Numerical Experiments for Verifying Demand Driven Deployment Algorithms

Jin Whan Bae and Gwendolyn Chee

2017-10-11

---

1   Introduction

For many fuel cycle simulations, it is currently up to the user to define a deploy scheme, or facility parameters, to make sure that there's no gap in the supply chain. Or, the same goal is achieved by setting the `facility` capacity to infinity, which does not reflect real-world conditions.

The Demand-Driven Cycamore Archetype project (NEUP-FY16-10512) aims to develop CY-CAMORE demand-driven deployment capabilities. The developed algorithm, in the form of CY-CLUS `Institution` agent, deploys `facilities` to meet the front-end and back-end demand of the fuel cycle.

This report provides numerical tests for non-optimizing, deterministic-optimizing and stochastic-optimizing prediction algorithms.

These prediction models are being developed by the University of South Carolina. In this report, we discuss numerical experiments for testing the non-optimizing, deterministic optimizing and stochastic optimizing methods. The numerical experiments will be designed for both the once through nuclear fuel cycle and advanced fuel cycles.

2   Method

This report lists necessary capabilities of the new CYCLUS `institute` for demand-driven deployment of fuel cycle facilities. Then the report lists tests to check correct implementation of the capabilities, with a sample fuel cycle with well-defined facility parameters.

3 Configuration

The user defines prototypes to be deployed for fuel facilities, and reactor deployment scheme. The reactor deployment causes the demand of fuel which triggers fuel facility deployment. The detailed input file XML input schema is shown in Appendix A.

4 Algorithm Flow

The algorithm, upon entering, creates a supply chain with the fuel facilities and the reactor. Then, at every timestep it calculates the demand from each fuel cycle facility and makes decisions to deploy or decommission.

4.1 Upon Entering (`Enternotify`)

The algorithm creates a supply chain with the fuel facilities, then calculates the demand for each facility for a unit quantity of fuel. A simple example is illustrated in figure 1.
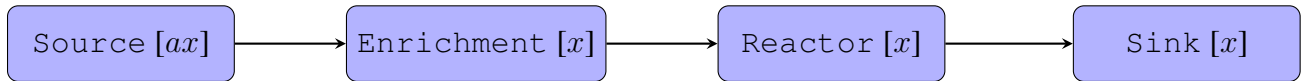

Figure 1: *Simple demand flow of materials. The values in the bracket are demands calculated by the algorithm. The* `Reactor` *demands x amount of fuel, which translates into demands of x from* `Enrichment` *and* `Sink`. *The* `Source` *has a demand of ax to take in for enrichment losses. $a \approx 9$ for 3% enrichment.*

4.2 Tick

Before the dynamic resource exchange phase, the algorithm calculates the fuel demand from the current fleet of reactors, and the corresponding demand for fuel facilities. The current capacity of each fuel cycle facility is also calculated. If the capacity is smaller than the demand, the algorithm build more facilities to meet the demand.

5 Simulation parameter for Test Scenarios

Simple parameters are given to fuel cycle facilities for the numerical test of the algorithm. Table 1 provides the parameters for the `reactors` in the test scenarios and Table 2 provides the parameters for the `source`, `enrichment` and `sink` facilities in the test scenarios.

Reactor Parameters	Value	Units
Cycle Time	2	timesteps
Refuel Time	1	timesteps
Lifetime	6	timesteps
Power Capacity	1000	MWe
Assembly Size	100	kg
# assemblies per core	3	
# assemblies per batch	1	

Table 1: Reactor Parameters

Parameters	Value	Units
Natural U Composition	0.71	% U235
Tails Assay	0.003	% U235
Fuel Enrichment	4	% U235
Enrichment SWU Capacity	2000	$\frac{SWU}{month \cdot facility}$
Source Throughput	3000	$\frac{kg}{month \cdot facility}$
Sink Capacity	200	$\frac{kg}{facility}$

Table 2: Source, Enrichment and Sink Facility Parameters

Table 3 provides the input and output commodity amounts and enrichment SWUs required based on a reactor fuel demand of 100 kg for one time step. These input and output commodities are based on the simple demand flow of materials shown in Figure 1.

Fuel (Reactor input commodity and Enrichment facility output commodity)	100 kg
Enrichment SWU	528 SWU
Natural Uranium (Source output commodity and enrichment input commodity)	901 kg

Table 3: Simulation parameters

An example input file with the facility and simulation definitions can be found in the input directory of this repository.

6   Numerical Tests for the Non-optimizing prediction method

To ensure that the non-optimizing prediction model is working correctly, each function of the code must be tested to determine if its output matches the analytical solution for the specified test scenario. In this section, the tests that must be met is described based on the parameters defined in Table 1 and 2 and analytical solution of a defined simple scenario. Unit test examples are included in Appendix B.

Test 1: A reactor outputs the user defined power capacity when deployed and does not output power capacity when decommissioned.
Test Scenario: A single reactor is deployed at time step 3 and decommissioned at time step 5. There is an infinite source of fuel for the reactor.
Analytical Solution: During cycle time, the reactor will have a power output of 1000MWe. Therefore, there is only be power output of 1000MWe at time steps 3 and 4. The analytical solution of the power output of the reactor per time step is given in Table 4.

Timestep	Reactor Power Output (MWe)
1	0
2	0
3	1000
4	1000
5	0
6	0

Table 4: Analytical solution of the power output of the reactor per time step

Test 2: A reactor outputs the user defined power capacity during its cycle time and not during its refuel time.
Test Scenario: A single reactor is deployed at time step 3 and decommissioned at time step 8.
Analytical Solution: Based on the reactor parameters defined in Table 1, the reactor will have a cycle time of 2 time steps and a refuel time of 1 time step. Therefore, there is only be power output of 1000MWe during cycle time steps. The analytical solution of the power output of the reactor per time step is given in Table 5.

Timestep	Reactor Power Output (MWe)
1	0
2	0
3	1000
4	1000
5	0
6	1000
7	1000
8	0
9	0

Table 5: Analytical solution of the power output of the reactor per time step

Test 3: A facility that produces reactor's input commodity (fuel) is deployed when the amount of fuel available is below the amount of fuel required by the reactor.

Test Scenario: A single reactor is deployed at time step 3.

Analytical Solution: Based on the simple supply chain example in Figure 1 and enrichment facility parameters defined in Table 2, an enrichment facility must be deployed at time step 3 to meet fuel demand. The analytical solution of the fuel facility deployment per time step is given in Table 6.

Timestep	Enrichment Facility deployment
1	0
2	0
3	1
4	0

Table 6: Analytical solution of the number of fuel facilities deployed per time step

Test 4: An appropriate number of facilities that produces reactor's input commodity (fuel) is deployed to meet the demand of the amount of fuel required by the reactor, when the initial fuel supply is non-zero.

Test Scenario: An initial fuel supply of 100kg. 2 reactors deployed at time step 2.

Analytical solution: Based on Table 1, each reactor has a fuel demand of 300kg per time step. Therefore, the fuel supply is 100kg at time step 1 and is 700kg at time steps 2 and 3. The analytical solution of fuel quantity per time step is given in Table 7

Timestep	Fuel Quantity (kg)
1	100
2	700
3	700

Table 7: Analytical solution of the fuel available per time step

Test 5: The fuel supply is within plus-minus the output of 1 fuel-producing facility of the reactor demand for fuel for all time steps.

Test Scenario: A reactor is deployed at timesteps 2, 3 and 4.

Analytical Solution: Based on Table 1, each reactor has a fuel demand of 300kg per time step. If an appropriate number of enrichment facilities is deployed to meet fuel demand, the difference between fuel quantity and fuel demand will be 100kg per time step. The analytical solution of difference between fuel quantity and fuel demand per time step is given in Table 8.

Timestep	Fuel Quantity (kg)	Fuel Demand (kg)	Difference (kg)
1	100	0	100
2	400	300	100
3	700	600	100
4	1000	900	100

Table 8: Analytical solution of the difference between fuel quantity and fuel demand per time step

Test 6: A facility that produces fuel producing facility's input commodity is deployed when the amount of input commodity is below the amount required by the fuel producing facility.

Test Scenario: An enrichment facility is deployed at time step 2.

Analytical Solution: Based on the simple supply chain example in Figure 1, a source facility must be deployed at time step 2 to meet natural uranium demand. The analytical solution of the source facility deployment per time step is given in Table **??**.

Timestep	Source Facility deployment
1	0
2	1
3	0

Table 9: Analytical solution of the number of source facilities deployed per time step

7 Appendix A - parameter configuration

First, the user defines the prototypes to be deployed to support the reactor.

```xml
<interleave>
  <element name="institution">
    <data type="string"/>
  </element>
    <element name="prototypes">
      <oneOrMore>
        <element name="val">
          <data type="string"/>
        </element>
      <oneOrMore>
    </element>
</interleave>
```

Code 1: Fuel cycle facility prototype definition

Then deployment of the power-producing reactors is defined, and the user is given two choices:

- Manually define the deployment scheme of reactors (code 2)

- Define power demand equation (code 3)

```
<interleave>
    <element name="reactors">
        <oneOrMore>
            <element name="val">
                <data type="string"/>
            </element>
        </oneOrMore>
    </element>
    <element name="build_times">
        <oneOrMore>
            <element name="val">
                <data type="int"/>
            </element>
        </oneOrMore>
    </element>
    <element name="n_build">
        <oneOrMore>
            <element name="val">
                <data type="int"/>
            </element>
        </oneOrMore>
    </element>
    <optional>
        <element name="lifetimes">
            <oneOrMore>
                <element name="val">
                    <data type="int"/>
                </element>
            </oneOrMore>
        </element>
    </optional>
</interleave>
```

Code 2: Manual definition of reactor deployment

```
<interleave>
    <element name="growth">
        <oneOrMore>
            <element name="item">
                <interleave>
                    <element name="reactors">
                        <data type="string"/>
                    </element>
                    <element name="piecewise_function">
                        <oneOrMore>
                            <element name="piece">
                                <interleave>
                                    <element name="start">
                                        <data type="int"/>
                                    </element>
                                    <element name="function">
                                        <interleave>
                                            <element name="type">
                                                <data type="string"/>
                                            </element>
                                            <element name="params">
                                                <data type="string"/>
                                            </element>
                                        </interleave>
                                    </element>
                                </interleave>
                            </element>
                        </oneOrMore>
                    </element>
                </interleave>
            </element>
        </oneOrMore>
    </element>
</interleave>
```

Code 3: Definition of power demand function