

Telecom Systems (Week 4)



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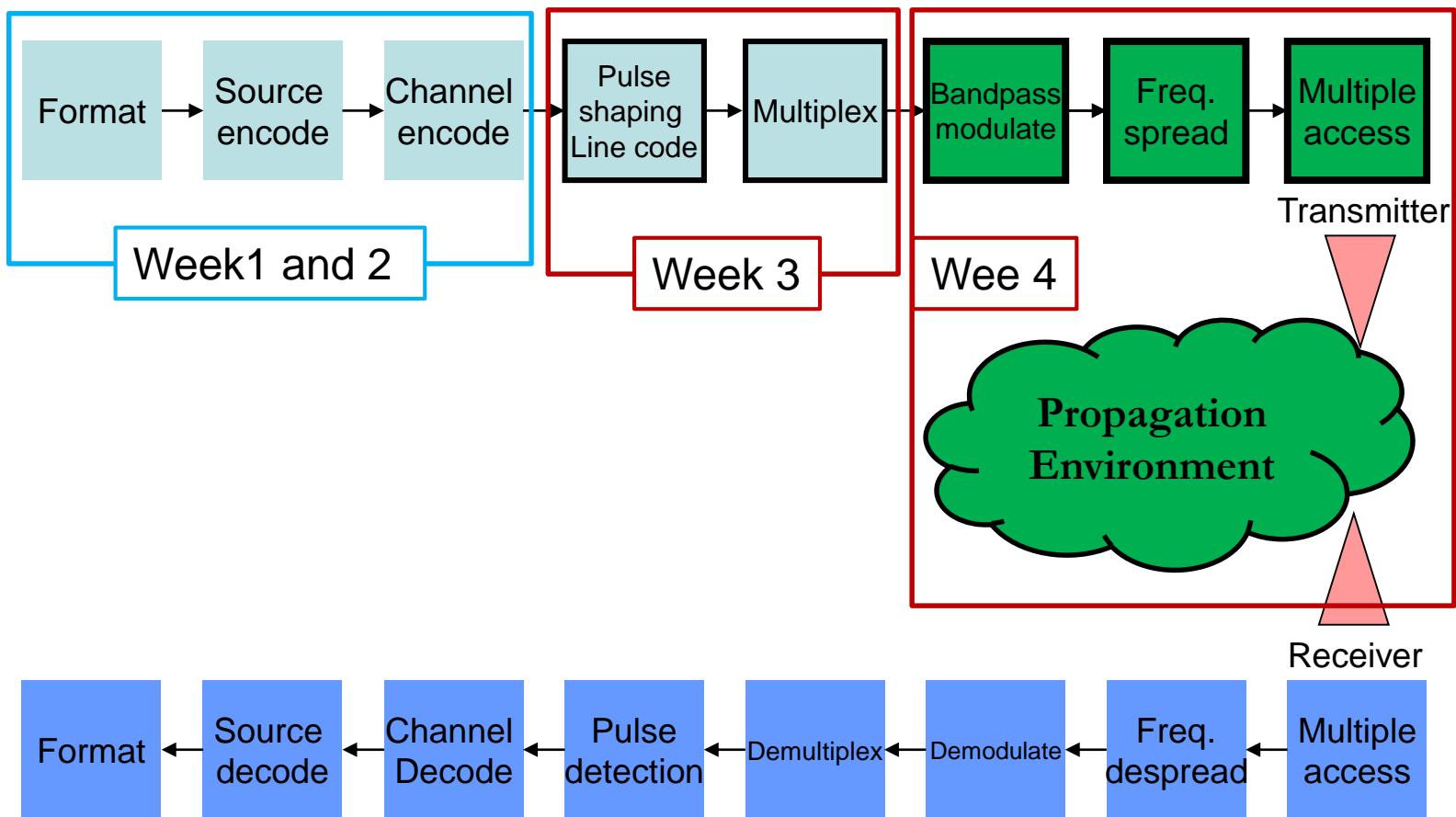
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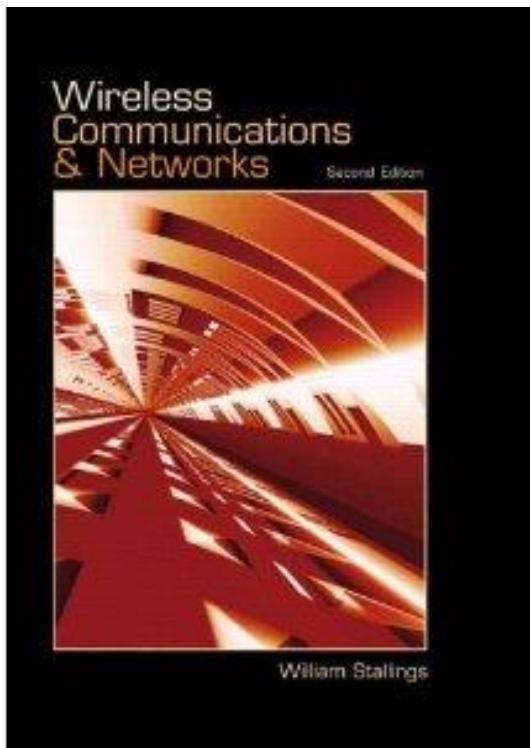
Overview of Wireless Communication System

Text
Voice
Video

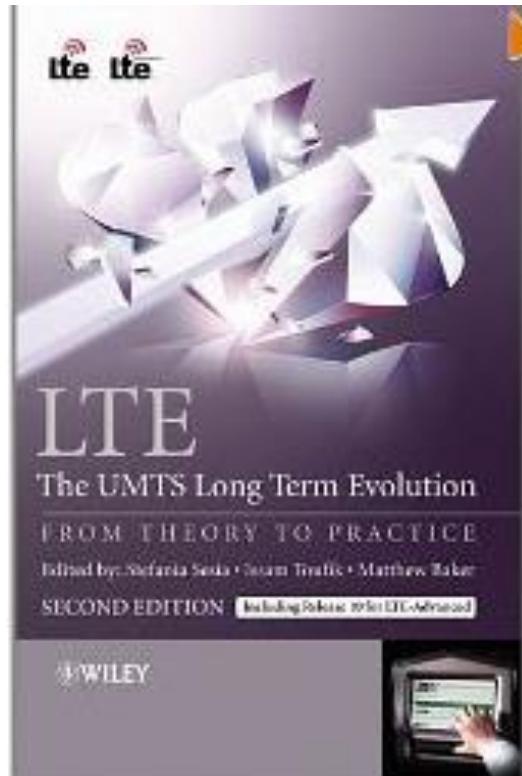


Reference books for week 4

Wireless Communications and Networks, Second Edition. by **William Stallings**



LTE: The UMTS Long Term Evolution: from Theory to Practice
by Stefania Sesia, Matthew Baker and Mr Issam Toufik



Modulation Techniques



Reasons for Choosing Encoding Techniques

- ◆ Digital data, digital signal
 - Equipment less complex and expensive than digital-to-analog modulation equipment
- ◆ Analog data, digital signal
 - Permits use of modern digital transmission and switching equipment
- ◆ Digital data, analog signal
 - Some transmission media will only propagate analog signals
 - E.g., optical fiber and unguided media
- ◆ Analog data, analog signal
 - Analog data in electrical form can be transmitted easily and cheaply
 - Done with voice transmission over voice-grade lines

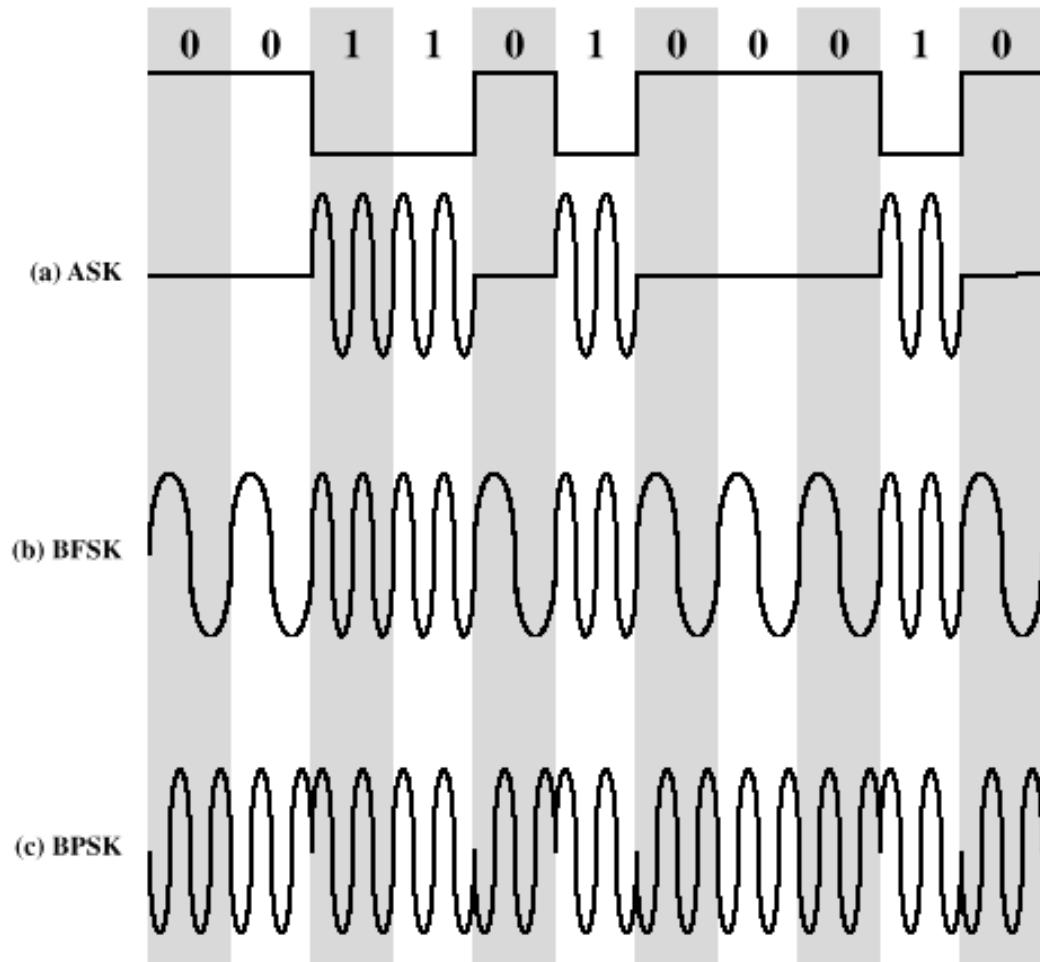
Signal Encoding Criteria

- ◆ What determines how successful a receiver will be in interpreting an incoming signal?
 - Signal-to-noise ratio
 - Data rate
 - Bandwidth
- ◆ An increase in data rate increases bit error rate
- ◆ An increase in SNR decreases bit error rate
- ◆ An increase in bandwidth allows an increase in data rate

Basic Encoding Techniques

- ◆ Digital data to analog signal
 - Amplitude-shift keying (ASK)
 - Amplitude difference of carrier frequency
 - Frequency-shift keying (FSK)
 - Frequency difference near carrier frequency
 - Phase-shift keying (PSK)
 - Phase of carrier signal shifted

Basic Encoding Techniques



Modulation of Analog Signals for Digital Data

Amplitude-Shift Keying

- ◆ One binary digit represented by presence of carrier, at constant amplitude
- ◆ Other binary digit represented by absence of carrier

$$s(t) = \begin{cases} A\cos(2\pi f_c t) & \text{binary 1} \\ 0 & \text{binary 0} \end{cases}$$

- where the carrier signal is $A\cos(2\pi f_c t)$

Binary Frequency-Shift Keying (BFSK)

- ◆ Two binary digits represented by two different frequencies near the carrier frequency

$$s(t) = \begin{cases} A \cos(2\pi f_1 t) & \text{binary 1} \\ A \cos(2\pi f_2 t) & \text{binary 0} \end{cases}$$

- where f_1 and f_2 are offset from carrier frequency f_c by equal but opposite amounts

Multiple Frequency-Shift Keying (MFSK)

- ◆ More than two frequencies are used
- ◆ More bandwidth efficient and less susceptible to error

$$s_i(t) = A \cos 2\pi f_i t \quad 1 \leq i \leq M$$

- $f_i = f_c + (2i - 1 - M)f_d$
- f_c = the carrier frequency
- f_d = the difference frequency
- M = number of different signal elements = 2^L
- L = number of bits per signal element

Multiple Frequency-Shift Keying (MFSK)

- ◆ To match data rate of input bit stream, each output signal element is held for:

$$T_s = LT \text{ seconds}$$

where T is the bit period (data rate = $1/T$)

- ◆ One signal element encodes L bits.
- ◆ The total bandwidth required is

$$2Mf_d$$

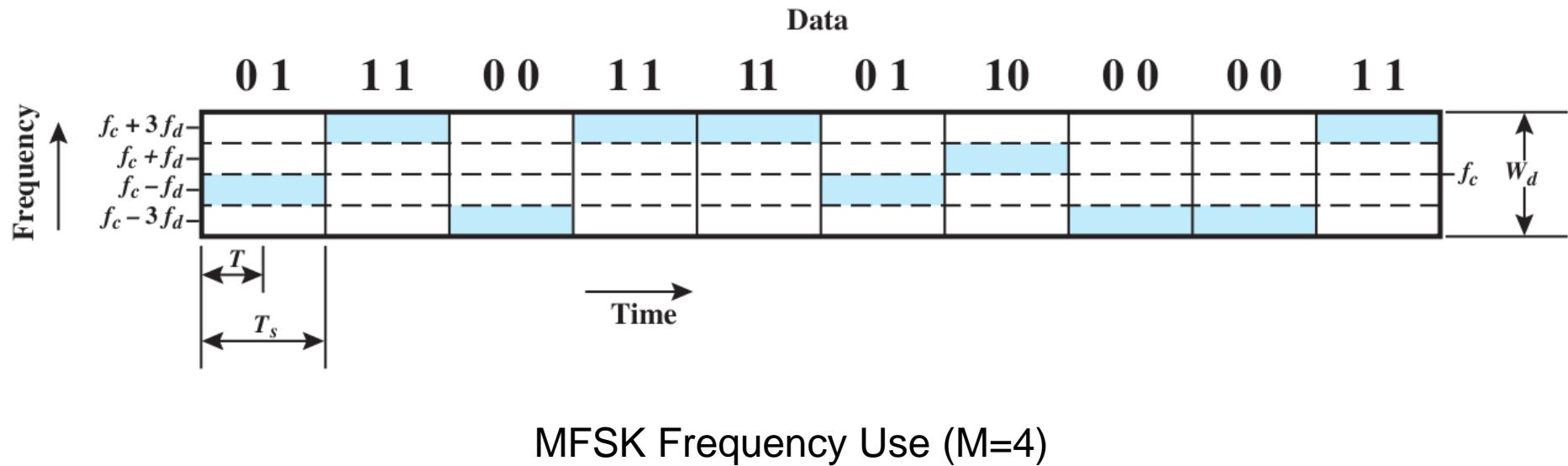
- ◆ Minimum frequency separation required

$$2f_d = 1/T_s$$

- ◆ Therefore, modulator requires a bandwidth of

$$W_d = 2^L / LT = M / T_s$$

Multiple Frequency-Shift Keying (MFSK)



MFSK Frequency Use (M=4)

Phase-Shift Keying (PSK)

- ◆ Two-level PSK (BPSK)
 - Uses two phases to represent binary digits

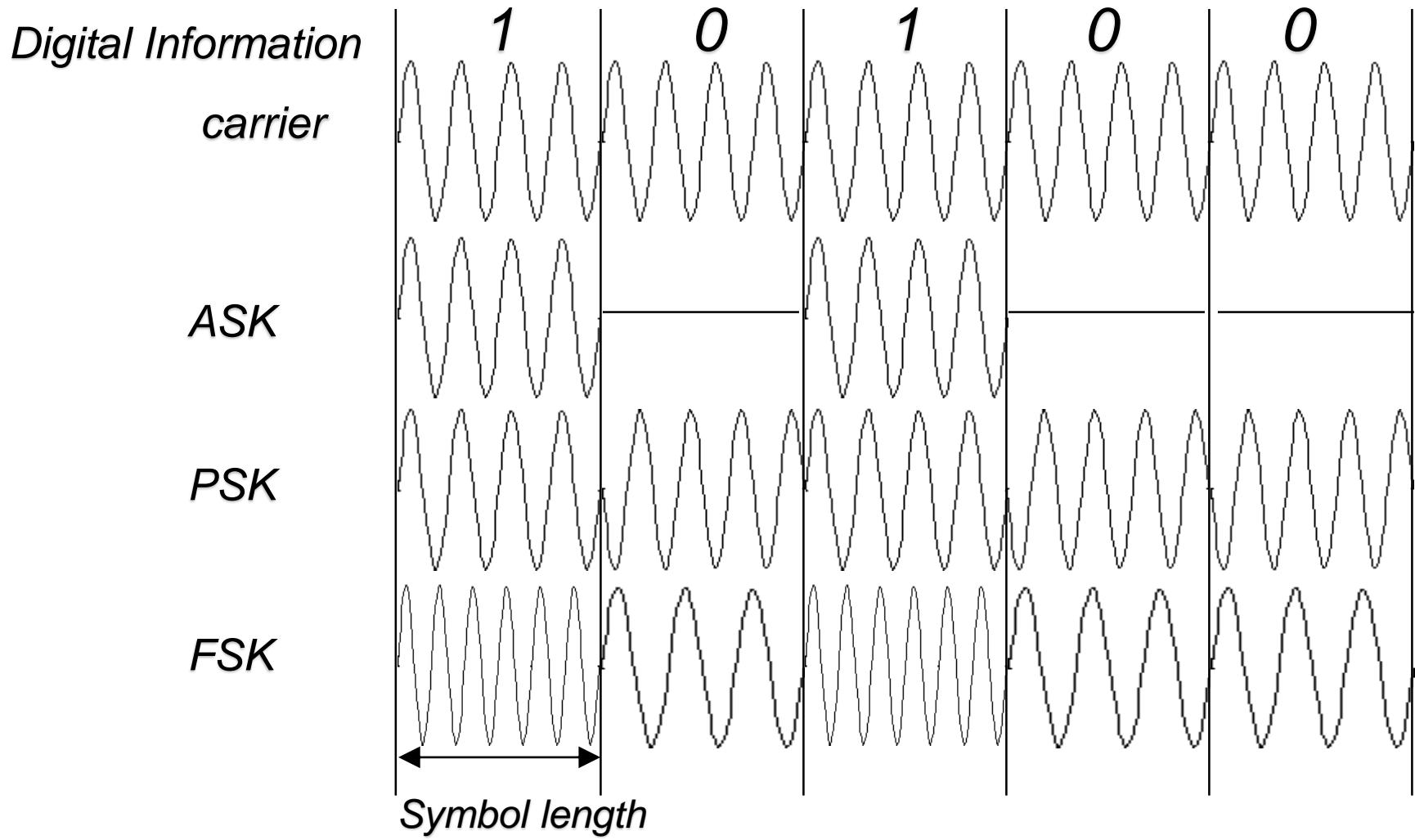
$$s(t) = \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ A \cos(2\pi f_c t + \pi) & \text{binary 0} \end{cases}$$
$$= \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ -A \cos(2\pi f_c t) & \text{binary 0} \end{cases}$$

Phase-Shift Keying (PSK)

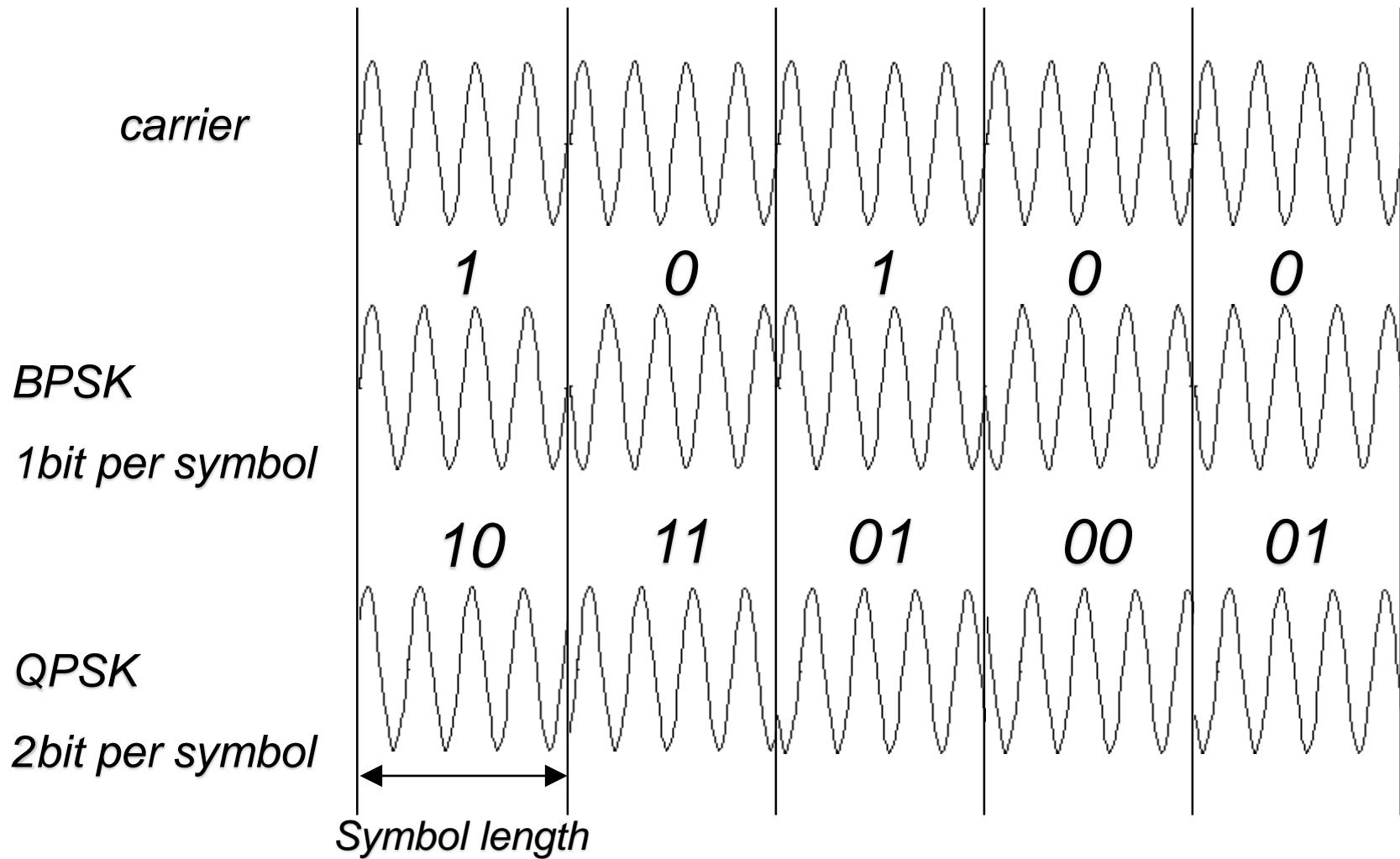
- ◆ Four-level PSK (QPSK)
 - Each element represents more than one bit

$$s(t) = \begin{cases} A \cos\left(2\pi f_c t + \frac{\pi}{4}\right) & 00 \\ A \cos\left(2\pi f_c t + \frac{3\pi}{4}\right) & 01 \\ A \cos\left(2\pi f_c t - \frac{3\pi}{4}\right) & 11 \\ A \cos\left(2\pi f_c t - \frac{\pi}{4}\right) & 10 \end{cases}$$

Symbol Waveform



Multi bit modulation



Mathematical expression of digital modulation

- ◆ Transmission signal can be expressed as follows

$$s(t) = \cos(2\pi \cdot f_c \cdot t + \theta_k)$$

$$= \cos \theta_k \cdot \cos(2\pi \cdot f_c \cdot t) - \sin \theta_k \cdot \sin(2\pi \cdot f_c \cdot t)$$

Let, $a_k = \cos \theta_k, b_k = \sin \theta_k$

$$s(t) = \operatorname{Re}[(a_k + jb_k)e^{j2\pi f_c \cdot t}] \text{ [Euler's formula: } \cos \theta_k = \operatorname{Re}(e^{j\theta_k})]$$

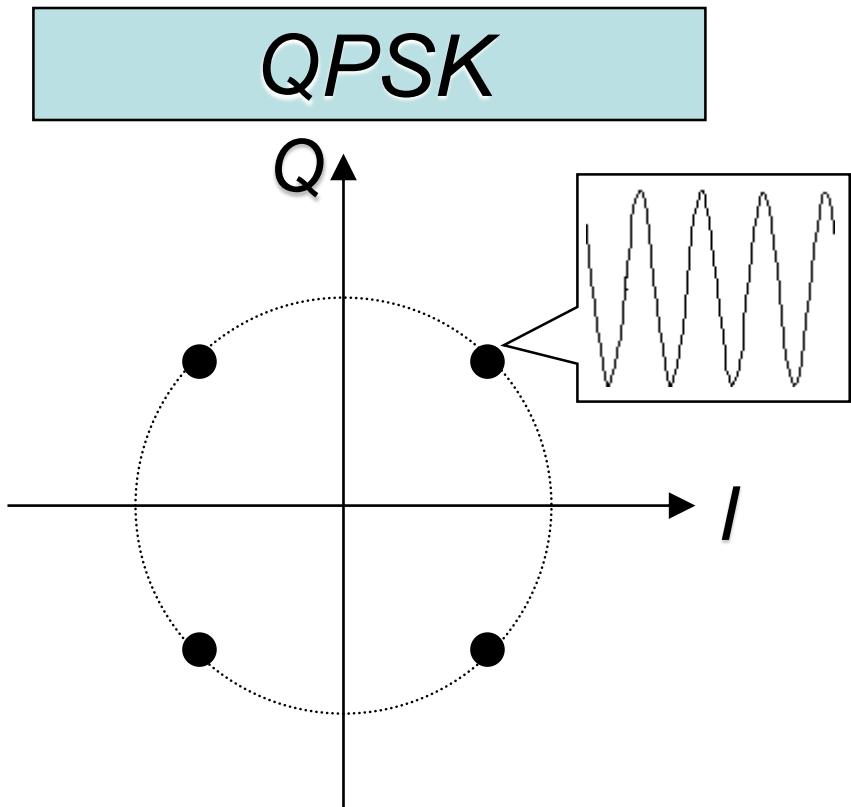
- ◆ $s(t)$ can be expressed by complex base-band signal $(a_k + jb_k)e^{j2\pi f_c \cdot t}$
 $e^{j2\pi f_c \cdot t}$ *Indicates carrier sinusoidal*
 $(a_k + jb_k)$ *Digital modulation*

Digital modulation can be expressed by the complex number

Constellation map

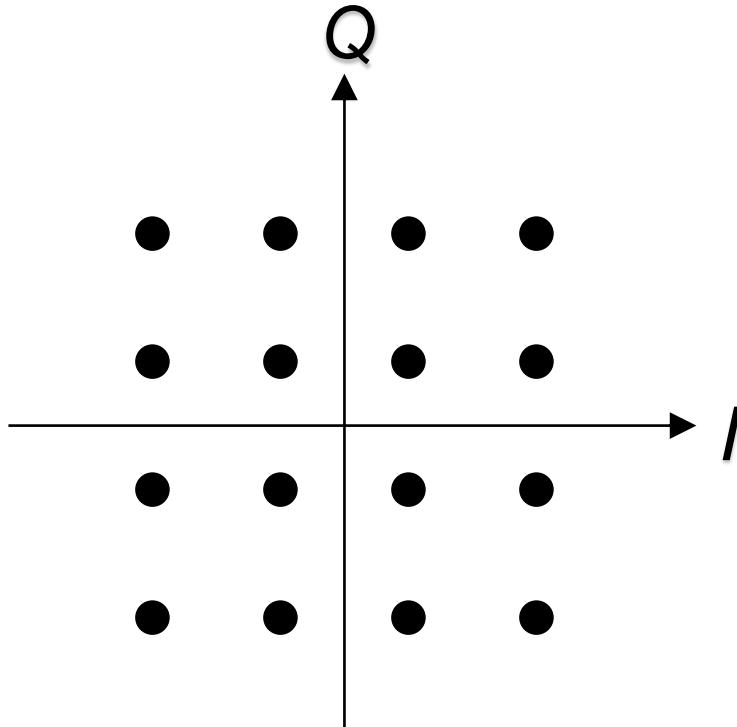
- ◆ $(a_k + jb_k)$ is plotted on I(real)-Q(imaginary) plane

data	Phase	a_k	b_k
00	$\pi/4$	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
01	$3\pi/4$	$-\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
11	$5\pi/4$	$-\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$
10	$7\pi/4$	$\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$

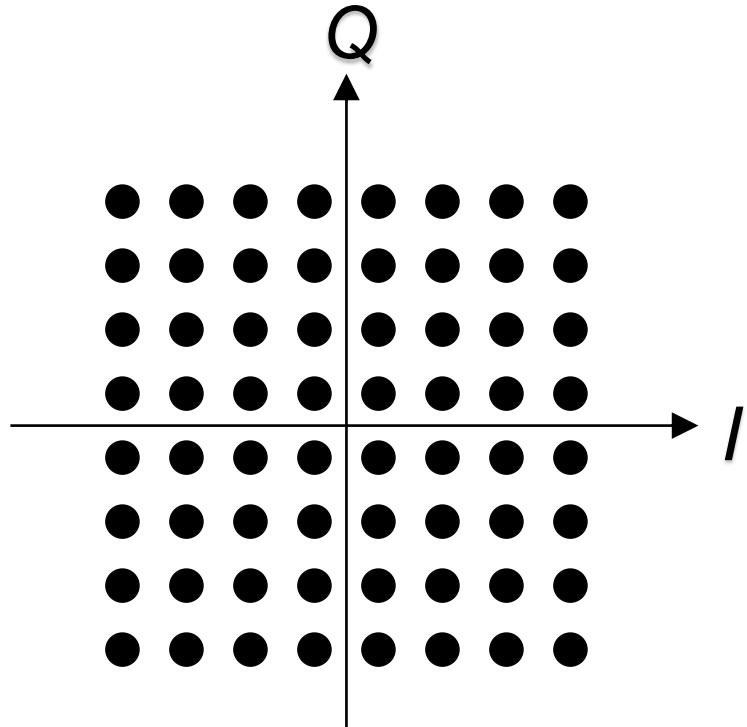


Quadrature Amplitude Modulation (QAM)

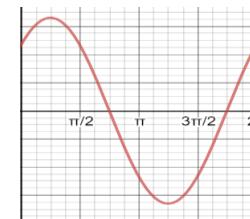
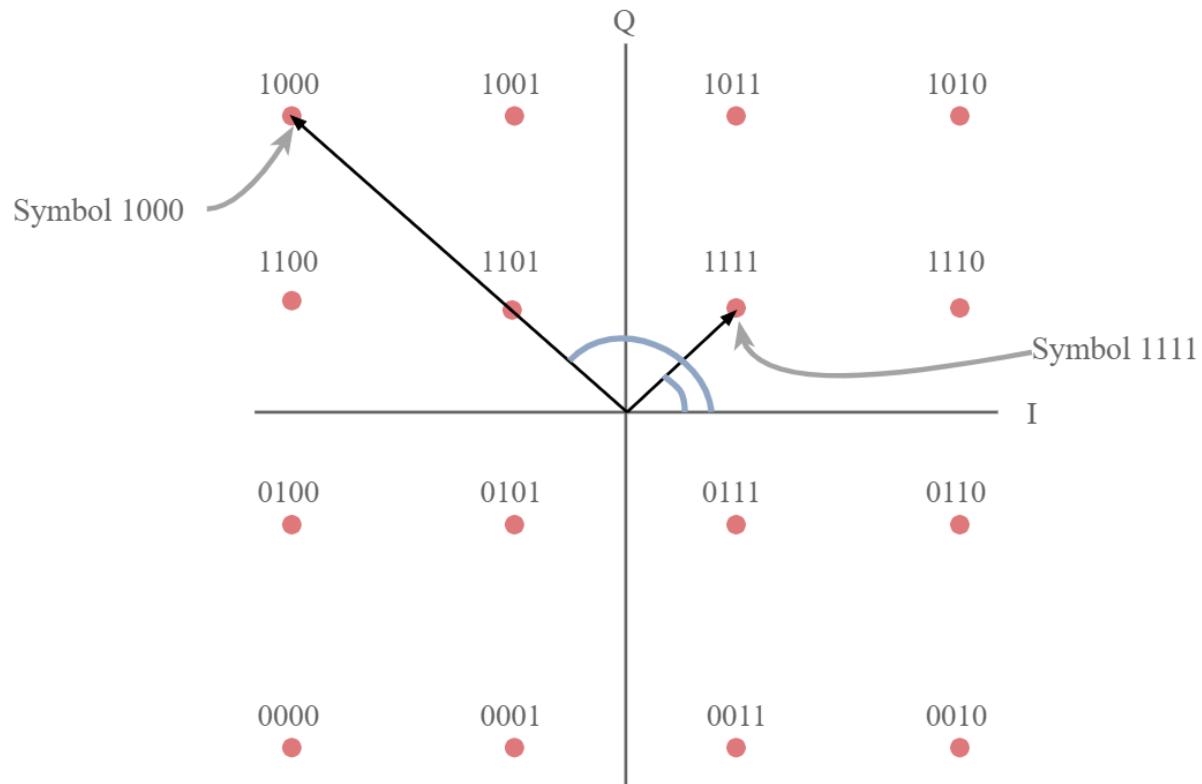
16QAM



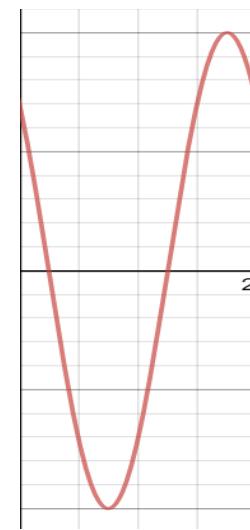
64QAM



Quadrature Amplitude Modulation (QAM)



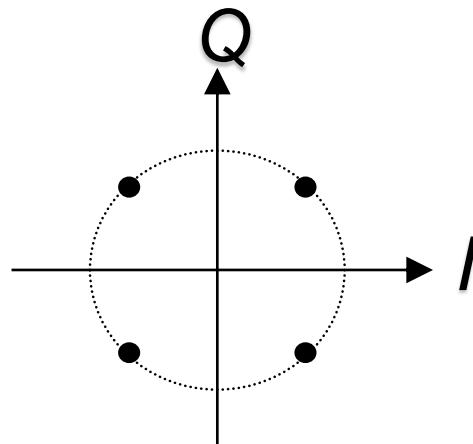
1111



1000

Summary of digital modulation

- ◆ Type of modulation: ASK,PSK,FSK,QAM
- ◆ OFDM uses PSK and QAM
- ◆ Digital modulation is mathematically characterized by the coefficient of complex base-band signal
 $(a_k + jb_k)$
- ◆ Plot of the coefficients gives the constellation map

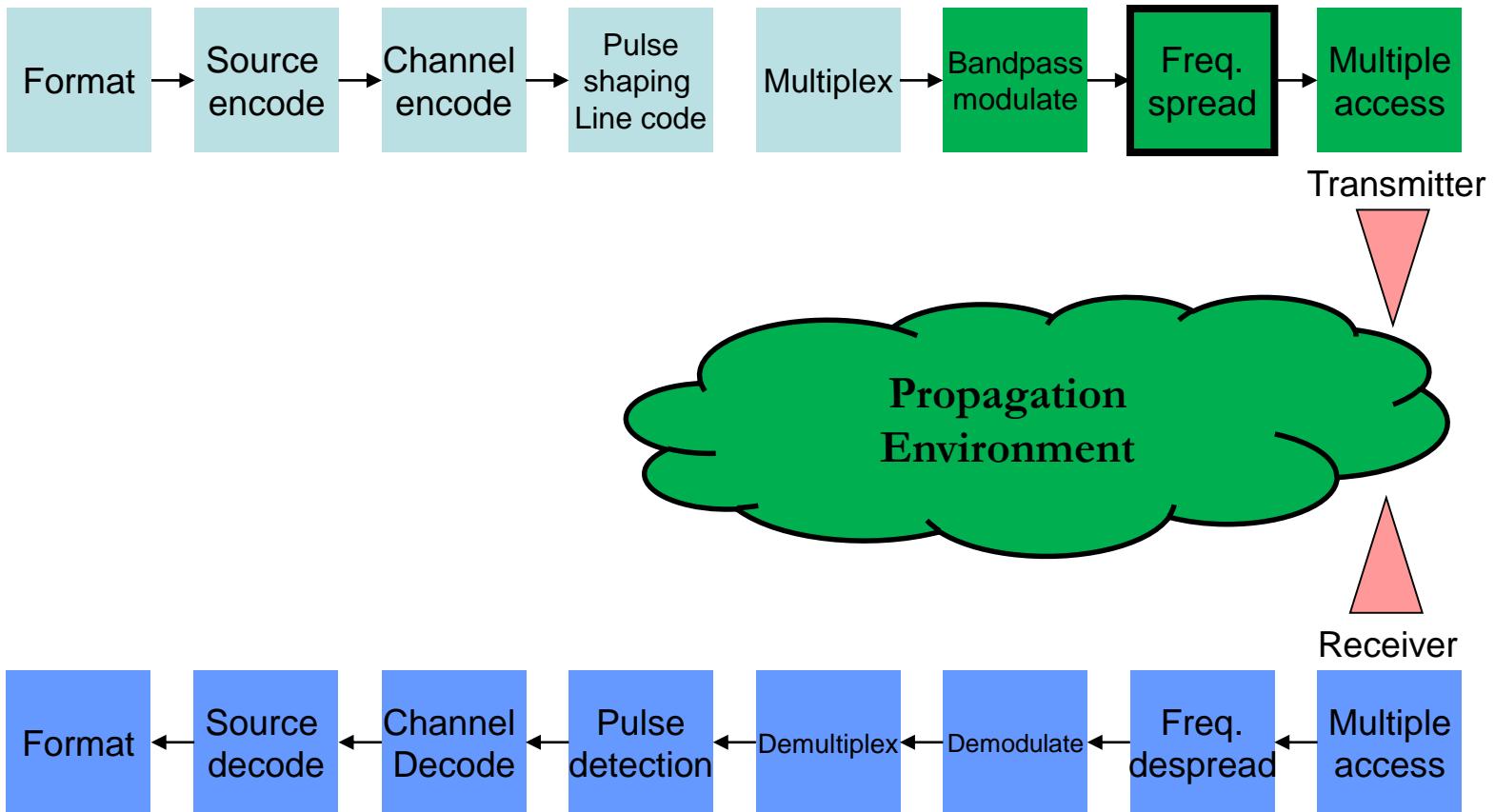


Spread Spectrum (Freq. Spread)



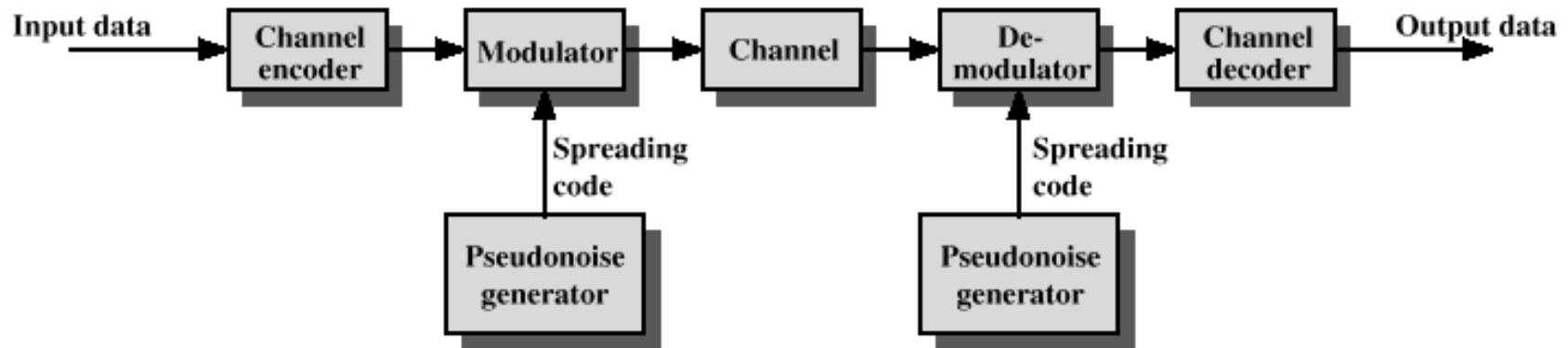
Overview of Wireless Communication System

Text
Voice
Video



Spread Spectrum

- ◆ Input is fed into a channel encoder
 - Produces analog signal with narrow bandwidth
- ◆ Signal is further modulated using sequence of digits
 - Spreading code or spreading sequence
 - Generated by pseudonoise, or pseudo-random number generator



Spread Spectrum

- Idea of this modulation is to increase bandwidth of signal to be transmitted and to make jamming and interception more difficult.
- General Techniques of Spread Spectrum in Digital Communication System:
 1. Frequency Hoping Spread Spectrum (FHSS)
 2. Direct Sequence Spread Spectrum (DSSS)

Frequency Hoping Spread Spectrum (FHSS)

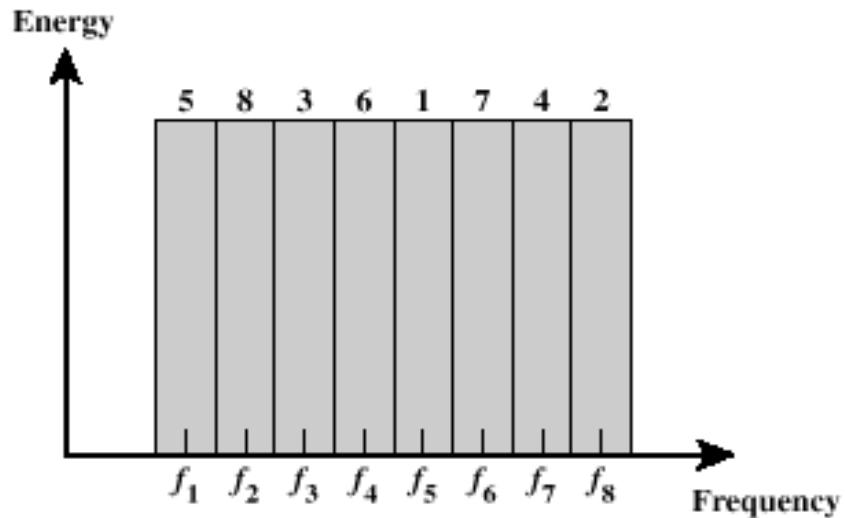
- ◆ Signal is broadcasted over seemingly random series of radio frequencies
 - A number of channels allocated for the FH signal.
 - Width of each channel corresponds to bandwidth of input signal
- ◆ Signal hops from frequency to frequency at fixed intervals
 - Transmitter operates in one channel at a time
 - Bits are transmitted using some encoding scheme
 - At each successive interval, a new carrier frequency is selected



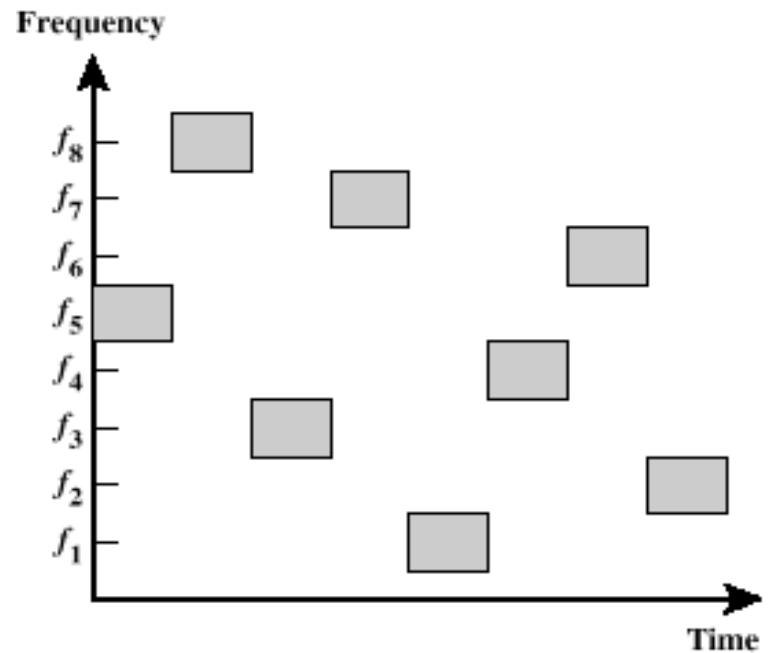
Frequency Hoping Spread Spectrum

- ◆ Channel sequence dictated by spreading code
 - ◆ Receiver, hopping between frequencies in synchronization with transmitter, picks up message
 - ◆ Both transmitter and receiver use the same code to tune into a sequence of channels in synchronization. On reception, the spread spectrum signal is demodulated using the same sequence
-
- ◆ **Advantages**
 - Eavesdroppers hear only unintelligible blips
 - Attempts to jam signal on one frequency succeed only at knocking out a few bits

Frequency Hoping Spread Spectrum



(a) Channel assignment



(b) Channel use

Frequency Hopping Example

FHSS Using MFSK

- ◆ MFSK signal is translated to a new frequency every T_c seconds by modulating the MFSK signal with the FHSS carrier signal
- ◆ The effect is to translate the MFSK signal into the appropriate FHSS channel.
- ◆ For data rate of R :
 - duration of a bit: $T = 1/R$ seconds
 - duration of signal element: $T_s = LT$ seconds
- ◆ $T_c \geq T_s$ - slow-frequency-hop spread spectrum
- ◆ $T_c < T_s$ - fast-frequency-hop spread spectrum

FHSS Performance Considerations

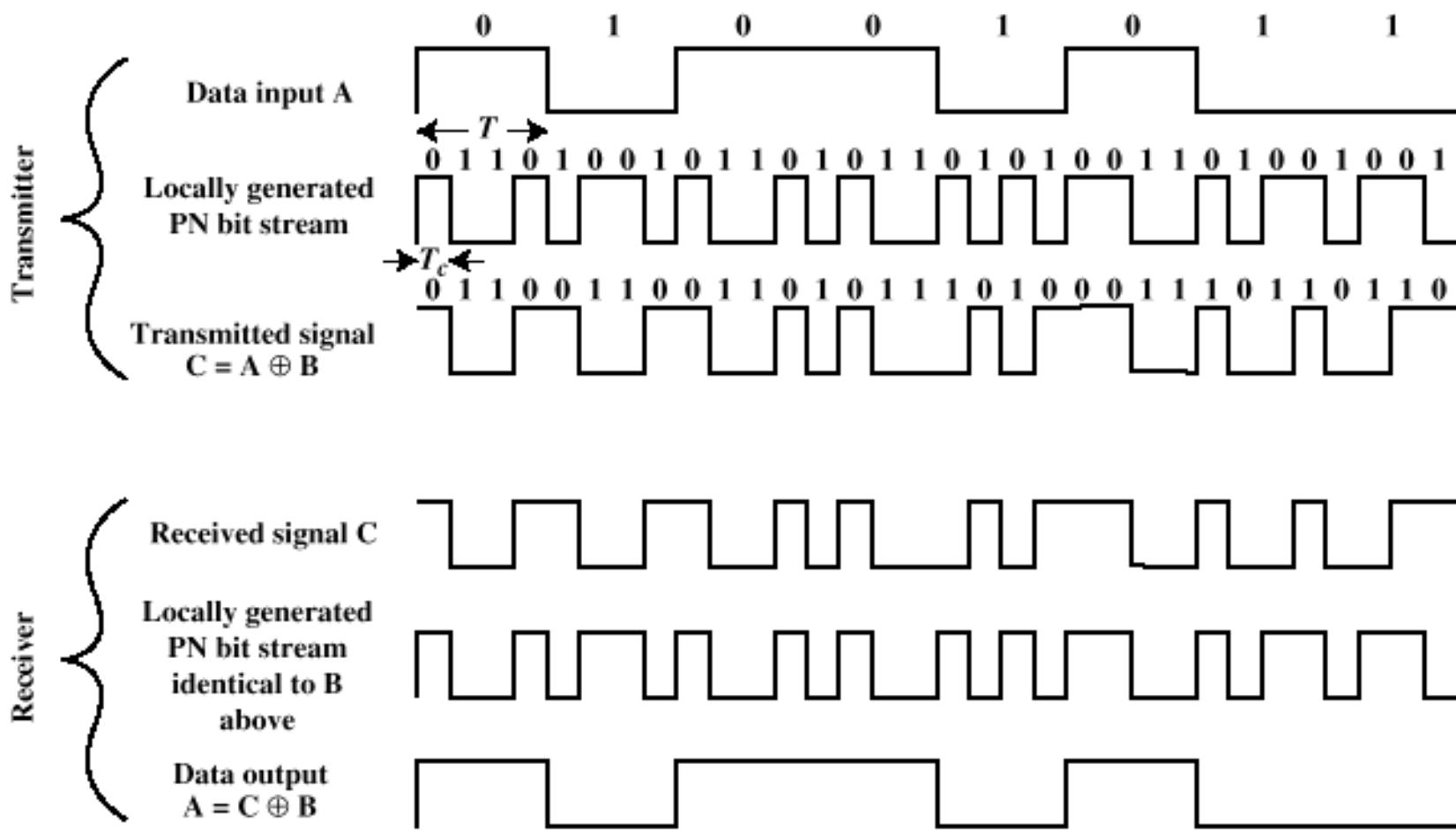
- ◆ Large number of frequencies are used
- ◆ Results in a system that is quite resistant to jamming
 - Jammer must jam all frequencies
 - With fixed power, this reduces the jamming power in any one frequency band



Direct Sequence Spread Spectrum (DSSS)

- ◆ Each bit in original signal is represented by multiple bits in the transmitted signal
- ◆ Spreading code spreads signal across a wider frequency band
 - Spread is in direct proportion to number of bits used
- ◆ One technique combines digital information stream with the spreading code bit stream using exclusive-OR (Figure in next slide)

Direct Sequence Spread Spectrum (DSSS)



DSSS Using BPSK

- ◆ Multiply BPSK signal,

$$s_d(t) = A d(t) \cos(2\pi f_c t)$$

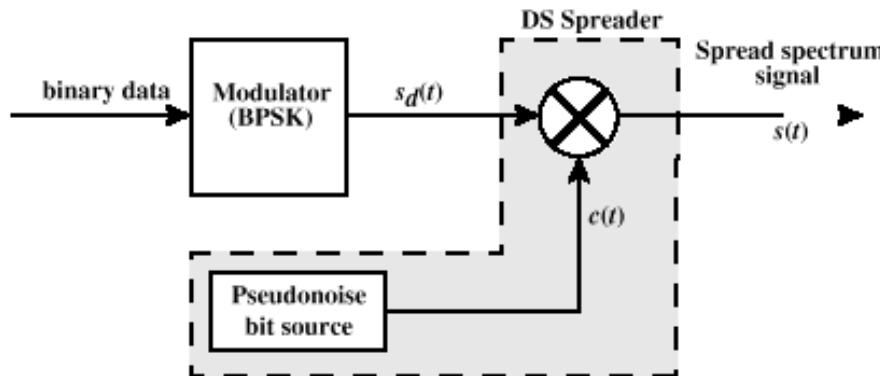
by $c(t)$ [PN sequence taking values +1, -1] to get

$$s(t) = A d(t)c(t) \cos(2\pi f_c t)$$

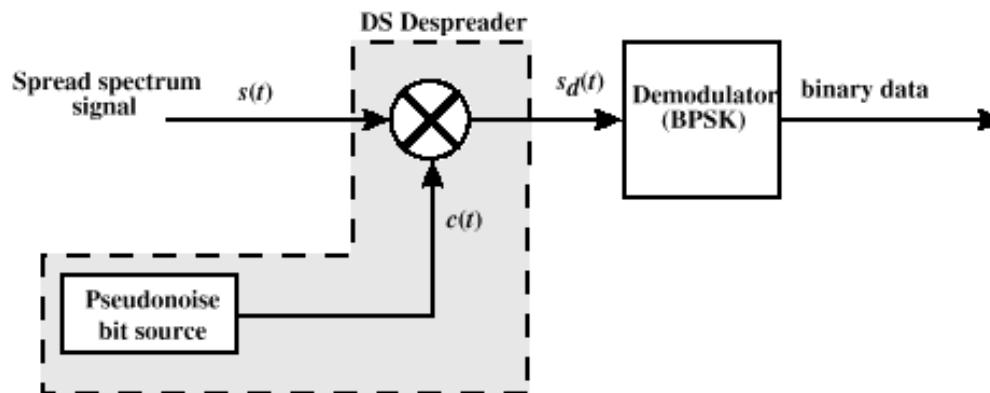
- A = amplitude of signal
- f_c = carrier frequency
- $d(t)$ = discrete function [+1, -1]

- ◆ At receiver, incoming signal is multiplied by $c(t)$
 - Since, $c(t) \times c(t) = 1$, incoming signal is recovered

DSSS Using BPSK



(a) Transmitter



(b) Receiver

Direct Sequence Spread Spectrum

Code-Division Multiple Access (CDMA)

◆ Basic Principles of CDMA

- D = rate of data signal
- Break each bit into k *chips*
 - Chips are a user-specific fixed pattern
- Chip data rate of new channel = kD

CDMA Example

- ◆ If $k=6$ and code is a sequence of 1s and -1s
 - For a '1' bit, A sends code as chip pattern
 - $\langle c_1, c_2, c_3, c_4, c_5, c_6 \rangle$
 - For a '0' bit, A sends complement of code
 - $\langle -c_1, -c_2, -c_3, -c_4, -c_5, -c_6 \rangle$
- ◆ Receiver knows sender's code and performs electronic decode function
 - $\langle d_1, d_2, d_3, d_4, d_5, d_6 \rangle$ = received chip pattern
 - $\langle c_1, c_2, c_3, c_4, c_5, c_6 \rangle$ = sender's code

$$S_u(d) = d_1 \times c_1 + d_2 \times c_2 + d_3 \times c_3 + d_4 \times c_4 + d_5 \times c_5 + d_6 \times c_6$$

CDMA Example

- ◆ User A code = $\langle 1, -1, -1, 1, -1, 1 \rangle$
 - To send a 1 bit = $\langle 1, -1, -1, 1, -1, 1 \rangle$
 - To send a 0 bit = $\langle -1, 1, 1, -1, 1, -1 \rangle$
- ◆ User B code = $\langle 1, 1, -1, -1, 1, 1 \rangle$
 - To send a 1 bit = $\langle 1, 1, -1, -1, 1, 1 \rangle$
- ◆ Receiver receiving with A's code
 - (A's code) \times (received chip pattern)
 - User A '1' bit: 6 \rightarrow 1
 - User A '0' bit: -6 \rightarrow 0
 - User B '1' bit: 0 \rightarrow unwanted signal ignored

Categories of Spreading Sequences

- ◆ Spreading Sequence Categories
 - PN sequences
 - Orthogonal codes
- ◆ For FHSS systems
 - PN sequences most common
- ◆ For DSSS systems not employing CDMA
 - PN sequences most common
- ◆ For DSSS CDMA systems
 - PN sequences
 - Orthogonal codes

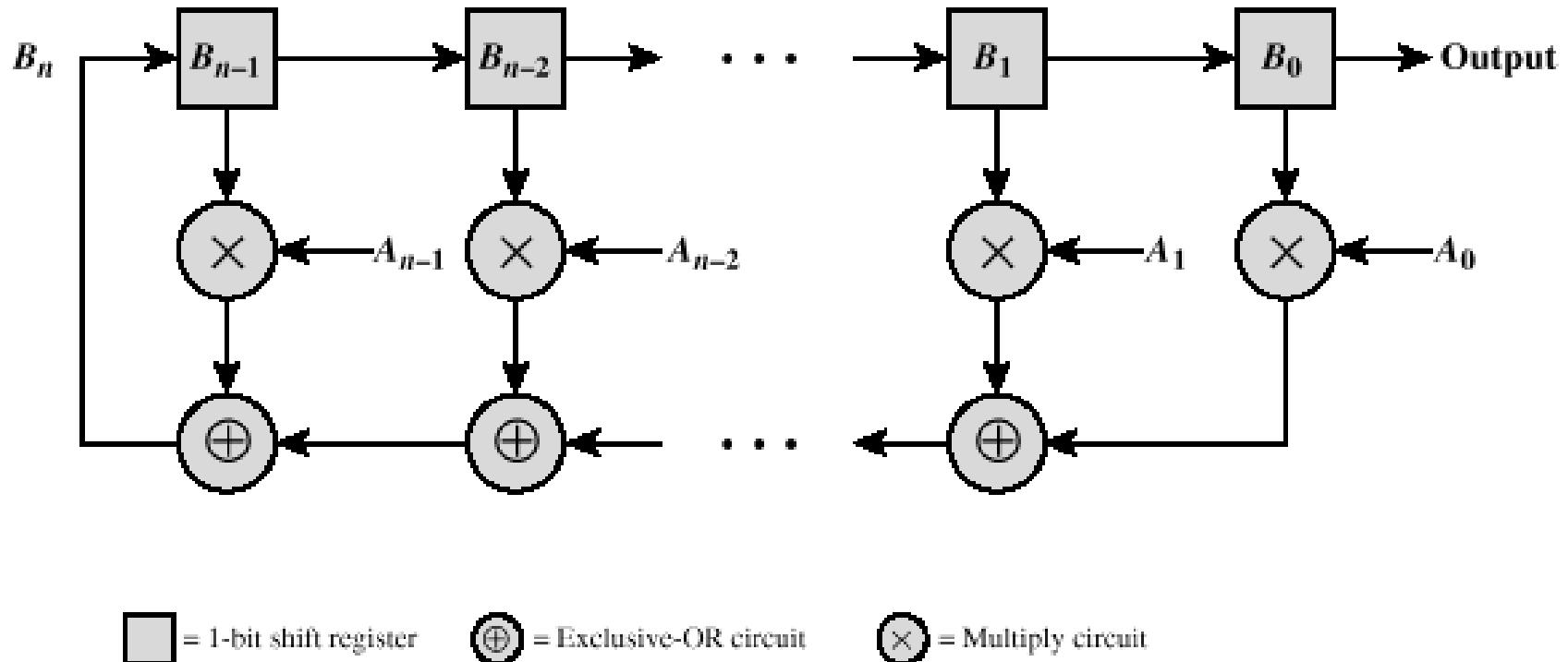
PN Sequences

- ◆ PN generator produces periodic sequence that appears to be random
- ◆ PN Sequences
 - Generated by an algorithm using initial seed
 - Sequence isn't statistically random but will pass many test of randomness
 - Sequences referred to as pseudorandom numbers or pseudonoise sequences
 - Unless algorithm and seed are known, the sequence is impractical to predict

Important PN Properties

- ◆ Randomness
 - Uniform distribution
 - Balance property
 - Run property
 - Independence
 - Correlation property
- ◆ Unpredictability

Linear Feedback Shift Register Implementation



Binary Linear Feedback Shift Register Sequence Generator

Properties of M-Sequences

- ◆ Property 1:
 - Has 2^{n-1} ones and $2^{n-1}-1$ zeros
- ◆ Property 2:
 - For a window of length n slide along output for $N (=2^n-1)$ shifts, each n -tuple appears once, except for the all zeros sequence
- ◆ Property 3:
 - Sequence contains one run of ones, length n
 - One run of zeros, length $n-1$
 - One run of ones and one run of zeros, length $n-2$
 - Two runs of ones and two runs of zeros, length $n-3$
 - 2^{n-3} runs of ones and 2^{n-3} runs of zeros, length 1



Properties of M-Sequences

- ◆ Property 4:
 - The periodic autocorrelation of a m-sequence is

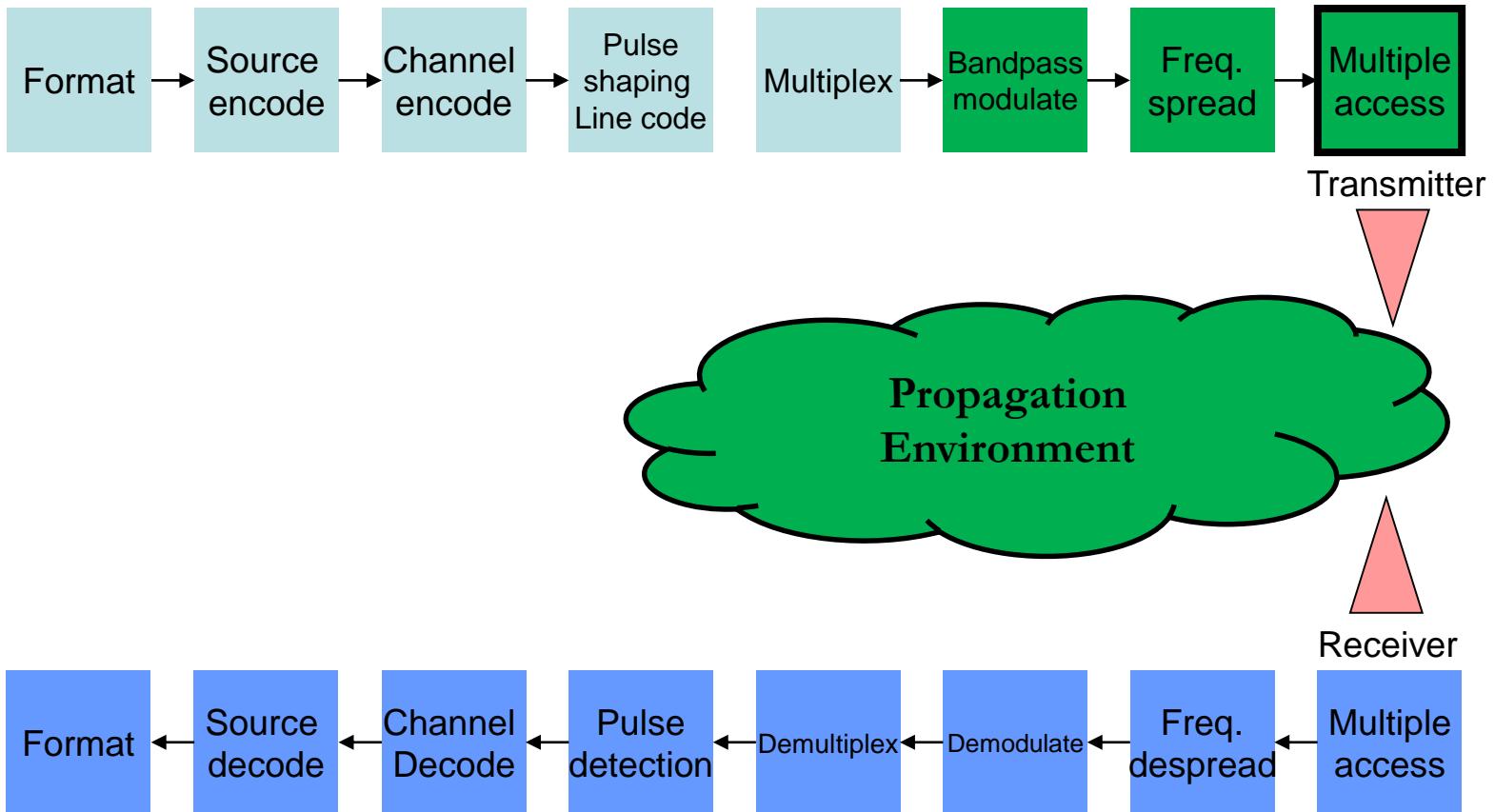
$$R(\tau) = \begin{cases} 1 & \tau = 0, N, 2N, \dots \\ -\frac{1}{N} & \text{otherwise} \end{cases}$$

Multiple Access Techniques



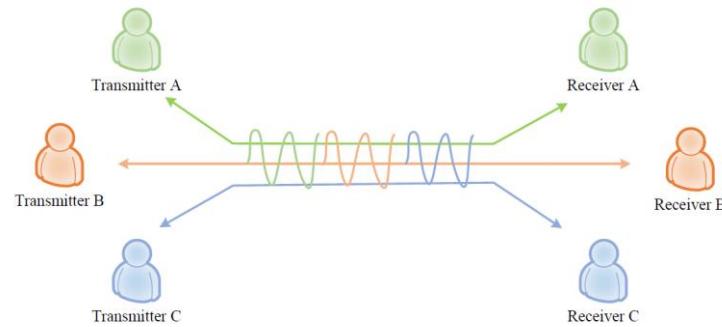
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Text
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Video



Multiple access

- ◆ **Multiple Access:** to enable multiple users to share the same channel simultaneously.

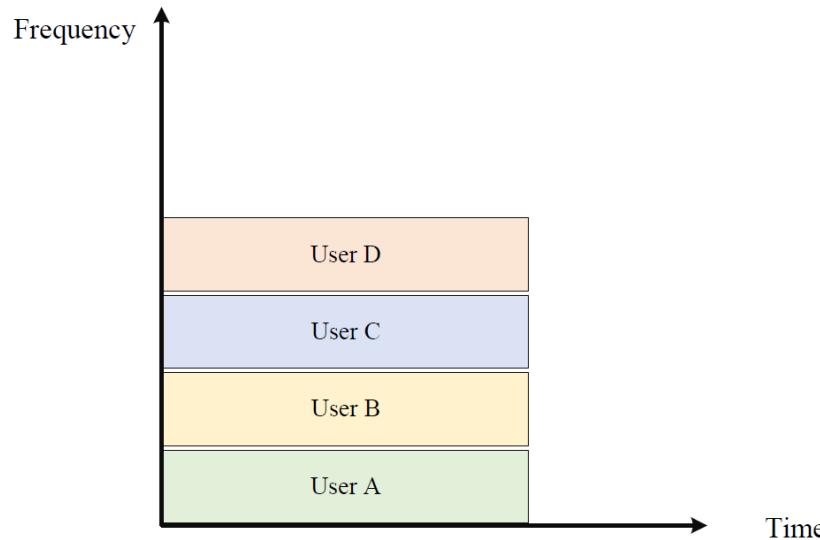


- ◆ Possible approaches for multiple access
 - Time.
 - Pitch.
 - Language.

Frequency Division Multiple Access (FDMA) - Pitch

- ◆ **Key features:**

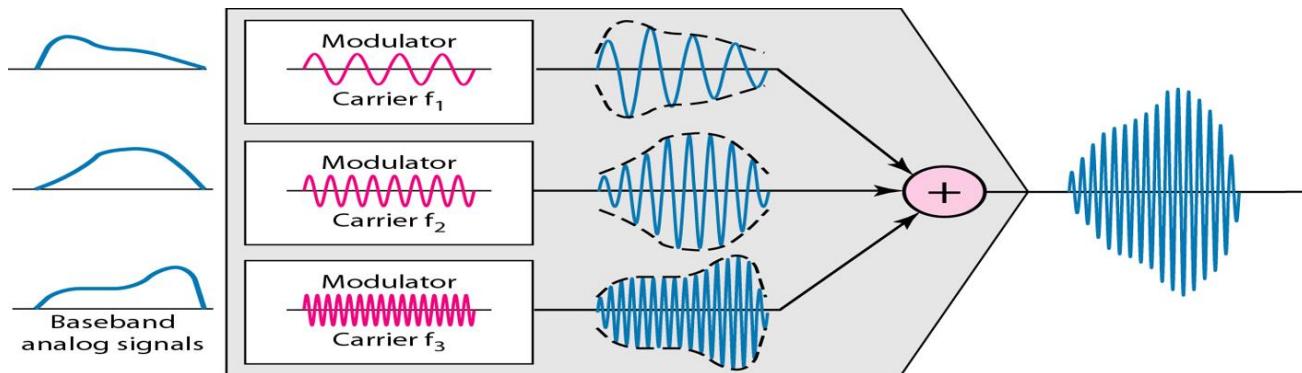
- Assign each user to a particular channel.
- Transmit signals simultaneously and continuously to enable multiple users to share the same channel simultaneously.



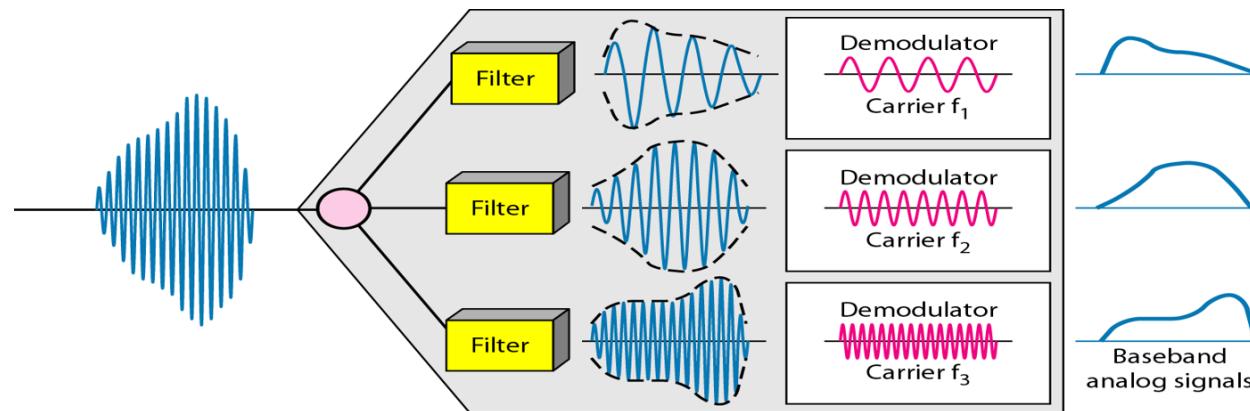
- ◆ **Application:** all 1G systems use FDMA.

Frequency Division Multiple Access (FDMA)

- ◆ Transmitter:



- ◆ Receiver:



Frequency Division Multiple Access (FDMA)

- ◆ **Advantages**

- Low overhead
- Simple hardware at users and base stations

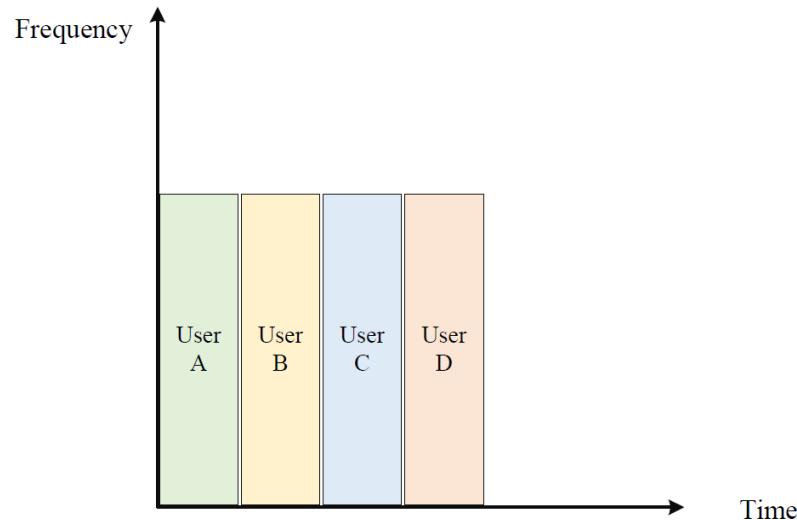
- ◆ **Disadvantages**

- If no talking, a channel sits idle (resource waste)
- Require tight radio frequency filters

Time Division Multiple Access (TDMA) - Time

- ◆ **Key features**

- Single carrier frequency with multiple users.
- Non-continuous transmission.
- Each user occupies a **cyclically repeating** time slot.



- ◆ **Application:** most 2G systems use TDMA.

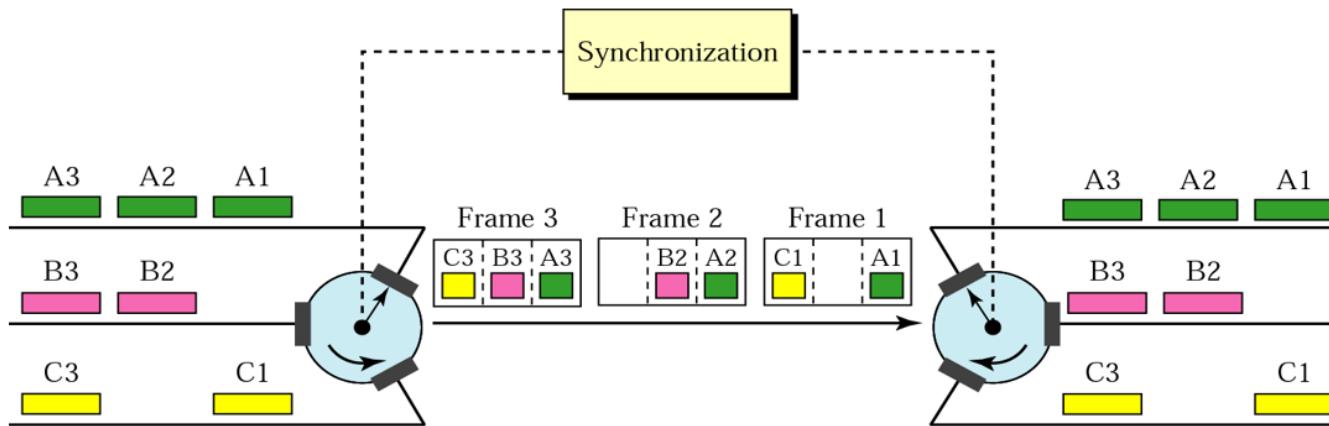
Time Division Multiple Access

- ◆ **Advantages**

- Interference-free technique.
- Low battery consumption.
- Slots can be assigned on demand.

- ◆ **Disadvantages:**

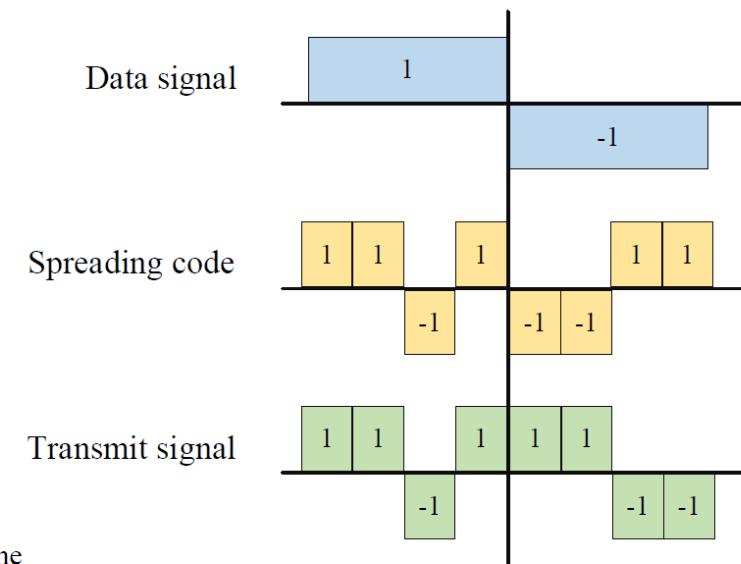
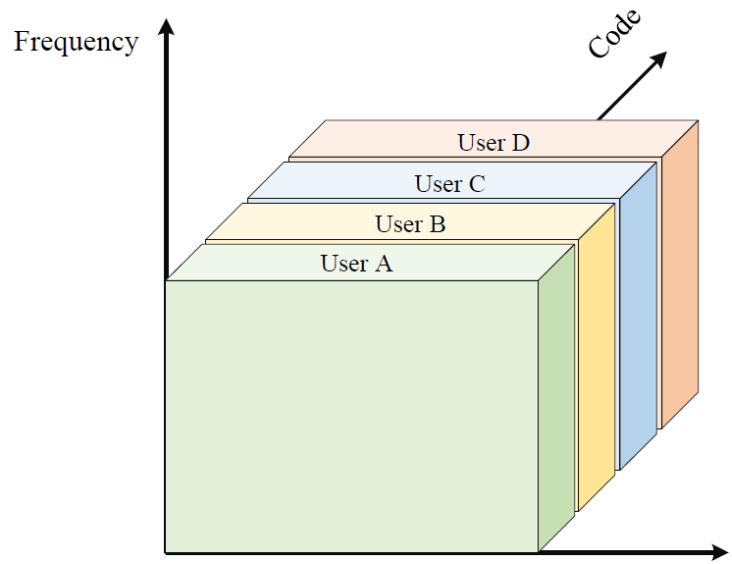
- “CLOCK” is required.
- Large synchronization overheads.
- Most 2G systems use TDMA



Code Division Multiple Access (CDMA) - Language

◆ Key features

- All users use same time and frequency.
- Narrowband signals multiplied by wideband spreading codes.



- ◆ **Application:** some 2G and most 3G systems.

Code Division Multiple Access (CDMA) - Language

◆ Advantages

- Easy addition of more users.
- No absolute limit on the number of users.

◆ Disadvantages

- Quality of Service (QoS) decreases as the number of users increases.
- Near-far problem exists (power control is required).

GSM Multiple access

- ◆ TDMA on each carrier
 - 8 time slots (channels) per carrier
- ◆ Multiple carriers (FDMA)
 - 200kHz spacing
 - Number of carriers per cell depends on network and radio planning
- ◆ So GSM uses combined TDMA/FDMA

OFDMA for 4G (3GPP LTE/LTE-A)

- ◆ **OFDM** =Orthogonal Frequency Division Multiplexing
- ◆ Many orthogonal sub-carriers are multiplexed in one symbol
 - What is the orthogonal?
 - How multiplexed?
 - What is the merit of OFDM?
 - What kinds of application?
 - What is the drawback of OFDM?

OFDMA for 4G (3GPP LTE/LTE-A)

- ◆ **OFDMA** =Orthogonal Frequency Division Multiple Access
- ◆ OFDMA is a multi-user version of the popular OFDM digital modulation scheme. Multiple access is achieved in OFDMA by assigning subsets of subcarriers to individual users.
- ◆ **Application:** 4G systems.

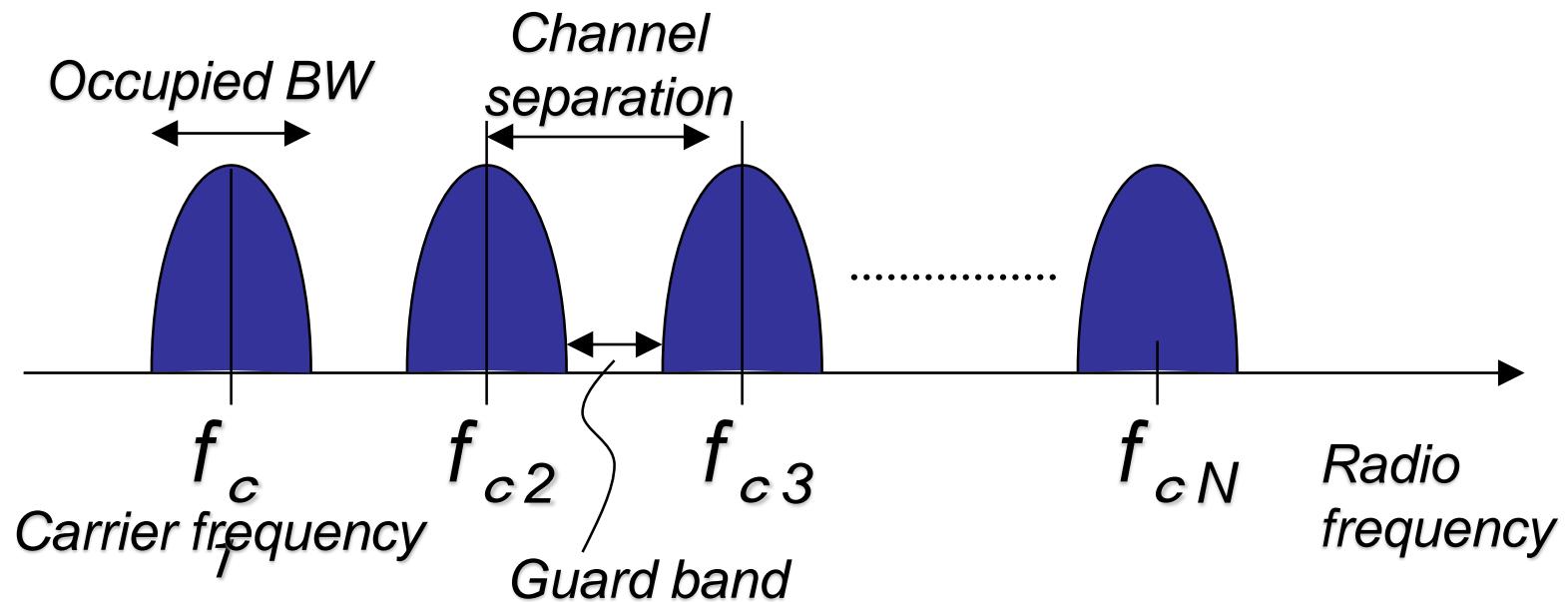


Why OFDM is getting popular ?

- ◆ State-of-the-art high bandwidth digital communication start using OFDM
 - Terrestrial Video Broadcasting in Japan and Europe
 - ADSL High Speed Modem
 - WLAN such as IEEE 802.11a/g/n
 - 3GPP LTE downlink
 - WiMAX as IEEE 802.16d/e
- ◆ Economical OFDM implementation become possible because of advancement in the LSI technology

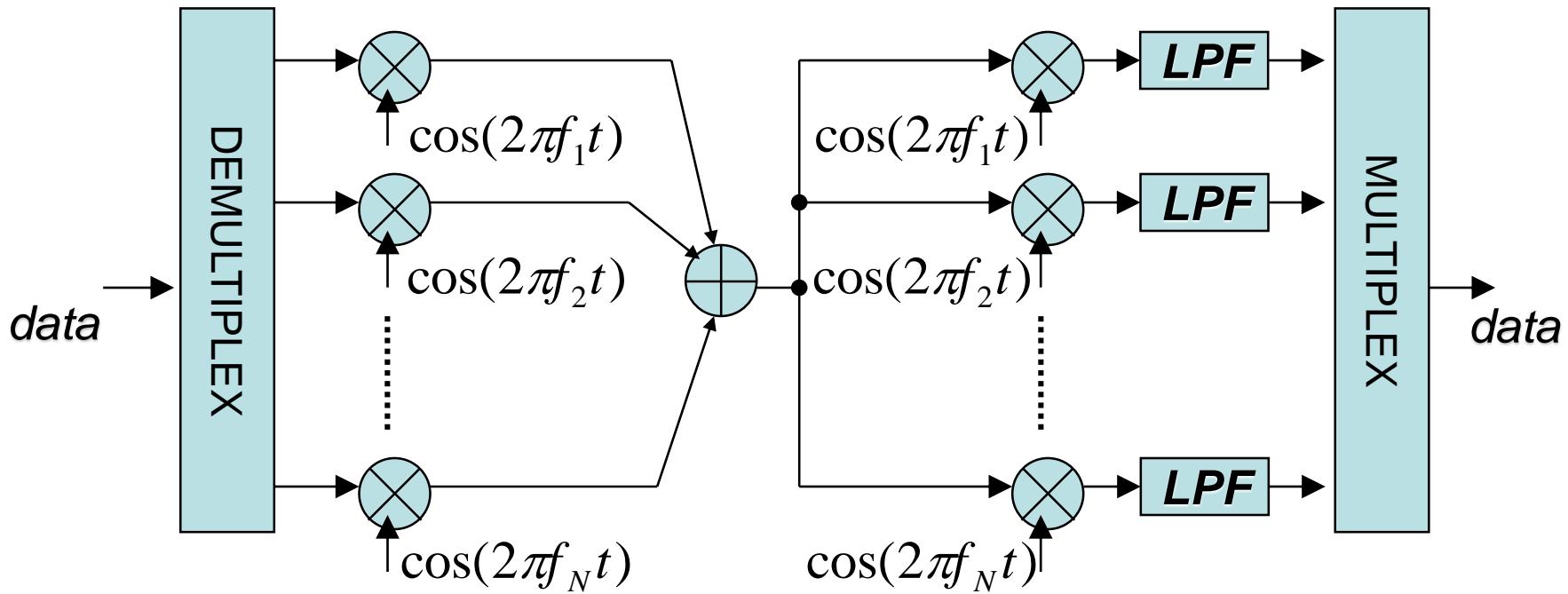
Frequency Division Multiple Access (FDMA)

- ◆ Old conventional method (Analog TV, Radio etc.)
- ◆ Use separate carrier frequency for individual transmission

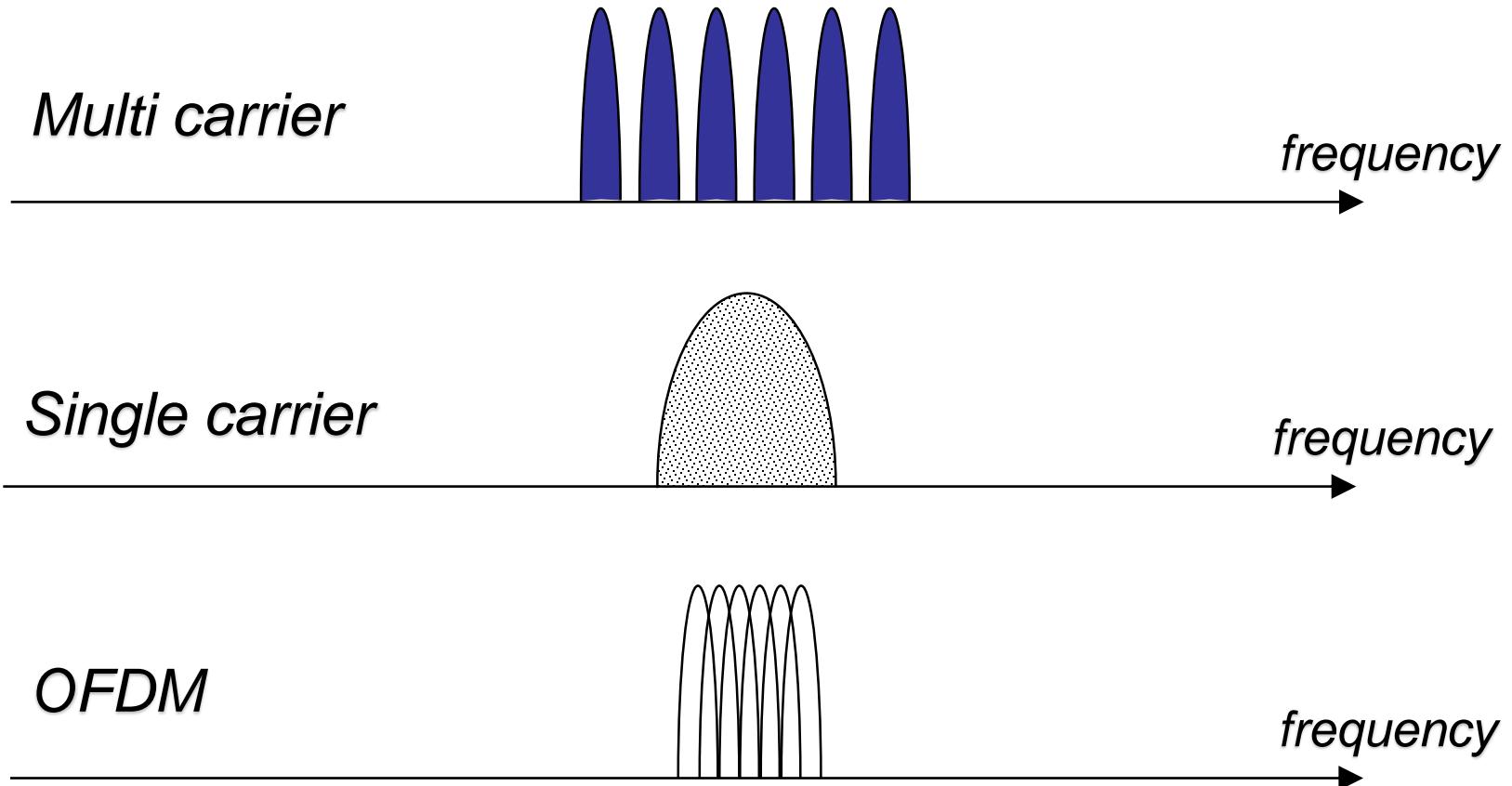


Multi-carrier modulation

- ◆ Use multiple channel (carrier frequency) for one data transmission



Spectrum comparison for same data rate transmission



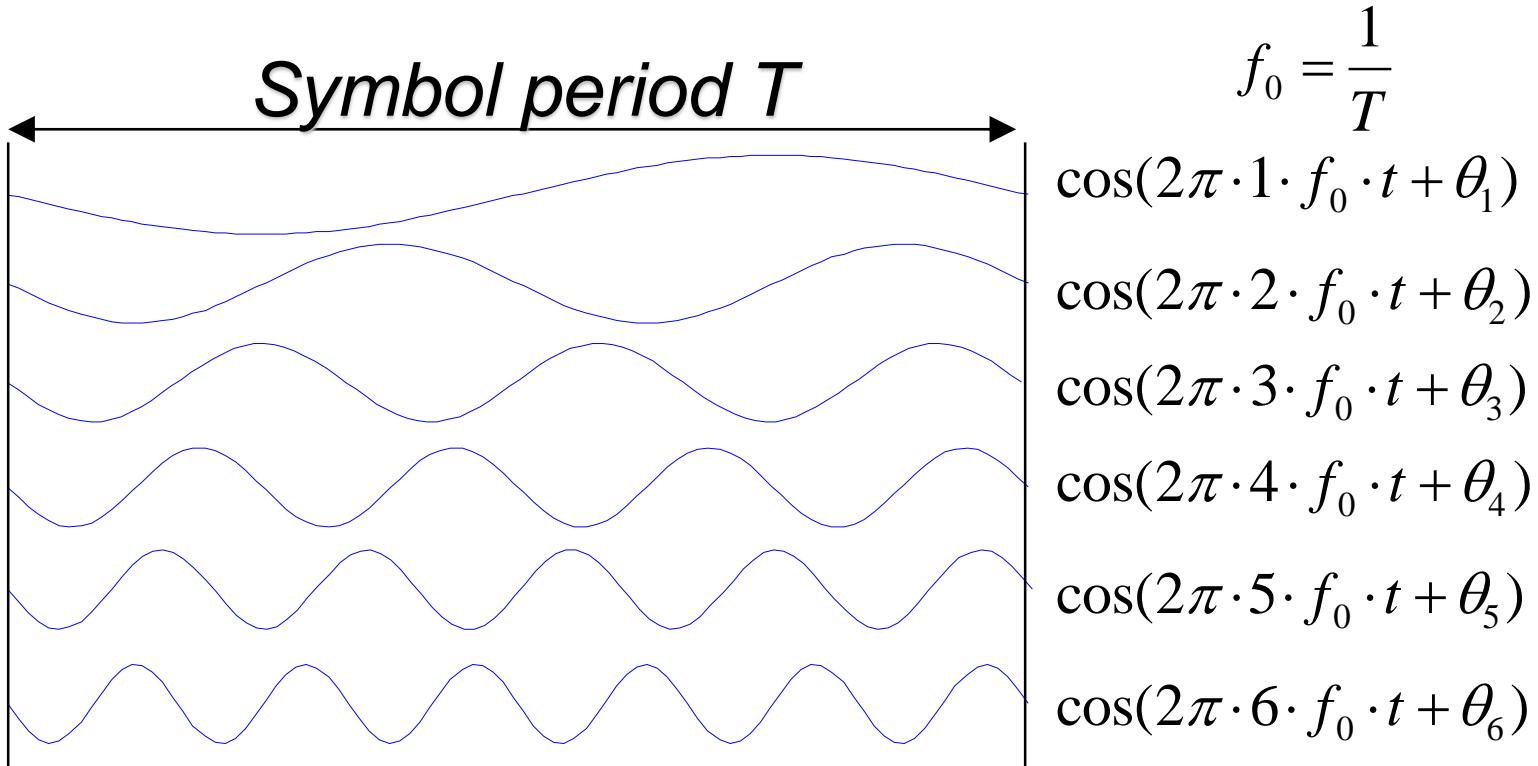
OFDM vs. Multi carrier

- ◆ OFDM is a multi-carrier modulation
- ◆ OFDM sub-carrier spectrum is overlapping
- ◆ In FDMA, band-pass filter separates each transmission
- ◆ In OFDM, each sub-carrier is separated by DFT because carriers are orthogonal
 - Condition of the orthogonality will be explained later
- ◆ Each sub-carrier is modulated by PSK, QAM

Thousands of PSK/QAM symbol can be simultaneously transmitted in one OFDM symbol

OFDM carriers

- ◆ OFDM carrier frequency is $n \cdot 1/T$



Sinusoidal Orthogonality

- m, n : integer, $T = 1/f_0$

$$\int_0^T \cos(2\pi m f_0 t) \cdot \cos(2\pi n f_0 t) dt = \begin{cases} \frac{T}{2} & (m = n) \\ 0 & (m \neq n) \end{cases} \rightarrow \text{Orthogonal}$$

$$\int_0^T \sin(2\pi m f_0 t) \cdot \sin(2\pi n f_0 t) dt = \begin{cases} \frac{T}{2} & (m = n) \\ 0 & (m \neq n) \end{cases} \rightarrow \text{Orthogonal}$$

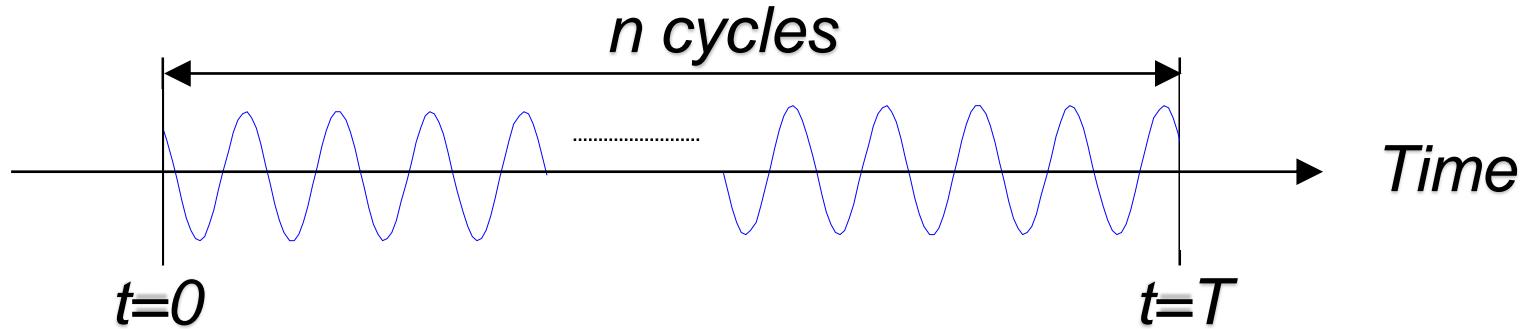
$$\int_0^T \cos(2\pi m f_0 t) \cdot \sin(2\pi n f_0 t) dt = 0$$

A sub-carrier of $f = nf_0$

$$a_n \cdot \cos(2\pi n f_0 t) - b_n \cdot \sin(2\pi n f_0 t)$$

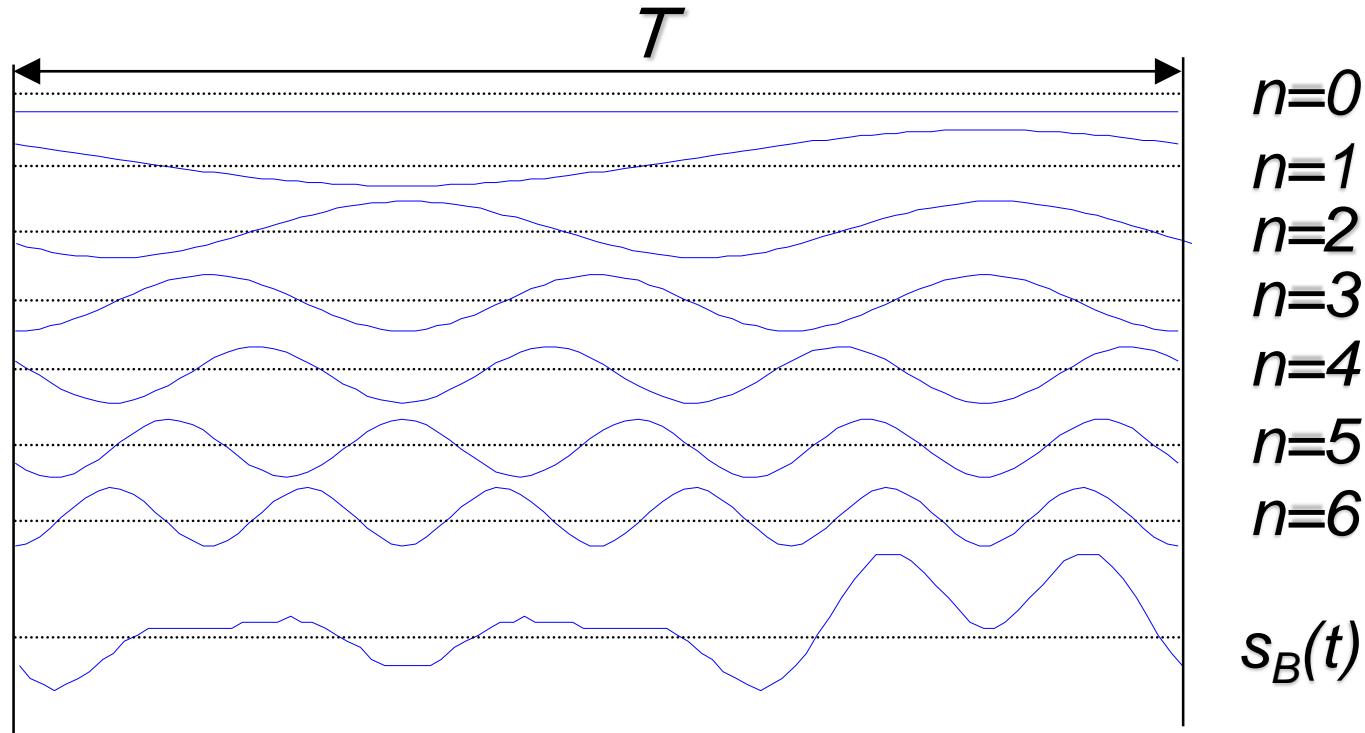
$$= \sqrt{a_n^2 + b_n^2} \cos(2\pi n f_0 t + \phi_n), \quad \phi_n = \tan^{-1} \frac{b_n}{a_n}$$

- ◆ Amplitude and Phase will be digitally modulated



Base-band OFDM signal

$$s_B(t) = \sum_{n=0}^{N-1} \{a_n \cos(2\pi n f_0 t) - b_n \sin(2\pi n f_0 t)\}$$



How a_n, b_n are calculated from $s_B(t)$

- Demodulation Procedure -

$$\int_0^T s_B(t) \cdot \cos(2\pi k f_0 t) dt$$

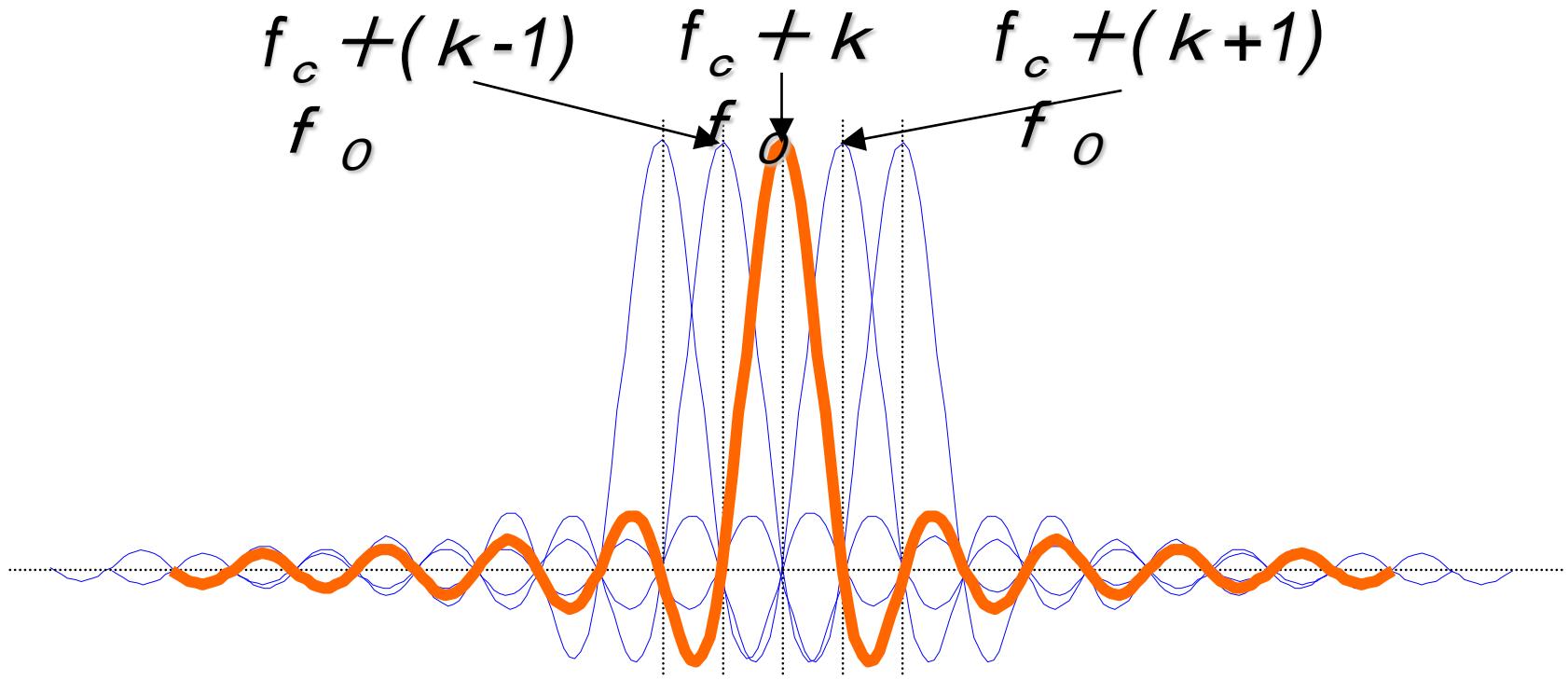
$$= \sum_{n=0}^{N-1} \left\{ a_n \int_0^T \cos(2\pi n f_0 t) \cos(2\pi k f_0 t) dt - b_n \int_0^T \sin(2\pi n f_0 t) \cos(2\pi k f_0 t) dt \right\}$$

$$= \frac{T}{2} a_k$$

$$\int_0^T s_B(t) \{-\sin(2\pi k f_0 t)\} dt = \frac{T}{2} b_k$$

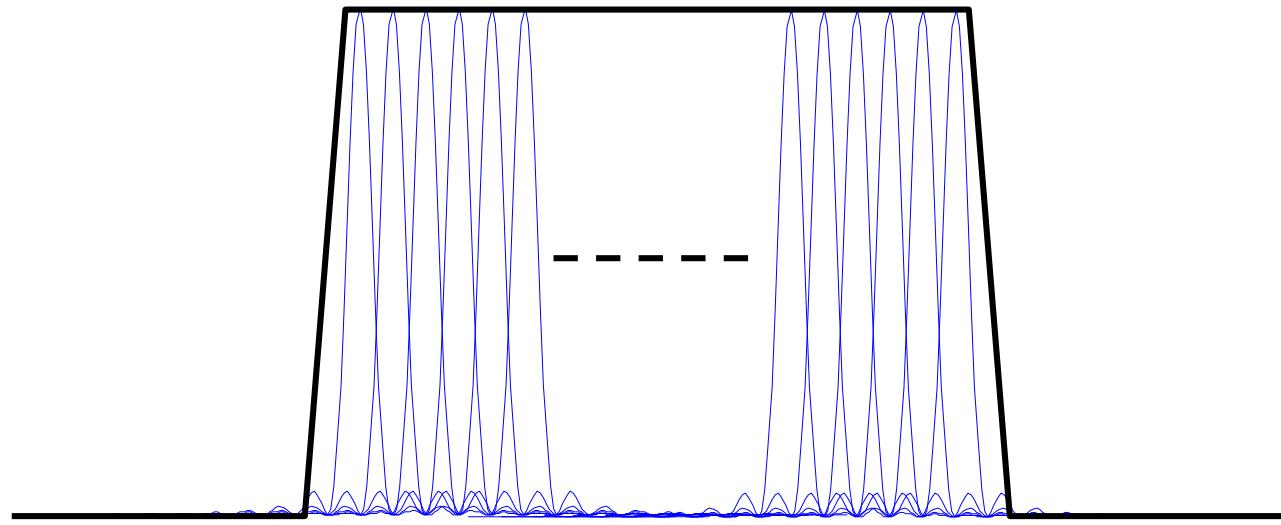
- ◆ According to the sinusoidal orthogonality, a_n, b_n can be extracted.
- ◆ In actual implementation, DFT(FFT) is used
- ◆ N is roughly 64 for WLAN, thousand for Terrestrial Video Broadcasting

Actual OFDM spectrum



OFDM power spectrum

- ◆ Total Power spectrum is almost square shape



OFDM signal generation

$$s(t) = \sum_{n=0}^{N-1} [a_n \cos\{2\pi(f_c + nf_0)t\} - b_n \sin\{2\pi(f_c + nf_0)t\}]$$

- ◆ Direct method needs
 - N digital modulators
 - N carrier frequency generator
 - ➔ Not practical
- ◆ In 1971, method using DFT is proposed to OFDM signal generation

OFDM signal generation in digital domain

- ◆ Define complex base-band signal $u(t)$ as follows

$$s_B(t) = \operatorname{Re}[u(t)]$$

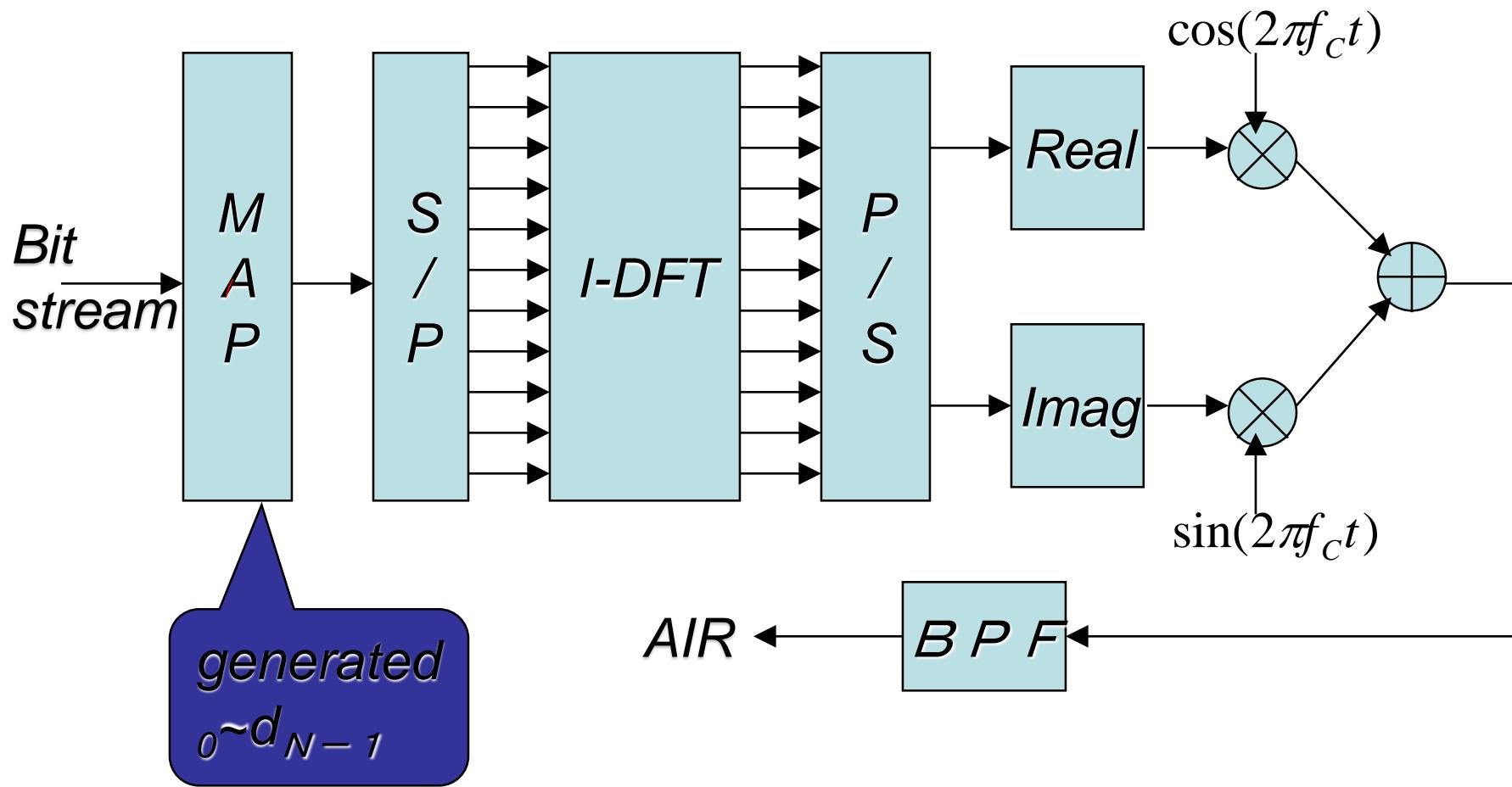
$$u(t) = \sum_{n=0}^{N-1} d_n \cdot e^{j2\pi n f_0 t}, \quad d_n = a_n + j b_n$$

- ◆ Perform N times sampling in period T

$$\begin{aligned} u\left(\frac{k}{Nf_0}\right) &= \sum_{n=0}^{N-1} d_n \cdot e^{j2\pi n f_0 \frac{k}{Nf_0}} = \sum_{n=0}^{N-1} d_n \cdot e^{j\frac{2\pi nk}{N}} \\ &= \sum_{n=0}^{N-1} d_n \cdot \left(e^{j\frac{2\pi}{N}}\right)^{nk} \quad (k = 0, 1, 2, \dots, N-1) \end{aligned}$$

$$u(k) = IFFT(d_n) = IFFT(a_n + jb_n)$$

OFDM modulator



OFDM demodulation

$$s(t) = \sum_{n=0}^{N-1} [a_n \cos\{2\pi(f_c + nf_0)t\} - b_n \sin\{2\pi(f_c + nf_0)t\}]$$

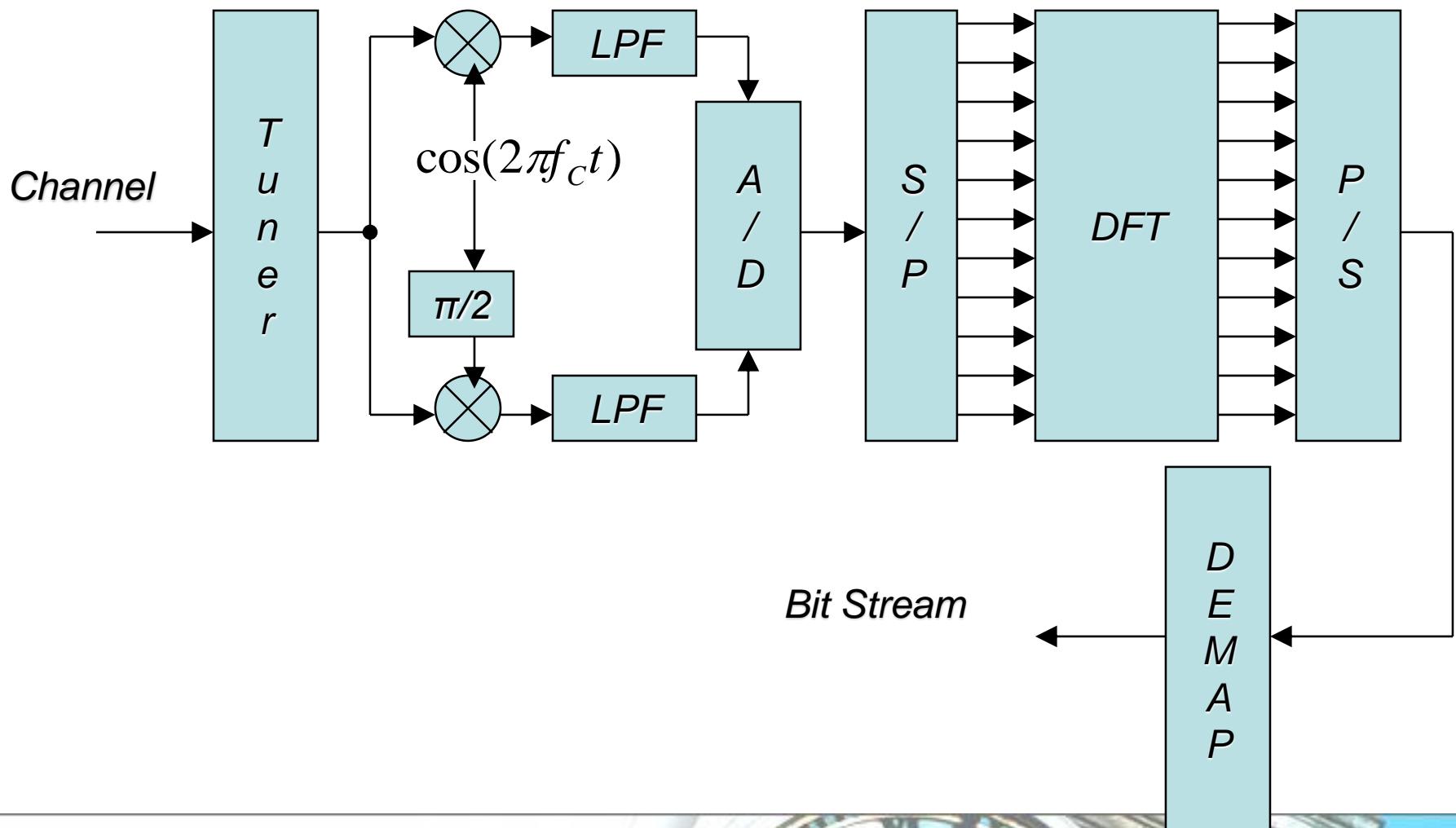
$$LPF[s(t) \cdot \cos(2\pi f_C t)] = \frac{1}{2} \sum_{n=0}^{N-1} \{a_n \cos(2\pi n f_0 t) - b_n \sin(2\pi n f_0 t)\} = \frac{1}{2} s_I(t)$$

$$LPF[s(t) \cdot \{-\sin(2\pi f_C t)\}] = \frac{1}{2} \sum_{n=0}^{N-1} \{a_n \sin(2\pi n f_0 t) + b_n \cos(2\pi n f_0 t)\} = \frac{1}{2} s_Q(t)$$

$$u(t) = s_I(t) + j s_Q(t) = \sum_{n=0}^{N-1} d_n \cdot e^{j2\pi n f_0 t}$$

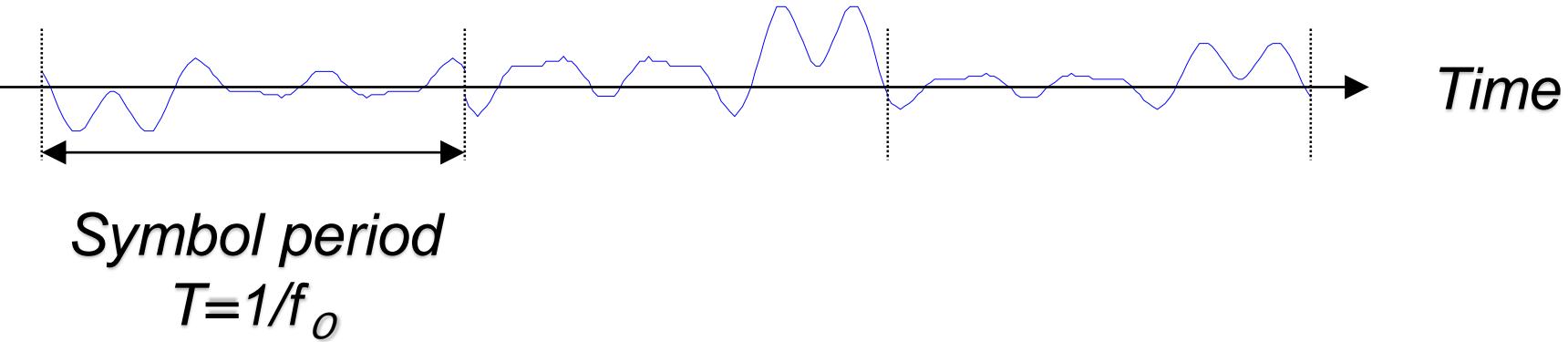
$$d_n = FFT(u(k))$$

OFDM demodulator



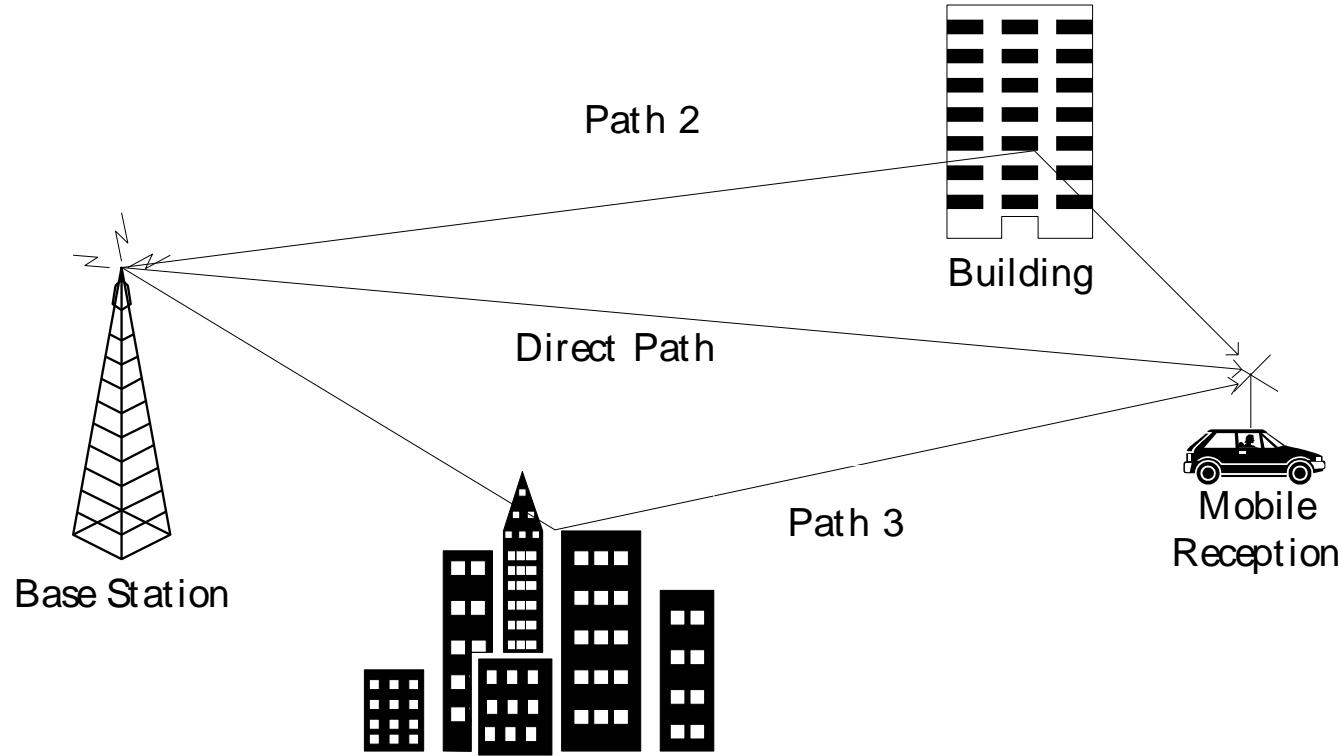
Summary of OFDM signal

- ◆ Each symbol carries information
- ◆ Each symbol wave is sum of many sinusoidal
- ◆ Each sinusoidal wave can be PSK, QAM modulated
- ◆ Using IDFT and DFT, OFDM implementation became practical



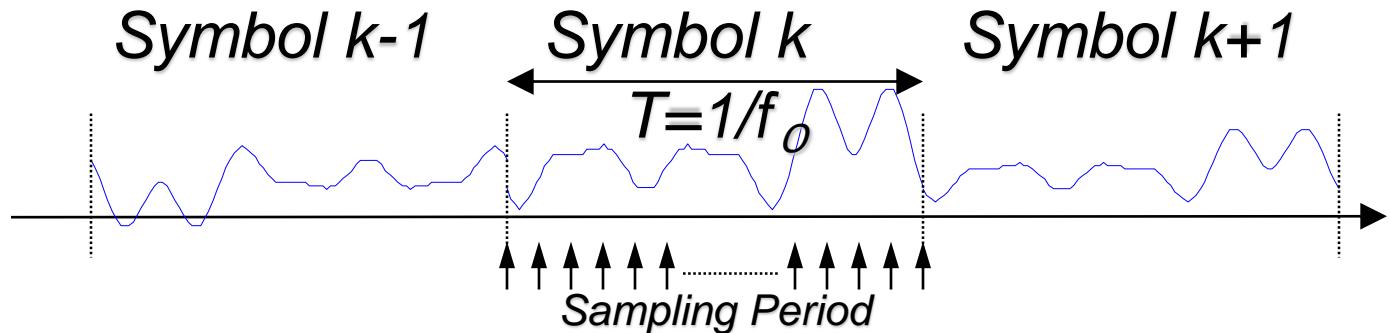
Multi-path

Delayed wave causes interference

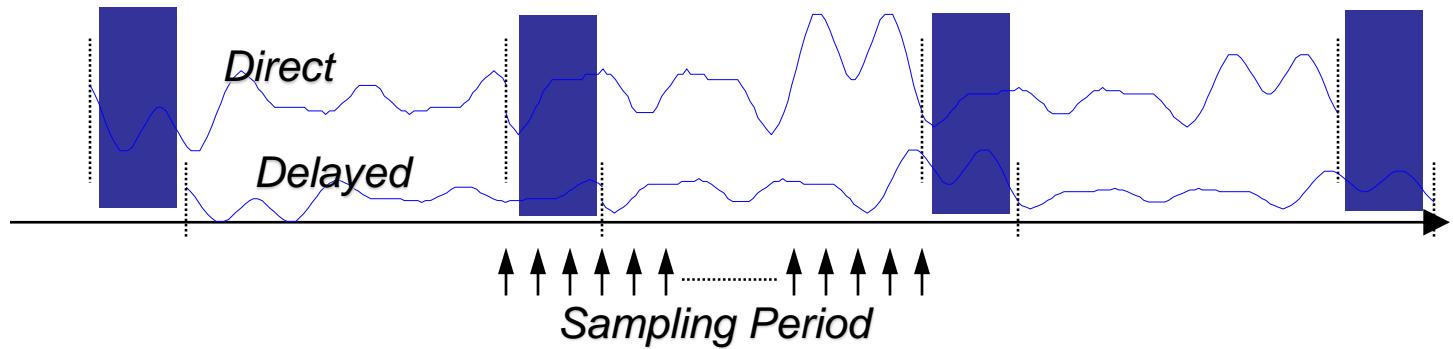


Multi-path effect

No multi-path

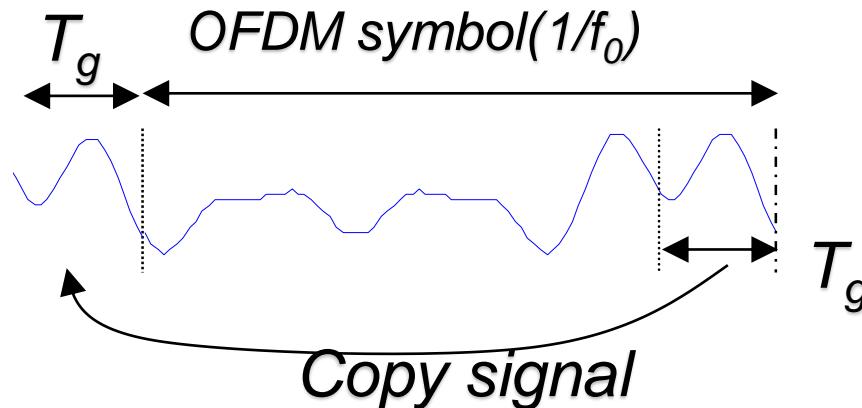


Multi-path

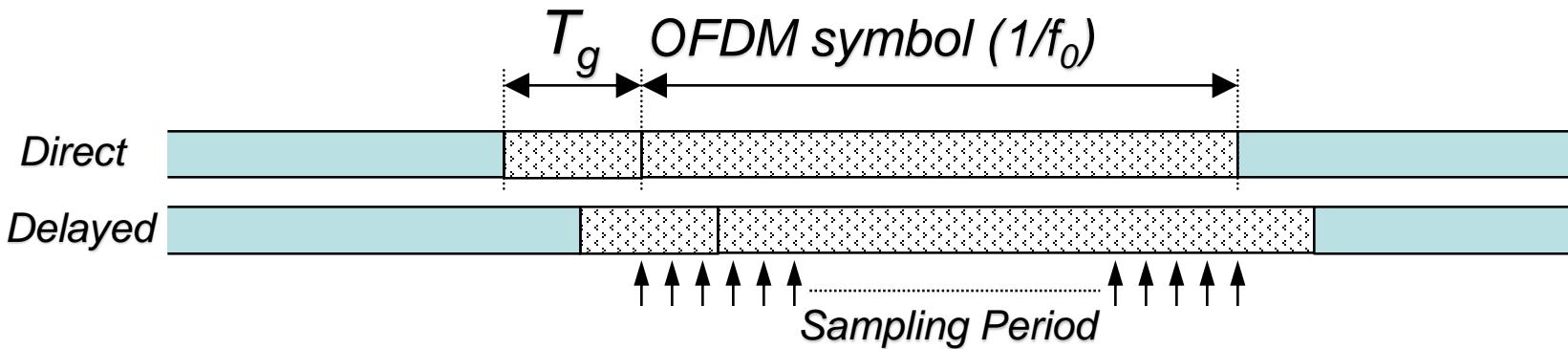


- ◆ Inter symbol interference (ISI) happens in Multi-path condition

Cyclic Prefix (Guard Interval) T_g

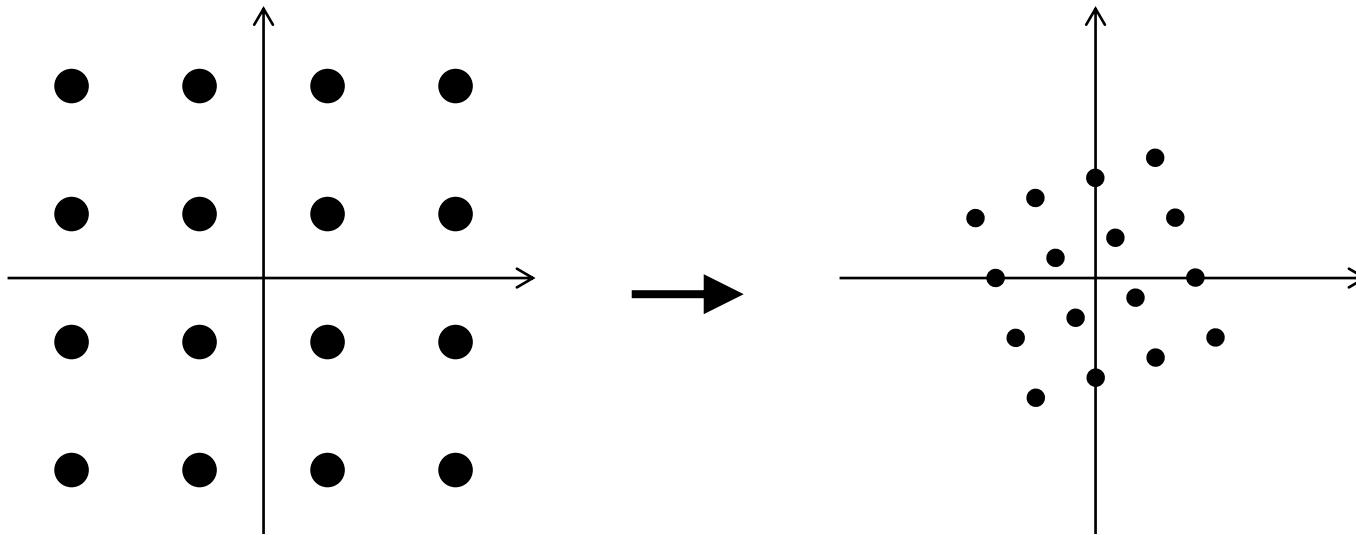


- ◆ By adding the Gurard Interval Period, ISI can be avoided



Multi-path

- ◆ By adding Cyclic Prefix, orthogonality can be maintained
- ◆ However, multi-path causes Amplitude and Phase distortion for each sub-carrier
- ◆ The distortion has to be compensated by Equalizer



Summary for OFDM

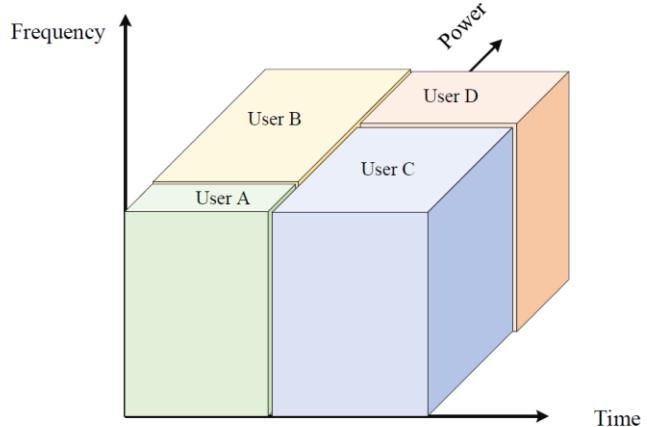
- ◆ Feature of OFDM
 - 1. High Frequency utilization by the square spectrum shape
 - 2. Multi-path problem is solved by Cyclic Prefix
 - 3. Multiple services in one OFDM by sharing sub-carriers
 - 4. Implementation was complicated but NOW possible because of LSI technology progress

Is OFDM robust?

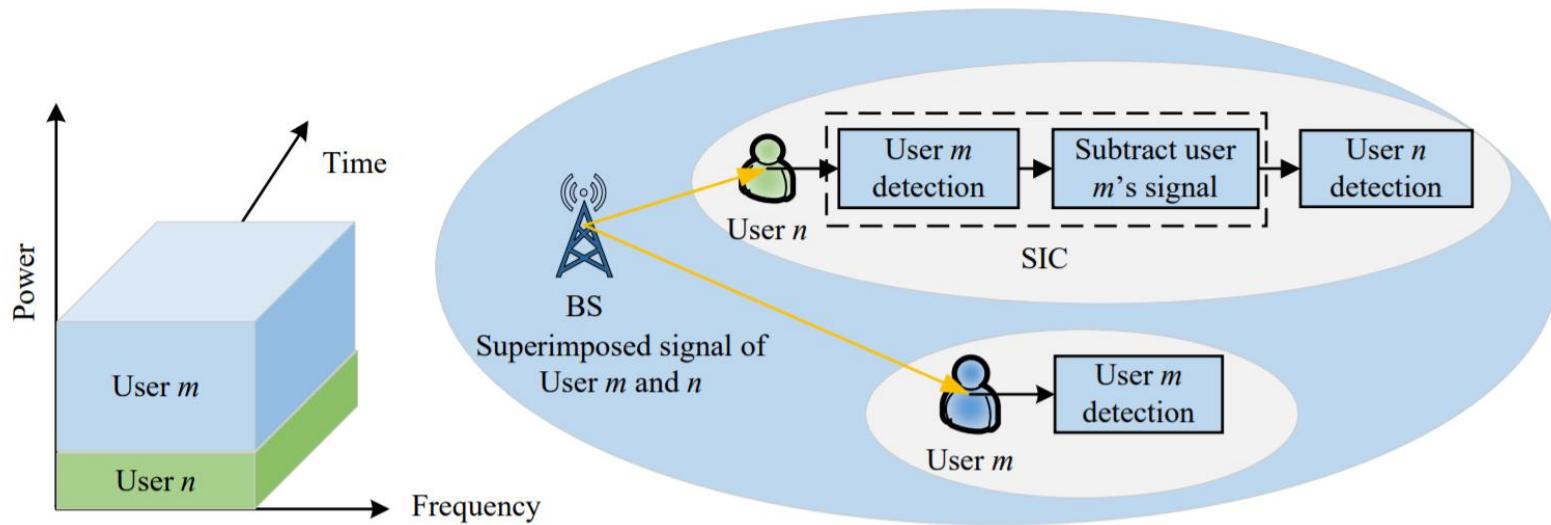
- ◆ The advantage of separating the transmission into multiple narrowband subchannels cannot itself translate into robustness against time variant channels if no channel coding is employed.
- ◆ The LTE downlink combines OFDM with channel coding and Hybrid Automatic Repeat reQuest (HARQ) to overcome the deep fading which may be encountered on the individual subchannels.

What's next - Non-orthogonal multiple access for 5G

- ◆ **Question:** What is multiple access?
- ◆ **Orthogonal multiple access (OMA):**
 - e.g., FDMA, TDMA, CDMA, OFDMA.
- ◆ **New requirements in 5G**
 - High spectrum efficiency.
 - Massive connectivity.
- ◆ **Non-orthogonal multiple access (NOMA)**
 - Power Domain.
 - to break orthogonality.
- ◆ Standard and industry developments on NOMA
 - **Whitepapers for 5G:** DOCOMO, METIS, NGMN, ZTE, SK Telecom, etc.
 - **LTE Release 13:** a two-user downlink special case of NOMA.
 - **Next generation digital TV standard ATSC 3.0:** a variation of NOMA, termed Layer Division Multiplexing (LDM).



Non-orthogonal multiple access for 5G



- ◆ Realize the multiple access in the same resource block (time/frequency/code), but with **different power levels** [R1].
- ◆ Apply successive interference cancellation (SIC) at the receiver [R1].

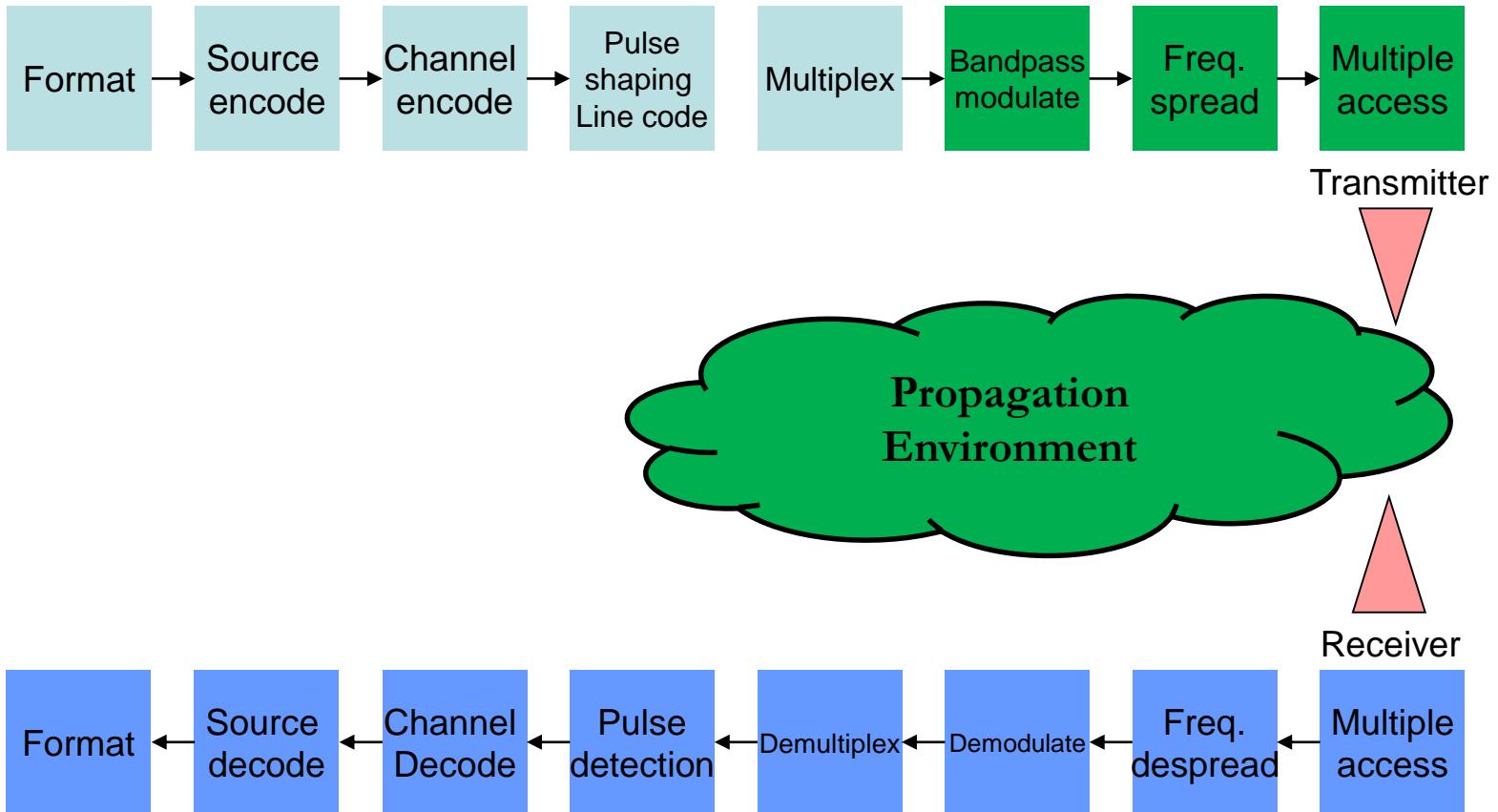
[R1] Y. Liu et al., “Non-Orthogonal Multiple Access for 5G and Beyond”, Proceedings of the IEEE; vol. 105, no. 12, pp. 2347-2381, Dec. 2017.

Radio Propagations & Network Architecture



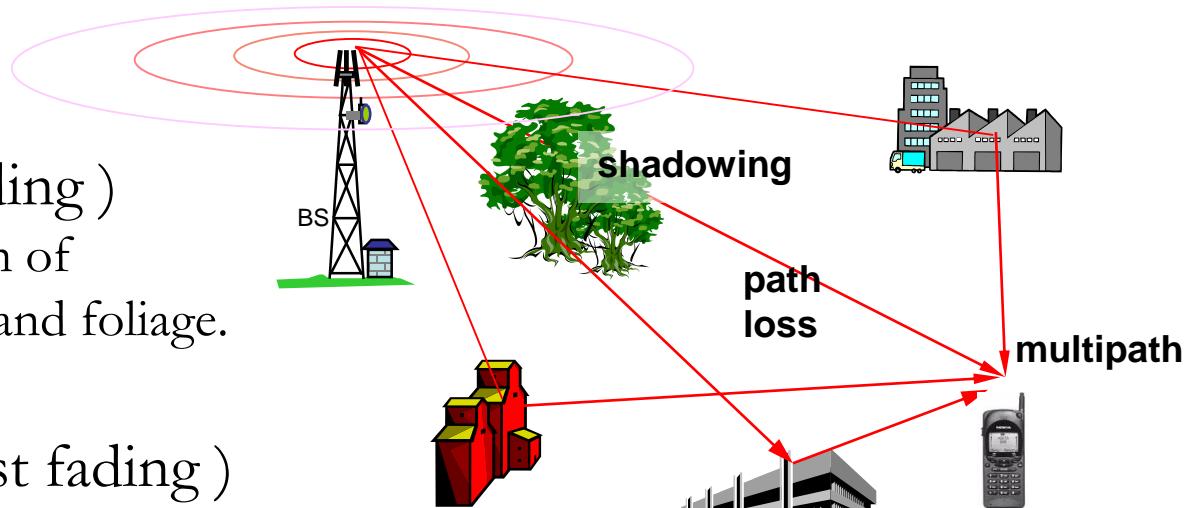
Overview of Wireless Communication System

Text
Voice
Video



Radio transmission impairments

- ◆ Path loss
 - received power decreases with distance.
- ◆ Shadowing (slow fading)
 - caused by obstruction of buildings, hills, trees and foliage.
- ◆ Multipath fading (fast fading)
 - caused by multipath reflection of a transmitted wave by objects



Antenna Gain

- ◆ Antenna gain
 - Power output, in a particular direction, compared to that produced in any direction by a perfect omnidirectional antenna (isotropic antenna)
- ◆ Effective area
 - Related to physical size and shape of antenna
- ◆ Relationship between antenna gain and effective area

$$G = \frac{4\pi A_e}{\lambda^2} = \frac{4\pi f^2 A_e}{c^2}$$

- G = antenna gain
- A_e = effective area
- f = carrier frequency
- c = speed of light ($\approx 3 \times 10^8$ m/s)
- λ = carrier wavelength

Line-of-Sight (LOS) Wireless Transmission Impairments

- ◆ Attenuation and distortion
- ◆ Free space loss
- ◆ Noise
- ◆ Atmospheric absorption
- ◆ Multipath
- ◆ Refraction
- ◆ Thermal noise

Attenuation

- ◆ Strength of signal falls off with distance over transmission medium
- ◆ Attenuation factors for unguided media:
 - Received signal must have sufficient strength so that circuitry in the receiver can interpret the signal
 - Signal must maintain a level sufficiently higher than noise to be received without error
 - Attenuation is greater at higher frequencies, causing distortion

Free Space Loss

- ◆ Free space loss, ideal isotropic antenna

$$\frac{P_t}{P_r} = \frac{(4\pi d)^2}{\lambda^2} = \frac{(4\pi f d)^2}{c^2}$$

- P_t = signal power at transmitting antenna
 - P_r = signal power at receiving antenna
 - λ = carrier wavelength
 - d = propagation distance between antennas
 - c = speed of light ($\approx 3 \times 10^8$ m/s)
- where d and λ are in the same units (e.g., meters)

Categories of Noise

- ◆ Thermal Noise
- ◆ Intermodulation noise
- ◆ Crosstalk
- ◆ Impulse Noise

Thermal Noise

- ◆ Amount of thermal noise to be found in a bandwidth of 1Hz in any device or conductor is:

$$N_0 = kT \text{ (W/Hz)}$$

- N_0 = noise power density in watts per 1 Hz of bandwidth
- k = Boltzmann's constant = 1.3803×10^{-23} J/K
- T = temperature, in kelvins (absolute temperature)

Thermal Noise

- ◆ Noise is assumed to be independent of frequency
- ◆ Thermal noise present in a bandwidth of B Hertz (in watts):
or, in decibel-watts

$$N = kTB$$

$$\begin{aligned} N &= 10 \log k + 10 \log T + 10 \log B \\ &= -228.6 \text{ dBW} + 10 \log T + 10 \log B \end{aligned}$$

Noise Terminology

- ◆ Intermodulation noise – occurs if signals with different frequencies share the same medium
 - Interference caused by a signal produced at a frequency that is the sum or difference of original frequencies
- ◆ Crosstalk – unwanted coupling between signal paths
- ◆ Impulse noise – irregular pulses or noise spikes
 - Short duration and of relatively high amplitude
 - Caused by external electromagnetic disturbances, or faults and flaws in the communications system

Expression E_b/N_0

- ◆ Ratio of signal energy per bit to noise power density per Hertz

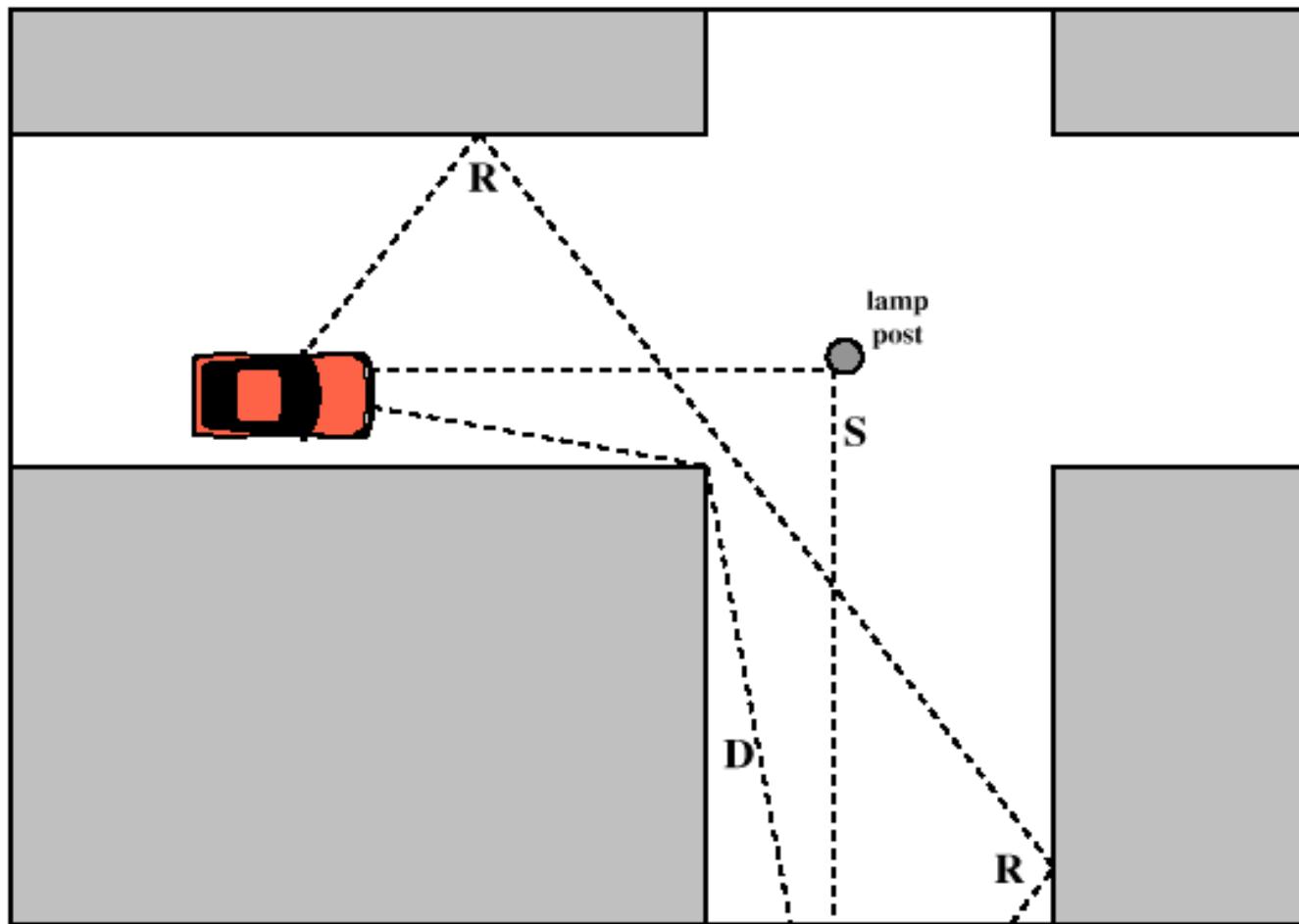
$$\frac{E_b}{N_0} = \frac{S / R}{N_0} = \frac{S}{kTR}$$

- ◆ The bit error rate for digital data is a function of E_b/N_0
 - Given a value for E_b/N_0 to achieve a desired error rate, parameters of this formula can be selected
 - As bit rate R increases, transmitted signal power must increase to maintain required E_b/N_0

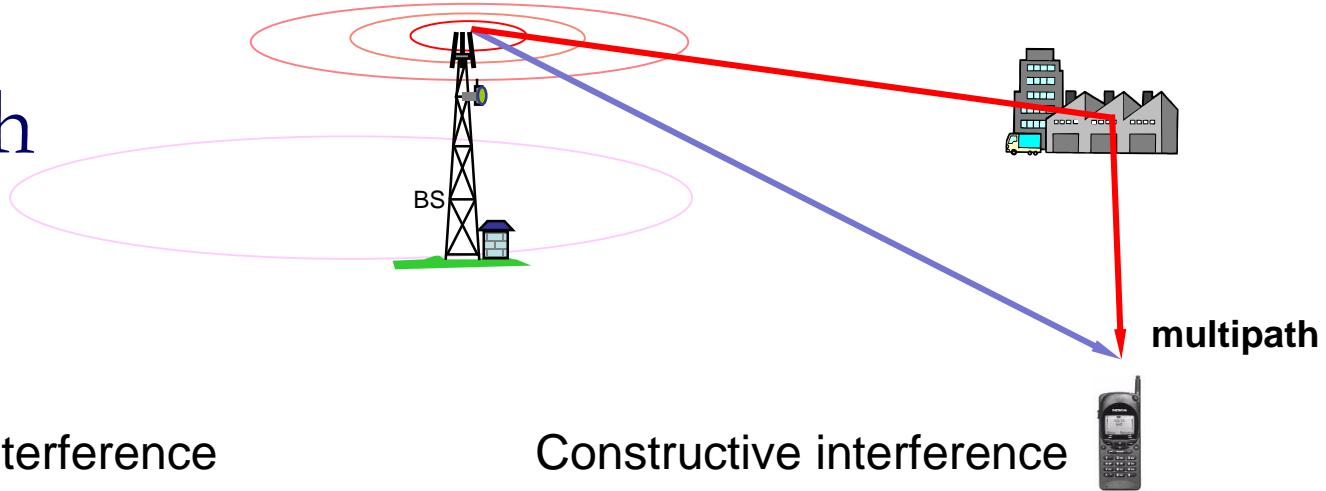
Other Impairments

- ◆ **Atmospheric absorption** – water vapor and oxygen contribute to attenuation
- ◆ **Multipath** – obstacles reflect signals so that multiple copies with varying delays are received
- ◆ **Refraction** – bending of radio waves as they propagate through the atmosphere

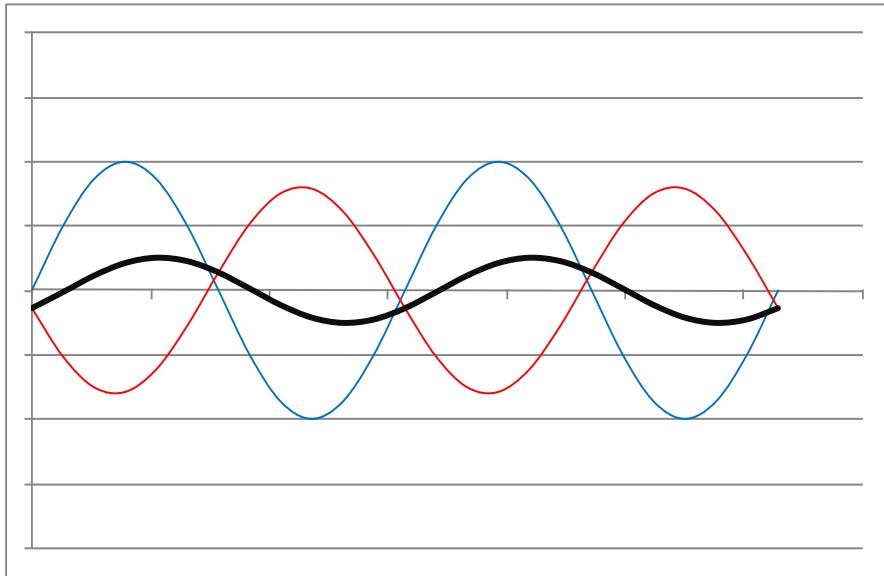
Multipath Propagation



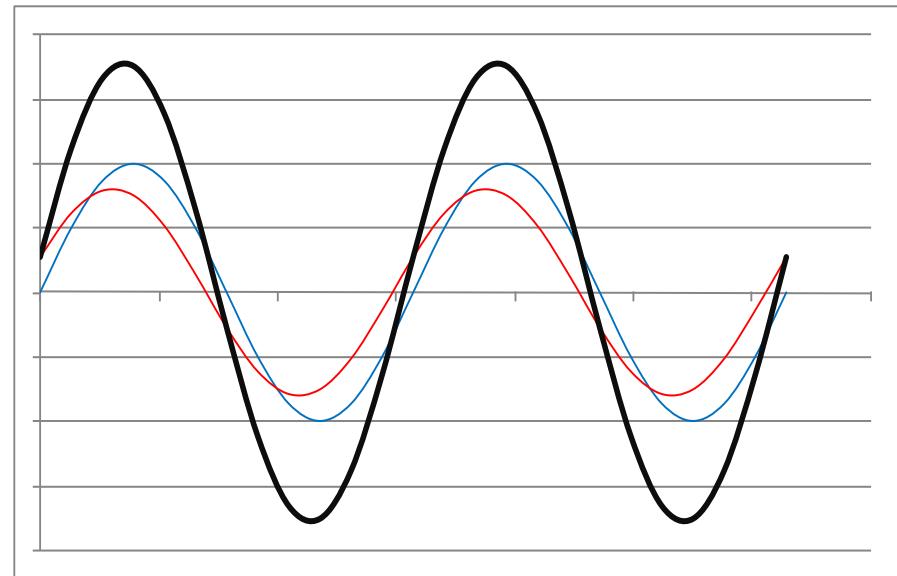
Multi-path



Destructive interference



Constructive interference



As mobile moves the relative phase changes and fading occurs

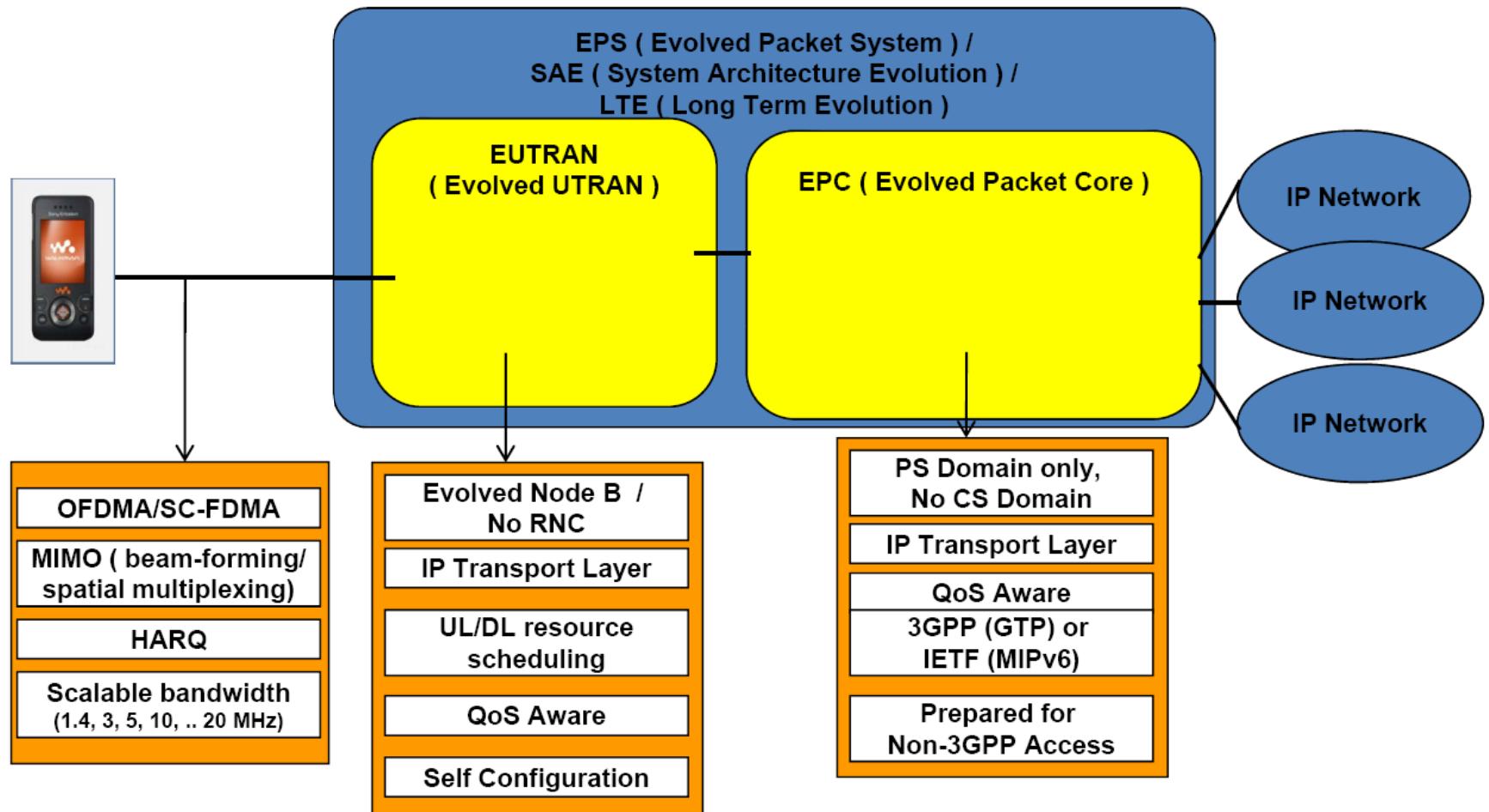
Types of Fading

- ◆ Fast fading, Slow fading, Flat fading, Selective fading
- ◆ Rayleigh fading, Nakagami-m, and Rician fading

Radio Propagations & Network Architecture

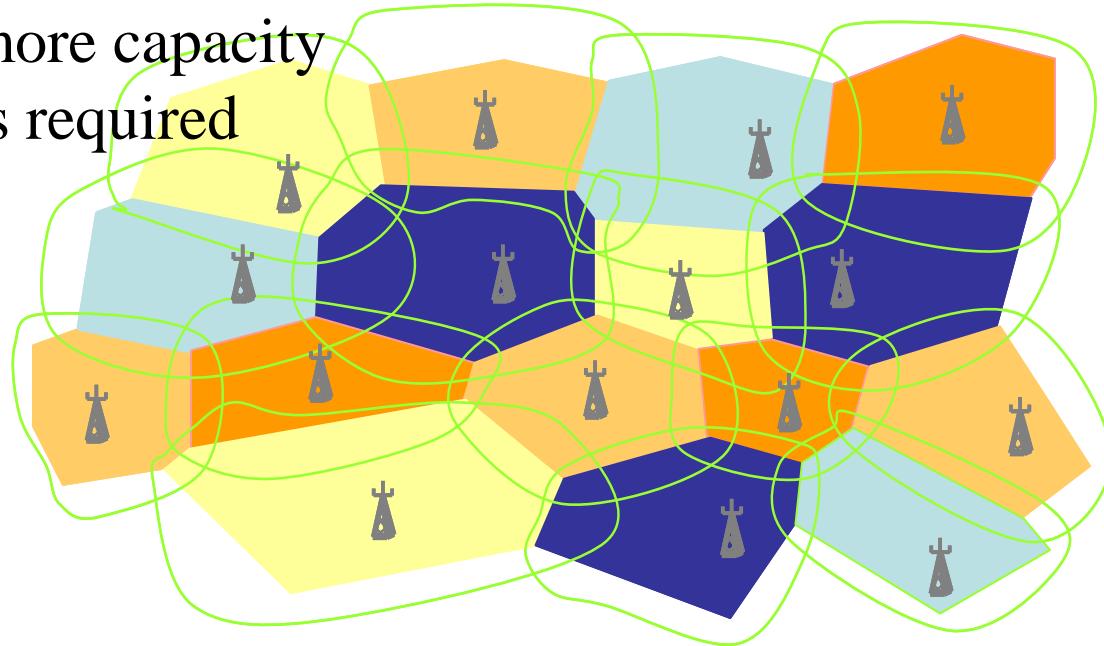


LTE/SAE Key Features – Overview



Cellular concept

- ◆ Late 40s: AT&T developed cellular concept for frequency re-use
- ◆ Break the service area into cells
- ◆ Shrink the cell size; adopt intensive frequency re-use
- ◆ Add more cells to add more capacity
- ◆ Mobility management is required

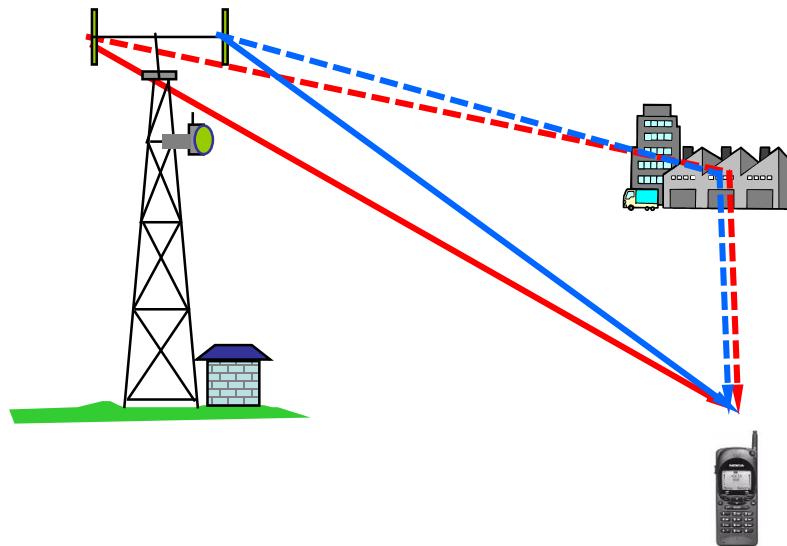


Radio access

- ◆ This base station has 3 sectors each equipped with independent TRXs (transmitter/receivers)
- ◆ It has spaced pairs of antennas in each sector to provide diversity reception
- ◆ Microwave link antenna to the network
- ◆ LNAs on the antennas (LNA=low noise amplifiers)



Diversity



Different phase relations will exist between the multipath rays from each antenna – so the interference will be different.

Diversity: used in 2G, 3G, WLAN and 4G

- ◆ Obtain two or more copies of the received signal
- ◆ Copies can be separated by:
 - **Time:** Convolutional coding ‘smears’ short errors
 - **Frequency:** Frequency hopping is used for GSM;
 - **Distance:** Spatial diversity (2G/3G/WLAN)
 - **Polarization:** Polarization diversity $\pm 45^\circ$ (2G/3G)

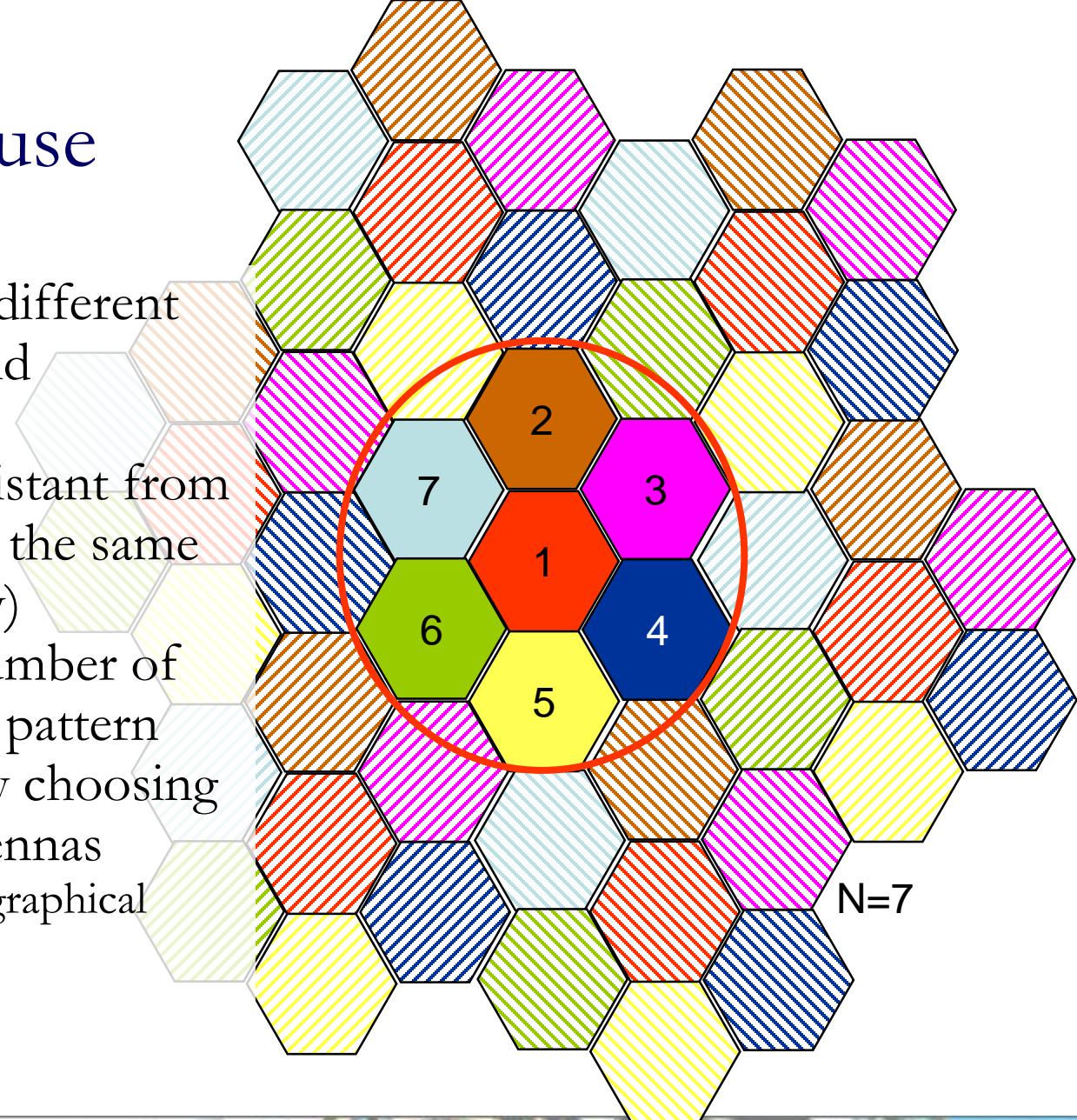


Diversity: Combining the signals

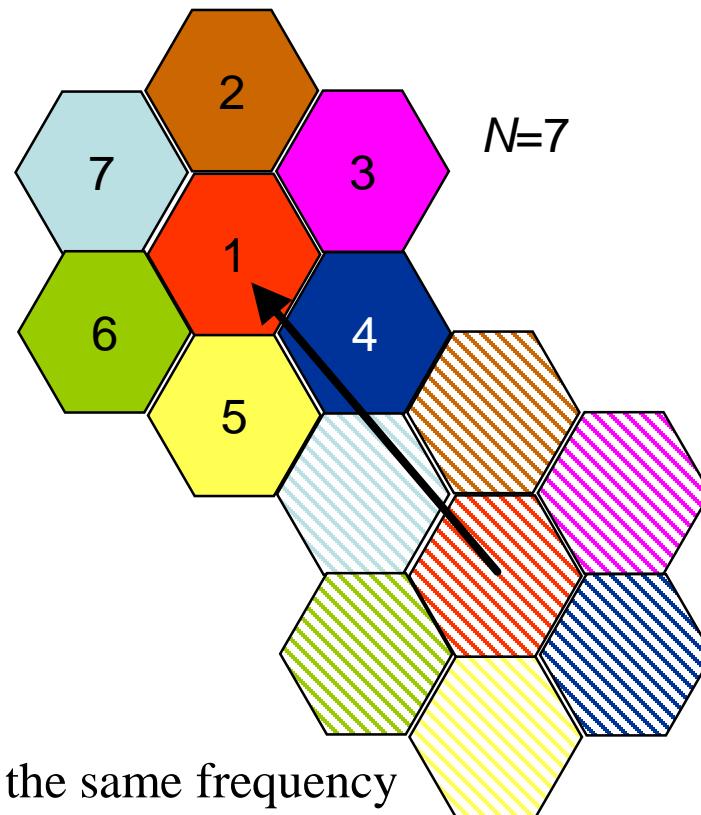
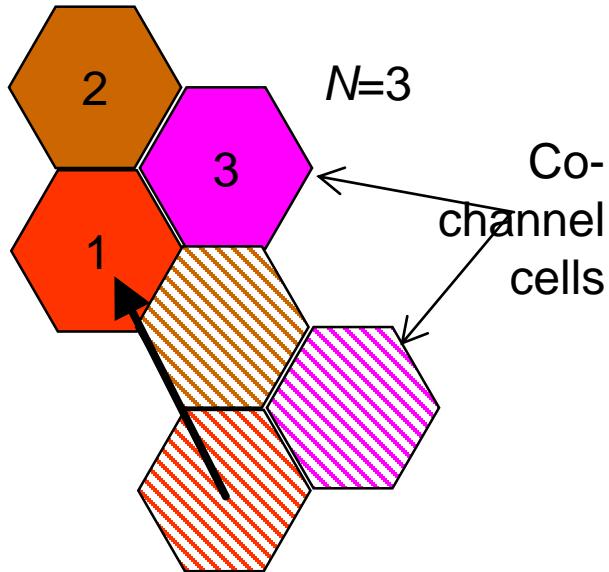
- ◆ Combine the signal from each branch and obtain a signal that is more reliable than any single branch
 - Switch diversity – when one is too low, try another
 - Selection diversity – choose the largest signal
 - Equal gain – signals equally weighted and added in phase
 - Maximal ratio – weight the power in the branches in proportion to their signal amplitude and add in phase
- ◆ Diversity gain = effective increase in signal power for some stated reliability. Typically **4–6dB** depending on the environment.

Frequency Reuse

- ◆ Adjacent cells use different frequencies to avoid interference
- ◆ Cells sufficiently distant from each other can use the same channel (frequency)
- ◆ Reuse factor N : number of cells in a repeating pattern
- ◆ Control cell size by choosing BS power and antennas
 - Make use of topographical screening



Effect of cluster size

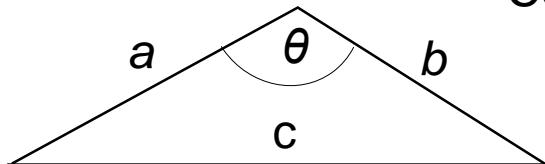
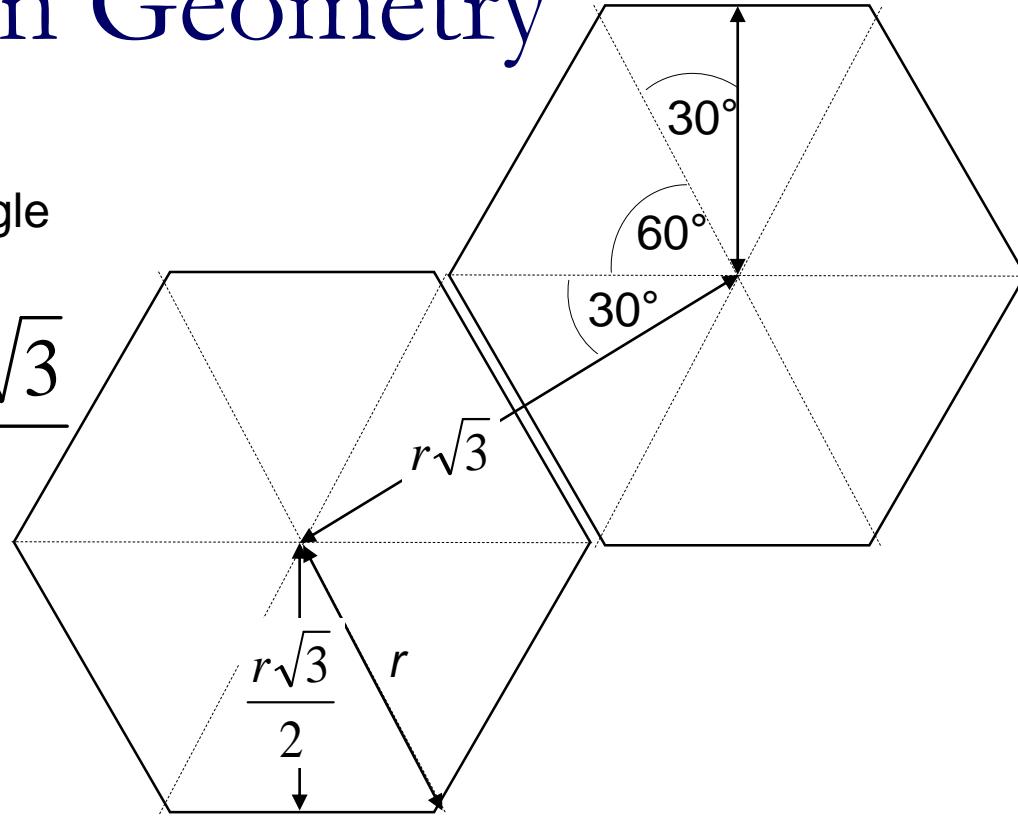


- ◆ Bigger cluster:
 - less interference from next cell using the same frequency
 - lower capacity – bandwidth available in cell is F_A/N
(F_A is frequency spectrum allocated)

Reminders on Geometry

Surface area of a hexagon
=6*area of equilateral triangle

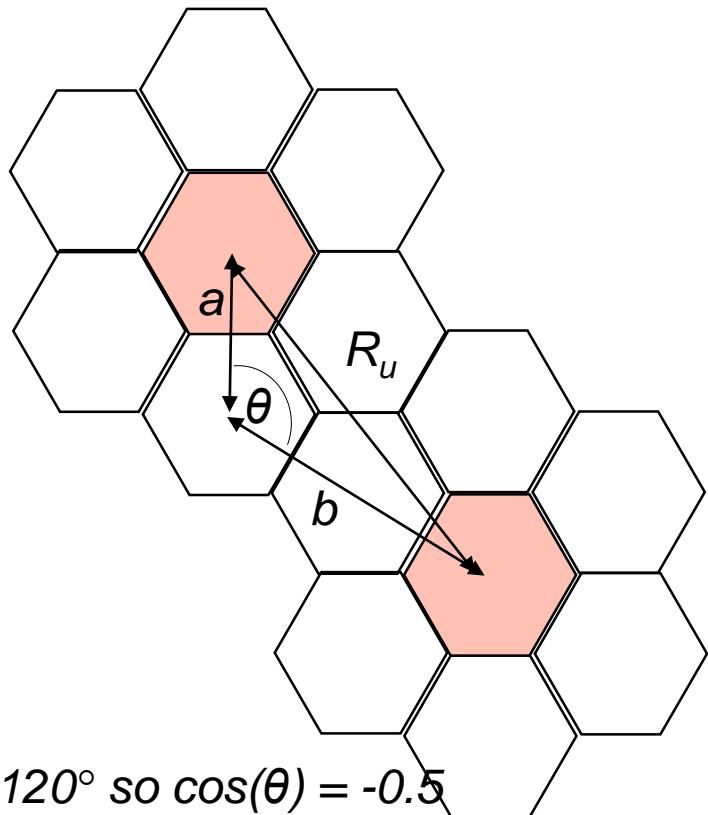
$$s = 6 \times r^2 \frac{\sqrt{3}}{4} = \frac{r^2 3\sqrt{3}}{2}$$



Cosine rule:

$$c^2 = a^2 + b^2 - 2ab\cos(\theta)$$

Derivation example ($N=7$ in pictures)



In general

a is distance between i cells

$$a = ir\sqrt{3}$$

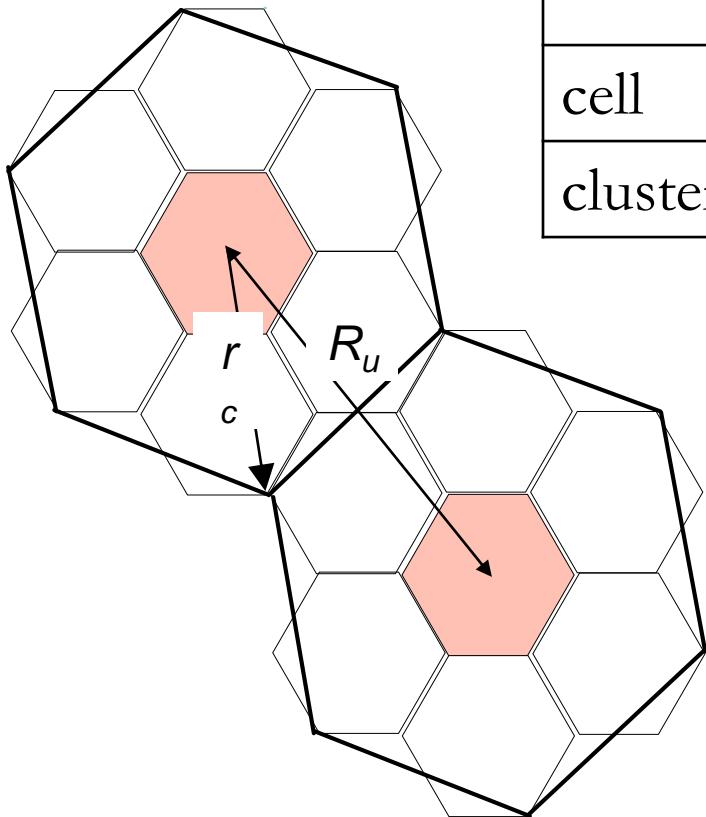
b is distance between j cells

$$b = jr\sqrt{3}$$

$$R_u^2 = i^2 r^2 3 + j^2 r^2 3 + 2 \times 0.5 i j r^2 3$$

$$R_u = \left(\sqrt{i^2 + j^2 + ij} \right) r\sqrt{3}$$

Cluster radius



	radius	area
cell	r	s
cluster	r_c	s_c

$$s_c = Ns$$

$$\frac{r_c^2 3\sqrt{3}}{2} = N \frac{r^2 3\sqrt{3}}{2}$$

$$r_c = r\sqrt{N}$$

$$R_u = r_c \sqrt{3}$$

$$R_u = r\sqrt{3N}$$

Thick lines define a cluster hexagon
of same area as N cells

Possible values of N

$$R_u = \left(\sqrt{i^2 + j^2 + ij} \right) (r\sqrt{3}) \text{ and } R_u = r\sqrt{3N}$$

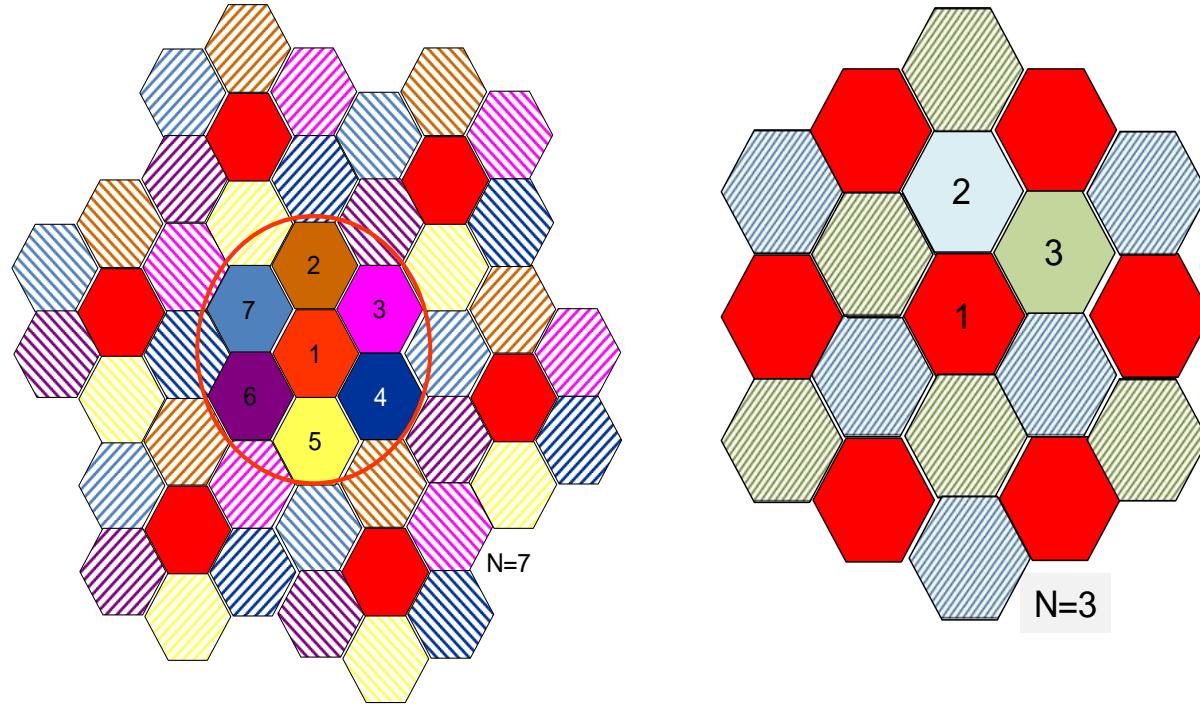
$$\left(\sqrt{i^2 + j^2 + ij} \right) (r\sqrt{3}) = r\sqrt{3N} \text{ or } \sqrt{i^2 + j^2 + ij} = \sqrt{N}$$

$$i^2 + j^2 + ij = N$$

These means that only certain values of N are possible

i	j	N
1	1	3
1	2	7
2	2	12
1	3	13
2	3	19
1	4	21
3	3	27
2	4	28

Different cluster size

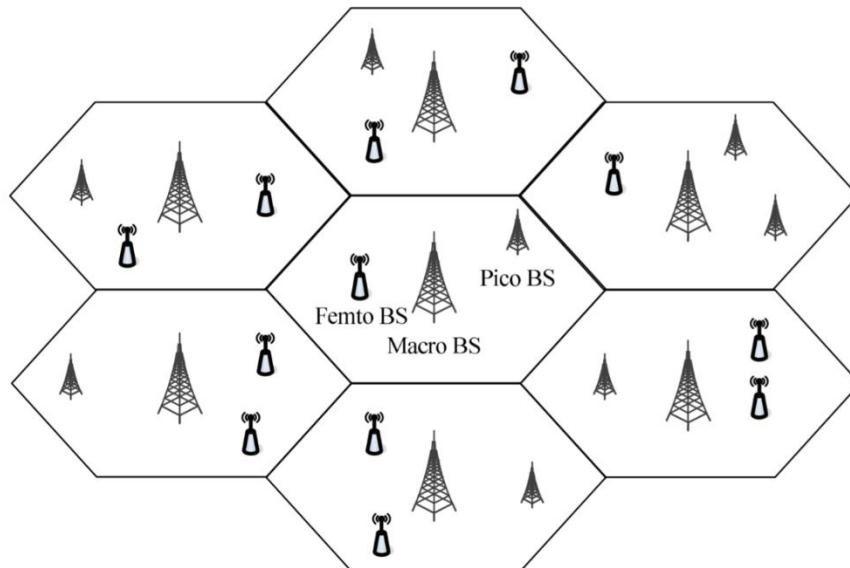


6 surrounding cells of same frequency for both cluster size

What is in practice?

◆ Conventional Networks

- 3-tier Heterogenous Networks topology for the grid model



What is in practice?

◆ Stochastic Geometry

- 3-tier Heterogenous Networks following the random spatial model

