Monads

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Objectives

- Describe the problem that monads attempt to solve.
- Know the three monad laws.
- Know the syntax for declaring monadic operations.
- Be able to give examples using the Maybe and List monads.

Monads

Motivation

- Monads are a way of defining computation.
- They are similar to continuations, but even more powerful.
- They are also related to the applicative functors from last time.
- Consider this program....

```
1 inc1 a = a + 1
2 r1 = inc1 <$> Just 10 -- result: Just 11
3 r2 = inc1 <$> Nothing -- result: Nothing
```

But what if we have functions like this?

```
_1 inc2 a = Just (a+1)
_2 recip a \mid a = / 0 = Just (1/a)
          | otherwise = Nothing
```

How can we pass a Nothing to it? How can we use what we get from it?

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Notice the pattern

- Applicatives take the values out of the parameters, run them through a function, and then repackage the result for us.
- The functions have no control: the applicative makes all the decisions.
- Monads let the functions themselves decide what should happen.



Introducing Monads

• A *monad* is a container type *m* along with two functions:

```
    return :: a -> m a
    bind :: m a -> (a -> m b) -> m b
    In Haskell, bind is written as >>=
```

• These functions must obey three laws:

```
Left identity return a >>= f is the same as f a

Right identity m >>= return is the same as m

Associativity (m >>= f) >>= g is the same as m >>= (\x -> f x >>= g)
```

Understanding Return

- The return keyword takes an element and puts it into a monad.
- This is a one way trip!
- Very much like pure in Applicative.

```
return a = Just a
```



Understanding Bind

- All the magic happens in bind.
- bind :: m a -> (a -> m b) -> m b
 - The first argument is a monad.
 - The second argument takes a monad, unpacks it, and repackages it with the help of the function argument.
 - Exactly *how* it does that is the magic part.

Bind for Maybe

```
Nothing >>= f = Nothing
(Just a) >>= f = f a
-- Remember that f returns a monad
```



A calculator, with monads

- Okay, the above code works, but here's a better way.
- First define functions lift to convert a function to monadic form for us!

These are part of Control.Monad



Continued

Lifting

- fail is another useful monadic function.
- Here it's defined as Nothing.



A monad definition

Here is the complete monad definition for Maybe

Maybe Monad

```
instance Monad Maybe where
return = Just

(>>=) Nothing f = Nothing
(>>=) (Just a) f = f a

fail s = Nothing
```

A list monad

Lists can be monads too. The trick is deciding what bind should do.

List Monad

```
1 instance Monad [] where
2  return a = [a]
3
4  (>>=) [] f = []
5  (>>=) xs f = concatMap f xs
6
7  fail s = []
```

• Note that we do not have to change *anything* in our lifted calculator example!



More capability

• What is the square root of 4?

Adding nondeterminism

```
1 msqrt a = a >>= (\aa ->
2     let sa = sqrt aa
3     in [-sa,sa])
4
5
6 msqrt [4] >>= minc -- becomes [-1,3]
```

Do notation

• Haskell has a special builtin syntax for monads.

- If you only need applicative, it's better to use that than monads.
- Avoid do notation if you can.

