

# Rational thoughts in neural codes

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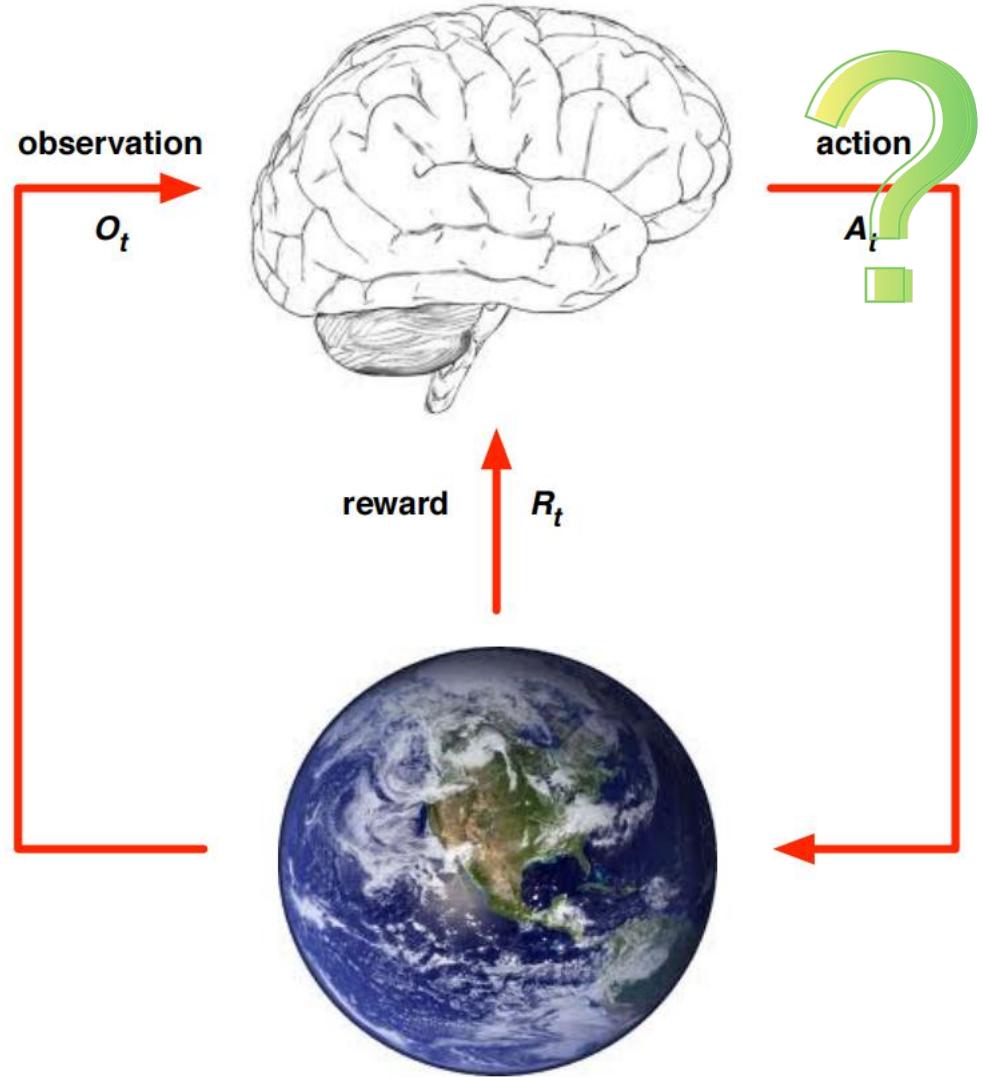
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Xaq Pitkow @ CMU, Neuroscience Institute, with affiliation to ML Department  
lab site: <https://xaqlab.com/>

presented by 陆杨帆, 张博涛

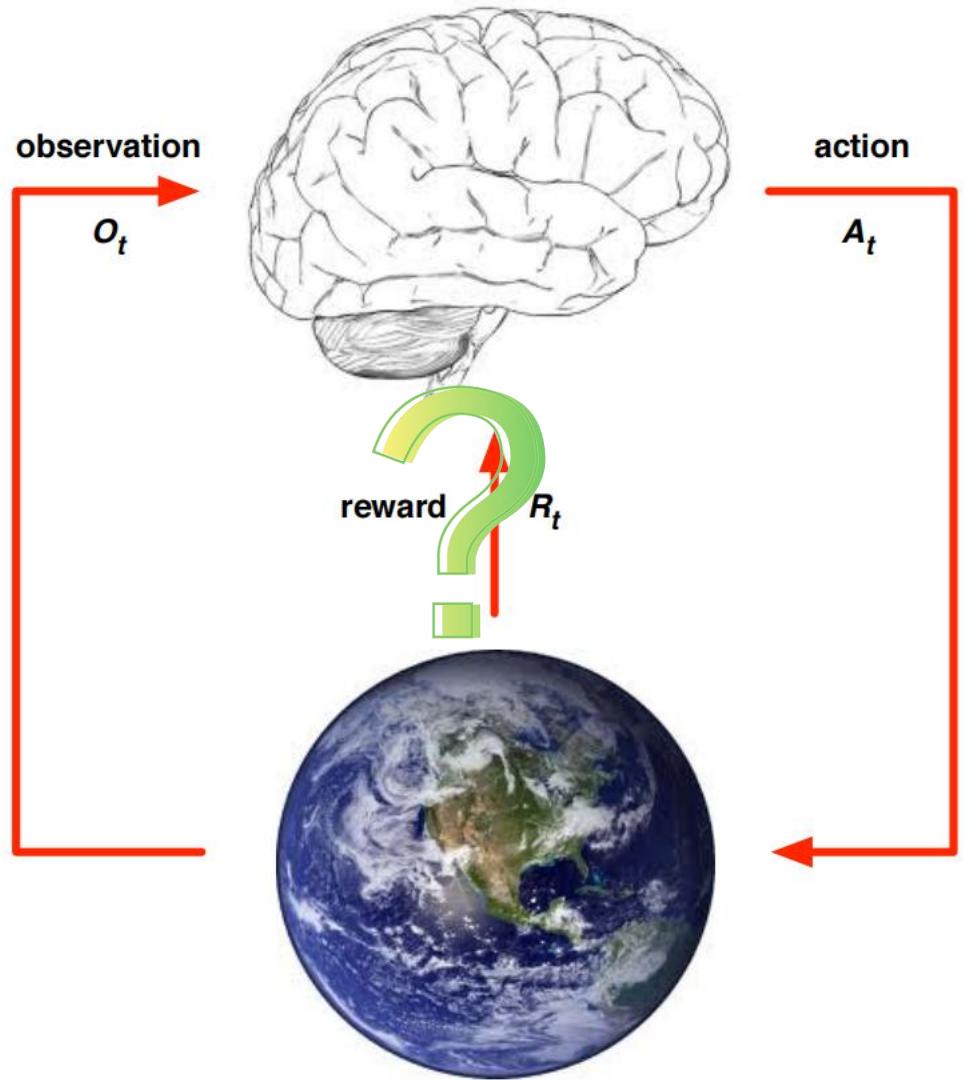
# Reinforcement Learning



Given: reward(, state)

What is the optimal action?

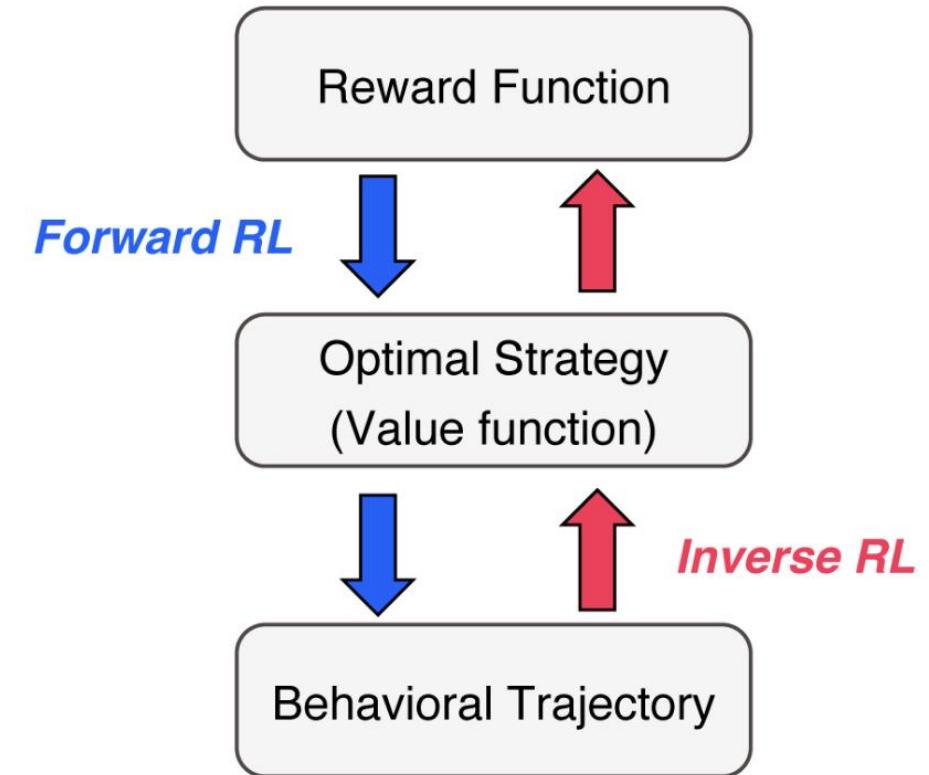
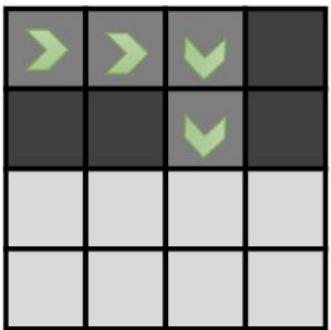
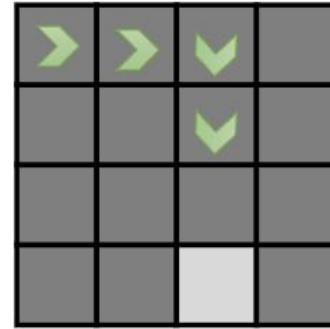
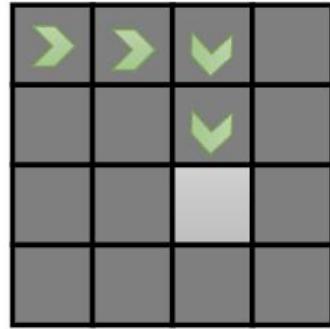
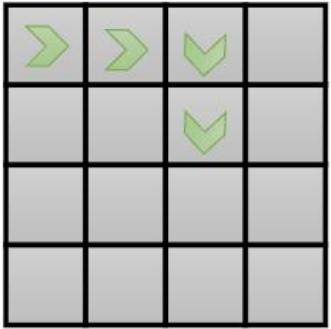
# Inverse Reinforcement Learning



Given: Action trajectory of an agent(mostly, an expert)

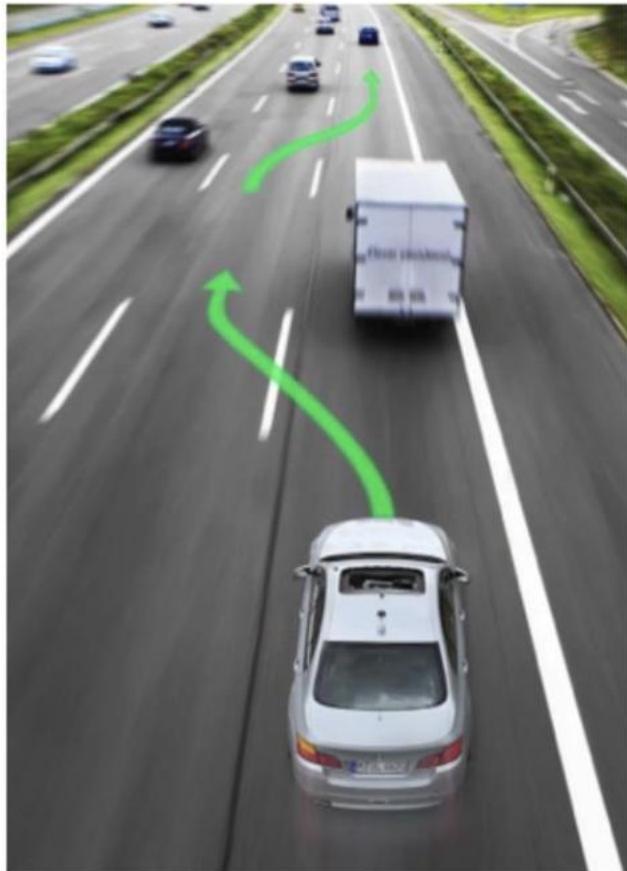
**What is the reward**(function that the agent is trying to maximize)?

# Inverse Reinforcement Learning



I saw him walking this way, what is his intention?  
i.e. What is the reward at each state(-action) that makes him act like this?

# Inverse Reinforcement Learning



maintaining safe following distance?

keeping away from the curb?

staying far from any pedestrians?

maintaining a reasonable speed?

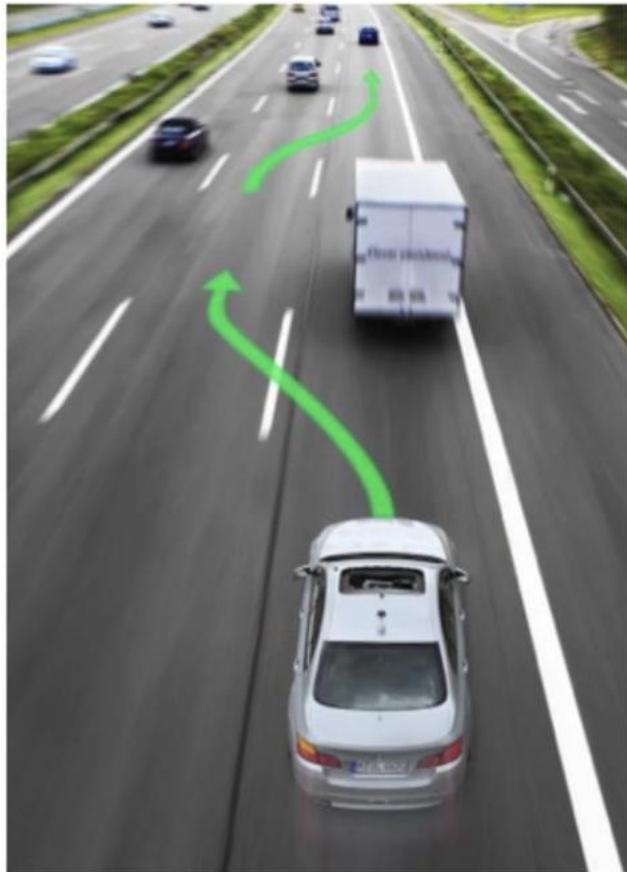
a slight preference for driving in the middle lane?

not changing lanes too often?

.....

reward function is too complicated to hand-tune

# Inverse Reinforcement Learning



apprenticeship learning  
but we can see what an expert does ☺  
(and thus infer the reward function that give rise to  
a good policy)

reward function is too complicated to hand-tune

# Inverse Reinforcement Learning

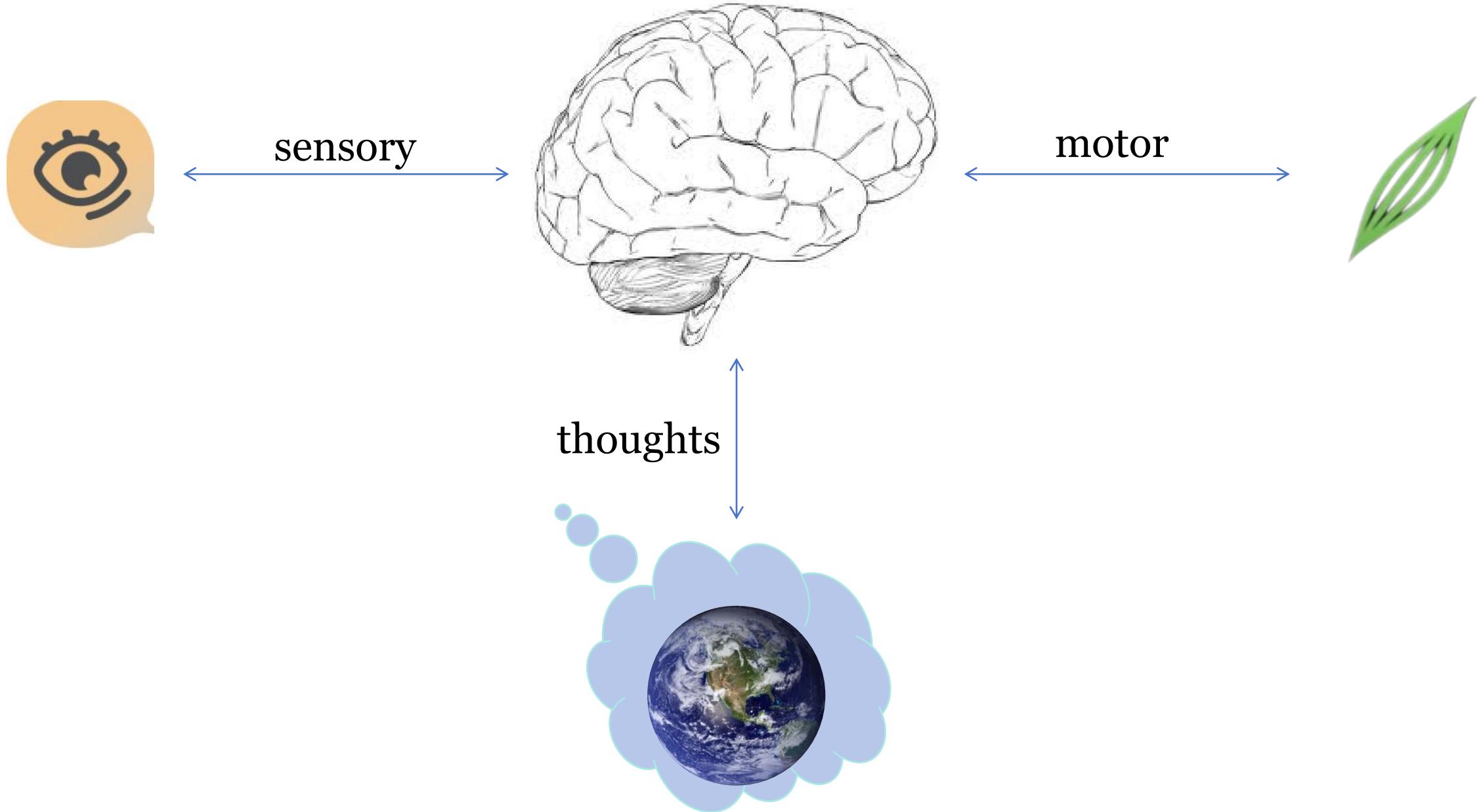
Formal Definition:

Given

- 1) measurements of an **agent's behaviour** over time, in a variety of circumstances,
- 2) measurements of the **sensory inputs** to that agent;
- 3) a model of the **physical environment** (including the agent's body).

Determine the reward function that the agent is optimizing.

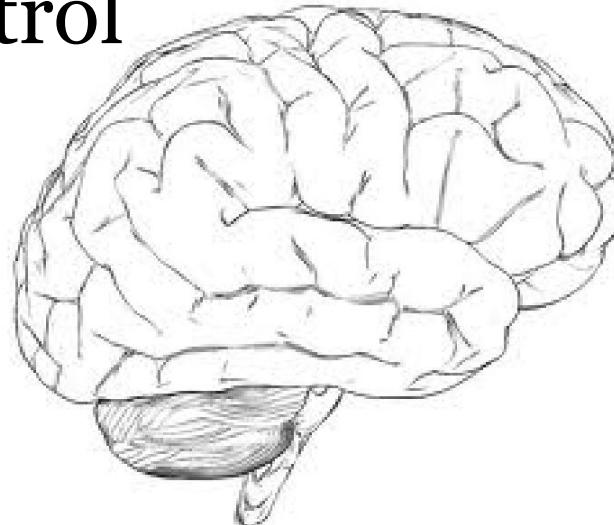
(Stuart Russell, 1998)



# Inverse Rational Control



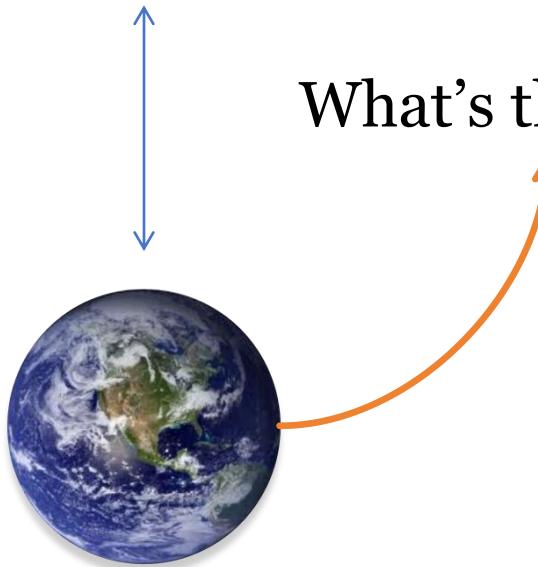
sensory



motor



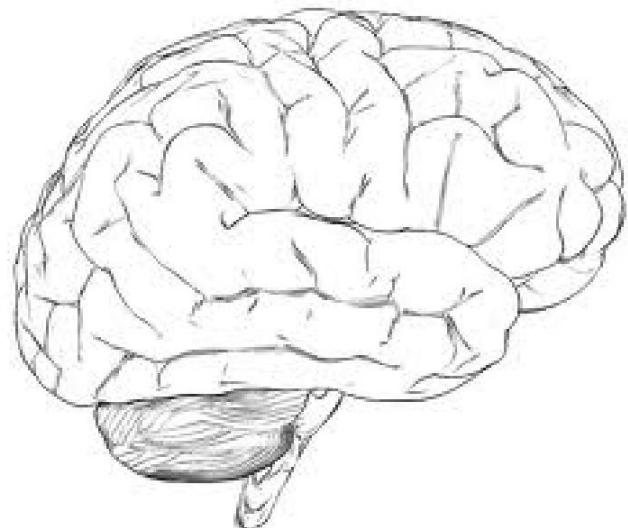
We see what the agent observes  
and how he acts  
Then we try to infer:



What's the agent's mental model?

What's his belief of  
the world, e.g.  
transition prob,  
reward..

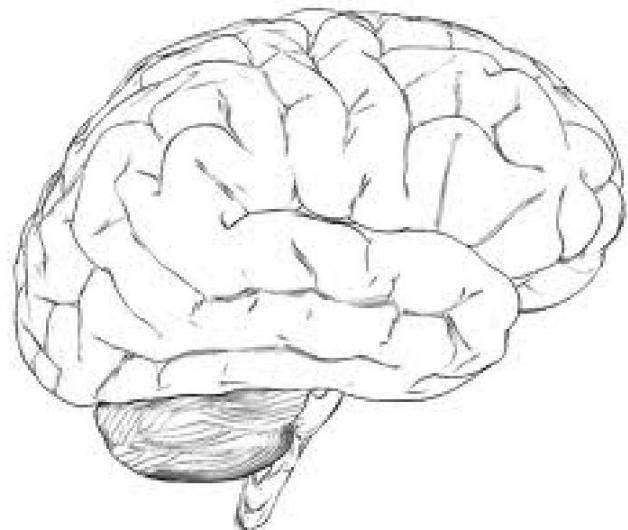
# Inverse Rational Control



What if the agent is wrong... but

**rational**: doing wrong things for  
the right reasons

# Inverse Rational Control

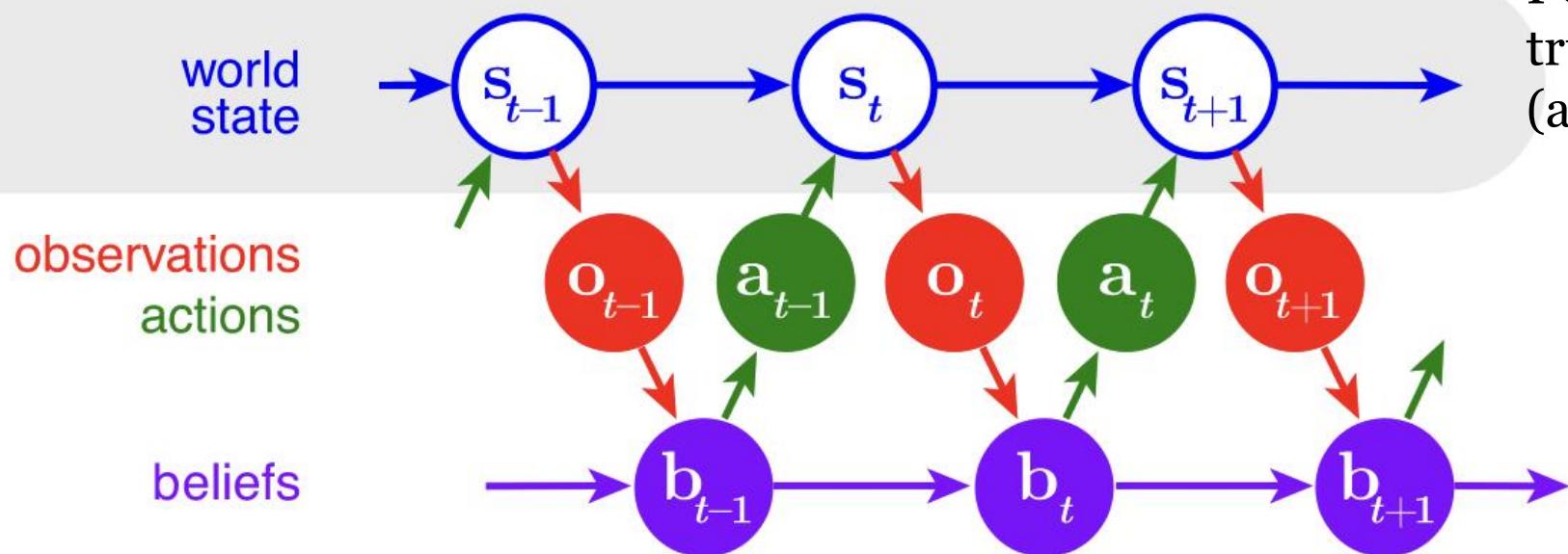


What if the agent is wrong... but  
rational: doing wrong things for  
the right reasons

The agent's **belief** about the world is wrong,  
but it acts **optimally** according to the belief  
(giving rise to **suboptimal** behavior)

# Modelling Behavior as Rational

## Partially Observable Markov Decision Process (POMDP)



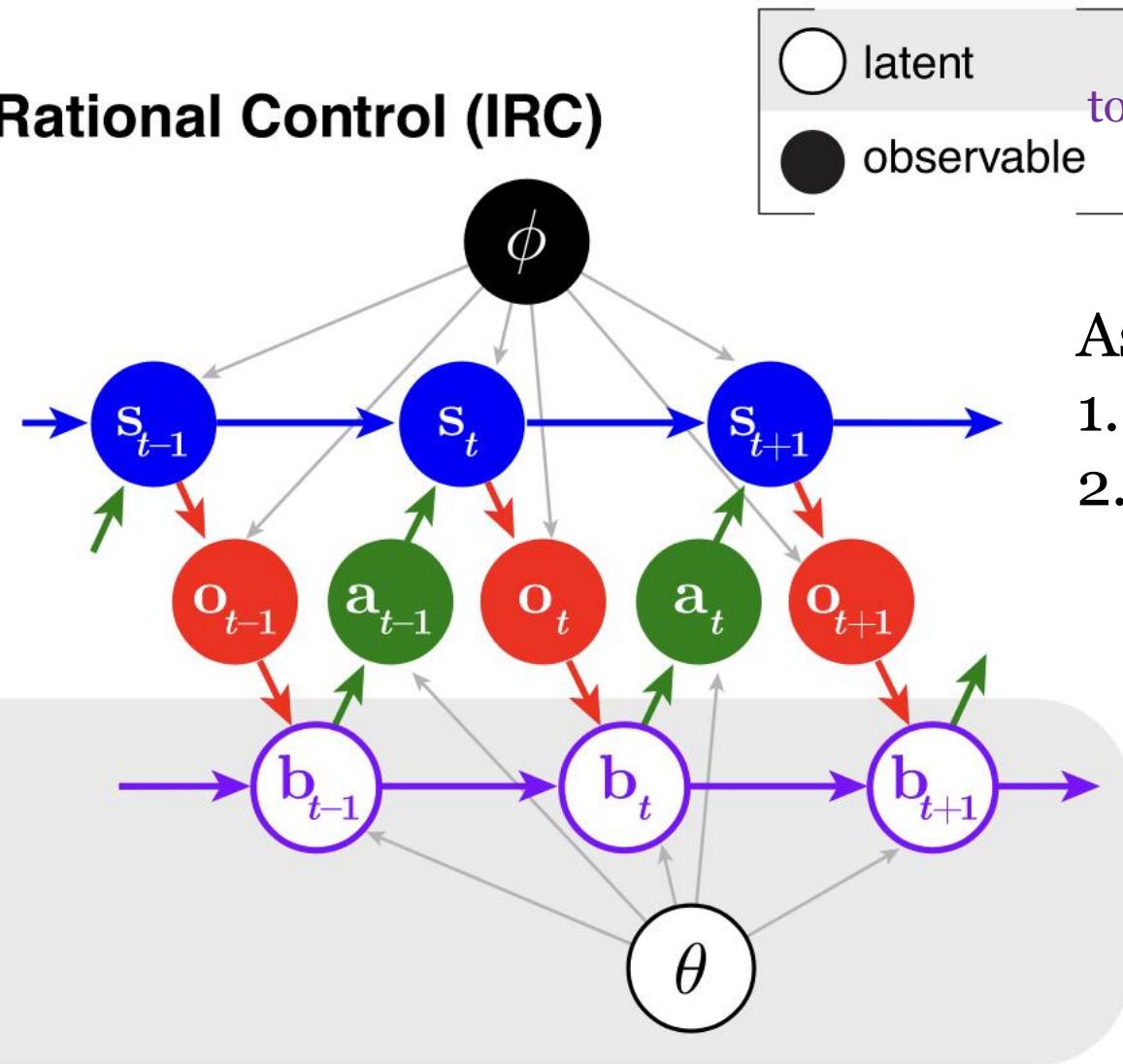
MDP: agent knows the real state

POMDP: agent has to infer the true state from observations (and actions)

# Modelling Behavior as Rational

## Inverse Rational Control (IRC)

true world parameters  
world state  
observations actions  
beliefs  
agent's assumed parameters:  
rewards dynamics



to the experimenter

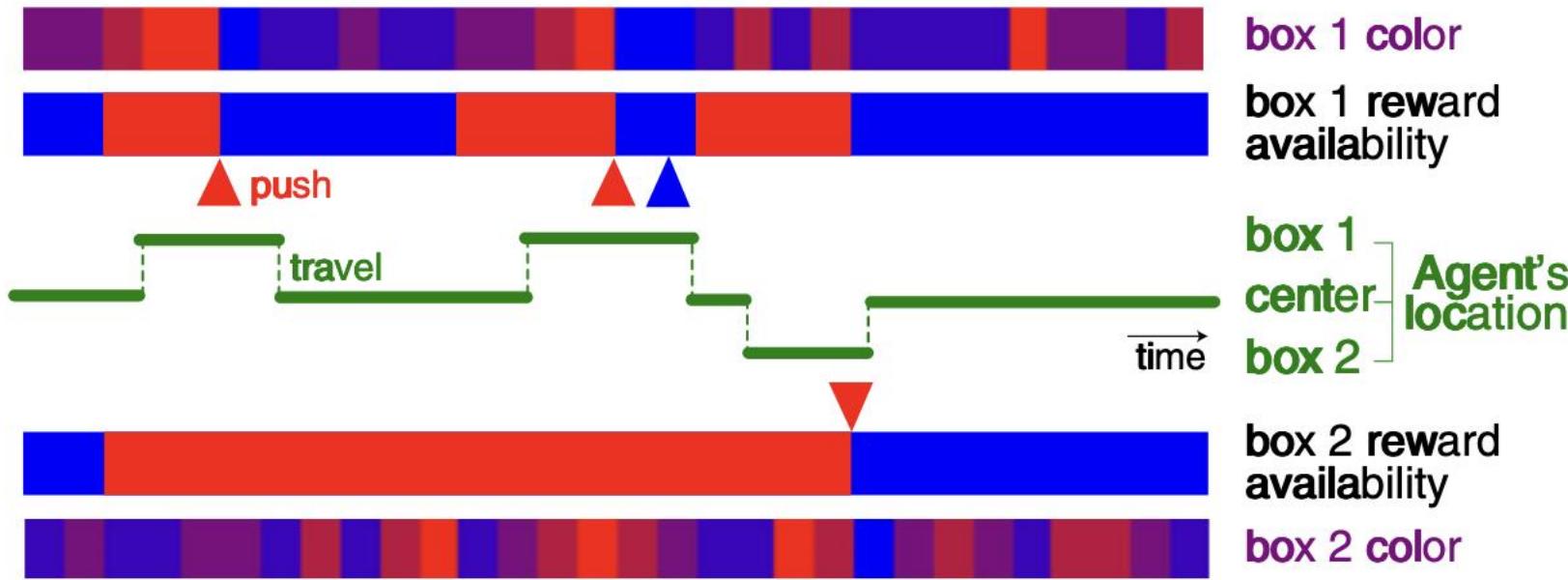
### Assumptions:

1. maximize total utility
2. stationary policy, no learning

# Modelling Behavior as Rational

## Foraging task

	yes	no
reward available?	■	□
got reward after push?	▲	▼
location	—	—



agent's parameters:

appearance rate(box1, 2),  
disappearance rate(box1, 2)

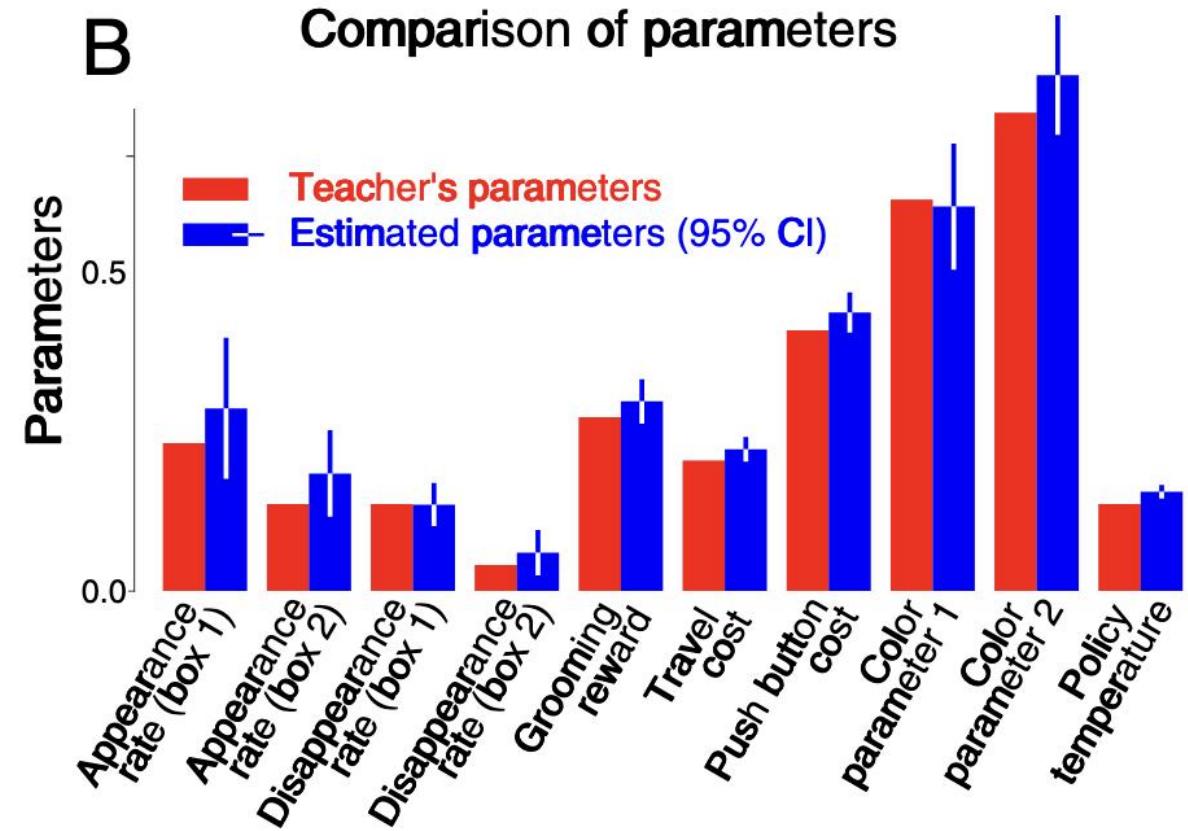
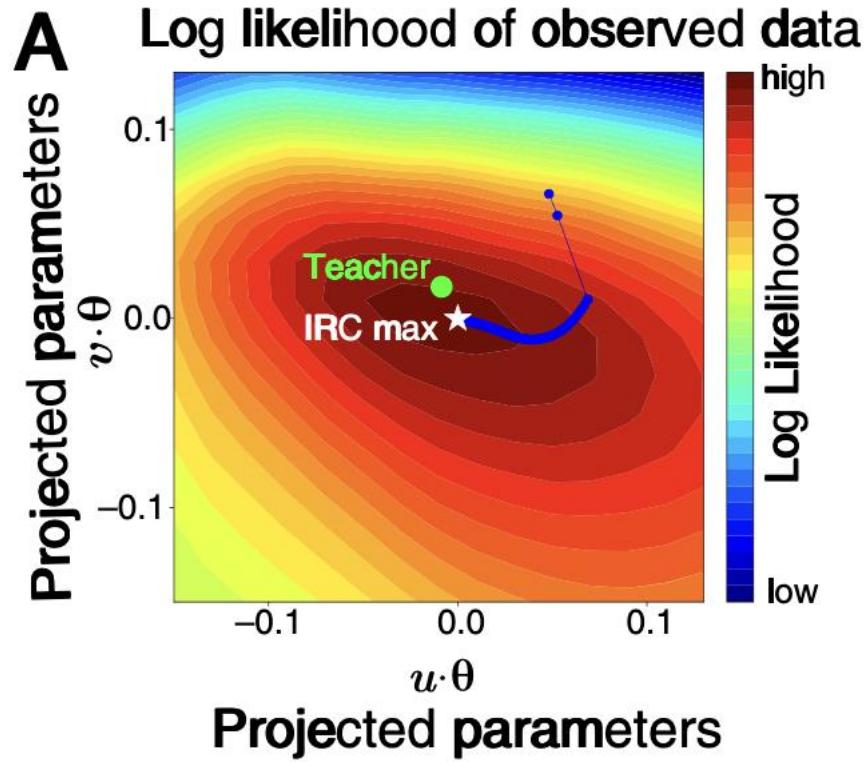
(reward availability as a telegraph process)  
(these parameters are very useful when you're far away from the box)

color parameters(box1, 2)  
(color drawn from a binomial)  
(useful when you're right at the box)

utility:  
grooming reward  
travel cost  
push button cost

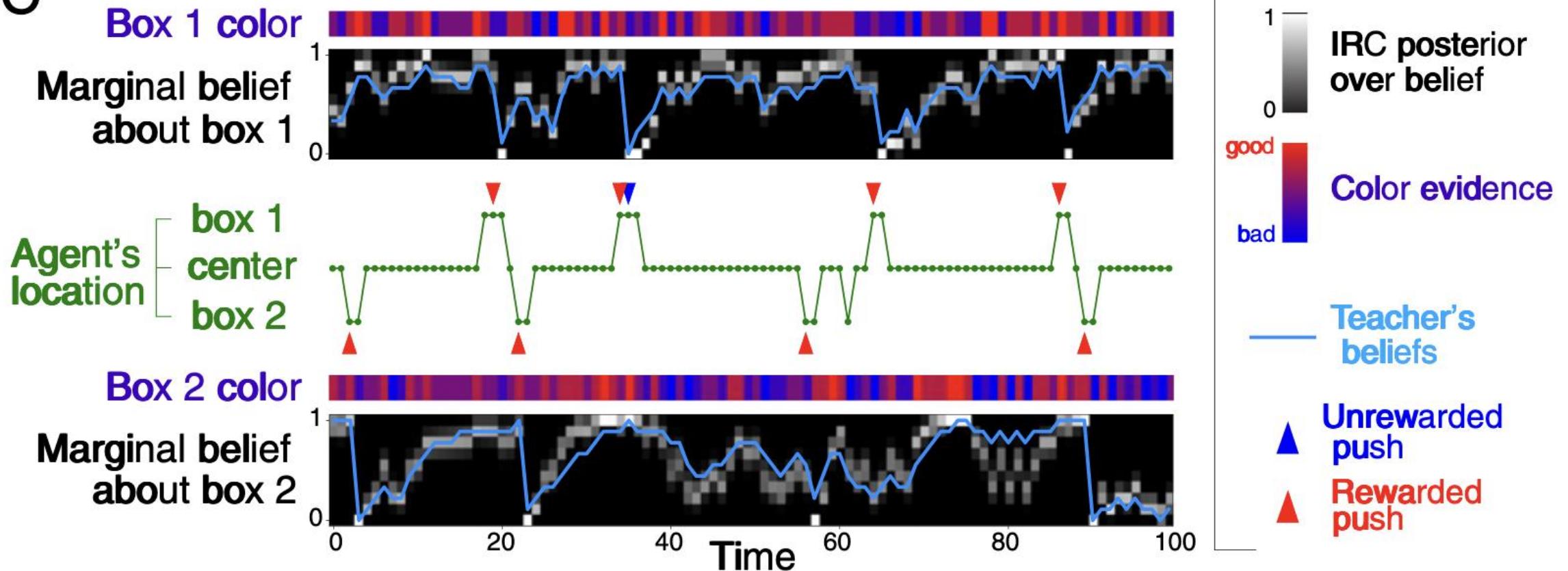
# Maths behind modelling

# Modelling Behavior as Rational

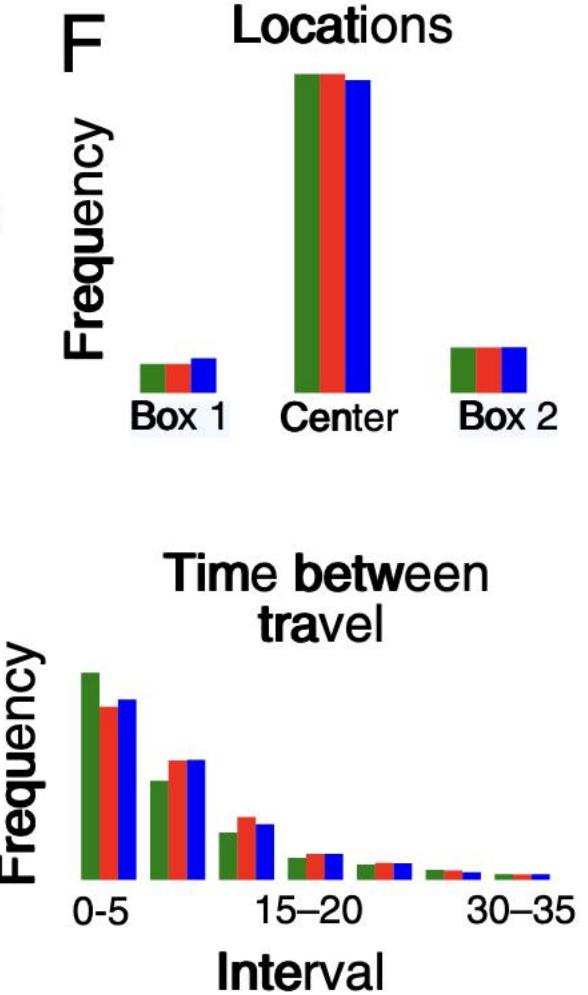
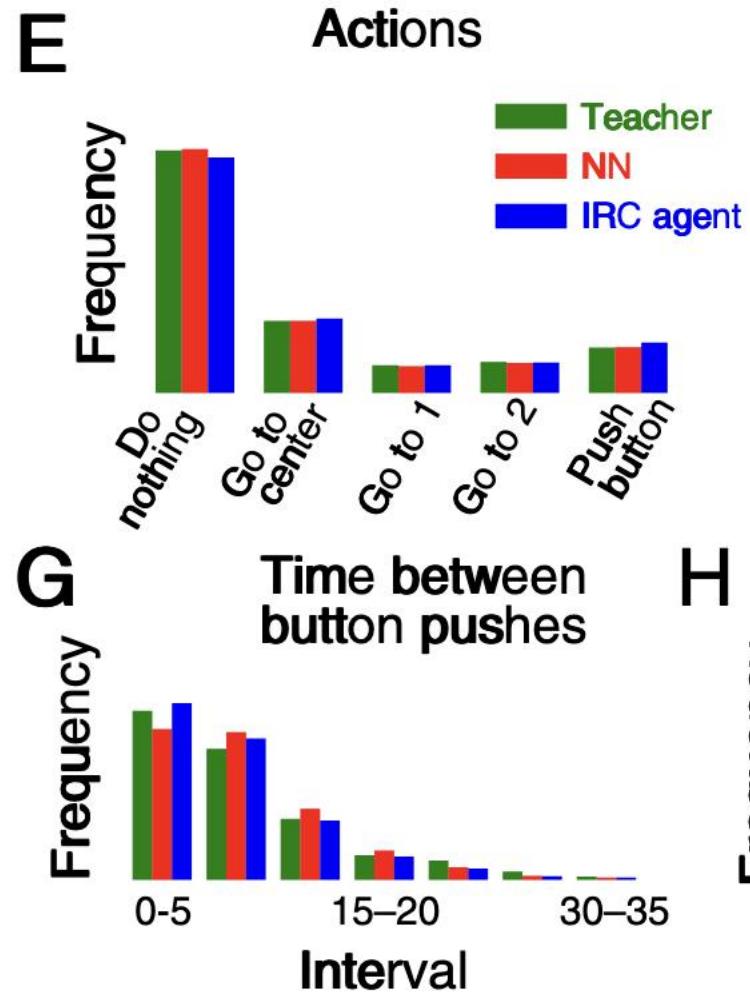
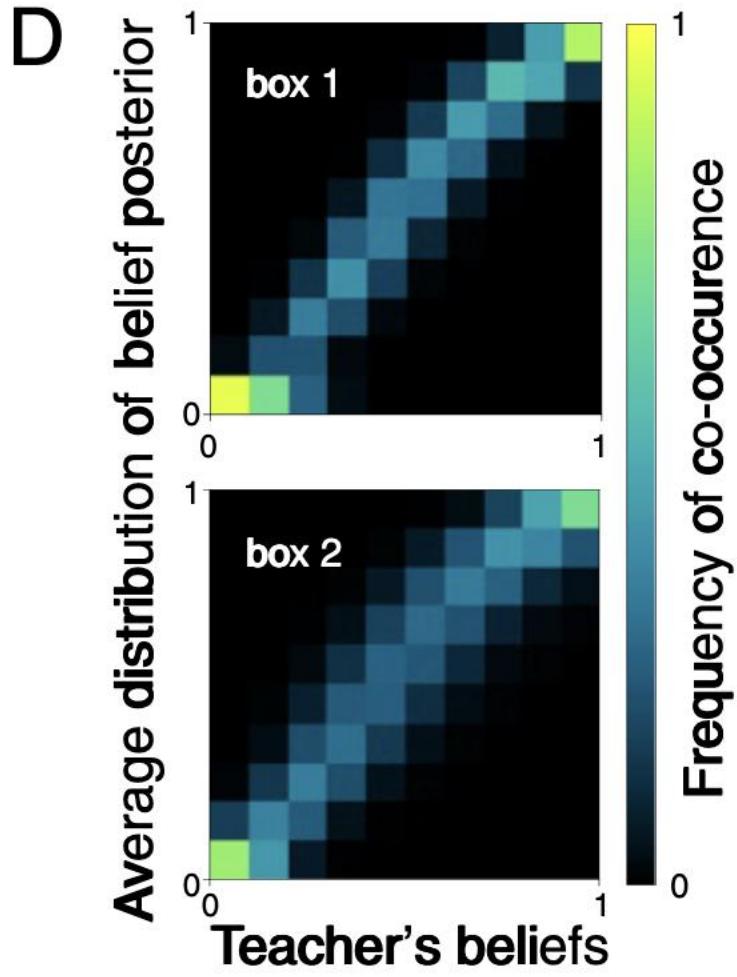


# Modelling Behavior as Rational

C



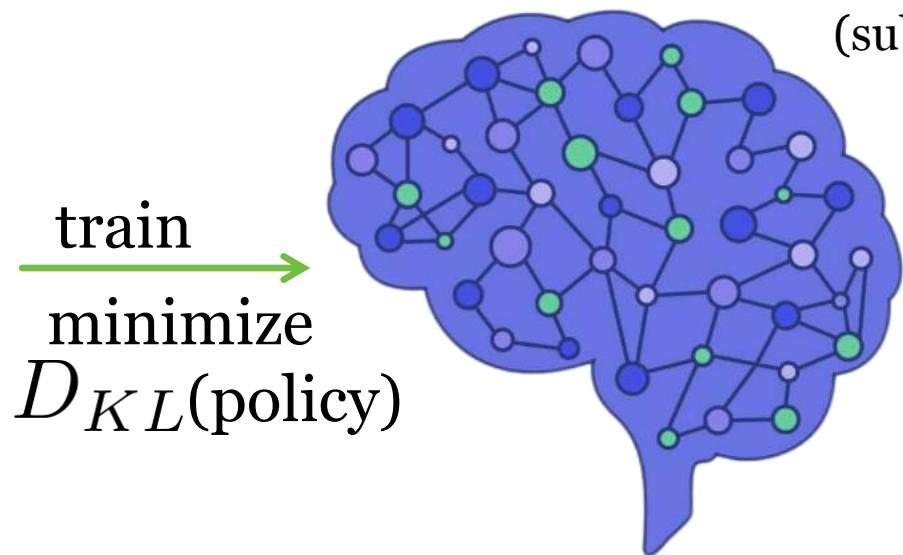
# Modelling Behavior as Rational



# Modelling Behavior as Rational



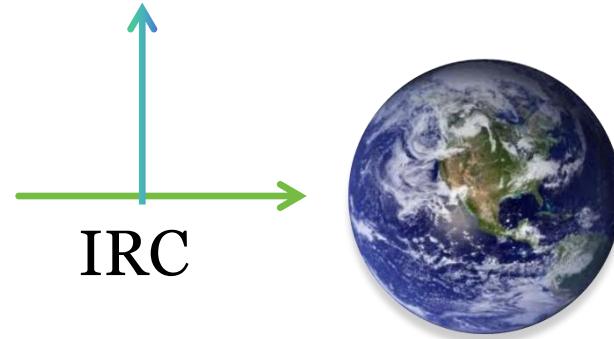
teacher POMDP



Neural Network model

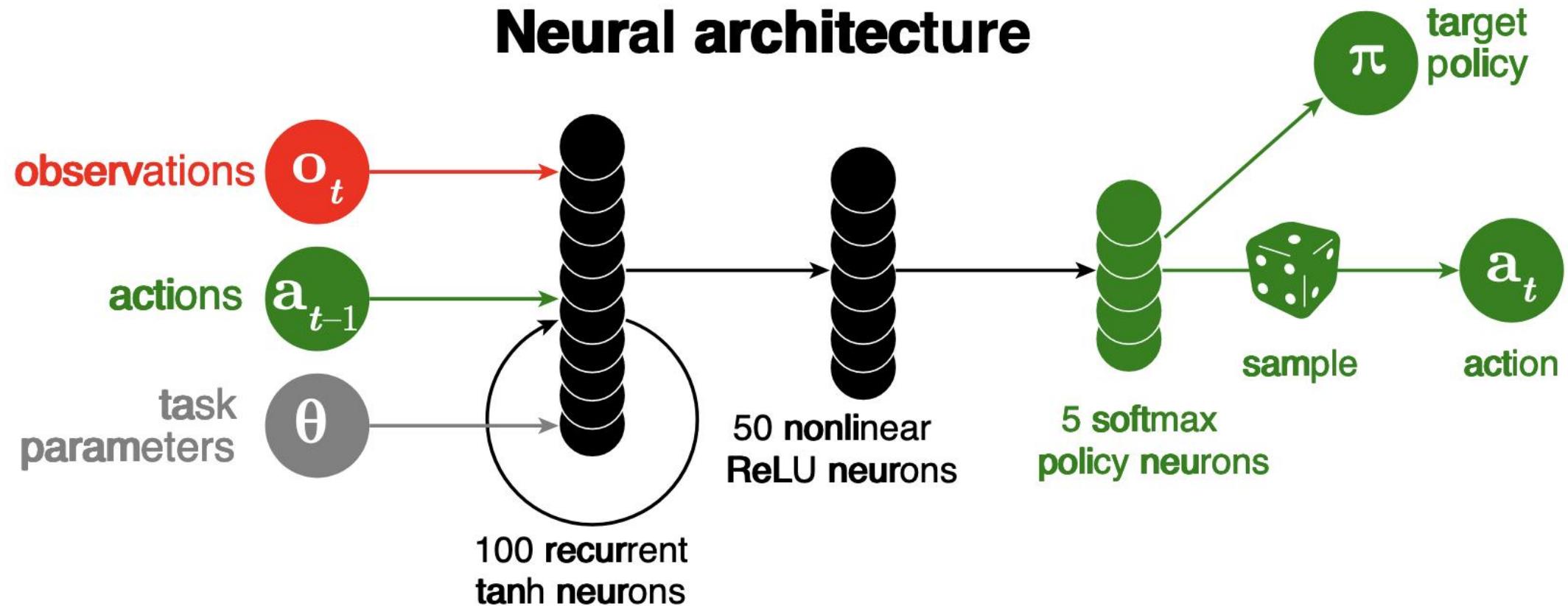
train  
minimize  
 $D_{KL}(\text{policy})$

input NN with slightly  
different parameters from  
the actual POMDP  
(suboptimality)

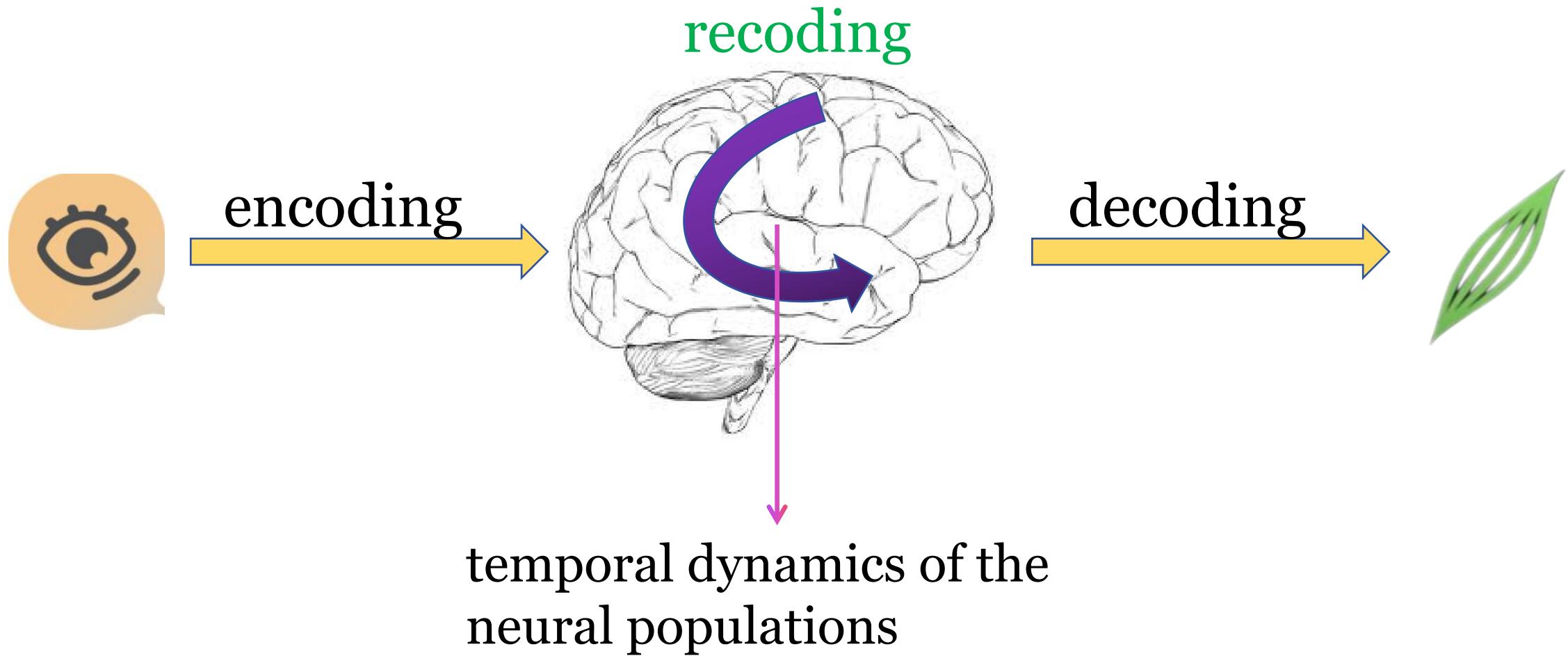


NN's POMDP  
(belief)

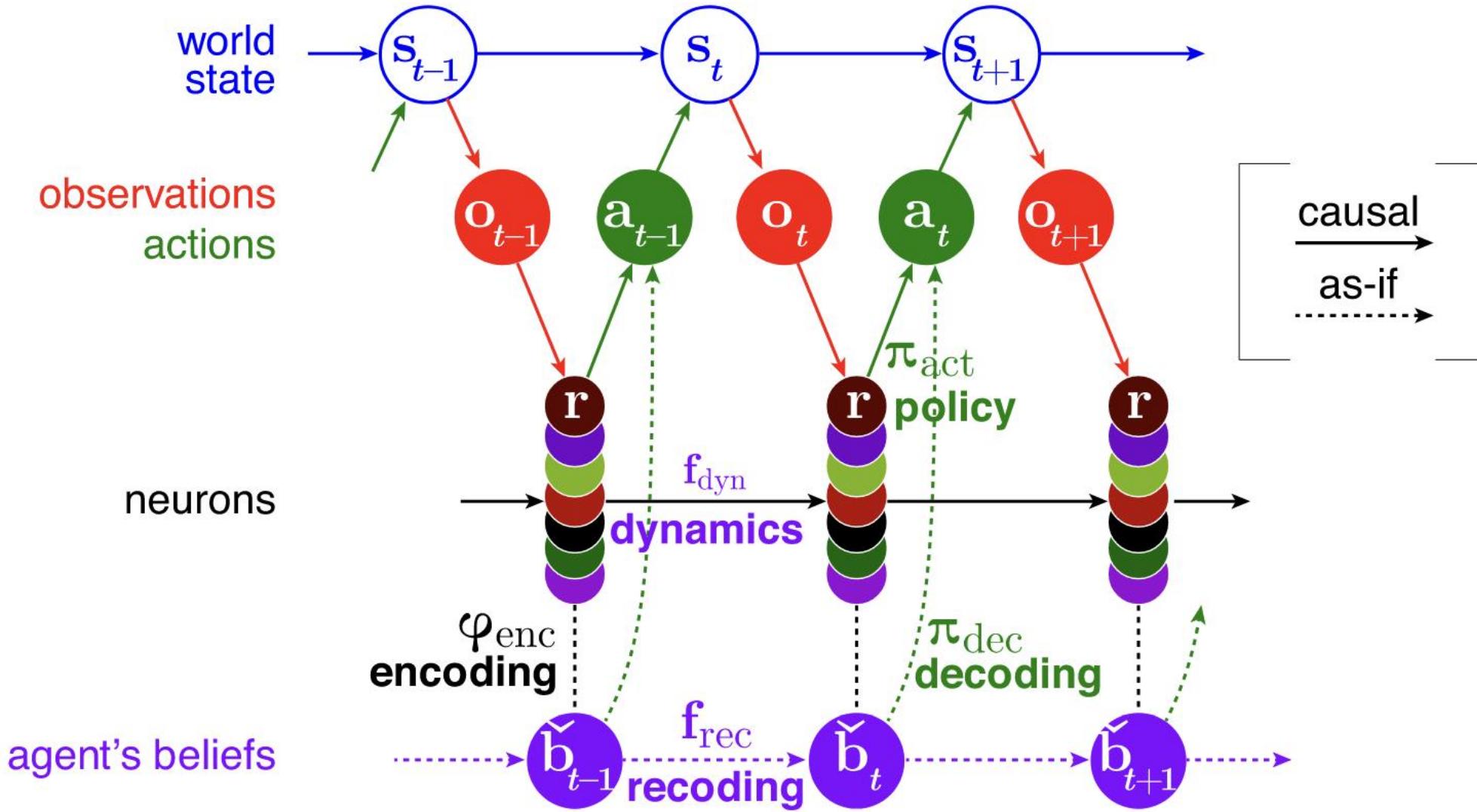
# Modelling Behavior as Rational



# Neural Coding



# Neural Coding: neural implementation of POMDP



# Neural Coding of rational thoughts

estimates from:  
behavior  $\hat{x}$   
neurons  $\check{x}$

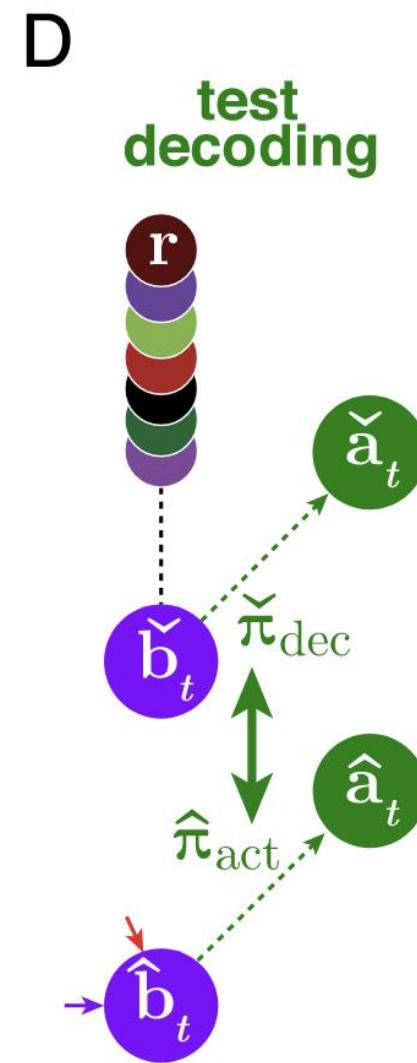
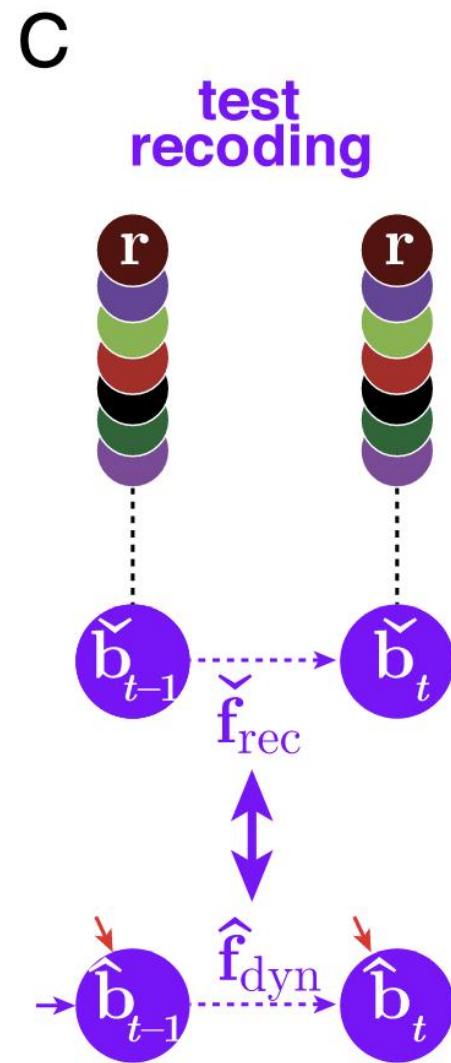
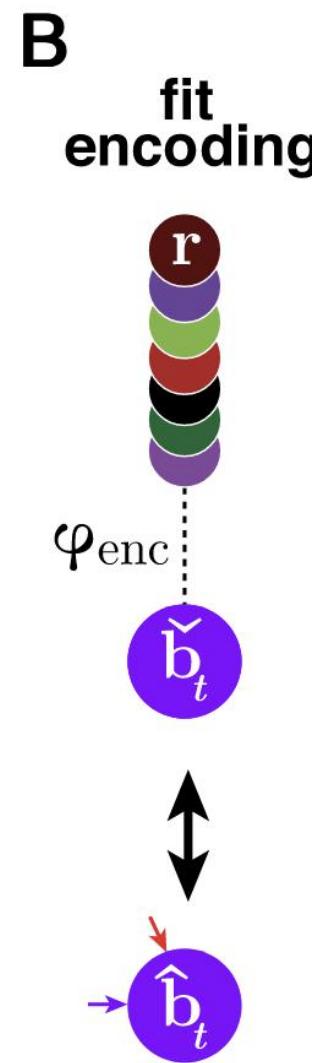
neurons

actions from  
neural code

beliefs from  
neural code

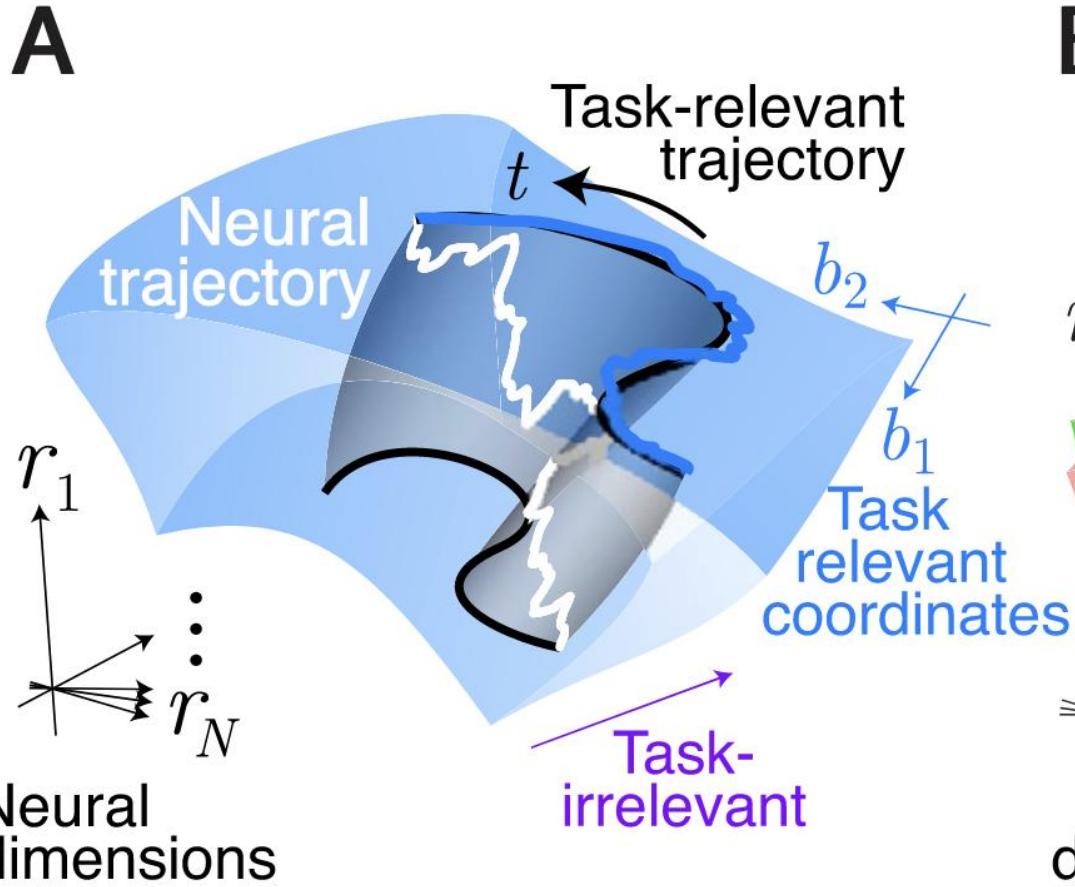
actions from  
behavioral model

beliefs from  
behavioral model

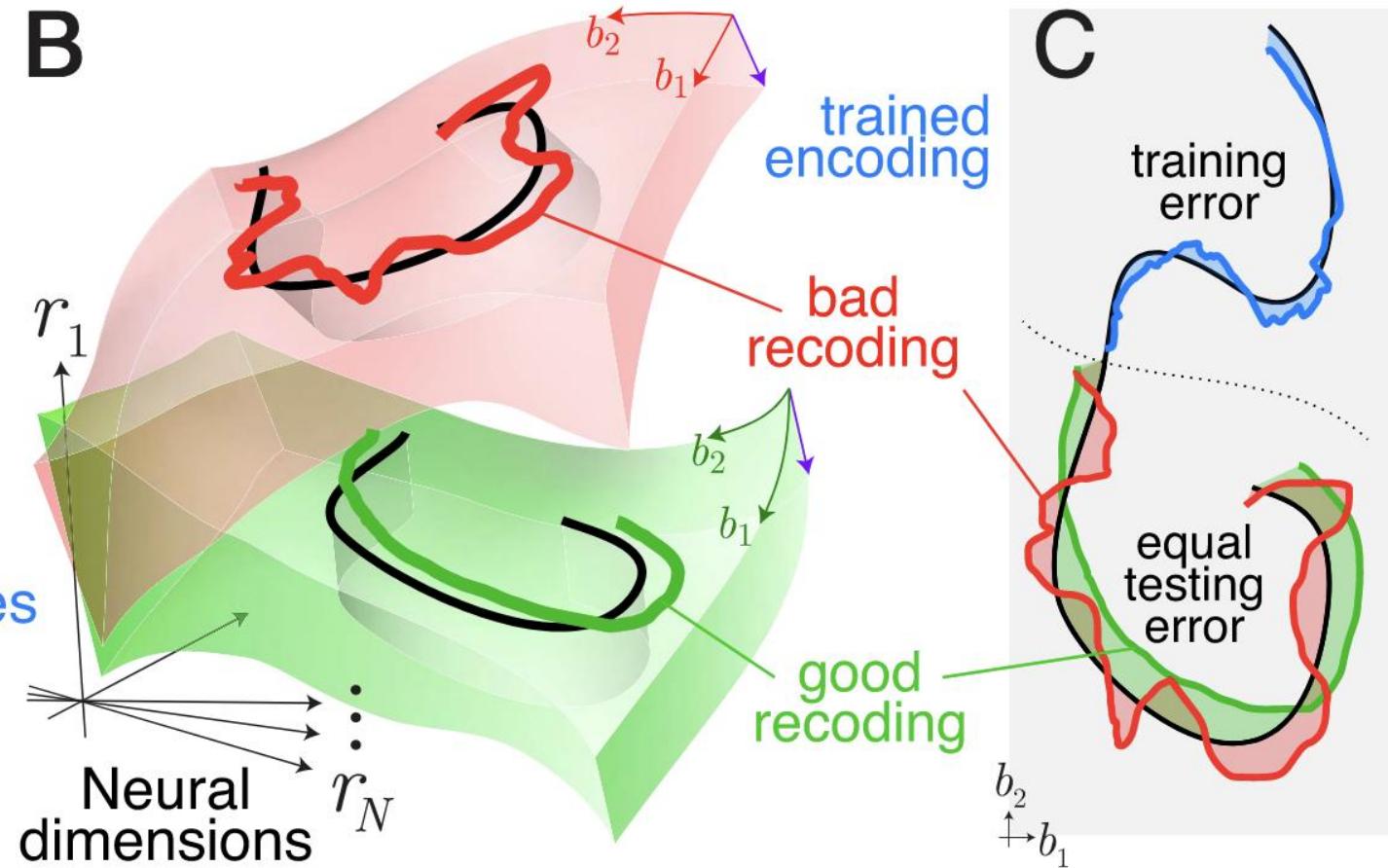


# Neural Coding

## Encoding of task variables

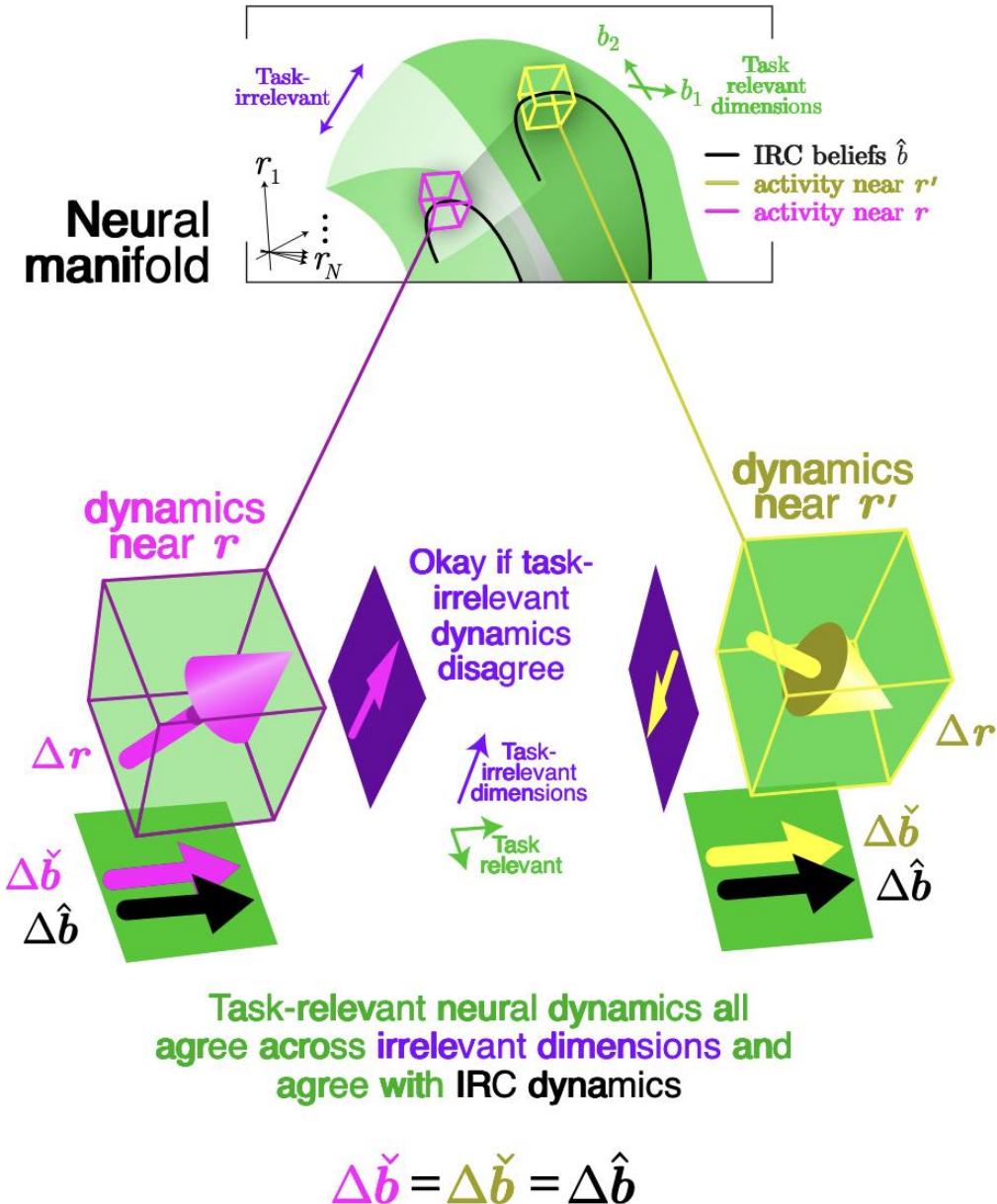


## Different recodings from different encoding fits

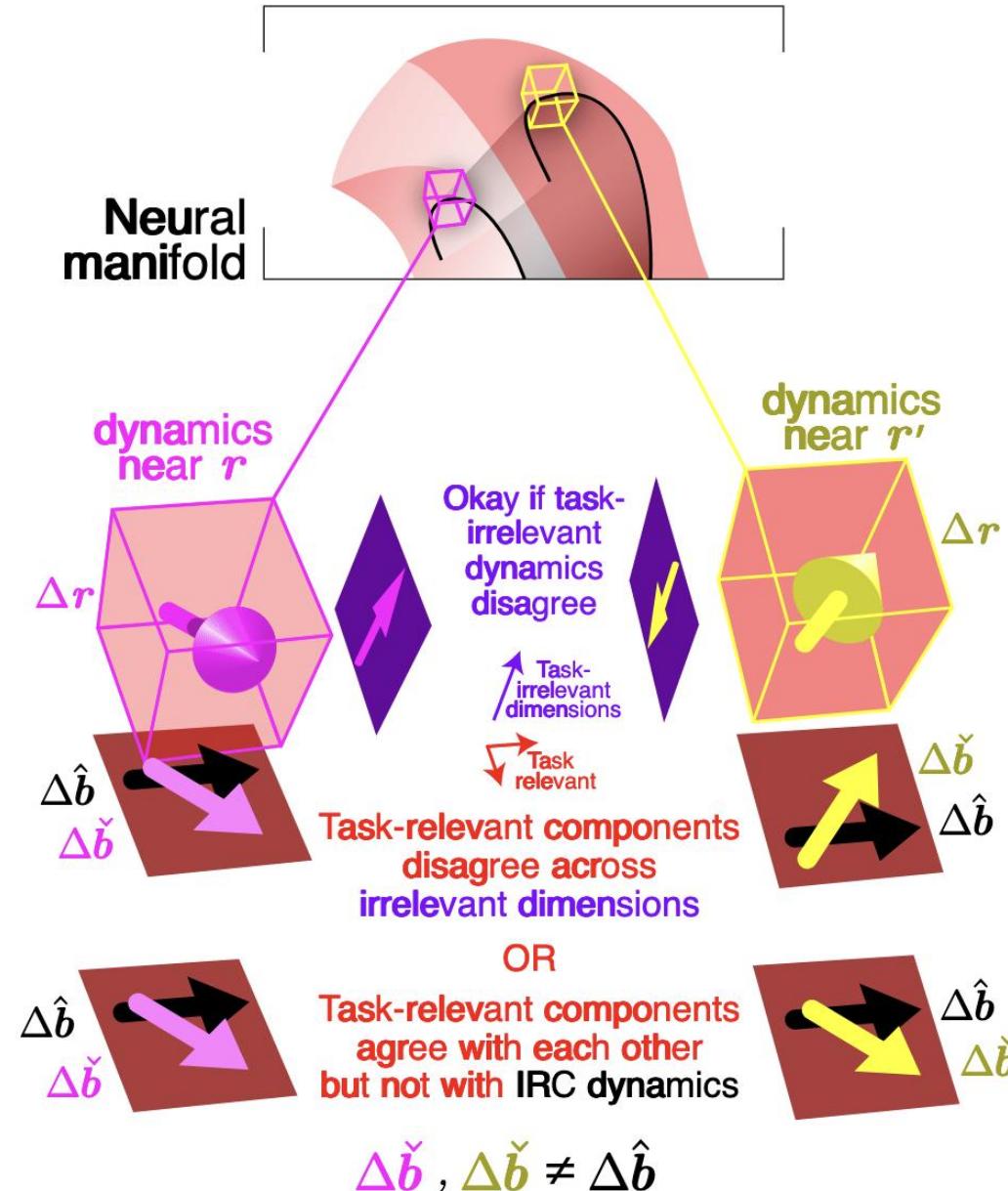


— Neural activity   — IRC beliefs  $\hat{b}$    — Neural beliefs  $\check{b}$  (train)   — Neural beliefs  $\check{b}$  (test)

## Good recoding

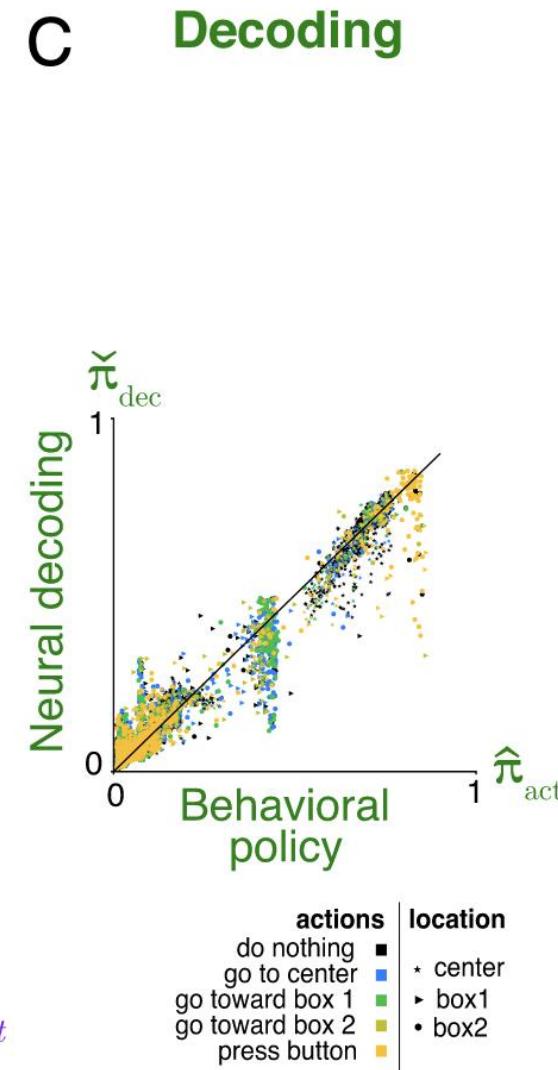
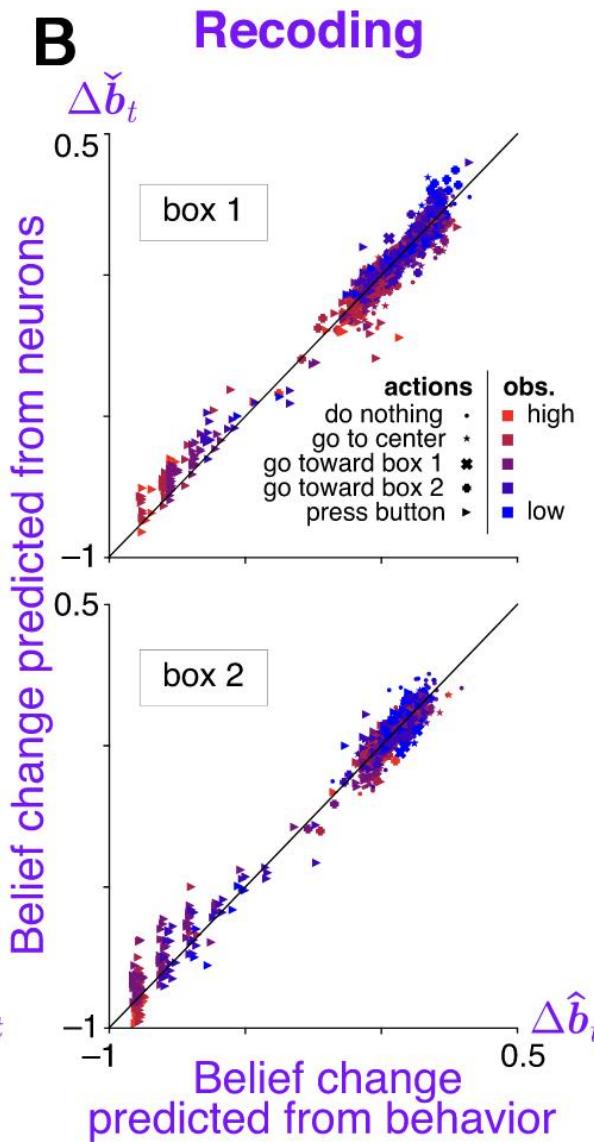
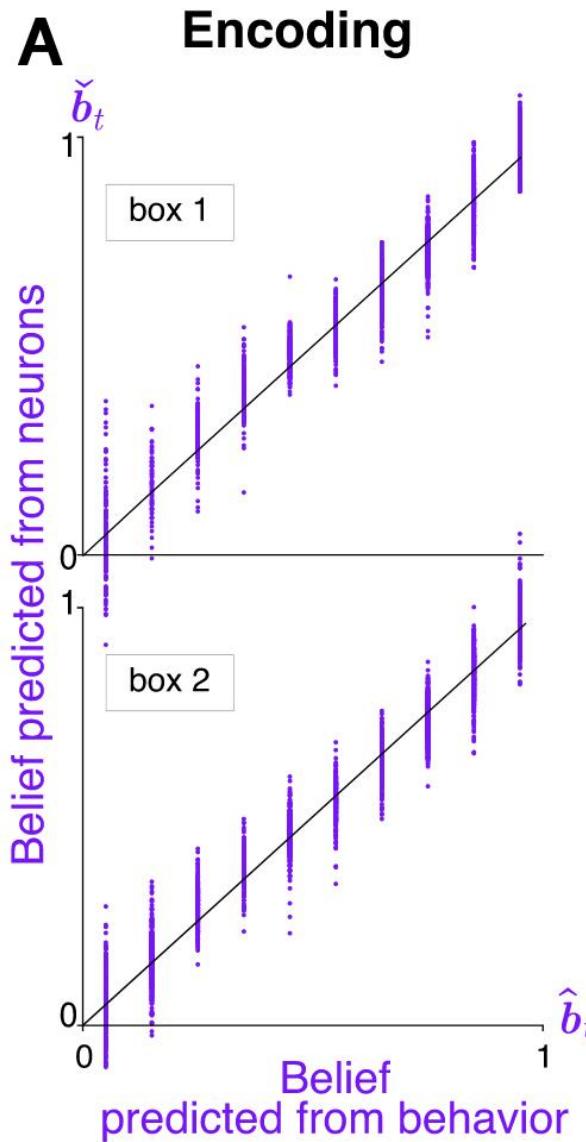


## Bad recoding



# Neural Coding

# Neural Coding



# Problems

# Problems

THE END

unless there's still time left

# (?)Representation learning is the bridge from planning to problem solving

PERSPECTIVE | FOCUS

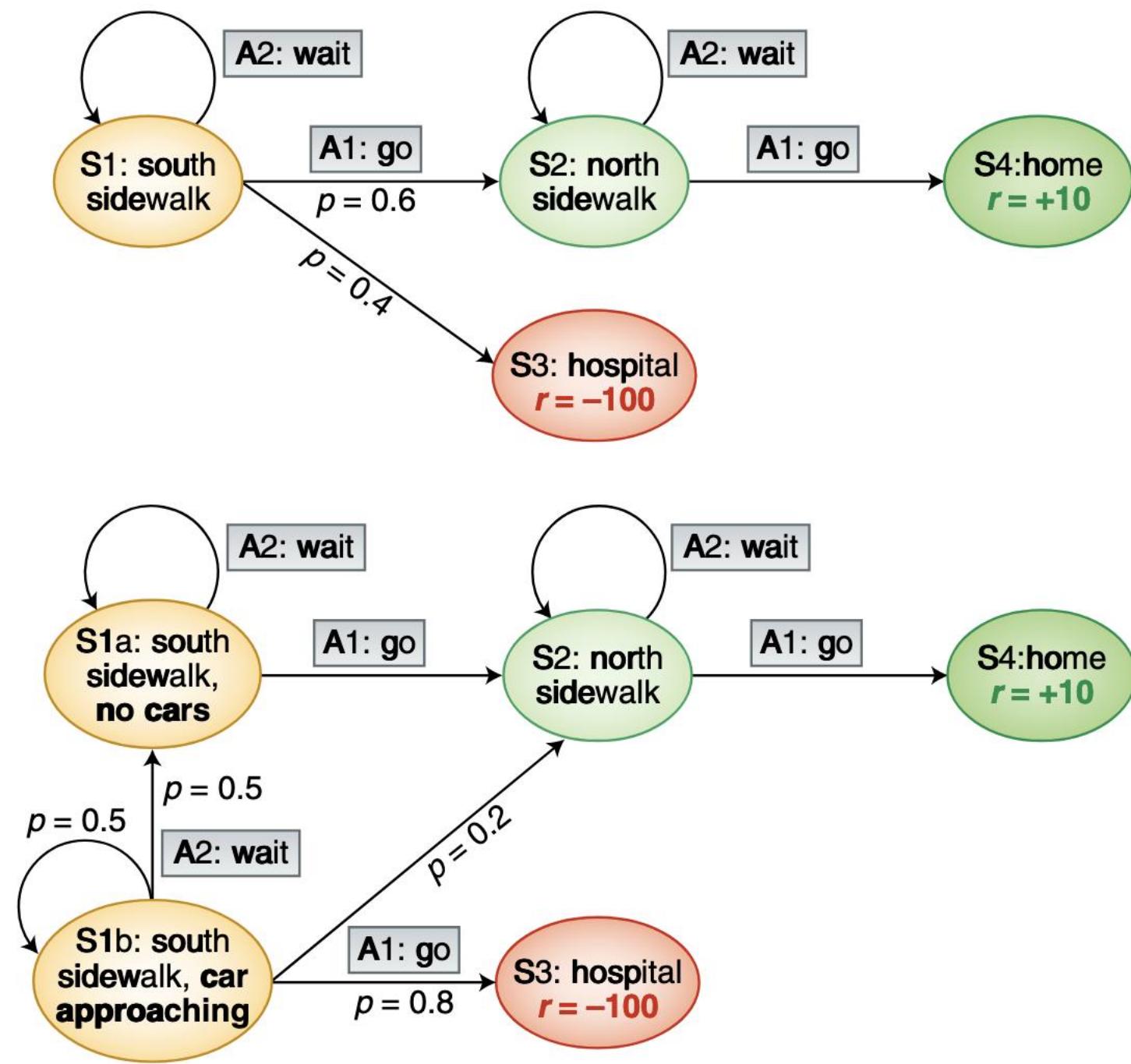
<https://doi.org/10.1038/s41593-019-0470-8>

nature  
neuroscience

## Learning task-state representations

Yael Niv 

Arguably, the most difficult part of learning is deciding what to learn about. Should I associate the positive outcome of safely completing a street-crossing with the situation ‘the car approaching the crosswalk was red’ or with ‘the approaching car was slowing down’? In this Perspective, we summarize our recent research into the computational and neural underpinnings of ‘representation learning’—how humans (and other animals) construct task representations that allow efficient learning and decision-making. We first discuss the problem of learning what to ignore when confronted with too much information, so that experience can properly generalize across situations. We then turn to the problem of augmenting perceptual information with inferred latent causes that embody unobservable task-relevant information, such as contextual knowledge. Finally, we discuss recent findings regarding the neural substrates of task representations that suggest the orbitofrontal cortex represents ‘task states’, deploying them for decision-making and learning elsewhere in the brain.



## Problems in Mathematics

10 people A1-A10 attend a meeting, some of them shake hands with each other.

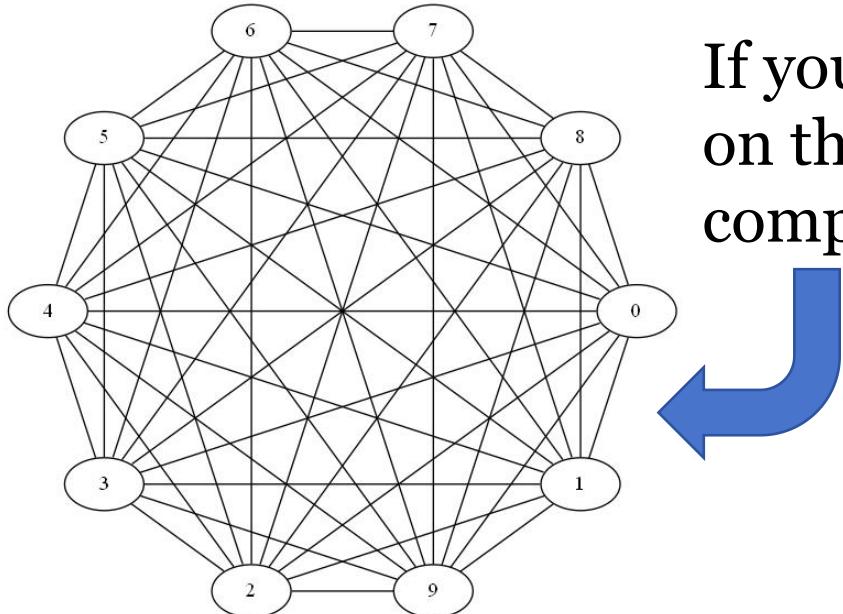
After the meeting, they report how many people they've shaked hands with:  
respectively 2, 5, 6, 3, 10, 5, 7, 1, 4, 8.

Is it possible?

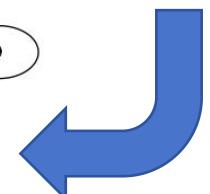
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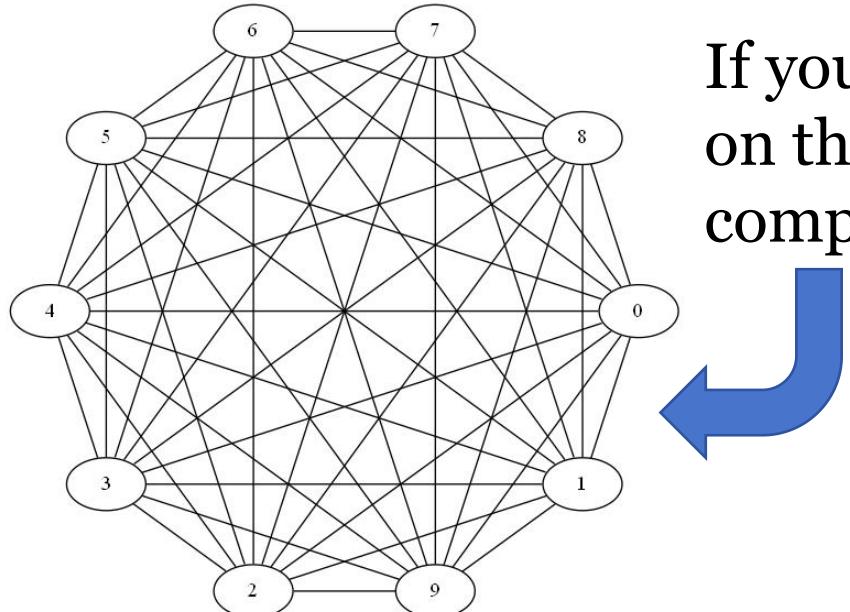
If you try to do a tree search  
on the graph, tremendous  
computation...



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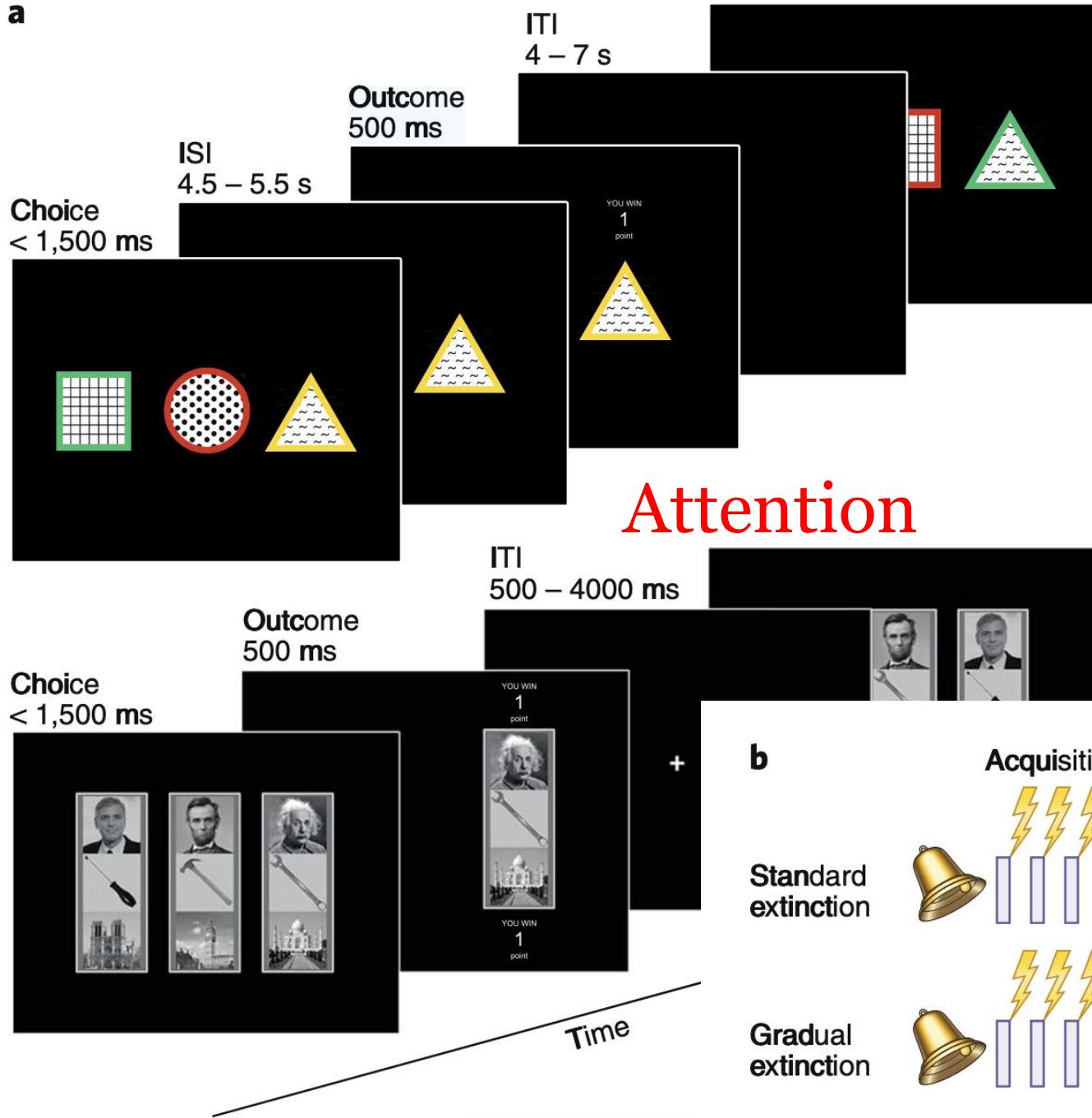
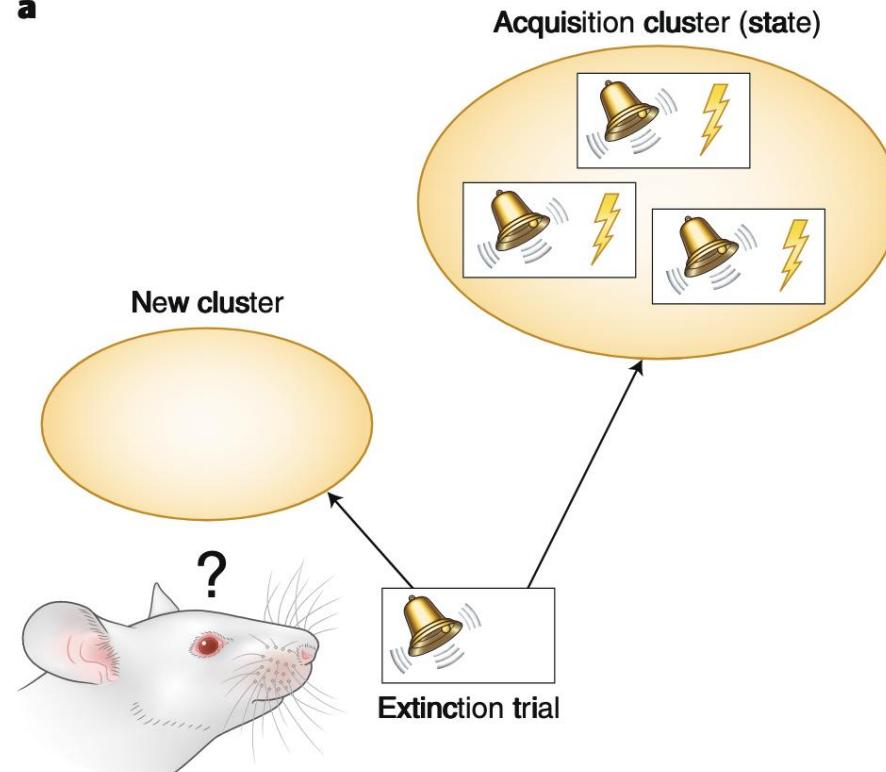


If you try to do a tree search  
on the graph, tremendous  
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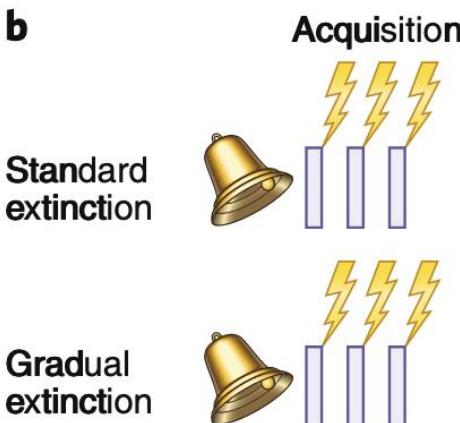
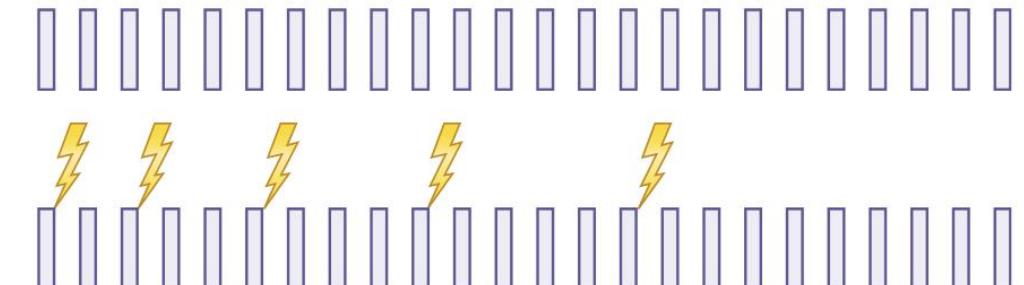
...but if you find an efficient representation  
of the task:  
Is the sum of the degrees even?

$2+5+\dots+8 = \text{odd}$ , so someone's lying!

- tasks do not have unique state representations
- the brain solves seemingly complex tasks by **learning efficient, low-dimensional representations** that simplify these tasks
- efficient representations are task-specific
- how living agents know what to represent in order to use neural RL to solve tasks?

**a****a**

## Similarity clustering of states

**b****Extinction**

Can we devise complex tasks where representation (learning) really is the game changer?

THE END