

**ENED 1091**  
**Midterm Exam Review**  
**of Concepts and Practice Problems**

# Arrays Review

- Arrays allow you to store and access data easily and in a programmatic way
- There are two main types of arrays we've used:
  - 1-dimensional arrays (also called vectors)
  - 2-dimensional arrays (also called array or matrix)

# Arrays Review

- The number of dimensions in an array determines how the data is stored and accessed:
  - Vectors have a single dimension, and thus a single index to access data:  
`vector_name(index)`
  - Arrays have two dimensions, requiring multiple indices to access data:  
`array_name(row_index,col_index)`
- Remember: indices always start at 1!

# Arrays Practice

- Assuming that A is created as shown below, determine the results of the following commands:

```
>> A = [9 8 7 6 5 4 3 2 1 0];
```

```
>> A(2)
```

```
>> A(1:4)
```

```
>> A(2:2:end)
```

```
>> A([1 3 5 7 9])
```

```
>> A.^2
```

```
>> A >= 3 & A < 6
```

# Arrays Practice

- Assuming that A is created as shown below, determine the results of the following commands:

```
>> A = [1 2 3 4; 5 6 7 8; 9 10 11 12];
```

```
>> A(2,3)
```

```
>> A(1,:)
```

```
>> A(:,4)
```

```
>> A(1:2,3:4)
```

```
>> A([1 3],[1 3])
```

```
>> A > 3 & A < 10
```

# Nested Loops Review

- Nested loops consist of one loop inside another
- You can nest any type of loop inside another
  - Most commonly used this semester was a for inside a for
- With nested loops, the inner loop will complete all iterations for every one iteration of the outer loop

# Nested Loops Practice

Determine the result of running the following script in MATLAB:

```
x = [1  2  3];  
y = [1  3  5  7];  
for r = 1:length(x)  
    P(r) = x(r);  
    for c = 1:length(y)  
        P(r) = P(r) + (-1)^r*y(c);  
    end  
end  
disp('P=');disp(P)
```

# Nested Loops Practice

- Consider the following code and determine the output when it is executed:

```
X = [1 2 3; 4 5 6; 7 8 9];
[rows cols] = size(X);
for r = 1:rows
    for c = 1:cols
        Y(r,c) = sum(X(r:3,c));
    end
end
disp('X = '); disp(X);
disp('Y = '); disp(Y);
```



# Nested Loops Practice

The voltage across the capacitor in a series RC circuit with a voltage source of 12 volts is:

$$V_{cap}(t) = 12(1 - e^{-\frac{t}{RC}})$$

Create a vector for time that starts at 0, increments by 0.01, and ends at 12. Create a vector of resistances that starts at 1000, increments by 500, and ends at 3000. Assume  $C = 0.001$ .

Using nested loops, go through each entry in the time vector and each entry in the resistance vector to create a matrix of capacitor voltages. Plot the results.

Note: this could be done without nested loops but the point is to practice nested loops!

# Array Functions Review

- There are a number of functions that are useful when dealing with arrays:
  - **length**: determines the number of entries in a vector
  - **size**: determines the number of elements along different dimensions of an array
  - **min**: determines the minimum value
  - **max**: determines the maximum value
  - **sum**: adds the values in an array
  - **find**: gives the index for any non-zero value in an array
  - **mean**: determines the average value

# Array Functions Practice

- What do each of the following commands do?

1-D Array

2-D Array

– sum()

– max()

– min()

– find()

# Array Functions Practice

- Assuming that A is created as shown below, determine the results of the following commands:

```
>> A = [4 5 3 1 8 9 5 7 2];
```

```
>> length(A)
```

```
>> sum(A)
```

```
>> max(A)
```

```
>> min(A(7:9))
```

```
>> find(A == 5)
```

# Array Functions Practice

- Assuming that A is created as shown below, determine the results of the following commands:

```
>> A = [4 5 7 6; 1 8 2 4; 3 9 7 1];
```

```
>> [a, b] = size(A)
```

```
>> sum(A)
```

```
>> max(A(3, :))
```

```
>> min(min(A))
```

```
>> sum(sum(A == 7))
```

# Array Functions Practice

- Assuming that A is created as shown below, determine the results of the following commands:

```
>> A = [4 5 7 6; 1 8 2 4; 3 9 7 1];
```

**Result:**

```
>> sum(A(2,:) >= 2) 3
```

```
>> sum(A(2,:) >= 2 & A(3,:) <= 7) 2
```

```
>> n = find(A(:,1) >= 2); mean(A(n,4)) 3.5
```

(Note: n would be [1 3])

# Matrix Operations

$$A = \begin{bmatrix} Y & Z & 8 \\ 2 & 7 & -3 \end{bmatrix} + \begin{bmatrix} 5 & -2 & 12 \\ 4 & 7 & -2 \end{bmatrix}$$

$$A = ?$$

# Matrix Operations

Which of the following are invalid matrix operations?

$$\begin{bmatrix} 2 \\ 1 \\ -2 \\ Z \end{bmatrix} \times \begin{bmatrix} 4 & -1 & Y \end{bmatrix}$$

$$\begin{bmatrix} 2 \\ 1 \\ -2 \\ Z \end{bmatrix} \times \begin{bmatrix} Y \\ 1 \\ 3 \\ 7 \end{bmatrix}$$

$$\begin{bmatrix} Z & 0 \\ -1 & 1 \\ 1 & 2 \end{bmatrix} \times \begin{bmatrix} 4 & 0 & Y \\ 5 & -3 & 2 \end{bmatrix}$$



# Matrix Operations

$$A = \begin{bmatrix} 2 \\ 1 \\ -2 \\ Z \end{bmatrix} \times \begin{bmatrix} 4 & -1 & Y \end{bmatrix}$$

$$A = ?$$

# Solving Systems of Linear Equations

Set up the matrix equation for the following set of linear equations. How do we determine whether or not there is a unique solution?

$$3x + 2y - z = 6$$

$$4x - 3y + 2z = 12$$

$$x + y - 5z = 4$$

# Solving Systems of Linear Equations

Set up the matrix equation for the following set of linear equations. How do we determine whether or not there is a unique solution?

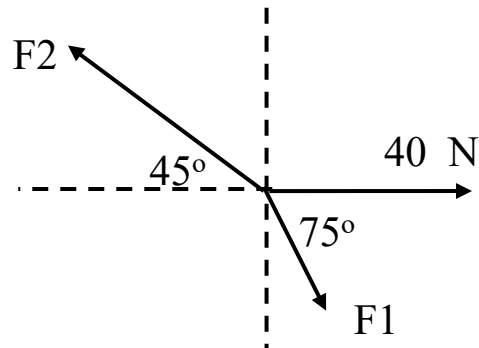
$$2v + x + 2y + z = 4$$

$$v + 5x - y - 3z = 1$$

$$4v - 2x + 6y - z = -16$$

$$2v + 6x - 9z = 10$$

# Force Balance Equations



Write the matrix equation for the force balance equations.

# Circuit Mesh Equations

Homework #5 – Problems 4 and 5

Lecture: Week 6