

# IF2240 – Basis Data Relational Database Design (part 2b)

SEVENTH EDITION

## Database System Concepts



# Sumber

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- Silberschatz, Korth, Sudarshan: "Database System Concepts", 7<sup>th</sup> Edition
  - Chapter 7: Relational Database Design

# Capaian

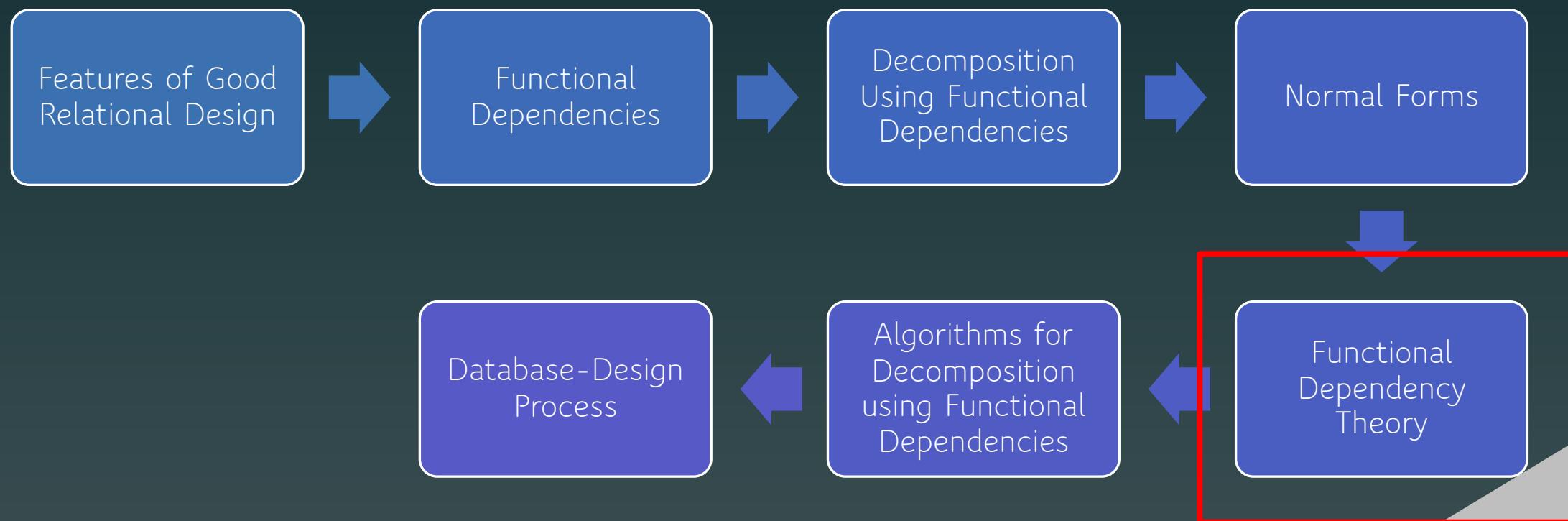
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- Mahasiswa dapat menghasilkan desain basis data relasional yang baik berdasarkan prinsip-prinsip yang diberikan



# Outline

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# Canonical Cover

The effort spent in checking for violations can be reduced by testing a simplified set of functional dependencies that has the same closure as the given set.



This simplified set is termed the **canonical cover**



To define canonical cover we must first define **extraneous attributes**.

An attribute of a functional dependency in  $F$  is **extraneous** if we can remove it without changing  $F^+$

# Extraneous Attributes

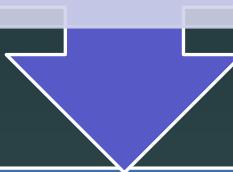
## Left-hand side

Removing an attribute from the **lhs** of a FD could make it a stronger constraint.

For example,  
removing B from  $AB \rightarrow C$ ,  
gives a possibly stronger  $A \rightarrow C$

It may be stronger because  
 $A \rightarrow C$  logically implies  $AB \rightarrow C$

But,  $AB \rightarrow C$  does not, on its  
own, logically imply  $A \rightarrow C$



But, we may be able to remove B from  $AB \rightarrow C$  safely.

For example, suppose that  
 $F = \{AB \rightarrow C, A \rightarrow D, D \rightarrow C\}$

Then we can show that  
 $F$  logically implies  $A \rightarrow C$ ,

making B extraneous in  $AB \rightarrow C$ .

# Extraneous Attributes

## Left-hand side

Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .



Attribute A is **extraneous** in  $\alpha$  if

$A \in \alpha$  and

$F$  logically implies  
 $(F - \{\alpha \rightarrow \beta\}) \cup \{(\alpha - A) \rightarrow \beta\}$ .



To test if attribute  $A \in \alpha$  is extraneous in  $\alpha$

Let  $\gamma = \alpha - \{A\}$ .

Check if  $\gamma \rightarrow \beta$  can be inferred from  $F$ .



# Extraneous Attributes

## Left-hand side

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 $(F - \{\alpha \rightarrow \beta\}) \cup \{(\alpha - A) \rightarrow \beta\}$ .



To test if attribute  $A \in \alpha$  is extraneous in  $\alpha$

Let  $\gamma = \alpha - \{A\}$ .

Check if  $\gamma \rightarrow \beta$  can be inferred from  $F$ .

Compute  $\gamma^+$  using the dependencies in  $F$

If  $\gamma^+$  includes all attributes in  $\beta$  then  $A$  is extraneous in  $\alpha$

- Let  $F = \{AB \rightarrow C, A \rightarrow B, B \rightarrow C\}$
- To check if  $B$  is extraneous in  $AB \rightarrow C$  we check if  $F$  implies  $F' = \{A \rightarrow C, A \rightarrow B, B \rightarrow C\}$
- Check if  $A \rightarrow C$  can be inferred from  $F$ 
  - Compute  $A^+$  under  $F$
  - $A^+$  is  $ABC$ , which includes  $C$
  - This implies that  $B$  is extraneous

# Extraneous Attributes

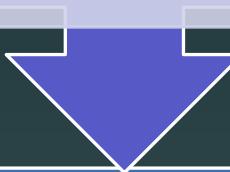
## Right-hand side

Removing an attribute from the **rhs** of a FD could make it a weaker constraint.

For example,  
if we have  $AB \rightarrow CD$   
and remove C,

we get the possibly weaker  
result  $AB \rightarrow D$ .

It may be weaker because  
using just  $AB \rightarrow D$ ,  
we can no longer infer  $AB \rightarrow C$ .



But, we may be able to remove C from  $AB \rightarrow CD$  safely.

For example, suppose that  
 $F = \{ AB \rightarrow CD, A \rightarrow C \}$

Even after replacing  $AB \rightarrow CD$   
by  $AB \rightarrow D$ ,  
we can still infer  $AB \rightarrow C$

and thus  $AB \rightarrow CD$ .

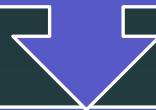


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# Extraneous Attributes

## Right-hand side

Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .



Attribute  $A$  is **extraneous** in  $\beta$  if

$A \in \beta$  and

$(F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$   
logically implies  $F$



To test if attribute  $A \in \beta$  is extraneous in  $\beta$

Let  $F' = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$

check that  $\alpha^+$  using  $F'$  contains  $A$ ;  
if it does,  $A$  is extraneous in  $\beta$

# Extraneous Attributes

## Right-hand side

Consider a set  $F$  of functional dependencies and the functional dependency  $\alpha \rightarrow \beta$  in  $F$ .

Attribute  $A$  is **extraneous** in  $\beta$  if

$A \in \beta$  and

$(F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$   
logically implies  $F$

To test if attribute  $A \in \beta$  is extraneous in  $\beta$

Let  $F' = (F - \{\alpha \rightarrow \beta\}) \cup \{\alpha \rightarrow (\beta - A)\}$

check that  $\alpha^+$  using  $F'$  contains  $A$ ;  
if it does,  $A$  is extraneous in  $\beta$

- Let  $F = \{AB \rightarrow CD, A \rightarrow E, E \rightarrow C\}$
- To check if  $C$  is extraneous in  $AB \rightarrow CD$ , we check if  $F' = \{AB \rightarrow D, A \rightarrow E, E \rightarrow C\}$  implies  $F$
- Check if  $AB \rightarrow CD$  can be inferred from  $F'$ 
  - Compute  $AB^+$  under  $F'$
  - $AB^+$  is  $ABCDE$ , which includes  $CD$
  - This implies that  $C$  is extraneous

# Canonical Cover

A **canonical cover** for  $F$  is a set of dependencies  $F_c$  such that

$F$  logically implies all dependencies in  $F_c$ , and

$F_c$  logically implies all dependencies in  $F$ , and

No functional dependency in  $F_c$  contains an extraneous attribute, and

Each left side of functional dependency in  $F_c$  is unique.

- That is, there are no two dependencies in  $F_c$ 
  - $\alpha_1 \rightarrow \beta_1$  and  $\alpha_2 \rightarrow \beta_2$  such that
    - $\alpha_1 = \alpha_2$

# Canonical Cover

Algorithm to compute a canonical cover for  $F$

$F_c := F$

**repeat**

    Use the union rule to replace any dependencies in  $F_c$  of the form  
         $\alpha_1 \rightarrow \beta_1$  and  $\alpha_1 \rightarrow \beta_2$  with  $\alpha_1 \rightarrow \beta_1 \beta_2$

    Find a functional dependency  $\alpha \rightarrow \beta$  in  $F_c$  with  
        an extraneous attribute either in  $\alpha$  or in  $\beta$

    /\* Note: test for extraneous attributes done using  $F_c$ , not  $F^*$  \*/

    If an extraneous attribute is found, delete it from  $\alpha \rightarrow \beta$

**until** ( $F_c$  not change)

Note: Union rule may become applicable after some extraneous attributes have been deleted, so it has to be re-applied

# Canonical Cover

$F_c := F$

repeat

    Use the union rule to replace any dependencies in  $F_c$  of the form  
         $\alpha_1 \rightarrow \beta_1$  and  $\alpha_1 \rightarrow \beta_2$  with  $\alpha_1 \rightarrow \beta_1 \beta_2$

    Find a functional dependency  $\alpha \rightarrow \beta$  in  $F_c$  with  
        an extraneous attribute either in  $\alpha$  or in  $\beta$

/\* Note: test for extraneous attributes done using  $F_c$  not  $F^*$  \*/

    If an extraneous attribute is found, delete it from  $\alpha \rightarrow \beta$

until ( $F_c$  not change)

Note: Union rule may become applicable after some extraneous  
attributes have been deleted, so it has to be re-applied

$R = (A, B, C)$

$F = \{A \rightarrow BC, B \rightarrow C, A \rightarrow B, AB \rightarrow C\}$

Combine  $A \rightarrow BC$  and  $A \rightarrow B$  into  $A \rightarrow BC$

- Set is now  $\{A \rightarrow BC, B \rightarrow C, AB \rightarrow C\}$

$A$  is extraneous in  $AB \rightarrow C$

- Set is now  $\{A \rightarrow BC, B \rightarrow C\}$

$C$  is extraneous in  $A \rightarrow BC$

- Set is now  $\{A \rightarrow B, B \rightarrow C\}$

The canonical cover is:  $\{ A \rightarrow B, B \rightarrow C \}$

# Dependency Preservation

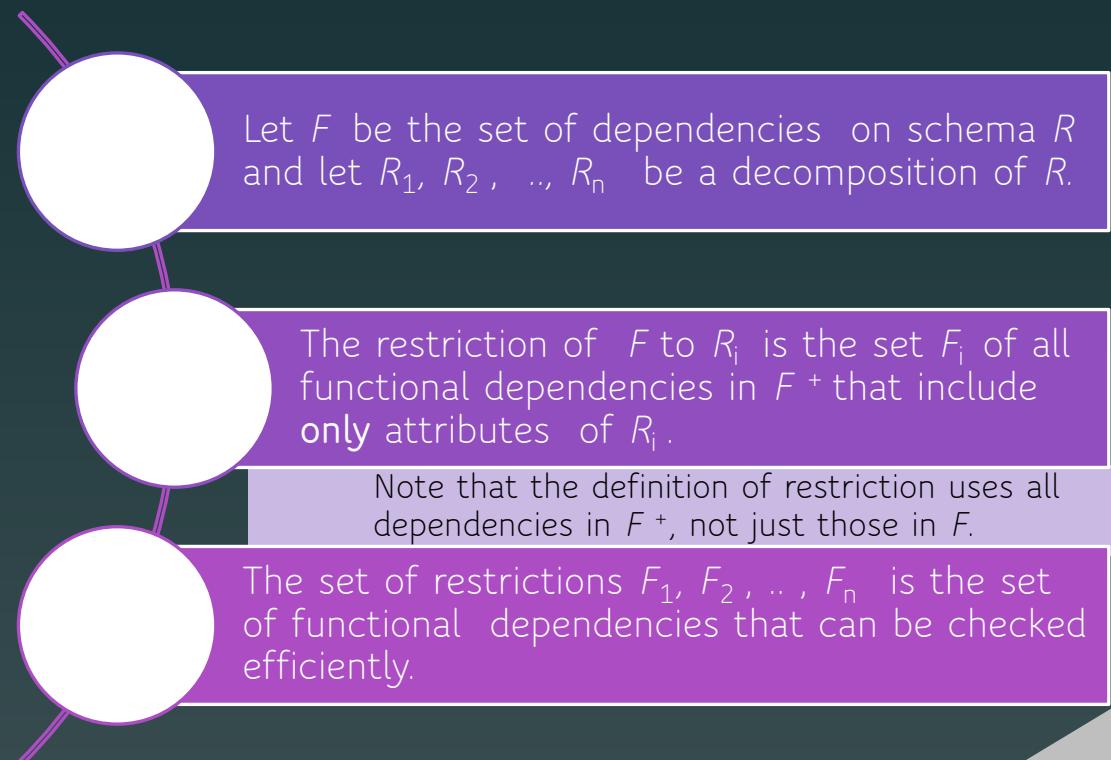
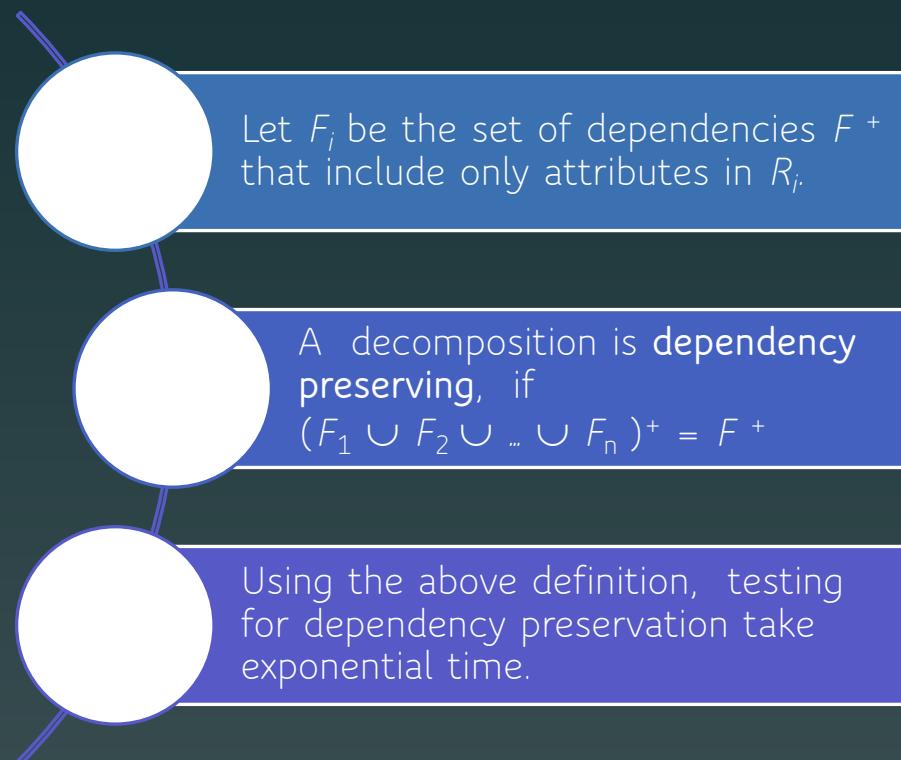
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Let  $F_i$  be the set of dependencies  $F^+$  that include only attributes in  $R_i$ .

A decomposition is **dependency preserving**, if  
 $(F_1 \cup F_2 \cup \dots \cup F_n)^+ = F^+$

Using the above definition, testing for dependency preservation take exponential time.

# Dependency Preservation



# Testing for Dependency Preservation

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- To check if a dependency  $\alpha \rightarrow \beta$  is preserved in a decomposition of  $R$  into  $R_1, R_2, \dots, R_n$ , apply the following test (with attribute closure done with respect to  $F$ )
- Apply the test on all dependencies in  $F$  to check if a decomposition is dependency preserving
- This procedure takes polynomial time

```
result =  $\alpha$ 
repeat
    for each  $R_i$  in the decomposition
         $t = (\textit{result} \cap R_i)^+ \cap R_i$ 
        result = result  $\cup t$ 
    until (result does not change)
```

If *result* contains all attributes in  $\beta$ , then the functional dependency  $\alpha \rightarrow \beta$  is preserved.

# Testing for Dependency Preservation

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```
result = α
repeat
    for each  $R_i$  in the decomposition
         $t = (result \cap R_i)^+ \cap R_i$ 
        result = result ∪ t
until (result does not change)
```

If  $result$  contains all attributes in  $β$ , then the functional dependency  $α → β$  is preserved.

$$\begin{aligned}R &= (A, B, C) \\F &= \{A \rightarrow B, B \rightarrow C\} \\Key &= \{A\}\end{aligned}$$

$R$  is not in BCNF

Decomposition  $R_1 = (A, B), F_1 = \{A \rightarrow B\}$   
 $R_2 = (B, C), F_2 = \{B \rightarrow C\}$

- $R_1$  and  $R_2$  in BCNF
- Lossless-join decomposition
- Dependency preserving

# Testing for Dependency Preservation

```
result = α
repeat
    for each  $R_i$  in the decomposition
         $t = (result \cap R_i)^+ \cap R_i$ 
        result = result  $\cup$  t
    until (result does not change)
```

If  $result$  contains all attributes in  $β$ , then the functional dependency  $α → β$  is preserved.

$$\begin{aligned}R &= (A, B, C) \\F &= \{A \rightarrow B, B \rightarrow C\} \\Key &= \{A\} \\&\quad R \text{ is not in BCNF}\end{aligned}$$

Decomposition  $R_1 = (A, B), F_1 = \{A \rightarrow B\}$   
 $R_2 = (A, C), F_2 = \{A \rightarrow C\}$

- $R_1$  and  $R_2$  in BCNF
- Lossless-join decomposition
- Not Dependency preserving
  - $A \rightarrow B$  is preserved
  - $B \rightarrow C$  is not preserved

result = B  
 $R_1:$   
 $(result \cap R_1)^+ = B^+ = BC$   
result =  $B \cup (BC \cap R_1) = B$   
 $R_2:$   
 $(result \cap R_2) = \emptyset$   
result = B

# Algorithm for Decomposition Using Functional Dependencies

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NEXT MEETING ...