Worked solutions to the problems

Problem 1

a) (i)
$$C_8H_{18}(1) + \frac{25}{2}O_2(g) \longrightarrow 8CO_2(g) + 9H_2O(1)$$

The heat capacity of the calorimeter and its content is

$$C_s = 48 + (750 \text{ x } 4.184) = 3186 \text{ J K}^{-1}$$

The amount of heat released at constant volume is

$$q_V = -C_s \Delta T = -(3186 \text{ J K}^{-1}) (8.220 \text{ K}) = -2.619 \text{ x } 10^4 \text{ J} = -26.19 \text{ kJ}$$

(Minus means exothermic reaction)

Hence, we obtain:

$$\Delta U^{o} = q_{V} = -26.19 \text{ kJ}$$

(ii) For the combustion of 1 mole of isooctane:

$$\Delta U^o \; = \; - \; \frac{(114.23 \; g \; mol^{-1})(26.19 \; kJ)}{0.542 \; g} \; = \; -5520 \; kJ \; mol^{-1}$$

(iii) The enthalpy change (ΔH^{o}) is related to ΔU^{o} as follows:

$$\Delta H^{o} = \Delta U^{o} + \Delta n_{gas} (RT)$$

From the reaction : $\Delta n_{gas} = 8 - \frac{25}{2} = -\frac{9}{2}$ mol

Thus,
$$\Delta n_{gas}$$
 (RT) = $(-\frac{9}{2})$ (8.314 J mol⁻¹ K⁻¹) (298.15 K)
= -11.15 x 10³ J

As ΔU^{o} is given in kJ, we obtain

$$\Delta H^{\circ} = \Delta U^{\circ} - 11.15 = -5520 - 11.15 = -5531 \text{ kJ mol}^{-1}$$

(iv) Since
$$\Delta H^o = 8\Delta H_f^o$$
, $CO_2(g) + 9\Delta H_f^o$, $H_2O(l) - \Delta H_f^o$, $C_8H_{18}(l)$

Therefore

$$\Delta H_f^{\circ}$$
, $C_8 H_{18}(1) = 8(-393.51) + 9(-285.83) - (-5531)$
= -190 kJ mol⁻¹

b) (i) From
$$\Delta G^{o} = -RT \ln K$$
, then

$$InK = -\frac{\Delta G^o}{RT} = \frac{-\Delta H^o}{RT} + \frac{\Delta S^o}{R}$$

If the lower temperature, 298.15 K, is written as T_1 ,

$$ln \; K_1 \quad = \quad \frac{-\Delta H^o}{RT_1} \, + \, \frac{\Delta S^o}{R}$$

Similarly, for the higher temperature 313.15 K

$$ln K_2 = \frac{-\Delta H^o}{RT_2} + \frac{\Delta S^o}{R}$$

Thus
$$\ln \frac{K_2}{K_1} = \frac{\Delta H^{\circ}}{R} (\frac{T_2 - T_1}{T_1 T_2})$$

$$\ln \frac{3.45 \times 10^3}{1.80 \times 10^3} = \frac{\Delta H^o \text{Jmol}^{-1}}{8.314} \cdot \frac{15.00 \text{ K}}{(298.15 \text{ K})(313.15 \text{ K})}$$

$$\Delta H^{o} = 33.67 \text{ kJ mol}^{-1}$$

For ΔS^o

In 3.45 x
$$10^3 = 8.146 = \frac{-33670 \text{ J mol}^{-1}}{(8.314 \text{ J mol}^{-1} \text{ K}^{-1})(313.15 \text{ K})} \frac{+\Delta S^o \text{ J mol}^{-1}}{8.314 \text{ J K}^{-1} \text{ mol}^{-1}}$$
 so that $\Delta S^o = 175.2 \text{ J K}^{-1} \text{ mol}^{-1}$

(ii) From the given equation, we obtain

$$K_p = \frac{P_{AB}}{P_A.P_B}$$

From PV = nRT, then

$$K_p \ = \frac{\text{[AB](RT)}}{\text{[A](RT)[B](RT)}} = \ \frac{K_{\text{C}}}{RT} \label{eq:Kp}$$

At 298.15 K

$$K_p = \frac{(1.80 \times 10^3 \text{ L mol}^{-1})}{(8.314 \text{ atm L K}^{-1} \text{mol}^{-1})(298.15 \text{ K})} = 0.726 \text{ atm}^{-1}$$

From $P_1 = X_1P$, then

$$K_{p} \; = \; \frac{X_{AB}}{X_{A}.X_{B}} \, . \; P^{\text{-}1} \; = \; K_{x} \, . \; P^{\text{-}1}$$

$$K_X = K_p \cdot P = (0.736 \text{ atm}^{-1})(1 \text{ atm}) = 0.726$$

c) From
$$\ln \frac{K_2}{K_1} = \frac{\Delta H^{\circ}}{R} (\frac{T_2 - T_1}{T_1 T_2})$$

Choose any two values of K at two different temperature, i.e. at 15.2°C (288.4 K) and 34.9°C (308.2 K).

$$\ln \frac{530}{840} = \frac{\Delta H^o}{8.314} \left(\frac{308.2 - 288.4}{288.4 \times 308.2} \right)$$

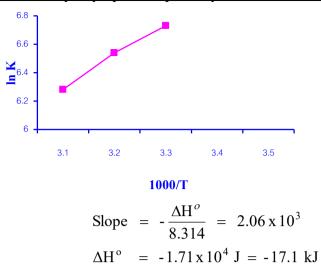
$$\Delta H^{o} = -1.72 \times 10^{4} \text{ J} = -17.2 \text{ kJ}$$

OR

From
$$\ln K = \frac{\Delta S^{o}}{R} - \frac{\Delta H^{o}}{R} \cdot \frac{1}{T}$$

 ΔH° and ΔS° are assumed to be constant. A plot of ln K against 1/T should be a straight line of slope equal to - $\Delta H^\circ/R$

T(Kelvin) : 288.4 298.2 308.1 K : 840 690 530 10³/T : 3.47 3.36 3.25 ln K : 6.73 6.54 6.28



Problem 2

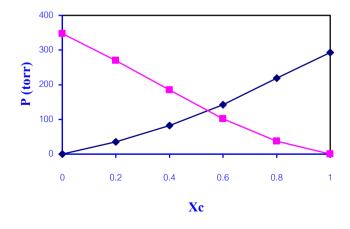
a) (i) By calculation from the Raout's law: $P_i = X_i P_i^o$, hence

 X_{C} : 0.20 0.40 0.60 0.80 $P_{C} = X_{C}P_{c}^{o}$ (torr) : 59 117 176 234 P_{C} (measured)(torr) : 35 82 142 219 $(P_{c}^{o} = 293 \text{ torr})$

 X_{A} 0.20 : 0.80 0.60 0.40 $P_A = X_A P_{\Delta}^o$ (torr) : 277 208 139 69 P_A (measured)(torr) : 270 185 102 37 $(P_A^o) = 347 \text{ torr})$

It can be seen that the calculated vapor pressures of both acetone and chloroform are higher than the measured values at all proportions. Thus, the solutions deviated from ideal solution.

It can be shown, however, by plotting the pressure-composition diagram as follows:



(ii) The solutions exhibit <u>negative deviation</u> from ideal behavior.

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(iii) From the data given, we can then calculated the activity of chloroform and acetone:

0.40 0.60 $X_{\rm C}$ 0.20 0.80 $a_C = P_C / P_C^0$ 0.28 0.48 0.75 0.12 X_A 0.80 0.60 0.40 0.20 $a_A = P_A / P_A^o$ 0.78 0.53 0.29 0.11

The activities of both chloroform and acetone are less than the mole fractions indicating negative deviation from ideal behavior.

b) (i) From the Gibbs-Helmholtz equation,

$$\frac{d\ln X_1}{dT} = \frac{\Delta H_{\text{fus}}^{\,\text{o}}}{RT^2} \tag{1}$$

Where X_1 is the mole fraction of the liquid solvent and $\Delta H_{\text{fus}}^{\text{o}}$, the heat of

fusion of pure solvent. If ΔH_{fus}^{o} is independent of T over a moderate range of

temperature, we my integate Eq.(1) from T_f° , the freezing point of pure solvent at $X_1 = 1$, to T, the temperature at which solid solvent is in equilibrium with liquid solvent of mole fraction X_1 . The result is

$$\ln X_1 = \frac{\Delta H_{\text{fis}}^{\circ}}{R} \left(\frac{1}{T_f^{\circ}} - \frac{1}{T} \right) \tag{2}$$

By expressing X_1 , in terms of X_2 , the mole fraction of the solute:

$$\ln (1-X_2) = \frac{\Delta H_{\text{fis}}^o}{R} \left(\frac{T - T_{\text{f}}^o}{T.T_{\text{f}}^o} \right)$$
 (3)

If X_2 is small (corresponding to a solution), then

$$ln (1-X_2) \sim -X_2$$

The freezing point depression is T_f^o - $T = \Delta T_f$. Since ΔT_f is small in comparison to T_f^o , we may set the product $TT_f^o \sim T_f^{o2}$. These changes convert Eq. (3) to

$$X_2 = \frac{\Delta H_{\text{fiis}}^o}{R} \cdot \frac{\Delta T_f}{T_f^{o^2}}$$
 (4)

In dilute solution, $X_2 = n_2/(n_1 + n_2) \sim n_2/n_1$.

The molality m_2 is related to the amount of n_2 of solute by $m_2 = \frac{n_2}{w_1} \times 1000$ where w_1 is the mass in grams of solvent.

For the solvent $n_1 = w_1/M_1$, where M_1 is its molar mass.

Then $X_2 = m_2 M_1 / 1000$.

Rearrangement of Eq. (4) and substitution for X2 yields

$$\Delta T_{\rm f} \sim \frac{M_1 R T_{\rm f}^{\rm o^2}}{\Delta H_{\rm f}.1000} . m_2$$
 (5)

The freezing point depression or cryoscopic constant K_f defined as

$$K_f = \frac{M_1 R T_f^{o^2}}{\Delta H_f \cdot 1000} \tag{6}$$

Therefore,

$$\begin{split} K_{\rm f} & = \frac{(147.01~g~mol^{-1})(8.314~J~K^{-1}mol^{-1})(326.28~K)^2}{(17880~J~mol^{-1})(1000~g~kg^{-1})} \\ & = ~7.26~K~kg~mol^{-1} \end{split}$$

(ii) $\Delta T_f = 326.28-323.78 = 2.50 \text{ K}$

With the definition of K_f , Eq. (6) may be expressed as

$$\Delta T_f = K_f m_2 \tag{7}$$

Since
$$m_2 = \frac{n_2}{w_1} .1000 = \frac{w_2.1000}{w_1.M_2}$$
 (8)

where M_2 is the molar mass of solute.

After rearrangement, we have

$$M_{2} = \frac{K_{f}.w_{2}.1000}{\Delta T_{f}.w_{1}}$$

$$= \frac{(7.28 \text{ K kg mol}^{-1})(1.50 \text{ g})(1000 \text{ g kg}^{-1})}{(2.50 \text{ K})(30.0 \text{ g})}$$

$$= 145.6 \text{ g mol}^{-1}$$
(9)

(iii) Using Eq. (2) we obtain

$$\ln X = \frac{17880}{8.314} \left(\frac{1}{326.28} - \frac{1}{298.15} \right) = -0.622$$

$$X = 0.537$$

The mole-fraction solubility of *p*-dichlorobenzene at 298.15 K in an ideal solution is, therefore, equal to 0.537.

Problem 3

a) (i) Reaction and total kinetic energy

1st step
$$^{238}_{92}$$
U $\rightarrow ^{234}_{90}$ Th $+ ^{4}_{2}$ He
Q = K_d + K_α = [m(238 U) - m(234 Th) - m(4 He)]c²
= [238.05079 u - 234.04360 u - 4.00260 u]931.5 MeV u⁻¹
= (4.59 x 10⁻³ u)(931.5 MeV u⁻¹) = 4.28 MeV
K_d and K_α are KE of daughter and α-particle.

$$\begin{array}{ll} \mbox{2nd step} & \mbox{$^{234}_{90}$Th} \rightarrow & \mbox{$^{234}_{91}$Pa} + \mbox{$^{\circ}_{-1}$e(or β^{-})} \\ Q & = & \mbox{K_d} + \mbox{$K_{\beta^{-}}$} = [\mbox{$m(234Th}$) - \mbox{$m(234Pa}$)]c^2 \\ & = & [\mbox{234.04360 u - 234.04332$ u] 931.5$ MeV u^{-1}} \\ & = & (2.8 \times 10^{-4} \, \mbox{$u($)$})(931.5 \, \mbox{MeV} \, \mbox{u^{-1}}) = 0.26 \, \mbox{MeV} \end{array}$$

(ii) At equilibrium (secular) $N_1\lambda_1 = N_2\lambda_2 = A$ (where A is activity)

For
226
Ra, $\lambda_1 = \frac{0.693}{(1620 \, y)(365 \, d \, y^{-1})} = 1.17 \, x \, 10^{-6} \, d^{-1}$
For 222 Rn, $\lambda_2 = \frac{0.693}{3.83} = 0.181 \, d^{-1}$
 $N_1 = \frac{1000 \, g \, x \, 6.022 \, x \, 10^{23} \, mol^{-1}}{226 \, g \, mol^{-1}} = 2.66 \, x \, 10^{24}$
 $N_2 \, (0.181 \, d^{-1}) = (2.66 \, x \, 10^{24})(1.17 \, x \, 10^{-6} d^{-1})$
 $N_2 = 1.72 \, x \, 10^{19}$
Number of moles of 222 Rn $= \frac{1.72 \, x \, 10^{19}}{2200 \, mol^{-1}} = 2.86 \, x \, 10^{-5} \, mol^{-1}$

Number of moles of
222
Rn = $\frac{1.72 \times 10^{19}}{6.022 \times 10^{23} \text{mol}^{-1}}$ = 2.86 x 10⁻⁵ mol

Volume of
222
Rn = $2.86 \times 10^{-5} \text{ mol } \times 25.0 \text{ L mol}^{-1}$
= $7.15 \times 10^{-4} \text{ L}$

(iii)
$$N_1 = N_0 e^{-\lambda t}$$

Then $\frac{N_1}{N_2} = \frac{N_0 e^{-\lambda t_1}}{N_0 e^{-\lambda t_2}} = \frac{e^{-\lambda t_1}}{e^{-\lambda t_2}} = e^{\lambda (t_2 - t_1)}$
and $10 = e^{\lambda (12.80 \text{ d})}$
 $\lambda = \frac{\ln 10}{12.80 \text{ d}} = 0.181 \text{ d}^{-1}$
 $t_{1/2} = \frac{0.693}{0.180 \text{ d}^{-1}} = 3.85 \text{ days}$

b) (i) On the reactant side there are 92 protons while on the product side there are 96 protons. There must be 4β - and 2n on the product side.

$$_{o}^{1}n$$
 + $_{92}^{235}U$ \rightarrow $_{42}^{98}Mo$ + $_{54}^{136}Xe$ + 4β - + $2_{o}^{1}n$

The elementary particles released : $4\beta^-$ and 2n

(ii) Input mass =
$$235.04393 \text{ u} + 1.00867 \text{ u} = 236.05260 \text{ u}$$

Output mass = $97.90551 \text{ u} + 135.90722 \text{ u} + (2)(1.00867 \text{ u})$
= 235.83007 u

Masses of $4\beta^-$ are included in the atomic mass of products., so they do not appear in the output mass.

$$\Delta m = 236.05260 \text{ u} - 235.83007 \text{ u} = 0.22253 \text{ u}$$

Energy= $(0.22253 \text{ u})(931.5 \text{ MeV u}^{-1}) = 207.3 \text{ MeV}$
Energy= $(207.3 \text{ MeV})(1.602 \text{ x } 10^{-13} \text{J MeV}^{-1}) = 3.32 \text{ x } 10^{-11} \text{ J}$
is the energy per fission.

which is the energy per fission.

(iii) Energy per gram =
$$\frac{6.022 \times 10^{23} \text{ mol}^{-1}}{235 \text{ g mol}^{-1}} \times 3.32 \times 10^{-11} \text{ J}$$

$$= 8.51 \times 10^{10} \text{ J g}^{-1}$$

$$1W = 1 \text{ J s}^{-1}$$

$$1 \text{ kW-hour} = (1000 \text{ W})(3600 \text{ s}) = 3.60 \text{ x } 10^6 \text{ Ws}$$

$$= 3.60 \text{ x } 10^6 \text{ J}$$

$$= \frac{8.51 \text{ x } 10^{10} \text{ J}}{3.60 \text{ x } 10^6 \text{ J/kW - hour}}$$

$$= 2.36 \text{ x } 10^4 \text{ kW-hour}$$

Problem 4

(i) Average initial rate (M^{-1} min⁻¹) 0.00330/25.0 = 0.000132 0.00390/15.0 = 0.0002600.00770/7.50 = 0.000103

When [B] is doubled, the rate is doubled, hence the reaction is first order in B. When [A] is doubled, the rate is quadrupled, hence the reaction is second order in A.

Rate =
$$k[A]^2[B]$$

(ii)

Entry	$k = \frac{\text{rate}}{[A]^2[B]}$	
1	$\frac{0.000132}{(0.100)^2(0.0500)}$	= 0.264
2	$\frac{0.00026}{(0.100)^2(0.0100)}$	= 0.260
3	$\frac{0.000103}{(0.200)^2(0.100)}$	= 0.258

The average of k is $0.261 L^2 mol^{-2} min^{-1} = 4.34 x 10^{-3} L^2 mol^{-2} s^{-1}$.

(2) in (1);
$$rate = \frac{d[HOCl]}{dt} = \frac{k_1 k_2 [OCl^-][I^-]}{k_2 [I^-]} = k_1 [OCl^-]$$
 (3)

Mechanism III

rate =
$$\frac{k_1 k_2 [OCl^-][I^-]}{k_{-1}[OH^-] + k_2[I^-]}$$
 (4)

if $k_2 << k_{-1}$

rate =
$$\frac{k_1 k_2 [OCl^-][I^-]}{k_{-1}[OH^-]}$$
 (5)

if
$$k_2 >> k_{-1}$$
 rate = $k_1[OC1^-]$ (6)

Therefore, Mechanism III is the most appropriate for observed kinetic behaviour when $k_2 \ll k_{-1}$

(ii) For Mechanism III $k = \frac{k_1k_2}{k_{-1}}$ $E_a = E_{a1} + E_{a2} - E_{a-1}$ $A = \frac{A_1A_2}{A_{-1}}$

(iv) In a buffer solution, [OH-] is constant and rate = k[OCl-][I-], therefore, the reaction is second order.

 $\begin{array}{ll} \text{(iv)} & K_w \, = \, [H_3O^+][OH^-] \, ; \, [OH^-] \, = \, K_w \, / \, [H_3O^+] \\ & \text{rate} \, = \, \frac{k[OCl^-][I^-]}{[OH^-]} \, = \, \frac{k}{K_w} \, \, [OCl^-][I^-][H_3O^+] \\ \text{(v)} & \text{rate} \, = \, \frac{k}{K_w} \, \, . \, [OCl^-][I^-][H_3O^+] \\ \end{array}$

 $(v) \qquad \text{rate } = \frac{k}{K_W} \cdot [OCl^-][I^-][H_3O^+]$ $\text{rate } = k_{\text{cat}}[OCl^-][I^-]$ $k_{\text{cat}} = \cdot [H_3O^+]$ $\log k_{\text{cat}} = \log \frac{k}{K_W} - pH$

Problem 6

a) NH_3^+ S S NH_3^+ NH_3^+

(ii) reducing agent

(iii)
$$HO_2C$$
 NH_3^+ SO_3

(iv) +4

b) (i) Gly-Asn-Phe-Glu

(ii) < 7

b)
(i) Nucleophilic Aromatic Substitution
General mechanism:

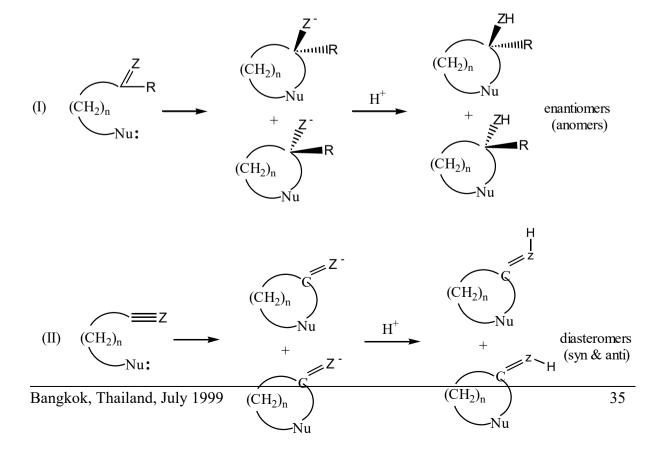
(ii) s 1 ower

(iii)
$$NO_2 \stackrel{CH_3}{\underset{N}{\bigvee}}$$

(iv) According to mechanism in (i), step 1 is slower than step 2, and step 1 is the rate determining step.

Problem 9

a) (i)



(ii)
$$(CH_{2})_{n} \longrightarrow H^{+} \longrightarrow (CH_{2})_{n} \longrightarrow (CH_{2$$

b)
$$HO \longrightarrow HCHO \longrightarrow HCHO \longrightarrow N \longrightarrow CH_3 \longrightarrow CH_3$$

- a) (i) Pyridine is less basic than piperidine because the pair of electrons that gives pyridine its basicity occupies an sp^2 orbital; it is held more tightly and is less available for sharing with acids than the pair of electrons of piperidine, which occupies an sp^3 orbital.
 - (ii) Pyridine has a pair of electrons (in an sp^2 orbital) that is available for sharing with acid; pyrrole has not, and can accept a proton only at the expense of the aromatic character of the ring.
 - (iii) There are two reasons behind this observation. First, the nitrogen of aniline is bonded to an sp^2 –hybridized carbon atom of the aromatic ring, which is more electronegative than the sp^3 –hybridized carbon atom of cyclohexylamine. Second, the non-bonding electron can be delocalized to the aromatic ring. Resonance contributions indicate that it has decreased electro density at the nitrogen. Therefore, cyclohexylamine is more basic than aniline.

$$NH_2$$
 NH_2 NH_2

(iv) Delocalization of lone pair of electrons of the NH₂ group into the ring is possible. This results in an increase electro density on the heterocyclic nitrogen atom, hence, an increase in basicity at this site.

$$NH_{2} \xrightarrow{NH_{2}^{+}} NH_{2} NH_{2} \xrightarrow{NH_{2}^{+}} NH_{2} NH_{2}$$

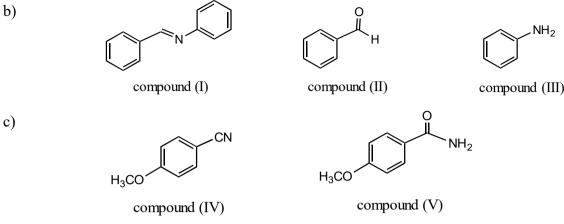
(v) Piperidine is more basic than morpholine. The oxygen atom in morpholine is more electronegative than methylene group (at the same position) of piperidine so there is less electron density on nitrogen atom of morpholine than that of piperidine.

(iii) isoelectric point = $(pK_{a1} + pK_{a2})/2 = 6.88$

- a) Substitution of benzene by auxochromes, chromophores, or fused rings has different effects on the absorption spectrum.
 - (i) Introduction of polar substituents such as -NH₂, -OH, OCH₃ cause marked spectral changes. The nonbonding electrons of the -OH group can conjugate with the π system of the ring. Since the energy of the π^* system is lowered by delocalization over the entire conjugated system, the n- π^* absorption occurs at longer wavelength than in benzene.
 - (ii) Conversion of phenol to the phenolate anion makes an additional pair of nonbonding electrons available to the conjugated system, and both the
 - wavelengths and the intensities of the absorption bands are increased. A suspected phenolic group may be determined by comparison of the uv spectrum of the compound in neutral and in alkaline (pH 13) solution.
 - (iii) Conversion of aniline to the anilinium cation involves attachment of a proton to the nonbonding electron pair, removing it from conjugation with the π

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electrons of the ring. The absorption of this ion closely resemble those of benzene.



d) (i) allyl alcohol

(ii) cyclopropanol

CH₂
$$\delta \Box 4$$
 ppm, m, 1H
CH—OH s, 1H, disappeared on shaking with D₂O
CH₂ $\delta \Box 1$ ppm, m, 4H

e)
$$CH_3$$
 CH_3 CH_3 CH_3 CH_3 CH_3 CH_3 CH_3 CH_3 CH_3 CH_3

- (i) "Zeolite (I)"

 Zeolite (I) (Si/Al = 1) contains more aluminium than zeolite (II) (Si/Al = 2), consequently it possess relatively higher number of exchangeable cation sites.
- (ii) "Zeolites with high Si/Al"

 In high silica zeolites, there is fewer number of acid sites than the lower one.

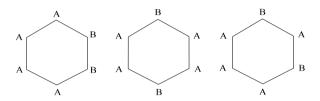
 In addition, electronegativity of Si is slightly higher than Al. Therefore, the more Si in the framework, the more electronegative the framework.

 Accordingly, strength of an acid site in such framework is markedly stronger than that of the other.

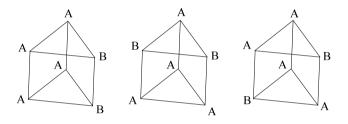
(iii) "Zeolite containing Li"
Li is the smallest alkali cation. Its charge density is very high, so it would strongly interact with water.

Problem 13

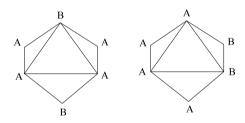
a) (i) For A1, there are three possible geometrical isomers.



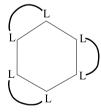
For A2, there are also three possible geometrical isomers.



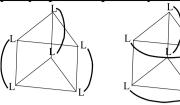
For A3, only two geometrical isomers are possible.



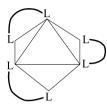
(ii) For A1, there is only one geometrical isomer but no optical isomer.

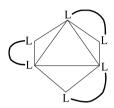


For A2, there are two geometrical isomers with no optical isomers.



For A3, two optical isomer existing in an enantiomeric pair.



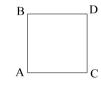


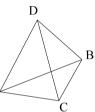
e)

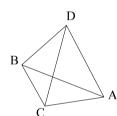
For the square planar geometry, there are three geometrical isomers, none has optical isomer. For the tetrahedral geometry there is only one geometrical arrangement which can exist as a pair of enantiomers.





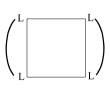






Both geometries can exist in one geometrical arrangement but no optical (ii) isomer.





Problem 14

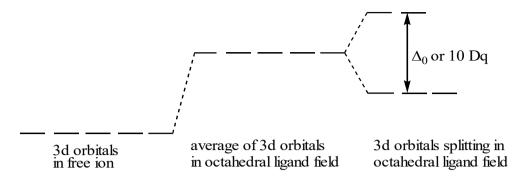
The electronic configuration of Co and Co³⁺ are as follows. a)

 $\begin{array}{lll} Co & : \ 1s^2 \ 2s^2 \ 2p^6 \ 3s^2 \ 3p^6 \ 3d^7 \ 4s^2 \\ Co^{3+} & : \ 1s^2 \ 2s^2 \ 2p^6 \ 3s^2 \ 3p^6 \ 3d^6 \end{array}$

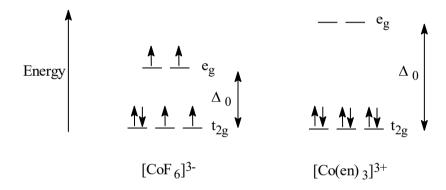
 ${\rm Co^{3^+}}$ ion is in octahedral crystal field. The electrons in d orbitals will be repelled by the field from the surrounding ligands. As a result, the d ${\rm x^2-y^2}$ and d ${\rm z^2}$ orbitals, which point direct and

head-on toward the ligands will be repelled strongly and raised in energy. The rest of the d orbitals, d_{xy} , d_{xz} and d_{yz} , point into the space between the ligands, their energies are thus

relatively unaffected by the field. These two sets of d orbitals are designated as e_g and t_{2g} , respectively, and their energy difference is designated as Δ_0 or 10 Dq. The crystal field splitting diagram is shown below.



Different ligands split the d-orbital energies to different extents. Strong field ligands lead to a larger crystal field splitting energy (larger Δ_0); weak field ligands lead to a smaller splitting energy (smaller Δ_0). In the case of $[CoF_6]^{3-}$ ion, Δ_0 is smaller than that of $[Co(en)_3]^{3+}$ ion. The splitting energy (Δ_0) and the orbital occupancy for these two complex ions are shown below.



The complex ion $[CoF_6]^{3-}$ has all its six electrons distributed in the high spin configuration , as a result there are four unpaired electrons so it is paramagnetic. Its magnetic moment, μ , can be estimated from the 'spin-only' formula.

$$\mu = \sqrt{n(n+2)}$$
 B.M.

where n is the number of unpaired electron. For $[CoF_6]^{3-}$, n = 4, therefore, $\mu = 4.89$ B.M.

While in $[Co(en)_3]^{3+}$ ion all electrons are paired in the low spin configuration leading to a diamagnetic property. Since, for $[Co(en)_3]^{3+}$, n = 0, therefore, $\mu = 0$ B.M.

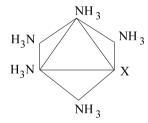
The complex ion $[CoF_6]^{3\text{-}}$ has smaller Δ_0 , so it should absorb at longer λ .

b) The information contained in the table of relationship of wavelengths to colors in Problem 14 is useful in working out for the answers.

Table Rewritten formula and color of complexes.

Complexes	$\lambda\square_{\max}$,	Color	
	nm		
1. [Co(NH ₃) ₆]Cl ₃	475	Yellowish red	
Hexaamminecobalt(III) chloride			
2. $[Co(H_2O)(NH_3)_5](NO_3)_3$	495	Red	
Aquopentaamminecobalt(III) nitrate			
3. $[Co(CO_3)(NH_3)_5]NO_3$	510	Red	
Carbonatopentaamminecobalt(III) nitrate			
4. $[CoF(NH_3)_5](NO_3)_2$	515	Red	
Fluoropentaamminecobalt(III) nitrate			
5. [CoCl(NH ₃) ₅]Cl ₂	534	Reddish violet	
Chloropentaamminecobalt(III) chloride			
6. [CoBr(NH ₃) ₅]Br ₂	552	Violet	
Bromopentaamminecobalt(III) bromide			

- (i) The IUPAC formula and the complex parts are shown in [] in the Table above.
- (ii) All these complexes can be written in the general form as $[\text{Co(NH}_3)_5\text{X}]^{(3-n)^+} \text{ where } n=0 \text{ , 1 or 2 depending on X groups. } (X=\text{NH}_3 \text{ , } \text{H}_2\text{O , CO}_3^{2^-} \text{ , } \text{F}^- \text{ , Cl}^- \text{ , Br}^- \text{)}.$

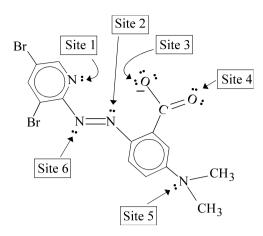


The different in λ_{max} arise from the nature of different X groups which exert repulsion on the electrons of the d orbitals. The stronger the X group bonds to the central metal atom the stronger repulsion would be, rendering shift of λ_{max} to the lower nm (higher energy) or larger Δ_0 as described in a). From the λ_{max} shift, we can arrange the strength of X as follows.

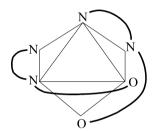
$$NH_3 > H_2O > CO_3^{2-} > F^- > Cl^- > Br^-$$
c)

- (i) Referring to the wavelength absorbed and the color, free BBDAB absorbs at 428 nm (curve A), so the color of free BBDAB should be yellow. For Co-BBDAB complex (curve B) the absorption appears at 540 nm, so the color of the complex would be red-violet.
- (ii) The structure of 3,5-diBr-PAMB is rewritten to expose the lone pair electrons it possesses. The atoms with lone pair electrons are the potential sites that can bond to the metal atom. There are six sites altogether, but only some of them will be available to bonding. Of these, sites 1, 2, and 3 can bond

simultaneously leading to the chelate complex which is more stable compared with the other sites. The rest, sites 4, 5, and 6, can bond one at a time as a monodentate ligand which is less stable. Sites 3 and 4 can be used together as a bidentate ligand, too, but is also less stable.



One form of the tentative complex is shown, by using sites 1, 2, and 3 to form a chelate complex. The complex consists of one metal atom and two molecules of 3,5-diBr-PAMB.



(iii) The color of the complexes can be deduced as follows.

Complex with reagent 1: red violet Complex with reagent 2: blue green Complex with reagent 3: red violet Complex with reagent 4: red violet Complex with reagent 5: violet Complex with reagent 6: blue green

Problem 15

(i)		Cr	\mathbf{C}	Н	O	
	Elemental composition	27.1	25.2	4.25	43.45	% by mass.
	Atomic weight	52	12	1	16	
	Number of moles	0.52	2.1	4.25	2.71	
	Moles ratio	1	4.04	8.17	5.21	
	From the mole ratio, the empirical formula woul					$CrC_4H_8O_5$.

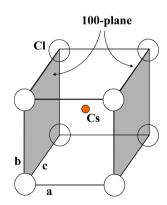
(ii) From the empirical formula CrC₄H₈O₅, the compound is [Cr(CH₃COO)₂(H₂O)]. Therefore, the ligands are acetate groups. Since the acetate group (CH₃COO) has a charge of -1, therefore, the oxidation state of Cr is 2⁺.

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(iii) Cr²⁺ ion is a d⁴ system, i.e., having 4 electrons in the d orbitals. The distribution of four electrons should be in the high spin type due to the low strength of the ligands. This alone would make [Cr(CH₃COO)₂(H₂O)] a paramagnetic species. However, from the experimental result this compound is, in fact, a diamagnetic compound. This is because the compound exists in the dimer form as shown.

In this structure, the two Cr atoms form a quadruple bond consisting of one sigma, two pi, and one delta bonds, giving a total bond order of four. The formation of the quadruple bond requires that all the d orbital electrons must be paired up. Therefore, in term of magnetic property, the compound in the dimer form is diamagnetic.

- (i) P
- (ii) The simplest (or empirical) formula is CsCl. Number of Cs atom (at the center) = 1 Number of Cl atoms = $(1/8) \times 8 = 1$ Cs: Cl = 1:1
- (iii) Coordination number is 8.
- (iv) From the given information, the distance between the (100)plane can be calculated by using Bragg's Law.



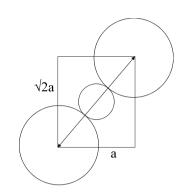
2d sin
$$\theta$$
 $\Box = n \lambda$
d $= n\lambda / 2\sin \theta$
 $= (1)(1.542) / (2)(0.1870)$
 $= 4.123 \text{ Å}$

That is the distance between (100)-planes, a, is 4.123 Å. For the cubic cell, a = b = c, therefore the volume of the cell = $(4.123)^3$ = 70.09 Å³.

(v) Density =
$$w/v = Z.M/v$$

= $(1 \times 168.36 \text{ g.mol}^{-1})/[(6.02 \times 10^{23} \text{ mol}^{-1})(4.123 \times 10^{-8} \text{ cm})^3]$
= 3.99 g.cm^{-3}

(vi) The diagonal plane of the unit cell can be shown below.



$$\begin{array}{lll} a^2 + (\sqrt{2}.a)^2 & = & (2.r_{Cs} + 2.r_{Cl})^2 \\ 3.a^2 & = & (2.r_{Cs} + 2(1.81))^2 \\ \sqrt{3}.a & = & 2.r_{Cs} + 3.62 \\ r_{Cs} & = & (\sqrt{3}.a - 3.62) / 2 \\ & = & (\sqrt{3} \times 4.123 - 3.62) / 2 \\ & = & 1.76 \quad \mathring{A}. \end{array}$$

Problem 17

a)

(i) Here, a buffer of H₃PO₄ and H₂PO₄ is present

$$[H_{3}PO_{4}] = [H_{2}PO_{4}^{-}]$$

$$[H^{+}] = K_{1} \frac{[H_{3}PO_{4}]}{[H_{2}PO_{4}^{-}]}$$

$$= K_{1} = 7.1x10^{-3} M$$

$$pH = -log (7.1x10^{-3}) = 2.15$$

(ii) At the 2 nd equivalent point, HPO₄²⁻ is present therefore

$$[H^+] = (K_2 K_3)^{1/2}$$

$$= [(6.2x10^{-8})(4.4x10^{-13})]^{1/2}$$

$$= 1.7x10^{-10} M$$

$$pH = -log (1.7x10^{-10}) = 9.77$$

(iii) HPO $_4^{2-}$ (K₃ = 4.4x10⁻¹³) is not really a much stronger acid than H₂O

 $(K_w = 1.00 \times 10^{-14})$. Addition of strong base to HPO₄²⁻ solution is similar to addition of a strong base to water.

b) Since the formation constant for $Ag(S_2O_3)_2^{3-}$, $K_f = \frac{1}{K_d} = 1.667 \times 10^{13}$ is very large, therefore most of the added Ag^+ forms complex with $S_2O_3^{2-}$ and

$$[Ag(S_2O_3)_2^{3-}] = \frac{20 \text{ mmol}}{200 \text{ ml}} = 0.100 \text{ M}$$
mmol of free $S_2O_3^{2-} = 530\text{-}(2x20) = 490 \text{ mmol}$

$$[S_2O_3^{2-}] = \frac{490 \text{ mmol}}{200 \text{ ml}} = 2.450 \text{ M}$$

concentration of free Ag⁺ calculated from Kd

$$K_d = \frac{[Ag^+][S_2O_3^{2-}]^2}{[Ag(S_2O_3)_2^{3-}]} = 6.0x10^{-14}$$

$$[Ag^{+}] = \frac{6.0x10^{-14}[Ag(S_{2}O_{3})_{2}^{3-}]}{[S_{2}O_{3}^{2-}]^{2}} = \frac{6.0x10^{-14}(0.100)}{(2.450)^{2}} = 1.0x10^{-15}$$

$$I^- + Ag^+ \longrightarrow AgI(s)$$

$$K_{sp} = [Ag^{+}][I^{-}] = 8.5x10^{-17}$$

 $(1x10^{-15})(I^{-}) = 8.5x10^{-17}$

[I⁻] =
$$\frac{8.5 \times 10^{-17}}{1.0 \times 10^{-15}}$$
 = 8.5×10^{-2} M

mmol KI =
$$(8.5 \times 10^{-2})(200)$$

= 17.0 mmol

Problem 18

a) Ans: p-nitro-di-Bolane is suitable indicator but not di-Bolane For di-Bolane,

$$E_{\text{solution}} = E_{\text{dip}}^{\text{o}} + \frac{0.059}{2} \log \frac{[\text{In}_{\text{ox}}]}{[\text{In}_{\text{red}}]}$$

When
$$[In_{ox}] / [In_{red}] = 10$$

$$E_{solution} = 0.76 + \frac{0.059}{2} \log 10 = 0.79$$

At 0.79 V, calculate $[Fe^{3+}]$ / $[Fe^{2+}]$

$$E_{\text{solution}} = E_{\text{Fe}}^{\text{o}} - \frac{0.059}{1} \log \frac{[\text{Fe}^{2+}]}{[\text{Fe}^{3+}]}$$

$$0.79 = 0.77 + 0.059 \log \frac{[\text{Fe}^{3+}]}{[\text{Fe}^{2+}]}$$

$$\frac{[\text{Fe}^{3+}]}{[\text{Fe}^{2+}]} = 2.2$$

Di-Bolane is not suitable indicator because $[Fe^{3+}]$ is 2.2 times $[Fe^{2+}]$ For *p*-nitro-di-Bolane

$$E_{\text{solution}} = E_{\text{pn}}^{\text{o}} + \frac{0.059}{2} \log \frac{[\text{In}_{\text{ox}}]}{[\text{In}_{\text{red}}]}$$

When $[In_{ox}] / [In_{red}] = 10$

$$E_{\text{solution}} = 1.01 + \frac{0.059}{2} \log 10 = 1.04 \text{ V}$$

At 1.04 V, calculate $[Fe^{3+}]$ / $[Fe^{2+}]$

$$E_{solution} = E_{Fe}^{o} + \frac{0.059}{1} log \frac{[Fe^{2+}]}{[Fe^{3+}]}$$

1.04 = 0.77 + 0.059
$$\log \frac{[Fe^{3+}]}{[Fe^{2+}]}$$

$$\frac{[Fe^{3+}]}{[Fe^{2+}]} = 3.80x10^4$$

b)

- (i) Sodium oxalate, Na₂C₂O₄
- (ii) $MnO_{4}^{-}(aq) + 8H^{+}(aq) + 5e^{-} \longrightarrow Mn^{2+}(aq) + 4H_{2}O(1)$ $E^{o} = +1.51 \text{ V}$

The Nernst equation is

$$E = E^{\circ} - \frac{RT}{5F} \ln \frac{[Mn^{2+}]}{[MnO_{4}^{-}].[H^{+}]^{8}}$$

or

E = 1.51 -
$$\frac{(257 \times 10^{-3})}{5} \ln \frac{[\text{Mn}^{2}]}{[\text{Mn}^{2}][\text{H}^{+}]^{8}}$$

or

$$E = 1.51 - \frac{(59.2 \times 10^{-3})}{5} \log \frac{[Mn^{2+}]}{[MnO_{4}^{-}].[H^{+}]^{8}}$$

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- (iii) One mole of electron is required for one mole of the gaseous product. Half reaction is $C_2O_4^{2-}$ (aq) \longrightarrow $2CO_2(g) + 2e^-$
- (iv) Ten moles of electron is involved in overall reaction.
- (v) The overall or net reaction of compound A and potassium permanganate.

$$2\text{MnO}_{4}^{-}(aq) + 5\text{C}_{2}\text{O}_{4}^{2-}(aq) + 16\text{H}^{+}(aq) \longrightarrow 2\text{Mn}^{2+}(aq) + 10\text{CO}_{2}(aq) + 8\text{H}_{2}\text{O}(aq)$$

- (vi) $Na^+ [1s^2 2s^2 2p^6]$
- (vii) Stoichiometric ratio = $\frac{\text{mol KMnO}_4}{\text{mol Na}_2\text{C}_2\text{O}_4} = \frac{2}{5}$

Therefore, the molarity of the potassium permanganate solution is 0.00146 M.

- (viii) No, since $E^{o}(M^{+}, M) = +1.69 \text{ V}$ is higher than the standard potential of potassium permanganate.
- (ix) The biological standard potential (at pH 7) of the half reaction is 1.69 V.

Problem 19

a)

(i) From

HA(aq)
$$+ A^{-}(aq) = K_a = \frac{[H^{+}]_{aq}[A^{-}]_{aq}}{[HA]_{aq}}$$

$$HA(aq)$$
 \longrightarrow $HA(org)$ $K_d = \frac{[HA]_{org}}{[HA]_{aq}}$

Distribution ratio (D) can be estimated as

$$D = \frac{[HA]_{org}}{[HA]_{aq} + [A^{-}]_{aq}}$$

$$= \frac{[HA]_{org}/[HA]_{aq}}{[HA]_{aq}/[HA]_{aq} + [A^{-}]_{aq}/[HA]_{aq}}$$

$$= \frac{K_{d}}{1 + K_{a}/[H^{+}]}$$

(ii) From answer (i)

$$\begin{array}{rll} & log \; D \; = \; log \; K_d \text{ - } log \; (1 + K_a/[H^+]) \\ at \; low \; pH : & [H^+] >> K_a \\ & log \; D \; = \; log \; K_d \; = \; constant \\ & D \; = \; K_d; \; \; K_d \; = \; 5.190 \; \; (average \; of \; 5.200, \; 5.180 \; and \; 5.190) \\ at \; high \; pH : & [H^+] << K_a \\ therefore \end{array}$$

$$log D = log K_d - log K_a/[H^+]$$

$$\begin{array}{lll} log \ D &=& log \ K_d \text{ - } log & K_a \text{ - } pH \\ \\ Therefore, & log \ K_d \text{ - } log \ K_a = 6.70 \\ K_a &=& 1.02 x 10^{-6} \end{array}$$

b)

- (i) Resolution, $R_S = 2[(t_R)_B (t_R)_A] / (W_A + W_B)$ = 2[(17.63-16.40)] / (1.11+1.21)= 1.06
- (ii) The number of theoretical plates, $N = 16(t_R/W)^2$ For the first peak, $N = 16(16.40/1.11)^2 = 3493$ for the second peak, $N = 16(17.63/1.21)^2 = 3397$

The average number of plates, $N_{av} = (3493+3397)/2 = 3495 \sim 3.4 \times 10^3$

(iii) The plate height (H) can be calculated from L/N when L = column length and N = number of theoretical plates. H = $30.0 \text{ cm}/3445 = 8.7 \text{x} 10^{-3} \text{ cm}$

(iv)
$$N = 16 R_S^2 (\frac{\alpha}{\alpha - 1})^2 (\frac{1 + k_B'}{k_B'})^2$$

The capacity factor (k') and the selectivity factor (α) do not change with N or L, therefore

$$(R_s)_1/R_s)_2 = \sqrt{N_1} / \sqrt{N_2}$$

where subscripts 1 and 2 refer to the original and the longer columns, respectively.

1.06/1.5 =
$$\sqrt{3.4 \times 10^3} / \sqrt{N_2}$$

N₂ = 6.9x10³
L = N.H = 60 cm

Problem 20

a) For peaks in the molecular ion cluster, three peaks are expected from two chlorine atoms. The intensities can be calculated from $(a+b)^n$

where $a = \text{relative abundance of the light isotope } (^{35}\text{Cl})$

 $b = relative abundance of the heavy isotope (<math>^{37}Cl$)

n = number of halogen atoms present.

Since the relative abundance of $^{35}Cl = 75.77$ and that of $^{37}Cl = 24.23$, it can be assumed then that their relative abundances are $^{35}Cl = 3$ and $^{37}Cl = 1$ for purpose of convenience.

(i) Relative intensties of the peaks at m/z 84, 86 and 88 = $a^2 + 2ab + b^2$ = $3^2 + 2x3x1 + 1^2$

That is, the relative intensities for m/z 84:86:88 = 9:6:1

(ii) As for the peaks at m/z 49 and 51, corresponding to the loss of one chlorine atom from the molecular ion, the two peaks are due to CH₂ ³⁵Cl⁺ and CH₂ ³⁷Cl⁺, respectively.

Relative intensity of the peak at m/z 49 and 51 = a + b

= 3 + 1

That is, the relative intensities for m/z 49:51 = 3:1

b) In terms of the relative abundance, 79 Be: 81 Br = $50.69:49.31\approx1:1$. Relative intensities of the isotopic peaks can be calculated from $(a+b)^n$

where $a = relative intensity of ^{79}Br = 1$

 $b = relative intensity of ^{81}Br = 1$

n = number of halogen atoms present = 3

Relative intensities $= a^3 + 3a^2b + 3ab^2 + b^3$ M: $(M+2): (M+4): (M+6) = 1^3: 3x1^2x1: 3x1x^2: 1^3 = 1:3:3:1$

Problem 21

(i) From Beer's Law, $A = \varepsilon bc$

$$\begin{split} \epsilon_{X}{}^{440} & = \frac{0.096}{1.00 \, x \, 8.00 \, x \, 10^{-5}} \, = \, 1.2 x 10^{3} \quad \text{cm}^{-1} \, \text{mol}^{-1} \, \text{L} \\ \epsilon_{X}{}^{660} & = \frac{0.373}{1.00 \, x \, 8.00 \, x \, 10^{-5}} \, = \, 4.67 x 10^{3} \quad \text{cm}^{-1} \, \text{mol}^{-1} \, \text{L} \\ \epsilon_{Y}{}^{440} & = \frac{0.600}{1.00 \, x \, 2.00 \, x \, 10^{-4}} \, = \, 3.00 x 10^{3} \quad \text{cm}^{-1} \, \text{mol}^{-1} \, \text{L} \\ \epsilon_{Y}{}^{660} & = \frac{0.030}{1.00 \, x \, 2.00 \, x \, 10^{-4}} \, = \, 1.50 x 10^{2} \quad \text{cm}^{-1} \, \text{mol}^{-1} \, \text{L} \end{split}$$

(ii) At 520 nm

Absorbance =
$$A_X + A_Y$$

= $\frac{3.00x10^{-5}}{8.00x10^{-5}} \times 0.113 + \frac{5.00x10^{-4}}{2.00x10^{-4}} \times 0.433$
= 1.125

At 600 nm

Absorbance =
$$A_X + A_Y$$

= $\frac{3.00 \times 10^{-5}}{8.00 \times 10^{-5}} \times 0.264 + \frac{5.00 \times 10^{-4}}{2.00 \times 10^{-4}} \times 0.100$
= 0.349

(iii) At 440 nm

$$0.400 = 1.2x10^3 C_X + 3.0x10^3 C_Y$$

At 660 nm

$$0.500 = 4.67x10^3 C_X + 1.5x10^2 C_Y$$

The above two equations can be solved for C_X and C_Y

$$C_X$$
 = 1.04x10⁻⁴ M
 C_Y = 9.17x10⁻⁵ M