



## Speedup Analysis

The speedup from 1 thread to 4 threads is:  $\text{Speedup} = 65.96 / 18.81 = 3.51$

This shows that using 4 threads makes the simulation approximately 3.51 times faster than using a single thread. This is closeish to the max speedup of 4, meaning that the parallelization was efficient.

## Parallel Fraction (Fp) Calculation

Using the formula:  $F_p = (4/3) * (1 - (1/S))$

$$F_p = (4/3)(1 - (1/3.51)) \quad F_p = (4/3)(1 - 0.284) \quad F_p = (4/3)(0.716) \quad F_p = 0.953$$

The parallel fraction of 0.953 (95.3%) indicates that a lot of our code can be parallelized.

## Maximum Theoretical Speedup

Using Amdahl's Law, the maximum theoretical speedup regardless of the number of cores is:  $S_{\text{max}} = 1/(1-F_p)$   
 $= 1/(1-0.953) = 1/0.047 = 21.28$

The maximum speedup we could achieve is approximately 21.28 times 1 thread performance.

## Why It Works This Way

The Monte Carlo simulation is easily parallelized because:

1. **Each trial can be executed independently**
2. **The workload can be evenly divided**
3. **Minimal thread synchronization**

The high  $F_p$  (95.3%) shows that this application has few sequential portions, making it an ideal candidate for parallel processing. The small difference from ideal speedup (3.51 vs 4) is due to thread creation overhead and other synchronization costs.