



InferTrade
PREDICTIVE RESEARCH TOOLS

Predictive Relationship: Combination Relationship

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1 Relationship Description

In a combination relationship, the combination of (1) the current value of the signal, (2) recent changes in the value of the signal, and (3) the difference between the signal and the market directly affect future changes in the price:

$$\Delta p_{t+1} \propto k_1 r_t + k_2 \left(\frac{r_t}{r_{t-1}} - 1 \right) + k_3 \left(\frac{p_t}{r_t} - 1 \right) + c \quad (1)$$

where Δp_{t+1} represents the future price change, r_t represents the current value of the research signal at current time t , p_t represents the current value of the market price at current time t , k_1 k_2 k_3 are scalars, and c is a constant. This relationship can capture more complex relationships which may be a combination of Level, Change and Difference Relationships. Each of these relationships is expressed in the first three terms of the above equation, each weighted by their importance. To learn more about each of these relationships, find their explanations in the corresponding downloadable PDFs.

After finding the relationship which maximises risk adjusted returns, InferTrade runs tests for statistical significance to verify that the relationship gives a predictive edge. A predictive combination relationship can be used to invest depending on the level of the signal, recent percentage changes in the signal, and percentage difference between the market and the signal.

2 Trading Strategy Description

A predictive combination relationship can be reflected in many kinds of rules. InferTrade uses a 120 period (6 months for daily data) rolling regression of the a combination of price-research value relationships against next day's price change as a benchmark. This trading rule recommends taking a position sized as a percentage of the capital you have allocated to trading this particular market.

This rule will show higher returns than usual after optimisation if a significant Combination Relationship is present between the price and signal series. The following equation shows how a Combination Regression trading rule calculates position sizing:

$$z_t = \kappa_1 r_t + \kappa_2 \left(\frac{r_t}{r_{t-1}} - 1 \right) + \kappa_3 \left(\frac{p_t}{r_t} - 1 \right) + \epsilon_{t+1} \quad (2)$$

with the error symmetric such that

$$E_t^{model}[\Delta p_{t+1}] = \kappa_1 r_t + \kappa_2 \left(\frac{r_t}{r_{t-1}} - 1 \right) + \kappa_3 \left(\frac{p_t}{r_t} - 1 \right) \quad (3)$$

where z_t is the recommended strategy allocation at time t , $E_t^{model}[\Delta p_{t+1}]$ is the predicted next day percentage price change, r_t is the research value at time t , p_t is the price value at time t and k_1 , k_2 and k_3 are the level, difference and static coefficients. ϵ_t represents the in sample regression error between the model predicted and observed price change for time t , such that $\epsilon_t = E_{t-1}^{model}[\Delta p_t] - \Delta p_t$.

To give a suggested portfolio allocation z_t for the market, e.g. “invest 5% of strategy allocation into the security”, the regression forecast’s expected next day % price move is divided by the square of the Standard Root Mean Squared Percentage Prediction Error $\varepsilon_{rms_t}^2$ in our above regression:

$$z_t = \begin{cases} \frac{\Delta p_{t+1}}{\varepsilon_{rms_t}^2} & \text{if } t > L, \\ 0 & \text{otherwise} \end{cases} \quad (4)$$

where z_t is the suggested allocation as a percentage of the capital which you have allocated to trading this market at time t .

Worked example for liquid market: current share price is \$50, regression coefficients are 0.00005 ($5 * 10^{-5}$) for level and 0.0 for the constant, with \$1,000 allocated to this single-stock strategy. The current research series - a sentiment index - is +5.0, with a RMS prediction error from the regression of 5%. In this situation the strategy recipe recommends an investment of $0.00005 * 5.0 / (0.05)^2 = 10\%$ be allocated. So $\$1,000 * 10\% = \100 would be allocated, so we would buy $\frac{\$100}{\$50} = 2$ shares. We see from this example the expected gain over the next day is 2.5 basis points (minus trading costs), versus 500 basis points of daily risk, so in practice this kind of strategy is most useful where the signal both has a predictive edge and is stable (auto-correlated) in recommendation over time, so that the ‘edge’ from multiple time steps can compound linearly without incurring additional bid-offer spreads whilst the ‘risk’ aggregates scales with the square-root of time (for random walk).

(Note that if the magnitude of the error term is smaller than the magnitude of the price change prediction, i.e. $|\varepsilon_{rms_t}| < |\Delta p_{t+1}|$, dividing Δp_{t+1} by $\varepsilon_{rms_t}^2$ would result in $z_t > 1$. Limits can then be applied to cap the allocation. E.g. between 0% and 100% if short selling is prohibited. In practice it is generally unlikely that in liquid markets a genuine statistical trading signal this strong will be found.)

3 Fixed Strategy Parameters

Below is a table summarizing the parameters specific to this trading rule.

Parameter Name	Default Value	Description	Symbol
Regression Length	120	This is the number of previous days used to estimate the regression coefficients.	L

For estimating the regression coefficients, a rolling window is used, so that at time t , the regression data uses research data from time $t - 121$ to $t - 1$ to calculate 120 research changes as the regression’s independent variable. Price data from $t - 120$ to t is used to calculate 120 next day price changes as the regression’s dependent variable.

Note that rule parameters are fixed to their default values for this and any other relationships optimised on simplified mode.

4 Glossary

- **Bullish:** Positive outlook on the market. Expectation of positive returns.
- **Bearish:** Negative outlook on the market. Expectation of negative returns.

- **Allocation:** The allocation is the fractional amount of the portfolios value used to determine the size of the trading position.
- **Parameter:** Value used by the trading rule in the calculation for trading position
- **Trading Rule:** Strategy to determine when to buy, hold or sell a position.

Further Links

1. InferTrade: <https://www.infertrade.com>
2. Privacy Policy/Legal notice: <https://www.infertrade.com/privacy-policy>
3. InferStat Ltd: <https://www.inferstat.com>

Appendix

Calculating Regression Error

This PDF omits any explanation of how the regression coefficients k_1 and k_2 are calculated as we are using a standard regression for calculation of both the coefficients and standard error. For InferTrade we used the open source *sklearn* Python library. The same can be achieved in Microsoft Excel by using the *FORECAST.LINEAR* function.

As a worked illustration of the error calculation, assume that InferTrade predicted that a security would increase in price by 0.1% between yesterday and today, and the price actually decreased by 4.9%. In this example, $\Delta p_t = +0.1\%$, and $\Delta o_t = -4.9\%$, giving $\Delta P_t - \Delta p_t = 0.1\% - 4.9\% = -5\% = -0.05$. This value is then squared to give $(\Delta p_t - \Delta o_t)^2 = (-0.05)^2 = 0.0025$. To obtain $\varepsilon_{rms_t}^2$ for day t , this calculation is repeated for every day from day $i = t - L$ to day $i = t$, with values summed before dividing by the regression length L .