

## Objectives

## Introduction to Grammars

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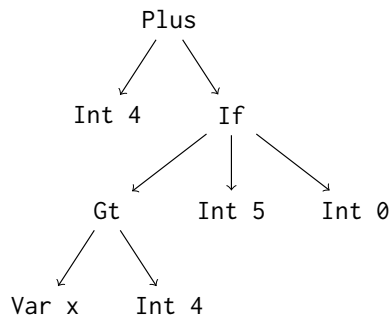
- Identify and explain the parts of a grammar.
- Define *terminal*, *nonterminal*, *production*, *sentence*, *parse tree*, *left-recursive*, *ambiguous*.
- Use a grammar to draw the parse tree of a sentence.
- Identify a grammar that is *left-recursive*.
- Know about *ambiguous grammars*:
  - Be able to identify, demonstrate, and eliminate ambiguity.

## Reminder: The Problem

- Computer programs are entered as a stream of ASCII (usually) characters.

4 + if x > 4 then 5 else 0

- We want to convert them into an *Abstract Syntax Tree*

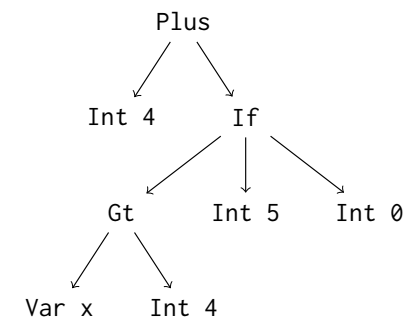


## Haskell Code

### Code

```

1 PlusExp (IntExp 4)
2   (IfExp (GtExp (VarExp "X") (IntExp 4))
3           (IntExp 5)
4           (IntExp 0))
  
```



## Reminder: The Solution



The conversion from strings to trees is accomplished in two steps.

- First, convert the stream of characters into a stream of *tokens*.
  - This is called *lexing* or *scanning*.
  - Turns characters into words and categorizes them.
  - We did this in the last two lectures!
- Second, convert the stream of tokens into an abstract syntax tree.
  - This is called *parsing*.
  - Turns words into *sentences*.

## What is in a sentence?

When we specify a sentence, we talk about two things that could be in them.

- 1 *Terminals*: tokens that are atomic — they have no smaller parts (e.g., “nouns”, “verbs”, “articles”)
- 2 *Non-terminals*: clauses that are not atomic — they are broken into smaller parts (e.g. “prepositional phrase”, “independent clause”, “predicate”)

Examples: (identify the terminals and the non-terminals)

- A sentence is a noun phrase, a verb, and a prepositional phrase
- A noun phrase is a determinant, and a noun
- A prepositional phrase is a preposition and a noun phrase.

## Notation

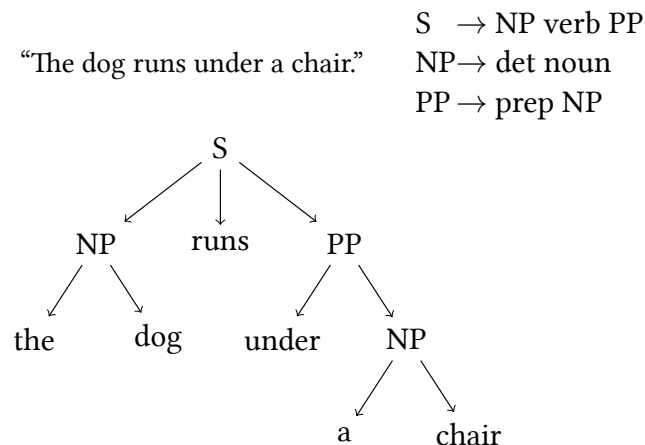
$$S \rightarrow N \text{ verb } P$$

$$N \rightarrow \text{det noun}$$

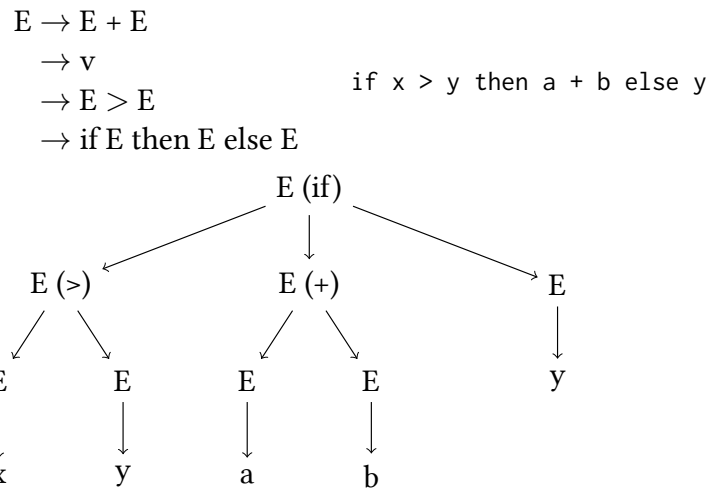
$$P \rightarrow \text{prep } N$$

- Each of the above lines is called a *production*.  
The *symbol* on the left hand side can be *produced* by collecting the symbols on the right hand side.
- The capital identifiers are *non-terminal* symbols.
- The lower case identifiers are *terminal* symbols.
- Because the left hand side is only a single non-terminal, the rules are *context free*. (Contrast:  $x S \rightarrow NP \text{ verb } PP$ )

## Grammars specify trees...



## Another Example...



## Properties of Grammars

It is important to be able to say what properties a grammar has.

**Epsilon Productions** A production of the form " $E \rightarrow \epsilon$ ", where  $\epsilon$  represents the empty string.

**Right Linear** Grammars where all the productions have the form " $E \rightarrow x F$ " or " $E \rightarrow x$ ".

**Left-Recursive** a production like " $E \rightarrow E + X$ "

**Ambiguous** More than one parse tree is possible for a specific sentence.

## Epsilon Productions

- Sometimes we want to specify that a symbol can become nothing.
- Example: " $E \rightarrow \epsilon$ "
- Another example:
  - $S \rightarrow \text{NP verb PP}$
  - $\text{NP} \rightarrow \text{det A noun}$
  - $\text{PP} \rightarrow \text{prep NP}$
  - $A \rightarrow \text{adjective A}$
  - $A \rightarrow \epsilon$

This says that adjectives are an optional part of noun phrases.

## Right Linear Grammars

- A *right linear* grammar is one in which all the productions have the form " $E \rightarrow x A$ " or " $E \rightarrow x$ ".
- This corresponds to the *regular languages*.
- Example: regular expression  $(10)^*23$  describes same language as this grammar:
  - $A_0 \rightarrow 1A_1 \mid 2A_2$
  - $A_1 \rightarrow 0A_0$
  - $A_2 \rightarrow 3A_3$
  - $A_3 \rightarrow \epsilon$

## Left-Recursive

- A grammar is *recursive* if the symbol being produced (the one on the left-hand side) also appears in the right hand side.
- Example: “ $E \rightarrow \text{if } E \text{ then } E \text{ else } E$ ”
- A grammar is *left-recursive* if the production symbol appears as the first symbol on the right-hand-side.
- Example: “ $E \rightarrow E + F$ ”
- ... or if is produced by a chain of left recursions ...

Example:  $A \rightarrow Bx$   
 $B \rightarrow Ay$

## Ambiguous Grammars

- A grammar is *ambiguous* if it can produce more than one parse tree for a single sentence.
- There are two common forms of ambiguity:
  - The “dangling else” form:
 
$$E \rightarrow \text{if } E \text{ then } E \text{ else } E$$

$$E \rightarrow \text{if } E \text{ then } E$$

$$E \rightarrow \text{whatever}$$
 Example: if a then if x then y else z ... to which if does the else belong?
  - The “double-ended recursion” form:
 
$$E \rightarrow E + E$$

$$E \rightarrow E * E$$
 Example “3 + 4 \* 5” ... is it “(3 + 4) \* 5” or “3 + (4 \* 5)”?

## Fixing Ambiguity

- Ambiguity can often be eliminated by thinking more carefully about what you are trying to express with your grammar.
- “Dangling else” usually matches with the nearest if. This can be encoded in the grammar.

## Fixing Ambiguity

- The “double-ended recursion” form usually reveals a lack of precedence and associativity information. A technique called *stratification* often fixes this.
  - Left-recursive means “associates to the left”, similarly right-recursive.
  - Higher precedence rules occur lower in the grammar.
$$E \rightarrow F + E$$

$$E \rightarrow F$$

$$F \rightarrow T * E$$

$$F \rightarrow T$$

$$T \rightarrow ( E )$$

$$T \rightarrow \text{integer}$$

## Next Up

- Parsing is hard! Let's break it up into parts.
- Compute First sets:
  - What is the first symbol I could see when parsing a given non-terminal?
- Compute Follow sets:
  - What is the first symbol I could see *after* parsing a given non-terminal?