOtherSURG
                          1
                               33930 33962
## - DRGOtherMED
                          1
                               33934 33966
## - logLOS
                          1
                               33937 33969
## - Age
                               33954 33986
                          1
## - logRiskscore
                               37742 37774
##
## Step: AIC=33959.83
## Readmission.Status ~ Gender + Age + logLOS + logRiskscore + Under65 +
       RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC + DRGOtherMED +
##
       DRGOtherSURG + DRGSurg.C + DRGUNGROUP + RaceGenderHispanicF +
##
       RaceGenderOthersF
##
                         Df Deviance
                                       AIC
## - DRGSurg.C
                               33928 33958
                         1
## - Gender
                          1
                               33928 33958
## - DRGUNGROUP
                          1
                               33929 33959
## - DRGMed.NoC
                          1
                               33929 33959
## - RaceOthers
                            33929 33959
## - RaceHispanic
                            33929 33959
                          1
## - RaceBlack
                          1
                               33929 33959
## - Under65
                          1
                               33930 33960
## <none>
                               33928 33960
## - RaceGenderHispanicF 1
                            33930 33960
## - RaceGenderOthersF
                          1
                               33930 33960
## - DRGOtherSURG
                               33930 33960
                          1
## - DRGOtherMED
                          1
                               33934 33964
                               33937 33967
## - logLOS
                          1
## - Age
                          1
                               33954 33984
## - logRiskscore
                          1
                               37742 37772
## Step: AIC=33958.11
## Readmission.Status ~ Gender + Age + logLOS + logRiskscore + Under65 +
##
       RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC + DRGOtherMED +
##
       DRGOtherSURG + DRGUNGROUP + RaceGenderHispanicF + RaceGenderOthersF
##
##
                         Df Deviance
                                       AIC
## - Gender
                         1
                            33929 33957
## - DRGUNGROUP
                          1
                               33929 33957
## - RaceOthers
                               33929 33957
```

```
## - RaceHispanic
                        1
                              33929 33957
## - DRGMed.NoC
                              33929 33957
                         1
## - RaceBlack
                              33930 33958
## - Under65
                              33930 33958
                         1
## <none>
                               33928 33958
## - RaceGenderHispanicF 1
                              33930 33958
## - RaceGenderOthersF
                            33930 33958
## - DRGOtherSURG
                              33930 33958
                         1
## - DRGOtherMED
                         1
                              33934 33962
## - logLOS
                         1
                              33937 33965
## - Age
                         1
                               33954 33982
## - logRiskscore
                               37742 37770
                         1
## Step: AIC=33956.68
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
##
       RaceBlack + RaceHispanic + RaceOthers + DRGMed.NoC + DRGOtherMED +
##
       DRGOtherSURG + DRGUNGROUP + RaceGenderHispanicF + RaceGenderOthersF
##
##
                        Df Deviance
                                      AIC
                              33929 33955
## - RaceOthers
                         1
## - DRGUNGROUP
                         1
                              33929 33955
## - RaceHispanic
                              33930 33956
## - DRGMed.NoC
                              33930 33956
                         1
## - RaceBlack
                         1
                              33930 33956
## - Under65
                              33930 33956
                         1
## - RaceGenderOthersF 1
                              33931 33957
## <none>
                               33929 33957
## - DRGOtherSURG
                               33931 33957
                         1
## - RaceGenderHispanicF 1
                               33931 33957
## - DRGOtherMED
                         1
                               33934 33960
## - logLOS
                          1
                               33938 33964
## - Age
                         1
                               33955 33981
## - logRiskscore
                               37743 37769
##
## Step: AIC=33955.42
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
##
      RaceBlack + RaceHispanic + DRGMed.NoC + DRGOtherMED + DRGOtherSURG +
##
      DRGUNGROUP + RaceGenderHispanicF + RaceGenderOthersF
##
##
                        Df Deviance
                                       AIC
## - DRGUNGROUP
                              33930 33954
                         1
## - RaceGenderOthersF
                               33931 33955
                         1
## - RaceHispanic
                               33931 33955
                         1
## - DRGMed.NoC
                               33931 33955
                         1
## - RaceBlack
                               33931 33955
                         1
## - Under65
                               33931 33955
                         1
## <none>
                               33929 33955
## - DRGOtherSURG
                              33932 33956
## - RaceGenderHispanicF
                               33932 33956
                        1
                               33935 33959
## - DRGOtherMED
                          1
## - logLOS
                              33939 33963
                         1
                              33956 33980
## - Age
## - logRiskscore
                        1
                              37743 37767
##
```

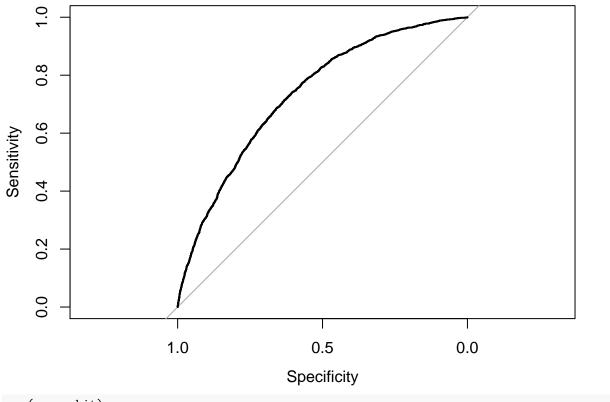
```
## Step: AIC=33954.19
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
      RaceBlack + RaceHispanic + DRGMed.NoC + DRGOtherMED + DRGOtherSURG +
##
      RaceGenderHispanicF + RaceGenderOthersF
##
##
                        Df Deviance
                                      AIC
## - RaceGenderOthersF
                        1 33931 33953
## - RaceHispanic
                              33931 33953
                         1
                            33932 33954
## - RaceBlack
                         1
## - DRGMed.NoC
                           33932 33954
                        1
## - Under65
                        1
                              33932 33954
                              33930 33954
## <none>
## - DRGOtherSURG
                              33932 33954
                         1
## - RaceGenderHispanicF 1
                           33933 33955
## - DRGOtherMED
                            33936 33958
                         1
## - logLOS
                         1
                             33940 33962
## - Age
                              33956 33978
                         1
## - logRiskscore
                              37747 37769
##
## Step: AIC=33953.39
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
      RaceBlack + RaceHispanic + DRGMed.NoC + DRGOtherMED + DRGOtherSURG +
      RaceGenderHispanicF
##
##
##
                        Df Deviance
                                      ATC
## - RaceHispanic
                        1
                              33933 33953
## - DRGMed.NoC
                              33933 33953
                         1
## - RaceBlack
                              33933 33953
                         1
## - Under65
                        1
                           33933 33953
## <none>
                              33931 33953
                           33934 33954
## - DRGOtherSURG
                         1
## - RaceGenderHispanicF 1
                            33934 33954
## - DRGOtherMED
                           33937 33957
## - logLOS
                              33941 33961
                         1
## - Age
                         1
                              33957 33977
## - logRiskscore
                         1
                              37749 37769
##
## Step: AIC=33952.59
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
      RaceBlack + DRGMed.NoC + DRGOtherMED + DRGOtherSURG + RaceGenderHispanicF
##
##
##
                        Df Deviance AIC
## - RaceGenderHispanicF 1
                              33934 33952
## - DRGMed.NoC
                              33934 33952
                         1
## - Under65
                              33934 33952
                         1
                              33934 33952
## - RaceBlack
                         1
## <none>
                              33933 33953
## - DRGOtherSURG
                            33935 33953
                         1
## - DRGOtherMED
                         1
                            33938 33956
## - logLOS
                         1
                              33942 33960
## - Age
                              33958 33976
                         1
                         1 37751 37769
## - logRiskscore
##
## Step: AIC=33951.95
```

```
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
      RaceBlack + DRGMed.NoC + DRGOtherMED + DRGOtherSURG
##
##
##
                 Df Deviance AIC
## - DRGMed.NoC
                  1
                       33935 33951
## - RaceBlack
                       33936 33952
                 1
## - Under65
                  1 33936 33952
                       33934 33952
## <none>
## - DRGOtherSURG 1
                       33936 33952
## - DRGOtherMED
                  1
                       33940 33956
## - logLOS
                  1
                       33943 33959
## - Age
                       33960 33976
                   1
## - logRiskscore 1
                       37754 37770
##
## Step: AIC=33951.46
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
##
       RaceBlack + DRGOtherMED + DRGOtherSURG
##
##
                 Df Deviance AIC
                       33937 33951
## - RaceBlack
                  1
## - Under65
                  1
                       33937 33951
## <none>
                       33935 33951
## - DRGOtherSURG 1
                       33938 33952
## - DRGOtherMED
                       33942 33956
                  1
## - logLOS
                   1
                       33945 33959
## - Age
                  1
                       33961 33975
## - logRiskscore 1
                       37754 37768
## Step: AIC=33951.02
## Readmission.Status ~ Age + logLOS + logRiskscore + Under65 +
      DRGOtherMED + DRGOtherSURG
##
##
##
                 Df Deviance
                               AIC
## - Under65
                       33938 33950
                  1
## <none>
                       33937 33951
## - DRGOtherSURG 1
                       33940 33952
## - DRGOtherMED
                  1
                       33944 33956
## - logLOS
                   1
                       33946 33958
## - Age
                   1
                       33964 33976
## - logRiskscore 1
                       37759 37771
## Step: AIC=33950.44
## Readmission.Status ~ Age + logLOS + logRiskscore + DRGOtherMED +
##
      DRGOtherSURG
##
                 Df Deviance
##
                               AIC
## <none>
                       33938 33950
## - DRGOtherSURG 1
                       33941 33951
## - DRGOtherMED
                  1
                       33945 33955
## - logLOS
                   1
                       33948 33958
## - Age
                       33981 33991
                   1
## - logRiskscore 1
                       37765 37775
##
```

```
## Call: glm(formula = Readmission.Status ~ Age + logLOS + logRiskscore +
##
       DRGOtherMED + DRGOtherSURG, family = binomial(link = "probit"),
##
       data = train.bin)
##
## Coefficients:
   (Intercept)
                                                             {\tt DRGOtherMED}
                                     logLOS logRiskscore
##
       -1.50930
                     -0.00371
                                    0.03436
                                                  0.71158
##
                                                                 0.07107
## DRGOtherSURG
##
        0.05586
##
## Degrees of Freedom: 50081 Total (i.e. Null); 50076 Residual
## Null Deviance:
                        38120
## Residual Deviance: 33940
                                AIC: 33950
The probit model is now run using the five surviving variables.
glmprobit <- glm(Readmission.Status ~ logLOS + Age + logRiskscore + DRGOtherSURG + DRGOtherMED, data=tr
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ logLOS + Age + logRiskscore +
       DRGOtherSURG + DRGOtherMED, family = binomial(link = "probit"),
##
##
       data = train.bin)
##
## Deviance Residuals:
##
       Min
                 10
                     Median
                                   30
                                           Max
## -1.2840 -0.5759 -0.3948 -0.2391
                                        3.2705
##
## Coefficients:
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.5092975 0.0469985 -32.114 < 2e-16 ***
## logLOS
                 0.0343635 0.0112216
                                        3.062
                                                0.0022 **
## Age
                -0.0037101 0.0005667
                                      -6.547 5.88e-11 ***
## logRiskscore 0.7115770 0.0124458
                                       57.174 < 2e-16 ***
## DRGOtherSURG 0.0558636 0.0341427
                                        1.636
                                                0.1018
## DRGOtherMED 0.0710677 0.0273260
                                        2.601
                                                0.0093 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33938 on 50076 degrees of freedom
## AIC: 33950
##
## Number of Fisher Scoring iterations: 5
predsprobit <- predict(glmprobit,newdat=test.bin,type="response")</pre>
rocprobit <- roc(test.bin$Readmission.Status,predsprobit)</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
```

confusionMatrix(factor(1*(predsprobit>.5)),factor(test.bin\$Readmission.Status)) ## Confusion Matrix and Statistics ## ## Reference ## Prediction 0 1 ## 0 14639 2047 1 4 ## ## ## Accuracy : 0.8771 95% CI : (0.8721, 0.8821) ## ## No Information Rate: 0.8771 ## P-Value [Acc > NIR] : 0.5059 ## ## Kappa: 0.0029 ## ## Mcnemar's Test P-Value : <2e-16 ## ## Sensitivity: 0.99973 ## Specificity: 0.00195 Pos Pred Value: 0.87732 ## ## Neg Pred Value : 0.50000 ## Prevalence: 0.87714 ## Detection Rate: 0.87690 Detection Prevalence: 0.99952 ## ## Balanced Accuracy: 0.50084 ## ## 'Positive' Class : 0

plot(rocprobit)



auc(rocprobit)

Area under the curve: 0.7334

Task 8

##

I first run the model on the full dataset.

data = readmission.bin)

```
glmprobit <- glm(Readmission.Status ~ logLOS + Age + logRiskscore + DRGOtherSURG + DRGOtherMED, data=re
summary(glmprobit)

##
## Call:
## glm(formula = Readmission.Status ~ logLOS + Age + logRiskscore +</pre>
```

```
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                           Max
                                   3Q
## -1.2680 -0.5747 -0.3952 -0.2421
                                        3.9745
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.5026235 0.0407530 -36.871 < 2e-16 ***
## logLOS
                0.0329948 0.0097365
                                        3.389 0.000702 ***
```

DRGOtherSURG + DRGOtherMED, family = binomial(link = "probit"),

logLus 0.0329948 0.0097365 3.389 0.000702 ***
Age -0.0036999 0.0004916 -7.526 5.25e-14 ***
logRiskscore 0.7008229 0.0107283 65.325 < 2e-16 ***
DRGOtherSURG 0.0560715 0.0293707 1.909 0.056250 .

```
0.0691546 0.0237996
                                         2.906 0.003664 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 50559 on 66775 degrees of freedom
## Residual deviance: 45116 on 66770 degrees of freedom
## AIC: 45128
##
## Number of Fisher Scoring iterations: 5
I now create some arbitrary patients to learn how changing the values affects the predicted probability of
readmission.
new.data \leftarrow data.frame("logLOS" = c(log(5),log(6),log(5),log(5),log(5),log(5)), "Age" = c(75,75,80,75,75,80,75,75)
new.data
       logLOS Age logRiskscore DRGOtherSURG DRGOtherMED
## 1 1.609438 75
                     0.6237971
## 2 1.791759
               75
                     0.6237971
                                           0
                                                        0
                                           0
                                                        0
## 3 1.609438 80
                     0.6237971
## 4 1.609438
               75
                     0.7193021
                                           0
                                                        0
## 5 1.609438
               75
                     0.6237971
                                                        0
                                           1
## 6 1.609438
                     0.6237971
              75
predict(glmprobit, newdat = new.data, type = "response")
##
## 0.09855331 0.09960192 0.09537932 0.11068247 0.10864481 0.11110281
```

Task 9

I rerun the model on the full dataset.

```
glmprobit <- glm(Readmission.Status ~ logLOS + Age + logRiskscore + DRGOtherSURG + DRGOtherMED, data=re
summary(glmprobit)
##
## Call:
  glm(formula = Readmission.Status ~ logLOS + Age + logRiskscore +
       DRGOtherSURG + DRGOtherMED, family = binomial(link = "probit"),
##
       data = readmission.bin)
## Deviance Residuals:
       Min
                 1Q
                     Median
                                           Max
## -1.2680 -0.5747 -0.3952 -0.2421
                                        3.9745
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.5026235 0.0407530 -36.871 < 2e-16 ***
                0.0329948 0.0097365
                                        3.389 0.000702 ***
## logLOS
                -0.0036999 0.0004916 -7.526 5.25e-14 ***
```

1.909 0.056250 .

logRiskscore 0.7008229 0.0107283 65.325 < 2e-16 ***

DRGOtherSURG 0.0560715 0.0293707

```
## DRGOtherMED
                 0.0691546 0.0237996
                                         2.906 0.003664 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 50559 on 66775 degrees of freedom
## Residual deviance: 45116 on 66770 degrees of freedom
## AIC: 45128
##
## Number of Fisher Scoring iterations: 5
predsprobit <- predict(glmprobit,newdat=readmission.bin,type="response")</pre>
confusionMatrix(factor(1*(predsprobit>.5)),factor(readmission.bin$Readmission.Status))
## Confusion Matrix and Statistics
##
             Reference
## Prediction
                  0
##
            0 58356
                     8399
##
                 11
##
##
                  Accuracy : 0.8741
                    95% CI: (0.8715, 0.8766)
##
##
       No Information Rate: 0.8741
##
       P-Value [Acc > NIR] : 0.5076
##
##
                     Kappa: 0.0017
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.999812
##
               Specificity: 0.001189
            Pos Pred Value: 0.874182
##
            Neg Pred Value: 0.476190
##
                Prevalence: 0.874072
##
            Detection Rate: 0.873907
##
      Detection Prevalence: 0.999686
##
##
         Balanced Accuracy: 0.500500
##
          'Positive' Class: 0
##
This code calculates the cost for different cutoff values. I ran it at different values and am presting the final
choice of 0.08.
```

```
cutoff <- 0.08
pred_readmit <- 1*(predsprobit > cutoff)
cm <- confusionMatrix(factor(pred_readmit),factor(readmission.bin$Readmission.Status))

no_intervention_cost <- 25*sum(readmission.bin$Readmission.Status == 1)
full_intervention_cost <- 2*nrow(readmission.bin)
modified_cost <- cm$table[2,1]*2+cm$table[2,2]*2+cm$table[1,2]*25
no_intervention_cost</pre>
```

```
## [1] 210225
full_intervention_cost
## [1] 133552
modified_cost
## [1] 106002
The final step is to get the confusion matrix.
## Confusion Matrix and Statistics
##
##
             Reference
                  0
## Prediction
                         1
##
            0 26379 1096
            1 31988 7313
##
##
##
                  Accuracy : 0.5046
##
                    95% CI: (0.5008, 0.5084)
##
       No Information Rate: 0.8741
       P-Value [Acc > NIR] : 1
##
##
##
                     Kappa : 0.125
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.4520
##
               Specificity: 0.8697
##
            Pos Pred Value: 0.9601
##
            Neg Pred Value: 0.1861
##
                Prevalence: 0.8741
##
            Detection Rate: 0.3950
##
      Detection Prevalence: 0.4115
         Balanced Accuracy: 0.6608
##
##
##
          'Positive' Class: 0
##
```

ALTERNATIVE FEATURE SELECTION

This section presents an alternative approach. It is based on using hypothesis tests to sequentially remove features. It begins by re-running the probit model on the training set using all the available features.

```
glmprobit <- glm(Readmission.Status ~ . + Race*Gender, data=train, family = binomial(link="probit"))
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ . + Race * Gender, family = binomial(link = "probit"),
## data = train)
##</pre>
```

```
## Deviance Residuals:
##
                      Median
       Min
                 10
                                    30
                                            Max
                              -0.2384
  -1.2689
           -0.5756 -0.3944
                                         3.2478
##
##
  Coefficients:
##
                           Estimate Std. Error z value Pr(>|z|)
                                     0.0741325 -19.387
## (Intercept)
                         -1.4371865
                                                         < 2e-16 ***
## GenderM
                         -0.0138744
                                     0.0168726
                                                -0.822
                                                         0.41090
## RaceBlack
                          0.0237364
                                     0.0321619
                                                  0.738
                                                         0.46050
## RaceHispanic
                          0.0763654
                                     0.0711823
                                                  1.073
                                                         0.28335
## RaceOthers
                         -0.0712955
                                     0.0606013
                                                 -1.176
                                                         0.23941
## ER
                         -0.0025486
                                     0.0093214
                                                 -0.273
                                                         0.78454
## Age
                         -0.0045131
                                     0.0008786
                                                 -5.137 2.79e-07 ***
## logLOS
                          0.0343572
                                     0.0112270
                                                  3.060
                                                         0.00221 **
## logRiskscore
                          0.7121243
                                     0.0124659
                                                 57.126
                                                         < 2e-16 ***
## Under65
                         -0.0408896
                                     0.0314227
                                                 -1.301
                                                         0.19316
## DRGMed.NoC
                                                 -0.940
                                                         0.34746
                         -0.0216338
                                     0.0230263
## DRGOtherMED
                          0.0679331
                                     0.0298657
                                                  2.275
                                                         0.02293 *
## DRGOtherSURG
                          0.0540437
                                     0.0362048
                                                  1.493
                                                         0.13551
## DRGSurg.C
                          0.0086575
                                     0.0215849
                                                  0.401
                                                         0.68835
## DRGSurg.NoC
                         -0.0045170
                                     0.0236140
                                                 -0.191
                                                         0.84830
## DRGUNGROUP
                                                  0.905
                          0.0704562
                                     0.0778915
                                                         0.36571
## GenderM:RaceBlack
                                     0.0493390
                                                  0.324
                                                         0.74579
                          0.0159955
## GenderM:RaceHispanic -0.1665655
                                     0.1147644
                                                 -1.451
                                                         0.14668
## GenderM:RaceOthers
                          0.1305341
                                     0.0854834
                                                  1.527
                                                         0.12676
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 38117
                              on 50081
                                        degrees of freedom
  Residual deviance: 33928
                              on 50063
                                        degrees of freedom
##
  AIC: 33966
##
## Number of Fisher Scoring iterations: 5
```

It is difficult to deal with a categorical interaction variable if the goal is to remove levels. With the interaction, there are actually 8 levels in play and they would need to be created as a new variable in order to merge some of them. Given that none of the three interaction terms appear to add value, I'll save time and go ahead and remove them.

```
glmprobit <- glm(Readmission.Status ~ ., data=train, family = binomial(link="probit"))
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ ., family = binomial(link = "probit"),</pre>
```

```
## Deviance Residuals:

## Min 1Q Median 3Q Max

## -1.2706 -0.5757 -0.3945 -0.2387 3.2499

##
```

Coefficients:

data = train)

##

##

```
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
              -1.4392073 0.0740620 -19.432 < 2e-16 ***
## GenderM
               -0.0107974 0.0154547 -0.699 0.48477
## RaceBlack
                0.0304827 0.0246611
                                      1.236 0.21644
## RaceHispanic 0.0102060 0.0557975
                                      0.183 0.85487
## RaceOthers
              -0.0067658 0.0427270 -0.158 0.87418
## ER
               -0.0025921 0.0093202 -0.278 0.78092
## Age
               -0.0045021 0.0008785
                                     -5.125 2.98e-07 ***
## logLOS
                0.0343042 0.0112250
                                      3.056 0.00224 **
## logRiskscore 0.7122625 0.0124642
                                     57.145 < 2e-16 ***
## Under65
               -0.0405129 0.0314153
                                     -1.290 0.19719
## DRGMed.NoC
                                     -0.958 0.33830
               -0.0220462 0.0230238
## DRGOtherMED
                0.0683215 0.0298592
                                      2.288 0.02213 *
## DRGOtherSURG 0.0531373 0.0362010
                                      1.468 0.14215
## DRGSurg.C
                                      0.388 0.69782
                0.0083802 0.0215833
## DRGSurg.NoC -0.0045720 0.0236071
                                     -0.194 0.84643
## DRGUNGROUP
                0.0678532 0.0778955
                                      0.871 0.38371
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 38117
                           on 50081 degrees of freedom
## Residual deviance: 33932 on 50066 degrees of freedom
## AIC: 33964
## Number of Fisher Scoring iterations: 5
```

Normally the next step would be combine Race-Others with Race-White (the base) but given the similarity to Race-Hispanic, both will be combined with Race-White. This is mostly done to save time.

```
readmission$RaceGender <- NULL #Need to remove this variable that was created earlier.
readmission2<-readmission
library(plyr)
var <- "Race"
var.levels <- levels(readmission2[,var])
readmission2[,var] <- mapvalues(readmission2[,var],var.levels,c("NonBlack","Black","NonBlack","NonBlack
#Relevel
table <- as.data.frame(table(readmission2[,var]))
    max <- which.max(table[,2])
    level.name <- as.character(table[max,1])
    readmission2[,var] <- relevel(readmission2[,var], ref = level.name)

table(readmission2[,var])
##</pre>
```

NonBlack Black ## 59679 7097

Running the model again, remembering to create new train and test sets. The same partition continues to be used to keep results consistent.

```
readmission <- readmission2
train <- readmission[partition,]
```

```
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ ., data=train, family = binomial(link="probit"))</pre>
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ ., family = binomial(link = "probit"),
       data = train)
##
## Deviance Residuals:
                     Median
                1Q
                                  3Q
                                          Max
## -1.2707 -0.5759 -0.3945 -0.2387
                                       3.2495
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.439477
                           0.073950 -19.465 < 2e-16 ***
               -0.010864
                           0.015453 -0.703 0.48201
## GenderM
## RaceBlack
               0.030502
                          0.024555
                                      1.242 0.21416
## ER
               -0.002584
                           0.009320 -0.277 0.78156
## Age
               -0.004499
                           0.000878
                                     -5.124 2.98e-07 ***
## logLOS
                0.034325
                           0.011224
                                      3.058 0.00223 **
## logRiskscore 0.712279 0.012464 57.147
                                            < 2e-16 ***
## Under65
               ## DRGMed.NoC
               -0.022075 0.023023 -0.959 0.33763
## DRGOtherMED 0.068353 0.029858
                                     2.289 0.02206 *
## DRGOtherSURG 0.053060 0.036199
                                     1.466 0.14271
## DRGSurg.C
                0.008356 0.021583
                                      0.387 0.69863
## DRGSurg.NoC -0.004598
                           0.023606 -0.195 0.84556
## DRGUNGROUP
                0.067814
                           0.077894
                                      0.871 0.38397
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117
##
                            on 50081 degrees of freedom
## Residual deviance: 33932 on 50068 degrees of freedom
## AIC: 33960
##
## Number of Fisher Scoring iterations: 5
For similar reasons, we simultaneously merge the two insignificant DRG levels into the base.
readmission2<-readmission
var <- "DRG"
var.levels <- levels(readmission2[,var])</pre>
readmission2[,var] <- mapvalues(readmission2[,var],var.levels,c("DRGbase","Med.NoC","OtherMED","OtherSU
#Relevel
table <- as.data.frame(table(readmission2[,var]))</pre>
  max <- which.max(table[,2])</pre>
  level.name <- as.character(table[max,1])</pre>
  readmission2[,var] <- relevel(readmission2[,var], ref = level.name)</pre>
table(readmission2[,var])
```

```
##
##
    DRGbase
              Med.NoC OtherMED OtherSURG
                                           UNGROUP
      45121
                12310
##
                           5357
                                     3424
                                               564
readmission <- readmission2</pre>
train <- readmission[partition,]</pre>
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ ., data=train, family = binomial(link="probit"))</pre>
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ ., family = binomial(link = "probit"),
##
      data = train)
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
## -1.2706 -0.5759 -0.3946 -0.2387
                                       3.2554
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.438216 0.073069 -19.683 < 2e-16 ***
## GenderM
               ## RaceBlack
               0.030546
                          0.024555
                                      1.244 0.21350
## ER
               -0.002595
                          0.009320 -0.278 0.78065
## Age
              -0.004493
                          0.000878 -5.118 3.09e-07 ***
## logLOS
               0.034320
                          0.011223
                                      3.058 0.00223 **
## logRiskscore 0.712242
                          0.012463 57.147 < 2e-16 ***
## Under65
               -0.040227
                          0.031401 -1.281 0.20017
## DRGMed.NoC
               -0.023769 0.020119 -1.181 0.23744
## DRGOtherMED 0.066662
                          0.027689
                                      2.408 0.01606 *
## DRGOtherSURG 0.051371
                           0.034428
                                      1.492 0.13567
## DRGUNGROUP
                0.066127
                           0.077090
                                      0.858 0.39101
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33933 on 50070 degrees of freedom
## AIC: 33957
## Number of Fisher Scoring iterations: 5
Now remove ER.
glmprobit <- glm(Readmission.Status ~ Gender + Race + Age + logLOS + logRiskscore + Under65 + DRG, data
summary(glmprobit)
##
```

glm(formula = Readmission.Status ~ Gender + Race + Age + logLOS +

```
##
       logRiskscore + Under65 + DRG, family = binomial(link = "probit"),
##
       data = train)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -1.2714 -0.5761 -0.3946 -0.2387
                                        3.2566
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept)
               -1.439469
                           0.072930 -19.738 < 2e-16 ***
## GenderM
               -0.010808
                           0.015452
                                     -0.699 0.48426
## RaceBlack
                0.030535
                           0.024555
                                      1.244 0.21367
## Age
                -0.004495
                           0.000878
                                     -5.119 3.07e-07 ***
## logLOS
                           0.011223
                                      3.061 0.00221 **
                0.034349
## logRiskscore 0.712211
                           0.012463
                                     57.148 < 2e-16 ***
## Under65
                -0.040278
                           0.031400
                                     -1.283
                                             0.19959
                -0.023733
## DRGMed.NoC
                           0.020119
                                     -1.180 0.23815
## DRGOtherMED
                0.066616
                           0.027688
                                      2.406 0.01613 *
                           0.034428
## DRGOtherSURG 0.051364
                                      1.492 0.13572
## DRGUNGROUP
                0.066078
                           0.077092
                                      0.857 0.39137
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117
                            on 50081 degrees of freedom
## Residual deviance: 33933 on 50071 degrees of freedom
## AIC: 33955
##
## Number of Fisher Scoring iterations: 5
Now remove Gender
glmprobit <- glm(Readmission.Status ~ Race + Age + logLOS + logRiskscore + Under65 + DRG, data=train,
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ Race + Age + logLOS + logRiskscore +
      Under65 + DRG, family = binomial(link = "probit"), data = train)
##
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -1.2749 -0.5758 -0.3947 -0.2389
                                        3.2608
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.4479936 0.0719116 -20.136 < 2e-16 ***
## RaceBlack
                0.0308596 0.0245506
                                       1.257 0.20876
## Age
                -0.0044419 0.0008748
                                      -5.078 3.82e-07 ***
## logLOS
                0.0343108 0.0112223
                                       3.057 0.00223 **
## logRiskscore 0.7120724
                           0.0124610
                                      57.144 < 2e-16 ***
## Under65
                -0.0395810 0.0313830
                                      -1.261 0.20723
```

-0.0237511 0.0201186 -1.181 0.23778

DRGMed.NoC

```
## DRGOtherMED 0.0667391 0.0276865
                                         2.411 0.01593 *
                                         1.497 0.13441
## DRGOtherSURG 0.0515353 0.0344275
## DRGUNGROUP
                 0.0658603 0.0770924
                                       0.854 0.39294
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33933 on 50072 degrees of freedom
## AIC: 33953
## Number of Fisher Scoring iterations: 5
Rather than remove DRGUNGROUP at this stage, it will be combined with DRGOtherSURG. The difference
in significance is likely due to sample sizes.
readmission2<-readmission
var <- "DRG"</pre>
var.levels <- levels(readmission2[,var])</pre>
readmission2[,var] <- mapvalues(readmission2[,var],var.levels,c("DRGbase","Med.NoC","OtherMED","OSUngro
#Relevel
table <- as.data.frame(table(readmission2[,var]))</pre>
  max <- which.max(table[,2])</pre>
 level.name <- as.character(table[max,1])</pre>
 readmission2[,var] <- relevel(readmission2[,var], ref = level.name)</pre>
table(readmission2[,var])
##
##
     DRGbase
               Med.NoC OtherMED OSUngroup
                 12310
##
       45121
                            5357
                                       3988
readmission <- readmission2
train <- readmission[partition,]</pre>
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ Race + Age + logLOS + logRiskscore + Under65 + DRG, data=train, f
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ Race + Age + logLOS + logRiskscore +
       Under65 + DRG, family = binomial(link = "probit"), data = train)
##
## Deviance Residuals:
                 10
                     Median
                                    3Q
                                            Max
## -1.2749 -0.5758 -0.3947 -0.2390
                                         3.2609
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.4480241 0.0719121 -20.136 < 2e-16 ***
## RaceBlack
                 0.0308837 0.0245501
                                         1.258 0.20840
                -0.0044420 0.0008748 -5.078 3.82e-07 ***
## Age
## logLOS
                 0.0343218 0.0112225
                                        3.058 0.00223 **
```

```
## logRiskscore 0.7120944 0.0124602 57.149 < 2e-16 ***
## Under65
               -0.0395813 0.0313827
                                      -1.261 0.20722
## DRGMed.NoC
               -0.0237522 0.0201187 -1.181 0.23776
## DRGOtherMED 0.0667366 0.0276866
                                       2.410 0.01593 *
## DRGOSUngroup 0.0537795 0.0318155
                                       1.690 0.09096 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33933 on 50073 degrees of freedom
## AIC: 33951
##
## Number of Fisher Scoring iterations: 5
Next to go is Med.NoC with the hightest p-value.
readmission2<-readmission
var <- "DRG"</pre>
var.levels <- levels(readmission2[,var])</pre>
readmission2[,var] <- mapvalues(readmission2[,var],var.levels,c("DRGbase","DRGbase","OtherMED","OSUngro
#Relevel
table <- as.data.frame(table(readmission2[,var]))</pre>
 max <- which.max(table[,2])</pre>
  level.name <- as.character(table[max,1])</pre>
 readmission2[,var] <- relevel(readmission2[,var], ref = level.name)</pre>
table(readmission2[,var])
##
##
     DRGbase
             OtherMED OSUngroup
       57431
                  5357
readmission <- readmission2
train <- readmission[partition,]</pre>
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ Race + Age + logLOS + logRiskscore + Under65 + DRG, data=train, f
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ Race + Age + logLOS + logRiskscore +
       Under65 + DRG, family = binomial(link = "probit"), data = train)
##
##
## Deviance Residuals:
      Min
                     Median
                                   3Q
                 1Q
                                           Max
## -1.2749 -0.5759 -0.3944 -0.2391
                                        3.2651
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.4524752 0.0718246 -20.223 < 2e-16 ***
## RaceBlack
                0.0305938 0.0245494
                                       1.246 0.21269
               ## Age
```

```
## logLOS
                0.0341318 0.0112210
                                      3.042 0.00235 **
## logRiskscore 0.7119330 0.0124591 57.142 < 2e-16 ***
## Under65
               -0.0394441 0.0313816 -1.257 0.20878
## DRGOtherMED
                0.0718764
                           0.0273458
                                       2.628 0.00858 **
## DRGOSUngroup 0.0589066 0.0315200
                                       1.869 0.06164 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33935 on 50074 degrees of freedom
## AIC: 33951
##
## Number of Fisher Scoring iterations: 5
Now remove Race.
readmission <- readmission2</pre>
train <- readmission[partition,]</pre>
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ Age + logLOS + logRiskscore + Under65 + DRG, data=train, family =</pre>
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ Age + logLOS + logRiskscore +
       Under65 + DRG, family = binomial(link = "probit"), data = train)
##
##
## Deviance Residuals:
      Min
                     Median
                1Q
                                  3Q
                                          Max
## -1.2801 -0.5760 -0.3945 -0.2391
                                       3.2626
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.4456943 0.0716320 -20.182 < 2e-16 ***
## Age
               -0.0044962  0.0008739  -5.145  2.68e-07 ***
## logLOS
                0.0340328 0.0112205
                                       3.033 0.00242 **
## logRiskscore 0.7121407 0.0124577 57.165 < 2e-16 ***
## Under65
               -0.0371728 0.0313192 -1.187 0.23527
## DRGOtherMED 0.0721155 0.0273450
                                       2.637 0.00836 **
## DRGOSUngroup 0.0588470 0.0315197
                                       1.867 0.06190 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 38117 on 50081 degrees of freedom
## Residual deviance: 33936 on 50075 degrees of freedom
## AIC: 33950
## Number of Fisher Scoring iterations: 5
Now remove Under65.
```

```
readmission <- readmission2</pre>
train <- readmission[partition,]</pre>
test <- readmission[-partition,]</pre>
glmprobit <- glm(Readmission.Status ~ Age + logLOS + logRiskscore + DRG, data=train, family = binomial(</pre>
summary(glmprobit)
##
## Call:
## glm(formula = Readmission.Status ~ Age + logLOS + logRiskscore +
      DRG, family = binomial(link = "probit"), data = train)
##
## Deviance Residuals:
      Min
                1Q
                     Median
                                  3Q
##
                                         Max
## -1.2838 -0.5759 -0.3948 -0.2391
                                       3.2709
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.5099622 0.0470000 -32.127 < 2e-16 ***
               ## logLOS
                0.0341991 0.0112199
                                      3.048 0.00230 **
## logRiskscore 0.7114348 0.0124460 57.162 < 2e-16 ***
## DRGOtherMED
                0.0719061 0.0273415
                                      2.630 0.00854 **
## DRGOSUngroup 0.0590267 0.0315181
                                      1.873 0.06110 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 38117
                           on 50081 degrees of freedom
##
## Residual deviance: 33938 on 50076 degrees of freedom
## AIC: 33950
##
## Number of Fisher Scoring iterations: 5
```

Everything is now significant at the 10% level and we stop. If we wanted a lower significance level for decision making, the process would continue.