

Conservation of mass

$$\frac{\partial}{\partial t} \int_{CV} \rho dV + \int_{CS} \rho \vec{V} \cdot d\vec{A} = 0$$

Momentum Equation

$$\vec{F} = \vec{F}_s + \vec{F}_b = \frac{\partial}{\partial t} \int_{CV} \vec{V} \rho dV + \int_{CS} \vec{V} \rho \vec{V} \cdot d\vec{A}$$

Continuity Equation

$$\frac{\partial \rho u}{\partial x} + \frac{\partial \rho v}{\partial y} + \frac{\partial \rho w}{\partial z} + \frac{\partial \rho}{\partial t} = 0$$

$$\nabla \cdot \rho \vec{V} + \frac{\partial \rho}{\partial t} = 0$$

incompressible: $\rho = \text{const.}$

S.S.: $\frac{\partial \rho}{\partial t} = 0$

$$\frac{1}{r} \frac{\partial (r \rho V_r)}{\partial r} + \frac{1}{r} \frac{\partial (r \rho V_\theta)}{\partial \theta} + \frac{\partial (\rho V_z)}{\partial z} + \frac{\partial \rho}{\partial t} = 0$$

$$\nabla \cdot \rho \vec{V} + \frac{\partial \rho}{\partial t} = 0$$

Acceleration:

$$\frac{D\vec{V}}{Dt} = u \frac{\partial \vec{V}}{\partial x} + v \frac{\partial \vec{V}}{\partial y} + w \frac{\partial \vec{V}}{\partial z} + \frac{\partial \vec{V}}{\partial t}$$

$$a_{rp} = \frac{Dv}{Dt} = u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + \frac{\partial v}{\partial t}$$

$$a_{yp} = \frac{Dv}{Dt} = u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} + \frac{\partial v}{\partial t}$$

$$a_{zp} = \frac{Dw}{Dt} = u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} + \frac{\partial w}{\partial t}$$

Navier-Stokes (incompressible, constant viscosity):

$$\rho \left(\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right) = \rho g_x - \frac{\partial p}{\partial x} + \mu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right)$$

$$\rho \left(\frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} \right) = \rho g_y - \frac{\partial p}{\partial y} + \mu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right)$$

$$\rho \left(\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} \right) = \rho g_z - \frac{\partial p}{\partial z} + \mu \left(\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right)$$

S.S.: $\frac{\partial}{\partial t} = 0$

incompressible flow $\rho = \text{const.}$

fully developed $\frac{\partial}{\partial x} = 0$

Bernoulli: $\frac{p}{\rho} + \frac{V^2}{2} + gz = \text{const.}$

1 slug = 32.2 lbm

1 $\frac{\text{ft} \cdot \text{slug}}{\text{s}^2} = 1 \text{ lbf}$

$g = 32.2 \frac{\text{ft}}{\text{s}^2} = 32.2 \frac{\text{ft}}{\text{s}^2}$

$g = 32.2 \frac{\text{ft}}{\text{s}^2} = 32.2 \frac{\text{lbf}}{\text{slug}}$

1 slug = 32.2 lbm

$0^\circ \text{F} = 32^\circ \text{C}$

$0^\circ \text{R} = 0^\circ \text{F} + 459.67$

$0^\circ \text{K} = 273.15^\circ \text{C}$

$0^\circ \text{K} = 0^\circ \text{F} + 459.67$

1 psi = 1 $\frac{\text{lbf}}{\text{in}^2}$

1 centipoise = 1 cP = $\frac{1}{100}$ poise

1 poise = 1 $\frac{\text{g}}{\text{cm} \cdot \text{s}}$

1 $\frac{\text{lbm}}{\text{ft} \cdot \text{s}} = 1.488 \frac{\text{kg}}{\text{m} \cdot \text{s}}$

1 lbm = 0.454 kg

1 ft = 0.3048 m