

## 2-2 Treasure Hunting

(Monday, April 2, 2018 ~ Saturday, April 7, 2018)

Hengfeng Wei

hfwei@nju.edu.cn

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Problem of the Week (Monday, April 2, 2018 ~ Saturday, April 7, 2018)

- (a) Given an array  $A[0 \cdots n - 1]$ , to determine whether there is a value that *occurs more than  $\lfloor n/k \rfloor$  times* in  $\Theta(n \lg k)$  time and  $\Theta(k)$  extra space.
- (b) Prove that the *lower bound* of this problem is  $\Theta(n \lg k)$ .

# TIP#1

(Monday, April 2, 2018)

Take  $k = 2$ .

$\Theta(n)$  time &  $\Theta(1)$  space

# TIP#2

(Tuesday, April 3, 2018)

## Definition ( $k$ -simplified Multiset)

Consider a multiset  $\mathcal{M}$ . A  *$k$ -simplified multiset* for  $\mathcal{M}$  is a multiset derived from  $\mathcal{M}$  by repeating *deleting  $k$  distinct elements* from it until no longer possible.

## Theorem

*If a value occurs more than  $\lfloor n/k \rfloor$  times in  $\mathcal{M}$  of  $n$  elements, then it is in a  $k$ -simplified multiset for  $\mathcal{M}$ .*

Prove this theorem. Take  $k = 2$  again. Design an  $\Theta(n)$  algorithm for  $k = 2$ . Generalize it to an algorithm for general  $k$  (ignoring  $\Theta(n \lg k)$  for now).

# TIP#3

(Wednesday, April 4, 2018)

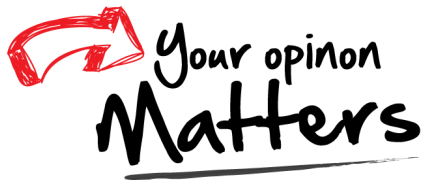
Today, you have an efficient data structure  $T$  for a multiset:

We denote a multiset by  $\mathcal{M} = \{(v_i, c_i)\}$ , where  $c_i$  is the number of times  $v_i$  occurs in  $\mathcal{M}$ . The number of distinct values in  $\mathcal{M}$  is denoted by  $d = |\{v_i\}|$ .

The data structure  $T$  for  $\mathcal{M}$  contains  $d$  nodes, each being a pair  $(v_i, c_i)$ . It supports INSERT, DELETE, and SEARCH in  $\Theta(\lg d)$ .

Use this data structure (you are not required to implement it) in your algorithm to achieve the time complexity of  $\Theta(n \lg k)$ .

Thank  
You!



Office 302

Mailbox: H016

hfwei@nju.edu.cn