Problem A-i

Use this notebook to write your code for perceptron by filling in the sections marked # TODO and running all cells.

```
In [5]: import numpy as np
   import matplotlib.pyplot as plt
   import itertools

from perceptron_helper import (
       predict,
       plot_data,
       boundary,
       plot_perceptron,
)

%matplotlib inline
```

Implementation of Perceptron

First, we will implement the perceptron algorithm. Fill in the update_perceptron() function so that it finds a single misclassified point and updates the weights and bias accordingly. If no point exists, the weights and bias should not change.

Hint: You can use the predict() helper method, which labels a point 1 or -1
depending on the weights and bias.

```
In [6]: def update perceptron(X, Y, w, b):
            This method updates a perceptron model. Takes in the previous weights
            and returns weights after an update, which could be nothing.
            Inputs:
                X: A (N, D) shaped numpy array containing a single point.
                Y: A (N, ) shaped numpy array containing the labels for the points.
                w: A (D, ) shaped numpy array containing the weight vector.
                b: A float containing the bias term.
            Output:
                next_w: A (D, ) shaped numpy array containing the next weight vector
                        after updating on a single misclassified point, if one exists.
                next_b: The next float bias term after updating on a single
                        misclassified point, if one exists.
            .....
            next_w, next_b = np.copy(w), np.copy(b)
            for x_i, y_i in zip(X, Y):
                if predict(x_i, next_w, next_b) != y_i:
                    next_w += y_i * x_i
                    next_b += y_i
                    break # Only update on one misclassified point
```

```
return next_w, next_b
```

Next you will fill in the run_perceptron() method. The method performs single updates on a misclassified point until convergence, or max_iter updates are made. The function will return the final weights and bias. You should use the update_perceptron() method you implemented above.

```
In [17]: def run_perceptron(X, Y, w, b, max_iter):
             This method runs the perceptron learning algorithm. Takes in initial weights
             and runs max_iter update iterations. Returns final weights and bias.
             Inputs:
                 X: A (N, D) shaped numpy array containing a single point.
                 Y: A (D, ) shaped numpy array containing the labels for the points.
                 w: A (D, ) shaped numpy array containing the initial weight vector.
                 b: A float containing the initial bias term.
                 max_iter: An int for the maximum number of updates evaluated.
             Output:
                 w: A (D, ) shaped numpy array containing the final weight vector.
                 b: The final float bias term.
             for i in range(max_iter):
                 next_w, next_b = update_perceptron(X, Y, w, b)
                 if np.array_equal(next_w, w) and next_b == b:
                     break # No updates happened - converged
                 w, b = next_w, next_b
             return w, b
```

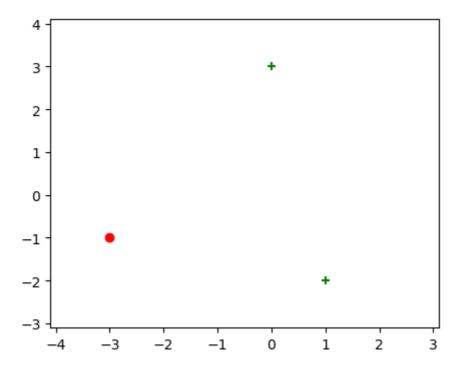
Problem A-ii

Visualizing a Toy Dataset

We will begin by training our perceptron on a toy dataset of 3 points. The green points are labelled +1 and the red points are labelled -1. We use the helper function plot_data() to do so.

```
In [27]: X = np.array([[ -3, -1], [0, 3], [1, -2]])
Y = np.array([ -1, 1, 1])

In [28]: fig = plt.figure(figsize=(5,4))
ax = fig.gca(); ax.set_xlim(-4.1, 3.1); ax.set_ylim(-3.1, 4.1)
plot_data(X, Y, ax)
```



Running the Perceptron

Next, we will run the perceptron learning algorithm on this dataset. Update the code to show the weights and bias at each timestep and the misclassified point used in each update. You may change the update_perceptron() method to do this, but be sure to update the starter code as well to reflect those changes.

Run the below code, and fill in the corresponding table in the set.

```
In [20]: # Initialize weights and bias.
weights = np.array([0.0, 1.0])
bias = 0.0

weights, bias = run_perceptron(X, Y, weights, bias, 16)

print()
print()
print ("final w = %s, final b = %.1f" % (weights, bias))
```

final w = [2. 0.], final b = 3.0

Visualizating the Perceptron

Getting all that information in table form isn't very informative. Let us visualize what the decision boundaries are at each timestep instead.

The helper functions boundary() and plot_perceptron() plot a decision boundary given a perceptron weights and bias. Note that the equation for the decision boundary is given by:

$$w_1x_1 + w_2x_2 + b = 0.$$

Using some algebra, we can obtain x_2 from x_1 to plot the boundary as a line.

$$x_2 = \frac{-w_1x_2 - b}{w_2}.$$

Below is a redefinition of the run_perceptron() method to visualize the points and decision boundaries at each timestep instead of printing. Fill in the method using your previous run_perceptron() method, and the above helper methods.

Hint: The axs element is a list of Axes, which are used as subplots for each timestep. You can do the following:

```
ax = axs[i]
```

to get the plot correponding to t=i. You can then use ax.set_title() to title each subplot. You will want to use the plot_data() and plot_perceptron() helper methods.

```
In [ ]: def run_perceptron(X, Y, w, b, axs, max_iter):
            This method runs the perceptron learning algorithm. Takes in initial weights
            and runs max iter update iterations. Returns final weights and bias.
            Inputs:
                X: A (N, D) shaped numpy array containing a single point.
                Y: A (N, ) shaped numpy array containing the labels for the points.
                w: A (D, ) shaped numpy array containing the initial weight vector.
                b: A float containing the initial bias term.
                axs: A list of Axes that contain suplots for each timestep.
                max_iter: An int for the maximum number of updates evaluated.
            Output:
                The final weight and bias vectors.
            for i in range(max_iter):
                ax = axs[i]
                plot_data(X, Y, ax)
                plot perceptron(w, b, ax)
                ax.set title(f"Timestep {i}")
                next w, next b = update perceptron(X, Y, w, b)
                if np.array_equal(next_w, w) and next_b == b:
                    break
                w, b = next_w, next_b
            return w, b
```

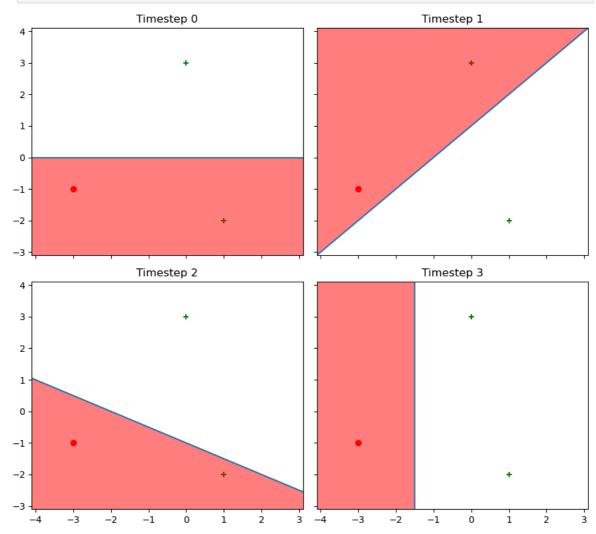
Run the below code to get a visualization of the perceptron algorithm. The red region are areas the perceptron thinks are negative examples.

```
In [30]: # Initialize weights and bias.
weights = np.array([0.0, 1.0])
bias = 0.0
```

```
f, ax_arr = plt.subplots(2, 2, sharex=True, sharey=True, figsize=(9,8))
axs = list(itertools.chain.from_iterable(ax_arr))
for ax in axs:
    ax.set_xlim(-4.1, 3.1); ax.set_ylim(-3.1, 4.1)

run_perceptron(X, Y, weights, bias, axs, 4)

f.tight_layout()
```



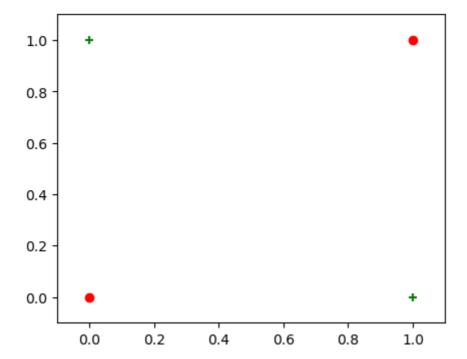
Problem A-iii

Visualize a Non-linearly Separable Dataset.

We will now work on a dataset that cannot be linearly separated, namely one that is generated by the XOR function.

```
In [31]: X = np.array([[0, 1], [1, 0], [0, 0], [1, 1]])
Y = np.array([1, 1, -1, -1])

In [32]: fig = plt.figure(figsize=(5,4))
ax = fig.gca(); ax.set_xlim(-0.1, 1.1); ax.set_ylim(-0.1, 1.1)
plot_data(X, Y, ax)
```



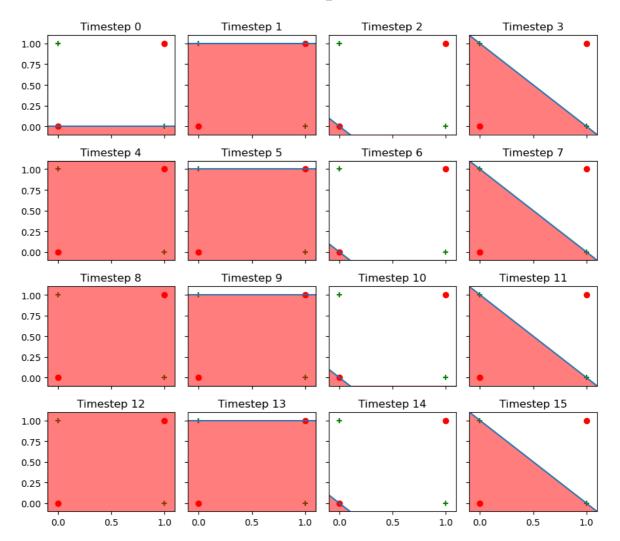
We will now run the perceptron algorithm on this dataset. We will limit the total timesteps this time, but you should see a pattern in the updates. Run the below code.

```
In [33]: # Initialize weights and bias.
weights = np.array([0.0, 1.0])
bias = 0.0

f, ax_arr = plt.subplots(4, 4, sharex=True, sharey=True, figsize=(9,8))
axs = list(itertools.chain.from_iterable(ax_arr))
for ax in axs:
    ax.set_xlim(-0.1, 1.1); ax.set_ylim(-0.1, 1.1)

run_perceptron(X, Y, weights, bias, axs, 16)

f.tight_layout()
```



Problem B

Implement MNIST Classification with MLP. Your train_mnist function should return the trained model.

Hint: use the torchvision library to load the MNIST dataset.

```
In [ ]:
        import torch.nn as nn
        from torchvision import datasets, transforms
        from torch.utils.data import DataLoader
        class MLP(nn.Module):
            def __init__(self):
                super().__init__()
                self.fc1 = nn.Linear(784, 500)
                 self.relu = nn.ReLU()
                 self.fc2 = nn.Linear(500, 10)
            def forward(self, x):
                x = x.view(-1, 784) # Flatten the image
                x = self.fc1(x)
                x = self.relu(x)
                 x = self.fc2(x)
                 return x
```

```
def train_mnist(device = 'cpu'):
   This method performs end to end training of a model for the MNIST
    classification task. Returns the final trained model, which should have
    one intermediate layer with 500 hidden units. Feel free to write helper
    functions/classes.
    model = MLP().to(device)
    transform = transforms.Compose([
        transforms.ToTensor(),
        transforms.Normalize((0.1307,), (0.3081,))
    1)
    train_data = datasets.MNIST(root='./data', train=True, download=True, transf
    test_data = datasets.MNIST(root='./data', train=False, download=True, transf
    train_loader = DataLoader(train_data, batch_size=64, shuffle=True)
    test_loader = DataLoader(test_data, batch_size=1000, shuffle=False)
    criterion = nn.CrossEntropyLoss()
    optimizer = optim.Adam(model.parameters(), lr=0.001)
    num_epochs = 5
    for epoch in range(num_epochs):
        model.train()
        for images, labels in train_loader:
            images, labels = images.to(device), labels.to(device)
            outputs = model(images)
            loss = criterion(outputs, labels)
            optimizer.zero grad()
            loss.backward()
            optimizer.step()
    return model
```

Let us test the output of model and evaluete its performance.

```
In [ ]: import torch
        import torch.nn as nn
        import torch.optim as optim
        from torchvision import datasets, transforms
        from torch.utils.data import DataLoader
        def evaluate(model, test_loader, device='cpu'):
            model.eval()
            correct = 0
            total = 0
            with torch.no_grad():
                for images, labels in test loader:
                    images, labels = images.to(device), labels.to(device)
                    outputs = model(images)
                    _, predicted = torch.max(outputs.data, 1)
                    total += labels.size(0)
                    correct += (predicted == labels).sum().item()
            accuracy = 100 * correct / total
            print(f'Test Accuracy: {accuracy:.2f}%')
            return accuracy
        device = torch.device('cuda' if torch.cuda.is_available() else 'cpu')
```

```
print(f'Using device: {device}')

model = train_mnist(device=device)

transform = transforms.Compose([
    transforms.ToTensor(),
    transforms.Normalize((0.1307,), (0.3081,))
])

test_data = datasets.MNIST(root='./data', train=False, download=True, transform=test_loader = DataLoader(test_data, batch_size=1000, shuffle=False)

evaluate(model, test_loader, device=device)
```

Using device: cuda Test Accuracy: 97.78% Test Accuracy: 97.78%

Out[]: 97.78