Flash-X User's Guide

Version alpha (last updated January 16, 2022)

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Chapter 1

Introduction

The Flash-X code is a component-based software system for simulation of multiphysics applications formulated largely as a collection of partial- and ordinary- differential equations as well as algebraic equations. The maintained code components are written in a combination of high level languages such as Fortran, C and C++ with an embedded domain-specific macro language implemented in the form of key-value dictionaries. The accompanying configuration tool-chain, written in Python and can translate and assemble different permutations and combinations of the components to configure a diverse set of applications. Also included in the distribution is a accompanying domain-specific runtime system that can orchestrate data movement between devices (CPU, accelerators, and other specialized devices that might exist) on a compute node of a high performance computing (HPC) platform. It uses the Message-Passing Interface (MPI) library communication between nodes, though more than one MPI rank can also be placed on a node. HDF5 is the default mode for IO. Flash-X has three interchangeable discretization grids: a Uniform Grid, a oct-tree based adaptive grid using the PARAMESH library, and a block-structured adaptive grid using AMReX library, which also mimics an oct-tree-like layout for use in Flash-X.

Part I Getting Started

Chapter 2

Quick Start

This chapter describes how to get up-and-running quickly with Flash-X with an example simulation, the Sedov explosion. We explain how to configure a problem, build it, run it, and examine the output using IDL.

2.1 System requirements

You should verify that you have the following:

- A copy of the Flash-X source code distribution. To obtain a copy of the source code, please visit https://github.com/Flash-X and request access to the Flash-X repository as a collaborator.
- A Fcompiler, a C compiler, and a C++ compiler, and Python 3 or above.
- An installed copy of the Message-Passing Interface (MPI) library, and the HDF5 library.
- To use AMReXfor AMR, it must be installed. AMReXrequires a different version each for 1, 2 or 3 dimensional application configurations. (for details see). Paramesh is included in the source code.
- AMReXis compatible with PETSc and Hypre math libraries, and Parameshis compatible with Hypre. They must be installed on the platform and their location should be made known to AMReX.
- The GNU make utility
- A copy of the Python language, version 3.0 or later is required.

2.2 Obtaining and configuring Flash-X for quick start

To begin, clone the Flash-X source code distribution.....

This quick start example uses Parameshfor AMR and does not depend on PETSc or Hypre. It also does not use accelerators or other devices on the node, neither does it exercise advanced features of the Orchestration System. It requires MPI and HDF5 installed, and runs using one CPU per MPI rank.

Once you have the source code and all the necessary libraries installed configure the Flash-X source tree for the Sedov explosion problem using the setup command Type

./setup Sedov -auto

This configures Flash-X for the 2d Sedovproblem using the default hydrodynamic solver, equation of state, Grid unit, and I/O format defined for this problem, linking all necessary files into a new directory, called 'object/'. For the purpose of this example, we will use the default I/O format, serial HDF5. In order to compile a problem on a given machine Flash-X allows the user to create a file called Makefile.hwhich sets the paths to compilers and libraries specific to a given platform. This file is located in the directory sites/mymachine.myinstitution.mydomain/. The setup script will attempt to see if your machine/platform

has a Makefile.halready created, and if so, this will be linked into the object/ directory. If one is not created the setup script will use a prototype Makefile.h with guesses as to the locations of libraries on your machine. The current distribution includes prototypes for *Linux*, *OSX* operating systems. In any case, it is advisable to create a Makefile.h specific to your machine. See ?? for details.

Type the command cd object to enter the object directory which was created when you setup the Sedov problem, and then execute make. This will compile the Flash-X code.

cd object
make

If you have problems and need to recompile, 'make clean'will remove all object files from the object/ directory, leaving the source configuration intact; 'make realclean'will remove all files and links from object/. After 'make realclean', a new invocation of setup is required before the code can be built. The building can take a long time on some machines; doing a parallel build (make -j for example) can significantly increase compilation speed, even on single processor systems.

Assuming compilation and linking were successful, you should now find an executable named flashx in the object/ directory. You may wish to check that this is the case.

If compilation and linking were not successful, here are a few common suggestions to diagnose the problem:

- Make sure the correct compilers are in your path, and that they produce a valid executable.
- The default Sedov problem uses HDF5 in serial. Make sure you have HDF5 installed. If you do not have HDF5, you can still setup and compile Flash-X, but you will not be able to generate either a checkpoint or a plot file. You can setup Flash-X without I/O by typing

./setup Sedov -auto +noio

- Make sure the paths to the MPI and HDF libraries are correctly set in the Makefile.h in the object/directory.
- Make sure your version of MPI creates a valid executable that can run in parallel.

Flash-X by default expects to find a text file named flash.parin the directory from which it is run. This file sets the values of various runtime parameters that determine the behavior of Flash-X. If it is not present, Flash-X will abort; flash.par must be created in order for the program to run (note: all of the distributed setups already come with a flash.par which is *copied* into the object/ directory at setup time). There is command-line option to use a different name for this file, described in the next section. Here we will create a simple flash.par that sets a few parameters and allows the rest to take on default values. With your text editor, edit the flash.par in the object directory so it looks like ??.

This example first instructs Flash-X to name output files appropriately (through the basenm parameter). Flash-X is then instructed to use up to five levels of adaptive mesh refinement (AMR) (through the lrefine_max parameter), with the actual refinement adapted based on the density and pressure of the solution (parameters refine_var_1 and refine_var_2). We will not be starting from a checkpoint file ("restart = .false." — this is the default, but here it is explicitly set for clarity). Output files are to be written every 0.01 time units (checkpointFileIntervalTime) and will be created until t = 0.05 or 10000 timesteps have been taken (tmax and nend respectively), whichever comes first. The ratio of specific heats for the gas (gamma = γ) is taken to be 1.4, and all four boundaries of the two-dimensional grid have outflow (zero-gradient or Neumann) boundary conditions (set via the [xy][lr]_boundary_type parameters).

Note the format of the file – each line is of the form variable = value, a comment (denoted by a hash mark, #), or a blank. String values are enclosed in double quotes ("). Boolean values are indicated in the FORTRAN style, .true. or .false.. Be sure to insert a carriage return after the last line of text. A full list of the parameters available for your current setup is contained in the file setup_params located in the object/ directory, which also includes brief comments for each parameter. If you wish to skip the creation of a flash.par, a complete example is provided in the source/Simulation/SimulationMain/Sedov/ directory.

```
# runtime parameters
basenm = "sedov_"
lrefine_max = 5
refine_var_1 = "dens"
refine_var_2 = "pres"
restart = .false.
checkpointFileIntervalTime = 0.01
nend = 10000
tmax = 0.05
gamma = 1.4
xl_boundary_type = "outflow"
xr_boundary_type = "outflow"
yl_boundary_type = "outflow"
yr_boundary_type = "outflow"
plot_var_1 = "dens"
plot_var_2 = "temp"
plot_var_3 = "pres"
sim_profFileName = "/dev/null"
```

Figure 2.1: Flash-X parameter file contents for the quick start example.

2.3 Running Flash-X

We are now ready to run Flash-X. To run Flash-X on N processors, type

```
mpirun -np N flashX
```

remembering to replace N and X with the appropriate values. Some systems may require you to start MPI programs with a different command; use whichever command is appropriate for your system. The FLASH-X executable accepts an optional command-line argument for the runtime parameters file. If "-par_file file-name" is present, Flash-X reads the file specified on command line for runtime parameters, otherwise it reads flash.par.

You should see a number of lines of output indicating that Flash-X is initializing the Sedov problem, listing the initial parameters, and giving the timestep chosen at each step. After the run is finished, you should find several files in the current directory:

- sedov.logechoes the runtime parameter settings and indicates the run time, the build time, and the build machine. During the run, a line is written for each timestep, along with any warning messages. If the run terminates normally, a performance summary is written to this file.
- sedov.datcontains a number of integral quantities as functions of time: total mass, total energy, total momentum, etc. This file can be used directly by plotting programs such as gnuplot; note that the first line begins with a hash (#) and is thus ignored by gnuplot.
- sedov_hdf5_chk_000* are the different checkpoint files. These are complete dumps of the entire simulation state at intervals of checkpointFileIntervalTime and are suitable for use in restarting the simulation.
- sedov_hdf5_plt_cnt_000* are plot files. In this example, these files contain density, temperature, and pressure in single precision. If needed, more variables can be dumped in the plotfiles by specifying them in flash.par. They are usually written more frequently than checkpoint files, since they are the primary output of Flash-X for analyzing the results of the simulation. They are also used for making simulation movies. Checkpoint files can also be used for analysis and sometimes it is necessary to use them since they have comprehensive information about the state of the simulation at a given time. However, in general, plotfiles are preferred since they have more frequent snapshots of the time evolution. Please see ?? for more information about IO outputs.

Flash-X is intended to be customized by the user to work with interesting initial and boundary conditions. In the following sections, we will cover in more detail the algorithms and structure of Flash-X and the sample problems and tools distributed with it.

Part II The Flash-X Software System

Chapter 3

Overview of Flash-X architecture

FLASH-X is a component based software system where different permutations and combinations of various components generate different applications. Some aspects of FLASH-X architecture are adapted from FLASH [?], but it is fundamentally a new software with a new architecture designed for use with heterogeneous platforms. Portability on heterogeneous platforms is achieved through an **orchestration system** (ORS), comprised of three sets of tools: the **configuration tools** (CFT), **code translators** (CT) and the **orchestration runtime** subsystem (OR).

The CFT include a configuration domain specific language (DSL) for program synthesis through assembly, and a key-value dictionary with a correspoding translator macroprocessor. The configuration toolchain takes its inspiration from the setup tool of FLASH which has been used to implement composability at the level of major functionalities in the code. The setup tool interprets the configuration (DSL), which encode metadata about each component and subcomponent of the code in a completely distributed fashion in config files. The metadata about one component is completely oblivious of the metadata about other components, though it has some knowledge of the components that are available in the code. The setup tool recursively parses the config file of each mentioned component, assimilates the information, and assembles a consistent, fully-configured instance of an application along with its build system and static runtime environment. The key-value dictionary serves dual purpose of lowering the granularity of components for assembly by the setup tool, and enables single expression of maintained source code. The keys are language agnostic macros with enhancements such as inlining, recursion and arguments. Combined with the setup tool, the macroprocessor brings the functionality of C++ template metaprogramming tools such as Kokkos and Raja that permits maintenance of single source code that can be specialized for target devices as needed.

The CTenable the maintained source code to be augmented with performance hints in the form of Flash-X native directives. Another DSL has been built for expressing recipies for overall control flow of the simulation. The recipes replace the timestepper functionality because control flow during evolution of solution now may involve offloading work and data to different devices, therefore, simple drivers are no longer adequate. The CThave two tasks: (1) parse the Flash-X directives for optimization within the physics operators; and (2) to translate the recipe into a data flow description of the execution suitable for the OR. The OR then uses this generated information to orchestrate computation and data movement between devices as needed. The overarching design principle of the ORS is to enable both domain-specific knowledge and platform knowledge to be utilized in application configuration without placing undue burden on either the tool developers or the domain experts.

The ORS exposes the hierarchy of data motion and allocations deep within the components of the applications and separates them from the arithmetic and logic implementing the numerical method. On the platform hardware side, they expose the hierarchical parallelism of a given platform's hardware through appropriately designed interfaces. The objective of this exercise is to enable the software to take maximal advantage of the exposed parallelism in hardware without having to alter the arithmetic. The directives serve the purpose of letting the code translators know which kind of transformations are safe for specific devices. Some program synthesis is involved in the process that can take several passes of code generation. Similar to the code expression, the offline tools themselves subscribe to separation of concerns in the sense that each tool addresses itself to a very focused program synthesis step.

We begin by casting every non-trivial function in the physics operators of the code as a collection of code blocks. Some code blocks may be declarations, some may implement the control logic, and some will implement the numerics of the function. Sometimes arithmetic and logic blocks cannot be separated out; some code blocks have both. These code blocks become components in a hierarchical composability through the use of key-value dictionary where values are code snippets of arbitrary length and complexity. Keys are user defined with a provision for multiple alternative definitions which lets them mimic the template metaprogramming in C++ where a single expression of an algorithm can have specializations through alternative definitions of the key (see ?? for details).

The information encoded in the directives is utilized by the CTto determine which code blocks can be treated as kernels on devices such as accelerators, which code blocks can have overlapped computation with other code blocks, which code blocks can be queued sequentially so that data movement is minimized, etc. Note that the absence of such metadata has no implication for correct execution. Instead, what this decomposition aims for is better optimization with richer metadata. While the present implementation primarily requires hand coding of this information, we expect to be able to utilize third-party code analysis tools to infer this information automatically in the future. This division of labor between multiple tools is made not only to achieve good encapsulation and modularity, but also to ensure that no single tool is too complex or requires too much intelligence. This design approach enables extraction of all useful information for orchestrating computations during runtime when the application is being configured. This is in contrast to general solutions that delay the orchestration decision due to the conservative assumption that information about the tasks and their dependencies is only fully known at runtime. While this approach may not squeeze every last bit of performance from the hardware, it has the virtue of being simple and maintainable with no runtime overheads. Also, by design, every step in program synthesis is human-readable to facilitate both correctness-debugging and performance-debugging.

The design goal of the OR is to develop a base set of runtime elements, such as thread teams, that can be composed at runtime into thread team configurations in ways that maximize the efficient use of the node. For a given simulation, the OR operates with N thread teams that are created when the simulation starts and persist until the simulation terminates, where each team is allowed to simultaneously use at most M threads at any given time. The thread teams are run in cycles such that for each cycle a team is assigned an action routine and a data type. Examples of data types are tiles, blocks, and data packets of blocks. Upon starting a cycle, the team is given data items of the appropriate type and the threads of the team work in a coordinated fashion so that the given action is applied to each data item once. The cycle ends once the team has been informed that no more data items will be given and the action has been applied to all given data items. In our design, the pairing of the action with data items is viewed as a task so that thread teams implement task-based parallelism via thread-level parallelism. While the threads in the team execute code in the host, they can also be used to launch kernels in accelerators and therefore make use of finer-grained parallelism. Ideally, the data type assigned to a thread team for a given action will be chosen based on the hardware that the action routine has been written to use. For instance, a tile would be a sensible data type for executing an action routine that uses the CPU for heavy computation or a data packet of blocks for a routine that launches kernels on a remote device with its own memory system. While it might have been possible to adapt existing tools such as Legion [?] for some of the functionality we are aiming for, we have opted for an end-to-end domain specific solution that has simple enough tools that even a small team can customize and maintain with their own code. Additionally, our orchestration system is absolutely language agnostic, even though we are exercising it with Fortran.

Note that no part of this design limits itself to using manually built task graphs nor requires extreme simplicity in them. The interfaces are designed to be robust enough that the OR can also execute complex task graphs. By disassociating the executor of the graph from the generator, we have ensured that in the future, we will be able to use automation in task graph generation without having to alter the mechanics of the OR. All the heavy lifting of analysis and scheduling can be done separately in the generator which never needs to interface with the executor. We believe that this model of combination of program synthesis with orthogonal composition concepts will have longevity because of its ability to adapt to new systems incrementally.

3.0.1 Translator

The translator for the keys adds a new capability to the Setup Tool that implements the key-value dictionary feature of the program synthesis. This tool, like the Setup Tool, is written in python and is the last feature invoked during the configuration of an application instance. Definitions are stored in ".ini" files, according to the Python ConfigParser format. Style guidelines are documented for ease of use by the developers. When a new definition file is created, the corresponding config file is informed about its existence so that the Setup Tool includes it during configuration. The source files needing translation are given the extension ".F90-mc" to differentiate them from the source files that do not need to have the translation applied on them. The translator can also be invoked independently if a developer wishes to inspect how keys are replaced by their definitions. The output comes out in a ".F90" file which is a normal Fortran file and can be compiled by any Fortran compiler. Various command-line arguments can specify which files to process and which definitions files to read. By default, the translator will read all '.ini' files in the directory, then process all '.F90-mc' files and write the modified files to '.F90' format.

3.1 Flash-X Inheritance

FLASH-X inheritance is implemented through the Unix directory structure and the setup tool. When the setup tool parses the source tree, it treats each child or subdirectory as inheriting all of the Config and Makefile files in its parent's directory. While source files at a given level of the directory hierarchy override files with the same name at higher levels, Makefiles and configuration files are cumulative. Since functions can have multiple implementations, selection for a specific application follows a few simple rules applied in order described in

However, we must take care that this special use of the directory structure for inheritance does not interfere with its traditional use for organization. We avoid any problems by means of a careful naming convention that allows clear distinction between organizational and namespace directories. See ?? for naming conventions.

3.2 Unit Test Framework

In keeping with good software practice, FLASH-X incorporates a unit test framework that allows for rigorous testing and easy isolation of errors. The components of the unit test show up in two different places in the FLASH-X source tree. One is a dedicated path in the Simulation unit, Simulation/SimulationMain/-unitTest/UnitTestName, where UnitTestName is the name of a specific unit test. The other place is a sub-directory called unitTest, somewhere in the hierarchy of the corresponding unit which implements a function Unit_unitTest and any helper functions it may need. The primary reason for organizing unit tests in this somewhat confusing way is that unit tests are special cases of simulation setups that also need extensive access to internal data of the unit being tested. By splitting the unit test into two places, it is possible to meet both requirements without violating unit encapsulation. We illustrate the functioning of the unit test framework with the unit test of the Eos unit. For more details please see ??. The Eos unit test needs its own version of the routine [[api reference]] which makes a call to its Eos_unitTest routine. The initial conditions specification and unit test specific Driver_evolveFlash are placed in Simulation/SimulationMain/unitTest/Eos, since the Simulation unit allows any substitute FLASH-X function to be placed in the specific simulation directory. The function Eos_unitTest resides in physics/Eos/unitTest, and therefore has access to all internal Eos data structures and helper functions.

Chapter 4

The Flash-X configuration script (setup)

The setup tool is the most important component of the Unix. It implements the inheritance and composability of the Flash-X software system. It traverses the Flash-X source tree starting from the directory hosting the specific application definition. This starting directory is essentially the selected implementation of the "Simulation" unit. While traversing the source three the setup tool does the following:

- arbitrate on map from a key to its definition, in particular if alternative definitions exist
- arbitrate on which implementation of a function to use
- link selected files (include source code and the key definitions) to the object/ directory
- invoke macroprocessor to translate keys and generate source file
- alter index order if desired
- find the target Makefile.h
- generate the Makefile that will build the Flash-X executable.
- generate the files needed to add runtime parameters to a given simulation.
- generate the files needed to parse the runtime parameter file.

More description of how setup and the FLASH-X architecture interact may be found in ??. Here we describe its usage.

The setup script determines site-dependent configuration information by looking for a directory sites/<hostname> where <hostname> is the hostname of the machine on which Flash-X is running. Failing this, it looks in sites/Prototypes/ for a directory with the same name as the output of the uname command. The site and operating system type can be overridden with the -site and -ostype command-line options to the setup command. Only one of these options can be used at one time. The directory for each site and operating system type contains a makefile fragment Makefile.h that sets command names, compiler flags, library paths, and any replacement or additional source files needed to compile Flash-X for that specific machine and machine type.

The setup script starts with the Config file of the specified application in the Simulation unit, finds its REQUIRED units and then works its way through their Config files. This process continues until all the dependencies are met and a self-consistent set of units has been found. At the end of this automatic generation, the Units file is created and placed in the object/directory, where it can be edited if necessary. setup also creates the master makefile (object/Makefile) and several FORTRAN include files that are needed by the code in order to parse the runtime parameters. After running setup, the user can create the

¹if a machine has multiple hostnames, setup tries them all

Flash-X executable by running make in the object directory. Note that the Flash-X build system assumes that the command make invokes GNU Make and is unlikely to work properly with other implementations of the make command. On some systems it may be necessary to invoke GNU Make under the name gmake.

Save some typing

- All the setup options can be shortened to unambiguous prefixes, e.g. instead of ./setup -auto can just say ./setup -a problem-name since there is only one setup option starting with a.
- The same abbreviation holds for the problem name as well. ./setup -a IsentropicVortex can be abbreviated to ./setup -a Isen assuming that IsentropicVortex is the only problem name which starts with Isen.
- Unit names are usually specified by their paths relative to the source directory. However, setup also allows unit names to be prefixed with an extra "source/", allowing you to use the TAB-completion features of your shell like this
 - ./setup -a Isen -unit=sou<TAB>rce/IO/IOM<TAB>ain/hd<TAB>f5
- If you use a set of options repeatedly, you can define a shortcut for them. FLASH-X comes with a number of predefined shortcuts that significantly simplify the setup line, particularly when trying to match the Grid with a specific I/O implementation. For more details on creating shortcuts see ??. For detailed examples of I/O shortcuts please see ??in the I/O chapter.

4.1 Setup Arguments

The setup script accepts a large number of command line arguments which affect the simulation in various ways. These arguments are divided into three categories:

- 1. Setup Options (example: -auto) begin with a dash and are built into the setup script itself. Many of the most commonly used arguments are setup options.
- 2. Setup Variables (example: species=air,h2o) are defined by individual units. When writing a Config file for any unit, you can define a setup variable. ?? explains how setup variables can be created and used.
- 3. Setup Shortcuts (example: +ug) begin with a plus symbol and are essentially macros which automatically include a set of setup variables and/or setup options. New setup shortcuts can be easily defined, see ?? for more information.

?? shows a list of some of the basic setup arguments that every Flash-X user should know about. A comprehensive list of all setup arguments can be found in ?? alongside more detailed descriptions of these options.

4.2 Comprehensive List of Setup Arguments

Argument	Description
-auto	this option should almost always be set
-unit= <unit></unit>	include a specified unit
-objdir= <dir></dir>	specify a different object directory location
-debug	compile for debugging
-opt	enable compiler optimization
-n[xyb]b=#	specify block size in each direction
-maxblocks=#	specify maximum number of blocks per process
-[123]d	specify number of dimensions
-maxblocks=#	specify maximum number of blocks per process
+cartesian	use Cartesian geometry
+cylindrical	use cylindrical geometry
+polar	use polar geometry
+spherical	use spherical geometry
+noio	disable IO
+ug	use the uniform grid in a fixed block size mode
+nofbs	use the uniform grid in a non-fixed block size mode
+pm2	use the PARAMESH2 grid
+pm40	use the PARAMESH4.0 grid
+pm4dev	use the PARAMESH4DEV grid
+uhd	use the Unsplit Hydro solver
+usm	use the Unsplit Staggered Mesh MHD solver
+splitHydro	use a split Hydro solver

Table 4.1: List of Commonly Used Setup Arguments

-verbose=<verbosity>

Normally setup prints summary messages indicating its progress. Use the -verbose to make the messages more or less verbose. The different levels (in order of increasing verbosity) are ERROR, IMPINFO, WARN, INFO, DEBUG. The default is WARN.

-auto

Normally, setup requires that the user supply a plain text file called Units (in the object directory ²) that specifies the units to include. A sample Units file appears in ??. Each line is either a comment (preceded by a hash mark (#)) or the name of a an include statement of the form INCLUDE *unit*. Specific implementations of a unit may be selected by specifying the complete path to the implementation in question; If no specific implementation is requested, setup picks the default listed in the unit's Config file.

The -auto option enables setup to generate a "rough draft" of a Units file for the user. The Config file for each problem setup specifies its requirements in terms of other units it requires. For example, a problem may require the perfect-gas equation of state (physics/Eos/EosMain/Gamma) and an unspecified hydro solver (physics/Hydro). With -auto, setup creates a Units file by converting these requirements into unit include statements. Most users configuring a problem for the first time will want to run setup with -auto to generate a Units file and then to edit it directly to specify alternate implementations of certain units. After editing the Units file, the user must re-run setup without -auto in order to incorporate his/her changes into the code configuration. The user may also use the command-line option -with-unit=<path> in conjunction with the -auto option, in order to pick a specific implementation of a unit, and thus eliminate the need to hand-edit the Units file.

²Formerly, (in Flash-X2) it was located in the Flash-X root directory

-[123]d

By default, setup creates a makefile which produces a Flash-X executable capable of solving two-dimensional problems (equivalent to -2d). To generate a makefile with options appropriate to three-dimensional problems, use -3d. To generate a one-dimensional code, use -1d. These options are mutually exclusive and cause setup to add the appropriate compilation option to the makefile it generates.

-maxblocks=#

setup in constructing the makefile compiler options. It determines the amount of memory allocated at runtime to the adaptive mesh refinement (AMR) block data structure. For example, to allocate enough memory on each processor for 500 blocks, use <code>-maxblocks=500</code>. If the default block buffer size is too large for your system, you may wish to try a smaller number here; the default value depends upon the dimensionality of the simulation and the grid type. Alternatively, you may wish to experiment with larger buffer sizes, if your system has enough memory. A common cause of aborted simulations occurs when the AMR grid creates greater than <code>maxblocks</code> during refinement. Resetup the simulation using a larger value of this option.

-nxb=# -nyb=# -nzb=# These options are used by setup inconstruct- \blacksquare ing the make- ${\rm file}$ com-■ piler options. The mesh on which the problemis solvedis com- posed of blocks, and each block contains somenum- $\quad \text{ber} \quad$ of cells. \blacksquare The -nxb,-nyb, and -nzb options determine how many ${\it cells}$ each block

contains
(not

[-debug|-opt|-test]

The default Makefile built by setup will use the optimized setting (-opt) for compilation and linking. Using -debug will force setup to use the flags relevant for debugging (e.g., including -g in the compilation line). The user may use the option -test to experiment with different combinations of compiler and linker options. Exactly which compiler and linker options are associated with each of these flags is specified in sites/<hostname>/Makefile* where <hostname> is the hostname of the machine on which Flash-X is running.

For example, to tell an Intel Fortran compiler to use real numbers of size 64 when the -test option is specified, the user might add the following line to his/her Makefile.h:

FFLAGS_TEST = -real_size 64

-objdir=<dir>

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-curvilinear

Enable code in PARAMESH 4 that implements geometrically correct data restriction for curvilinear coordinates. This setting is automatically enabled if a non-cartesian geometry is chosen with the -geometry flag; so specifying -curvilinear only has an effect in the Cartesian case.

-defines=<def>[,<def>]...

<def> is of the form SYMBOL or SYMBOL=value. This causes the specified pre-processor symbols
to be defined when the code is being compiled. This is mainly useful for debugging the code.
For e.g., -defines=DEBUG_ALL turns on all debugging messages. Each unit may have its own
DEBUG_UNIT flag which you can selectively turn on.

[-fbs|-nofbs]

Causes the code to be compiled in fixed-block or non-fixed-block size mode. Fixed-block mode is the default. In non-fixed block size mode, all storage space is allocated at runtime. This mode is available only with Uniform Grid.

-geometry=<geometry>

Choose one of the supported geometries cartesian, cylindrical, spherical, or polar. Some Grid implementations require the geometry to be known at compile-time while others don't. This setup option can be used in either case; it is a good idea to specify the geometry here if it is known at setup-time. Choosing a non-Cartesian geometry here automatically sets the -gridinterpolation=monotonic option below.

-gridinterpolation=<scheme>

Select a scheme for Grid interpolation. Two schemes are currently supported:

• monotonic

This scheme attempts to ensure that monotonicity is preserved in interpolation, so that interpolation does not introduce small-scale non-monotonicity in the data.

The monotonic scheme is required for curvilinear coordinates and is automatically enabled if a non-cartesian geometry is chosen with the -geometry flag. For AMR Grid implementations, This flag will automatically add additional directories so that appropriate data interpolation methods are compiled it. The monotonic scheme is the default (by way of the +default shortcut), unlike in FLASH-X.

• native

Enable the interpolation that is native to the AMR Grid implementation (PARAMESH 2 or PARAMESH 4) by default. This option is only appropriate for Cartesian geometries.

```
#Units file for Sod generated by setup
INCLUDE Driver/DriverMain/Split
INCLUDE Grid/GridBoundaryConditions
INCLUDE Grid/GridMain/paramesh/interpolation/Paramesh4/prolong
INCLUDE Grid/GridMain/paramesh/interpolation/prolong
INCLUDE Grid/GridMain/paramesh/paramesh4/Paramesh4.0/PM4_package/headers
INCLUDE Grid/GridMain/paramesh/paramesh4/Paramesh4.0/PM4_package/mpi_source
INCLUDE Grid/GridMain/paramesh/paramesh4/Paramesh4.0/PM4_package/source
INCLUDE Grid/GridMain/paramesh/paramesh4/Paramesh4.0/PM4_package/utilities/multigrid
INCLUDE Grid/localAPI
INCLUDE IO/IOMain/hdf5/serial/PM
INCLUDE IO/localAPI
INCLUDE PhysicalConstants/PhysicalConstantsMain
INCLUDE RuntimeParameters/RuntimeParametersMain
INCLUDE Simulation/SimulationMain/Sod
INCLUDE flashUtilities/contiguousConversion
INCLUDE flashUtilities/general
INCLUDE flashUtilities/interpolation/oneDim
INCLUDE flashUtilities/nameValueLL
INCLUDE monitors/Logfile/LogfileMain
INCLUDE monitors/Timers/TimersMain/MPINative
INCLUDE physics/Eos/EosMain/Gamma
INCLUDE physics/Hydro/HydroMain/split/PPM/PPMKernel
```

Figure 4.1: Example of the Units file used by setup to determine which Units to include

-makefile=<extension>

setup normally uses the Makefile.h from the directory determined by the hostname of the machine and the -site and -os options. If you have multiple compilers on your machine you can create Makefile.h.

extension> for different compilers. e.g., you can have a Makefile.h and Makefile.h.

lahey for the three different compilers. setup will still use the Makefile.h file by default, but supplying -makefile=intel on the command-line causes setup to use Makefile.h.
intel instead.

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-makehide

Ordinarily, the commands being executed during compilation of the Flash-X executable are sent to standard out. It may be that you find this distracting, or that your terminal is not able to handle these long lines of display. Using the option -makehide causes setup to generate a Makefile so that GNU make only displays the names of the files being compiled and not the exact compiler call and flags. This information remains available in setup_flags in the object/ directory.

-noclobber

setup normally removes all code in the object directory before linking in files for a simulation. The ensuing make must therefore compile all source files anew each time setup is run. The -noclobber option prevents setup from removing compiled code which has not changed from the previous setup in the same directory. This can speed up the make process significantly.

-os=<os>

If setup is unable to find a correct sites/ directory it picks the Makefile based on the operating system. This option instructs setup to use the default Makefile corresponding to the specified operating system.

-parfile=<filename>

This causes setup to copy the specified runtime-parameters file in the simulation directory to the object directory with the new name flash.par.

-append-parfiles=[location1/]<filename1>[,[location2/]<filename2>]...

This option takes a comma-separated list of names of parameter files and combines them into one flash.par file in the object directory. File names without an absolute path are taken to be relative to the simulation directory, as for the -parfile option.

To use such a combined flash.par in case of runtime parameters occurring more than once, note that when Flash-X reads a parameter file, the last instance of a runtime parameter supersedes previous ones.

If both -append-parfiles and -parfile are used, the files from the list are appended to the single parfile given by the latter in the order listed. If used with -parfile, -append-parfiles can append one or more parfiles to the one given by -parfile. If you only use -append-parfiles and not -parfile and give it fewer than two paths, an error will result. If more than one -append-parfiles option appears, the lists are concatenated in the order given.

-particlemethods=TYPE=<particle type>[,INIT=<init method>][,MAP=<map method>][,ADV=<advance method>]

This option instructs setup to adjust the particle methods for a particular particle type. It can only be used when a particle type has already been registered with a PARTICLETYPE line in a Config file (see ??). A possible scenario for using this option involves the user wanting to use a different passive particle initialization method without modifying the PARTICLETYPE line in the simulation Config file. In this case, an additional -particlemethods=TYPE=passive,INIT=cellmass adjusts the initialization method associated with passive particles in the setup generated Particles_specifyMethods() subroutine. Since the specification of a method for mapping and initialization requires inclusions of appropriate implementations of ParticlesMapping and ParticlesInitialization subunits, and the specification of a method for time advancement requires inclusion of an appropriate implementation under ParticlesMain, it is the user's responsibility to adjust the included units appropriately. For example a user may want want to override Config file defined particle type passive using lattice initialization CellMassBins density based distribution method using the setup command line. Here the user must first specify -without-unit=Particles/ParticlesInitialization/Lattice to exclude the lattice initialization, followed by -with-unit=Particles/ParticlesInitialization/WithDensity/-CellMassBins specification to include the appropriate implementation. In general, using command line overrides of -particlemethods are not recommended, as this option increases the chance of creating an inconsistent simulation setup. More information on multiple particle types can be found in ??, especially ??.

-portable

This option causes setup to create a portable object directory by copying instead of linking to the source files. The resulting object directory can be tarred and sent to another machine for actual compilation.

-site=<site>

setup searches the sites/ directory for a directory whose name is the hostname of the machine on which setup is being run. This option tells setup to use the Makefile of the specified site. This option is useful if setup is unable to find the right hostname (which can happen on multiprocessor or laptop machines). Also useful when combined with the -portable option.

-unitsfile=<filename>

This causes setup to copy the specified file to the object directory as Units before setting up the problem. This option can be used when -auto is not used, to specify an alternate Units file. -with-library=<libname>[,args], -library=<libname>[,args]

This option instructs setup to link in the specified library when building the final executable. A *library* is a piece of code which is independent of Flash-X. Internal libraries are those libraries whose code is included with Flash-X. The setup script supports external as well as internal libraries. Information about external libraries is usually found in the site specific Makefile. The additional args if any are library-specific and may be used to select among multiple implementations.

-tau=<makefile>

This option causes the inclusion of an additional Makefile necessary for the operation of Tau, which may be used by the user to profile the code. More information on Tau can be found at http://acts.nersc.gov/tau/

-without-library=<libname>

Negates a previously specified -with-library=<libname>[,args]

-without-unit=<unit>

This removes all units specified in the command line so far, which are children of the specified unit (including the unit itself). It also negates any REQUESTS keyword found in a Config file for units which are children of the specified unit. However it does not negate a REQUIRES keyword found in a Config file.

+default

This shortcut specifies using basic default settings and is equivalent to the following:

--with-library=mpi +io +grid-gridinterpolation=monotonic

+noio

This shortcut specifies a simulation without IO and is equivalent to the following:

--without-unit=physics/sourceTerms/EnergyDeposition/EnergyDepositionMain/Laser/LaserIO

--without-unit=IO

+io

This shortcut specifies a simulation with basic IO and is equivalent to the following:

--with-unit=I0

+serialIO

This shortcut specifies a simulation using serial IO, it has the effect of setting the setup variable parallelIO = False

+parallelIO

This shortcut specifies a simulation using serial IO, it has the effect of setting the setup variable parallelIO = True

+hdf5

This shortcut specifies a simulation using hdf5 for compatible binary IO output, it has the effect of setting the setup variable

I0 = hdf5

+hdf5TypeIO

This shortcut specifies a simulation using hdf5, with parallel io capability for compatible binary IO output, and is equivalent to the following:

+io +parallelIO +hdf5 typeIO=True

+nolog

This shortcut specifies a simulation without log capability it is equivalent to the following: -without-unit=monitors/Logfile

+grid

This shortcut specifies a simulation with the Grid unit, it is equivalent to the following: -unit=Grid

+ug

This shortcut specifies a simulation using a uniform grid, it is equivalent to the following: +grid Grid=UG

+pm2

This shortcut specifies a simulation using Paramesh2 for the grid, it is equivalent to the following: +grid Grid=PM2

+pm40

This shortcut specifies a simulation using Paramesh4.0 for the grid, it is equivalent to the following: +grid Grid=PM40

+pm4dev_clean

This shortcut specifies a simulation using a version of Paramesh 4 that is closer to the version available on sourceforge. It is equivalent to:

+grid Grid=PM4DEV ParameshLibraryMode=True

+pm4dev

This shortcut specifies a simulation using a modified version of Paramesh 4 that includes a more scalable way of filling the surr_blks array. It is equivalent to:

+pm4dev_clean FlashAvoidOrrery=True

+usm

This shortcut specifies a MHD simulation using the unsplit staggered mesh hydro solver, if pure hydro mode is used with the USM solver add +pureHydro in the setup line. It is equivalent to:

--with-unit=physics/Hydro/HydroMain/unsplit/MHD_StaggeredMesh

--without-unit=physics/Hydro/HydroMain/split/MHD_8Wave

+pureHydro

This shortcut specifies using pure hydro mode, it is equivalent to:

physicsMode=hydro

+splitHydro

This shortcut specifies a simulation using a split hydro solver and is equivalent to:

--unit=physics/Hydro/HydroMain/split -without-unit=physics/Hydro/HydroMain/unsplit SplitDriver=True

+unsplitHydro

This shortcut specifies a simulation using the unsplit hydro solver and is equivalent to:

--with-unit=physics/Hydro/HydroMain/unsplit/Hydro_Unsplit

+uhd

This shortcut specifies a simulation using the unsplit hydro solver and is equivalent to:

--with-unit=physics/Hydro/HydroMain/unsplit/Hydro_Unsplit

+supportPPMUpwind

This shortcut specifies a simulation using a specific Hydro method that requires an increased number of guard cells, this may need to be combined with -nxb=... -nyb=... etc. where the specified blocksize is greater than or equal to 12 (==2*GUARDCELLS). It is equivalent to: SupportPpmUpwind=True

+cube64

This shortcut specifies a simulation with a block size of $64^{**}3$, it is equivalent to: -nxb=64 -nyb=64 -nzb=64

+cube32

This shortcut specifies a simulation with a block size of 32**3, it is equivalent to: -nxb=32 -nyb=32 -nzb=32

+cube16

This shortcut specifies a simulation with a block size of 16**3, it is equivalent to: -nxb=16 -nyb=16 -nzb=16

+ptio

This shortcut specifies a simulation using particles and IO for uniform grid, it is equivalent to: +ug -with-unit=Particles

+rnf

This shortcut is used for checking Flash-X with rectangular block sizes and non-fixed block size. It is equivalent to:

-3d -nxb=8 -nyb=16 -nzb=32 -nofbs +ug

+nofbs

This shortcut specifies a simulation using a uniform grid with a non-fixed block size. It is equivalent to:

-nofbs +ug parallelIO=True

+curvilinear

This shortcut specifies a simulation using curvilinear geometry. It is equivalent to:

-curvilinear

+cartesian

This shortcut specifies a simulation using cartesian geometry. It is equivalent to:

-geometry=cartesian

+spherical

This shortcut specifies a simulation using spherical geometry. It is equivalent to:

-geometry=spherical

+polar

This shortcut specifies a simulation using polar geometry. It is equivalent to:

-geometry=polar

+cylindrical

This shortcut specifies a simulation using cylindrical geometry. It is equivalent to:

-geometry=cylindrical

+ptdens

This shortcut specifies a simulation using passive particles initialized by density. It is equivalent to:

-without-unit=Particles/ParticlesInitialization/Lattice

-without-unit=Particles/ParticlesInitialization/WithDensity/CellMassBins

-unit=Particles/ParticlesMain

-unit=Particles/ParticlesInitialization/WithDensity

-particlemethods=TYPE=passive, INIT=With_Density

```
+npg
```

This shortcut specifies a simulation using NO PERMANENT GUARDCELLS mode in Paramesh 4. It is equivalent to:

npg=True

+mpole

This shortcut specifies a smilulation using multipole gravity, it is equivalent to:

-with-unit=physics/Gravity/GravityMain/Poisson/Multipole

+longrange

This shortcut specifies a simulation using long range active particles. It is equivalent to:

-with-unit=Particles/ParticlesMain/active/longRange/gravity/ParticleMesh

+gravPfftNofbs

This shortcut specifies a simulation using FFT based gravity solve on a uniform grid with no fixed block size. It is equivalent to:

 $\hbox{+ug +nofbs -with-unit=physics/Gravity/GravityMain/Poisson/Pfft}$

+gravMgrid

This shortcut specifies a simulation using a multigrid based gravity solve. It is equivalent to:

+pm40 -with-unit=physics/Gravity/GravityMain/Poisson/Multigrid

+gravMpole

This shortcut specifies a smilulation using multipole gravity, it is equivalent to:

-with-unit=physics/Gravity/GravityMain/Poisson/Multipole

+noDefaultMpole

This shortcut specifies a simulation *not* using the multipole based gravity solve. It is equivalent to:

-without-unit=Grid/GridSolvers/Multipole

+noMgrid

This shortcut specifies a simulation *not* using the multigrid based gravity solve. It is equivalent to:

-without-unit=physics/Gravity/GravityMain/Poisson/Multigrid

+newMpole

This shortcut specifies a simulation using the new multipole based gravity solve. It is equivalent to:

+noMgrid +noDefaultMpole +gravMpole -with-unit=Grid/GridSolvers/Multipole_new +pic

This shortcut specifies use of proper particle units to perform PIC (particle in cell) method. It is equivalent to:

+ug -unit=Grid/GridParticles/GridParticlesMove

-without-unit=Grid/GridParticles/GridParticlesMove/UG

 $-without-unit=\tt Grid/GridParticles/GridParticlesMove/UG/Directional$

Grid

This setup variable can be used to specify which gridding package to use in a simulation:

Name: Grid
Type: String

Values: PM4DEV, PM40, UG

ΙO

This setup variable can be used to specify which IO package to use in a simulation:

Name: IO
Type: String

Values: hdf5, pnetcdf, MPIHybrid, MPIDump, direct

parallelI0

This setup variable can be used to specify which type of IO strategy will be used. A "parallel" strategy will be used if the value is true, a "serial" strategy otherwise.

Name: parallelIO Type: Boolean Values: True, False

fixedBlockSize

This setup variable indicates whether or not a fixed block size is to be used. This variable should not be assigned explicitly on the command line. It defaults to True, and the setup options -nofbs and -fbs modify the value of this variable.

Name: fixedBlockSize

Type: Boolean Values: True, False

nDim

This setup variable gives the dimensionality of a simulation. This variable should not be set explicitly on the command line, it is automatically set by the setup options -1d, -2d, and -3d.

Name: nDim Type: integer Values: 1,2,3

GridIndexOrder

This setup variable indicates whether the -index-reorder setup option is in effect. This variable should not be assigned explicitly on the command line.

Name: GridIndexOrder

Type: Boolean Values: True, False

nxb

This setup variable gives the number of zones in a block in the X direction. This variable should not be assigned explicitly on the command line, it is automatically set by the setup option <code>-nxb</code>.

Name: nxb Type: integer

nyb

This setup variable gives the number of zones in a block in the Y direction. This variable should not be assigned explicitly on the command line, it is automatically set by the setup option -nyb.

Name: nyb Type: integer

nzb

This setup variable gives the number of zones in a block in the Z direction. This variable should not be assigned explicitly on the command line, it is automatically set by the setup option <code>-nzb</code>.

Name: nzb Type: integer

maxBlocks

This setup variable gives the maximum number of blocks per processor. This variable should not be assigned explicitly on the command line, it is automatically set by the setup option -maxblocks.

Name: maxBlocks Type: integer

ParameshLibraryMode

If true, the setup script will generate file amr_runtime_parameters from template amr_runtime_parameters.tpl found in either the object directory (preferred) or the setup script (bin) directory. Selects whether Paramesh4 should be compiled in LIBRARY mode, i.e., with the preprocessor symbol LIBRARY defined.

Name: ParameshLibraryMode

Type: Boolean Values: True, False

PfftSolver

PfftSolver selects a PFFT solver variant when the hybrid (i.e., Multigrid with PFFT) Poisson

solver is used. Name: PfftSolver Type: String

Values: DirectSolver (default), HomBcTrigSolver, others (unsupported) if recognized in

source/Grid/GridSolvers/Multigrid/PfftTopLevelSolve/Config

SplitDriver

If True, a Split Driver implementation is requested.

Name: SplitDriver Type: Boolean

Mtmmmt

Automatically set True by +mtmmmt shortcut. When true, this option activates the MTMMMT EOS.

Name: Mtmmmt Type: Boolean

mgd_meshgroups

mgd meshgroups * meshCopyCount sets the MAXIMUM number of radiation groups that can be used in a simulation. The ACTUAL number of groups (which must be less than mgd meshgroups * meshCopyCount) is set by the rt mgdNumGroups runtime parameter.

Name: mgd_meshgroups

Type: Integer

species

This setup variable can be used as an alternative specifying species using the SPECIES Config file directive by listing the species in the setup command. Some units, like the Multispecies Opacity unit, will ONLY work when the species setup variable is set. This is because they use the species name to automatically create runtime paramters which include the species names.

Name: species

Type: String, comma seperated list of strings (e.g., species=air,sf6)

ed_maxPulses

Name: ed_maxPulses

Type: integer

Remark: Maximum number of laser pulses (defaults to 5)

ed_maxBeams

Name: ed_maxBeams
Type: integer

Remark: Maximum number of laser beams (defaults to 6)

threadHydroBlockList

This is used to turn on block list OPENMP threading of hydro routines.

Name: threadHydroBlockList

Type: Boolean
Values: True, False
threadMpoleBlockList

This is used to turn on block list OPENMP threading of the multipole routine.

Name: threadMpoleBlockList

Type: Boolean Values: True, False

threadRayTrace

This is used to turn on block list OPENMP threading of Enery Deposition source term routines.

Name: threadRayTrace

Type: Boolean Values: True, False threadHydroWithinBlock

This is used to turn on within block OPENMP threading of hydro routines.

Name: threadHydroWithinBlock

Type: Boolean
Values: True, False
threadEosWithinBlock

This is used to turn on within block OPENMP threading of Eos routines.

Name: threadEosWithinBlock

Type: Boolean
Values: True, False
threadMpoleWithinBlock

This is used to turn on within block OPENMP threading of then multipole routine.

Name: threadMpoleWithinBlock

Type: Boolean Values: True, False

4.3 Using Shortcuts

Apart from the various setup options the setup script also allows you to use shortcuts for frequently used combinations of options. For example, instead of typing in

```
./setup -a Sod -with-unit=Grid/GridMain/UG
you can just type
./setup -a Sod +ug
```

The +ug or any setup option starting with a '+' is considered as a shortcut. By default, setup looks at bin/setup_shortcuts.txt for a list of declared shortcuts. You can also specify a ":" delimited list of files in the environment variable SETUP_SHORTCUTS and setup will read all the files specified (and ignore those which don't exist) for shortcut declarations. See ?? for an example file.

The shortcuts are replaced by their expansions in place, so options which come after the shortcut override (or conflict with) options implied by the shortcut. A shortcut can also refer to other shortcuts as long as there are no cyclic references.

The "default" shortcut is special. setup always prepends +default to its command line thus making ./setup -a Sod equivalent to ./setup +default -a Sod. Thus changing the default IO to "hdf5/parallel", is as simple as changing the definition of the "default" shortcut.

Some of the more commonly used shortcuts are described below:

```
# comment line
# each line is of the form # shortcut:arg1:arg2:...:
# These shortcuts can refer to each other.

default:--with-library=mpi:-unit=IO/IOMain:-gridinterpolation=monotonic

# io choices
noio:--without-unit=IO/IOMain:
io:--with-unit=IO/IOMain:
# Choice of Grid
ug:-unit=Grid/GridMain/UG:
pm2:-unit=Grid/GridMain/paramesh/Paramesh2:
pm40:-unit=Grid/GridMain/paramesh/paramesh4/Paramesh4.0:
pm4dev:-unit=Grid/GridMain/paramesh/paramesh4/Paramesh4dev:
# frequently used geometries
cube64:-nxb=64:-nzb=64:-nzb=64:
```

Figure 4.2: A sample setup_shortcuts.txt file

Table 4.5: Shortcuts for often-used options

Shortcut	Description
+cartesian	use cartesian geometry
+cylindrical	use cylindrical geometry
+noio	omit IO
+nolog	omit logging
+pm4dev	use the PARAMESH4DEV grid
+polar	use polar geometry
+spherical	use spherical geometry
+ug	use the uniform grid in a fixed block size mode
+nofbs	use the uniform grid in a non-fixed block size mode
+usm	use the Unsplit Staggered Mesh MHD solver
+8wave	use the 8-wave MHD solver
+splitHydro	use a split Hydro solver

Table 4.6: Shortcuts for HEDP options

Shortcut	Description
+mtmmmt	Use the 3-T, multimaterial, multitype EOS
+uhd3t	Use the 3-T version of Unsplit Hydro
+usm3t	Use the 3-T version of Unsplit Staggered Mesh MHD
+mgd	Use Multigroup Radiation Diffusion and Opacities
+laser	Use the Laser Ray Trace package

4.4 Setup Variables and Preprocessing Config Files

setup allows you to assign values to "Setup Variables". These variables can be string-valued, integer-valued, or boolean. A setup call like

```
./setup -a Sod Foo=Bar Baz=True
```

sets the variable "Foo" to string "Bar" and "Baz" to boolean True³. setup can conditionally include and exclude parts of the Config file it reads based on the values of these variables. For example, the IO/IOMain/hdf5/Config file contains

```
DEFAULT serial

USESETUPVARS parallelIO

IF parallelIO

DEFAULT parallel
ENDIF
```

The code sets IO to its default value of "serial" and then resets it to "parallel" if the setup variable "parallelIO" is True. The USESETUPVARS keyword in the Config file instructs setup that the specified variables must be defined; undefined variables will be set to the empty string.

Through judicious use of setup variables, the user can ensure that specific implementations are included or the simulation is properly configured. For example, the setup line ./setup -a Sod +ug expands to ./setup -a Sod -unit=Grid/GridMain/ Grid=UG. The relevant part of the Grid/GridMain/Config file is given below:

```
# Requires use of the Grid SetupVariable
USESETUPVARS Grid

DEFAULT paramesh

IF Grid=='UG'
    DEFAULT UG
ENDIF
IF Grid=='PM2'
    DEFAULT paramesh/Paramesh2
ENDIF
```

The Grid/GridMain/Config file defaults to choosing PARAMESH. But when the setup variable Grid is set to "UG" through the shortcut +ug, the default implementation is set to "UG". The same technique is used to ensure that the right IO unit is automatically included.

See bin/Readme.SetupVars for an exhaustive list of Setup Variables which are used in the various Config files. For example the setup variable nDim can be test to ensure that a simulation is configured with the appropriate dimensionality (see for example Simulation/SimulationMain/unitTest/Eos/Config).

³ All non-integral values not equal to True/False/Yes/No/On/Off are considered to be string values

4.5 Config Files

Information about unit dependencies, default sub-units, runtime parameter definitions, library requirements, and physical variables, etc. is contained in plain text files named Config in the different unit directories. These are parsed by setup when configuring the source tree and are used to create the code needed to register unit variables, to implement the runtime parameters, to choose specific sub-units when only a generic unit has been specified, to prevent mutually exclusive units from being included together, and to flag problems when dependencies are not resolved by some included unit. Some of the Config files contain additional information about unit interrelationships. As mentioned earlier, setup starts from the Config file in the Simulation directory of the problem being built.

4.5.1 Configuration file syntax

Configuration files come in two syntactic flavors: static text and python. In static mode, configuration directives are listed as lines in a plain text file. This mode is the most readable and intuitive of the two, but it lacks flexibility. The python mode has been introduced to circumvent this inflexibility by allowing the configuration file author to specify the configuration directives as a function of the setup variables with a python procedure. This allows the content of each directive and the number of directives in total to be amenable to general programming.

The rule the setup script uses for deciding which flavor of configuration file it's dealing with is simple. Python configuration files have as their first line ##python:genLines. If the first line does not match this string, then static mode is assumed and each line of the file is interpreted verbatim as a directive.

If python mode is triggered, then the entire file is considered as valid python source code (as if it were a .py). From this python code, a function of the form def genLines(setupvars) is located and executed to generate the configuration directives as an array (or any iterable collection) of strings. The sole argument to genLines is a dictionary that maps setup variable names to their corresponding string values.

As an example, here is a configuration file in python mode that registers runtime parameters named indexed parameter x where x ranges from 1 to NP and NP is a setup line variable.

```
##python:genLines

# We define genLines as a generator with the very friendly "yield" syntax.

# Alternatively, we could have genLines return an array of strings or even
# one huge multiline string.
def genLines(setupvars):
    # emit some directives that dont depend on any setup variables
    yield """

REQUIRES Driver
REQUIRES physics/Hydro
REQUIRES physics/Eos
"""

# read a setup variable value from the dictionary
    np = int(setupvars("NP")) # must be converted from a string
# loop from 0 to np-1
    for x in xrange(np):
        yield "PARAMETER indexed_parameter_\%d REAL 0." \% (x+1)
```

When setting up a problem with NP=5 on the setup command line, the following directives will be processed:

```
REQUIRES Driver
REQUIRES physics/Hydro
```

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```
REQUIRES physics/Eos

PARAMETER indexed_parameter_1 REAL 0.

PARAMETER indexed_parameter_2 REAL 0.

PARAMETER indexed_parameter_3 REAL 0.

PARAMETER indexed_parameter_4 REAL 0.

PARAMETER indexed_parameter_5 REAL 0.
```

4.5.2 Configuration directives

The syntax of the configuration directives is described here. Arbitrarily many spaces and/or tabs may be used, but all keywords must be in uppercase. Lines not matching an admissible pattern will raise an error when running setup.

• # comment

A comment. Can appear as a separate line or at the end of a line.

• DEFAULT sub-unit

Every unit and sub-unit designates one implementation to be the "default", as defined by the keyword DEFAULT in its Config file. If no specific implementation of the unit or its sub-units is selected by the application, the designated default implementation gets included. For example, the Config file for the EosMain specifies Gamma as the default. If no specific implementation is explicitly included (i.e., INCLUDE physics/Eos/EosMain/Multigamma), then this command instructs setup to include the Gamma implementation, as though INCLUDE physics/Eos/EosMain/Gamma had been placed in the Units file.

ullet EXCLUSIVE implementation...

Specifies a list of implementations that cannot be included together. If no EXCLUSIVE instruction is given, it is perfectly legal to simultaneously include more than one implementation in the code. Using "EXCLUSIVE *" means that at most one implementation can be included.

- CONFLICTS unit1[/sub-unit[/implementation...]] ...

 Specifies that the current unit, sub-unit, or specific implementation is not compatible with the list of units, sub-units or other implementations that follows. setup issues an error if the user attempts a conflicting unit configuration.
- REQUIRES unit[/sub-unit[/implementation...]] [OR unit[/sub-unit...]]...

 Specifies a unit requirement. Unit requirements can be general, without asking for a specific implementation, so that unit dependencies are not tied to particular algorithms. For example, the statement REQUIRES physics/Eos in a unit's Config file indicates to setup that the physics/Eos unit is needed, but no particular equation of state is specified. As long as an Eos implementation is included, the dependency will be satisfied. More specific dependencies can be indicated by explicitly asking for an implementation. For example, if there are multiple species in a simulation, the Multigamma equation of state is the only valid option. To ask for it explicitly, use REQUIRES physics/Eos/EosMain/Multigamma. Giving a complete set of unit requirements is helpful, because setup uses them to generate the units file when invoked with the -auto option.
- REQUESTS unit[/sub-unit[/implementation...]]
 Requests that a unit be added to the Simulation. All requests are upgraded to a "REQUIRES" if they are not negated by a "-without-unit" option from the command line. If negated, the REQUEST is ignored. This can be used to turn off profilers and other "optional" units which are included by default.
- SUGGEST unitname unitname ...

Unlike REQUIRES, this keyword suggests that the current unit be used along with one of the specified units. The setup script will print details of the suggestions which have been ignored. This is useful

in catching inadvertently omitted units before the run starts, thus avoiding a waste of computing resources.

• PARAMETER name type [CONSTANT] default [range-spec]

Specifies a runtime parameter. Parameter names are unique up to 20 characters and may not contain spaces. Admissible types include REAL, INTEGER, STRING, and BOOLEAN. Default values for REAL and INTEGER parameters must be valid numbers, or the compilation will fail. Default STRING values must be enclosed in double quotes ("). Default BOOLEAN values must be .true. or .false. to avoid compilation errors. Once defined, runtime parameters are available to the entire code. Optionally, any parameter may be specified with the CONSTANT attribute (e.g., PARAMETER foo REAL CONSTANT 2.2). If a user attempts to set a constant parameter via the runtime parameter file, an error will occur.

The range specification is optional and can be used to specify valid ranges for the parameters. The range specification is allowed only for REAL, INTEGER, STRING variables and must be enclosed in '[]'.

For a STRING variable, the range specification is a comma-separated list of strings (enclosed in quotes). For a INTEGER, REAL variable, the range specification is a comma-separated list of (closed) intervals specified by min ... max, where min and max are the end points of the interval. If min or max is omitted, it is assumed to be $-\infty$ and $+\infty$ respectively. Finally val is a shortcut for val ... val. For example

```
PARAMETER pres REAL 1.0 [ 0.1 ... 9.9, 25.0 ... ]
PARAMETER coords STRING "polar" ["polar", "cylindrical", "2d", "3d"]
```

indicates that **pres** is a REAL variable which is allowed to take values between 0.1 and 9.9 or above 25.0. Similarly **coords** is a string variable which can take one of the four specified values.

• D parameter-name comment

Any line in a Config file is considered a parameter comment line if it begins with the token D. The first token after the comment line is taken to be the parameter name. The remaining tokens are taken to be a description of the parameter's purpose. A token is delineated by one or more white spaces. For example,

D SOME_PARAMETER The purpose of this parameter is whatever

If the parameter comment requires additional lines, the & is used to indicate continuation lines. For example,

```
D SOME_PARAMETER The purpose of this parameter is whatever D \&\hspace{1cm} This is a second line of description
```

You can also use this to describe other variables, fluxes, species, etc. For example, to describe a species called "xyz", create a comment for the parameter "xyz_species". In general the name should be followed by an underscore and then by the lower case name of the keyword used to define the name.

Parameter comment lines are special because they are used by setup to build a formatted list of commented runtime parameters for a particular problem. This information is generated in the file setup_params in the object directory.

• VARIABLE name TYPE: vartype | [eosmap-spec]

Registers variable with the framework with name *name* and a variable typedefined by *vartype*. The setup script collects variables from all the included units, and creates a comprehensive list with no duplications. It then assigns defined constants to each variable and calculates the amount of storage required in the data structures for storing these variables. The defined constants and the calculated sizes are written to the file Simulation.h.

The possible types for *vartype* are as follows:

- PER_VOLUME

This solution variable is represented in **conserved** form, *i.e.*, it represents the density of a conserved extensive quantity. The prime example is a variable directly representing mass density.

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Energy densities, momentum densities, and partial mass densities would be other examples (but these quantities are usually represented in PER_MASS form instead).

PER_MASS

This solution variable is represented in **mass-specific**form, *i.e.*, it represents quantities whose nature is extensive quantity per mass unit. Examples are specific energies, velocities of material (since they are equal to momentum per mass unit), and abundances or mass fractions (partial density divided by density).

- GENERIC

This is the default *vartype* and need not be specified. This type should be used for any variables that do not clearly belong to one of the previous two categories.

In the current version of the code, the TYPE attribute is only used to determine which variables should be converted to conservative form for certain Grid operations that may require interpolation (i.e., prolongation, guardcell filling, and restriction) when one of the runtime parameters [[rpi reference]] or [[rpi reference]] is set true. Only variables of type PER_MASS are converted: values are multiplied cell-by-cell with the value of the "dens" variable, and potential interpolation results are converted back by cell-by-cell division by "dens" values after interpolation.

Note that therefore

- variable types are irrelevant for uniform grids,
- variable types are irrelevant if neither [[rpi reference]] nor [[rpi reference]] is true, and
- variable types (and conversion to and from conserved form) only take effect if a

```
VARIABLE dens ... exists.
```

An eosmap-spec has the syntax EOSMAP: eos-role | ([EOSMAPIN: eos-role] [EOSMAPOUT: eos-role]), where eos-role stands for a role as defined in Eos_map.h. These roles are used within implementations of the [[api reference]] interface, via the subroutines [[api reference]] and [[api reference]], to map variables from Grid data structures to the eosData array that [[api reference]] understands, and back. For example,

```
VARIABLE eint TYPE: PER_MASS EOSMAPIN: EINT
```

means that within Eos_wrapped, the EINT_VAR component of unk will be treated as the grid variable in the "internal energy" role for the purpose of constructing input to [[api reference]], and

```
VARIABLE gamc EOSMAPOUT: GAMC
```

means that within Eos_wrapped, the GAMC_VAR component of unk will be treated as the grid variable in the EOSMAP_GAMC role for the purpose of returning results from calling [[api reference]] to the grid. The specification

```
VARIABLE pres EOSMAP: PRES
```

has the same effect as

```
VARIABLE pres EOSMAPIN: PRES EOSMAPOUT: PRES
```

Note that not all roles defined in Eos_map.h are necessarily meaningful or actually used in a given Eos implementation. An *eosmap-spec* for a VARIABLE is only used in an [[api reference]] invocation when the optional gridDataStruct argument is absent or has a value of CENTER.

• FACEVAR name [eosmap-spec]

This keyword has the same meaning for face-centered variables, that VARIABLE does for cell-centered variables. It allocates space in the grid data structure that contains face-centered physical variables for "name". See ?? for more information

For *eosmap-spec*, see above under VARIABLE. An *eosmap-spec* for FACEVAR is only used when [[api reference]] is called with an optional gridDataStruct argument of FACEX, FACEY, or FACEZ.

• FLUX name

Registers flux variable *name* with the framework. When using an adaptive mesh, flux conservation is needed at fine-coarse boundaries. PARAMESH uses a data structure for this purpose, the flux variables provide indices into that data structure. See ?? for more information.

• SCRATCHCENTERVAR name [eosmap-spec]

This keyword is used in connection with the grid scope scratch space for cell-centered data supported by Flash-X. It allows the user to ask for scratch space with "name". The scratch variables do not participate in the process of guardcell filling, and their values become invalid after a grid refinement step. While users can define scratch variables to be written to the plotfiles, they are not by default written to checkpoint files. Note this feature wasn't available in Flash-X2. See ?? for more information.

• SCRATCHFACEVAR name [eosmap-spec]

This keyword is used in connection with the grid scope scratch space for face-centered data, it is identical in every other respect to SCRATCHCENTERVAR.

• SCRATCHVAR name [eosmap-spec]

This keyword is used for specifying instances of general purpose grid scope scratch space. The same space can support cell-centered as well as face-centered data. Like other scratch data structures, the variables in this data structure can also be asked with "name" and do not participate in guardcell filling.

For *eosmap-spec*, see above under VARIABLE. An *eosmap-spec* for SCRATCHVAR is only used when [[api reference]] is called with an optional gridDataStruct argument of SCRATCH.

• MASS_SCALAR name [RENORM: group-name] [eosmap-spec]

If a quantity is defined with keyword MASS_SCALAR, space is created for it in the grid "unk" data structure. It is treated like any other variable by PARAMESH, but the hydrodynamic unit treats it differently. It is advected, but other physical characteristics don't apply to it. If the optional "RENORM" is given, this mass-scalar will be added to the renormalization group of the accompanying group name. The hydrodynamic solver will renormalize all mass-scalars in a given group, ensuring that all variables in that group will sum to 1 within an individual cell. See ??

For *eosmap-spec*, see above under VARIABLE. An *eosmap-spec* for a MASS_SCALAR may be used in an [[api reference]] invocation when the optional gridDataStruct argument is absent or has a value of CENTER.

Avoid Confusion!

It is inadvisable to name variables, species, and mass scalars with the same prefix, as post-processing routines have difficulty deciphering the type of data from the output files. For example, don't create a variable "temp" to hold temperature and a mass scalar "temp" indicating a temporary variable. Although the Simulation.h file can distinguish between these two types of variables, many plotting routines cannot.

 $\bullet \ \ {\tt PARTICLETYPE} \ particle-type \ \ {\tt INITMETHOD} \ initialization-method \ \ {\tt MAPMETHOD} \ map-method \ \ {\tt ADVMETHOD} \ time-advance-method$

This keyword associates a particle type with mapping and initialization sub-units of Particles unit

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to operate on this particle type during the simulation. Here, map-method describes the method used to map the particle properties to and from the mesh (see ??), initialization-method describes the method used to distribute the particles at initialization, and time-advance-method describes the method used to advance the associated particle type in time (see ??, and in general ??). This keyword has been introduced to facilitate inclusion of multiple particle types in the same simulation. It imposes certain requirements on the use of the ParticlesMapping and ParticlesInitialization subunits. Particles (of any type, whether called passive or anything else) do not have default methods for initialization, mapping, or time integration, so a PARTICLETYPE directive in a Config file (or an equivalent -particlemethods= setup option, see ??) is the only way to specify the appropriate implementations of the Particles subunits to be used. The declaration should be accompanied by appropriate "RE-QUESTS" or "REQUIRES" directives to specify the paths of the appropriate subunit implementation directories to be included. For clarity, our technique has been to include this information in the simulation directory Config files only. All the currently available mapping and initialization methods have a corresponding identifier in the form of preprocessor definition in Particles.h. The user may select any particle-type name, but the map-method, initialization-method and time-advance-method must correspond to existing identifiers defined in Particles.h. This is necessary to navigate the data structure that stores the particle type and its associated mapping and initialization methods. Users desirous of adding new methods for mapping or initialization should also update the Particles.h file with additional identifiers and their preprocessor definitions. Note, it is possible to use the same methods for different particle types, but each particle type name must only appear once. Finally, the Simulations Config file is also expected to request appropriate implementations of mapping and initialization subunits using the keyword REQUESTS, since the corresponding Config files do not specify a default implementation to include. For example, to include passive particle types with Quadratic mapping, Lattice initialization, and Euler for advancing in time the following code segment should appear in the Config file of the Simulations directory.

PARTICLETYPE passive INITMETHOD lattice MAPMETHOD quadratic ADVMETHOD Euler REQUIRES Particles/ParticlesMain
REQUESTS Particles/ParticlesMain/passive/Euler
REQUESTS Particles/ParticlesMapping/Quadratic
REQUESTS Particles/ParticlesInitialization/Lattice

• PARTICLEPROP name type

This keyword indicates that the particles data structure will allocate space for a sub-variable "NAME_-PART_PROP." For example if the Config file contains

PARTICLEPROP dens

then the code can directly access this property as

particles(DENS_PART_PROP,1:localNumParticles) = densInitial

type may be REAL or INT, however INT is presently unused. See ?? for more information and examples.

• PARTICLEMAP TO partname FROM vartype varname

This keyword maps the value of the particle property partname to the variable varname. vartype can take the values VARIABLE, MASS_SCALAR, SPECIES, FACEX, FACEY, FACEZ, or one of SCRATCH types (SCRATCHVAR/ SCRATCHCENTERVAR, SCRATCHFACEXVAR. SCRATCHFACEXVAR) These maps are used to generate Simulation_mapParticlesVar, which takes the particle property partname and returns varname and vartype. For example, to have a particle property tracing density:

PARTICLEPROP dens REAL PARTICLEMAP TO dens FROM VARIABLE dens

or, in a more advanced case, particle properties tracing some face-valued function Mag:

```
PARTICLEPROP Mag_x REAL
PARTICLEPROP Mag_y REAL
PARTICLEPROP Mag_z REAL
PARTICLEMAP TO Mag_x FROM FACEX Mag
PARTICLEMAP TO Mag_y FROM FACEY Mag
PARTICLEMAP TO Mag_z FROM FACEZ Mag
```

Additional information on creating Config files for particles is obtained in ??.

• SPECIES name [TO number of ions]

An application that uses multiple species uses this keyword to define them. See ?? for more information. The user may also specify an optional number of ions for each element, *name*. For example, SPECIES o TO 8 creates 9 spaces in unk for Oxygen, that is, a single space for Oxygen and 8 spaces for each of its ions. This is relevant to simulations using the ionize unit. (Omitting the optional TO specifier is equivalent to specifying TO 0).

• DATAFILES wildcard

Declares that all files matching the given wildcard in the unit directory should be copied over to the object directory. For example,

```
DATAFILES *.dat
```

will copy all the ".dat" files to the object directory.

• KERNEL /subdir/

Declares that all subdirectories must be recursively included. This usually marks the end of the high level architecture of a unit. Directories below it may be third party software or a highly optimized solver, and are therefore not required to conform to Flash-X architecture.

Without a *subdir*, the current directory (*i.e.*, the one containing the Config file with the KERNEL keyword) is marked as a kernel directory, so code from all its subdirectories (with the exception of subdirectories whose name begins with a dot) is included. When a *subdir* is given, then that subdirectory must exist, and it is treated as a kernel directory in the same way.

Note that currently the setup script can process only one KERNEL directive per Config file.

ullet LIBRARY name

Specifies a library requirement. Different Flash-X units require different libraries, and they must inform setup so it can link the libraries into the executable. Some valid library names are HDF5, MPI. Support for external libraries can be added by modifying the site-specific Makefile.h files to include appropriate Makefile macros. It is possible to use internal libraries, as well as switch libraries at setup time. To use these features, see

• LINKIF filename unitname

Specifies that the file filename should be used only when the unit unitname is included. This keyword allows a unit to have multiple implementations of any part of its functionality, even down to the kernel level, without the necessity of creating children for every alternative. This is especially useful in Simulation setups where users may want to use different implementations of specific functions based upon the units included. For instance, a user may wish to supply his/her own implementation of Grid_markRefineDerefine.F90, instead of using the default one provided by Flash-X. However, this function is aware of the internal workings of Grid, and has different implementations for different grid packages. The user could therefore specify different versions of his/her own file that are intended for use with the different grids. For example, adding

```
LINKIF Grid_markRefineDerefine.F90.ug Grid/GridMain/UG LINKIF Grid_markRefineDerefine.F90.pmesh Grid/GridMain/paramesh
```

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to the Config file ensures that if the application is built with UG, the file

Grid_markRefineDerefine.F90.ug will be linked in as Grid_markRefineDerefine.F90, whereas if it is built with Paramesh2 or Paramesh4.0 or Paramesh4dev, then the file Grid_markRefineDerefine.F90.pmesh will be linked in as Grid_markRefineDerefine.F90. Alternatively, the user may want to provide only one implementation specific to, say, PARAMESH. In this case, adding

```
LINKIF Grid_markRefineDerefine.F90 Grid/GridMain/paramesh
```

to the Config file ensures that the user-supplied file is included when using PARAMESH (either version), while the default Flash-X file is included when using UG.

• PPDEFINE $sym1 \ sym2 \dots$

Instructs setup to add the PreProcessor symbols SYM1 and SYM2 to the generated Simulation.h. Here SYM1 is sym1 converted to uppercase. These pre-process symbols can be used in the code to distinguish between which units have been used in an application. For example, a Fortran subroutine could include

```
#ifdef Flash-X_GRID_UG
   ug specific code
#endif

#ifdef Flash-X_GRID_PARAMESH3OR4
   pm3+ specific code
#endif
```

By convention, many preprocessor symbols defined in Config files included in the Flash-X code distribution start with the prefix "Flash-X.".

• USESETUPVARS var1, var2, ...

This tells setup that the specified "Setup Variables" are being used in this Config file. The variables initialize to an empty string if no values are specified for them. Note that commas are required if listing several variables.

• CHILDORDER child1 child2 ...

When setup links several implementations of the same function, it ensures that implementations of children override that of the parent. Its method is to lexicographically sort all the names and allow implementations occurring later to override those occurring earlier. This means that if two siblings implement the same code, the names of the siblings determine which implementation wins. Although it is very rare for two siblings to implement the same function, it does occur. This keyword permits the Config file to override the lexicographic order by one preferred by the user. Lexicographic ordering will prevail as usual when deciding among implementations that are not explicitly listed.

• GUARDCELLS num

Allows an application to choose the stencil size for updating grid points. The stencil determines the number of guardcells needed. The PPM algorithm requires 4 guardcells, hence that is the default value. If an application specifies a smaller value, it will probably not be able to use the default monotonic AMR Grid interpolation; see the -gridinterpolation setup flag for additional information.

• SETUPERROR error message

This causes setup to abort with the specified error message. This is usually used only inside a conditional IF/ENDIF block (see below).

• IF, ELSEIF, ELSE, ENDIF

A conditional block is of the following form:

```
IF cond ... ELSEIF cond
```

ELSE ... ENDIF

where the ELSEIF and ELSE blocks are optional. There is no limit on the number of ELSEIF blocks. "..." is any sequence of valid Config file syntax. The conditional blocks may be nested. "cond" is any boolean valued Python expression using the setup variables specified in the USESETUPVARS.

• NONREP unktype name localmax globalparam ioformat

Declares an array of UNK variables that will be partitioned across the replicated meshes. Using various preprocessor macros in Simulation.h each copy of the mesh can determine at runtime its own subset of indexes into this global array. This allows an easy form of parallelism where regular "replicated" mesh variables are computed redundantly across processors, but the variables in the "non-replicated" array are computed in parallel.

- unktype: must be either MASS_SCALAR or VARIABLE
- name: the name of this variable array. It is suggested that it be all capital letters, and must conform to what the C preprocessor will consider as a valid symbol for use in a #define statement.
- localmax: a positive integer specifying the maximum number of elements from the global variable
 array a mesh can hold. This is the actual number of UNK variables that are allocated on each
 processor, though not all of them will necessarily be used.
- global param: the name of a runtime parameter which dictates the size of this global array of variables.
- ioformat: a string representing how the elements of the array will be named when written to the output files. The question mark character? is used as a placeholder for the digits of the array index. As an example, the format string x??? will generate the dataset names x001, x002, x003, etc. This string must be no more than four characters in length.

The number of meshes is dictated by the runtime parameter meshCopyCount. The following constraint must be satisfied or Flash-X will fail at runtime:

```
globalparam \leq meshCopyCount * localmax
```

The reason for this restriction is that localmax is the maximum number of array elements a mesh can be responsible for, and meshCopyCount is the number of meshes, so their product bounds the size of the array.

Example:

Config file:

```
NONREP MASS_SCALAR A 4 numA a???
NONREP MASS_SCALAR B 5 numB b???
```

flash.par file:

```
meshCopyCount = 3
numA = 11
numB = 15
```

In this case two non-replicated mass-scalar arrays are defined, A and B. Their lengths are specified by the runtime parameters numA and numB respectively. numB is set to its maximum value of 5*meshCopyCount = 15, but numA is one less than its maximum value of 4*meshCopyCount = 12 so at runtime one of the meshes will not have all of its UNK variables in use. The dataset names generated by IO will take the form a001 ...a011 and b001 ...b015.

The preprocessor macros defined in Simulation.h for these arrays will have the prefixes A_ and B_ respectively. For details about these macros and how they will distribute the array elements across the meshes see ??.

4.6 Creating a Site-specific Makefile

If setup does not find your hostname in the sites/ directory it picks a default Makefile based on the operating system. This Makefile is not always correct but can be used as a template to create a Makefile for your machine. To create a Makefile specific to your system follow these instructions.

- Create the directory sites/<hostname>, where <hostname> is the hostname of your machine.
- Start by copying os/<your os>/Makefile.h to sites/<hostname>
- Use bin/suggestMakefile.sh to help identify the locations of various libraries on your system. The script scans your system and displays the locations of some libraries. You must note the location of MPI library as well. If your compiler is actually an mpi-wrapper (e.g.mpif90), you must still define LIB_MPI in your site specific Makefile.h as the empty string.
- Edit sites/<hostname>/Makefile.h to provide the locations of various libraries on your system.
- Edit sites/<hostname>/Makefile.h to specify the FORTRAN and C compilers to be used.

Compilation warning

The Makefile.h *must* include a compiler flag to promote Fortran Reals to Double Precision. Flash-X performs all MPI communication of Fortran Reals using MPI_DOUBLE_PRECISION type, and assumes that Fortran Reals are interoperable with C doubles in the I/O unit.

4.7 Files Created During the setup Process

When setup is run it generates many files in the object directory. They fall into three major categories:

- (a) Files not required to build the Flash-X executable, but which contain useful information,
- (b) Generated F90 or C code, and
- (c) Makefiles required to compile the Flash-X executable.

4.7.1 Informational files

These files are generated before compilation by setup. Each of these files begins with the prefix setup_ for easy identification.

setup_call	contains the options with which setup was called and the com-
	mand line resulting after shortcut expansion
setup_libraries	contains the list of libraries and their arguments (if any) which
	was linked in to generate the executable
setup_units	contains the list of all units which were included in the current
	setup
$\mathtt{setup_defines}$	contains a list of all pre-process symbols passed to the compiler
	invocation directly
setup_flags	contains the exact compiler and linker flags
$\mathtt{setup_params}$	contains the list of runtime parameters defined in the Config files
	processed by setup
setup_vars	contains the list of variables, fluxes, species, particle properties,
	and mass scalars used in the current setup, together with their
	descriptions.

4.7.2 Code generated by the setup call

These routines are generated by the setup call and provide simulation-specific code.

setup_buildstamp.F90	contains code for the subroutine setup_buildstamp which
	returns the setup and build time as well as code for
	setup_systemInfo which returns the uname of the system
	used to setup the problem
setup_buildstats.c	contains code which returns build statistics including the actual setup call as well as the compiler flags used for the build
setup_getFlashUnits.F90	contains code to retrieve the number and list of flashUnits used to compile code
setup_flashRelease.F90	contains code to retrieve the version of Flash-X used for the build
Simulation.h	contains simulation specific preprocessor macros, which change based upon setup unlike constants.h. It is described in ??
[[api reference]].F90	contains code to map an index described in Simulation.h to a string described in the Config file.
[[api reference]].F90	contains code to map a string described in the Config file to an integer index described in the Simulation.h file.
[[api reference]].F90	contains a mapping between particle properties and grid variables. Only generated when particles are included in a simulation.
[[api reference]].F90	contains code to make a data structure with information about the mapping and initialization method for each type of particle. Only generated when particles are included in a simulation.

4.7.3 Makefiles generated by setup

Apart from the master Makefile, setup generates a makefile for each unit, which is "included" in the master Makefile. This is true even if the unit is not included in the application. These unit makefiles are named Makefile. Unit and are a concatenation of all the Makefiles found in unit hierarchy processed by setup.

For example, if an application uses Grid/GridMain/paramesh/paramesh4/Paramesh4.0, the file Makefile.Grid will be a concatenation of the Makefiles found in

- Grid,
- Grid/GridMain,

- Grid/GridMain/paramesh,
- Grid/GridMain/paramesh/paramesh4, and
- Grid/GridMain/paramesh/paramesh4/Paramesh4.0

As another example, if an application does not use PhysicalConstants, then Makefile.PhysicalConstants is just the contents of PhysicalConstants/Makefile at the API level.

Since the order of concatenation is arbitrary, the behavior of the Makefiles should not depend on the order in which they have been concatenated. The makefiles inside the units contain lines of the form:

```
Unit += file1.o file2.o ...
```

where Unit is the name of the unit, which was Grid in the example above. Dependency on data modules files need not be specified since the setup process determines this requirement automatically.

4.8 Setup a hybrid MPI+OpenMP Flash-X application

There is the experimental inclusion of Flash-X multithreading with OpenMP in the FLASH-X beta release. The units which have support for multithreading are split hydrodynamics ??, unsplit hydrodynamics ??, Gamma law and multigamma EOS ??, Helmholtz EOS ??, Multipole Poisson solver (improved version (support for 2D cylindrical and 3D cartesian)) ?? and energy deposition ??.

The Flash-X multithreading requires a MPI-2 installation built with thread support (building with an MPI-1 installation or an MPI-2 installation without thread support is possible but strongly discouraged). The Flash-X application requests the thread support level MPI_THREAD_SERIALIZED to ensure that the MPI library is thread-safe and that any OpenMP thread can call MPI functions safely. You should also make sure that your compiler provides a version of OpenMP which is compliant with at least the OpenMP 2.5 (200505) standard (older versions may also work but I have not checked).

In order to make use of the multithreaded code you must setup your application with one of the setup variables threadBlockList, threadWithinBlock or threadRayTrace equal to True, e.g.

```
./setup Sedov -auto threadBlockList=True
./setup Sedov -auto threadBlockList=True +mpi1 (compatible with MPI-1 - unsafe!)
```

When you do this the setup script will insert USEOPENMP = 1 instead of USEOPENMP = 0 in the generated Makefile. If it is equal to 1 the Makefile will prepend an OpenMP variable to the FFLAGS, CFLAGS, LFLAGS variables.

Makefile.h variables

In general you should not define FLAGS, CFLAGS and LFLAGS in your Makefile.h. It is much better to define FFLAGS_OPT, FFLAGS_TEST, FFLAGS_DEBUG, CFLAGS_OPT, CFLAGS_TEST, CFLAGS_DEBUG, LFLAGS_OPT, LFLAGS_TEST and LFLAGS_DEBUG in your Makefile.h. The setup script will then initialize the FFLAGS, CFLAGS and LFLAGS variables in the Makefile appropriately for an optimized, test or debug build.

The OpenMP variables should be defined in your Makefile.h and contain a compiler flag to recognize OpenMP directives. In most cases it is sufficient to define a single variable named OPENMP, but you may encounter special situations when you need to define OPENMP_FORTRAN, OPENMP_C and OPENMP_LINK. If you want to build Flash-X with the GNU Fortran compiler gfortran and the GNU C compiler gcc then your Makefile.h should contain

```
OPENMP = -fopenmp
```

If you want to do something more complicated like build Flash-X with the Lahey Fortran compiler 1f90 and the GNU C compiler gcc then your Makefile.h should contain

```
OPENMP_FORTRAN = --openmp -Kpureomp

OPENMP_C = -fopenmp

OPENMP_LINK = --openmp -Kpureomp
```

When you run the hybrid Flash-X application it will print the level of thread support provided by the MPI library and the number of OpenMP threads in each parallel region

```
[Driver_initParallel]: Called MPI_Init_thread - requested level 2, given level 2 [Driver_initParallel]: Number of OpenMP threads in each parallel region 4
```

Note that the Flash-X application will still run if the MPI library does not provide the requested level of thread support, but will print a warning message alerting you to an unsafe level of MPI thread support. There is no guarantee that the program will work! I strongly recommend that you stop using this Flash-X application - you should build a MPI-2 library with thread support and then rebuild Flash-X.

We record extra version and runtime information in the Flash-X log file for a threaded application. Table ?? shows log file entries from a threaded Flash-X application along with example safe and unsafe values. All cells colored red show unsafe values.

Log file stamp	safe	unsafe (1)	unsafe (2)	unsafe (3)
Number of MPI tasks:	1	1	1	1
MPI version:	2	1	2	2
MPI subversion:	2	2	1	2
MPI thread support:	Т	F	F	F
OpenMP threads/MPI task:	2	2	2	2
OpenMP version:	200805	200505	200505	200805
Is "_OPENMP" macro defined:	T	Т	Т	F

Table 4.7: Log file entries showing safe and unsafe threaded Flash-X applications

The Flash-X applications in Table ?? are unsafe because

- 1. we are using an MPI-1 implementation.
- 2. we are using an MPI-2 implementation which is not built with thread support the "MPI thread support in OpenMPI" Flash tip may help.
- 3. we are using a compiler that does not define the macro _OPENMP when it compiles source files with OpenMP support (see OpenMP standard). I have noticed that Absoft 64-bit Pro Fortran 11.1.3 for Linux x86_64 does not define this macro. We use this macro in Driver_initParallel.F90 to conditionally initialize MPI with MPI_Init_thread. If you find that _OPENMP is not defined you should define it in your Makefile.h in a manner similar to the following:

```
OPENMP_FORTRAN = -openmp -D_OPENMP=200805
```

You should not setup a Flash-X application with both threadBlockList and threadWithinBlock equal to True - nested OpenMP parallelism is not supported. For further information about Flash-X multithreaded applications please refer to Chapter ??.

Part III Driver Unit

Chapter 5

Driver Unit

The Driver unit controls the initialization and evolution of Flash-X simulations. In addition, at the highest level, the Driver unit organizes the interaction between units. Initialization can be from scratch or from a stored checkpoint file. For advancing the solution, the drivers can use either an operator-splitting technique adapted to directionally split physics operators like split Hydro (Split), or a more generic "Unsplit" implementation. The Driver unit also calls the IO unit at the end of every timestep to produce checkpoint files, plot files, or other output.

5.1 Driver Routines

The most important routines in the Driver API are those that initialize, evolve, and finalize the Flash-X program. The file Flash.F90 contains the main Flash-X program (equivalent to main() in C). The default top-level program of Flash-X, Simulation/Flash.F90, calls Driver routines in this order:

```
program Flash
  implicit none

call Driver_initParallel()
 call Driver_initFlash()
 call Driver_evolveFlash()
 call Driver_finalizeFlash ()
```

Therefore the no-operation stubs for these routines in the Driver source directory must be overridden by an implementation function in a unit implementation directory under the Driver or Simulation directory trees, in order for a simulation to perform any meaningful actions. The most commonly used implementations for most of these files are located in the Driver/DriverMain unit implementation directory, with a few specialized ones in either Driver/DriverMain/Split or Driver/DriverMain/Unsplit.

5.1.1 Driver_initFlash

end program Flash

The first of these routines is [[api reference]], which initializes the parallel environment for the simulation. New in Flash-X is an ability to replicate the mesh where more than one copy of the discretized mesh may exist with some overlapping and some non-overlapping variables. Because of this feature, the parallel environment differentiates between global and mesh communicators. All the necessary communicators, and the attendant meta-data is generated in this routine. Also because of this modification, runtime parameters such as iProcs, jProcs etc, which were under the control of the Grid unit in Flash-X, are now under the control of the Driver unit. Several new accessor interface allow other code units to query the driver unit for

this information. The [[api reference]], the next routine, in general calls the initialization routines in each of the units. If a unit is not included in a simulation, its stub (or empty) implementation is called. Having stub implementations is very useful in the Driver unit because it allows the user to avoid writing a new driver for each simulation. For a more detailed explanation of stub implementations please see ??. It is important to note that when individual units are being initialized, order is often very important and the order of initialization is different depending on whether the run is from scratch or being restarted from a checkpoint file.

5.1.2 Driver_evolveFlash

The next routine is [[api reference]] which controls the timestepping of the simulation, as well as the normal termination of Flash-X based on time. Driver_evolveFlash checks the parameters tmax, nend and zFinal to determine that the run should end, having reached a particular point in time, a certain number of steps, or a particular cosmological redshift, respectively. Likewise the initial simulation time, step number and cosmological redshift for a simulation can be set using the runtime parameters tmin, nbegin, and zInitial. This version of Flash-X includes versions of Driver_evolveFlash for directionally-split and unsplit staggered mesh operators.

5.1.2.1 Strang Split Evolution

The code in the Driver/DriverMain/Split unit implementation directory has been the default time update method earlier, and can still be be used for many setups that can be configured with Flash-X. The routine Driver_evolveFlash implements a Strang-split method of time advancement where each physics unit updates the solution data for two equal timesteps – thus the sequence of calls to physics and other units in each time step goes something like this: Hydro, diffusive terms, source terms, Particles, Gravity; Hydro, diffusive terms, source terms, Particles, Gravity, IO (for output), Grid (for grid changes). The hydrodynamics update routines take a "sweep order" argument since they must be directionally split to work with this driver. Here, the first call usually uses the ordering x - y - z, and the second call uses z - y - x. Each of the update routines is assumed to directly modify the solution variables. At the end of one loop of timestep advancement, the condition for updating the mesh refinement pattern is tested if the adaptive mesh is being used, and a refinement update is carried out if required.

5.1.2.2 Unsplit Evolution

The driver implementation in the Driver/DriverMain/Unsplit directory is the default since FLASH-X. It is required specifically for the two unsplit solvers: unsplit staggered mesh MHD solver (??) and the unsplit gas hydrodynamics solver (??). This implementation in general calls each of the physics routines only once per time step, and each call advances solution vectors by one timestep. At the end of one loop of timestep advancement, the condition for updating the adaptive mesh refinement pattern is tested and applied.

5.1.2.3 Super-Time-Stepping (STS)

A new timestepping method implemented in FLASH-X is a technique called Super-Time-Stepping (STS). The STS is a simple explicit method which is used to accelerate restrictive parabolic timestepping advancements ($\Delta t_{\rm CFL_para} \approx \Delta x^2$) by relaxing the CFL stability condition of parabolic equation system.

The STS has been proposed by Alexiades et al., (1996), and used in computational astrophysics and sciences recenly (see Mignone et al., 2007; O'Sullivan & Downes, 2006; Commerçon et al., 2011; Lee, D. et al, 2011) for solving systems of parabolic PDEs numerically. The method increases its effective time steps $\Delta t_{\rm StS}$ using two properties of stability and optimality in Chebychev polynomial of degree n. These properties optimally maximize the time step $\Delta t_{\rm StS}$ by which a solution vector can be evolved. A stability condition is imposed only after each time step $\Delta t_{\rm StS}$, which is further subdivided into smaller $N_{\rm StS}$ sub-time steps, τ_i , that is, $\Delta t_{\rm StS} = \sum_{i=1}^{N_{\rm StS}} \tau_i$, where the sub-time step is given by

$$\tau_i = \Delta t_{\text{CFL-para}} \left[(-1 + \nu_{\text{sts}}) cos \left(\frac{\pi (2j - 1)}{2N_{\text{sts}}} + 1 + \nu_{\text{sts}} \right) \right]^{-1},$$
(5.1)

Variable	Type	Default	Description
useSTS	logical	.false.	Enable STS
${ t nstepTotalSTS}$	integer	5	Suggestion: ~ 5 for hyperbolic; ~ 10 for parabolic
nuSTS	real	0.2	Suggestion: ~ 0.2 for hyperbolic; ~ 0.01 for parabolic. It
			is known that a very low value of ν may result in unstable
			temporal integrations, while a value close to unity can de-
			crease the expected efficiency of STS.
${\tt useSTSforDiffusion}$	logical	.false.	This setup will use the STS for overcoming small diffusion
			time steps assuming $\Delta t_{\text{CFL-adv}} > \Delta t_{\text{CFL-para}}$. In im-
			plementation, it will set $\Delta t_{\text{CFL}} = \Delta t_{\text{CFL-para}}$ in Eqn.
			??. Do not allow to turn on this switch when there is no
			diffusion (viscosity, conductivity, and magnetic resistivity)
			used.
$\verb allowDtSTSDominate $	logical	.false.	If true, this will allow to have $\tau_i > \Delta t_{\text{CFL-adv}}$, which may
			result in unstable integrations.

Table 5.1: Runtime parameters for STS

where $\Delta t_{\mathrm{CFL_para}}$ is an explicit time step for a given parabolic system based on the CFL stability condition. ν (nuSTS) is a free parameter less than unity. For $\nu \to 0$, STS is asymptotically N_{StS} times faster than the conventional explicit scheme based on the CFL condition. During the N_{sts} sub-time steps, the STS method still solves solutions at each intermediate step τ_i ; however, such solutions should not be considered as meaningful solutions.

Extended from the original STS method for accelerating parabolic timestepping, our STS method advances advection and/or diffusion (hyperbolic and/or parabolic) system of equations. This means that the STS algorithm in Flash-X invokes a single Δt_{sts} for both advection and diffusion, and does not use any sub-cycling for diffusion based on a given advection time step. In this case, τ_i is given by

$$\tau_i = \Delta t_{\text{CFL}} \left[(-1 + \nu_{\text{sts}}) cos \left(\frac{\pi (2j - 1)}{2N_{\text{sts}}} + 1 + \nu_{\text{sts}} \right) \right]^{-1},$$
(5.2)

where $\Delta t_{\rm CFL}$ can be an explicit time step for advection ($\Delta t_{\rm CFL_adv}$) or parabolic ($\Delta t_{\rm CFL_para}$) systems. In cases of advection-diffusion system, $\Delta t_{\rm CFL}$ takes ($\Delta t_{\rm CFL_para}$) when it is smaller than ($\Delta t_{\rm CFL_adv}$); otherwise, Flash-X's timestepping will proceed without using STS iterations (i.e., using standard explicit timestepping that is either Strang split evolution or unsplit evolution.

Since the method is explicit, it works equally well on both a uniform grid and AMR grids without modification. The STS method is first-order accurate in time.

Both directionally-split and unsplit hydro solvers can use the STS method, simply by invoking a runtime parameter useSTS = .true. in flash.par. There are couple of runtime parameters that control solution accuracy and stability. They are decribed in Table ??.

5.1.2.4 Runtime Parameters

The Driver unit supplies certain runtime parameters regardless of which type of driver is chosen. These are described in the online [[rpi reference]]Driver/Runtime Parameters Documentation page.

5.1.3 Driver_finalizeFlash

Finally, the the Driver unit calls [[api reference]] which calls the finalize routines for each unit. Typically this involves deallocating memory and any other necessary cleanup.

5.1.4 Driver accessor functions

In FLASH-X the Driver unit also provides a number of accessor functions to get data stored in the Driver unit, for example [[api reference]], [[api reference]], [[api reference]].

The Driver unit API also defines two interfaces for halting the code, [[api reference]] and [[C api reference]].c. The 'c' routine version is available for calls written in C, so that the user does not have to worry about any name mangling. Both of these routines print an error message and call MPI_Abort.

5.1.5 Time Step Limiting

The Driver unit is responsible for determining the time step Δt that is used to advance the solution from time $t=t^{n-1}$ to t^n . At startup, a tentative Δt is chosen based in runtime parameters, in particular [[rpi reference]]. The routine [[api reference]] (usually invoked from [[api reference]]) is used to check and, if necessary, modify the initial Δt . Subsequently, the routine [[api reference]] (usually invoked from [[api reference]] at the end of an iteration of the main evolution loop) is used to recompute Δt for the next evolution step.

The implementation of [[api reference]] can lower or increase the time step. It takes various runtime parameters into consideration, including [[rpi reference]], [[rpi reference]], and [[rpi reference]]. For the most part, however, [[api reference]] calls on UNIT_computeDt routines of various code units to query those units for their time step requirements, and usually chooses the smallest time step that is acceptable to all units queried.

The code units that participate in this negotiation return a Δt , and usually some additional information about which location in the simulaton domain caused the reequired step to be as low as returned. A unit's time step requirement can depend on the current state of the solution as well as on further runtime parameters. For example, the dt returned by [[api reference]] depends on the state of density, pressure, and velocities (and possibly additional variables) in the cells of the domain, as well as on the runtime parameter [[rpi reference]].

5.1.5.1 Generic time step limiting for positive definiteness

A generic method for limiting time steps, based on a requirement that certain (user-specified) variables should never become negative, has been added in FLASH-X. To understand the basic idea, think of each variable that this limiter is applied to as a density of some quantity q. (Variables of PER_MASS type are actually converted to their PER_VOLUME counterparts in the implementation of the method.)

The algorithm is based on examining the distribution of q in neighboring cells, and making for each cell a near-worst-case estimate of the rate of depletion \dot{q} based on projected fluxes of q out of the cell over its faces. This can be applied to any variable, it is not required that the variable represents any quantity that is actually advected as described. See ?? for how to use. This feature may be particularly useful when applied to "eion" in multidimensional 3T simulations in order to avoid some kinds of "negative ion temperature" failures, as an alternative to lowering the Hydro runtime parameter [[rpi reference]].

Table 5.2: Runtime parameters for positive definiteness.

Parameter	Type	Default	Description
[[rpi reference]]	boolean	.false.	Set to .true. to turn positive-definite time step lim-
			iter on.
[[rpi reference]]	integer	4	Number of variables for which positive definiteness
			should be enforced
${\tt dr_posdefVar_N}$	string	"none"	Name of Nth variable for positive-definite dt lim-
			iter
dr_posdefDtFactor	real	1.0	Scaling factor for dt limit from positive-definite
			time step limiter. Similar to CFL factor. If set to
			-1, use [[rpi reference]] factor from Hydro.

Part IV Infrastructure Units

Chapter 6

Grid Unit

6.1 Overview

The Grid unit has four subunits: GridMain is responsible for maintaining the Eulerian grid used to discretize the spatial dimensions of a simulation; GridParticles manages the data movement related to active, and Lagrangian tracer particles; GridBoundaryConditions handles the application of boundary conditions at the physical boundaries of the domain; and GridSolvers provides services for solving some types of partial differential equations on the grid. In the Eulerian grid, discretization is achieved by dividing the computational domain into one or more sub-domains or blocksand using these blocks as the primary computational entity visible to the physics units. A blockcontains a number of computational cells (nxb in the x-direction, nyb in the y-direction, and nzb in the z-direction). A perimeter of guardcellsof width nguard cells in each coordinate direction, surrounds each block of local data, providing it with data from the neighboring blocks or with boundary conditions, as shown in ??. Since the majority of physics solvers used in Flash-X are explicit, a block with its surrounding guard cells becomes a self-contained computational domain. Thus the physics units see and operate on only one block at a time, and this abstraction is reflected in their design.

Therefore any mesh package that can present a self contained block as a computational domain to a client unit can be used with Flash-X. However, such interchangeability of grid packages also requires a careful design of the Grid API to make the underlying management of the discretized grid completely transparent to outside units. The data structures for physical variables, the spatial coordinates, and the management of the grid are kept private to the Grid unit, and client units can access them only through accessor functions. This strict protocol for data management along with the use of blocks as computational entities enables Flash-X to abstract the grid from physics solvers and facilitates the ability of Flash-X to use multiple mesh packages.

Any unit in the code can retrieve all or part of a block of data from the Grid unit along with the coordinates of corresponding cells; it can then use this information for internal computations, and finally return the modified data to the Grid unit. The Grid unit also manages the parallelization of Flash-X. It consists of a suite of subroutines which handle distribution of work to processors and guard cell filling. When using an adaptive mesh, the Grid unit is also responsible for refinement/derefinement and conservation of flux across block boundaries.

Flash-X can interchangeably use either a **uniform** or **adaptive grid** for most problems. Additionally, a new feature in FLASH-X is an option to replicate the mesh; that is processors are assumed to be partitioned into groups, each group gets a copy of the entire domain mesh. This feature is useful when it is possible to decompose the computation based upon certain compute intensive tasks that apply across the domain. One such example is radiation transfer with multigroup flux limited diffusion where each group needs an implicit solve. Here the state variable of the mesh are replicated on each group of processors, while the groups are unique. Thus at the cost of some memory redundancy, it becomes possible to compute a higher fidelity problem (see ?? for an example). Because of this feature, the parallel environment of the simulation is now controlled by the Driver which differentiates between global communicators and mesh communicators. The Grid unit queries the Driver unit for mesh communicators. In all other respects this change is transparent to the Grid unit. Mesh replication can be invoked through the runtime parameter [[rpi reference]]

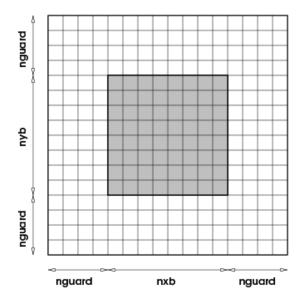


Figure 6.1: A single 2-D block showing the interior cells (shaded) and the perimeter of guard cells.

The uniform grid supported in Flash-X discretizes the physical domain by placing grid points at regular intervals defined by the geometry of the problem. The grid configuration remains unchanged throughout the simulation, and exactly one block is mapped per processor. An adaptive grid changes the discretization over the course of the computation, and several blocks can be mapped to each computational processor. Two AMR packages are currently supported in Flash-X for providing adaptive grid capbility. The block-structured oct-tree based AMR package, PARAMESH has been the work horse since the beginning of the code.

Flash-X Transition

The following two commands will create the same (identical) application: a simulation of a Sod shock tube in 3 dimensions with PARAMESH 4 managing the grid.

./setup Sod -3d -auto

./setup Sod -3d -auto -unit=Grid/GridMain/paramesh/paramesh4/Paramesh4.0

However, if the command is changed to

./setup Sod -3d -auto -unit=Grid/GridMain/UG

the application is set up with a uniform grid instead. Additionally, because two different grids types are supported in Flash-X, the user must match up the correct IO alternative implementation with the correct Grid alternative implementation. Please see ?? for more details. Note that the setup script has capabilities to let the user set up shortcuts, such as "+ugio", which makes sure that the appropriate branch of IO is included when the uniform grid is being used. Please see ?? for more information. Also see for shortcuts useful for the Grid unit.

6.2 GridMain Data Structures

The Grid unit is the most extensive infrastructure unit in the Flash-X code, and it owns data that most other units wish to fetch and modify. Since the data layout in this unit has implications on the manageability and performance of the code, we describe it in some detail here.

Flash-X can be run with a grid discretization that assumes cell-centered data, face-centered data, or a combination of the two. Paramesh and Uniform Grid store physical data in multidimensional F90 arrays; cell-centered variables in unk, short for "unknowns", and face-centered variables in arrays called facevarx, facevary, and facevarz, which contain the face-centered data along the x, y, and z dimensions, respectively. The cell-centered array unk is dimensioned as array(NUNK_VARS,nxb,nyb,nzb,blocks), where nxb, nyb, nzb are the spatial dimensions of a single block, and blocks is the number of blocks per processor (MAXBLOCKS for PARAMESH and 1 for UG). The face-centered arrays have one extra data point along the dimension they are representing, for example facevarx is dimensioned as array(NFACE_VARS,nxb+1,nyb,nzb,blocks). Some or all of the actual values dimensioning these arrays are determined at application setup time. The number of variables and the value of MAXBLOCKS are always determined at setup time. The spatial dimensions nxb,nyb,nzb can either be fixed at setup time, or they may be determined at runtime. These two modes are referred to as FIXEDBLOCKSIZE and NONFIXEDBLOCKSIZE.

All values determined at setup time are defined as constants in a file Simulation.h generated by the setup tool. This file contains all application-specific global constants such as the number and naming of physical variables, number and naming of fluxes and species, etc.; it is described in detail in ??.

For cell-centered variables, the **Grid** unit also stores a **variable type** that can be retrieved using the [[api reference]] routine; see **??** for the syntax and meaning of the optional **TYPE** attribute that can be specified as part of a **VARIABLE** definition read by the setup tool.

In addition to the primary physical variables, the Grid unit has another set of data structures for storing auxiliary fluid variables. This set of data structures provides a mechanism for storing such variables whose spatial scope is the entire physical domain, but who do not need to maintain their guard cells updated at all times. The data structures in this set include: SCRATCHCENTERVAR, which has the same shape as the cell centered variables data structure; and SCRATCHFACEXVAR, SCRATCHFACEYVAR and SCRATCHFACEZVAR, which have the same shape as the corresponding face centered variables data structures. Early releases of Flash-X3 had SCRATCHVAR, dimensioned array (NSCRATCH_GRID_VARS, nxb+1, nyb+1, nzb+1, blocks), as the only grid scope scratch data structure. For reasons of backward compatibility, and to maximize reusability of space, SCRATCHVAR continues to exist as a supported data structure, though its use is deprecated. The datastructures for face variables, though supported, are not used anywhere in the released code base. The unsplit MHD solver StaggeredMesh discussed in ?? gives an example of the use of some of these data structures. It is important to note that there is no guardcell filling for the scratch variables, and the values in the scratch variables become invalid after a grid refinement step. While users can define scratch variables to be written to the plotfiles, they are not by default written to checkpoint files. The Grid unit also stores the metadata necessary for work distribution, load balancing, and other housekeeping activities. These activities are further discussed in ?? and ??, which describe individual implementations of the Grid unit.

6.3 Computational Domain

The size of the computational domainin physical units is specified at runtime through the ([[rpi reference]], [[rpi reference]])([[rpi reference]])([[rpi reference]]) ([[rpi reference]]) ([[rpi reference]]) ([[rpi reference]]) runtime parameters. When working with curvilinear coordinates (see below in ??), the extrema for angle coordinates are specified in degrees. Internally all angles are represented in radians, so angles are converted to radians at Grid initialization.

The physical domain is mapped into a computational domain at problem initialization through routine [[api reference]] in PARAMESH and [[api reference]] in UG.When using the uniform grid UG, the mapping is easy: one block is created for each processor in the run, which can be sized either at build time or runtime depending upon the mode of UG use. ¹ Further description can be found in ??. When using the AMR

¹Note that the term processor, as used here and elsewhere in the documentation, does not necessarily correspond to a separate hardware processor. It is also possible to have several logical "processors" mapped to the same hardware, which can be useful for debugging and testing; this is a matter for the operating environment to regulate.

grid PARAMESH, the mapping is non-trivial. The adaptive mesh <code>gr_createDomain</code> function creates an initial mesh of <code>nblockx * nblocky * nblockz</code> top level blocks, where [[rpi reference]], [[rpi reference]], and [[rpi reference]] are runtime parameters which default to 1.² The resolution of the computational domain is usually very coarse and unsuitable for computation after the initial mapping. The <code>gr_expandDomain</code> routine remedies the situation by applying the refinement process to the initial domain until a satisfactory level of resolution is reached everywhere in the domain. This method of mapping the physical domain to computational domain is effective because the resultant resolution in any section is related to the demands of the initial conditions there.

6.4 Boundary Conditions

Much of the Flash-X code within the Grid unit that deals with implementing boundary conditions has been organized into a separate subunit, GridBoundaryConditions. Note that the following aspects are still handled elsewhere:

- Recognition of bounday condition names as strings (in runtime parameters) and constants (in the source code); these are defined in [[api reference]] and in constants.h, respectively.
- Handling of periodic boundary conditions; this is done within the underlying GridMain implementation. When using PARAMESH, the subroutine gr_createDomain is responsible for setting the neighbors of top-level blocks (to either other top-level blocks or to external boundary conditions) at initialization, after [[rpi reference]] × [[rpi reference]] × [[rpi reference]] root blocks have been created. periodic (wrap-around) boundary conditions are initially configured in this routine as well. If periodic boundary conditions are set in the x-direction, for instance, the first blocks in the x-direction are set to have as their left-most neighbor the blocks that are last in the x-direction, and vice versa. Thus, when the guard cell filling is performed, the periodic boundary conditions are automatically maintained.
- Handling of user-defined boundary conditions; this should be implemented by code under the Simulation directory.
- Low-level implementation and interfacing, such as are part of the PARAMESH code.
- Behavior of particles at a domain boundary. This is based on the boundary types described below, but their handling is implemented in GridParticles.

Although the GridBoundaryConditions subunit is included in a setup by default, it can be excluded (if no Config file "REQUIRES" it) by specifying -without-unit=Grid/GridBoundaryConditions. This will generally only make sense if all domain boundaries are to be treated as periodic. (All relevant runtime parameters [[rpi reference]] etc. need to be set to "periodic" in that case.)

6.4.1 Boundary Condition Types

Boundary conditions are determined by the physical problem. Within Flash-X, the parallel structure of blocks means that each processor works independently. If a block is on a physical boundary, the guard cells are filled by calculation since there are no neighboring blocks from which to copy values. Boundaries are selected by setting runtime parameters such as [[rpi reference]] (for the 'left' X-boundary) to one of the supported boundary types (??) in flash.par. Even though the runtime parameters for specifying boundary condition types are strings, the Grid unit understands them as defined integer constants defined in the file constants.h, which contains all global constants for the code. The translation from the string specified in "flash.par" to the constant understood by the Grid unit is done by the routine [[api reference]].

To use any of the hydrostatic-f2* boundary conditions, the setup must include Grid/GridBoundary-Conditions/Flash2HSE. This must usually be explicitly requested, for example with a line

REQUIRES Grid/GridBoundaryConditions/Flash2HSE

²The gr_createDomain function also can remove certain blocks of this initial mesh, if this is requested by a non-default [[api reference]] implementation.

$ab_\mathbf{boundary_type}$	Description	
periodic	Periodic ('wrap-around')	
reflect,reflecting	Non-penetrating boundaries; plane symmetry, the normal vector components change sign	
outflow	Zero-gradient boundary conditions; allows shocks to leave the domain	
diode	like outflow, but fluid velocities are never allowed to let matter flow into the domain: normal velocity components are forced to zero in guard cells if necessary	
axisymmetric	like reflect, but both normal and toroidal vector components change sign. Typically used with cylindrical geometry (R-Z) for the Z symmetry axis.	
eqtsymmetric	like reflect for velocities but the magnetic field components, poloidal and toroidal, change sign. The sign of the normal magnetic field component remains the same. Typically used with cylindrical geometry (R-Z) for the R axis to emulate equatorial symmetry.	
hydrostatic-f2	Hydrostatic boundary handling as in Flash-X. See remark in text.	
hydrostatic-f2+nvrefl, hydrostatic-f2+nvout, hydrostatic-f2+nvdiode	Variants of hydrostatic-f2, where the normal velocity is handled specially in various ways, analogous to reflect, outflow, and diode boundary conditions, respectively. See remark in text.	
user-defined or user	The user must implement the desired boundary behavior; see text.	

Table 6.1: Hydrodynamical boundary conditions supported by Flash-X. Boundary type ab may be replaced with $a=\{x,y,z\}$ for direction and $b=\{l,r\}$ for left/right edge. All boundary types listed except the last (user) have an implementation in GridBoundaryConditions.

in the simulation directory's Config file.

Note that the [[rpi reference]] runtime parameter is used by some implementations of the **Gravity** unit to define the type of boundary for solving a self-gravity (Poisson) problem; see [[api reference]]. This runtime parameter is separate from the ab-boundary_type ones interpreted by **GridBoundaryConditions**, and its recognized values are not the same (although there is some overlap).

6.4.2 Boundary Conditions at Obstacles

The initial coarse grid of root blocks can be modified by removing certain blocks. This is done by providing a non-trivial implementation of [[api reference]]. Effectively this creates additional domain boundaries at the interface between blocks removed and regions still included. All boundary conditions other than periodic are possible at these additional boundaries, and are handled there in the same way as on external domain boundaries. This feature is only available with PARAMESH. See the documentation and example in [[api reference]] for more details and some caveats.

6.4.3 Implementing Boundary Conditions

Users may need to implement boundary conditions beyond those provided with FLASH-X, and the Grid-BoundaryConditions subunit provides several ways to achieve this. Users can provide an implementation for the user boundary type; or can provide or override an implementation for one of the other recognized types.

The simple boundary condition types reflect, outflow, diode are implemented in the [[api reference]].F90 file in Grid/GridBoundaryConditions. A users can add or modify the handling of some

$ab_\mathbf{boundary_type}$	Constant	Remark
isolated	_	used by Gravity only for [[rpi reference]]
_	DIRICHLET	used for multigrid solver
_	GRIDBC_MG_EXTRAPOLATE	for use by multigrid solver
	PNEUMANN	(for use by multigrid solver)
hydrostatic	HYDROSTATIC	Hydrostatic, other implementation than Flash-X
hydrostatic+nvrefl	HYDROSTATIC_NVREFL	Hydrostatic variant, other impl. than Flash-X
hydrostatic+nvout	$ t HYDROSTATIC_NVOUT$	Hydrostatic variant, other impl. than Flash-X
hydrostatic+nvdiode	HYDROSTATIC_NVDIODE	Hydrostatic variant, other impl. than Flash-X

Table 6.2: Additional boundary condition types recognized by Flash-X. Boundary type ab may be replaced with $a=\{x,y,z\}$ for direction and $b=\{l,r\}$ for left/right edge. These boundary types are either reserved for implementation by users and/or future Flash-X versions for a specific purpose (as indicate by the remarks), or are for special uses within the **Grid** unit.

boundary condition types in a version of this file in the simulation directory, which overrides the regular version. There is, however, also the interface [[api reference]] which by default is only provided as a stub and is explicitly intended to be implemented by users.

A [[api reference]] implementation gets called before [[api reference]] and can decide to either handle a specific combination of boundary condition type, direction, grid data structure, etc., or leave it to [[api reference]]. These calls operate on a region of one block's cells at a time. Flash-X will pass additional information beyond that needed for handling simple boundary conditions to [[api reference]], in particular a block handle through which an implementation can retrieve coordinate information and access other information associated with a block and its cells.

The GridBoundaryConditions subunit also provides a simpler kind of interface if one includes Grid/-GridBoundaryConditions/OneRow in the setup. When using this style of interface, users can implement guard cell filling one row at a time. Flash-X passes to the implementation one row of cells at a time, some of which are interior cells while the others represent guard cells outside the boundary that are to be modified in the call. A row here means a contiguous set of cells along a line perpendicular to the boundary surface. There are two versions of this interface: [[api reference]] is given only one fluid variable at a time, but can also handle data structures other than unk; whereas [[api reference]] handles all variables of unk along a row in one call. Cell coordinate information is included in the call arguments. Flash-X invokes these functions through an implementation of [[api reference]] in Grid/GridBoundaryConditions/OneRow which acts as a wrapper. GridBoundaryConditions/OneRow also provides a default implementation of [[api reference]] (which implements the simple boundary conditions) and [[api reference]] (which calls Grid_applyBCEdge) each. Another implementation of [[api reference]] can be found in GridBoundaryConditions/OneRow/Flash2HSE, this one calls Grid_applyBCEdge or, for FLASH-X-type hydrostatic boundaries, the code for handling them. These can be used as templates for overriding implementations under Simulation. It is not recommended to try to mix both Grid_bcApplyToRegion*-style and Grid_applyBCEdge*-style overriding implementations in a simulation directory, since this could become confusing.

Note that in all of these cases, i.e., whether boundary guard cell filling for a boundary type is implemented in [[api reference]], [[api reference]], [[api reference]], or

[[api reference]], the implementation does not fill guard cells in permanent data storage (the unk array and similar data structures) directly, but operates on buffers. FLASH-X fills some parts of the buffers with current values for interior cells before the call, and copies updated guardcell data from some (other) parts of the buffers back into unk (or similar) storage after the handling routine returns.

All calls to handlers for boundary conditions are for one face in a given dimension at a time. Thus for each of the IAXIS, JAXIS, and KAXIS dimensions there can be up to two series of calls, once for the left, *i.e.*, "LOW," and once for the right, *i.e.*, "HIGH," face. PARAMESH 4 makes additional calls for filling guard cells in edge and corner regions of blocks, these calls result in additional Grid_bcApplyToRegion* invocations for those cells that lie in diagonal directions from the block interior.

The boundary condition handling interfaces described so far can be implemented (and will be used!)

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independent of the Grid implementation chosen. At a lower level, the various implementations of GridMain have different ways of requesting that boundary guard cells be filled. The GridBoundaryConditions subunit collaborates with GridMain implementations to provide to user code uniform interfaces that are agnostic of lower-level details. However, it is also possible — but not recommended — for users to replace a routine that is located deeper in the Grid unit. For PARAMESH 4, the most relevant routine is amr_1blk_bcset.F90, for PARAMESH 2 it is tot_bnd.F90, and for uniform grid UG it is gr_bcApplyToAllBlks.F90.

6.4.3.1 Additional Concerns with PARAMESH 4

Boundary condition handling has become significantly more complex in FLASH-X. In part this is so because PARAMESH 4 imposes requirements on guard cell filling code that do not exist in the other GridMain implementations:

- 1. In other Grid implementations, filling of domain boundary guard cells is under control of the "user" (in this context, the user of the grid implementation, i.e., Flash-X): These cells can be filled for all blocks at a time that is predictable to the user code, as a standard part of handling [[api reference]], only. With PARAMESH 4, the user-provided amr_1blk_bcset routine can be called from within the depths of PARAMESH on individual blocks (and cell regions, see below) during guard cell filling and at other times when the user has called a PARAMESH routine. It is not easy to predict when and in which sequence this will happen.
- 2. PARAMESH 4 does not want all boundary guard cells filled in one call, but requests individual regions in various calls.
- 3. PARAMESH 4 does not let the user routine amr_1blk_bcset operate on permanent storage (unk etc.) directly, but on (regions of) one-block buffers.
- 4. PARAMESH 4 occasionally invokes amr_1blk_bcset to operate on regions of a block that belongs to a remote processor (and for which data has been cached locally). Such block data is not associated with a valid local blockID, making it more complicated for user code to retrieve metadata that may be needed to implement the desired boundary handling.

Some consequences of this for Flash-X users:

- User code that implements boundary conditions for the grid inherits the requirement that it must be ready to be called at various times (when certain Grid routines are called).
- User code that implements boundary conditions for the grid inherits the requirement that it must operate on a region of the cells of a block, where the region is specified by the caller.
- Such user code must not assume that it operates on permanent data (in unk etc.). Rather, it must be prepared to fill guardcells for a block-shaped buffer that may or may not end up being copied back to permanent storage.
 - User code also is not allowed to make certain PARAMESH 4 calls while a call to amr_1blk_bcset is active, namely those that would modify the same one-block buffers that the current call is working on.
- The user code must not assume that the block data it is acting on belongs to a local block. The data
 may not have a valid blockID. The code will be passed a "block hande" which can be used in some
 ways, but not all, like a valid blockID.

6.5 Uniform Grid

The Uniform Grid has the same resolution in all the blocks throughout the domain, and each processor has exactly one block. The uniform grid can operate in either of two modes: fixed block size (FIXEDBLOCK-SIZE) mode, and non-fixed block size (NONFIXEDBLOCKSIZE) mode. The default fixed block size grid is statically defined at compile time and can therefore take advantage of compile-time optimizations. The non-fixed block size version uses dynamic memory allocation of grid variables.

6.5.1 FIXEDBLOCKSIZE Mode

FIXEDBLOCKSIZEmode, also called static mode, is the default for the uniform grid. In this mode, the block size is specified at compile time as $NXB \times NYB \times NZB$. These variables default to 8 if the dimension is defined and 1 otherwise -e.g. for a two-dimensional simulation, the defaults are NXB = 8, NYB = 8, NZb = 1. To change the static dimensions, specify the desired values on the command line of the **setup** script; for example

```
./setup Sod -auto -3d -nxb=12 -nyb=12 -nzb=4 +ug
```

The distribution of processors along the three dimensions is given at run time as $iprocs \times jprocs \times kprocs$ with the constraint that this product must be equal to the number of processors that the simulation is using. The global domain size in terms of number of grid points is NXB * $iprocs \times$ NYB * $jprocs \times$ NZB * kprocs. For example, if iprocs = jprocs = 4 and kprocs = 1, the execution command should specify np = 16 processors.

```
mpirun -np 16 flash3
```

When working in static mode, the simulation is constrained to run on the same number of processors when restarting, since any different configuration of processors would change the domain size.

At Grid initialization time, the domain is created and the communication machinery is also generated. This initialization includes MPI communicators and datatypes for directional guardcell exchanges. If we view processors as arranged in a three-dimensional processor grid, then a row of processors along each dimension becomes a part of the same communicator. We also define MPI datatypes for each of these communicators, which describe the layout of the block on the processor to MPI. The communicators and datatypes, once generated, persist for the entire run of the application. Thus the MPI_SEND/RECV function with specific communicator and its corresponding datatype is able to carry out all data exchange for guardcell fill in the selected direction in a single step.

Since all blocks exist at the same resolution in the Uniform Grid, there is no need for interpolationwhile filling the guardcells. Simple exchange of correct data between processors, and the application of boundary conditions where needed is sufficient. The guard cells along the face of a block are filled with the layers of the interior cells of the block on the neighboring processor if that face is shared with another block, or calculated based upon the boundary conditions if the face is on the physical domain boundary. Also, because there are no jumps in refinement in the Uniform Grid, the flux conservation step across processor boundaries is unnecessary. For correct functioning of the Uniform Grid in Flash-X, this conservation step should be explicitly turned off with a runtime parameter [[rpi reference]] which controls whether or not to run the flux conservation step in the PPM Hydrodynamics implementation. AMR sets it by default to true, while UG sets it to false. Users should exercise care if they wish to override the defaults via their "flash.par" file.

6.5.2 NONFIXEDBLOCKSIZE mode

Up ot version 2, Flash-X always ran in a mode where all blocks have exactly the same number of grid points in exactly the same shape, and these were fixed at compile time. Flash-X was limited to use the fixed block size mode described above. With Flash-X this constraint was eliminated through an option at setup time. The two main reasons for this development were: one, to allow a uniform grid based simulation to be able to restart with different number of processors, and two, to open up the possibility of using other AMR packages with Flash-X. Patch-based packages typically have different-sized block configurations at different times. This mode, called the "NONFIXEDBLOCKSIZE" mode, can currently be selected for use with Uniform Grid. To run an application in "NONFIXEDBLOCKSIZE" modethe "-nofbs" option must be used when invoking the setup tool; see ?? for more information. For example:

```
./setup Sod -3d -auto -nofbs
```

Note that NONFIXEDBLOCKSIZE mode requires the use of its own IO implementation, and a convenient shortcut has been provided to ensure that this mode is used as in the example below:

```
./setup Sod -3d -auto +nofbs
```

In this mode, the blocksize in UG is determined at execution from runtime parameters [[rpi reference]], [[rpi reference]] and [[rpi reference]]. These parameters specify the global number of grid points in the computational domain along each dimension. The blocksize then is $(iGridSize/iprocs) \times (jGridSize/jprocs) \times (kGridSize/kprocs)$.

Unlike FIXEDBLOCKSIZE mode, where memory is allocated at compile time, in the NONFIXEDBLOCKSIZE modeallocation is dynamic. The global data structures are allocated when the simulation initializes and deallocated when the simulation finalizes, whereas the local scratch space is allocated and deallocated every time a unit is invoked in the simulation. Clearly there is a trade-off between flexibility and performance as the NONFIXEDBLOCKSIZE mode typically runs about 10-15% slower. We support both to give choice to the users. The amount of memory consumed by the Grid data structure of the Uniform Grid is $nvar \times (2*nguard + nxb) \times (2*nguard + nyb) \times (2*nguard + nzb)$ irrespective of the mode. Note that this is not the total amount of memory used by the code, since fluxes, temporary variables, coordinate information and scratch space also consume a large amount of memory.

The example shown below gives two possible ways to define parameters in flash.par for a 3d problem of global domain size $64 \times 64 \times 64$, being run on 8 processors.

```
iprocs = 2
jprocs = 2
kprocs = 2
iGridSize = 64
jGridSize = 64
kGridSize = 64
```

This specification will result in each processor getting a block of size $32 \times 32 \times 32$. Now consider the following specification for the number of processors along each dimension, keeping the global domain size the same.

```
iprocs = 4
jprocs = 2
kprocs = 1
```

In this case, each processor will now have blocks of size $16 \times 32 \times 64$.

6.6 Adaptive Mesh Refinement (AMR) Grid with Paramesh

The default package in Flash-X is PARAMESH (MacNeice et al. 1999) for implementing the adaptive mesh refinement (AMR) grid. PARAMESH uses a block-structured adaptive mesh refinement scheme similar to others in the literature (e.g., Parashar 1999; Berger & Oliger 1984; Berger & Colella 1989; DeZeeuw & Powell 1993). It also shares ideas with schemes which refine on an individual cell basis (Khokhlov 1997). In block-structured AMR, the fundamental data structure is a block of cells arranged in a logically Cartesian fashion. "Logically Cartesian" implies that each cell can be specified using a block identifier (processor number and local block number) and a coordinate triple (i,j,k), where i=1...nxb, j=1...nyb, and k=1...nzb refer to the x-, y-, and z-directions, respectively. It does not require a physically rectangular coordinate system; for example a spherical grid can be indexed in this same manner.

The complete computational grid consists of a collection of blocks with different physical cell sizes, which are related to each other in a hierarchical fashion using a tree data structure. The blocks at the root of the tree have the largest cells, while their children have smaller cells and are said to be refined. Three rules govern the establishment of refined child blocks in PARAMESH. First, a refined child block must be one-half as large as its parent block in each spatial dimension. Second, a block's children must be nested; *i.e.*, the child blocks must fit within their parent block and cannot overlap one another, and the complete set of children of a block must fill its volume. Thus, in d dimensions a given block has either zero or 2^d children. Third, blocks which share a common border may not differ from each other by more than one level of refinement.

A simple two-dimensional domain is shown in ??, illustrating the rules above. Each block contains $\mathtt{nxb} \times \mathtt{nyb} \times \mathtt{nzb}$ interior cells and a set of guard cells. The guard cells contain boundary information needed to update the interior cells. These can be obtained from physically neighboring blocks, externally specified boundary conditions, or both. The number of guard cells needed depends upon the interpolation schemes

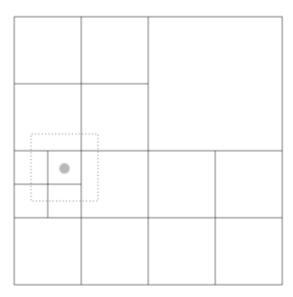


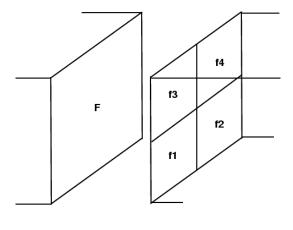
Figure 6.2: A simple computational domain showing varying levels of refinement in a total of 16 blocks. The dotted lines outline the guard cells for the block marked with a circle.

and the differencing stencils used by the various physics units (usually hydrodynamics). For the explicit PPM algorithm distributed with Flash-X, four guard cells are needed in each direction, as illustrated in ??. The blocksize while using the adaptive grid is fixed at compile time, resulting in static memoryallocation. The total number of blocks a processor can manage is determined by MAXBLOCKSwhich can be overridden at setup time with the setup ...-maxblocks=# argument. The amount of memory consumed by the Grid data structure of code when running with PARAMESH is NUNK_VARS \times (2 * nguard + nxb) \times (2 * nguard + nyb) \times (2 * nguard + nzb) \times MAXBLOCKS. PARAMESH also needs memory to store its tree data structure for adaptive mesh management, over and above what is already mentioned with Uniform Grid. As the levels of refinement increase, the size of the tree also grows.

PARAMESH handles the filling of guard cells with information from other blocks or, at the boundaries of the physical domain, from an external boundary routine (see ??). If a block's neighbor exists and has the same level of refinement, PARAMESH fills the corresponding guard cells using a direct copy from the neighbor's interior cells. If the neighbor has a different level of refinement, the data from the neighbor's cells must be adjusted by either interpolation(to a finer level of resolution) or averaging (to a coarser level)—see ?? below for more information. If the block and its neighbor are stored in the memory of different processors, PARAMESH handles the appropriate parallel communications (blocks are never split between processors). The filling of guard cells is a global operation that is triggered by calling [[api reference]].

Grid Interpolationis also used when filling the blocks of children newly created in the course of automatic refinement. This happens during [[api reference]] processing. Averaging also used to regularly update the solution data in at least one level of parent blocks in the oct-tree. This ensures that after leaf nodes are removed during automatic refinement processing (in regions of the domain where the mesh is becoming coarser), the new leaf nodes automatically have valid data. This averaging happens as an initial step in [[api reference]] processing.

PARAMESH also enforces flux conservation at jumps in refinement, as described by Berger and Colella (1989). At jumps in refinement, the fluxes of mass, momentum, energy (total and internal), and species density in the fine cells across boundary cell faces are summed and passed to their parent. The parent's neighboring cell will be at the same level of refinement as the summed flux cell because PARAMESH limits the jumps in refinement to one level between blocks. The flux in the parent that was computed by the more accurate fine cells is taken as the correct flux through the interface and is passed to the corresponding coarse face on the neighboring block (see ??). The summing allows a geometrical weighting to be implemented for



F = [f1 + f2 + f3 + f4]

Figure 6.3: Flux conservation at a jump in refinement. The fluxes in the fine cells are added and replace the coarse cell flux (F).

non-Cartesian geometries, which ensures that the proper volume-corrected flux is computed.

6.6.1 Additional Data Structures

PARAMESH maintains much additional information about the mesh. In particular, oct-tree related information is kept in various arrays which are declared in a F90 module called "tree". It includes the physical coordinate of a block's center, its physical size, level of refinement, and much more. These data structures also acts as temporary storage while updating refinement in the grid and moving the blocks. This metadata should in general not be accessed directly by application code. The Grid API contains subroutines for accessing the most important pars of this metadata on a block by block basis, like [[api reference]], [[api reference]], [[api reference]], and [[api reference]].

Flash-X has its own oneBlock data structure that stores block specific information. This data structure keeps the physical coordinates of each cell in the block. For each dimension, the coordinates are stored for the LEFT_EDGE, the RIGHT_EDGE and the center of the cell. The coordinates are determined from "cornerID" which is also a part of this data structure.

The concept of cornerID was introduced in FLASH-X; it serves three purposes. First, it creates a unique global identity for every cell that can come into existence at any time in the course of the simulation. Second, it can prevent machine precision error from creeping into the spatial coordinates calculation. Finally, it can help pinpoint the location of a block within the oct-tree of PARAMESH. Another useful integer variable is the concept of a *stride*. A stride indicates the spacing factor between one cell and the cell directly to its right when calculating the cornerID. At the maximum refinement level, the stride is 1, at the next higher level it is 2, and so on. Two consecutive cells at refinement level n are numbered with a stride of $2^{lrefine_max-n}$ where $1 \le n \le lrefine_max$.

The routine [[api reference]] provides a convenient way for the user to retrieve the location of a block or cell. A usage example is provided in the documentation for that routine. The user should retrieve accurate physical and grid coordinates by calling the routines [[api reference]], [[api reference]], [[api reference]] and [[api reference]], instead of calculating their own from local block information, since they take advantage of the cornerID scheme, and therefore avoid the possibility of introducing machine precision induced numerical drift in the calculations.

6.6.2 Grid Interpolation (and Averaging)

The adaptive grid requires data **interpolation** or **averaging** when the refinement level (*i.e.*, mesh resolution) changes in space or in time. ³ If during guardcell filling a block's neighbor has a coarser level of refinement, the neighbor's cells are used to **interpolate** guard cell values to the cells of the finer block. Interpolationis also used when filling the blocks of children newly created in the course of automatic refinement. Data **averaging** is used to adapt data in the opposite direction, *i.e.*, from fine to coarse.

In the AMR context, the term **prolongation** is used to refer to data interpolation (because it is used when the tree of blocks grows longer). Similarly, the term **restriction** is used to refer to fine-to-coarse data averaging.

The algorithm used for restriction is straightforward (equal-weight) averaging in Cartesian coordinates, but has to take cell volume factors into account for curvilinear coordinates; see ??.

PARAMESH supports various interpolationschemes, to which user-specified interpolation schemes can be added. Flash-X currently allows to choose between two interpolation schemes:

- 1. monotonic
- 2. native

The choice is made at setup time, see ??.

The versions of PARAMESH supplied with FLASH-X supply their own default interpolation scheme, which is used when FLASH-X is configured with the -gridinterpolation=native setup option (see ??). The default schemes are only appropriate for Cartesian coordinates. If FLASH-X is configured with curvilinear support, an alternative scheme (appropriate for all supported geometries) is compiled in. This so-called "monotonic" interpolation attempts to ensure that interpolation does not introduce small-scale non-monotonicity in the data. The order of "monotonic" interpolation can be chosen with the [[rpi reference]]runtime parameter. See ?? for some more details on prolongation for curvilinear coordinates. At setup time, monotonic interpolation is the default interpolation used.

6.6.2.1 Interpolation for mass-specific solution variables

To accurately preserve the total amount of conserved quantities, the interpolation routines have to be applied to solution data in **conserved**, *i.e.*, volume-specific, form. However, many variables are usually stored in the unk array in mass-specific form, *e.g.*, specific internal and total energies, velocities, and mass fractions. See ?? for how to use the optional TYPE attribute in a Config file's VARIABLE definitions to inform the Grid unit which variables are considered mass-specific.

FLASH-X provides three ways to deal with this:

- 1. Do nothing—i.e., assume that ignoring the difference between mass-specific and conserved form is a reasonable approximation. Depending on the smoothness of solutions in regions where refinement, derefinement, and jumps in refinement level occur, this assumption may be acceptable. This behavior can be forced by setting the [[rpi reference]] runtime parameter to .false.
- 2. Convert mass-specific variables to conserved form in all blocks throughout the physical domain before invoking a Grid function that may result in some data interpolation or restriction (refinement, derefinement, guardcell filling); and convert back after these functions return. Conversion is done by cell-by-cell multiplication with the density (i.e., the value of the "dens" variable, which should be declared as

VARIABLE dens TYPE: PER_VOLUME

in a Config file).

This behavior is available in both PARAMESH 2 and PARAMESH 4. It is enabled by setting the [[rpi reference]] runtime parameter and corresponds roughly to FLASH-X with conserved_var enabled.

³Particles and Physics units may make additional use of interpolation as part of their function, and the algorithms may or may not be different. This subsection only discusses interpolation automatically performed by the Grid unit on the fluid variables in a way that should be transparent to other units.

3. Convert mass-specific variables to conserved form only where and when necessary, from the Grid user's point of view as part of data interpolation. Again, conversion is done by cell-by-cell multiplication with the value of density. In the actual implementation of this approach, the conversion and back-conversion operations are closely bracketing the interpolation (or restriction) calls. The implementation avoids spurious back-and-forth conversions (i.e., repeated successive multiplications and divisions of data by the density) in blocks that should not be modified by interpolation or restriction.

This behavior is available only for PARAMESH 4. As of FLASH-X, this is the default behavior whenever available. It can be enabled explicitly (only necessary in setups that change the default) by setting the [[rpi reference]] runtime parameter.

6.6.3 Refinement

6.6.3.1 Refinement Criteria

The refinement criterion used by PARAMESH is adapted from Löhner (1987). Löhner's error estimator was originally developed for finite element applications and has the advantage that it uses a mostly local calculation. Furthermore, the estimator is dimensionless and can be applied with complete generality to any of the field variables of the simulation or any combination of them.

Flash-X Transition

FLASH-X does not define any refinement variables by default. Therefore simulations using AMR have to make the appropriate runtime parameter definitions in flash.par, or in the simulation's Config file. If this is not done, the program generates a warning at startup, and no automatic refinement will be performed. The mistake of not specifying refinement variables is thus easily detected. To define a refinement variable, use [[rpi reference]] (where # stands for a number from 1 to 4) in the flash.par file.

Löhner's estimator is a modified second derivative, normalized by the average of the gradient over one computational cell. In one dimension on a uniform mesh, it is given by

$$E_{i} = \frac{|u_{i+1} - 2u_{i} + u_{i-1}|}{|u_{i+1} - u_{i}| + |u_{i} - u_{i-1}| + \epsilon[|u_{i+1}| + 2|u_{i}| + |u_{i-1}|]},$$
(6.1)

where u_i is the refinement test variable's value in the *i*th cell. The last term in the denominator of this expression acts as a filter, preventing refinement of small ripples, where ϵ should be a small constant.

When extending this criterion to multidimensions, all cross derivatives are computed, and the following generalization of the above expression is used

$$E_{i_{1}i_{2}i_{3}} = \left\{ \frac{\sum_{pq} \left(\frac{\partial^{2}u}{\partial x_{p}\partial x_{q}} \Delta x_{p} \Delta x_{q} \right)^{2}}{\sum_{pq} \left[\left(\left| \frac{\partial u}{\partial x_{p}} \right|_{i_{p}+1/2} + \left| \frac{\partial u}{\partial x_{p}} \right|_{i_{p}-1/2} \right) \Delta x_{p} + \epsilon \frac{\partial^{2}|u|}{\partial x_{p}\partial x_{q}} \Delta x_{p} \Delta x_{q} \right]^{2}} \right\}^{1/2},$$
(6.2)

where the sums are carried out over coordinate directions, and where, unless otherwise noted, partial derivatives are evaluated at the center of the $i_1i_2i_3$ -th cell.

The estimator actually used in Flash-X's default refinement criterion is a modification of the above, as follows:

$$E_{i} = \frac{|u_{i+2} - 2u_{i} + u_{i-2}|}{|u_{i+2} - u_{i}| + |u_{i} - u_{i-2}| + \epsilon[|u_{i+2}| + 2|u_{i}| + |u_{i-2}|]},$$
(6.3)

where again u_i is the refinement test variable's value in the *i*th cell. The last term in the denominator of this expression acts as a filter, preventing refinement of small ripples, where ϵ is a small constant.

When extending this criterion to multidimensions, all cross derivatives are computed, and the following generalization of the above expression is used

$$E_{i_X i_Y i_Z} = \left\{ \frac{\sum_{pq} \left(\frac{\partial^2 u}{\partial x_p \partial x_q} \right)^2}{\sum_{pq} \left[\frac{1}{2 \Delta x_q} \left(\left| \frac{\partial u}{\partial x_p} \right|_{i_q + 1} + \left| \frac{\partial u}{\partial x_p} \right|_{i_q - 1} \right) + \epsilon \frac{|\vec{u_{pq}}|}{\Delta x_p \Delta x_q} \right]^2} \right\}^{1/2}, \tag{6.4}$$

where again the sums are carried out over coordinate directions, where, unless otherwise noted, partial derivatives are actually finite-difference approximations evaluated at the center of the $i_X i_J i_K$ -th cell, and $|u_{pq}|$ stands for an average of the values of |u| over several neighboring cells in the p and q directions.

The constant ϵ is by default given a value of 10^{-2} , and can be overridden through the [[rpi reference]] runtime parameters. Blocks are marked for refinement when the value of $E_{i_X i_Y i_Z}$ for any of the block's cells exceeds a threshold given by the runtime parameters [[rpi reference]], where the number # matching the number of the [[rpi reference]] runtime parameter selecting the refinement variable. Similarly, blocks are marked for derefinement when the values of $E_{i_X i_Y i_Z}$ for all of the block's cells lie below another threshold given by the runtime parameters [[rpi reference]].

Although PPM is formally second-order and its leading error terms scale as the third derivative, we have found the second derivative criterion to be very good at detecting discontinuities and sharp features in the flow variable u. When Particles (active or tracer) are being used in a simulation, their count in a block can also be used as a refinement criterion by setting [[rpi reference]] to true and setting [[rpi reference]] to the desired count.

6.6.3.2 Refinement Processing

Each processor decides when to refine or derefine its blocks by computing a user-defined error estimator for each block. Refinement involves creation of either zero or 2^d refined child blocks, while derefinement involves deletion of all of a parent's child blocks (2^d blocks). As child blocks are created, they are temporarily placed at the end of the processor's block list. After the refinements and derefinements are complete, the blocks are redistributed among the processors using a work-weighted Morton space-filling curve in a manner similar to that described by Warren and Salmon (1987) for a parallel treecode. An example of a Morton curve is shown in ??.

During the distribution step, each block is assigned a weight which estimates the relative amount of time required to update the block. The Morton number of the block is then computed by interleaving the bits of its integer coordinates, as described by Warren and Salmon (1987). This reordering determines its location along the space-filling curve. Finally, the list of all blocks is partitioned among the processors using the block weights, equalizing the estimated workload of each processor. By default, all leaf-blocks are weighted twice as heavily as all other blocks in the simulation.

6.6.3.3 Specialized Refinement Routines

Sometimes, it may be desirable to refine a particular region of the grid independent of the second derivative of the variables. This criterion might be, for example, to better resolve the flow at the boundaries of the domain, to refine a region where there is vigorous nuclear burning, or to better resolve some smooth initial condition. For curvilinear coordinates, regions around the coordinate origin or the polar z-axis may require special consideration for refinement. A collection of methods that can refine a (logically) rectangular region or a circular region in Cartesian coordinates, or can automatically refine by using some variable threshold, are available through the [[api reference]]. It is intended to be called from the [[api reference]] routine. The interface works by allowing the calling routine to pick one of the routines in the suite through an integer argument. The calling routine is also expected to populate the data structure specs before making the call. A copy of the file Grid_markRefineDerefine.F90 should be placed in the Simulation directory, and the interface file Grid_interface.F90 should be used in the header of the function.

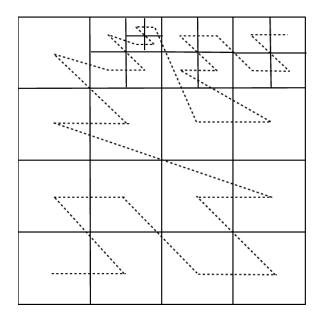


Figure 6.4: Morton space-filling curve for adaptive mesh grids.

6.7 GridMain Usage

The Grid unit has the largest API of all units, since it is the custodian of the bulk of the simulation data, and is responsible for most of the code housekeeping. The [[api reference]] routine, like all other Unit_init routines, collects the runtime parameters needed by the unit and stores values in the data module. If using UG, the [[api reference]] also creates the computational domain and the housekeeping data structures and initializes them. If using AMR, the computational domain is created by the [[api reference]] routine, which also makes a call to mesh package's own initialization routine. The physical variables are all owned by the Grid unit, and it initializes them by calling the [[api reference]] routine which applies the specified initial conditions to the domain. If using an adaptive grid, the initialization routine also goes through a few refinement iterations to bring the grid to desired initial resolution, and then applies the [[api reference]] function to bring all simulation variables to thermodynamic equilibrium. Even though the mesh-based variables are under Grid's control, all the physics units can operate on and modify them.

A suite of get/put accessor/mutator functions allows the calling unit to fetch or send data by the block. One option is to get a pointer [[api reference]], which gives unrestricted access to the whole block and the client unit can modify the data as needed. The more conservative but slower option is to get some portion of the block data, make a local copy, operate on and modify the local copy and then send the data back through the "put" functions. The Grid interface allows the client units to fetch the whole block ([[api reference]]), a partial or full plane from a block ([[api reference]]), a partial or full row ([[api reference]]), or a single point ([[api reference]]). Corresponding "put" functions allow the data to be sent back to the Grid unit after the calling routine has operated on it. Various getData functions can also be used to fetch some derived quantities such as the cell volume or face area of individual cells or groups of cells. There are several other accessor functions available to query the housekeeping information from the grid. For example [[api reference]] returns a list of blocks that meet the specified criterion such as being "LEAF" blocks in PARAMESH, or residing on the physical boundary.

In addition to the functions to access the data, the Grid unit also provides a collection of routines that drive some housekeeping functions of the grid without explicitly fetching any data. A good example of such routines is [[api reference]]. Here no data transaction takes place between Grid and the calling unit. The calling unit simply instructs the Grid unit that it is ready for the guard cells to be updated, and doesn't concern itself with the details. The [[api reference]] routine makes sure that all the blocks get the right data in their guardcells from their neighbors, whether they are at the same, lower or higher resolution, and if

instructed by the calling routine, also ensures that EOS is applied to them.

In large-scale, highly parallel Flash-X simulations with AMR, the processing of Grid_fillGuardCells calls may take up a significant part of available resource like CPU time, communication bandwidth, and buffer space. It can therefore be important to optimize these calls in particular. From Flash-X, [[api reference]] provides ways to

- operate on only a subset of the variables in unk (and facevarx, facevary, and facevarz), by masking out other variables;
- fill only some the **nguard** layers of guard cells that surround the interior of a block (while possibly excepting a "sweep" direction);
- combine guard cell filling with EOS calls (which often follow guard cell exchanges in the normal flow of execution of a simulation in order to ensure thermodynamical consistency in all cells, and which may also be very expensive), by letting Grid_fillGuardCells make the calls on cells where necessary;
- automatically determine masks and whether to call EOS, based on the set of variables that the calling code actually needs updated. by masking out other variables.

These options are controlled by OPTIONAL arguments, see [[api reference]] for documentation. When these optional arguments are absent or when a Grid implementation does not support them, Flash-X falls back to safe default behavior which may, however, be needlessly expensive.

Another routine that may change the global state of the grid is [[api reference]]. This function is called when the client unit wishes to update the grid's resolution. again, the calling unit does not need to know any of the details of the refinement process.

Flash-X Transition

As mentioned in ??, Flash-X allows every unit to identify scalar variables for checkpointing. In the Grid unit, the function that takes care of consolidating user specified checkpoint variable is [[api reference]]. Users can select their own variables to checkpoint by including an implementation of this function specific to their requirements in their Simulation setup directory.

6.8 GridParticles

Flash-X is primarily an Eulerian code, however, there is support for tracing the flow using Lagrangian particles. In Flash-X we have generalized the interfaces in the Lagrangian framework of the Grid unit in such a way that it can also be used for miscellaneous non-Eulerian data such as tracing the path of a ray through the domain, or tracking the motion of solid bodies immersed in the fluid. Flash-X also uses active particles with mass in cosmological simulations, and charged particles in a hybrid PIC solver. Each particle has an associated data structure, which contains fields such as its physical position and velocity, and relevant physical attributes such as mass or field values in active particles. Depending upon the time advance method, there may be other fields to store intermediate values. Also, depending upon the requirements of the simulation, other physical variables such as temperature etc. may be added to the data structure. The GridParticles subunit of the Grid unit has two sub-subunits of its own. The GridParticlesMove sub-subunit moves the data structures associated with individual particles when the particles move between blocks; the actual movement of the particles through time advancement is the responsibility of the Particles unit. Particles move from one block to another when their time advance places them outside their current block. In AMR, the particles can also change their block through the process of refinement and derefinement. The GridParticlesMap sub-subunit provides mapping between particles data and the mesh variables. The mesh variables are either cell-centered or face-centered, whereas a particle's position could be anywhere in the cell. The GridParticlesMap sub-subunit calculates the particle's properties at its position from the corresponding mesh variable values in the appropriate cell. When using active particles, this sub-subunit

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also maps the mass of the particles onto the specified mesh variable in appropriate cells. The next sections describe the algorithms for moving and mapping particles data.

6.8.1 GridParticlesMove

FLASH-X has implementations of three different parallel algorithms for moving the particles data when they are displaced from their current block. FLASH-X had an additional algorithm, Perfect Tree Level which made use of the oct-tree structure. However, because in all performance experiments it performed significantly worse than the other two algorithms, it is not supported currently in FLASH-X. The simplest algorithm, Directional algorithm is applicable only to the uniform grid when it is configured with one block per processor. This algorithm uses directional movement of data, and is easy because the directional neighbors are trivially known. The movement of particles data is much more challenging with AMR even when the grid is not refining. Since the blocks are at various levels of refinement at any given moment, a block may have more than one neighbor along one or more of its faces. The distribution of blocks based on space-filling curve is an added complication since the neighboring blocks along a face may reside at a nonneighboring processor The remaining two algorithmss included in FLASH-X implement GridParticlesMove subunit for the adaptive mesh; Point to Point and Sieve, of which only the Sieve algorithm is able to move the data when the mesh refines. Thus even when a user opts for the PointToPoint implementation for moving particles with time evolution, some part of the Sieve implementation must necessarily be included to successfully move the data upon refinement.

6.8.1.1 Directional Move

The Directional Move algorithm for moving particles in a Uniform Grid minimizes the number of communication steps instead of minimizing the volume of data moved. Its implementation has the following steps:

- 1. Scan particle positions. Place all particles with their x coordinate value greater than the block bounding box in the Rightmove bin, and place those with x coordinate less than block bounding box in Leftmove bin.
- 2. Exchange contents of Rightbin with the right block neighbor's Leftbin contents, and those of the Leftbin with left neighbor's Rightbin contents.
- 3. Merge newly arrived particles from step 2 with those which did not move outside their original block.
- 4. Repeat steps 1-3 for the y direction.
- 5. Repeat step 1-2 for the z direction.

At the end of these steps, all particles will have reached their destination blocks, including those that move to a neighbor on the corner. ?? illustrates the steps in getting a particle to its correct destination.

6.8.1.2 Point To Point Algorithm

A bitmap of the mesh maintained by the Bittree algorithm has complete information about the neighborhood of all the blocks on a processor. Thus it is possible to determine the processor and block number of the destination block for each particle. The PointToPoint implementation finds out the destinations for every particles that is getting displaced from its block. Particles going to local destination blocks are moved first. The remaining particles are sorted based on their destination processor number, followed by a couple of global operations that allow every processor to determine the number of particles it is expected to receive from all of the other processors. A processor then posts asynchronous receives for every source processor that had at least one particle to send to it. In the next step, the processor cycles through the sorted list of particles and sends them to the appropriate destinations using synchronous mode of communition.

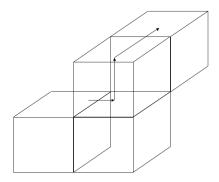


Figure 6.5: Moving one particle to a neighbor on the corner.

6.9 GridSolvers

The GridSolvers unit groups together subunits that are used to solve particular types of differential equations. Currently, there are two types of solvers: a parallel Fast Fourier Transform package (??) and various solvers for the Poisson equation (??).

6.9.0.1 Unit Test

The unit test for Pfft solver solves the following equation:

$$\nabla^2(\mathbf{F}) = -13.0 * \cos 2x * \sin 3y \tag{6.5}$$

The simplest analytical solution of this equation assuming no constants is

$$F = \cos 2x * \sin 3y \tag{6.6}$$

We discretize the domain by assuming xmin, ymin, zmin = 0, and $xmax, ymax, zmax = 2\pi$. The equation satisfies periodic boundary conditions in this formulation and FFT based poisson solve techniques can be applied. In the unit test we initialize one variable of the solution data with the function F, and another one with the right hand side of (??). We compute the forward real-to-complex transform of the solution data variable that is initialized with the right hand side of (??). This variable is then divided by $(k_i^2 + k_j^2 + k_k^2)$ where k_i, k_j and k_k are the wavenumbers at any point i,j,k in the domain. An inverse complex-to-real transform after the division should give the function F as result. Hence the unit test is considered successful if both the variables have matching values within the specified tolerance.

6.9.1 Poisson equation

The GridSolvers subunit contains several different algorithms for solving the general Poisson equation for a potential $\phi(\mathbf{x})$ given a source $\rho(\mathbf{x})$

$$\nabla^2 \phi(\mathbf{x}) = \alpha \rho(\mathbf{x}) \ . \tag{6.7}$$

Here α is a constant that depends upon the application. For example, when the gravitational Poisson equation is being solved, $\rho(\mathbf{x})$ is the mass density, $\phi(\mathbf{x})$ is the gravitational potential, and $\alpha = 4\pi G$, where G is Newton's gravitational constant.

6.9.1.1 Multipole Poisson solver

The multipole Poisson solver is based on a multipolar expansion of the source (mass for gravity, for example) distribution around a conveniently chosen center of expansion. The angular number L entering this expansion

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is a measure of how detailed the description of the source distribution will be on an angular basis. Higher L values mean higher angular resolution with respect to the center of expansion. The multipole Poisson solver is thus appropriate for spherical or nearly-spherical source distributions with isolated boundary conditions. For problems which require high spatial resolution throughout the entire domain (like, for example, galaxy collision simulations), the multipole Poisson solver is less suited, unless one is willing to go to extremely (computationally unfeasible) high L values. For stellar evolution, however, the multipole Poisson solver is the method of choice.

The new implementation of the multipole Poisson solver is located in the directory

source/Grid/GridSolvers/Multipole_new.

This implementation improves upon the original implemention in many ways: i) efficient memory layout ii) elimination of numerical over- and underflow errors for large angular momenta when using astrophysical (dimensions $\approx 10^9$) domains iii) elimination of subroutine call overhead (1 call per cell), iv) minimization of error due to non-statistical distributions of moments near the multipolar origin. The following paragraphs explain the new approach to the multipole solver and an explanation of the above improvements. Details about the theory of the new implementation of the Poisson solver can be found in Couch et al. (2013).

The multipole Poisson solver is appropriate for spherical or nearly-spherical source distributions with isolated boundary conditions. It currently works in 1D spherical, 2D spherical, 2D cylindrical, 3D Cartesian and 3D cylindrical. Symmetries can be specified for the 2D spherical and 2D cylindrical cases (a horizontal symmetry plane along the radial axis) and the 3D Cartesian case (assumed axisymmetric property). Because of the radial symmetry in the 1D spherical case, only the monopole term ($\ell = 0$) contributes, while for the 3D Cartesian axisymmetric, the 2D cylindrical and 2D spherical cases only the m = 0 moments need to be used (the other $m \neq 0$ moments effectively cancel out).

The multipole algorithm consists of the following steps. First, the center of the multipolar expansion \mathbf{x}_{cen} is determined via density-squared weighted integration over position:

$$\mathbf{x}_{\text{cen}} = \frac{\int \mathbf{x} \rho^2(\mathbf{x}) \, d\mathbf{x}}{\int \rho^2(\mathbf{x}) \, d\mathbf{x}}.$$
 (6.8)

We will take \mathbf{x}_{cen} as our origin. In integral form, Poisson's equation (??) becomes

$$\phi(\mathbf{x}) = -\frac{\alpha}{4\pi} \int \frac{\rho(\mathbf{x}')}{|\mathbf{x} - \mathbf{x}'|} d\mathbf{x}'. \tag{6.9}$$

The inverse radial distance part can be expanded in terms of Legendre polynomials

$$\frac{1}{|\mathbf{x} - \mathbf{x}'|} = \sum_{\ell=0}^{\infty} \frac{x_{<}^{\ell}}{x_{>}^{\ell+1}} P_{\ell}(\cos \gamma), \tag{6.10}$$

where $x_{<}(x_{>})$ indicate the smaller (larger) of the magnitudes and γ denotes the angle between \mathbf{x} and \mathbf{x}' . Note, that this definition includes those cases where both magnitudes are equal. The expansion is always convergent if $\cos \gamma < 1$. Expansion of the Legendre polynomials in terms of spherical harmonics gives

$$P_{\ell}(\cos \gamma) = \frac{4\pi}{2\ell + 1} \sum_{m=-\ell}^{+\ell} Y_{\ell m}^{*}(\theta', \phi') Y_{\ell m}(\theta, \phi), \tag{6.11}$$

where θ, ϕ and θ', ϕ' are the spherical angular components of \mathbf{x} and \mathbf{x}' about \mathbf{x}_{cen} . Defining now the regular $R_{\ell m}$ and irregular $I_{\ell m}$ solid harmonic functions

$$R_{\ell m}(x_{<}) = \sqrt{\frac{4\pi}{2\ell+1}} x_{<}^{\ell} Y_{\ell m}(\theta, \phi)$$
 (6.12)

$$I_{\ell m}(x_{>}) = \sqrt{\frac{4\pi}{2\ell+1}} \frac{Y_{\ell m}(\theta,\phi)}{x_{>}^{\ell+1}},$$
 (6.13)

we can rewrite Eq.(??) in the form

$$\phi(\mathbf{x}) = -\frac{\alpha}{4\pi} \int \sum_{\ell m} R_{\ell m}(x_{<}) I_{\ell m}^*(x_{>}) \rho(\mathbf{x}') d\mathbf{x}', \qquad (6.14)$$

where the summation sign is a shorthand notation for the double sum over all the allowed ℓ and m values. In Flash-X both the source and the potential are assumed to be cell-averaged quantities discretized on a block-structured mesh with varying cell size. The integration must hence be replaced by a summation over all leaf cells

$$\phi(q) = -\frac{\alpha}{4\pi} \sum_{q'} \sum_{\ell m} R_{\ell m}(q_{<}) I_{\ell m}^{*}(q_{>}) m(q'), \qquad (6.15)$$

where m denotes the cell's mass. Note, that the symbol q stands for cell index as well as its defining distance position from the expansion center in the computational domain. This discrete Poisson equation is incorrect. It contains the divergent q' = q term on the rhs. The q' = q contribution to the potential corresponds to the cell self potential $\phi_{Self}(q)$ and is divergent in our case because all the cell's mass is assumed to be concentrated at the cell's center. The value of this divergent term can easily be calculated from Eq.(??) by setting $\cos \gamma = 1$:

$$\phi_{Self}(q) = m(q) \frac{L+1}{x_q}, \tag{6.16}$$

where m is the cell's mass, L the highest angular number considered in the expansion and x_q the radial distance of the cell center from the expansion center. To avoid this divergence problem, we evaluate the potentials on each face of the cell and form the average of all cell face potentials to get the cell center potential. Eq.(??) will thus be replaced by

$$\phi(q) = \frac{1}{n_F} \sum_{F} \phi(\mathbf{x}_F) \tag{6.17}$$

and

$$\phi(\mathbf{x}_F) = -\frac{\alpha}{4\pi} \sum_{q'} \sum_{\ell m} R_{\ell m}([q', x_F]_<) I_{\ell m}^*([q', x_F]_>) m(q'), \tag{6.18}$$

where \mathbf{x}_F is the cell face radial distance from the expansion center and $[q', x_F]_{<}$ denotes the larger of the magnitudes between the cell center radial distance q' and the cell face radial distance x_F . Splitting the summation over cells in two parts

$$\phi(\mathbf{x}_F) = -\frac{\alpha}{4\pi} \left\{ \sum_{q' \le x_F} \sum_{\ell m} \left[R_{\ell m}(q') m(q') \right] I_{\ell m}^*(\mathbf{x}_F) + \sum_{q' > x_F} \sum_{\ell m} R_{\ell m}(\mathbf{x}_F) \left[I_{\ell m}^*(q') m(q') \right] \right\}, \tag{6.19}$$

and defining the two moments

$$M_{\ell m}^{R}(\mathbf{x}_{F}) = \sum_{q' < x_{F}} R_{\ell m}(q') m(q')$$
 (6.20)

$$M_{\ell m}^{I}(\mathbf{x}_{F}) = \sum_{q'>x_{F}} I_{\ell m}(q')m(q'),$$
 (6.21)

we obtain

$$\phi(\mathbf{x}_F) = -\frac{\alpha}{4\pi} \left[\sum_{\ell m} M_{\ell m}^R(\mathbf{x}_F) I_{\ell m}^*(\mathbf{x}_F) + \sum_{\ell m} M_{\ell m}^{I*}(\mathbf{x}_F) R_{\ell m}(\mathbf{x}_F) \right]$$
(6.22)

and using vector notation

$$\phi(\mathbf{x}_F) = -\frac{\alpha}{4\pi} \left[\mathbf{M}^R(\mathbf{x}_F) \cdot \mathbf{I}^*(\mathbf{x}_F) + \mathbf{M}^{I*}(\mathbf{x}_F) \cdot \mathbf{R}(\mathbf{x}_F) \right]. \tag{6.23}$$

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We now change from complex to real formulation. We state this for the regular solid harmonic functions, the same reasoning being applied to the irregular solid harmonic functions and all their derived moments. The regular solid harmonic functions can be split into a real and imaginary part

$$R_{\ell m} = R_{\ell m}^c + i R_{\ell m}^s. (6.24)$$

The labels 'c' and 's' are shorthand notations for 'cosine' and 'sine', reflecting the nature of the azimuthal function of the corresponding real spherical harmonics. When inserting (??) into (??) all cosine and sine mixed terms of the scalar products cancel out. Also, due to the symmetry relations

$$R_{\ell,-m}^c = (-1)^m R_{\ell m}^c (6.25)$$

$$R_{\ell,-m}^{s} = -(-1)^{m} R_{\ell m}^{s} \tag{6.26}$$

we can restrict ourselves to the following polar angle number ranges

$$c: \ell \ge 0, \ell \ge m \ge 0$$
 (6.27)

$$s : \ell \ge 1 , \ell \ge m \ge 1. \tag{6.28}$$

The real formulation of (??) becomes then

$$\phi(\mathbf{x}_F) = -\frac{\alpha}{4\pi} \left\{ \begin{bmatrix} \mathbf{M}^{Rc}(\mathbf{x}_F) \\ \mathbf{M}^{Rs}(\mathbf{x}_F) \end{bmatrix} \cdot \mathbf{\Delta} \begin{bmatrix} \mathbf{I}^c(\mathbf{x}_F) \\ \mathbf{I}^s(\mathbf{x}_F) \end{bmatrix} + \begin{bmatrix} \mathbf{M}^{Ic}(\mathbf{x}_F) \\ \mathbf{M}^{Is}(\mathbf{x}_F) \end{bmatrix} \cdot \mathbf{\Delta} \begin{bmatrix} \mathbf{R}^c(\mathbf{x}_F) \\ \mathbf{R}^s(\mathbf{x}_F) \end{bmatrix} \right\}, \tag{6.29}$$

which, when compared to $(\ref{eq:constrain})$, shows, that all vectors now contain a cosine and a sine section. The Δ matrix is a diagonal matrix whose elements are equal to 2 for $m \neq 0$ and 1 otherwise, i.e.:

$$\Delta = diag(2 - \delta_{m0}). \tag{6.30}$$

The recursion relations for calculating the solid harmonic vectors are

$$R_{00}^c = 1 ag{6.31}$$

$$R_{\ell\ell}^c = -\frac{xR_{\ell-1,\ell-1}^c - yR_{\ell-1,\ell-1}^s}{2\ell}$$
(6.32)

$$R_{\ell\ell}^s = -\frac{yR_{\ell-1,\ell-1}^c + xR_{\ell-1,\ell-1}^s}{2\ell}$$
(6.33)

$$R_{\ell m}^{c/s} = \frac{(2\ell - 1)zR_{\ell-1,m}^{c/s} - r^2R_{\ell-2,m}^{c/s}}{(\ell+m)(\ell-m)}, \quad 0 \le m < \ell$$
(6.34)

and

$$I_{00}^{c} = \frac{1}{r} (6.35)$$

$$I_{\ell\ell}^c = -(2\ell - 1)\frac{xI_{\ell-1,\ell-1}^c - yI_{\ell-1,\ell-1}^s}{r^2}$$
 (6.36)

$$I_{\ell\ell}^s = -(2\ell - 1)\frac{yI_{\ell-1,\ell-1}^c + xI_{\ell-1,\ell-1}^s}{r^2}$$
(6.37)

$$I_{\ell m}^{c/s} = \frac{(2\ell - 1)zI_{\ell-1,m}^{c/s} - \left[(\ell - 1)^2 - m^2\right]I_{\ell-2,m}^{c/s}}{r^2}, \quad 0 \le m < \ell$$
(6.38)

in which x, y, z are the cartesian location coordinates of the cell face and $r^2 = x^2 + y^2 + z^2$. For geometries depending on polar angles one must first calculate the corresponding cartesian coordinates for each cell before applying the recursions. In Flash-X, the order of the two cosine and sine components for each solid harmonic vector is such that ℓ precedes m. This allows buildup of the vectors with maximum number of unit strides. The same applies of course for the assembly of the moments. For 2D cylindrical and 2D spherical geometries only the m=0 parts of both recursions are needed, involving only the cartesian z coordinate and r^2 . Symmetry along the radial axes of these 2D geometries inflicts only the sign change $z \to -z$, resulting

in the symmetry relations $R^c_{\ell 0} \to R^c_{\ell 0}$ for even ℓ and $R^c_{\ell 0} \to -R^c_{\ell 0}$ for odd ℓ , the same holding for the irregular solid harmonic vector components. Thus symmetry in 2D can effectively be treated by halving the domain size and multiplying each even ℓ moments by a factor of 2 while setting the odd ℓ moments equal to 0. For 3D cartesian geometries introduction of symmetry is far more complicated since all m components need to be taken into account. It is not sufficient to simply reduce the domain to the appropriate size and multiply the moments by some factor, but rather one would have to specify the exact symmetry operations intended (generators of the symmetry group O_h or one of its subgroups) in terms of their effects on the x, y, z cartesian basis. The resulting complications in calculating symmetry adapted moments outweighs the computational gain that can be obtained from it. Options for 3D symmetry are thus no longer available in the improved Flash-X multipole solver. The 'octant' symmetry option from the old multipole solver, using only the monopole $\ell=0$ term, was too restrictive in its applicability (exact only for up to angular momenta $\ell = 3$ due to cancellation of the solid harmonic vector components).

From the above recursion relations (??-??), the solid harmonic vector components are functions of $x^i y^j z^k$ monomials, where $i+j+k=\ell$ for the **R** and (formally) $i+j+k=-(\ell+1)$ for the **I**. For large astrophysical coordinates and large ℓ values this leads to potential computational over- and underflow. To get independent of the size of both the coordinates and ℓ we introduce a damping factor Dx, Dy, Dz for the coordinates for each solid harmonic type before entering the recursions. D will be chosen such that for the highest specified $\ell = L$ we will have approximately a value close to 1 for both solid harmonic components:

$$R_{Lm}^{c/s} \approx 1$$
 (6.39)
 $I_{Lm}^{c/s} \approx 1$. (6.40)

$$I_{Lm}^{c/s} \approx 1. ag{6.40}$$

This ensures proper handling of size at the solid harmonic function evaluation level and one does not have to rely on size cancellations at a later stage when evaluating the potential via Eq. (??). We next state the evaluation of the damping factor D. Due to the complicated nature of the recursions, the first step is to find solid harmonic components which have a simple structure. To do this, consider a cell face with x, y = 0 and $z \neq 0$. Then $r^2 = z^2$, |z| = r and only the m = 0 components are different from zero. An explicit form can be stated for the absolute values of these components in terms of r:

$$|R_{\ell 0}| = \frac{r^{\ell}}{\ell!} \tag{6.41}$$

$$|I_{\ell 0}| = \frac{\ell!}{r^{\ell+1}}. (6.42)$$

Since $r = \sqrt{x^2 + y^2 + z^2}$, damping of the coordinates with D results in a damped radial cell face distance Dr. Inserting this result into (??) and (??) and imposing conditions (??) and (??) results in

$$D_R = \frac{1}{r} \sqrt[L]{L!} \approx \frac{1}{r} \frac{L}{e} \sqrt[2L]{2\pi L}$$

$$(6.43)$$

$$D_I = \frac{1}{r} \sqrt[L+1]{L!} \approx \frac{1}{r} \frac{L}{e} \sqrt[2L+2]{\frac{2\pi e^2}{L}},$$
 (6.44)

where the approximate forms are obtained by using Stirling's factorial approximation formula for large L. In Flash-X only the approximate forms are computed for D_R and D_I to avoid having to deal with factorials of large numbers.

From the moment defining equations (??) and (??) we see, that the moments are sums over subsets of cell center solid harmonic vectors multiplied by the corresponding cell mass. From Eq. (??) it follows that for highest accuracy, the moments should be calculated and stored for each possible cell face. For high refinement levels and/or 3D simulations this would result in an unmanageable request for computer memory. Several cell face positions have to be bundled into radial bins Q defined by lower and upper radial bounds. Once a cell center solid harmonic vector pair $\mathbf{R}(q)$ and $\mathbf{I}(q)$ for a particular cell has been calculated, its radial bin location $q \to Q$ is determined and its contribution is added to the radial bin moments $\mathbf{M}^R(Q)$ 6.9. GRIDSOLVERS 81

and $\mathbf{M}^{I}(Q)$. The computational definition of the radial bin moments is

$$\mathbf{M}^{R}(Q) = \sum_{q \leq Q} \mathbf{R}(q)m(q)$$

$$\mathbf{M}^{I}(Q) = \sum_{q \geq Q} \mathbf{I}(q)m(q),$$
(6.45)

$$\mathbf{M}^{I}(Q) = \sum_{q \ge Q} \mathbf{I}(q)m(q), \tag{6.46}$$

where $q \leq Q$ means including all cells belonging to Q and all radial bins with lower radial boundaries than Q. The two basic operations of the multipole solver are thus: i) assembly of the radial bin moments and ii) formation of the scalar products via Eq. (??) to obtain the potentials. The memory declaration of the moment array should reflect the way the individual moment components are addressed and the most efficient layout puts the angular momentum indices in rows and the radial bin indices in columns.

How do we extract moments $\mathbf{M}^{R}(\mathbf{x})$ and $\mathbf{M}^{I}(\mathbf{x})$ at any particular position \mathbf{x} inside the domain (and, in particular, at the cell face positions \mathbf{x}_F), which are ultimately needed for the potential evaluation at that location? Assume that the location \mathbf{x} corresponds to a particular radial bin $\mathbf{x} \to Q$. Consider the three consecutive radial bins Q-1, Q and Q+1, together with their calculated moments:

$$\mathbf{M}^{R}(Q-1) \mid \mathbf{M}^{R}(Q) \mid \mathbf{M}^{R}(Q+1)
\mathbf{M}^{I}(Q-1) \mid \mathbf{M}^{I}(Q) \mid \mathbf{M}^{I}(Q+1)$$
(6.47)

Let us concentrate on the Q bin, whose lower and upper radial limits are shown as solid vertical lines. The radial distance corresponding to \mathbf{x} splits the Q bin into two parts: the left fractional part, denoted R_{frac} , and the right fractional part, denoted I_{frac} . Since both $\mathbf{M}^R(Q-1)$ and $\mathbf{M}^I(Q+1)$ are completely contained respectively in $\mathbf{M}^{R}(Q)$ and $\mathbf{M}^{I}(Q)$, the moments at \mathbf{x} be approximately evaluated as:

$$\mathbf{M}^{R}(\mathbf{x}) = \mathbf{M}^{R}(Q-1) + R_{frac} \left[\mathbf{M}^{R}(Q) - \mathbf{M}^{R}(Q-1) \right]$$
(6.48)

$$\mathbf{M}^{I}(\mathbf{x}) = \mathbf{M}^{I}(Q+1) + I_{frac} \left[\mathbf{M}^{I}(Q) - \mathbf{M}^{I}(Q+1) \right], \tag{6.49}$$

The extraction of the moments via (??) and (??) is of course an approximation that relies on the statistically dense distribution of the individual cell center moments inside each radial bin. For bins which are reasonably far away from the expansion center this statistical approximation is valid but for those close to the expansion center the statistical distribution does not hold and calculating the moments via the above scheme introduces a large statistical error. The way out of this problem is to move from a statistical radial bin description around the expansion center to a more discrete one, by constructing very narrow isolated radial bins. The code is thus forced to analyze the detailed structure of the geometrical domain grid surrounding the expansion center and to establish the inner radial zone of discrete distributed radial bins. The statistical radial bins are then referred to as belonging to the outer radial zone(s).

While the structure of the inner radial zone is fixed due to the underlying geometrical grid, the size of each radial bin in the outer radial zones has to be specified by the user. There is at the moment no automatic derivation of the optimum (accuracy vs memory cost) bin size for the outer zones. There are two types of radial bin sizes defined for the Flash-X multipole solver: i) exponentially and/or ii) logarthmically growing:

exponential bin size upper radial limit =
$$s \cdot \Delta r \cdot Q^t$$
 (6.50)

logarithmic bin size upper radial limit =
$$s \cdot \Delta r \cdot \frac{e^{tQ} - 1}{e^t - 1}$$
. (6.51)

In these definitions, Δr is a small distance 'atomic' (basic unit) radial measure, defined as half the geometric mean of appropriate cell dimensions at highest refinement level, s is a scalar factor to optionally increase or decrase the atomic unit radial measure and $Q=1,2,\ldots$ is a local bin index counter for each outer zone. The atomic radial distance Δr is calculated for each individual domain geometry as follows:

$$\begin{array}{c|cccc} \hline \text{Domain Geometry} & \Delta r \\ \hline \hline 3D \text{ cartesian} & \frac{1}{2}\sqrt[3]{\Delta x \Delta y \Delta z} \\ 3D \text{ cylindrical} & \frac{1}{2}\sqrt{\Delta R \Delta z} \\ 2D \text{ cylindrical} & \frac{1}{2}\sqrt{\Delta R \Delta z} \\ 2D \text{ spherical} & \frac{1}{2}\Delta R \\ 1D \text{ spherical} & \frac{1}{2}\Delta R \\ \end{array} , \tag{6.52}$$

where $\Delta x, \Delta y, \Delta z$ are the usual cartesian cell dimensions and ΔR is the radial cell dimension. Note, that since Δr measures a basic radial unit along the radial distance from the expansion center (which, for approximate spherical problems, is located close to the domain's geometrical origin), only those cell dimensions for calculating each Δr are taken, which are directly related to radial distances from the geometrical domain origin. For 3D cylindrical domain geometries for example, only the radial cylindrical and z-coordinate cell dimensions determine the 3D radial distance from the 3D cylindrical domain origin. The angular coordinate is not needed. Likewise for spherical domains only the radial cell coordinate is of importance. Definitions (??) and (??) define the upper limit of the radial bins. Hence in order to obtain the true bin size for the Q-th bin one has to subtract its upper radial limit from the corresponding one of the (Q-1)-th bin:

$$Q$$
-th exponential bin size $= s \cdot \Delta r \cdot [Q^t - (Q-1)^t]$ (6.53)

Q-th logarithmic bin size
$$= s \cdot \Delta r \cdot e^{t(Q-1)}$$
. (6.54)

In principle the user can specify as many outer zone types as he/she likes, each having its own exponential or logarithmic parameter pair $\{s, t\}$.

Multithreading of the code is currently enabled in two parts: 1) during moment evaluation and 2) during potential evaluation. The threading in the moment evaluation section is achieved by running multiple threads over separate, non-conflicting radial bin sections. Moment evaluation is thus organized as a single loop over all relevant radial bins on each processor. Threading over the potential evaluation is done over blocks, as these will address different non-conflicting areas of the solution vector.

The improved multipole solver was extensively tested and several runs have been performed using large domains (> 10^{10}) and extremely high angular numbers up to L = 100 for a variety of domain geometries. Currently, the following geometries can be handled: 3D cartesian, 3D cylindrical, 2D cylindrical, 2D spherical and 1D spherical. The structure of the code is such that addition of new geometries, should they ever be needed by some applications, can be done rapidly.

6.9.1.2 Multipole Poisson solver unit test (MacLaurin spheroid)

The first unit test for the multipole Poisson solver is based on the MacLaurin spheroid analytical gravitational solution given in section ??. The unit test sets up a spheroid with uniform unit density and determines both the analytical and numerical gravitational fields. The absolute relative error based on the analytical solution is formed for each cell and the maximum of all the absolute errors is compared to a predefined error tolerance value for a particular uniform refinement level. The multipole unit test runs in 2D cylindrical, 2D spherical, 3D cartesian and 3D cylindrical geometries and threaded multipole unit tests are also available.

6.9.1.3 Multigrid Poisson solver

6.9.2 Using the Poisson solvers

The GridSolvers subunit solves the Poisson equation ((??)). Two different elliptic solvers are supplied with Flash-X: a multipole solver, suitable for approximately spherical source distributions, and a multigrid solver, which can be used with general source distributions. The multipole solver accepts only isolated boundary conditions, whereas the multigrid solver supports Dirichlet, given-value, Neumann, periodic, and isolated boundary conditions. Boundary conditions for the Poisson solver are specified using an argument to the [[api reference]] routine which can be set from different runtime parameters depending on the physical context in which the Poisson equation is being solved. The Grid_solvePoisson routine is the primary entry point to the Poisson solver module and has the following interface

```
call Grid_solvePoisson (iSoln, iSrc, bcTypes(6), bcValues(2,6), poisfact),
```

where iSoln and iSrc are the integer-valued indices of the solution and source (density) variables, respectively. bcTypes(6) is an integer array specifying the type of boundary conditions to employ on each of the (up to) 6 sides of the domain. Index 1 corresponds to the -x side of the domain, 2 to +x, 3 to -y, 4 to +y, 5 to -z, and 6 to +z. The following values are accepted in the array

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Table 6.3 :	Runtime	parameters	used	with	poisson	multipole.
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Variable	Type	Default	Description
mpole_lmax	integer	10	Maximum multipole moment
quadrant	logical	.false.	Use symmetry to solve a single quadrant in 2D axisymmetric cylindrical (r, z) coordinates, instead of a half domain.

bcTypes	Type of boundary condition
0	Isolated boundaries
1	Periodic boundaries
2	Dirichlet boundaries
3	Neumann boundaries
4	Given-value boundaries

Not all boundary types are supported by all solvers. In this release, bcValues(2,6) is not used and can be filled arbitrarily. Given-value boundaries are treated as Dirichlet boundaries with the boundary values subtracted from the outermost interior cells of the source; for this case the solution variable should contain the boundary values in its first layer of boundary cells on input to $Grid_solvePoisson$. It should be noted that if PARAMESH is used, the values must be set for all levels. Finally, poisfact is real-valued and indicates the value of α multiplying the source function in ((??)).

When solutions found using the Poisson solvers are to be differenced (e.g., in computing the gravitational acceleration), it is strongly recommended that for AMR meshes, quadratic (or better) spatial interpolationat fine-coarse boundaries is chosen. (For PARAMESH, this is automatically the case by default, and is handled correctly for Cartesian as well as the supported curvilinear geometries. But note that the default interpolation implementation may be changed at configuration time with the '-gridinterpolation=...'setup option; and with the default implementation, the interpolation order may be lowered with the [[rpi reference]] runtime parameter.) If the order of the gridinterpolation of the mesh is not of at least the same order as the differencing scheme used in places like [[api reference]], unphysical forces will be produced at refinement boundaries. Also, using constant or linear grid interpolation may cause the multigrid solver to fail to converge.

6.9.2.1 Multipole (original version)

The poisson/multipole sub-module takes two runtime parameters, listed in ??. Note that storage and CPU costs scale roughly as the square of mpole_lmax, so it is best to use this module only for nearly spherical matter distributions.

6.9.2.2 Multipole (improved version)

To include the new multipole solver in a simulation, the best option is to use the shortcut +newMpole at setup command line, effectively replacing the following setup options:

- -with-unit=Grid/GridSolvers/Multipole_new
- -with-unit=physics/Gravity/GravityMain/Poisson/Multipole
- -without-unit=Grid/GridSolvers/Multipole

The improved multipole solver currently accepts only two setup parameters, either one switching on multithreading:

- threadBlockList: enables multithreaded compilation and execution.
- threadWithinBlock: enables multithreaded compilation and execution.

The names of these two setup parameters are missleading, since there is only one universal threading strategy used. The use of these two setup parameters is a temporary solution and will be replaced in near future by only one setup parameter.

The improved multipole solver takes several runtime parameters, whose functions are explained in detail below, together with comments about expected time and memory scaling.

- [[rpi reference]]: The maximum angular moment L to be used for the multipole Poisson solver. Depending on the domain geometry, the memory and time scaling factors due to this variable alone are:
 i) 3D cartesian, 3D cylindrical → (L + 1)(L + 1), ii) 3D cartesian axisymmetric, 2D cylindrical, 2D spherical → (L + 1), iii) 1D spherical → 1. Assuming no memory limitations, the multipole solver is numerically stable for very large L values. Runs up to L = 100 for 3D cartesian domains have been performed. For 2D geometries, L = 1000 was the maximum tested.
- [[rpi reference]]: In 2D coordinates, this runtime parameter enables the user to specify a plane of symmetry along the radial part of the domain coordinates. In effect, this allows a reduction of the computational domain size by one half. The code internally computes the multipole moments as if the other symmetric part is present, i.e. no memory or execution time savings can be achieved by this runtime parameter.
- [[rpi reference]]: Forces rotational invariance around the main (z) axis in 3D cartesian domains. The assumed rotational invariance in the (x,y) plane effectively cancels all $m \neq 0$ multipole moments and one can restrict the calculation to the m=0 multipole moments only. The time and memory savings compared to a asymmetric 3D cartesian run is thus about a factor of (L+1). For 3D cylindrical domains, rotational invariance in the (x,y) plane is equivalent of setting up the corresponding 2D cylindrical domain, hence this runtime parameter is not honored for 3D cylindrical domains, and the user is informed about the 3D to 2D cylindrical domain reduction possibility.
- [[rpi reference]]: This parameter is meant mainly for debugging purposes. It prints the entire moment array for each radial bin for each time step. This option should be used with care and for small problems only. The output is printed to a text file named '
basenm>_dumpMoments.txt', where < basenm> is the base name given for the output files.
- [[rpi reference]]: This parameter enables showing all detailed radial bin information at each time step. This option is especially useful for optimizing the radial bin sizes. The output is written to the text file '
basenm>_printRadialInfo.txt'.
- [[rpi reference]]: Controls switching on/off the radial inner zone. If it is set .true., the inner zone will not be recognized and all inner zone radii will be treated statistically. This parameter is meant only for performing some error analysis. For production runs it should always be at its default value of false. Otherwise errors will be introduced in calculating the moments near the expansion center.
- [[rpi reference]]: The size defining the discrete inner zone. The size is given in terms of the inner zone smallest (atomic) radius, which is determined at each time step by analyzing the domain grid structure around the multipolar origin (expansion center). Only very rarely will this value ever have to be changed. The default setting is very conservative and only under unusual circumstances (ex: highly nonuniform grid around the expansion center) this might be necessary. This value needs to be an integer, as it is used by the code to define dimensions of certain arrays. Note, that by giving this runtime parameter a large integer value (¿ 1000 for domain refinement levels up to 5) one can enforce the code to use only non-statistical radial bins.
- [[rpi reference]]: Defines the inner zone radial bin size for the inner zone in terms of the inner zone smallest (atomic) radius. Two inner zone radii will be considered different, if they are more than this resolution value apart. A very tiny number (for example 10⁻⁸) will result in a complete separation of all inner zone radii into separate radial bins. The default value of 0.1 should never be surpassed, and any attempt to do so will stop the program with the appropriate information to the user. Likewise with a meaningless resolution value of 0.

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• [[rpi reference]]: The maximum number of outer radial zones to be used. In contrast to the inner radial zone, the outer radial zones are much more important for the user. Their layout defines the performance of the multipole solver both in cpu time spent and accuracy of the potential obtained at each cell. The default value of 1 outer radial zone at maximum refinement level leads to high accuracy, but at the same time can consume quite a bit of memory, especially for full 3D runs. In these cases the user can specify several outer radial zones each having their own radial bin size determination rule.

- [[rpi reference]]: The fraction of the maximum domain radius defining the n-th outer zone maximum radial value. The total number of fractions given must match the maximum number of outer radial zones specified and the fractions must be in increasing order and less than unity as we move from the 1st outer zone upwards. The last outer zone must always have a fraction of exactly 1. If not, the code will enforce it.
- [[rpi reference]]: String value containing the outer radial zone type for the n-th outer zone. If set to 'exponential', the radial equation $r(Q) = s \cdot \Delta r \cdot Q^t$, defining the upper bound radius of the Q-th radial bin in the n-th outer zone, is used. If set to 'logarithmic', the radial equation $r(Q) = s \cdot \Delta r \cdot (e^{Qt} 1)/(e^t 1)$ is used. In these equations Q is a local radial bin counting index for each outer zone and s, t are parameters defining size and growth of the outer zone radial bins (see below).
- [[rpi reference]]: The scalar value s in the n-th outer radial zone equation $r(Q) = s \cdot \Delta r \cdot Q^t$ or $r(Q) = s \cdot \Delta r \cdot (e^{Qt} 1)/(e^t 1)$. The scalar is needed to be able to increase (or decrease) the size of the first radial bin with respect to the default smallest outer zone radius Δr .
- [[rpi reference]]: The exponent value t in the n-th outer radial zone equations $r(Q) = s \cdot \Delta r \cdot Q^t$ or $r(Q) = s \cdot \Delta r \cdot (e^{Qt} 1)/(e^t 1)$. The exponent controls the growth (shrinkage) in size of each radial bin with increasing bin index. For the first equation, growing will occur for t > 1, shrinking for t < 1 and same size for t = 1. For the logarithmic equation, growing will occur for t > 0, shrinking for t < 0, but the same size option t = 0 will not work because the denominator becomes undefined. The same size option must hence be treated using the exponential outer zone type choice.

• Runtime parameter types, defaults and options:

Parameter	Type	Default	Options
[[rpi reference]]	integer	0	> 0
[[rpi reference]]	logical	false	true
[[rpi reference]]	logical	false	true
[[rpi reference]]	logical	false	true
[[rpi reference]]	logical	false	true
[[rpi reference]]	logical	false	true
[[rpi reference]]	integer	16	> 0
[[rpi reference]]	real	0.1	less than 0.1 and > 0.0
[[rpi reference]]	integer	1	> 1
[[rpi reference]]	real	1.0	less than 1.0 and > 0.0
[[rpi reference]]	string	"exponential"	"logarithmic"
[[rpi reference]]	real	1.0	> 0.0
[[rpi reference]]	real	1.0	> 0.0 (exponential)
	real	-	any $\neq 0$ (logarithmic)

6.9.2.3 Multigrid

The Grid/GridSolvers/Multigrid module is appropriate for general source distributions. It solves Poisson's equation for 1, 2, and 3 dimensional problems with Cartesian geometries. It only supports the AMReX Grid in the current version (See AMReX documentation for more detail). It may be included by setup or Config by including:

physics/Gravity/GravityMain/Poisson/Multigrid

The multigrid solver may also be included stand-alone using:

Grid/GridSolvers/Multigrid

6.9.3 HYPRE

As a part of implicit time advancement we end up with a system of equations that needs to be solved at every time step. In Flash-X the HYPRE linear algebra package is used to solve these systems of equations. Therefore it is necessary to install Hypre if this capability of Flash-X is to be used.

[[api reference]] is the API function which solves the system of equations. This API is provided by both the split and unsplit solvers. The unsplit solver uses HYPRE to solve the system of equations and split solver does a direct inverse using Thomas algorithm. Note that the split solver relies heavily on PFFT infrastructure for data exchange and a significant portion of work in split Grid_advanceDiffusion involves PFFT routines. In the unsplit solver the data exchange is implicitly done within HYPRE and is hidden.

The steps in unsplit Grid_advanceDiffusion are as follows:

- Setup HYPRE grid object
- Exchange Factor B
- Set initial guess
- Compute HYPRE Matrix M such that B = MX
- Compute RHS Vector B
- Compute matrix A
- Solve system AX = B
- Update solution (in Flash-X)

Mapping UG grid to HYPRE matrix is trivial, however mapping PARAMESH grid to a HYPRE matrix can be quite complicated. The process is simplified using the grid interfaces provided by HYPRE.

- Struct Grid interface
- SStruct Grid interface
- IJ System interface

The choice of an interface is tightly coupled to the underlying grid on which the problem is being solved. We have chosen the SSTRUCT interface as it is the most compatible with the block structured AMR mesh in Flash-X. Two terms commonly used in HYPRE terminology are part and box. We define these terms in equivalent Flash-X terminology. A HYPRE box object maps directly to a leaf block in Flash-X. The block is then defined by it's extents. In Flash-X this information can be computed easily using a combination of Grid_getBlkCornerID and Grid_getBlkIndexLimits.All leaf blocks at a given refinement level form a HYPRE part. So number of parts in a typical Flash-X grid would be give by,

```
nparts = leaf_block(lrefine_max) - leaf_block(lrefine_min) + 1
```

So, if a grid is fully refined or UG, nparts = 1. However, there could still be more then one box object.

Setting up the HYPRE grid object is one of the most important step of the solution process. We use the SSTRUCT interface provided in HYPRE to setup the grid object. Since the HYPRE Grid object is mapped directly with FLASH-X grid, whenever the FLASH-X grid changes the HYPRE grid object needs to 6.9. GRIDSOLVERS 87

be updated. Consequently with AMR the HYPRE grid setup might happen multiple times.

Setting up a HYPRE grid object is a two step process,

- Creating stenciled relationships.
- Creating Graph relationships.

Stenciled relationships typically exist between leaf blocks at same refinement level (intra part) and graph relationships exist between leaf blocks at different refinement levels (inter part). The fine-coarse boundary is handled in such a way that fluxes are conserved at the interface (see ?? for details). UG does not require any graph relationships.

Whether a block needs a graph relationship depends on the refinement level of it's neighbor. While this information is not directly available in PARAMESH, it is possible to determine whether the block neighbor is coarser or finer. Combining this information with the constraint of at best a factor of two jump in refinement at block boundaries, it is possible to compute the part number of a neighbor block, which in turn determines whether we need a graph. Creating a graph involves creating a link between all the cells on the block boundary.

Once the grid object is created, the matrix and vector objects are built on the grid object. The diffusion solve needs uninterpolated data from neighbor blocks even when there is a fine-coarse boundary, therefore it cannot rely upon the guardcell fill process. A two step process is used to handle this situation,

- Since HYPRE has access to X(at n, *i.e.*, initial guess), the RHS vector B can be computed as MX where M is a modified Matrix.
- Similarly the value of Factor B can be shared across the fine-coarse boundary by using Grid_conserveFluxes, the fluxes need to be set in a intuitive to way to achieve the desired effect.

With the computation of Vector B (RHS), the system can be solved using HYPRE and UNK can be updated.

6.9.3.1 HYPRE Solvers

In FLASH-X we use the HYPRE PARCSR storage format as this exposes the maximum number of iterative solvers.

Table 6.4: Solvers, Preconditioners combinations used with Grid/GridSolvers/HYPRE.

Solver	Preconditioner
PCG	AMG, ILU(0)
BICGSTAB	AMG, ILU(0)
GMRES	AMG, ILU(0)
AMG	-
SPLIT	-

Parallel runs: One issue that has been observed is that there is a difference in the results produced by HYPRE using one or more processors. This would most likely be due to use of CG (krylov subspace methods), which involves an MPLSUM over the dot product of the residue. We have found this error to be dependent on the type of problem. One way to get across this problem is to use direct solvers in HYPRE like SPLIT. However we have noticed that direct solvers tend to be slow. The released code has an option to use the SPLIT solver, but this solver has not been extensively tested and was used only for internal debugging purposes and the usage of the HYPRE SPLIT solver in Flash-X is purely experimental.

Customizing solvers: HYPRE exposes a lot more parameters to tweak the solvers and preconditioners mentioned above. We have only used those which are applicable to general diffusion problems. Although in general these settings might be good enough it is by no means complete and might not be applicable to all class of problems. Use of additional HYPRE parameters might require direct manipulation of Flash-X code.

Symmetric Positive Definite (SPD) Matrix: PCG has been noticed to have convergence issues which might be related to (not necessarily),

- A non-SPD matrix generated due to round of errors (only).
- Use of BoomerAMG as PC (refer to HYPRE manual).

The default settings use PCG as the solver with AMG as preconditioner. The following parameters can be tweaked at run time,

V:-1-1-	Т	D - f 14	Diti
Variable	Type	Default	Description
gr_hyprePCType	string	$"hypre_amg"$	Algebraic Multigrid as Preconditioner
${ t gr_hypreMaxIter}$	integer	10000	Maximum number of iterations
gr_hypreRelTol	real	1×10^{-8}	Maximum ratio of the norm of the
			residual to that of the initial residue
gr_hypreSolverType	string	"hypre_pcg"	Type of linear solver, Preconditioned
			Conjugate gradient
gr_hyprePrintSolveInfo	boolean	FALSE	enables/disables some basic solver in-
			formation (for e.g number of itera-
			tions)
gr_hypreInfoLevel	integer	1	Verbosity level of solver diagnostics
			(refer HYPRE manual).
gr_hypreFloor	real	1×10^{-12}	Used to floor the end solution.
gr_hypreUseFloor	boolean	TRUE	whether to apply gr_hypreFloor to
			floor results from HYPRE.

Table 6.5: Runtime parameters used with Grid/GridSolvers/HYPRE.

6.10 Grid Geometry

Flash-X can use various kinds of coordinates ("**geometries**") for modeling physical problems. The available geometries represent different (orthogonal) curvilinear coordinate systems.

The geometry for a particular problem is set at runtime (after an appropriate invocation of setup) through the geometry runtime parameter, which can take a value of "cartesian", "spherical", "cylindrical", or "polar". Together with the dimensionality of the problem, this serves to completely define the nature of the problem's coordinate axes (??). Note that not all Grid implementations support all geometry/dimension combinations. Physics units may also be limited in the geometries supported, some may only work for Cartesian coordinates.

The core code of a **Grid** implementation is not concerned with the mapping of cell indices to physical coordinates; this is not required for under-the-hood **Grid** operations such as keeping track of which blocks are neighbors of which other blocks, which cells need to be filled with data from other blocks, and so on. Thus the physical domain can be logically modeled as a rectangular mesh of cells, even in curvilinear coordinates.

There are, however, some areas where geometry needs to be taken into consideration. The correct implementation of a given geometryrequires that gradients and divergences have the appropriate area factors and that the volume of a cell is computed properly for that geometry. Initialization of the grid as well as AMR operations (such as restriction, prolongation, and flux-averaging) must respect the geometry also. Furthermore, the hydrodynamic methods in Flash-X are finite-volume methods, so the interpolationmust also be conservative in the given geometry. The default mesh refinement criteria of Flash-X also currently take geometry into account, see ?? above.

Table 6.6: Different geometry types. For each geometry/dimensionality combination, the "support" column lists the Grid implementations that support it: pm4 stands for PARAMESH 4.0 and PARAMESH 4dev, pm2 for PARAMESH 2, UG for Uniform Grid implementations, respectively.

name	dimensions	support	axisymmetric	X-coord	Y-coord	Z-coord
cartesian	1	pm4,pm2,UG	n	x		
cartesian	2	pm4,pm2,UG	n	x	y	
cartesian	3	pm4,pm2,UG	n	x	y	z
cylindrical	1	pm4,UG	у	r		
cylindrical	2	pm4,pm2,UG	У	r	z	
cylindrical	3	pm4,UG	n	r	z	ϕ
spherical	1	pm4,pm2,UG	у	r		
spherical	2	pm4,pm2,UG	У	r	θ	
spherical	3	pm4,pm2,UG	n	r	θ	ϕ
polar	1	pm4,UG	У	r		
polar	2	pm4,pm2,UG	n	r	ϕ	
"polar + z" (cylindrical with a dif- ferent ordering of coordi- nates)	3	_	n	r	φ	<i>z</i>

A **convention:** in this section, Small letters x, y, and z are used with their usual meaning in designating coordinate directions for specific coordinate systems: *i.e.*, x and y refer to directions in Cartesian coordinates, and z may refer to a (linear) direction in either Cartesian or cylindrical coordinates.

On the other hand, capital symbols X, Y, and Z are used to refer to the (up to) three directions of any coordinate system, *i.e.*, the directions corresponding to the IAXIS, JAXIS, and KAXIS dimensions in FLASH-X, respectively. Only in the Cartesian case do these correspond directly to their small-letter counterparts. For other geometries, the correspondence is given in ??.

6.10.1 Understanding 1D, 2D, and Curvilinear Coordinates

In the context of Flash-X, curvilinear coordinates are most useful with 1-d or 2-d simulations, and this is how they are commonly used. But what does it mean to apply curvilinear coordinates in this way? And what does it mean to do a 1D or a 2D simulation of threedimensional reality? Physical reality has three spatial dimensions (as far as the physical problems simulated with Flash-X are concerned). In Cartesian coordinates, it is relatively straightforward to understand what a 2-d (or 1-d) simulation means: "Just leave out one (or two) coordinates." This is less obvious for other coordinate systems, therefore some fundamental discussion follows.

A reduced dimensionality (RD) simulation can be naively understood as taking a cut (or, for 1-d, a linear probe) through the real 3-d problem. However, there is also an assumption, not always explicitly stated, that is implied in this kind of simulation: namely, that the cut (or line) is representative of the 3-d

problem. This can be given a stricter meaning: it is assumed that the physics of the problem do not depend on the omitted dimension (or dimensions). A RD simulation can be a good description of a physical system only to the degree that this assumption is warranted. Depending on the nature of the simulated physical system, non-dependence on the omitted dimensions may mean the absence of force and/or momenta vector components in directions of the omitted coordinate axes, zero net mass and energy flow out of the plane spanned by the included coordinates, or similar.

For omitted dimensions that are lengths — z and possibly y in Cartesian, and z in cylindrical and polar RD simulations — one may think of a 2-d cut as representing a (possibly very thin) layer in 3-d space sandwiched between two parallel planes. There is no a priori definition of the thickness of the layer, so it is not determined what 3-d volume should be asigned to a 2-d cell in such coordinates. We can thus arbitrarily assign the length "1" to the edge length of a 3-d cell volume, making the volume equal to the 2-d area. We can understand generalizations of "volume" to 1-d, and of "face areas" to 2-d and 1-d RD simulations with omitted linear coordinates, in an equivalent way: just set the length of cell edges along omitted dimensions to 1.

For omitted dimensions that are angles — the θ and ϕ coordinates on spherical, cylindrical, and polar geometries — it is easier to think of omitting an angle as the equivalent of integrating over the full range of that angle coordinate (under the assumption that all physical solution variables are independent of that angle). Thus omitting an angle ϕ in these geometries implies the assumption of axial symmetry, and this is noted in ??. Similarly, omitting both ϕ and θ in spherical coordinates implies an assumption of complete spherical symmetry. When ϕ is omitted, a 2-d cell actually represents the 3-d object that is generated by rotating the 2-d area around a z-axis. Similarly, when only r is included, 1-d cells (i.e., r intervals) represent hollow spheres or cylinders. (If the coordinate interval begins at $r_l = 0.0$, the sphere or cylinder is massive instead of hollow.)

As a result of these considerations, the measures for cell (and block) volumes and face areas in a simulation depends on the chosen geometry. Formulas for the volume of a cell dependent on the geometry are given in the geometry-specific sections further below.

As discussed in ??, to ensure conservation at a jump in refinement in AMR grids, a flux correction step is taken. The fluxes leaving the fine cells adjacent to a coarse cell are used to determine more accurately the flux entering the coarse cell. This step takes the coordinate geometry into account in order to accurately determine the areas of the cell faces where fine and coarse cells touch. By way of example, an illustration is provided below in the section on cylindrical geometry.

6.10.1.1 Extensive Quantities in Reduced Dimensionality

The considerations above lead to some consequences for the understanding of extensive quantities, like mass or energies, that may not be obvious.

The following discussion applies to geometries with omitted dimensions that are lengths — z and possibly y in Cartesian, and z in cylindrical and polar RD simulations. We will consider Cartesian geometries as the most common case, and just note that the remaining cases can be thought of analogously.

In 2D Cartesian, the "volume" of a cell should be $\Delta V = \Delta x \, \Delta y$. We would like to preserve the form of equations that relate extensive quantities to their densities, e.g., $\Delta m = \rho \Delta V$ for mass and $\Delta E_{tot} = \rho e_{tot} \Delta V$ for total energy in a cell. We also like to retain the usual definitions for intensive quantities such as density ρ , including their physical values and units, so that material density ρ is expressed in g/cm^3 (more generally M/L^3), no matter whether 1D, 2D, or 3D. We cannot satisfy both desiderata without modifying the interpretation of "mass", "energy", and similar extensive quantities in the system of equations modeled by Flash-X.

Specifically, in a 2D Cartesian simulation, we have to interpret "mass" as really representing a linear mass density, measured in M/L. Similarly, an "energy" is really a linear energy density, etc.

In a 1D Cartesian simulation, we have to interpret "mass" as really representing a surface mass density, measured in M/L^2 , and an "energy" is really a surface energy density.

(There is a different point of view, which amounts to the same thing: One can think of the "mass" of a cell (in 2D) as the physical mass contained in a three-dimensional cell of volume $\Delta x \Delta y \Delta z$ where the cell height Δz is set to be exactly 1 length unit. Always with the understanding that "nothing happens" in the z direction.)

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Note that this interpretation of "mass", "energy", etc. must be taken into account not just when examining the physics in individual cells, but equally applies for quantities integrated over larger regions, including the "total mass" or "total energy" etc. reported by Flash-X in flash.dat files — they are to be interpreted as (linear or surface) densities of the nominal quantities (or, alternatively, as integrals over 1 length unit in the missing Cartesian directions).

6.10.2 Choosing a Geometry

The user chooses a geometry by setting the [[rpi reference]] runtime parameter in flash.par. The default is "cartesian" (unless overridden in a simulation's Config file). Depending on the Grid implementation used and the way it is configured, the geometry may also have to be compiled into the program executable and thus may have to be specified at configuration time; the setup flag -geometry should be used for this purpose, see ??.

The [[rpi reference]] runtime parameter is most useful in cases where the geometry does not have to be specified at compile-time, in particular for the Uniform Grid. The runtime parameter will, however, always be considered at run-time during Grid initialization. If the [[rpi reference]] runtime parameter is inconsistent with a geometry specified at setup time, Flash-X will then either override the geometry specified at setup time (with a warning) if that is possible, or it will abort.

This runtime parameter is used by the **Grid** unit and also by hydrodynamics solvers, which add the necessary geometrical factors to the divergence terms. Next we describe how user code can use the runtime parameter's value.

6.10.3 Getting Geometry Information in Program Code

The Grid unit provides an accessor [[api reference]] property that returns the geometry as an integer, which can be compared to the symbols {CARTESIAN, SPHERICAL, CYLINDRICAL, POLAR} defined in "constants.h" to determine which of the supported geometries we are using. A unit writer can therefore determine flow-control based on the geometry type (see ??). Furthermore, this provides a mechanism for a unit to determine at runtime whether it supports the current geometry, and if not, to abort.

Coordinate information for the mesh can be determined via the [[api reference]] routine. This routine can provide the coordinates of cells at the left edge, right edge, or center. The width of cells can be determined via the [[api reference]] routine. Angle values and differences are given in radians. Coordinate information for a block of cells as a whole is available through [[api reference]] and [[api reference]].

The volume of a single cell can be obtained via the [[api reference]] or the [[api reference]] routine. Use the [[api reference]], [[api reference]], or [[api reference]] routines with argument dataType=CELL_VOLUME To retrieve cell volumes for more than one cell of a block. To retrieve cell face areas, use the same Grid_get*Data interfaces with the appropriate dataType argument.

Note the following difference between the two groups of routines mentioned in the previous two paragraphs: the routines for volumes and areas take the chosen geometry into account in order to return geometric measures of physical volumes and faces (or their RD equivalents). On the other hand, the routines for coordinate values and widths return values for X, Y, and Z directly, without converting angles to (arc) lengths.

6.10.4 Available Geometries

Currently, all of Flash-X's physics support one-, two-, and (with a few exceptions explicitly stated in the appropriate chapters) three-dimensional Cartesian grids. Some units, including the Flash-X Grid unit and PPM hydrodynamics unit (??), support additional geometries, such as two-dimensional cylindrical (r, z) grids, one/two-dimensional spherical $(r)/(r, \theta)$ grids, and two-dimensional polar (r, ϕ) grids. Some specific considerations for each geometry follow.

The following tables use the convention that r_l and r_r stand for the values of the r coordinate at the "left" and "right" end of the cell's r-coordinate range, respectively (i.e., $r_l < r_r$ is always true), and $\Delta r = r_r - r_l$; and similar for the other coordinates.

```
#include "constants.h"
integer :: geometry
call Grid_getGeometry(geometry)
select case (geometry)

case (CARTESIAN)
! do Cartesian stuff here ...
case (SPHERICAL)
! do spherical stuff here ...
case (CYLINDRICAL)
! do cylindrical stuff here ...
case (POLAR)
! do polar stuff here ...
end select
```

Figure 6.6: Branching based on geometry type

6.10.4.1 Cartesian geometry

Flash-X uses Cartesian (plane-parallel) geometry by default. This is equivalent to specifying geometry = "cartesian"

in the runtime parameter file.

Cell Volume in Cartesian Coordinates

1-d	Δx
2-d	$\Delta x \Delta y$
3-d	$\Delta x \Delta y \Delta z$

6.10.4.2 Cylindrical geometry

To run Flash-X with cylindrical coordinates, the geometry parameter must be set thus:

Cell Volume in Cylindrical Coordinates
$$\begin{array}{c|c} 1\text{-d} & \pi(r_r^2-r_l^2) \\ 2\text{-d} & \pi(r_r^2-r_l^2)\Delta z \\ \hline 3\text{-d} & \frac{1}{2}(r_r^2-r_l^2)\Delta z\Delta \phi \end{array}$$

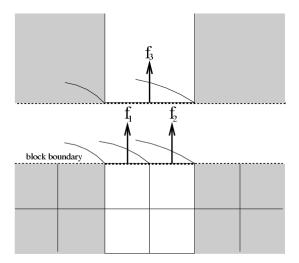


Figure 6.7: Diagram showing two fine cells and a coarse cell at a jump in refinement in the cylindrical 'z' direction. The block boundary has been cut apart here for illustrative purposes. The fluxes out of the fine blocks are shown as f_{-1} and f_{-2} . These will be used to compute a more accurate flux entering the coarse flux f_{-3} . The area that the flux passes through is shown as the annuli at the top of each fine cell and the annulus below the coarse cell.

As in other non-Cartesian geometries, if the minimum radius is chosen to be zero (xmin = 0.), the left-hand boundary type should be reflecting (or axisymmetric). Of all supported non-Cartesian geometries, the cylindrical is in 2-d most similar to a 2-d coordinate system: it uses two linear coordinate axes (r and z) that form a rectangular grid physically as well as logically.

As an illustrative example of the kinds of considerations necessary in curved coordinates, ?? shows a jump in refinement along the cylindrical 'z' direction. When performing the flux correction step at a jump in refinement, we must take into account the area of the annulus through which each flux passes to do the proper weighting. We define the cross-sectional area through which the z-flux passes as

$$A = \pi (r_r^2 - r_l^2) . ag{6.55}$$

The flux entering the coarse cell above the jump in refinement is corrected to agree with the fluxes leaving the fine cells that border it. This correction is weighted according to the areas

$$f_3 = \frac{A_1 f_1 + A_2 f_2}{A_3} \ . \tag{6.56}$$

For fluxes in the radial direction, the cross-sectional area is independent of the height, z, so the corrected flux is simply taken as the average of the flux densities in the adjacent finer cells.

6.10.4.3 Spherical geometry

One or two dimensional spherical problems can be performed by specifying

in the runtime parameter file.

If the minimum radius is chosen to be zero (xmin = 0.), the left-hand boundary type should be reflecting.

6.10.4.4 Polar geometry

Polar geometry is a 2-D subset of 3-D cylindrical configuration without the "z" coordinate. Such geometry is natural for studying objects like accretion disks. This geometry can be selected by specifying

in the runtime parameter file.

Cell Volume in Polar Coordinates
$$\begin{array}{c|c} 1\text{-d} & \pi(r_r^2-r_l^2) \\ 2\text{-d} & \frac{1}{2}(r_r^2-r_l^2)\Delta\phi \\ \\ 3\text{-d} & \frac{1}{2}(r_r^2-r_l^2)\Delta\phi\Delta z \text{ (not supported)} \\ \end{array}$$

As in other non-Cartesian geometries, if the minimum radius is chosen to be zero (xmin = 0.), the left-hand boundary type should be reflecting.

6.10.5 Conservative Prolongation/Restriction on Non-Cartesian Grids

When blocks are refined, we need to initialize the child data using the information in the parent cell in a manner which preserves the cell-averages in the coordinate system we are using. When a block is derefined, the parent block (which is now going to be a leaf block) needs to be filled using the data in the child blocks (which are soon to be destroyed). The first procedure is called prolongation. The latter is called restriction. Both of these procedures must respect the geometry in order to remain conservative. Prolongation and restriction are also used when filling guard cells at jumps in refinement.

6.10.5.1 Prolongation

When using a supported non-Cartesian geometry, Flash-X has to use geometrically correct prolongation routines. These are located in:

- source/Grid/GridMain/paramesh/Paramesh2/monotonic (for PARAMESH 2)
- source/Grid/GridMain/paramesh/interpolation/Paramesh4/prolong (for PARAMESH 4)

These paths will be be automatically added by the setup script when the -gridinterpolation=monotonic option is in effect (which is the case by default, unless -gridinterpolation=native was specified). The "monotonic" interpolationscheme used in both cases is taking geometry into consideration and is appropriate for all supported geometries.

6.10.5.2 Restriction

The default restriction routines understand the supported geometries by default. A cell-volume weighted average is used when restricting the child data up to the parent. For example, in 2-d, the restriction would look like

$$\langle f \rangle_{i,j} = \frac{V_{ic,jc} \langle f \rangle_{ic,jc} + V_{ic+1,jc} \langle f \rangle_{ic+1,jc} + V_{ic,jc+1} \langle f \rangle_{ic,jc+1} + V_{ic+1,jc+1} \langle f \rangle_{ic+1,jc+1}}{V_{i,j}}, \qquad (6.57)$$

where $V_{i,j}$ is the volume of the cell with indices, i, j, and the ic, jc indices refer to the children.

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6.11 Unit Test

The Grid unit test has implementations to test Uniform Grid and PARAMESH. The Uniform Grid version of the test has two parts; the latter portion is also tested in PARAMESH. The test initializes the grid with a sinusoid function $\sin(x) \times \cos(y) \times \cos(z)$, distributed over a number of processors. Knowing the configuration of processors, it is possible to determine the part of the sinusoid on each processor. Since guardcells are filled either from the interior points of the neighboring processor, or from boundary conditions, it is also possible to predict the values expected in guard cells on each processor. The first part of the UG unit test makes sure that the actual received values of guard cell match with the predicted ones. This process is carried out for both cell-centered and face-centered variables.

The second part of the UG test, and the only part of the PARAMESH test, exercises the get and put data functions. Since the Grid unit has direct access to all of its own data structures, it can compare the values fetched using the getData functions against the directly accessible values and report an error if they do not match. The testing of the Grid unit is not exhaustive, and given the complex nature of the unit, it is difficult to devise tests that would do so. However, the more frequently used functions are exercised in this test.

Chapter 7

IO Unit

Flash-X uses parallel input/output (IO) libraries to simplify and manage the output of the large amounts of data usually produced. In addition to keeping the data output in a standard format, the parallel IO libraries also ensure that files will be portable across various platforms. The mapping of Flash-X data-structures to records in these files is controlled by the Flash-X IO unit. Flash-X can output data with HDF5 parallel IO library. Various techniques can be used to write the data to disk when running a parallel simulation. The first is to move all the data to a single processor for output; this technique is known as serial IO. Secondly, each processor can write to a separate file, known as direct IO. As a third option, each processor can use parallel access to write to a single file in a technique known as parallel IO. Finally, a hybrid method can be used where clusters of processors write to the same file, though different clusters of processors output to different files. In general, parallel access to a single file will provide the best parallel IO performance unless the number of processors is very large. On some platforms, such as Linux clusters, there may not be a parallel file system, so moving all the data to a single processor is the only solution. Therefore Flash-X supports HDF5 libraries in both serial and parallel forms, where the serial version collects data to one processor before writing it, while the parallel version has every processor writing its data to the same file.

7.1 IO Implementations

FLASH-X supports multiple IO implementations: direct, serial and parallel implementations as well as support for different parallel libraries. In addition, FLASH-X also supports multiple (??) Grid implementations. As a consequence, there are many permutations of the IO API implementation, and the selected implementation must match not only the correct IO library, but also the correct grid. Although there are many IO options, the setup script in FLASH-X is quite 'smart' and will not let the user setup a problem with incompatible IO and Grid unit implementations. ?? summarizes the different implementation of the Flash-X IO unit in the current release.

Table 7.1: IO implementations available in Flash-X. All implementations begin at the /source directory.

Implementation Path	Description
IO/IOMain/HDF5/parallel/PM	Hierarchical Data Format (HDF) 5 output. A single HDF5
	file is created, with each processor writing its data to the
	same file simultaneously. This particular implementation
	only works with the PARAMESH grid package.
IO/IOMain/HDF5/parallel/AM	Hierarchical Data Format (HDF) 5 output. A single HDF5
	file is created, with each processor writing its data to the
	same file simultaneously. This particular implementation
	only works with the AMReXgrid package.

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Table 7.1: Flash-X IO implementations (continued).

Implementation path	Description
IO/IOMain/hdf5/paralle1/UG	Hierarchical Data Format (HDF) 5 output. A single HDF5 file is created, with each processor writing its data to the same file simultaneously. This implementation only works with the Uniform Grid.
IO/IOMain/hdf5/parallel/NoFbs	Hierarchical Data Format (HDF) 5 output. A single HDF5 file is created, with each processor writing its data to the same file simultaneously. All data is written out as one block. This implementation only works with the Uniform Grid.
IO/IOMain/hdf5/serial/PM	Hierarchical Data Format (HDF) 5 output. Each processor passes its data to processor 0 through explicit MPI sends and receives. Processor 0 does all of the writing. The resulting file format is identical to the parallel version; the only difference is how the data is moved during the writing. This implementation only works with the PARAMESH grid package.
IO/IOMain/hdf5/serial/AM	Hierarchical Data Format (HDF) 5 output. Each processor passes its data to processor 0 through explicit MPI sends and receives. Processor 0 does all of the writing. The resulting file format is identical to the parallel version; the only difference is how the data is moved during the writing. This implementation only works with the AMReXgrid package.
IO/IOMain/hdf5/serial/UG	Hierarchical Data Format (HDF) 5 output. Each processor passes its data to processor 0 through explicit MPI sends and receives. Processor 0 does all of the writing. The resulting file format is identical to the parallel version; the only difference is how the data is moved during the writing. This particular implementation only works with the Uniform Grid.

FLASH-X also comes with some predefined setup **shortcuts** which make choosing the correct IO significantly easier; see ?? for more details about shortcuts. In FLASH-X HDF5 serial IO is included by default. Since PARAMESH 4.0 is the default grid, the included IO implementations will be compatible with PARAMESH 4.0. For clarity, a number or examples are shown below.

An example of a basic setup with HDF5 serial IO and the PARAMESH grid, (both defaults) is:

./setup Sod -2d -auto

To include a parallel implementation of HDF5 for a PARAMESH grid the setup syntax is:

./setup Sod -2d -auto -unit=IO/IOMain/hdf5/parallel/PM

using the already defined shortcuts the setup line can be shortened to

./setup Sod -2d -auto +parallelio

To set up a problem with the Uniform Grid and HDF5 serial IO, the setup line is:

./setup Sod -2d -auto -unit=Grid/GridMain/UG -unit=I0/I0Main/hdf5/serial/UG

using the already defined shortcuts the setup line can be shortened to

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```
./setup Sod -2d -auto +ug
```

To set up a problem with the Uniform Grid and HDF5 parallel IO, the complete setup line is:

```
./setup Sod -2d -auto -unit=Grid/GridMain/UG -unit=IO/IOMain/hdf5/parallel/UG
```

using the already defined shortcuts the setup line can be shortened to

```
./setup Sod -2d -auto +ug +parallelio
```

If you do *not* want to use IO, you need to *explicitly* specify on the **setup** line that it should not be included, as in this example:

```
./setup Sod -2d -auto +noio
```

To setup a problem using the Parallel-NetCDF library the user should include either

```
-unit=IO/IOMain/pnetcdf/PM or -unit=IO/IOMain/pnetcdf/UG
```

to the setup line. The predefined shortcut for including the Parallel-NetCDF library is

```
+pnetcdf
```

Note that Parallel-NetCDF IO unit does not have a serial implementation.

If you are using non-fixedblocksize the shortcut

+nofbs

will bring in both Uniform Grid, set the mode to nonfixed blocksize, and choose the appropriate IO.

In keeping with the Flash-X code architecture, the F90 module IO_data stores all the data with IO unit scope. The routine [[api reference]] is called once by [[api reference]] and initializes IO data and stores any runtime parameters. See ??.

7.2 Output Files

The IO unit can output 4 different types of files: checkpoint files, plotfiles, particle files and flash.dat, a text file holding the integrated grid quantities. Flash-X also outputs a logfile, but this file is controlled by the Logfile Unit; see ?? for a description of that format.

There are a number of runtime parameters that are used to control the output and frequency of IO files. A list of all the runtime parameters and their descriptions for the IO unit can be found online [[rpi reference]]IO/all of them. Additional description is located in ?? for checkpoint parameters, ?? for plotfile parameters, ?? for particle file parameters, ?? for flash.dat parameters, and ?? for genereal IO parameters.

7.2.1 Checkpoint files - Restarting a Simulation

Checkpoint files are used to restart a simulation. In a typical production run, a simulation can be interrupted for a number of reasons—e.g., if the machine crashes, the present queue window closes, the machine runs out of disk space, or perhaps (gasp) there is a bug in Flash-X. Once the problem is fixed, a simulation can be restarted from the last checkpoint file rather than the beginning of the run. A checkpoint filecontains all the information needed to restart the simulation. The data is stored at full precision of the code (8-byte reals) and includes all of the variables, species, grid reconstruction data, scalar values, as well as meta-data about the run.

The API routine for writing a checkpoint file is [[api reference]]. Users usually will not need to call this routine directly because the Flash-X IO unit calls IO_writeCheckpoint from the routine [[api reference]] which checks the runtime parameters to see if it is appropriate to write a checkpoint file at this time. There are a number of ways to get Flash-X to produce a checkpoint file for restarting. Within the flash.par, runtime parameters can be set to dump output. A checkpoint file can be dumped based on elapsed simulation time, elapsed wall clock time or the number of timesteps advanced. A checkpoint file is also produced when the simulation ends, when the max simulation time [[rpi reference]], the minimum cosmological redshift, or the

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total number of steps [[rpi reference]] has been reached. A user can force a dump to a checkpoint file at another time by creating a file named .dump_checkpoint in the output directory of the master processor. This manual action causes Flash-X to write a checkpoint in the next timestep. Checkpoint files will continue to be dumped after every timestep as long as the code finds a .dump_checkpoint file in the output directory, so the user must remember to remove the file once all the desired checkpoint files have been dumped. Creating a file named .dump_restart in the output directory will cause Flash-X to output a checkpoint file and then stop the simulation. This technique is useful for producing one last checkpoint file to save time evolution since the last checkpoint, if the machine is going down or a queue window is about to end. These different methods can be combined without problems. Each counter (number of timesteps between last checkpoint, amount of simulation time single last checkpoint, the change in cosmological redshift, and the amount of wall clock time elapsed since the last checkpoint) is independent of the others, and are not influenced by the use of a .dump_checkpoint or .dump_restart.

Runtime Parameters used to control checkpoint file output include:

Table 7.2: Checkpoint IO parameters.

	10010 1.2.	checkpoint to	por differences.
Parameter Type	Default va	due Description	on
checkpointFileNumber	INTEGER	0	The number of the initial checkpoint file. This number is appended to the end of the filename and incremented at each subsequent output. When restarting a simulation, this indicates which checkpoint file to use.
checkpointFileIntervalStep	INTEGER	0	The number of timesteps desired between subsequent checkpoint files.
checkpointFileIntervalTime	REAL	1.	The amount of simulation time desired between subsequent checkpoint files.
${\tt checkpointFileIntervalZ}$	REAL	HUGE(1.)	The amount of cosmological redshift change that is desired between subsequent checkpoint files.
rolling_checkpoint	INTEGER	10000	The number of checkpoint files to keep available at any point in the simulation. If a checkpoint number is greater than rolling_checkpoint, then the checkpoint number is reset to 0. There will be at most rolling_checkpoint checkpoint files kept. This parameter is intended to be used when disk space is at a premium.
wall_clock_checkpoint	REAL	43200.	The maximum amount of wall clock time (seconds) to elapse between checkpoints. When the simulation is started, the current time is stored. If wall_clock_checkpoint seconds elapse over the course of the simulation, a checkpoint file is stored. This is useful for ensuring that a checkpoint file is produced before a queue closes.

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Table 7.2: Checkpoint IO parameters (continued	Table 7.2:	Checkpoint IC	parameters	(continued
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	Parameter	Type	Default value	Description	on
restart			BOOLEAN .:	false.	A logical variable indicating whether the
					simulation is restarting from a checkpoint
					file (.true.) or starting from scratch
					(.false.).

Flash-X is capable of restarting from any of the checkpoint files it produces. The user should make sure that the checkpoint file is valid (e.g., the code did not stop while outputting). To tell Flash-X to restart, set the [[rpi reference]] runtime parameter to .true. in the flash.par. Also, set [[rpi reference]] to the number of the file from which you wish to restart. If plotfiles or particle files are being produced set [[rpi reference]] and [[rpi reference]] to the number of the next plotfile and particle file you want Flash-X to output. In Flash-X plotfiles and particle file outputs are forced whenever a checkpoint file is written. Sometimes several plotfiles may be produced after the last valid checkpoint file. Resetting plotfileNumber to the first plotfile produced after the checkpoint from which you are restarting will ensure that there are no gaps in the output. See ?? for more details on plotfiles.

7.2.2 Plotfiles

A plotfilecontains all the information needed to interpret the grid data maintained by Flash-X. The data in plotfiles, including the grid metadata such as coordinates and block sizes, are stored at single precision to preserve space. This can, however, be overridden by setting the runtime parameters plotfileMetadataDP and/or plotfileGridQuantityDP to true to set the grid metadata and the quantities stored on the grid (dens, pres, temp, etc.) to use double precision, respectively. Users must choose which variables to output with the runtime parameters [[rpi reference]], [[rpi reference]], etc., by setting them in the flash.par file. For example:

```
plot_var_1 = "dens"
plot_var_2 = "pres"
```

Currently, we support a number of plotvars named plot_var_n up to the number of UNKVARS in a given simulation. Similarly, scratch variables may be output to plot files ??. At this time, the plotting of face centered quantities is not supported.

Flash-X Transition

In Flash-X a few variables like density and pressure were output to the plotfiles by default. Because Flash-X supports a wider range of simulations, it makes no assumptions that density or pressure variables are even included in the simulation. In Flash-X a user *must* define plotfile variables in the flash.par file, otherwise the plotfiles will not contain any variables.

The interface for writing a plotfile is the routine [[api reference]]. As with checkpoint files, the user will not need to call this routine directly because it is invoked indirectly through calling [[api reference]] when, based on runtime parameters, FLASH-X needs to write a plotfile. Flash-X can produce plotfiles in much the same manner as it does with checkpoint files. They can be dumped based on elapsed simulation time, on steps since the last plotfile dump or by forcing a plotfile to be written by hand by creating a.dump_plotfile in the output directory. A plotfile will also be written at the termination of a simulation as well.

If plotfiles are being kept at particular intervals (such as time intervals) for purposes such as visualization or analysis, it is also possible to have Flash-X denote a plotfile as "forced". This designation places

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the word forced between the basename and the file format type identifier (or the split number if splitting is used). These files are numbered separately from normal plotfiles. By default, plotfiles are considered forced if output for any reason other than the change in simulation time, change in cosmological redshift, change in step number, or the termination of a simulation from reaching nend, zFinal, or tmax. This option can be disabled by setting ignoreForcedPlot to true in a simulations flash.par file. The following runtime parameters pertain to controlling plotfiles:

Table 7.3: Plotfile IO parameters.

Parameter	Type	Default value	Description
plotFileNumber	INTEGER	0	The number of the starting (or restarting) plotfile. This number is appended to the filename.
plotFileIntervalTime	REAL	1.	The amount of simulation time desired between subsequent plotfiles.
plotFileIntervalStep	INTEGER	0	The number of timesteps desired between subsequent plotfiles.
plotFileIntervalZ	INTEGER	HUGE(1.)	The change in cosmological redshift desired between subsequent plotfiles.
plot_var_1,, plot_var_n	STRING	"none"	Name of the variables to store in a plotfile. Up to 12 variables can be selected for storage, and the standard 4-character variable name can be used to select them.
ignoreForcedPlot	BOOLEAN	.false.	A logical variable indicating whether or not to denote certain plotfiles as forced.
forcedPlotfileNumber	INTEGER	0	An integer that sets the starting number for a forced plotfile.
plotfileMetadataDP	BOOLEAN	.false.	A logical variable indicating whether or or not to output the normally single-precision grid metadata fields as double precision in plotfiles. This specifically affects coordinates, block size, and bounding box.
plotfileGridQuantityDP	BOOLEAN	.false.	A logical variable that sets whether or not quantities stored on the grid, such as those stored in unk, are output in single precision or double precision in plotfiles.

7.2.3 Particle files

When Lagrangian particles are included in a simulation, the ParticleIO subunit controls input and output of the particle information. The particle files are stored in double precision. Particle data is written to the checkpoint file in order to restart the simulation, but is not written to plotfiles. Hence analysis and metadata about particles is also written to the particle files. The particle files are intended for more frequent dumps. The interface for writing the particle file is [[api reference]]. Again the user will not usually call this function

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directly because the routine IO_output controls particle output based on the runtime parameters controlling particle files. They are controlled in much of the same way as the plotfiles or checkpoint files and can be dumped based on elapsed simulation time, on steps since the last particle dump or by forcing a particle file to be written by hand by creating a .dump_particle_file in the output directory. The following runtime parameters pertain to controlling particle files:

Table 7.4: Particle File IO	runtime parameters.
-----------------------------	---------------------

Parameter Type	Default value	Description
particleFileNumber	INTEGER O	The number of the starting (or restarting) particle file. This number is appended to the end of the filename.
particleFileIntervalTime	REAL 1.	The amount of simulation time desired between subsequent particle file dumps.
particleFileIntervalStep	INTEGER O	The number of timesteps desired between subsequent particle file dumps.
particleFileIntervalZ	REAL HU	The change in cosmological redshift desired between subsequent particle file dumps.

All the code necessary to output particle data is contained in the IO subunit called IOParticles. Whenever the Particles unit is included in a simulation the correct IOParticles subunit will also be included. For example as setup:

./setup IsentropicVortex -2d -auto -unit=Particles +ug

will include the IO unit IO/IOMain/hdf5/serial/UG and the correct IOParticles subunit IO/IOParticles/hdf5/serial/UG. The shortcuts +parallelio, +pnetcdf, +ug will also cause the setup script to pick up the correct IOParticles subunit as long as a Particles unit is included in the simulation.

7.2.4 Integrated Grid Quantities – flash.dat

At each simulation time step, values which represent the overall state (e.g., total energy and momentum) are computed by calculating over all cells in the computations domain. These integral quantities are written to the ASCI file flash.dat. A default routine [[api reference]] is provided to output standard measures for hydrodynamic simulations. The user should copy and modify the routine IO_writeIntegralQuantities into a given simulation directory to store any quantities other than the default values. Two runtime parameters pertaining to the flash.dat file are listed in the table below.

Table 7.5: flash.dat runtime parameters.

Parameter	Type	Default value	Description
stats_file	STRING	"flash.dat"	Name of the file to which the integral quantities are written.

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Table 7.5: flash.dat parameters (continued).

Parameter	Type	Default value	Description
wr_integrals_freq	INTEGER	1	The number of timesteps to elapse be-
			tween outputs to the scalar/integral data file
			$({\tt flash.dat})$

7.2.5 General Runtime Parameters

There are several runtime parameters that pertain to the general IO unit or multiple output files rather than one particular output file. They are listed in the table below.

Table 7.6: General IO runtime parameters.

Parameter	Type	Default value	Description
basenm	STRING	"flash_"	The main part of the output filenames. The full filename consists of the base name, a series of three-character abbreviations indicating whether it is a plotfile, particle file or checkpoint file, the file format, and a 4-digit file number. See ?? for a description of how Flash-X output files are named.
output_directory	STRING	11 11	Output directory for plotfiles, particle files and checkpoint files. The default is the directory in which the executable sits. output_directory can be an absolute or relative path.
memory_stat_freq	INTEGER	100000	The number of timesteps to elapse between memory statistic dumps to the log file (flash.log).
useCollectiveHDF5	BOOLEAN	.true.	When using the parallel HDF5 implementation of IO, will enable collective mode for HDF5.
summaryOutputOnly	BOOLEAN	.false.	When set to .true. write an integrated grid quantities file only. Checkpoint, plot and particle files are not written unless the user creates a .dump_plotfile, .dump_checkpoint, .dump_restart or .dump_particle file.

7.3 Restarts and Runtime Parameters

FLASH-X outputs the runtime parameters of a simulation to all checkpoint files. When a simulation is restarted, these values are known by the RuntimeParameters unit while the code is running. On a restart, all values from the checkpoint used in the restart are stored as previous values in the lists kept by the RuntimeParameters unit. All current values are taken from the defaults used by FLASH-X and any simulation parameter files (e.g., flash.par). If needed, the previous values from the checkpoint file can be

obtained using the routines [[api reference]].

7.4 Output Scalars

In FLASH-X, each unit has the opportunity to request scalar data to be output to checkpoint or plotfiles. Because there is no central database, each unit "owns" different data in the simulation. For example, the Driver unit owns the timestep variable dt, the simulation variable simTime, and the simulation step number nStep. The Grid unit owns the sizes of each block, nxb, nyb, and nzb. The IO unit owns the variable checkpointFileNumber. Each of these quantities are output into checkpoint files. Instead of hard coding the values into checkpoint routines, FLASH-X offers a more flexible interface whereby each unit sends its data to the IO unit. The IO unit then stores these values in a linked list and writes them to the checkpoint file or plotfile. Each unit has a routine called "Unit_sendOutputData", e.g., [[api reference]] and [[api reference]]. These routines in turn call [[api reference]]. For example, the routine [[api reference]] calls

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```
IO_setScalar("nxb", NXB)
IO_setScalar("nyb", NYB)
IO_setScalar("nzb", NZB)
```

To output additional simulation scalars in a checkpoint file, the user should override one of the "Unit_sendOutputData" or Simulation_sendOutputData.

After restarting a simulation from a checkpoint file, a unit might call [[api reference]] to reset a variable value. For example, the Driver unit calls IO_getScalar("dt", dr_dt) to get the value of the timestep dt reinitialized from the checkpoint file. A value from the checkpoint file can be obtained by calling [[api reference]]. This call can take an optional argument to find out if an error has occurred in finding the previous value, most commonly because the value was not found in the checkpoint file. By using this argument, the user can then decide what to do if the value is not found. If the scalar value is not found and the optional argument is not used, then the subroutine will call [[api reference]] and terminate the run.

7.5 Output User-defined Arrays

Often in a simulation the user needs to output additional information to a checkpoint or plotfile which is not a grid scope variable. In Flash-X any additional information had to be hard coded into the simulation. In Flash-X, we have provided a general interface [[api reference]] and [[api reference]] which allows the user to write and read any generic array needed to be stored. The above two functions do not have any implementation and it is up to the user to fill them in with the needed calls to the HDF5 or pnetCDF C routines. We provide implementation for reading and writing integer and double precision arrays with the helper routines io h5write_generic_iarr, io_h5write_generic_rarr, io_ncmpi_write_generic_iarr, and io_ncmpi_write_generic_iarr. Data is written out as a 1-dimensional array, but the user can write multidimensional arrays simply by passing a reference to the data and the total number of elements to write. See these routines and the simulation StirTurb for details on their usage.

7.6 Output Scratch Variables

In Flash-X a user can allocate space for a scratch or temporary variable with grid scope using one of the Config keywords SCRATCHVAR, SCRATCHCENTERVAR, SCRATCHFACEXVAR, SCRATCHFACEXVAR, SCRATCHFACEXVAR or SCRATCHFACEXVAR (see ??). To output these scratch variables, the user only needs to set the values of the runtime parameters [[rpi reference]], [[rpi reference]], etc., by setting them in the flash.par file. For example to output the magnitude of vorticity with a declaration in a Config file of SCRATCHVAR mvrt:

```
plot_grid_var_1 = "mvrt"
```

Note that the post-processing routines like fidlr do not display these variables, although they are present in the output file. Future implementations may support this visualization.

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7.7 Face-Centered Data

Face-centered variables are now output to checkpoint files, when they are declared in a configuration file. Presently, up to nine face-centered variables are supported in checkpoint files. Plotfile output of face-centered data is not yet supported.

7.8 Output Filenames

Flash-X constructs the output filenames based on the user-supplied basename, (runtime parameter basenm) and the file counter that is incremented after each output. Additionally, information about the file type and data storage is included in the filename. The general checkpoint filename is:

$${\tt basename_s0000_} \left\{ \begin{array}{c} {\tt hdf5} \\ {\tt ncmpi} \end{array} \right\}_{\tt chk_0000} \ ,$$

where hdf5 or ncmpi (prefix for PnetCDF) is picked depending on the particular IO implementation, the number following the "s" is the split file number, if split file IO is in use, and the number at the end of the filename is the current checkpointFileNumber. (The PnetCDF function prefix "ncmpi" derived from the serial NetCDF calls beginning with "nc")

The general plotfile filename is:

$${\tt basename_s0000_} \left\{ \begin{array}{c} {\tt hdf5} \\ {\tt ncmpi} \end{array} \right\} _{\tt plt_} \left\{ \begin{array}{c} {\tt crn} \\ {\tt cnt} \end{array} \right\} _{\tt 0000} \ ,$$

where hdf5 or ncmpi is picked depending on the IO implementation used, crn and cnt indicate data stored at the cell corners or centers respectively, the number following "s" is the split file number, if used, and the number at the end of the filename is the current value of plotfileNumber. crn is reserved, even though corner data output is not presently supported by Flash-X's IO.

7.9 Output Formats

HDF5 is our most most widely used IO library although Parallel-NetCDF is rapidly gaining acceptance among the high performance computing community. In Flash-X we also offer a serial direct FORTRAN IO which is currently only implemented for the uniform grid. This option is intended to provide users a way to output data if they do not have access to HDF5 or PnetCDF. Additionally, if HDF5 or PnetCDF are not performing well on a given platform the direct IO implementation can be used as a last resort. Our tools, fidlr and sfocu (??), do not currently support the direct IO implementation, and the output files from this mode are not portable across platforms.

7.9.1 HDF5

HDF5is supported on a large variety of platforms and offers large file support and parallel IO via MPI-IO. Information about the different versions of HDF can be found at https://support.hdfgroup.org/documentation/. The IO in FLASH-X implementations require HDF5 1.4.0 or later. Please note that HDF5 1.6.2 requires IDL 1.6 or higher in order to use fidlr3.0 for post processing.

Implementations of the HDF510 unit use the HDF application programming interface (API) for organizing data in a database fashion. In addition to the raw data, information about the data type and byte ordering (little- or big-endian), rank, and dimensions of the dataset is stored. This makes the HDF format extremely portable across platforms. Different packages can query the file for its contents without knowing the details of the routine that generated the data.

Flash-X provides different HDF5 IO unit implementations – the serial and parallel versions for each supported grid, Uniform Grid and PARAMESH. It is important to remember to match the IO implementation with the correct grid, although the setup script generally takes care of this matching. PARAMESH 2, PARAMESH 4.0, and PARAMESH 4dev all work with the PARAMESH (PM) implementation of IO. Nonfixed blocksize IO has its own implementation in parallel, and is presently not supported in serial mode. Examples are given below for the five different HDF5 IO implementations.

```
./setup Sod -2d -auto -unit=IO/IOMain/hdf5/serial/PM (included by default)
./setup Sod -2d -auto -unit=IO/IOMain/hdf5/parallel/PM
./setup Sod -2d -auto -unit=Grid/GridMain/UG -unit=IO/IOMain/hdf5/serial/UG
./setup Sod -2d -auto -unit=Grid/GridMain/UG -unit=IO/IOMain/hdf5/parallel/UG
./setup Sod -2d -auto -nofbs -unit=Grid/GridMain/UG -unit=IO/IOMain/hdf5/parallel/NoFbs
```

The default IO implementation is IO/IOMain/hdf5/serial/PM. It can be included simply by adding -unit=IO to the setup line. In FLASH-X, the user can set up shortcutsSee ?? for more information about creating shortcuts.

The format of the HDF5 output files produced by these various IO implementations is identical; only the method by which they are written differs. It is possible to create a checkpoint file with the parallel routines and restart Flash-X from that file using the serial routines or vice-versa. (This switch would require resetting up and compiling a code to get an executable with the serial version of IO.) When outputting with the Uniform Grid, some data is stored that isn't explicitly necessary for data analysis or visualization, but is retained to keep the output format of PARAMESH the same as with the Uniform Grid. See ?? for more information on output data formats. For example, the refinement level in the Uniform Grid case is always equal to 1, as is the nodetype array. A tree structure for the Uniform Grid is 'faked' for visualization purposes. In a similar way, the non-fixedblocksize mode outputs all of the data stored by the grid as though it is one large block. This allows restarting with differing numbers of processors and decomposing the domain in an arbitrary fashion in Uniform Grid.

Parallel HDF5 mode has two runtime parameters useful for debugging: [[rpi reference]] and [[rpi reference]]. When these runtime parameters are true, the FLASH-X input and output routines read and/or output the guard cells in addition to the normal interior cells. Note that the HDF5 files produced are *not* compatible with the visualization and analysis tools provided with FLASH-X.

7.9.1.1 Collective Mode

By default, the parallel mode of HDF5 uses an independent access pattern for writing datasets and performs IO without aggregating the disk access for writing. Parallel HDF5 can also be run so that the writes to the file's datasets are aggregated, allowing the data from multiple processors to be written to disk in fewer operations. This can greatly increase the performance of IO on filesystems that support this behavior. FLASH-X can make use of this mode by setting the runtime parameter useCollectiveHDF5 to true.

7.9.1.2 Machine Compatibility

The HDF5 modules have been tested successfully on the ASC platforms and on a Linux clusters. Performance varies widely across the platforms, but the parallel version is usually faster than the serial version. Experience on performing parallel IO on a Linux Cluster using PVFS is reported in Ross *et al.* (2001). Note that for clusters without a parallel filesystem, you should not use the parallel HDF5 IO module with an NFS mounted filesystem. In this case, all of the information will still have to pass through the node from which the disk is hanging, resulting in contention. It is recommended that a serial version of the HDF5 unit be used instead.

7.9.1.3 HDF5 Data Format

The HDF5 data format for FLASH-X is identical to FLASH-X for all grid variables and datastructures used to recreate the tree and neighbor data with the exception that bounding box, coordinates, and block size are now sized as mdim, or the maximum dimensions supported by Flash-X's grids, which is three, rather than ndim. PARAMESH 4.0 and PARAMESH 4dev, however, do requires a few additional tree data structures to be output which are described below. The format of the metadata stored in the HDF5 files has changed to reduce the number of 'writes' required. Additionally, scalar data, like time, dt, nstep, etc., are now stored in a linked list and written all at one time. Any unit can add scalar data to the checkpoint file by calling the routine [[api reference]]. See ?? for more details. The FLASH-X HDF5 format is summarized in ??.

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Table 7.7: Flash-X HDF5 file format.

Record label Description of the record

Simulation Meta Data: included in all files

sim_info.fflags:

sim info Stores simulation meta data in a user defined C structure.

Structure datatype and attributes of the structure are de-

```
scribed below.
typedef struct sim_info_t {
  int file_format_version;
  char setup_call[400];
  char file_creation_time[MAX_STRING_LENGTH];
  char flash_version[MAX_STRING_LENGTH];
  char build_date[MAX_STRING_LENGTH];
  char build_dir[MAX_STRING_LENGTH];
  char build_machine[MAX_STRING_LENGTH];
  char cflags[400];
  char fflags[400];
  char setup_time_stamp[MAX_STRING_LENGTH];
  char build_time_stamp[MAX_STRING_LENGTH];
} sim_info_t;
sim_info_t sim_info;
sim_info.file_format_version:
                                    An integer giving the version number of the HDF5 file
                                    format. This is incremented anytime changes are made to
                                    the layout of the file.
sim_info.setup_call:
                                    The complete syntax of the setup command used when
                                    creating the current Flash-X executable.
sim_info.file_creation_time:
                                    The time and date that the file was created.
                                    The version of Flash-X used for the current simulation.
sim_info.flash_version:
                                    This is returned by routine setup_flashVersion.
sim_info.build_date:
                                    The date and time that the Flash-X executable was com-
                                    piled.
sim_info.build_dir:
                                    The complete path to the Flash-X root directory of the
                                    source tree used when compiling the Flash-X executable.
                                    This is generated by the subroutine setup_buildstats
                                    which is created at compile time by the Makefile.
sim_info.build_machine:
                                    The name of the machine (and anything else returned from
                                    uname -a) on which Flash-X was compiled.
sim_info.cflags:
                                    The c compiler flags used in the given simulation. The
                                    routine setup_buildstats is written by the setup script
                                    at compile time and also includes the fflags below.
```

The f compiler flags used in the given simulation.

Table 7.7: HDF5 format (continued).

Record label	Description of the record
sim_info.setup_time_stamp:	The date and time the given simulation was setup. The routine setup_buildstamp is created by the setup script at compile time.
${\tt sim_info.build_time_stamp:}$	The date and time the given simulation was built. The routine setup_buildstamp is created by the setup script at compile time.

RuntimeParameter and Scalar data

Data are stored in linked lists with the nodes of each entry for each type listed below.

```
typedef struct int_list_t {
  char name[MAX_STRING_LENGTH];
  int value;
} int_list_t;
typedef struct real_list_t {
  char name[MAX_STRING_LENGTH];
  double value;
} real_list_t;
typedef struct str_list_t {
  char name[MAX_STRING_LENGTH];
  char value[MAX_STRING_LENGTH];
} str_list_t;
typedef struct log_list_t {
  char name[MAX_STRING_LENGTH];
  int value;
} log_list_t;
int_list_t *int_list;
real_list_t *real_list;
str_list_t *str_list;
log_list_t *log_list;
integer runtime parameters
                                   int_list_t int_list(numIntParams)
                                   A linked list holding the names and values of all the integer
                                   runtime parameters.
real runtime parameters
                                   real_list_t real_list(numRealParams)
                                   A linked list holding the names and values of all the real
                                   runtime parameters.
                                   str_list_t str_list(numStrParams)
string runtime parameters
                                   A linked list holding the names and values of all the string
                                   runtime parameters.
```

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Table 7.7: HDF5 format (continued).

Record label	Description of the record
logical runtime parameters	log_list_t log_list(numLogParams)
	A linked list holding the names and values of all the logical runtime parameters.
integer scalars	int_list_t int_list(numIntScalars)
	A linked list holding the names and values of all the integer scalars.
real scalars	real_list_t real_list(numRealScalars)
	A linked list holding the names and values of all the real scalars.
string scalars	str_list_t str_list(numStrScalars)
	A linked list holding the names and values of all the string scalars.
logical scalars	<pre>log_list_t log_list(numLogScalars)</pre>
	A linked list holding the names and values of all the logical scalars.
Grid data: included only in checkpoin unknown names	et files and plotfiles character*4 unk_names(nvar)
	This array contains four-character names corresponding to the first index of the unk array. They serve to identify the variables stored in the 'unknowns' records.
refine level	<pre>integer lrefine(globalNumBlocks)</pre>
	This array stores the refinement level for each block.
node type	<pre>integer nodetype(globalNumBlocks)</pre>
	This array stores the node type for a block. Blocks with node type 1 are leaf nodes, and their data will always be valid. The leaf blocks contain the data which is to be used for plotting purposes.
gid	<pre>integer gid(nfaces+1+nchild,globalNumBlocks)</pre>
	This is the global identification array. For a given block, this array gives the block number of the blocks that neighbor it and the block numbers of its parent and children.
coordinates	real coord(mdim,globalNumBlocks)
	This array stores the coordinates of the center of the block. coord(1,blockID) = x-coordinate coord(2,blockID) = y-coordinate coord(3,blockID) = z-coordinate

Table 7.7: HDF5 format (continued).

Record label	Description of the record
block size	real size(mdim,globalNumBlocks) This array stores the dimensions of the current block. size(1,blockID) = x size size(2,blockID) = y size size(3,blockID) = z size
bounding box	real bnd_box(2,mdim,globalNumBlocks) This array stores the minimum (bnd_box(1,:,:)) and maximum (bnd_box(2,:,:)) coordinate of a block in each spatial direction.
which child (Paramesh4.0 and Paramesh4dev only!)	integer which_child(globalNumBlocks) An integer array identifying which part of the parents' volume this child corresponds to.
variable	 real unk(nxb,nyb,nzb,globalNumBlocks) nx = number of cells/block in x ny = number of cells/block in y nz = number of cells/block in z This array holds the data for a single variable. The record label is identical to the four-character variable name stored in the record unknown names. Note that, for a plot file with CORNERS=.true. in the parameter file, the information is interpolated to the cell corners and stored.
Particle Data: included in checkpoint localnp	files and particle files integer localnp(globalNumBlocks) This array holds the number of particles on each processor.
particle names	character*24 particle_labels(NPART_PROPS) This array contains twenty four-character names corresponding to the attributes in the particles array. They serve to identify the variables stored in the 'particles' record.
tracer particles	real particles (NPART_PROPS, globalNumParticles Real array holding the particles data structure. The first dimension holds the various particle properties like, velocity, tag etc. The second dimension is sized as the total number of particles in the simulation. Note that all the particle properties are real values.

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7.9.1.4 Split File IO

On machines with large numbers of processors, IO may perform better if, all processors write to a limited number of separate files rather than one single file. This technique can help mitigate IO bottlenecks and contention issues on these large machines better than even parallel-mode IO can. In addition this technique has the benefit of keeping the number of output files much lower than if every processor writes its own file. Split file IO can be enabled by setting the [[rpi reference]] parameter to the number of files desired (i.e. if outputSplitNum is set to 4, every checkpoint, plotfile and particle file will be broken into 4 files, by processor number). This feature is only available with the HDF5 parallel IO mode, and is still experimental. Users should use this at their own risk.

7.9.2 Parallel-NetCDF

Another implementation of the IO unit uses the Parallel-NetCDF library available at http://www.mcs.anl.gov/parallel-netcdf/. At this time, the Flash-X code requires version 1.1.0 or higher. Our testing shows performance of PNetCDF library to be very similar to HDF5 library when using collective I/O optimizations in parallel I/O mode.

There are two different PnetCDF IO unit implementations. Both are parallel implementations, one for each supported grid, the Uniform Grid and PARAMESH. It is important to remember to match the IO implementation with the correct grid. To include PnetCDF IO in a simulation the user should add—unit=IO/IOMain/pnetcdf..... to the setup line. See examples below for the two different PnetCDF IO implementations.

```
./setup Sod -2d -auto -unit=I0/I0Main/pnetcdf/PM
./setup Sod -2d -auto -unit=Grid/GridMain/UG -unit=I0/I0Main/pnetcdf/UG
```

The paths to these IO implementations can be long and tedious to type, users are advised to set up shortcutsfor various implementations. See ?? for information about creating shortcuts.

To the end-user, the PnetCDF data format is very similar to the HDF5 format. (Under the hood the data storage is quite different.) In HDF5 there are datasets and dataspaces, in PnetCDF there are dimensions and variables. All the same data is stored in the PnetCDF checkpoint as in the HDF5 checkpoint file, although there are some differences in how the data is stored. The grid data is stored in multidimensional arrays, as it is in HDF5. These are unknown names, refine level, node type, gid, coordinates, proc number, block size and bounding box. The particles data structure is also stored in the same way. The simulation metadata, like file format version, file creation time, setup command line, etc., are stored as global attributes. The runtime parameters and the output scalars are also stored as attributes. The unk and particle labels are also stored as global attributes. In PnetCDF, all global quantities must be consistent across all processors involved in a write to a file, or else the write will fail. All IO calls are run in a collective mode in PnetCDF.

7.9.3 Direct IO

As mentioned above, the direct IO implementation has been added so users can always output data even if the HDF5 or pnetCDF libraries are unavailable. The user should examine the two helper routines <code>io_writeData</code> and <code>io_readData</code>. Copy the base implementation to a simulation directory, and modify them in order to write out specifically what is needed. To include the direct IO implementation add the following to your setup line:

-unit=IO/IOMain/direct/UG or -unit=IO/IOMain/direct/PM

7.9.4 Output Side Effects

In FLASH-X when plotfiles or checkpoint files are output by [[api reference]], the grid is fully restricted and user variables are computed prior to writing the file. [[api reference]] and [[api reference]] by default, do not do this step themselves. The restriction can be forced for all writes by setting runtime parameter [[rpi reference]] to true and the user variables can always be computed prior to output by setting [[rpi reference]] to true.

7.10 Working with Output Files

The checkpoint file output formats offer great flexibility when visualizing the data. The visualization program does not have to know the details of how the file was written; rather it can query the file to find the number of dimensions, block sizes, variable data etc that it needs to visualize the data. IDL routines for reading HDF5 and PnetCDF formats are provided in tools/fidlr3/. These can be used interactively though the IDL command line (see ??). In addition, ViSit version 10.0 and higher (see ??) can natively read FLASH-X HDF5 output files by using the command line option -assume_format Flash-X.

7.11 Unit Test

The IO unit test is provided to test IO performance on various platforms with the different Flash-X IO implementations and parallel libraries. The unitTest is setup like any other FLASH-X simulation. It can be run with any IO implementation as long as the correct Grid implementation is included. This unitTest writes a checkpoint file, a plotfile, and if particles are included, a particle file. Particles IO can be tested simply by including particles in the simulation. Variables needed for particles should be uncommented in the Config file.

Example setups:

mpirun -np numProcs flash3

```
#setup for PARAMESH Grid and serial HDF5 io
./setup unitTest/IO -auto

#setup for PARAMESH Grid with parallel HDF5 IO (see shortcuts docs for explanation)
./setup unitTest/IO -auto +parallelIO (same as)
./setup unitTest/IO -auto -unit=IO/IOMain/hdf5/parallel/PM

#setup for Uniform Grid with serial HDF5 IO, 3d problem, increasing default number of zones
./setup unitTest/IO -3d -auto +ug -nxb=16 -nyb=16 -nzb=16 (same as)
./setup unitTest/IO -3d -auto -unit=Grid/GridMain/UG -nxb=16 -nyb=16 -nzb=16

#setup for PM3 and parallel netCDF, with particles
./setup unitTest/IO -auto -unit=Particles +pnetcdf

#setup for UG and parallel netCDF
./setup unitTest/IO -auto +pnetcdf +ug
Run the test like any other Flash-X simulation:
```

There are a few things to keep in mind when working with the IO unit test:

- The Config file in unitTest/IO declares some dummy grid scope variables which are stored in the unk array. If the user wants a more intensive IO test, more variables can be added. Variables are initialized to dummy values in Driver_evolveFlash.
- Variables will only be output to the plotfile if they are declared in the flash.par (see the example flash.par in the unit test).
- The only units besides the simulation unit included in this simulation are Grid, IO, Driver, Timers, Logfile, RuntimeParameters and PhysicalConstants.
- If the PARAMESH Grid implementation is being used, it is important to note that the grid will not refine on its own. The user should set lrefine_min to a value > 1 to create more blocks. The user could also set the runtime parameters nblockx, nblocky, nblockz to make a bigger problem.

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• Just like any other simulation, the user can change the number of zones in a simulation using -nxb=-numZones on the setup line.

7.12 Derived data type I/O

In FLASH-X we introduced an alternative I/O implementation for both HDF5 and Parallel-NetCDF which is a slight spin on the standard parallel I/O implementations. In this new implementation we select the data from the mesh data structures directly using HDF5 hyperslabs (HDF5) and MPI derived datatypes (Parallel-NetCDF) and then write the selected data to datasets in the file. This eliminates the need for manually copying data into a Flash-X allocated temporary buffer and then writing the data from the temporary buffer to disk.

You can include derived data type I/O in your Flash-X application by adding the setup shortcuts <code>+hdf5TypeIO</code> for HDF5 and <code>+pnetTypeIO</code> for Parallel-NetCDF to your setup line. If you are using the HDF5 implementation then you need a parallel installation of HDF5. All of the runtime parameters introduced in this chapter should be compatible with derived data type I/O.

A nice property of derived data type I/O is that it eliminates a lot of the I/O code duplication which has been spreading in the Flash-X I/O unit over the last decade. The same code is used for UG, NoFBS and Paramesh Flash-X applications and we have also shared code between the HDF5 and Parallel-NetCDF implementations. A technical reason for using the new I/O implementation is that we provide more information to the I/O libraries about the exact data we want to read from / write to disk. This allows us to take advantage of recent enhancements to I/O libraries such as the nonblocking APIs in the Parallel-NetCDF library. We discuss experimentation with this API and other ideas in the paper "A Case Study for Scientific I/O: Improving the Flash-X Astrophysics Code" www.mcs.anl.gov/uploads/cels/papers/P1819.pdf

The new I/O code has been tested in our internal Flash-X regression tests from before the FLASH-X release and there are no known issues, however, it will probably be in the release following FLASH-X when we will recommend using it as the default implementation. We have made the research ideas from our case study paper usable for all Flash-X applications, however, the code still needs a clean up and exhaustive testing with all the Flash-X runtime parameters introduced in this chapter.

Chapter 8

Runtime Parameters Unit

The RuntimeParameters Unit stores and maintains a global linked lists of runtime parameters that are used during program execution. Runtime parameters can be added to the lists, have their values modified, and be queried. This unit handles adding the default runtime parameters to the lists as well as reading any overwritten parameters from the flash.par file.

8.1 Defining Runtime Parameters

All parameters must be declared in a Config file with the keyword declaration PARAMETER. In the Config file, assign a data type and a default value for the parameter. If possible, assign a range of valid values for the parameter. You can also provide a short description of the parameter's function in a comment line that begins with D.

```
#section of Config file for a Simulation
D myParameter Description of myParameter
PARAMETER myParameter REAL 22.5 [20 to 60]
```

To change the runtime parameter's value from the default, assign a new value in the flash.par for the simulation.

```
#snippet from a flash.par
myParameter = 45.0
```

See ?? for more information on declaring parameters in a Config file.

8.2 Identifying Valid Runtime Parameters

The values of runtime parameters are initialized either from default values defined in the Config files, or from values explicitly set in the file flash.par. Variables that have been changed from default are noted in the simulation's output log. For example, the RuntimeParameters section of the output log shown in ?? indicates that [[rpi reference]] and [[rpi reference]] have been read in from flash.par and are different than the default values, whereas the runtime parameter [[rpi reference]] has been left at the default value of 0.

After a simulation has been configured with a setup call, all possible valid runtime parameters are listed in the file setup-params located in the object directory (or whatever directory was chosen with -objdir=) with their default values. This file groups the runtime parameters according to the units with which they are associated and in alphabetical order. A short description of the runtime parameter, and the valid range or values if known, are also given. See ?? for an example listing.

8.3 Routine Descriptions

The Runtime Parameters unit is included by default in all of the provided Flash-X simulation examples, through a dependence within the Driver unit. The main Flash-X initialization routine ([[api reference]]) and

Figure 8.1: Section of output log showing runtime parameters values

```
physics/Eos/EosMain/Multigamma
gamma [REAL] [1.6667]
Valid Values: Unconstrained
Ratio of specific heats for gas

physics/Hydro/HydroMain
cfl [REAL] [0.8]
Valid Values: Unconstrained
Courant factor
```

Figure 8.2: Portion of a setup_params file from an object directory.

the initialization code created by setup handles the creation and initialization of the runtime parameters, so users will mainly be interested in querying parameter values. Because the RuntimeParameters routines are overloaded functions which can handle character, real, integer, or logical arguments, the user *must* make sure to use the interface file RuntimeParameters_Interfaces in the calling routines.

The user will typically only have to use one routine from the Runtime Parameters API, [[api reference]]. This routine retrieves the value of a parameter stored in the linked list in the Runtime-Parameters_data module. In Flash-X the value of runtime parameters for a given unit are stored in that unit's Unit_data Fortran module and they are typically initialized in the unit's Unit_init routine. Each unit's 'init' routine is only called once at the beginning of the simulation by [[api reference]]. For more documentation on the Flash-X code architecture please see ??. It is important to note that even though runtime parameters are declared in a specific unit's Config file, the runtime parameters linked list is a global space and so any unit can fetch a parameter, even if that unit did not declare it. For example, the Driver unit declares the logical parameter restart, however, many units, including the IO unit get restart parameter with the [[api reference]] interface. If a section of the code asks for a runtime parameter that was not declared in a Config file and thus is not in the runtime parameters linked list, the Flash-X code will call [[api reference]] and stamp an error to the logfile. The other RuntimeParameter routines in the API are not generally called by user routines. They exist because various other units within Flash-X need to access parts of the RuntimeParameters interface. For example, the input/output unit IO needs [[api reference]]. There are no user-defined parameters which affect the RuntimeParameters unit.

8.4 Example Usage

An implementation example from the [[api reference]] is straightforward. First, use the module containing definitions for the unit (for _init subroutines, the usual use Unit_data, ONLY: structure is waived). Next, use the module containing interface definitions of the RuntimeParameters unit, i.e., use Runtime-

8.4. EXAMPLE USAGE

Parameters_interface, ONLY:. Finally, read the runtime parameters and store them in unit-specific variables.

```
subroutine IO_init()

use IO_data
use RuntimeParamters_interface, ONLY : RuntimeParameters_get
implicit none

call RuntimeParameters_get('plotFileNumber',io_plotFileNumber)
call RuntimeParameters_get('checkpointFileNumber',io_checkpointFileNumber)

call RuntimeParameters_get('plotFileIntervalTime',io_plotFileIntervalTime)
call RuntimeParameters_get('plotFileIntervalStep',io_plotFileIntervalStep)
call RuntimeParameters_get('checkpointFileIntervalTime',io_checkpointFileIntervalTime)
call RuntimeParameters_get('checkpointFileIntervalStep',io_checkpointFileIntervalStep)
!! etc ...
```

Note that the parameters found in the flash.par or in the Config files, for example [[rpi reference]], are generally stored in a variable of the same name with a unit prefix prepended, for example io_plotFileNumber. In this way, a program segment clearly indicates the origin of variables. Variables with a unit prefix (e.g., io_for IO, pt_ for particles) have been initialized from the RuntimeParameters database, and other variables are locally declared. When creating new simulations, runtime parameters used as variables should be prefixed with sim_.

Chapter 9

Multispecies Unit

Flash-X has the ability to track multiple fluids, each of which can have its own properties. The Multi-species unit handles setting and querying on the properties of fluids, as well as some common operations on properties. The advection and normalization of species is described in the context of the Hydro unit in ??.

9.1 Defining Species

The names and properties of fluids are accessed by using their constant integer values defined in the Simulation.h header file. The species names are defined in a Config file. The names of the species, for example AIR, NI56, are given in the Config file with keyword SPECIES.

In the traditional method for defining species, this Config would typically be the application's Config file in the Simulation unit. In the alternative method described below in ??, SPECIES are normally not listed explicitly in the Simulation unit Config, but instead are automatically generated by Multispecies/MultispeciesMain/Config based on the contents of the species setup variable. Either way, the setup procedure transforms those names into accessor integers with the appended description _SPEC.

These names are stored in the Simulation.h file. The total number of species defined is also defined within Simulation.h as NSPECIES, and the integer range of their definition is given by SPECIES_BEGIN and SPECIES_END. To access the species in your code, use the index listed in Simulation.h, for example AIR_SPEC, NI56_SPEC.

Note that NSPECIES_BEGIN, and SPECIES_END are always defined, whether a simulation uses multiple species or not (and whether the simulation includes the Multispecies unit or not). However, if NSPECIES_END will be less than SPECIES_BEGIN, and then neither of them should be used as an index into solution vectors.

As an illustration, Figures ?? and ?? are snippets from a configuration file and the corresponding section of the Flash-X header file, respectively. For more information on Config files, see ??; for more information on the setup procedure, see ??; for more information on the structure of the main header file Simulation.h, see ??.

```
# Portion of a Config file for a Simulation
SPECIES AIR
SPECIES SF6
```

Figure 9.1: Sample Config file showing how to define required fluid species.

```
#define SPECIES_BEGIN (NPROP_VARS + CONSTANT_ONE)
#define AIR_SPEC 11
#define SF6_SPEC 12
#define NSPECIES 2
#define SPECIES_END (SPECIES_BEGIN + NSPECIES - CONSTANT_ONE)
```

Figure 9.2: Sample excerpt from header file Simulation.h showing integer definition of fluid species.

Table 9.1.	Properties	available	through	the	Multispecies	unit
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Property Name	Description	Data type
A	Number of protons and neutrons in nucleus	real
Z	Atomic number	real
N	Number of neutrons	real
E	Number of electrons	real
BE	Binding Energy	real
GAMMA	Ratio of heat capacities	real
MS_ZMIN	Minimum allowed average ionization	real
MS_EOSTYPE	EOS type to use for MTMMMT EOS	integer
MS_EOSSUBTYPE	EOS subtype to use for MTMMMT EOS	integer
MS_EOSZFREEFILE	Name of file with ionization data	string
MS_EOSENERFILE	Name of file with internal energy data	string
MS_EOSPRESFILE	Name of file with pressure data	string
$MS_NUMELEMS$	Number of elements comprising this species	integer
MS_ZELEMS	Atomic number of each species element	array(integer)
MS_AELEMS	Mass number of each species element	array(real)
MS_FRACTIONS	Number fraction of each species element	array(real)
MS_OPLOWTEMP	Temperature at which cold opacities are used	real

Flash-X Transition

In FLASH-X, you found the integer index of a species by using find_fluid_index. In FLASH-X, the species index is always available because it is defined in Simulation.h. Use the index directory, as in xIn(NAME_SPEC - SPECIES_BEGIN + 1) = solnData(NAME_SPEC,i,j,k). But be careful that the species name is really defined in your simulation! You can test with

```
if (NAME_SPEC /= NONEXISTENT) then
   okVariable = solnData(NAME_SPEC,i,j,k)
endif
```

The available properties of an individual fluid are listed in ?? and are defined in file Multispecies.h. In order to reference the properties in code, you must #include the file Multispecies.h. The initialization of properties is described in the following section.

9.2 Initializing Species Information in Simulation_initSpecies

Before you can work with the properties of a fluid, you must initialize the data in the Multispecies unit. Normally, initialization is done in the routine [[api reference]]. An example procedure is shown below and

subroutine Simulation_initSpecies()

end subroutine Simulation_initSpecies

implicit none
#include "Multispecies.h"
#include "Simulation.h"

! These two variables are defined in the Config file as
! SPECIES SF6 and SPECIES AIR
 call Multispecies_setProperty(SF6_SPEC, A, 146.)
 call Multispecies_setProperty(SF6_SPEC, Z, 70.)
 call Multispecies_setProperty(SF6_SPEC, GAMMA, 1.09)

call Multispecies_setProperty(AIR_SPEC, A, 28.66)
 call Multispecies_setProperty(AIR_SPEC, Z, 14.)
 call Multispecies_setProperty(AIR_SPEC, GAMMA, 1.4)

Figure 9.3: A Simulation_initSpecies.F90 file showing Multispecies initialization

consists of setting relevant properties for all fluids/SPECIES defined in the Config file. Fluids do not have to be isotopes; any molecular substance which can be defined by the properties shown in ?? is a valid input to the Multispecies unit.

Flash-X Transition

For nuclear burning networks, a Simulation_initSpecies routine is already predefined. It automatically initializes all isotopes found in the Config file. To use this shortcut, REQUIRE the module Simulation/SimulationComposition in the Config file.

9.3 Specifying Constituent Elements of a Species

A species can represent a specific isotope or a single element or a more complex material. Some units in Flash-X require information about the elements that constitute a single species. For example, water is comprised of two elements: Hydrogen and Oxygen. The Multispecies database can store a list of the atomic numbers, mass numbers, and relative number fractions of each of the elements within a given species. This information is stored in the array properties MS_ZELEMS, MS_AELEMS, and MS_FRACTIONS respectively. The property MS_NUMELEMS contains the total number of elements for a species (MS_NUMELEMS would be two for water since water is made of Hydrogen and Oxygen). There is an upper bound on the number of elements for a single species which is defined using the preprocessor symbol MS_MAXELEMS in the "Simulation.h" header file and defaults to six. The value of MS_MAXELEMS can be changed using the ms_maxelems setup variable. ?? shows an example of how the constituent elements for water can be set using the Simulation_initSpecies subroutine.

The constituent element information is optional and is only needed if a particular unit of interest requires it. At present, only the analytic cold opacities used in the Opacity unit make use of the constituent element information.

9.4 Alternative Method for Defining Species

?? described how species can be defined by using the SPECIES keyword in the Config file. ?? then described how the properties of the species can be set using various subroutines defined in the Multispecies unit.

```
#include "Simulation.h"
#include "Multispecies.h"
! Create arrays to store constituent element data. Note that these
! arrays are always of length MS_MAXELEMS.
real :: aelems(MS_MAXELEMS)
real :: fractions(MS_MAXELEMS)
integer :: zelems(MS_MAXELEMS)
call Multispecies_setProperty(H2O_SPEC, A, 18.0/3.0) ! Set average mass number
call Multispecies_setProperty(H2O_SPEC, Z, 10.0/3.0) ! Set average atomic number
call Multispecies_setProperty(H2O_SPEC, GAMMA, 5.0/3.0)
call Multispecies_setProperty(H20_SPEC, MS_NUMELEMS, 2)
aelems(1) = 1.0 ! Hydrogen
aelems(2) = 16.0 ! Oxygen
call Multispecies_setProperty(H2O_SPEC, MS_AELEMS, aelems)
zelems(1) = 1 ! Hydrogen
zelems(2) = 8 ! Oxygen
call Multispecies_setProperty(H20_SPEC, MS_ZELEMS, zelems)
fractions(1) = 2.0/3.0 ! Two parts Hydrogen
fractions(2) = 1.0/3.0 ! One part Oxygen
call Multispecies_setProperty(H2O_SPEC, MS_FRACTIONS, fractions)
```

Figure 9.4: A Simulation_initSpecies.F90 file showing Multispecies initialization

Property Name	Runtime Parameter Name
A	ms_ <spec>A</spec>
Z	ms_ <spec>Z</spec>
N	ms_ <spec>Neutral</spec>
E	ms_ <spec>Negative</spec>
BE	ms_ <spec>BindEnergy</spec>
GAMMA	ms_ <spec>Gamma</spec>
MS_ZMIN	$ms_{<}spec>Zmin$
MS_EOSTYPE	eos_ <spec>EosType</spec>
MS_EOSSUBTYPE	eos_ <spec>SubType</spec>
MS_EOSZFREEFILE	eos_ <spec>TableFile</spec>
MS_EOSENERFILE	eos_ <spec>TableFile</spec>
MS_EOSPRESFILE	eos_ <spec>TableFile</spec>
MS_NUMELEMS	ms_ <spec>NumElems</spec>
MS_ZELEMS	ms_ <spec>ZElems_<n></n></spec>
MS_AELEMS	ms_ <spec>AElems_<n></n></spec>
MS_FRACTIONS	ms_ <spec>Fractions_<n></n></spec>
MS_OPLOWTEMP	op_ <spec>LowTemp</spec>

Table 9.2: Automatically Generated Multispecies Runtime Parameters

There is an alternative to these approaches which uses setup variables to define the species, then uses runtime parameters to set the properties of each species. This allows users to change the number and names of species without modifying the Config file and also allows users to change properties without recompiling the code.

Species can be defined using the species setup variable. For example, to create two species called AIR and SF6 one would specify species=air,sf6 in the simulation setup command. Using this setup variable and using the SPECIES keyword in the Config file are mutually exclusive. Thus, the user must choose which method they wish to use for a given simulation. Certain units, such as the Opacity unit, requires the use of the setup variable.

When species are defined using the setup variable approach, the Multispecies unit will automatically define several runtime parameters for each species. These runtime parameters can be used set the properties shown in ??. The runtime parameter names contain the species name. ?? shows an example of the mapping between runtime parameters and Multispecies properties, where <spec> is replaced by the species name as specified in the species setup argument list. Some of these runtime parameters are arrays, and thus the <N> is a number ranging from 1 to MS_MAXELEMS. The Simulation_initSpecies subroutine can be used to override the runtime parameter settings.

9.5 Routine Descriptions

We now briefly discuss some interfaces to the multifluid database that are likely of interest to the user. Many of these routines include optional arguments.

• [[api reference]] This routine sets the value species property. It should be called within the subroutine [[api reference]] for all the species of interest in the simulation problem, and for all the required properties (any of A, Z, N, E, EB, GAMMA).

Flash-X Transition

In FLASH-X, you could set multiple properties at once in a call to add_fluid_to_db. In FLASH-X, individual calls are required. If you are setting up a nuclear network, there is a precoded [[api reference]] to easily initialize all necessary species. It is located in the unit Simulation/SimulationComposition, which must be listed in your simulation Config file.

- [[api reference]] Returns the value of a requested property.
- [[api reference]] Returns a weighted sum of a chosen property of species. The total number of species can be subset. The weights are optional, but are typically the mass fractions X_i of each of the fluids at a point in space. In that case, if the selected property (one of $A_i, Z_i, \ldots, \gamma_i$) is denoted \mathcal{P}_i , the sum calculated is

$$\sum_{i} X_{i} \mathcal{P}_{i} \quad .$$

• [[api reference]] Returns the weighted average of the chosen property. As in Multispecies_getSum, weights are optional and a subset of species can be chosen. If the weights are denoted w_i and the selected property (one of $A_i, Z_i, \ldots, \gamma_i$) is denoted \mathcal{P}_i , the average calculated is

$$\frac{1}{N} \sum_{i}^{N} w_i \mathcal{P}_i \quad ,$$

where N is the number of species included in the sum; it may be less than the number of all defined species if an average over a subset is requested.

• [[api reference]] Same as Multispecies_getSum, but compute the weighted sum of the inverse of the chosen property. If the weights are denoted w_i and the selected property (one of $A_i, Z_i, \ldots, \gamma_i$) is denoted \mathcal{P}_i , the sum calculated is

$$\sum_{i}^{N} \frac{w_i}{\mathcal{P}_i} \quad .$$

For example, the average atomic mass of a collection of fluids is typically defined by

$$\frac{1}{\bar{A}} = \sum_{i} \frac{X_i}{A_i} , \qquad (9.1)$$

where X_i is the mass fraction of species i, and A_i is the atomic mass of that species. To compute \bar{A} using the multifluid database, one would use the following lines

where xn(:) is an array of the mass fractions of each species in Flash-X. This method allows some of the mass fractions to be zero.

• [[api reference]] Same as Multispecies_getSum, but compute the weighted sum of the chosen property divided by the total number of particles (A_i) . If the weights give the mass fractions X_i of the fluids at a point in space and the selected property (one of $A_i, Z_i, \ldots, \gamma_i$) is denoted \mathcal{P}_i , the sum calculated is

$$\sum_{i} \frac{X_i}{A_i} \mathcal{P}_i \quad .$$

9.6. EXAMPLE USAGE 125

• [[api reference]] Same as Multispecies_getSum, but compute the weighted sum of the squares of the chosen property values. If the weights are denoted w_i and the selected property (one of $A_i, Z_i, \ldots, \gamma_i$) is denoted \mathcal{P}_i , the sum calculated is

$$\sum_{i}^{N} w_i \mathcal{P}_i^2 \quad .$$

• [[api reference]] List the contents of the multifluid database in a snappy table format.

9.6 Example Usage

In general, to use Multispecies properties in a simulation, the user must only properly initialize the species as described above in the Simulation_init routine. But to program with the Multispecies properties, you must do three things:

- #include the Simulation.h file to identify the defined species
- #include the Multispecies.h file to identify the desired property
- use the Fortran interface to the Multispecies unit because the majority of the routines are overloaded.

The example below shows a snippet of code to calculate the electron density.

9.7 Unit Test

The unit test for Multispecies provides a complete example of how to call the various API routines in the unit with all variations of arguments. Within [[api reference]], incorrect usage is also indicated within commented-out statements.

Chapter 10

Physical Constants Unit

The Physical Constants unit provides a set of common constants, such as Pi and the gravitational constant, in various systems of measurement units. The default system of units is CGS, so named for having a length unit in centimeters, a mass unit in grams, and a time unit in seconds. In CGS, the charge unit is the esu, and the temperature unit is the Kelvin. The constants can also be obtained in the standard MKS system of units, where length is in meters, mass in kilograms, and time in seconds. For MKS units, charge is in Coloumbs, and temperature in Kelvin.

Flash-X Transition

For ease of usage, the constant PI=3.14159.... is defined in the header file constants.h. Including this file with #include "constants.h" is an alternate way to access the value of π , rather than needing to include the PhysicalConstants unit.

Any constant can optionally be converted from the standard units into any other available units. This facility makes it easy to ensure that all parts of the code are using a consistent set of physical constant values and unit conversions.

For example, a program using this unit might obtain the value of Newton's gravitational constant G in units of $\mathrm{Mpc^3~Gyr^{-2}}M_{\odot}^{-1}$ by calling

In this example, the local variable G is set equal to the result, 4.4983×10^{-15} (to five significant figures). Physical constants are taken from K. Nahamura *et al.* (Particle Data Group), J. Phys. G **37**, 075021 (2010).

10.1 Available Constants and Units

There are many constants and units available within FLASH-X, see ?? and ??. Should the user wish to add additional constants or units to a particular setup, the routine [[api reference]] should be overridden and the new constants added within the directory of the setup.

10.2 Applicable Runtime Parameters

There is only one runtime parameter used by the Physical Constants unit: [[rpi reference]] selects the default system of units for returned constants. It is a three-character string set to "CGS" or "MKS"; the default is CGS.

String Constant	Description
Newton	Gravitational constant G
speed of light	Speed of light
Planck	Planck's constant
electron charge	charge of an electron
electron mass	mass of an electron
proton mass	Mass of a proton
fine-structure	fine-structure constant
Avogadro	Avogadro's Mole Fraction
Boltzmann	Boltzmann's constant
ideal gas constant	ideal gas constant
Wien	Wien displacement law constant
Stefan-Boltzmann	Stefan-Boltzman constant
pi	Pi
e	e
Euler	Euler-Mascheroni constant

Table 10.1: Available Physical Constants

10.3 Routine Descriptions

The following routines are supplied by this unit.

- [[api reference]] Request a physical constant given by a string, and returns its real value. This routine takes optional arguments for converting units from the default. If the constant name or any of the optional unit names aren't recognized, a value of 0 is returned.
- [[api reference]] Initializes the Physical Constants Unit by loading all constants. This routine is called by [[api reference]] and must be called before the first invocation of PhysicalConstants_get. In general, the user does not need to invoke this call.
- [[api reference]] Lists the available physical constants in a snappy table.
- [[api reference]] Lists all the units available for optional conversion.
- [[api reference]] Lists all physical constants and units, and tests the unit conversion routines.

Flash-X Transition

The header file PhysicalConstants.h must be included in the calling routine due to the optional arguments of PhysicalConstants_get.

10.4 Unit Test

The PhysicalConstants unit test [[api reference]] is a simple exercise of the functionality in the unit. It does not require time stepping or the grid. "Correct" usage is indicated, as is erroneous usage.

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Table 10.2: Available Units for Conversion of Physical Constants

Base unit	String Constant	Value in CGS units	Description
length	cm	1.0	centimeter
time	\mathbf{S}	1.0	second
temperature	K	1.0	degree Kelvin
mass	g	1.0	gram
charge	esu	1.0	ESU charge
length	m	1.0E2	meter
length	km	1.0E5	kilometer
length	pc	3.0856775807E18	parsec
length	kpc	3.0856775807E21	kiloparsec
length	Mpc	3.0856775807E24	megaparsec
length	Gpc	3.0856775807E27	gigaparsec
length	Rsun	6.96E10	solar radius
length	AU	1.49597870662E13	astronomical unit
time	yr	3.15569252E7	year
time	Myr	3.15569252E13	megayear
time	Gyr	3.15569252E16	gigayear
mass	kg	1.0E3	kilogram
mass	Msun	1.9889225E33	solar mass
mass	amu	1.660538782E-24	atomic mass unit
charge	C	2.99792458E9	Coulomb
	Cosmology-friendly un	nits using $H_0 = 100 \text{ km/s}$	/Mpc:
length	LFLY	3.0856775807E24	1 Mpc
time	TFLY	2.05759E17	$\frac{2}{3H_0}$
mass	MFLY	9.8847E45	5.23e12 Msun

Part V Physics Units

Chapter 11

Hydrodynamics Units

The Hydro unit solves Euler's equations for compressible gas dynamics in one, two, or three spatial dimensions. We first describe the basic functionality; see implementation sections below for various extensions.

The Euler equations can be written in conservative form as

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \tag{11.1}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) + \nabla P = \rho \mathbf{g}$$
(11.1)

$$\frac{\partial \rho E}{\partial t} + \nabla \cdot [(\rho E + P) \mathbf{v}] = \rho \mathbf{v} \cdot \mathbf{g} , \qquad (11.3)$$

where ρ is the fluid density, \mathbf{v} is the fluid velocity, P is the pressure, E is the sum of the internal energy ϵ and kinetic energy per unit mass,

$$E = \epsilon + \frac{1}{2}|\mathbf{v}|^2 , \qquad (11.4)$$

g is the acceleration due to gravity, and t is the time coordinate. The pressure is obtained from the energy and density using the equation of state. For the case of an ideal gas equation of state, the pressure is given by

$$P = (\gamma - 1)\rho\epsilon , \qquad (11.5)$$

where γ is the ratio of specific heats. More general equations of state are discussed in ?? and ??.

In regions where the kinetic energy greatly dominates the total energy, computing the internal energy using

$$\epsilon = E - \frac{1}{2} |\mathbf{v}|^2 \tag{11.6}$$

can lead to unphysical values, primarily due to truncation error. This results in inaccurate pressures and temperatures. To avoid this problem, we can separately evolve the internal energy according to

$$\frac{\partial \rho \epsilon}{\partial t} + \nabla \cdot [(\rho \epsilon + P) \mathbf{v}] - \mathbf{v} \cdot \nabla P = 0.$$
(11.7)

If the internal energy is a small fraction of the kinetic energy (determined via the runtime parameter [[rpi reference]), then the total energy is recomputed using the internal energy from (??) and the velocities from the momentum equation. Numerical experiments using the PPM solver included with Flash-X showed that using (??) when the internal energy falls below 10^{-4} of the kinetic energy helps avoid the truncation errors while not affecting the dynamics of the simulation.

For reactive flows, a separate advection equation must be solved for each chemical or nuclear species

$$\frac{\partial \rho X_{\ell}}{\partial t} + \nabla \cdot (\rho X_{\ell} \mathbf{v}) = 0 , \qquad (11.8)$$

where X_{ℓ} is the mass fraction of the ℓ th species, with the constraint that $\sum_{\ell} X_{\ell} = 1$. Flash-X will enforce this constraint if you set the runtime parameter irenorm equal to 1. Otherwise, Flash-X will only restrict

Variable	Type	Default	Description
eintSwitch	real	0	If $\epsilon < \text{eintSwitch} \cdot \frac{1}{2} \mathbf{v} ^2$, use the internal energy
			equation to update the pressure
irenorm	integer	0	If equal to one, renormalize multifluid abundances
			following a hydro update; else restrict their values
			to lie between smallx and 1.
cfl	real	0.8	Courant-Friedrichs-Lewy (CFL) factor; must be
			less than 1 for stability in explicit schemes

Table 11.1: Runtime parameters used with the hydrodynamics (Hydro) unit.

Table 11.2: Solution variables used with the hydrodynamics (Hydro) unit.

Variable	Type	Description
dens	PER_VOLUME	density
velx	PER_MASS	x-component of velocity
vely	PER_MASS	y-component of velocity
velz	PER_MASS	z-component of velocity
pres	GENERIC	pressure
ener	PER_MASS	specific total energy $(T+U)$
temp	GENERIC	temperature

the abundances to fall between smallx and 1. The quantity ρX_{ℓ} represents the partial density of the ℓ th fluid. The code does not explicitly track interfaces between the fluids, so a small amount of numerical mixing can be expected during the course of a calculation.

The hydro unit has a capability to advect mass scalars. Mass scalars are field variables advected with density, similar to species mass fractions,

$$\frac{\partial \rho \phi_{\ell}}{\partial t} + \nabla \cdot (\rho \phi_{\ell} \mathbf{v}) = 0 , \qquad (11.9)$$

where ϕ_{ℓ} is the ℓ th mass scalar. Note that mass scalars are optional variables; to include them specify the name of each mass scalar in a Config file using the MASS_SCALAR keyword. Mass scalars are not renormalized in order to sum to 1, except when they are declared to be part of a renormalization group. See ?? for more details.

11.1 Gas hydrodynamics

11.1.1 Usage

The two gas hydrodynamic solvers supplied in the release of FLASH-X are organized into two different operator splitting methods: directionally split and unsplit. The directionally split piecewise-parabolic method (PPM) makes use of second-order Strang time splitting, and the new directionally unsplit solver is based on Monotone Upstream-centered Scheme for Conservation Laws (MUSCL) Hancock type second-order scheme.

The algorithms are described in ?? and ?? and implemented in the directory tree under physics/Hydro/HydroMain/split, and physics/Hydro/HydroMain/unsplit/Hydro_Unsplit.

Current and future implementations of Hydro use the runtime parameters and solution variables described in ?? and ??. Additional runtime parameters used either solely by the PPM method or the unsplit hydro solver are described in [[rpi reference]].

11.1.2 The unsplit hydro solver

A directionally unsplit pure hydrodynamic solver (unsplit hydro) is an alternate gas dynamics solver to the split PPM scheme. The method basically adopts a predictor-corrector type formulation (zone-edge data-extrapolated method) that provides second-order solution accuracy for smooth flows and first-order accuracy for shock flows in both space and time. Recently, the order of spatial accuracy in data reconstruction for the normal direction has been extended to implement the 3rd order PPM and 5th order Weighted ENO (WENO) methods. This unsplit hydro solver can be considered as a reduced version of the Unsplit Staggered Mesh (USM) MHD solver (see details in ??) that has been available in previous FLASH-X releases.

The unsplit hydro implementation can solve 1D, 2D and 3D problems with added capabilities of exploring various numerical implementations: different types of Riemann solvers; slope limiters; first, second, third and fifth reconstruction methods; a strong shock/rarefaction detection algorithm as well as two different entropy fix routines for Roe's linearized Riemann solver.

One of the notable features of the unsplit hydro scheme is that it particularly improves the preservation of flow symmetries as compared to the splitting formulation. Also, the scheme used in this unsplit algorithm can take a wide range of CFL stability limits (e.g., CFL < 1) for all three dimensions, which is based on using upwinded transverse flux formulations developed in the multidimensional USM MHD solver (Lee, 2006; Lee and Deane, 2009; Lee, 2013).

The above set of runtime parameters provide various types of different combinations that help in obtaining numerical accuracy, efficiency and stability. However, there are some important tips users should know before using them.

- [Extended stencil]: When NGUARD=6 is used, users should also use nxb, nyb, and nzb larger than 2*NGUARD. For example, specifying -nxb=16 in the setup works well for 1D cases. Once setting up NGUARD=6, users still can use FOG, MH, PPM, or WENO without changing NGUARD back to 4.
- [transOrder]: The first order method transOrder=1 is a default and only supported method that is stable according to the linear Fourier stability analysis. The choices for higher-order interpolations are no longer available in this release.
- [EOSforRiemann]: EOSforRiemann = .true. will call (expensive) EOS routines to compute consistent adiabatic indices (i.e., gamc, game) according to the given left and right states in Riemann solvers. For the ideal gamma law, in which those adiabatic indices are constant, it is not required to call EOS at all and users can set it .false. to reduce computation time. On the other hand, for a degenerate gas, one can enable this switch to compute thermodynamically consistent gamc, game, which in turn are used to compute the sound speed and internal energy in Riemann flux calculations. When disabled, interpolations will be used instead to get approximations of gamc, game. This interpolation method has been tested and proven to gain significant computational efficiency and accuracy, giving reliable numerical solutions even for simulating a degenerate gas.
- [Gravity coupling with Unplit Hydro Solvers]: When gravity is included in a simulation using the unsplit hydro and MHD solvers, users can choose to include gravitational source terms in the Riemann state update at n+1/2 time step (i.e., use_gravHalfUpdate=.true.). This will provide an improved second-order accuracy with respect to coupling gravitational accelerations to hydrodynamics. It should be noted that current optimized unsplit hydro/MHD codes (e.g., those selected with +uhd, +usm) do not support the runtime parameters use_gravPotUpdate and use_gravConsv of some previous Flash-X versions any more.
- [Reduced CTU vs. Full CTU for 3D in the unsplit hydro (UHD) and staggered mesh (USM) solvers]: use_3dFullCTU is a new switch that enhances a numerical stability for 3D simulations in the unsplit solvers using the corner transport upwind (CTU) algorithm by Colella. The unsplit solvers of Flash-X are different from many other shock capturing codes, in that neither UHD nor USM solvers need intermediate Riemann solver solutions for updating transverse fluxes in multidimensional problems. This provides a computational efficiency because there is a reduced number of calls to Riemann solvers per cell per time step. The total number of required Riemann solver solutions are two for 2D and three for 3D (except for extra Riemann calls for constraint-transport (CT) update in USM). This is smaller

 $\begin{tabular}{ll} Table 11.3: & Additional runtime parameters for $Interpolation Schemes$ in the unsplit hydro-solver (physics/Hydro-Mydro-Main/unsplit/Hydro-Unsplit) \end{tabular}$

Variable	Type	Default	Description
order	integer	2	Order of method in data reconstruction: 1st order Godunov (FOG), 2nd order MUSCL-Hancock (MH), 3rd order PPM, 5th order WENO.
transOrder	integer	1	Interpolation order of accuracy of taking upwind biased transverse flux derivatives in the unsplit data reconstruction: 1st, 2nd, 3rd. The choice of using transOrder=4 adopts a slope limiter between the 1st and 3rd order accurate methods to minimize oscillations in upwinding at discontinuities.
slopeLimiter	string	"vanLeer"	Slope limiter: "MINMOD", "MC", "VANLEER", "HY-BRID", "LIMITED"
LimitedSlopeBeta	real	1.0	Slope parameter specific for the "LIMITED" slope by Toro
charLimiting	logical	.true.	Enable/disable limiting on characteristic variables (.false. will use limiting on primitive variables)
${\tt use_steepening}$	logical	.false.	Enable/disable contact discontinuity steepening for PPM and WENO
$use_flattening$	logical	.false.	Enable/disable flattening (or reducing) numerical oscillations for MH, PPM, and WENO
use_avisc	logical	.false.	Enable/disable artificial viscosity for FOG, MH, PPM, and WENO
cvisc	real	0.1	Artificial viscosity coefficient
${\tt use_upwindTVD}$	logical	.false.	Enable/disable upwinded TVD slope limiter PPM. NOTE: This requires NGUARD=6
use_hybridOrder	logical	.false.	Enable an adaptively varying reconstruction order scheme reducing its order from a high-order to first-order depend- ing on monotonicity constraints
use_gravHalfUpdate	logical	.false.	On/off gravitational acceleration source terms at the half time Riemann state update
use_3dFullCTU	logical	.true.	Enable a full CTU (e.g., similar to the standard 12-Riemann solve) algorithm that provides full CFL stability in 3D. If .false., then the theoretical CFL bound for 3D becomes less than 0.5 based on the linear Fourier analysis.

Table 11.4: Additional runtime parameters for *Riemann Solvers* in the unsplit hydro solver (physics/Hydro/HydroMain/unsplit/Hydro_Unsplit)

Variable	Type	Default	Description
RiemannSolver	string	"Roe"	Different choices for Riemann solver. "LLF (local
			Lax-Friedrichs)", "HLL", "HLLC", "HYBRID",
			"ROE", and "Marquina"
${ t shock Detect}$	logical	.false.	On/off attempting to detect strong
			shocks/rarefactions (and saving flag in "shok"
			variable)
${ t shockLowerCFL}$	logical	.false.	On/off lowering of CFL factor where strong shocks
			are detected, automatically sets shockDetect if
			on.
EOSforRiemann	logical	.false.	Enable/disable calling EOS in computing each Go-
			dunov flux
entropy	logical	.false.	On/off entropy fix algorithm for Roe solver
${\tt entropyFixMethod}$	string	''HARTENHYMAN''	Entropy fix method for the Roe solver.
			"HARTEN", "HARTENHYMAN"

than the usual stabilty requirement in many other codes which needs four for 2D and twelve for 3D in order to provide a full CFL limit (i.e., CFL < 1).

In general for 3D, there is another computationally efficient approach that only uses six Riemann solutions (aka, 6-CTU) instead of solving twelve Riemann problems (aka, 12-CTU). In this efficient 6-CTU, however, the numerical stability limit becomes CFL< 0.5.

For solving 3D problems in UHD and USM, enabling the new switch use_3dFullCTU=.true. (i.e., full-CTU) will make the solution evolution scheme similar to 12-CTU while requiring to solve three Riemann problems only (again, except for the CT update in USM). On the other hand, use_3dFullCTU=.false. (i.e., reduced-CTU) will be similar to the 6-CTU integration algorithm with a reduced CFL limit (i.e., CFL < 0.5).

Stability Limits for Unsplit Hydro Solver

The unsplit solver can take a wide range of CFL limits in all three dimensions (i.e., CFL < 1). However, in some circumstances where there are strong shocks and rarefactions, shockLowerCFL=.true. could be useful to gain more numerical stability by lowering the CFL accordingly (e.g., default settings provide 0.45 for 2D and 0.25 for 3D for the Donor scheme). This approach will automatically revert such reduced stability conditions to any given original condition set by users when there are no significant shocks and rarefactions detected.

Chapter 12

Incompressible Navier-Stokes Unit

The IncompNS unit solves incompressible Navier-Stokes equations in two or three spatial dimensions. The currently released implementation assumes constant density throughout the simulation domain.

Multistep and Runge-Kutta explicit projection schemes are used for time integration. These methods are described in Armfield & Street 2002, Yang & Balaras 2006, and Vanella et al. 2010. Implementations using a staggered grid arrangement are provided for both uniform grid (UG) and PARAMESH adaptive mesh refinement Grid implementations. The MultigridMC and BiPCGStab Poisson solvers con be employed for AMR cases, whereas the homogeneous trigonometric solver + PFFT can be used in UG. Typical velocity boundary conditions for this problem are implemented.

More documentation to appear later.

Chapter 13

Equation of State Unit

13.1 Introduction

The Eos unit implements the equation of state needed by the hydrodynamics and nuclear burning solvers. The function [[api reference]] provides the interface for operating on a one-dimensional vector. The same interface can be used for a single cell by reducing the vector size to 1. Additionally, this function can be used to find the thermodynamic quantities either from the density, temperature, and composition or from the density, internal energy, and composition. For user's convenience, a wrapper function ([[api reference]]) is provided, which takes a section of a block and translates it into the data format required by the [[api reference]] function, then calls the function. Upon return from the [[api reference]] function, the wrapper translates the returned data back to the same section of the block.

Four implementations of the (Eos) unit are available in the current release of FLASH-X: Gamma which implements a perfect-gas equation of state; Gamma/RHDwhich implements a perfect-gas equation taking relativistic effects into account; Multigammawhich implements a perfect-gas equation of state with multiple fluids, each of which can have its own adiabatic index (γ) ; and Helmholtzwhich uses a fast Helmholtz free-energy table interpolation to handle degenerate/relativistic electrons/positrons and includes radiation pressure and ions (via the perfect gas approximation).

As described in previous sections, Flash-X evolves the Euler equations for compressible, inviscid flow. This system of equations must be closed by an additional equation that provides a relation between the thermodynamic quantities of the gas. This relationship is known as the equation of state for the material, and its structure and properties depend on the composition of the gas.

It is common to call an equation of state (henceforth EOS) routine more than 10⁹ times during a twodimensional simulation and more than 10¹¹ times during the course of a three-dimensional simulation of stellar phenomena. Thus, it is very desirable to have an EOS that is as efficient as possible, yet accurately represents the relevant physics. While Flash-X is capable of using any general equation of state, we discuss here the three equation of state routines that are supplied: an ideal-gas or gamma-law EOS, an EOS for a fluid composed of multiple gamma-law gases, and a tabular Helmholtz free energy EOS appropriate for stellar interiors. The two gamma-law EOSs consist of simple analytic expressions that make for a very fast EOS routine both in the case of a single gas or for a mixture of gases. The Helmholtz EOS includes much more physics and relies on a table look-up scheme for performance.

13.2 Gamma Law and Multigamma

Flash-X uses the method of Colella & Glaz (1985) to handle general equations of state. General equations of state contain 4 adiabatic indices (Chandrasekhar 1939), but the method of Colella & Glaz parameterizes the EOS and requires only two of the adiabatic indices The first is necessary to calculate the adiabatic sound speed and is given by

$$\gamma_1 = \frac{\rho}{P} \frac{\partial P}{\partial \rho} \ . \tag{13.1}$$

The second relates the pressure to the energy and is given by

$$\gamma_4 = 1 + \frac{P}{\rho \epsilon} \ . \tag{13.2}$$

These two adiabatic indices are stored as the mesh-based variables GAMC_VAR and GAME_VAR. All EOS routines must return γ_1 , and γ_4 is calculated from (??).

The gamma-lawEOS models a simple ideal gas with a constant adiabatic index γ . Here we have dropped the subscript on γ , because for an ideal gas, all adiabatic indices are equal. The relationship between pressure P, density ρ , and specific internal energy ϵ is

$$P = (\gamma - 1) \rho \epsilon . \tag{13.3}$$

We also have an expression relating pressure to the temperature T

$$P = \frac{N_a k}{\bar{A}} \rho T \,, \tag{13.4}$$

where N_a is the Avogadro number, k is the Boltzmann constant, and \bar{A} is the average atomic mass, defined as

$$\frac{1}{\bar{A}} = \sum_{i} \frac{X_i}{A_i} \,, \tag{13.5}$$

where X_i is the mass fraction of the *i*th element. Equating these expressions for pressure yields an expression for the specific internal energy as a function of temperature

$$\epsilon = \frac{1}{\gamma - 1} \frac{N_a k}{\bar{A}} T \ . \tag{13.6}$$

The relativistic variant of the ideal gas equation is explained in more detail in ??.

Simulations are not restricted to a single ideal gas; the multigamma EOSsimulations with several species of ideal gases each with its own value of γ . In this case the above expressions hold, but γ represents the weighted average adiabatic index calculated from

$$\frac{1}{(\gamma - 1)} = \bar{A} \sum_{i} \frac{1}{(\gamma_i - 1)} \frac{X_i}{A_i} . \tag{13.7}$$

We note that the analytic expressions apply to both the forward (internal energy as a function of density, temperature, and composition) and backward (temperature as a function of density, internal energy and composition) relations. Because the backward relation requires no iteration in order to obtain the temperature, this EOS is quite inexpensive to evaluate. Despite its fast performance, use of the gamma-law EOS is limited, due to its restricted range of applicability for astrophysical problems.

13.3 Helmholtz

The Helmholtz EOSprovided with the Flash-X distribution contains more physics and is appropriate for addressing astrophysical phenomena in which electrons and positrons may be relativistic and/or degenerate and in which radiation may significantly contribute to the thermodynamic state. Full details of the Helmholtz equation of state are provided in Timmes & Swesty (1999). This EOS includes contributions from radiation, completely ionized nuclei, and degenerate/relativistic electrons and positrons. The pressure and internal energy are calculated as the sum over the components

$$P_{\text{tot}} = P_{\text{rad}} + P_{\text{ion}} + P_{\text{ele}} + P_{\text{pos}} + P_{\text{coul}}$$

$$\tag{13.8}$$

$$\epsilon_{\text{tot}} = \epsilon_{\text{rad}} + \epsilon_{\text{ion}} + \epsilon_{\text{ele}} + \epsilon_{\text{pos}} + \epsilon_{\text{coul}}$$
 (13.9)

Here the subscripts "rad," "ion," "ele," "pos," and "coul" represent the contributions from radiation, nuclei, electrons, positrons, and corrections for Coulomb effects, respectively. The radiation portion assumes a

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blackbody in local thermodynamic equilibrium, the ion portion (nuclei) is treated as an ideal gas with $\gamma = 5/3$, and the electrons and positrons are treated as a non-interacting Fermi gas.

The blackbody pressure and energy are calculated as

$$P_{\rm rad} = \frac{aT^4}{3} \tag{13.10}$$

$$\epsilon_{\rm rad} = \frac{3P_{\rm rad}}{\rho} \tag{13.11}$$

where a is related to the Stephan-Boltzmann constant $\sigma_B = ac/4$, and c is the speed of light. The ion portion of each routine is the ideal gas of (Equations ?? – ??) with $\gamma = 5/3$. The number densities of free electrons $N_{\rm ele}$ and positrons $N_{\rm pos}$ in the noninteracting Fermi gas formalism are given by

$$N_{\text{ele}} = \frac{8\pi\sqrt{2}}{h^3} \ m_{\text{e}}^3 \ c^3 \ \beta^{3/2} \ \left[F_{1/2}(\eta,\beta) + F_{3/2}(\eta,\beta) \right]$$
 (13.12)

$$N_{\text{pos}} = \frac{8\pi\sqrt{2}}{h^3} \ m_{\text{e}}^3 \ c^3 \ \beta^{3/2} \left[F_{1/2} \left(-\eta - 2/\beta, \beta \right) + \beta \ F_{3/2} \left(-\eta - 2/\beta, \beta \right) \right] , \tag{13.13}$$

where h is Planck's constant, $m_{\rm e}$ is the electron rest mass, $\beta=kT/(m_{\rm e}c^2)$ is the relativity parameter, $\eta=\mu/kT$ is the normalized chemical potential energy μ for electrons, and $F_k(\eta,\beta)$ is the Fermi-Dirac integral

$$F_k(\eta, \beta) = \int_0^\infty \frac{x^k (1 + 0.5 \beta x)^{1/2} dx}{\exp(x - \eta) + 1} .$$
 (13.14)

Because the electron rest mass is not included in the chemical potential, the positron chemical potential must have the form $\eta_{\text{pos}} = -\eta - 2/\beta$. For complete ionization, the number density of free electrons in the matter is

$$N_{\rm ele, matter} = \frac{\bar{Z}}{\bar{A}} N_a \ \rho = \bar{Z} \ N_{\rm ion} \ ,$$
 (13.15)

and charge neutrality requires

$$N_{\text{ele,matter}} = N_{\text{ele}} - N_{\text{pos}}$$
 (13.16)

Solving this equation with a standard one-dimensional root-finding algorithm determines η . Once η is known, the Fermi-Dirac integrals can be evaluated, giving the pressure, specific thermal energy, and entropy due to the free electrons and positrons. From these, other thermodynamic quantities such as γ_1 and γ_4 are found. Full details of this formalism may be found in Fryxell *et al.* (2000) and references therein.

The above formalism requires many complex calculations to evaluate the thermodynamic quantities, and routines for these calculations typically are designed for accuracy and thermodynamic consistency at the expense of speed. The Helmholtz EOS in Flash-X provides a table of the Helmholtz free energy (hence the name) and makes use of a thermodynamically consistent interpolation scheme obviating the need to perform the complex calculations required of the above formalism during the course of a simulation. The interpolation scheme uses a bi-quintic Hermite interpolant resulting in an accurate EOS that performs reasonably well.

The Helmholtz free energy,

$$F = \epsilon - T S \tag{13.17}$$

$$dF = -S \ dT + \frac{P}{\rho^2} \ d\rho \ , \tag{13.18}$$

is the appropriate thermodynamic potential for use when the temperature and density are the natural thermodynamic variables. The free energy table distributed with Flash-X was produced from the Timmes EOS (Timmes & Arnett 1999). The Timmes EOS evaluates the Fermi-Dirac integrals (??) and their partial derivatives with respect to η and β to machine precision with the efficient quadrature schemes of Aparicio (1998) and uses a Newton-Raphson iteration to obtain the chemical potential of (??). All partial derivatives of the pressure, entropy, and internal energy are formed analytically. Searches through the free energy table are avoided by computing hash indices from the values of any given $(T, \rho \bar{Z}/\bar{A})$ pair. No computationally

expensive divisions are required in interpolating from the table; all of them can be computed and stored the first time the EOS routine is called.

We note that the Helmholtz free energy table is constructed for only the electron-positron plasma, and it is a 2-dimensional function of density and temperature, i.e. $F(\rho, T)$. It is made with $\bar{A} = \bar{Z} = 1$ (pure hydrogen), with an electron fraction $Y_e = 1$. One reason for not including contributions from photons and ions in the table is that these components of the Helmholtz EOS are very simple (Equations ?? – ??), and one doesn't need fancy table look-up schemes to evaluate simple analytical functions. A more important reason for only constructing an electron-positron EOS table with $Y_e = 1$ is that the 2-dimensional table is valid for any composition. Separate planes for each Y_e are not necessary (or desirable), since simple multiplication by Y_e in the appropriate places gives the desired composition scaling. If photons and ions were included in the table, then this valuable composition independence would be lost, and a 3-dimensional table would be necessary.

The Helmholtz EOS has been subjected to considerable analysis and testing (Timmes & Swesty 2000), and particular care was taken to reduce the numerical error introduced by the thermodynamical models below the formal accuracy of the hydrodynamics algorithm (Fryxell, et al. 2000; Timmes & Swesty 2000). The physical limits of the Helmholtz EOS are $10^{-10} < \rho < 10^{11}$ (g cm⁻³) and $10^4 < T < 10^{11}$ (K). As with the gamma-law EOS, the Helmholtz EOS provides both forward and backward relations. In the case of the forward relation (ρ , T, given along with the composition) the table lookup scheme and analytic formulae directly provide relevant thermodynamic quantities. In the case of the backward relation (ρ , ϵ , and composition given), the routine performs a Newton-Rhaphson iteration to determine temperature. It is possible for the input variables to be changed in the iterative modes since the solution is not exact. The returned quantities are thermodynamically consistent.

13.4 Usage

13.4.1 Initialization

The initialization function of the Eos unit [[api reference]] is fairly simple for the two ideal gas gamma law implementations included. It gathers the runtime parameters and the physical constants needed by the equation of state and stores them in the data module. The Helmholtz EOS [[api reference]] routine is a little more complex. The Helmholtz EOS requires an input file helm_table.dat that contains the lookup table for the electron contributions. This table is currently stored in ASCII for portability purposes. When the table is first read in, a binary version called helm_table.bdat is created. This binary format can be used for faster subsequent restarts on the same machine but may not be portable across platforms. The Eos_init routine reads in the table data on processor 0 and broadcasts it to all other processors.

13.4.2 Runtime Parameters

Runtime parameters for the Gamma unit require the user to set the thermodynamic properties for the single gas. [[rpi reference]], [[rpi reference]], [[rpi reference]] set the ratio of specific heats and the nucleon and proton numbers for the gas. In contrast, the Multigamma implementation does not set runtime parameters to define properties of the multiple species. Instead, the simulation Config file indicates the requested species, for example helium and oxygen can be defined as

```
SPECIES HE4
SPECIES 016
The properties of the gases are initialized in the file [[api reference]].F90, for example
```

```
subroutine Simulation_initSpecies()
  use Multispecies_interface, ONLY : Multispecies_setProperty
  implicit none
#include "Simulation.h"
#include "Multispecies.h"
  call Multispecies_setProperty(HE4_SPEC, A, 4.)
```

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```
call Multispecies_setProperty(HE4_SPEC, Z, 2.)
call Multispecies_setProperty(HE4_SPEC, GAMMA, 1.666666666667e0)
call Multispecies_setProperty(O16_SPEC, A, 16.0)
call Multispecies_setProperty(O16_SPEC, Z, 8.0)
call Multispecies_setProperty(O16_SPEC, GAMMA, 1.4)
end subroutine Simulation_initSpecies
```

For the Helmholtz equation of state, the table-lookup algorithm requires a given temperature and density. When temperature or internal energy are supplied as the input parameter, an iterative solution is found. Therefore, no matter what mode is selected for Helmholtz input, the best initial value of temperature should be provided to speed convergence of the iterations. The iterative solver is controlled by two runtime parameters [[rpi reference]] and [[rpi reference]] which define the maximum number of iterations and convergence tolerance. An additional runtime parameter for Helmholtz, [[rpi reference]], indicates whether or not to apply Coulomb corrections. In some regions of the ρ -T plane, the approximations made in the Coulomb corrections may be invalid and result in negative pressures. When the parameter eos_coulombMult is set to zero, the Coulomb corrections are not applied.

13.4.3 Direct and Wrapped Calls

The primary function in the Eos unitoperates on a vector, taking density, composition, and either temperature, internal energy, or pressure as input, and returning γ_1 , and either the pressure, temperature or internal energy (whichever was not used as input). This equation of state interface is useful for initializing a problem. The user is given direct control over the input and output, since everything is passed through the argument list. Also, the vector data format is more efficient than calling the equation of state routine directly on a point by point basis, since it permits pipelining and provides better cache performance. Certain optional quantities such electron pressure, degeneracy parameter, and thermodynamic derivatives can be calculated by the [[api reference]] function if needed. These quantities are selected for computation based upon a logical mask array provided as an input argument. A .true. value in the mask array results in the corresponding quantity being computed and reported back to the calling function. Examples of calling the basic implementation Eos are provided in the API description, see [[api reference]].

The hydrodynamic and burning computations repeatedly call the Eos function to update pressure and temperature during the course of their calculation. Typically, values in all the cells of the block need of be updated in these calls. Since the primary Eos interface requires the data to be organized as a vector, using it directly could make the code in the calling unit very cumbersome and error prone. The wrapper interface, [[api reference]] provides a means by which the details of translating the data from block to vector and back are hidden from the calling unit. The wrapper interface permits the caller to define a section of block by giving the limiting indices along each dimension. The Eos_wrapped routine translates the block section thus described into the vector format of the [[api reference]] interface, and upon return translates the vector format back to the block section. This wrapper routine cannot calculate the optional derivative quantities. If they are needed, call the Eos routine directly with the optional mask set to true and space allocated for the returned quantities.

13.5 Unit Test

The unit test of the Eos function can exercise all three implementations. Because the Gamma law allows only one species, the setup required for the three implementations is specific. To invoke any three-dimensional Eos unit test, the command is:

```
./setup unitTest/Eos/implementation -auto -3d
```

where *implementation* is one of Gamma, Multigamma, Helmholtz. The Eos unit test works on the assumption that if the four physical variables in question (density, pressure, energy and temperature) are in thermal equilibrium with one another, then applying the equation of state to any two of them should leave the other two completely unchanged. Hence, if we initialize density and temperature with some arbitrary values, and apply the equation of state to them in MODE_DENS_TEMP, then we should get pressure and energy values that

are thermodynamically consistent with density and temperature. Now after saving the original temperature value, we apply the equation of state to density and newly calculated pressure. The new value of the temperature should be identical to the saved original value. This verifies that the Eos unit is computing correctly in MODE_DENS_PRES mode. By repeating this process for the remaining two modes, we can say with great confidence that the Eos unit is functioning normally.

In our implementation of the Eos unit test, the initial conditions applied to the domain create a gradient for density along the x axis and gradients for temperature and pressure along the y axis. If the test is being run for the Multigamma or Helmholtz implementations, then the species are initialized to have gradients along the z axis.

Chapter 14

Local Source Terms

The physics/sourceTerms organizational directory contains several units that implement forcing terms. The Burn, Stir, Ionize, and Diffuse units contain implementations in FLASH-X. Two other units, Cool and Heat, contain only stub level routines in their API.

14.1 Burn Unit

The nuclear burning implementation of the Burn unit uses a sparse-matrix semi-implicit ordinary differential equation (ODE) solver to calculate the nuclear burning rate and to update the fluid variables accordingly (Timmes 1999). The primary interface routines for this unit are [[api reference]], which sets up the nuclear isotope tables needed by the unit, and [[api reference]], which calls the ODE solver and updates the hydrodynamical variables in a single row of a single block. The routine [[api reference]] may limit the computational timestep because of burning considerations. There is also a helper routine Simulation/-Simulation/omposition/Simulation_initSpecies (see [[api reference]]) which provides the properties of ions included in the burning network.

14.1.1 Algorithms

Modeling thermonuclear flashes typically requires the energy generation rate due to nuclear burning over a large range of temperatures, densities and compositions. The average energy generated or lost over a period of time is found by integrating a system of ordinary differential equations (the nuclear reaction network) for the abundances of important nuclei and the total energy release. In some contexts, such as supernova models, the abundances themselves are also of interest. In either case, the coefficients that appear in the equations are typically extremely sensitive to temperature. The resulting stiffness of the system of equations requires the use of an implicit time integration scheme.

A user can choose between two implicit integration methods and two linear algebra packages in Flash-X. The runtime parameter [[rpi reference]] controls which integration method is used in the simulation. The choice odeStepper = 1 is the default and invokes a Bader-Deuflhard scheme. The choice odeStepper = 2 invokes a Kaps-Rentrop or Rosenbrock scheme. The runtime parameter [[rpi reference]] controls which linear algebra package is used in the simulation. The choice algebra = 1 is the default and invokes the sparse matrix MA28 package. The choice algebra = 2 invokes the GIFT linear algebra routines. While any combination of the integration methods and linear algebra packages will produce correct answers, some combinations may execute more efficiently than others for certain types of simulations. No general rules have been found for best combination for a given simulation. The most efficient combination depends on the timestep being taken, the spatial resolution of the model, the values of the local thermodynamic variables, and the composition. Users are advised to experiment with the various combinations to determine the best one for their simulation. However, an extensive analysis was performed in the Timmes paper cited below.

Timmes (1999) reviewed several methods for solving stiff nuclear reaction networks, providing the basis for the reaction network solvers included with Flash-X. The scaling properties and behavior of three semi-implicit time integration algorithms (a traditional first-order accurate Euler method, a fourth-order accurate

Kaps-Rentrop / Rosenbrock method, and a variable order Bader-Deuflhard method) and eight linear algebra packages (LAPACK, LUDCMP, LEQS, GIFT, MA28, UMFPACK, and Y12M) were investigated by running each of these 24 combinations on seven different nuclear reaction networks (hard-wired 13- and 19-isotope networks and soft-wired networks of 47, 76, 127, 200, and 489 isotopes). Timmes' analysis suggested that the best balance of accuracy, overall efficiency, memory footprint, and ease-of-use was provided by the two integration methods (Bader-Deuflhard and Kaps-Rentrop) and the two linear algebra packages (MA28 and GIFT) that are provided with the Flash-X code.

14.1.2 Reaction networks

We begin by describing the equations solved by the nuclear burning unit. We consider material that may be described by a density ρ and a single temperature T and contains a number of isotopes i, each of which has Z_i protons and A_i nucleons (protons + neutrons). Let n_i and ρ_i denote the number and mass density, respectively, of the ith isotope, and let X_i denote its mass fraction, so that

$$X_i = \rho_i/\rho = n_i A_i/(\rho N_A) , \qquad (14.1)$$

where N_A is Avogadro's number. Let the molar abundance of the *i*th isotope be

$$Y_i = X_i / A_i = n_i / (\rho N_A)$$
 (14.2)

Mass conservation is then expressed by

$$\sum_{i=1}^{N} X_i = 1 \ . \tag{14.3}$$

At the end of each timestep, Flash-X checks that the stored abundances satisfy (??) to machine precision in order to avoid the unphysical buildup (or decay) of the abundances or energy generation rate. Roundoff errors in this equation can lead to significant problems in some contexts (e.g., classical nova envelopes), where trace abundances are important.

The general continuity equation for the ith isotope is given in Lagrangian formulation by

$$\frac{dY_i}{dt} + \nabla \cdot (Y_i \mathbf{V}_i) = \dot{R}_i \ . \tag{14.4}$$

In this equation R_i is the total reaction rate due to all binary reactions of the form i(j,k)l,

$$\dot{R}_i = \sum_{j,k} Y_l Y_k \lambda_{kj}(l) - Y_i Y_j \lambda_{jk}(i) , \qquad (14.5)$$

where λ_{kj} and λ_{jk} are the reverse (creation) and forward (destruction) nuclear reaction rates, respectively. Contributions from three-body reactions, such as the triple- α reaction, are easy to append to (??). The mass diffusion velocities \mathbf{V}_i in (??) are obtained from the solution of a multicomponent diffusion equation (Chapman & Cowling 1970; Burgers 1969; Williams 1988) and reflect the fact that mass diffusion processes arise from pressure, temperature, and/or abundance gradients as well as from external gravitational or electrical forces.

The case $V_i \equiv 0$ is important for two reasons. First, mass diffusion is often unimportant when compared to other transport processes, such as thermal or viscous diffusion (i.e., large Lewis numbers and/or small Prandtl numbers). Such a situation obtains, for example, in the study of laminar flame fronts propagating through the quiescent interior of a white dwarf. Second, this case permits the decoupling of the reaction network solver from the hydrodynamical solver through the use of operator splitting, greatly simplifying the algorithm. This is the method used by the default Flash-X distribution. Setting $V_i \equiv 0$ transforms (??) into

$$\frac{dY_i}{dt} = \dot{R}_i , \qquad (14.6)$$

which may be written in the more compact, standard form

$$\dot{\mathbf{y}} = \mathbf{f} \ (\mathbf{y}) \ . \tag{14.7}$$

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Stated another way, in the absence of mass diffusion or advection, any changes to the fluid composition are due to local processes.

Because of the highly nonlinear temperature dependence of the nuclear reaction rates and because the abundances themselves often range over several orders of magnitude in value, the values of the coefficients which appear in (??) and (??) can vary quite significantly. As a result, the nuclear reaction network equations are "stiff." A system of equations is stiff when the ratio of the maximum to the minimum eigenvalue of the Jacobian matrix $\tilde{\bf J}\equiv\partial{\bf f}/\partial{\bf y}$ is large and imaginary. This means that at least one of the isotopic abundances changes on a much shorter timescale than another. Implicit or semi-implicit time integration methods are generally necessary to avoid following this short-timescale behavior, requiring the calculation of the Jacobian matrix.

It is instructive at this point to look at an example of how (??) and the associated Jacobian matrix are formed. Consider the $^{12}\mathrm{C}(\alpha,\gamma)^{16}\mathrm{O}$ reaction, which competes with the triple- α reaction during helium burning in stars. The rate R at which this reaction proceeds is critical for evolutionary models of massive stars, since it determines how much of the core is carbon and how much of the core is oxygen after the initial helium fuel is exhausted. This reaction sequence contributes to the right-hand side of (??) through the terms

$$\dot{Y}(^{4}He) = -Y(^{4}He) Y(^{12}C) R + \dots
\dot{Y}(^{12}C) = -Y(^{4}He) Y(^{12}C) R + \dots
\dot{Y}(^{16}O) = +Y(^{4}He) Y(^{12}C) R + \dots,$$
(14.8)

where the ellipses indicate additional terms coming from other reaction sequences. The minus signs indicate that helium and carbon are being destroyed, while the plus sign indicates that oxygen is being created. Each of these three expressions contributes two terms to the Jacobian matrix $\tilde{\bf J} = \partial {\bf f}/\partial {\bf y}$

$$J(^{4}He,^{4}He) = -Y(^{12}C) R + \dots$$

$$J(^{12}C,^{4}He) = -Y(^{12}C) R + \dots$$

$$J(^{12}C,^{12}C) = -Y(^{12}C) R + \dots$$

$$J(^{12}C,^{12}C) = -Y(^{12}C) R + \dots$$

$$J(^{16}C,^{12}C) = -Y(^{12}C) R + \dots$$

$$J(^{16}C,^{12}C) = +Y(^{12}C) R + \dots$$

Entries in the Jacobian matrix represent the flow, in number of nuclei per second, into (positive) or out of (negative) an isotope. All of the temperature and density dependence is included in the reaction rate R. The Jacobian matrices that arise from nuclear reaction networks are neither positive-definite nor symmetric, since the forward and reverse reaction rates are generally not equal. In addition, the magnitudes of the matrix entries change as the abundances, temperature, or density change with time.

This release of FLASH-X contains three reaction networks. A seven-isotope alpha-chain (Iso7) is useful for problems that do not have enough memory to carry a larger set of isotopes. The 13-isotope α -chain plus heavy-ion reaction network (Aprox13) is suitable for most multi-dimensional simulations of stellar phenomena, where having a reasonably accurate energy generation rate is of primary concern. The 19-isotope reaction network (Aprox19) has the same α -chain and heavy-ion reactions as the 13-isotope network, but it includes additional isotopes to accommodate some types of hydrogen burning (PP chains and steady-state CNO cycles), along with some aspects of photo-disintegration into ⁵⁴Fe. This 19 isotope reaction network is described in Weaver, Zimmerman, & Woosley (1978).

The networks supplied with Flash-X are examples of a "hard-wired" reaction network, where each of the reaction sequences are carefully entered by hand. This approach is suitable for small networks, when minimizing the CPU time required to run the reaction network is a primary concern, although it suffers the disadvantage of inflexibility.

The MA28 sparse matrix package used by Flash-X is described by Duff, Erisman, & Reid (1986) and is used as an external library. This package, which has been described as the "Coke classic" of sparse linear algebra packages, uses a direct – as opposed to an iterative – method for solving linear systems. Direct methods typically divide the solution of $\tilde{\mathbf{A}} \cdot \mathbf{x} = \mathbf{b}$ into a symbolic LU decomposition, a numerical LU decomposition, and a backsubstitution phase. In the symbolic LU decomposition phase, the pivot order of a matrix is determined, and a sequence of decomposition operations that minimizes the amount of fill-in is recorded. Fill-in refers to zero matrix elements which become nonzero (e.g., a sparse matrix times a sparse matrix is generally a denser matrix). The matrix is not decomposed; only the steps to do so are stored. Since

the nonzero pattern of a chosen nuclear reaction network does not change, the symbolic LU decomposition is a one-time initialization cost for reaction networks. In the numerical LU decomposition phase, a matrix with the same pivot order and nonzero pattern as a previously factorized matrix is numerically decomposed into its lower-upper form. This phase must be done only once for each set of linear equations. In the backsubstitution phase, a set of linear equations is solved with the factors calculated from a previous numerical decomposition. The backsubstitution phase may be performed with as many right-hand sides as needed, and not all of the right-hand sides need to be known in advance.

MA28 uses a combination of nested dissection and frontal envelope decomposition to minimize fill-in during the factorization stage. An approximate degree update algorithm that is much faster (asymptotically and in practice) than computing the exact degrees is employed. One continuous real parameter sets the amount of searching done to locate the pivot element. When this parameter is set to zero, no searching is done and the diagonal element is the pivot, while when set to unity, partial pivoting is done. Since the matrices generated by reaction networks are usually diagonally dominant, the routine is set in Flash-X to use the diagonal as the pivot element. Several test cases showed that using partial pivoting did not make a significant accuracy difference but was less efficient, since a search for an appropriate pivot element had to be performed. MA28 accepts the nonzero entries of the matrix in the $(i, j, a_{i,j})$ coordinate system and typically uses 70–90% less storage than storing the full dense matrix.

14.1.2.1 Two time integration methods

One of the time integration methods used by Flash-X for evolving the reaction networks is a 4th-order accurate Kaps-Rentrop, or Rosenbrock method. In essence, this method is an implicit Runge-Kutta algorithm. The reaction network is advanced over a timestep h according to

$$\mathbf{y}^{n+1} = \mathbf{y}^n + \sum_{i=1}^4 b_i \Delta_i , \qquad (14.10)$$

where the four vectors Δ^i are found from successively solving the four matrix equations

$$(\tilde{\mathbf{1}}/\gamma h - \tilde{\mathbf{J}}) \cdot \Delta_1 = \mathbf{f}(\mathbf{y}^n)$$
 (14.11)

$$(\tilde{\mathbf{1}}/\gamma h - \tilde{\mathbf{J}}) \cdot \Delta_2 = \mathbf{f}(\mathbf{y}^n + a_{21}\Delta_1) + c_{21}\Delta_1/h$$
(14.12)

$$(\tilde{\mathbf{1}}/\gamma h - \tilde{\mathbf{J}}) \cdot \Delta_3 = \mathbf{f}(\mathbf{y}^n + a_{31}\Delta_1 + a_{32}\Delta_2) + (c_{31}\Delta_1 + c_{32}\Delta_2)/h$$
 (14.13)

$$(\tilde{\mathbf{1}}^{\gamma}h - \tilde{\mathbf{J}}) \cdot \Delta_4 = \mathbf{f}(\mathbf{y}^n + a_{31}\Delta_1 + a_{32}\Delta_2) + (c_{41}\Delta_1 + c_{42}\Delta_2 + c_{43}\Delta_3)/h$$
 (14.14)

 b_i , γ , a_{ij} , and c_{ij} are fixed constants of the method. An estimate of the accuracy of the integration step is made by comparing a third-order solution with a fourth-order solution, which is a significant improvement over the basic Euler method. The minimum cost of this method — which applies for a single timestep that meets or exceeds a specified integration accuracy — is one Jacobian evaluation, three evaluations of the right-hand side, one matrix decomposition, and four backsubstitutions. Note that the four matrix equations represent a staged set of linear equations (Δ_4 depends on Δ_3 ... depends on Δ_1). Not all of the right-hand sides are known in advance. This general feature of higher-order integration methods impacts the optimal choice of a linear algebra package. The fourth-order Kaps-Rentrop routine in Flash-X makes use of the routine GRK4T given by Kaps & Rentrop (1979).

Another time integration method used by Flash-X for evolving the reaction networks is the variable order Bader-Deuflhard method (e.g., Bader & Deuflhard 1983). The reaction network is advanced over a large timestep H from \mathbf{y}^n to \mathbf{y}^{n+1} by the following sequence of matrix equations. First,

$$h = H/m$$

$$(\tilde{\mathbf{1}} - \tilde{\mathbf{J}}) \cdot \Delta_0 = h\mathbf{f}(\mathbf{y}^n)$$

$$\mathbf{y}_1 = \mathbf{y}^n + \Delta_0.$$
(14.15)

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Then from k = 1, 2, ..., m - 1

$$(\tilde{\mathbf{1}} - \tilde{\mathbf{J}}) \cdot \mathbf{x} = h\mathbf{f}(\mathbf{y}_k) - \Delta_{k-1}$$

$$\Delta_k = \Delta_{k-1} + 2\mathbf{x}$$

$$\mathbf{y}_{k+1} = \mathbf{y}_k + \Delta_k ,$$
(14.16)

and closure is obtained by the last stage

$$(\tilde{\mathbf{1}} - \tilde{\mathbf{J}}) \cdot \Delta_m = h[\mathbf{f}(\mathbf{y}_m) - \Delta_{m-1}]$$

$$\mathbf{y}^{n+1} = \mathbf{y}_m + \Delta_m.$$
 (14.17)

This staged sequence of matrix equations is executed at least twice with m=2 and m=6, yielding a fifth-order method. The sequence may be executed a maximum of seven times, which yields a fifteenth-order method. The exact number of times the staged sequence is executed depends on the accuracy requirements (set to one part in 10⁶ in Flash-X) and the smoothness of the solution. Estimates of the accuracy of an integration step are made by comparing the solutions derived from different orders. The minimum cost of this method — which applies for a single timestep that met or exceeded the specified integration accuracy — is one Jacobian evaluation, eight evaluations of the right-hand side, two matrix decompositions, and ten backsubstitutions. This minimum cost can be increased at a rate of one decomposition (the expensive part) and m backsubstitutions (the inexpensive part) for every increase in the order 2k+1. The cost of increasing the order is compensated for, hopefully, by being able to take correspondingly larger (but accurate) timestep. The controls for order versus step size are a built-in part of the Bader-Deuflhard method. The cost per step of this integration method is at least twice as large as the cost per step of either a traditional first-order accurate Euler method or the fourth-order accurate Kaps-Rentrop discussed above. However, if the Bader-Deuflhard method can take accurate timesteps that are at least twice as large, then this method will be more efficient globally. Timmes (1999) shows that this is typically (but not always!) the case. Note that in Equations ?? - ??, not all of the right-hand sides are known in advance, since the sequence of linear equations is staged. This staging feature of the integration method may make some matrix packages, such as MA28, a more efficient choice.

The Flash-X runtime parameter [[rpi reference]] controls which integration method is used in the simulation. The choice odeStepper = 1 is the default and invokes the variable order Bader-Deuflhard scheme. The choice odeStepper = 2 invokes the fourth order Kaps-Rentrop / Rosenbrock scheme.

14.1.3 Detecting shocks

For most astrophysical detonations, the shock structure is so thin that there is insufficient time for burning to take place within the shock. However, since numerical shock structures tend to be much wider than their physical counterparts, it is possible for a significant amount of burning to occur within the shock. Allowing this to happen can lead to unphysical results. The burner unit includes a multidimensional shock detection algorithm that can be used to prevent burning in shocks. If the [[rpi reference]] parameter is set to .false., this algorithm is used to detect shocks in the Burn unit and to switch off the burning in shocked cells.

Currently, the shock detection algorithm supports Cartesian and 2-dimensional cylindrical coordinates. The basic algorithm is to compare the jump in pressure in the direction of compression (determined by looking at the velocity field) with a shock parameter (typically 1/3). If the total velocity divergence is negative and the relative pressure jump across the compression front is larger than the shock parameter, then a cell is considered to be within a shock.

This computation is done on a block by block basis. It is important that the velocity and pressure variables have up-to-date guard cells, so a guard cell call is done for the burners only if we are detecting shocks (*i.e.* useShockBurning = .false.).

14.1.4 Energy generation rates and reaction rates

The instantaneous energy generation rate is given by the sum

$$\dot{\epsilon}_{\text{nuc}} = N_A \sum_{i} \frac{dY_i}{dt} \,. \tag{14.18}$$

Note that a nuclear reaction network does not need to be evolved in order to obtain the instantaneous energy generation rate, since only the right hand sides of the ordinary differential equations need to be evaluated. It is more appropriate in the Flash-X program to use the average nuclear energy generated over a timestep

$$\dot{\epsilon}_{\text{nuc}} = N_A \sum_{i} \frac{\Delta Y_i}{\Delta t} \ . \tag{14.19}$$

In this case, the nuclear reaction network does need to be evolved. The energy generation rate, after subtraction of any neutrino losses, is returned to the Flash-X program for use with the operator splitting technique.

The tabulation of Caughlan & Fowler (1988) is used in Flash-X for most of the key nuclear reaction rates. Modern values for some of the reaction rates were taken from the reaction rate library of Hoffman (2001, priv. comm.). A user can choose between two reaction rate evaluations in Flash-X. The runtime parameter [[rpi reference]] controls which reaction rate evaluation method is used in the simulation. The choice useBurnTable = 0 is the default and evaluates the reaction rates from analytical expressions. The choice useBurnTable = 1 evaluates the reactions rates from table interpolation. The reaction rate tables are formed on-the-fly from the analytical expressions. Tests on one-dimensional detonations and hydrostatic burnings suggest that there are no major differences in the abundance levels if tables are used instead of the analytic expressions; we find less than 1% differences at the end of long timescale runs. Table interpolation is about 10 times faster than evaluating the analytic expressions, but the speedup to Flash-X is more modest, a few percent at best, since reaction rate evaluation never dominates in a real production run.

Finally, nuclear reaction rate screening effects as formulated by Wallace et al. (1982) and decreases in the energy generation rate $\dot{\epsilon}_{\text{nuc}}$ due to neutrino losses as given by Itoh et al. (1996) are included in Flash-X.

14.1.5 Temperature-based timestep limiting

When using explicit hydrodynamics methods, a timestep limiter must be used to ensure the stability of the numerical solution. The standard CFL limiter is always used when an explicit hydrodynamics unit is included in Flash-X. This constraint does not allow any information to travel more than one computational cell per timestep. When coupling burning with the hydrodynamics, the CFL timestep may be so large compared to the burning timescales that the nuclear energy release in a cell may exceed the existing internal energy in that cell. When this happens, the two operations (hydrodynamics and nuclear burning) become decoupled.

To limit the timestep when burning is performed, an additional constraint is imposed. The limiter tries to force the energy generation from burning to be smaller than the internal energy in a cell. The runtime parameter [[rpi reference]] controls this ratio. The timestep limiter is calculated as

$$\Delta t_{burn} = \texttt{enucDtFactor} \cdot \frac{E_{int}}{E_{nuc}} \tag{14.20}$$

where E_{nuc} is the nuclear energy, expressed as energy per volume per time, and E_{int} is the internal energy per volume. For good coupling between the hydrodynamics and burning, enucDtFactor should be < 1. The default value is kept artificially high so that in most simulations the time limiting due to burning is turned off. Care must be exercised in the use of this routine.

Chapter 15

Gravity Unit

15.1 Introduction

The Gravity unit supplied with FLASH-X computes gravitational source terms for the code. These source terms can take the form of the gravitational potential $\phi(\mathbf{x})$ or the gravitational acceleration $\mathbf{g}(\mathbf{x})$,

$$\mathbf{g}(\mathbf{x}) = -\nabla \phi(\mathbf{x}) \ . \tag{15.1}$$

The gravitational field can be externally imposed or self-consistently computed from the gas density via the Poisson equation,

$$\nabla^2 \phi(\mathbf{x}) = 4\pi G \rho(\mathbf{x}) , \qquad (15.2)$$

where G is Newton's gravitational constant. In the latter case, either periodic or isolated boundary conditions can be applied.

15.2 Externally Applied Fields

The Flash-X distribution includes three externally applied gravitational fields, along with a placeholder module for you to create your own. Each provides the acceleration vector $\mathbf{g}(\mathbf{x})$ directly, without using the gravitational potential $\phi(\mathbf{x})$ (with the exception of UserDefined, see below).

When building an application that uses an external, time-independent Gravity implementation, no additional storage in unk for holding gravitational potential or accelerations is needed or defined.

15.2.1 Constant Gravitational Field

This implementation creates a spatially and temporally constant field parallel to one of the coordinate axes. The magnitude and direction of the field can be set at runtime. This unit is called Gravity/GravityMain/-Constant.

15.2.2 Plane-parallel Gravitational field

This PlanePar version implements a time-constant gravitational field that is parallel to one of the coordinate axes and falls off with the square of the distance from a fixed location. The field is assumed to be generated by a point mass or by a spherically symmetric mass distribution. A finite softening length may optionally be applied.

This type of gravitational field is useful when the computational domain is large enough in the direction radial to the field source that the field is not approximately constant, but the domain's dimension perpendicular to the radial direction is small compared to the distance to the source. In this case the angular variation of the field direction may be ignored. The PlanePar field is cheaper to compute than the PointMass field described below, since no fractional powers of the distance are required. The acceleration vector is parallel to one of the coordinate axes, and its magnitude drops off with distance along that axis as the inverse distance squared. Its magnitude and direction are independent of the other two coordinates.

15.2.3 Gravitational Field of a Point Mass

This PointMass implementation describes the gravitational field due to a point mass at a fixed location. A finite softening length may optionally be applied. The acceleration falls off with the square of the distance from a given point. The acceleration vector is everywhere directed toward this point.

15.2.4 User-Defined Gravitational Field

The UserDefined implementation is a placeholder module for the user to create their own external gravitational field. All of the subroutines in this module are stubs, and the user may copy these stubs to their setup directory to write their own implementation, either by specifying the gravitational acceleration directly or by specifying the gravitational potential and taking its gradient. If your user-defined gravitational field is time-varying, you may also want to set PPDEFINE Flash-X_GRAVITY_TIMEDEP in your setup's Config file.

15.3 Self-gravity

The self-consistent gravity algorithm supplied with Flash-X computes the Newtonian gravitational field produced by the matter. The produced potential function satisfies Poisson's equation (??). This unit's implementation can also return the acceleration field $\mathbf{g}(\mathbf{x})$ computed by finite-differencing the potential using the expressions

$$g_{x;ijk} = \frac{1}{2\Delta x} (\phi_{i-1,j,k} - \phi_{i+1,j,k}) + \mathcal{O}(\Delta x^{2})$$

$$g_{y;ijk} = \frac{1}{2\Delta y} (\phi_{i,j-1,k} - \phi_{i,j+1,k}) + \mathcal{O}(\Delta y^{2})$$

$$g_{z;ijk} = \frac{1}{2\Delta z} (\phi_{i,j,k-1} - \phi_{i,j,k+1}) + \mathcal{O}(\Delta z^{2}) .$$
(15.3)

In order to preserve the second-order accuracy of these expressions at jumps in grid refinement, it is important to use quadratic interpolants when filling guard cells at such locations. Otherwise, the truncation error of the interpolants will produce unphysical forces at these block boundaries.

Two algorithms are available for solving the Poisson equations: Gravity/GravityMain/Multipole and Gravity/GravityMain/Multigrid. The initialization routines for these algorithms are contained in the Gravity unit, but the actual implementations are contained below the Grid unit due to code architecture constraints.

The multipole-based solver described in ?? for self gravity is appropriate for spherical or nearly-spherical mass distributions with isolated boundary conditions. For non-spherical mass distributions higher order moments of the solver must be used. Note that storage and CPU costs scale roughly as the square of number of moments used, so it is best to use this solver only for nearly spherical matter distributions.

The multigrid solver described in ?? is appropriate for general mass distributions and can solve problems with more general boundary conditions.

The tree solver described in ?? is appropriate for general mass distributions and can solve problems with both isolated and periodic boundary conditions set independently in individual directions.

15.3.1 Coupling Gravity with Hydrodynamics

The gravitational field couples to the Euler equations only through the momentum and energy equations. If we define the total energy density as

$$\rho E \equiv \frac{1}{2}\rho v^2 + \rho \epsilon , \qquad (15.4)$$

where ϵ is the specific internal energy, then the gravitational source terms for the momentum and energy equations are $\rho \mathbf{g}$ and $\rho \mathbf{v} \cdot \mathbf{g}$, respectively. Because of the variety of ways in which different hydrodynamics schemes treat these source terms, the gravity module only supplies the potential ϕ and acceleration \mathbf{g} , leaving the implementation of the fluid coupling to the hydrodynamics module. Finite-difference and finite-volume hydrodynamic schemes apply the source terms in their advection steps, sometimes at multiple intermediate timesteps and sometimes using staggered meshes for vector quantities like \mathbf{v} and \mathbf{g} .

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For example, the PPM algorithm supplied with Flash-X uses the following update steps to obtain the momentum and energy in cell i at timestep n+1

$$(\rho v)_i^{n+1} = (\rho v)_i^n + \frac{\Delta t}{2} g_i^{n+1} \left(\rho_i^n + \rho_i^{n+1} \right) (\rho E)_i^{n+1} = (\rho E)_i^n + \frac{\Delta t}{4} g_i^{n+1} \left(\rho_i^n + \rho_i^{n+1} \right) \left(v_i^n + v_i^{n+1} \right) .$$
 (15.5)

Here g_i^{n+1} is obtained by extrapolation from ϕ_i^{n-1} and ϕ_i^n . The Poisson gravity implementation supplies a mesh variable to contain the potential from the previous timestep; future releases of Flash-X may permit the storage of several time levels of this quantity for hydrodynamics algorithms that require more steps. Currently, \mathbf{g} is computed at cell centers.

Note that finite-volume schemes do not retain explicit conservation of momentum and energy when gravity source terms are added. Godunov schemes such as PPM, require an additional step in order to preserve second-order time accuracy. The gravitational acceleration component g_i is fitted by interpolants along with the other state variables, and these interpolants are used to construct characteristic-averaged values of \mathbf{g} in each cell. The velocity states $v_{L,i+1/2}$ and $v_{R,i+1/2}$, which are used as inputs to the Riemann problem solver, are then corrected to account for the acceleration using the following expressions

$$v_{L,i+1/2} \rightarrow v_{L,i+1/2} + \frac{\Delta t}{4} \left(g_{L,i+1/2}^+ + g_{L,i+1/2}^- \right)$$

$$v_{R,i+1/2} \rightarrow v_{R,i+1/2} + \frac{\Delta t}{4} \left(g_{R,i+1/2}^+ + g_{R,i+1/2}^- \right) . \tag{15.6}$$

Here $g_{X,i+1/2}^{\pm}$ is the acceleration averaged using the interpolant on the X side of the interface (X = L, R) for $v \pm c$ characteristics, which bring material to the interface between cells i and i+1 during the timestep.

15.3.2 Tree Gravity

The Tree implementation of the gravity unit in physics/Gravity/GravityMain/Poisson/BHTree is meant to be used together with the tree solver implementation Grid/GridSolvers/BHTree/Wunsch. It either calculates the gravitational potential field which is subsequently differentiated in subroutine [[api reference]] to obtain the gravitational acceleration, or it calculates the gravitational acceleration directly. The latter approach is more accurate, because the error due to numerical differentiation is avoided, however, it consumes more memory for storing three components of the gravitational acceleration. The direct acceleration calculation can be switched on by specifying bhtreeAcc=1 as a command line argument of the setup script.

The gravity unit provides subroutines for building and walking the tree called by the tree solver. In this version, only monopole moments (node masses) are used for the potential/acceleration calculation. It also defines new multipole acceptance criteria (MACs) that estimate the error in gravitational acceleration of a contribution of a single node to the potential (hereafter partial error) much better than purely geometrical MAC defined in the tree solver. They are: (1) the approximate partial error (APE), and (2) the maximum partial error (MPE). The first one is based on an assumption that the partial error is proportional to the multipole moment of the node. The node is accepted for calculation of the potential if

$$D^{m+2} > \frac{GMS_{\text{node}}^m}{\Delta a_{\text{p,APE}}} \tag{15.7}$$

where D is distance between the point-of-calculation and the node, M is the node mass, S_{node} is the node size, m is a degree of the multipole approximation and $\Delta a_{\text{p,APE}}$ is the requested maximum error in acceleration (controlled by runtime parameter [[rpi reference]]). Since only monopole moments are used for the potential calculation, the most reasonable choice of m seems to be m=2. This MAC is similar to the one used in Gadget2 (see Springel, 2005, MNRAS, 364, 1105).

The second MAC (maximum partial error, MPE) calculates the error in acceleration of a single node contribution $\Delta a_{\rm p,MPE}$ according to formula 9 from Salmon&Warren (1994; see this paper for details):

$$\Delta a_{\text{p,MPE}} \le \frac{1}{D^2} \frac{1}{(1 - S_{\text{node}}/D)^2} \left(\frac{3\lceil B_2 \rceil}{D^2} - \frac{2\lfloor B_3 \rfloor}{D^3} \right)$$

$$(15.8)$$

where $B_n = \sum_i m_i |\mathbf{r}_i - \mathbf{r}_0|^n$ where m_i and \mathbf{r}_i are masses and positions of individual grid cells within the node and \mathbf{r}_0 is the node mass center position. Moment B_2 can be easily determined during the tree build, moment B_3 can be estimated as $B_3^2 \geq B_2^3/M$. The maximum allowed partial error in gravitational acceleration is controlled by runtime parameters [[rpi reference]] and [[rpi reference]] (see ??).

During the tree walk, subroutine [[api reference]] adds contributions of tree nodes to the gravitational potential or acceleration fields. In case of the potential, the contribution is

$$\Phi = -\frac{GM}{|\vec{r}|} \tag{15.9}$$

if isolated boundary conditions are used, or

$$\Phi = -GM f_{\text{EF},\Phi}(\vec{r}) \tag{15.10}$$

if periodic periodic or mixed boundary conditions are used. In case of the acceleration, the contributions are

$$\vec{a}_g = \frac{GM\vec{r}}{|\vec{r}|^3} \tag{15.11}$$

for isolated boundary conditions, or

$$\vec{a}_q = GM f_{\text{EF,a}}(\vec{r}) \tag{15.12}$$

for periodic or mixed boundary conditions. In In the above formulae, G is the constant of gravity, M is the node mass, \vec{r} is the position vector between *point-of-calculation* and the node mass center and $f_{\text{EF},\Phi}$ and $f_{\text{EF},a}$ are the Ewald fields for the potential and the acceleration (see below).

Boundary conditions can be isolated or periodic, set independently for each direction. If they are periodic at least in one direction, the Ewald method is used for the potential calculation (Ewald, P. P., 1921, Ann. Phys. 64, 253). The original Ewald method is an efficient method for computing gravitational field for problems with periodic boundary conditions in three directions. Ewald speeded up evaluation of the gravitational potential by splitting it into two parts, $Gm/r = Gm \operatorname{erf}(\alpha r)/r + Gm \operatorname{erfc}(\alpha r)/r$ (α is an arbitrary constant) and then by applying Poisson summation formula on erfc terms, gravitational field at position \bar{r} can be written in the form

$$\phi(\vec{r}) = -G\sum_{a=1}^{N} m_a \left(\sum_{i_1, i_2, i_3} A_S(\vec{r}, \vec{r}_a, \vec{l}_{i_1, i_2, i_3}) + A_L(\vec{r}, \vec{r}_a, \vec{l}_{i_1, i_2, i_3}) \right) = -G\sum_{a=1}^{N} m_a f_{\text{EF}, \Phi}(\vec{r}_a - \vec{r}) , \quad (15.13)$$

the first sum runs over whole computational domain, where at position \vec{r}_a is mass m_a . Second sum runs over all neigbouring computational domains, which are at positions \vec{l}_{i_1,i_2,i_3} and $A_S(\vec{r},\vec{r}_a,\vec{l}_{i_1,i_2,i_3})$ and $A_L(\vec{r},\vec{r}_a,\vec{l}_{i_1,i_2,i_3})$ are short and long-range contributions, respectively. It is sufficient to take into account only few terms in eq. ??. The Ewald field for the acceleration, $f_{\text{EF},a}$, is obtained using a similar decomposition. We modified Ewald method for problems with periodic boundary conditions in two directions and isolated boundary conditions in the third direction and for problems with periodic boundary conditions in one direction and isolated in two directions.

The gravity unit allows also to use a static external gravitational field read from file. In this version, the field can be either spherically symmetric or planar being only a function of the z-coordinate. The external field file is a text file containing three columns of numbers representing the coordinate, the potential and the acceleration. The coordinate is the radial distance or z-distance from the center of the external field given by runtime parameters. The external field if mapped to a grid using a linear interpolation each time the gravitational acceleration is calculated (in subroutine [[api reference]]).

15.4 Usage

To include the effects of gravity in your Flash-X executable, include the option

-with-unit=physics/Gravity

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on your command line when you configure the code with setup. The default implementation is Constant, which can be overridden by including the entire path to the specific implementation in the command line or Config file. The other available implementations are Gravity/GravityMain/Planepar, Gravity/GravityMain/Pointmass and Gravity/GravityMain/Poisson. The Gravity unit provides accessor functions to get gravitational acceleration and potential. However, none of the external field implementations of Section ?? explicitly compute the potential, hence they inherit the null implementation from the API for accessing potential. The gravitation acceleration can be obtained either on the whole domain, a single block or a single row at a time.

When building an application that solves the Possion equation for the gravitational potential, additional storage is needed in unk for holding the last, as well as (usually) the previous, gravitational potential field; and, depending on the Poisson solver used, additional variables may be needed. The variables GPOT_VAR and GPOT_VAR, and others as needed, will be automatically defined in Simulation.h in those cases. See [[api reference]] for more information.

15.4.1 Tree Gravity Unit Usage

Calculation of gravitational potential can be enabled by compiling in this unit and setting the runtime parameter [[rpi reference]] true. The constant of gravity can be set independently by runtime parameter [[rpi reference]]; if it is not positive, the constant Newton from the Flash-X PhysicalConstants database is used. If parameters [[rpi reference]] or [[rpi reference]] are set, the gravity unit MAC is used and it can be chosen by setting [[rpi reference]] to either ApproxPartialErr or MaxPartialErr. If the first one is used, the order of the multipole approximation is given by [[rpi reference]].

The maximum allowed partial error in gravitational acceleration is set with the runtime parameter [[rpi reference]]. It has either the meaning of an error in absolute acceleration or in relative acceleration normalized by the acceleration from the previous time-step. The latter is used if [[rpi reference]] is set to True, and in this case the first call of the tree solver calculates the potential using purely geometrical MAC (because the acceleration from the previous time-step does not exist).

Boundary conditions are set by the runtime parameter [[rpi reference]] and they can be isolated, periodic or mixed. In the case of mixed boundary conditions, runtime parameters [[rpi reference]], [[rpi reference]] and [[rpi reference]] specify along which coordinate boundary conditions are periodic and isolated (possible values are periodic or isolated). Arbitrary combination of these values is permitted, thus suitable for problems with planar resp. linear symmetry. It should work for computational domain with arbitrary dimensions. The highest accuracy is reached with blocks of cubic physical dimensions.

If runtime parameter [[rpi reference]] is periodic or mixed, then the Ewald field for appropriate symmetry is calculated at the beginning of the simulation. Parameter [[rpi reference]] controls the range of indices i_1, i_2, i_3 in (eq. ??). There are two implementations of the Ewald method: the new one (default) requires less memory and it should be faster and of comparable accuracy as the old one. The default implementation computes Ewald field minus the singular 1/r term and its partial derivatives on a single cubic grid, and the Ewald field is then approximated by the first order Taylor formula. Parameter [[rpi reference]] controls number of grid points in the x direction in the case of periodic or in periodic direction(s) in the case of mixed boundary conditions. Since an elongated computational domain is often desired when [[rpi reference]] is mixed, the cubic grid would lead to a huge field of data. In this case, the amount of necessary grid points is reduced by using an analytical estimate to the Ewald field sufficiently far away of the symmetry plane or axis.

The old implementation (from Flash4.2) is still present and is enabled by adding bhtreeEwaldV42=1 on the setup command line. The Ewald field is then stored in a nested set of grids, the first of them corresponds in size to full computational domain, and each following grid is half the size (in each direction) of the previous grid. Number of nested grids is controlled by runtime parameter [[rpi reference]]. If [[rpi reference]] is too low to cover origin (where is the Ewald field discontinuous), then the run is terminated. Each grid is composed of [[rpi reference]] × [[rpi reference]] × [[rpi reference]] points. When evaluation of the Ewald Field at particular point is needed at any time during a run, the field value is found by interpolation in a suitable level of the grid. Linear or semi-quadratic interpolation can be chosen by runtime parameter [[rpi reference]] (option true corresponds to linear interpolation). Semi-quadratic interpolation is recommended only in the case when there are periodic boundary conditions in two directions.

The external gravitational field can be switched on by setting [[rpi reference]] true. The parameter [[rpi reference]] gives the name of the file with the external potential and [[rpi reference]] specifies the field symmetry: spherical for the spherical symmetry and planez for the planar symmetry with field being a function of the z-coordinate. Parameters [[rpi reference]], [[rpi reference]] and [[rpi reference]] specify the position (in the simulation coordinate system) of the external field origin (the point where the radial or z-coordinate is zero).

Variable	Type	Default	Description	
[[rpi reference]]	real	-1.0	constant of gravity; if < 0 , it is obtained	
			from internal physical constants database	
[[rpi reference]]	string	"ApproxPartialErr"	MAC, other option: "MaxPartialErr"	
[[rpi reference]]	integer	2	degree of multipole in error estimate in APE MAC	
[[rpi reference]]	logical	.false.	if .true., grv_bhAccErr has meaning of	
			relative error, otherwise absolute	
[[rpi reference]]	real	0.1	maximum allowed error in gravitational	
			acceleration	

Table 15.1: Tree gravity unit parameters controlling the accuracy of calculation.

Table 15.2: Tree gravity unit parameters controlling the boundary conditions.

Variable	Type	Default	Description
[[rpi reference]]	string	"isolated"	or "periodic" or "mixed"
[[rpi reference]]	string	"isolated"	or "periodic"
[[rpi reference]]	string	"isolated"	or "periodic"
[[rpi reference]]	string	"isolated"	or "periodic"
[[rpi reference]]	boolean	true	whether Ewald field should be regenerated
[[rpi reference]]	integer	10	number of terms in the Ewald series
[[rpi reference]]	integer	32	number of points+1 of the Taylor expansion
[[rpi reference]]	string	"ewald_coeffs"	file with coefficients of the Ewald field Taylor expansion
[[rpi reference]]	integer	32	size of the Ewald field grid in x-direction
[[rpi reference]]	integer	32	size of the Ewald field grid in y-direction
[[rpi reference]]	integer	32	size of the Ewald field grid in z-direction
[[rpi reference]]	integer	-1	number of refinement levels (nested grids) for the Ewald
			field; if < 0 , determined automatically
[[rpi reference]]	logical	.true.	if .false., semi-quadratic interpolation is used for
			interpolation in the Ewald field
[[rpi reference]]	string	"ewald_field_acc"	file with the Ewald field for acceleration
[[rpi reference]]	string	"ewald_field_pot"	file with coefficients of the Ewald field for potential

Tree gravity unit parameters controlling the external gravitational field.

Variable	Type	Default	Description	
[[rpi reference]]	logical	.false.	whether to use external field	
[[rpi reference]]	logical	.true.	whether to use gravitational field calculated by the	
			tree solver	
[[rpi reference]]	string	"external_potential.dat"	file containing the external gravitational field	
[[rpi reference]]	string	"planez"	type of the external field: planar or spherical symmetry	
[[rpi reference]]	real	0.0	x-coordinate of the center of the external field	
[[rpi reference]]	real	0.0	y-coordinate of the center of the external field	
[[rpi reference]]	real	0.0	z-coordinate of the center of the external field	

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15.5 Unit Tests

There are two unit tests for the gravity unit. Poisson3 is essentially the Maclaurin spheroid problem described in ??. Because an analytical solution exists, the accuracy of the gravitational solver can be quantified. The second test, Poisson3_active is a modification of Poisson3 to test the mapping of particles in [[api reference]]. Some of the mesh density is redistributed onto particles, and the particles are then mapped back to the mesh, using the analytical solution to verify completeness. This test is similar to the simulation PoisParticles discussed in ??. PoisParticles is based on the Huang-Greengard Poisson gravity test described in ??.

Chapter 16

Particles Unit

The support for particles in FLASH-X will eventually be in two flavors, active and passive. This version only supports passive particles. Passive particles acquire their kinematic information (velocities) directly from the mesh. They are meant to be used as passive flow tracers and do not make sense outside of a hydrodynamical context. The governing equation for the *i*th passive particle is particularly simple and requires only the time integration of interpolated mesh velocities.

$$\frac{d\mathbf{x}_i}{dt} = \mathbf{v}_i \tag{16.1}$$

Active particles experience forces and may themselves contribute to the problem dynamics (e.g., through long-range forces or through collisions). They may additionally have their own motion independent of the grid, so an additional motion equation of

$$\mathbf{v}_i^{n+1} = \mathbf{v}_i^n + \mathbf{a}_i^n \Delta t^n \ . \tag{16.2}$$

may come into play. Here \mathbf{a}_i is the particle acceleration. Solving for the motion of active particles is also referred to as solving the N-body problem. The equations of motion for the *i*th active particle include the equation (??) and another describing the effects of forces.

$$m_i \frac{d\mathbf{v}_i}{dt} = \mathbf{F}_{\mathrm{lr},i} + \mathbf{F}_{\mathrm{sr},i} , \qquad (16.3)$$

Here, $\mathbf{F}_{\mathrm{lr},i}$ represents the sum of all long-range forces (coupling all particles, except possibly those handled by the short-range term) acting on the *i*th particle and $\mathbf{F}_{\mathrm{sr},i}$ represents the sum of all short-range forces (coupling only neighboring particles) acting on the particle.

For both types of particles, the primary challenge is to integrate (??) forward through time. Many alternative integration methods are described in Section ?? below. Additional information about the mesh to particle mapping is described in ??. An introduction to the particle techniques used in Flash-X is given by R. W. Hockney and J. W. Eastwood in *Computer Simulation using Particles* (Taylor and Francis, 1988).

16.1 Time Integration

The passive particles have many different time integration schemes available. The subroutine [[api reference]] handles the movement of particles through space and time. Because FLASH-X will have support for including different types of both active and passive particles in a single simulation, the implementation of [[api reference]] may call several helper routines of the form pt_advanceMETHOD (e.g., pt_advanceLeapfrog, pt_advanceEuler_active, pt_advanceCustom), each acting on an appropriate subset of existing particles. The METHOD here is determined by the ADVMETHOD part of the PARTICLETYPE Config statement (or the ADV par of a -particlemethods setup option) for the type of particle. See the Particles_advance source code for the mapping from ADVMETHOD keyword to pt_advanceMETHOD subroutine call.

16.1.1 Passive Particles

Passive particles may be moved using one of several different methods available in Flash-X. With the exception of **Midpoint**, they are all single-step schemes. The methods are either first-order or second-order accurate, and all are explicit, as described below. In all implementations, particle velocities are obtained by mapping grid-based velocities onto particle positions as described in ??.

Numerically solving Equation (??) for passive particles means solving a set of simple ODE initial value problems, separately for each particle, where the velocities \mathbf{v}_i are given at certain discrete points in time by the state of the hydrodynamic velocity field at those times. The time step is thus externally given and cannot be arbitrarily chosen by a particle motion ODE solver¹. Statements about the order of a method in this context should be understood as referring to the same method if it were applied in a hypothetical simulation where evaluations of velocities \mathbf{v}_i could be performed at arbitrary times (and with unlimited accuracy). Note that FLASH-X does not attempt to provide a particle motion ODE solver of higher accuracy than second order, since it makes little sense to integrate particle motion to a higher order than the fluid dynamics that provide its inputs.

In all cases, particles are advanced in time from t^n (or, in the case of Midpoint, from t^{n-1}) to $t^{n+1} = t^n + \Delta t^n$ using one of the difference equations described below. The implementations assume that at the time when [[api reference]] is called, the fluid fields have already been updated to t^{n+1} , as is the case with the [[api reference]] implementations provided with FLASH-X. A specific implementation of the passive portion of [[api reference]] is selected by a setup option such as -with-unit=Particles/ParticlesMain/passive/Euler in a simulation's Config file (or by listing the path in the Units file if not using the -auto configuration option). Further details are given is ?? below.

• Forward Euler (Particles/ParticlesMain/passive/Euler). Particles are advanced in time from t^n to $t^{n+1} = t^n + \Delta t^n$ using the following difference equation:

$$\mathbf{x}_i^{n+1} = \mathbf{x}_i^n + \mathbf{v}_i^n \Delta t^n \quad . \tag{16.4}$$

Here \mathbf{v}_i^n is the velocity of the particle, which is obtained using particle-mesh interpolation from the grid at $t = t^n$.

Note that this evaluation of \mathbf{v}_i^n cannot be deferred until the time when it is needed at $t=t^{n+1}$, since at that point the fluid variables have been updated and the velocity fields at $t=t^n$ are not available any more. Particle velocities are therefore interpolated from the mesh at $t=t^n$ and stored as particle attributes. Similar concerns apply to the remaining methods but will not be explicitly mentioned every time.

• Two-Stage Runge-Kutta (Particles/ParticlesMain/passive/RungeKutta). This 2-stage Runge-Kutta scheme is the preferred choice in Flash-X. It is also the default which is compiled in if particles are included in the setup but no specific alternative implementation is requested. The scheme is also known as Heun's Method:

$$\mathbf{x}_{i}^{n+1} = \mathbf{x}_{i}^{n} + \frac{\Delta t^{n}}{2} \left[\mathbf{v}_{i}^{n} + \mathbf{v}_{i}^{*,n+1} \right] ,$$
where $\mathbf{v}_{i}^{*,n+1} = \mathbf{v}(\mathbf{x}_{i}^{*,n+1}, t^{n+1}) ,$

$$\mathbf{x}_{i}^{*,n+1} = \mathbf{x}_{i}^{n} + \Delta t^{n} \mathbf{v}_{i}^{n} .$$
(16.5)

Here $\mathbf{v}(\mathbf{x},t)$ denotes evaluation (interpolation) of the fluid velocity field at position \mathbf{x} and time t; $\mathbf{v}_i^{*,n+1}$ and $\mathbf{x}_i^{*,n+1}$ are intermediate results ²; and $\mathbf{v}_i^n = \mathbf{v}(\mathbf{x}_i^n,t^n)$ is the velocity of the particle, obtained using particle-mesh interpolation from the grid at $t=t^n$ as usual.

¹Even though it is possible to do so, see [[api reference]], one does not in general wish to let particles integration dictate the time step of the simulation.

²They can be considered "predicted" positions and velocities.

• Midpoint (Particles/ParticlesMain/passive/Midpoint). This Midpoint scheme is a two-step scheme. Here, the particles are advanced from time t^{n-1} to $t^{n+1} = t^{n-1} + \Delta t^{n-1} + \Delta t^n$ by the equation

$$\mathbf{x}_i^{n+1} = \mathbf{x}_i^{n-1} + \mathbf{v}_i^n (\Delta t^{n-1} + \Delta t^n) \quad . \tag{16.6}$$

The scheme is second order if $\Delta t^n = \Delta t^{n-1}$.

To get the scheme started, an Euler step (as described for passive/Euler) is taken the first time Particles/ParticlesMain/passive/Midpoint/pt_advancePassive is called.

The Midpoint alternative implementation uses the following additional particle attributes:

```
PARTICLEPROP pos2PrevX REAL # two previous x-coordinate
PARTICLEPROP pos2PrevY REAL # two previous y-coordinate
PARTICLEPROP pos2PrevZ REAL # two previous z-coordinate
```

• Estimated Midpoint with Correction (Particles/ParticlesMain/passive/EstiMidpoint2). The scheme is second order even if $\Delta t^n = \Delta t^{n+1}$ is not assumed. It is essentially the EstiMidpoint or "Predictor-Corrector" method of previous releases, with a correction for non-constant time steps by using additional evaluations (at times and positions that are easily available, without requiring more particle attributes).

Particle advancement follows the equation

$$\mathbf{x}_i^{n+1} = \mathbf{x}_i^n + \Delta t^n \, \mathbf{v}_i^{\text{comb}} \,, \tag{16.7}$$

where

$$\mathbf{v}_{i}^{\text{comb}} = c_{1} \mathbf{v}(\mathbf{x}_{i}^{*,n+\frac{1}{2}}, t^{n}) + c_{2} \mathbf{v}(\mathbf{x}_{i}^{*,n+\frac{1}{2}}, t^{n+1}) + c_{3} \mathbf{v}(\mathbf{x}_{i}^{n}, t^{n}) + c_{4} \mathbf{v}(\mathbf{x}_{i}^{n}, t^{n+1})$$
(16.8)

is a combination of four evaluations (two each at the previous and the current time),

$$\mathbf{x}_i^{*,n+\frac{1}{2}} = \mathbf{x}_i^n + \frac{1}{2}\Delta t^{n-1}\mathbf{v}_i^n$$

are estimated midpoint positions as before in the Estimated Midpoint scheme, and the coefficients

$$c_{1} = c_{1}(\Delta t^{n-1}, \Delta t^{n}),$$

$$c_{2} = c_{2}(\Delta t^{n-1}, \Delta t^{n}),$$

$$c_{3} = c_{3}(\Delta t^{n-1}, \Delta t^{n}),$$

$$c_{4} = c_{4}(\Delta t^{n-1}, \Delta t^{n})$$

are chosen dependent on the change in time step so that the method stays second order when $\Delta t^{n-1} \neq \Delta t^n$.

Conditions for the correction can be derived as follows: Let $\Delta t^n_* = \frac{1}{2} \Delta t^{n-1}$ the estimated half time step used in the scheme, let $t^{n+\frac{1}{2}}_* = t^n + \Delta t^n_*$ the estimated midpoint time, and $t^{n+\frac{1}{2}} = t^n + \frac{1}{2} \Delta t^n$ the actual midpoint of the $[t^n, t^{n+1}]$ interval. Also write $\mathbf{x}^{\mathrm{E}, n+\frac{1}{2}}_i = \mathbf{x}^n_i + \frac{1}{2} \Delta t^n \mathbf{v}^n_i$ for first-order (Euler) approximate positions at the actual midpoint time $t^{n+\frac{1}{2}}_*$, and we continue to denote with $\mathbf{x}^{*,n+\frac{1}{2}}_i$ the estimated positions reached at the estimated mipoint time $t^{n+\frac{1}{2}}_*$.

Assuming reasonably smooth functions $\mathbf{v}(\mathbf{x},t)$, we can then write for the exact value of the velocity field at the approximate positions evaluated at the actual midpoint time

$$\mathbf{v}(\mathbf{x}_{i}^{\mathbf{E},n+\frac{1}{2}},t^{n+\frac{1}{2}}) = \mathbf{v}(\mathbf{x}_{i}^{n},t^{n}) + \mathbf{v}_{t}(\mathbf{x}_{i}^{n},t^{n}) \frac{1}{2}\Delta t^{n} + (\mathbf{v}_{i}^{n} \cdot \frac{\partial}{\partial \mathbf{x}})\mathbf{v}(\mathbf{x}_{i}^{n},t^{n}) \frac{1}{2}\Delta t^{n} + O((\frac{1}{2}\Delta t^{n})^{2})$$
(16.9)

by Taylor expansion. It is known that the propagation scheme $\tilde{\mathbf{x}}_i^{n+1} = \mathbf{x}_i^n + \mathbf{v}(\mathbf{x}_i^{\mathrm{E},n+\frac{1}{2}},t^{n+\frac{1}{2}})\Delta t$ using these velocities is second order (this is known as the modified Euler method).

On the other hand, expansion of (??) gives

$$\mathbf{v}_{i}^{\text{comb}} = (c_{1} + c_{2} + c_{3} + c_{4})\mathbf{v}(\mathbf{x}_{i}^{n}, t^{n})$$

$$+ (c_{2} + c_{4})\mathbf{v}_{t}(\mathbf{x}_{i}^{n}, t^{n})\Delta t + (c_{1} + c_{2})(\mathbf{v}_{i}^{n} \cdot \frac{\partial}{\partial \mathbf{x}})\mathbf{v}(\mathbf{x}_{i}^{n}, t^{n})\Delta t_{*}^{n}$$

$$+ \text{ higher order terms in } \Delta t \text{ and } \Delta t_{*}^{n}.$$

After introducing a time step factor f defined by $\Delta t_*^n = f \Delta t^n$, this becomes

$$\mathbf{v}_{i}^{\text{comb}} = (c_{1} + c_{2} + c_{3} + c_{4})\mathbf{v}(\mathbf{x}_{i}^{n}, t^{n})$$

$$+ (c_{2} + c_{4})\mathbf{v}_{t}(\mathbf{x}_{i}^{n}, t^{n})\Delta t + (c_{1} + c_{2})(\mathbf{v}_{i}^{n} \cdot \frac{\partial}{\partial \mathbf{x}})\mathbf{v}(\mathbf{x}_{i}^{n}, t^{n}) f \Delta t$$

$$+ O((\Delta t)^{2}) .$$

$$(16.10)$$

One can derive conditions for second order accuracy by comparing (??) with (??) and requiring that

$$\mathbf{v}_{i}^{\text{comb}} = \mathbf{v}(\mathbf{x}_{i}^{\text{E},n+\frac{1}{2}}, t^{n+\frac{1}{2}}) + O((\Delta t)^{2})$$
 (16.11)

It turns out that the coefficients have to satisfy three conditions in order to eliminate from the theoretical difference between numerical and exact solution all $O(\Delta t^{n-1})$ and $O(\Delta t^n)$ error terms:

$$c_1+c_2+c_3+c_4=1$$
 (otherwise the scheme will not even be of first order),
 $c_2+c_4=\frac{1}{2}$ (and thus also $c_1+c_3=\frac{1}{2}$),
 $c_1+c_2=\frac{\Delta t^n}{\Delta t^{n-1}}$.

The provided implementation chooses $c_4 = 0$ (this can be easily changed if desired by editing in the code). All four coefficients are then determined:

$$c_{1} = \frac{\Delta t^{n}}{\Delta t^{n-1}} - \frac{1}{2} ,$$

$$c_{2} = \frac{1}{2} ,$$

$$c_{3} = 1 - \frac{\Delta t^{n}}{\Delta t^{n-1}} ,$$

$$c_{4} = 0 .$$

Note that when the time step remains unchanged we have $c_1 = c_2 = \frac{1}{2}$ and $c_3 = c_4 = 0$, and so (??) simplifies significantly.

An Euler step, as described for passive/Euler in (??), is taken the first time when Particles/-ParticlesMain/passive/EstiMidpoint2/pt_advancePassive is called and when the time step has changed too much. Since the integration scheme is tolerant of time step changes, it should usually not be necessary to apply the second criterion; even when it is to be employed, the criteria should be less strict than for an uncorrected EstiMidpoint scheme. For EstiMidPoint2 the timestep is considered to have changed too much if either of the following is true:

$$\Delta t^n > \Delta t^{n-1} \quad \text{and} \quad \left| \Delta t^n - \Delta t^{n-1} \right| \geq \mathtt{pt_dtChangeToleranceUp} \times \Delta t^{n-1}$$

or

$$\Delta t^n < \Delta t^{n-1} \quad \text{and} \quad \left| \Delta t^n - \Delta t^{n-1} \right| \geq \mathtt{pt_dtChangeToleranceDown} \times \Delta t^{n-1},$$

where [[rpi reference]] and [[rpi reference]] are runtime parameter specific to the EstiMidPoint2 alternative implementation.

The EstiMidpoint2 alternative implementation uses the following additional particle attributes for storing the values of $\mathbf{x}_i^{*,n+\frac{1}{2}}$ and $\mathbf{v}_i^{*,n+\frac{1}{2}}$ between the Particles_advance calls at t^n and t^{n+1} :

```
PARTICLEPROP velPredX REAL PARTICLEPROP velPredZ REAL PARTICLEPROP posPredX REAL PARTICLEPROP posPredX REAL PARTICLEPROP posPredZ REAL PARTICLEPROP posPredZ REAL
```

The time integration of passive particles is tested in the ParticlesAdvance unit test, which can be used to examine the convergence behavior, see ??.

16.2 Mesh/Particle Mapping

Particles behave in a fundamentally different way than grid-based quantities. Lagrangian, or passive particles are essentially independent of the grid mesh and move along with the velocity field. Active particles may be located independently of mesh refinement. In either case, there is a need to convert grid-based quantities into similar attributes defined on particles, or vice versa. The method for interpolating mesh quantities to tracer particle positions must be consistent with the numerical method to avoid introducing systematic error. In the case of a finite-volume methods such as those used in FLASH-X, the mesh quantities have cell-averaged rather than point values, which requires that the interpolation function for the particles also represent cell-averaged values. Cell averaged quantities are defined as

$$f_i(x) \equiv \frac{1}{\Delta x} \int_{x_{i-1/2}}^{x_{i-1/2}} f(x') dx'$$
 (16.12)

where i is the cell index and Δx is the spatial resolution. The mapping back and forth from the mesh to the particle properties are defined in the routines Particles_mapFromMesh and Particles_mapToMeshOneBlk.

Specifying the desired mapping method is accomplished by designating the MAPMETHOD in the Simulation Config file for each type of particle. See ?? for more details.

16.2.1 Quadratic Mesh Mapping

The quadratic mapping package defines an interpolation back and forth to the mesh which is second order. This implementation is primarily meant to be used with passive tracer particles.

To derive it, first consider a second-order interpolation function of the form

$$f(x) = A + B(x - x_i) + C(x - x_i)^2. (16.13)$$

Then integrating gives

$$f_{i-1} = \frac{1}{\Delta x} \left[A + \frac{1}{2} B (x - x_i)^2 \Big|_{x_{i-3/2}}^{x_{i-1/2}} + \frac{1}{3} C (x - x_i)^3 \Big|_{x_{i-3/2}}^{x_{i-1/2}} \right]$$

$$= A - B \Delta x + \frac{13}{12} C \Delta x^2 , \qquad (16.14)$$

$$f_{i} = \frac{1}{\Delta x} \left[A + \frac{1}{2} B (x - x_{i})^{2} \Big|_{x_{i-1/2}}^{x_{i+1/2}} + \frac{1}{3} C (x - x_{i})^{3} \Big|_{x_{i-1/2}}^{x_{i+1/2}} \right]$$

$$= A + \frac{1}{12} C \Delta x^{2} , \qquad (16.15)$$

and

$$f_{i+1} = \frac{1}{\Delta x} \left[A + \frac{1}{2} B (x - x_i)^2 \Big|_{x_{i+1/2}}^{x_{i+3/2}} + \frac{1}{3} C (x - x_i)^3 \Big|_{x_{i-3/2}}^{x_{i-1/2}} \right]$$

$$= A - B \Delta x + \frac{13}{12} C \Delta x^2 , \qquad (16.16)$$

We may write these as

$$\begin{bmatrix} f_{i+1} \\ f_i \\ f_{i-1} \end{bmatrix} = \begin{bmatrix} 1 & -1 & \frac{13}{12} \\ 1 & 0 & \frac{1}{12} \\ 1 & 1 & \frac{13}{12} \end{bmatrix} \begin{bmatrix} A \\ B\Delta x \\ C\Delta x^2 \end{bmatrix}.$$
 (16.17)

Inverting this gives expressions for A, B, and C

$$\begin{bmatrix} A \\ B\Delta x \\ C\Delta x^2 \end{bmatrix} = \begin{bmatrix} -\frac{1}{24} & \frac{13}{12} & -\frac{1}{24} \\ -\frac{1}{2} & 0 & \frac{1}{2} \\ \frac{1}{2} & -1 & \frac{1}{2} \end{bmatrix} \begin{bmatrix} f_{i+1} \\ f_i \\ f_{i-1} \end{bmatrix}.$$
(16.18)

In two dimensions, we want a second-order interpolation function of the form

$$f(x,y) = A + B(x - x_i) + C(x - x_i)^2 + D(y - y_j) + E(y - y_j)^2 + F(x - x_i)(y - y_j).$$
 (16.19)

In this case, the cell averaged quantities are given by

$$f_{i,j}(x,y) \equiv \frac{1}{\Delta y} \Delta x \int_{x_{i-1/2}}^{x_{i+1/2}} dx' \int_{y_{j-1/2}}^{x_{j-1/2}} dy' f(x',y') . \tag{16.20}$$

Integrating the 9 possible cell averages gives, after some algebra,

$$\begin{bmatrix} f_{i-1,j-1} \\ f_{i,j-1} \\ f_{i+1,j-1} \\ f_{i-1,j} \\ f_{i,j} \\ f_{i+1,j} \\ f_{i-1,j+1} \\ f_{i+1,j+1} \end{bmatrix} = \begin{bmatrix} 1 & -1 & \frac{13}{12} & -1 & \frac{13}{12} & 1 \\ 1 & 0 & \frac{1}{12} & -1 & \frac{13}{12} & 0 \\ 1 & 1 & \frac{13}{12} & -1 & \frac{13}{12} & -1 \\ 1 & -1 & \frac{13}{12} & 0 & \frac{1}{12} & 0 \\ 1 & 0 & \frac{1}{12} & 0 & \frac{1}{12} & 0 \\ 1 & 1 & \frac{13}{12} & 0 & \frac{1}{12} & 0 \\ 1 & 1 & \frac{13}{12} & 1 & \frac{13}{12} & -1 \\ 1 & 0 & \frac{1}{12} & 1 & \frac{13}{12} & -1 \\ 1 & 0 & \frac{1}{12} & 1 & \frac{13}{12} & 0 \\ 1 & 1 & \frac{13}{12} & 1 & \frac{13}{12} & 1 \end{bmatrix} \begin{bmatrix} A \\ B\Delta x \\ C\Delta x^2 \\ D\Delta y \\ E\Delta y^2 \\ F\Delta x\Delta y \end{bmatrix}.$$

$$(16.21)$$

At this point we note that there are more constraints than unknowns, and we must make a choice of the constraints. We chose to ignore the cross terms and take only the face-centered cells next to the cell containing the particle, giving

$$\begin{bmatrix} f_{i,j-1} \\ f_{i-1,j} \\ f_{i,j} \\ f_{i+1,j} \\ f_{i,j+1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & \frac{1}{12} & -1 & \frac{13}{12} \\ 1 & -1 & \frac{13}{12} & 0 & \frac{1}{12} \\ 1 & 0 & \frac{1}{12} & 0 & \frac{1}{12} \\ 1 & 1 & \frac{13}{12} & 0 & \frac{1}{12} \\ 1 & 0 & \frac{1}{12} & 1 & \frac{13}{12} \end{bmatrix} \begin{bmatrix} A \\ B\Delta x \\ C\Delta x^2 \\ D\Delta y \\ E\Delta y^2 \end{bmatrix}.$$
(16.22)

Inverting gives

$$\begin{bmatrix} A \\ B\Delta x \\ C\Delta x^2 \\ D\Delta y \\ E\Delta y^2 \end{bmatrix} = \begin{bmatrix} -\frac{1}{24} & -\frac{1}{24} & \frac{7}{6} & -\frac{1}{24} & -\frac{1}{24} \\ 0 & -\frac{1}{2} & 0 & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & -1 & \frac{1}{2} & 0 \\ -\frac{1}{2} & 0 & 0 & 0 & \frac{1}{2} \\ \frac{1}{2} & 0 & -1 & 0 & \frac{1}{2} \end{bmatrix} \begin{bmatrix} f_{i,j-1} \\ f_{i-1,j} \\ f_{i,j} \\ f_{i+1,j} \\ f_{i,j+1} \end{bmatrix}.$$
(16.23)

Similarly, in three dimensions, the interpolation function is

$$f(x,y,z) = A + B(x - x_i) + C(x - x_i)^2 + D(y - y_j) + E(y - y_j)^2 + F(z - z_k) + G(z - z_k)^2.$$
 (16.24) and we have

$$\begin{bmatrix} A \\ B\Delta x \\ C\Delta x^{2} \\ D\Delta y \\ E\Delta y^{2} \\ F\Delta z \\ G\Delta z^{2} \end{bmatrix} = \begin{bmatrix} -\frac{1}{24} & -\frac{1}{24} & -\frac{1}{24} & \frac{5}{4} & -\frac{1}{24} & -\frac{1}{24} & -\frac{1}{24} \\ 0 & 0 & -\frac{1}{2} & 0 & \frac{1}{2} & 0 & 0 \\ 0 & 0 & \frac{1}{2} & -1 & \frac{1}{2} & 0 & 0 \\ 0 & -\frac{1}{2} & 0 & 0 & 0 & \frac{1}{2} & 0 \\ 0 & \frac{1}{2} & 0 & -1 & 0 & \frac{1}{2} & 0 \\ -\frac{1}{2} & 0 & 0 & 0 & 0 & 0 & \frac{1}{2} \\ \frac{1}{2} & 0 & 0 & -1 & 0 & 0 & \frac{1}{2} \end{bmatrix} \begin{bmatrix} f_{i,j,k-1} \\ f_{i,j-1,k} \\ f_{-i,j,k} \\ f_{i,j,k} \\ f_{i,j+1,k} \\ f_{i,j,k+1} \end{bmatrix}.$$
(16.25)

Finally, the above expressions apply only to Cartesian coordinates. In the case of cylindrical (r, z) coordinates, we have

$$f(r,z) = A + B(r - r_i) + C(r - r_i)^2 + D(z - z_j) + E(z - z_j)^2 + F(r - r_i)(z - z_j).$$
(16.26)

and

$$\begin{bmatrix} A \\ B\Delta r \\ C\Delta r^{\frac{2}{6}} \\ D\Delta z \\ E\Delta z^{2} \end{bmatrix} = \begin{bmatrix} -\frac{1}{24} & -\frac{h_{1}-1}{24h_{1}} & \frac{7}{6} & -\frac{h_{1}-1}{24h_{1}} & -\frac{1}{24} \\ 0 & -\frac{(7+6h_{1})(h_{1}-1)}{3h_{2}} & \frac{2h_{1}}{3h_{2}} & \frac{(7+6h_{1})(h_{1}-1)}{3h_{2}} & 0 \\ 0 & \frac{(12h_{1}^{2}+12h_{1}-1)(h_{1}-1)}{h_{1}h_{2}} & -2\frac{12h_{1}^{2}-13}{h_{2}} & -\frac{(12h_{1}^{2}+12h_{1}-1)(h_{1}-1)}{h_{1}h_{2}} & 0 \\ 0 & \frac{1}{2} & 0 & 0 & \frac{1}{2} & 0 \end{bmatrix} \begin{bmatrix} f_{i,j-1} \\ f_{i-1,j} \\ f_{i,j} \\ f_{i+1,j} \\ f_{i,j+1} \end{bmatrix}. \quad (16.27)$$

16.2.2 Cloud in Cell Mapping

Other interpolation routines can be defined that take into account the actual quantities defined on the grid. These "mesh-based" algorithms are represented in FLASH-X by the Cloud-in-Cell mapping, where the interpolation to/from the particles is defined as a simple linear weighting from nearby grid points. The weights are defined by considering only the region of one "cell" size around each particle location; the proportional volume of the particle "cloud" corresponds to the amount allocated to/from the mesh. The CIC method can be used with both types of particles. When using it with active particles the MapToMesh methods should also be selected. In order to include the CIC method with passive particles, the setup command line option is -with-unit=Particles/ParticlesMapping/CIC. Two additional command line option -with-unit=Particles/ParticlesMapping/MapToMesh and -with-unit=Grid/GridParticles/MapToMesh are necessary when using the active particles. All of these command line options can be replaced by placing the appropriate REQUIRES/REQUESTS directives in the Simulation Config file.

16.3 Using the Particles Unit

The Particles unit encompasses nearly all aspects of Lagrangian particles. The exceptions are input/output the movement of related data structures between different blocks as the particles move from one block to another, and mapping the particle attributes to and from the grid.

Particle types must be specified in the Config file of the Simulations unit setup directory for the application, and the syntax is explained in ??. At configuration time, the setup script parses the PARTICLETYPE specifications in the Config files, and generates an F90 file [[api reference]].F90 that populates a data structure gr_ptTypeInfo. This data structure contains information about the method of initialization and interpolation methods for mapping the particle attributes to and from the grid for each included particle type. Different time integration schemes are applied to active and passive particles. However, in one simulation, all active particles are integrated using the same scheme, regardless of how many active types exists. Similarly, only one passive integration scheme is used. The added complexity of multiple particle types allows different methods to be used for initialization of particles positions and their mapping to and from the grid quantities. Because several different implementations of each type of functionality can co-exist in one simulation, there are no defaults in the Particles unit Config files. These various functionalities are organized into different subunits; a brief description of each subunit is included below and further expanded in subsections in this chapter.

• The ParticlesInitialization subunit distributes a given set of particles through the spatial domain at the simulation startup. Some type of spatial initialization is always required; the functionality is provided by [[api reference]]. The users of active particles typically have their own custom initialization. The following two implementations of initialization techniques are included in the FLASH-X distribution (they are more likely to used with the passive tracer particles):

Lattice distributes particles regularly along the axes directions throughout a subsection of the physical grid.

WithDensity distributes particles randomly, with particle density being proportional to the grid gas density.

Users have two options for implementing custom initialization methods. The two files involved in the process are: [[api reference]] and pt_initPositions. The former does some housekeeping such as allowing for inclusion of one of the available methods along with the user specified one, and assigning tags at the end. A user wishing to add one custom method with no constraints on tags etc is advised to implement a custom version of the latter. This approach allows the user to focus the implementation on the placement of particles only. Users desirous of refining the grid based on particles count during initialiation should see the setup PoisParticles for an example implementation of the Particles_initPositions routine. If more than one implementation of pt_initPositions is desired in the same simulation then it is necessary to implement each one separately with different names (as we do for tracer particles: pt_initPositionsLattice and pt_initPositionsWithDensity) in their simulation setup directory. In addition, a modified copy of Particles_initPositions, which calls these new routines in the loop over types, must also be placed in the same directory.

- The ParticlesMain subunit contains the various time-integration options for both active and passive particles. A detailed overview of the different schemes is given in ??.
- The ParticlesMapping subunit controls the mapping of particle properties to and from the grid. Flash-X currently supplies the following mapping schemes:

Cloud-in-cell (ParticlesMapping/meshWeighting/CIC), which weights values at nearby grid cells; and

Quadratic (ParticlesMapping/Quadratic), which performs quadratic interpolation.

Some form of mapping must always be included when running a simulation with particles. As mentioned in ?? the quadratic mapping scheme is only available to map *from* the grid quantities to the corresponding particle attributes. Since active particles require the same mapping scheme to be used in mapping to and from the mesh, they cannot use the quadratic mapping scheme as currently implemented in FLASH-X. The CIC scheme may be used by both the active and passive particles.

After particles are moved during time integration or by forces, they may end up on other blocks within or without the current processor. The redistribution of particles among processors is handled by the <code>GridParticles</code> subunit, as the algorithms required vary considerably between the grid implementations. The boundary conditions are also implemented by the <code>GridParticles</code> unit. See <code>??</code> for more details of these redistribution algorithms. The user should include the option <code>-with-unit=Grid/GridParticles</code> on the setup line, or <code>REQUIRES Grid/GridParticles</code> in the Config file.

In addition, the input-output routines for the Particles unit are contained in a subunit IOParticles. Particles are written to the main checkpoint files. If the user desires, a separate output file can be created which contains only the particle information. See ?? below as well as ?? for more details. The user should include the option -with-unit=IO/IOParticles on the setup line, or REQUIRES IO/IOParticles in the Config file.

In FLASH-X, the initial particle positions can be used to construct an appropriately refined grid, i.e. more refined in places where there is a clustering of particles. To use this feature the flash.par file must include: refine_on_particle_count=.true. and max_particles_per_blk=[some value]. Please be aware that Flash-X will abort if the criterion is too demanding. To overcome the abort, specify a less demanding criterion, or increase the value of lrefine_max.

16.3.1 Particles Runtime Parameters

There are several general runtime parameters applicable to the Particles unit, which affect every implementation. The variable [[rpi reference]] obviously must be set equal to .true. to utilize the Particles unit. The time stepping is controlled with [[rpi reference]]; a value less than one ensures that particles will not step farther than one entire cell in any given time interval. The Lattice initialization routines have additional parameters. The number of evenly spaced particles is controlled in each direction by [[rpi reference]] and similar variables in Y and Z. The physical range of initialization is controlled by [[rpi reference]] and the like. Finally, note that the output of particle properties to special particle files is controlled by runtime parameters found in the IO unit. See ?? for more details.

16.3.2 Particle Attributes

By default, particles are defined to have eight real properties or attributes: 3 positions in x,y,z; 3 velocities in x,y,z; the current block identification number; and a tag which uniquely identifies the particle. Additional properties can be defined for each particle. For example, active particles usually have the additional properties of mass and acceleration (needed for the integration routines, see Table ??). Depending upon the simulation, the user can define particle properties in a manner similar to that used for mesh-based solution variables. To define a particle attribute, add to a Config file a line of the form

PARTICLEPROP property-name

For attributes that are meant to merely sample and record the state of certain mesh variables along trajectories, Flash-X can automatically invoke interpolation (or, in general, some map method) to generate attribute values from the appropriate grid quantities. (For passive tracer particles, these are typically the only attributes beyond the default set of eight mentioned above.) The routine [[api reference]] is invoked by Flash-X at appropriate times to effect this mapping, namely before writing particle data to checkpoint and particle plot files. To direct the default implementation of Particles_updateAttributes to act as desired for tracer attributes, the user must define the association of the particle attribute with the appropriate mesh variable by including the following line in the Config file:

PARTICLEMAP TO property-name FROM VARIABLE variable-name

These particle attributes are carried along in the simulation and output in the checkpoint files. At runtime, the user can specify the attributes to output through runtime parameters [[rpi reference]], [[rpi reference]], etc. These specified attributes are collected in an array by the [[api reference]] routine. This array in turn is used by [[api reference]] to calculate the values of the specified attributes from the corresponding mesh quantities before they are output.

16.3.3 Particle I/O

Particle data are written to and read from checkpoint files by the I/O modules (??). For more information on the format of particle data written to output files, see ?? and ??.

Particle data can also be written out to the flash.dat file. The user should include a local copy of [[api reference]] in their Simulation directory. The Orbit test problem supplies an example IO_writeIntegralQuantities routine that is useful for writing individual particle trajectories to disk at every timestep.

There is also a utility routine [[api reference]] which can be used to dump particle output to a plain text file. An example of usage can be found in [[api reference]]. Output from this routine can be read using the fidlr routine particles_dump.pro.

Part VI Monitor Units

Chapter 17

Logfile Unit

Flash-X supplies the Logfile unit to manage an output log during a Flash-X simulation. The logfile contains various types of useful information, warnings, and error messages produced by a Flash-X run. Other units can add information to the logfile through the Logfile unit interface. The Logfile routines enable a program to open and close a log file, write time or date stamps to the file, and write arbitrary messages to the file. The file is kept closed and is only opened for appending when information is to be written, thus avoiding problems with unflushed buffers. For this reason, Logfile routines should not be called within time-sensitive loops, as system calls are generated. Even when starting from scratch, the logfile is opened in append mode to avoid deleting important logfiles. Two kinds of Logfiles are supported. The first kind is similar to that in Flash-X2 and early releases of FLASH-X, where the master processor has exclusive access to the logfile and writes global information to it. The newer kind gives all processors access to their own private logfiles if they need to have one. Similar to the traditional logfile, the private logfiles are opened in append mode, and they are created the first time a processor writes to one. The private logfiles are extremely useful to gather information about failures causes by a small fraction of processors; something that cannot be done in the traditional logfile.

The Logfile unit is included by default in all the provided Flash-X simulations because it is required by the Driver/DriverMain Config. As with all the other units in Flash-X, the data specific to the Logfile unit is stored in the module Logfile_data.F90. Logfile unit scope data variables begin with the prefix log_variableName and they are initialized in the routine [[api reference]].

By default, the logfile is named flash.log and found in the output directory. The user may change the name of the logfile by altering the runtime parameter [[rpi reference]] in the flash.par.

```
# names of files
basenm = "cellular_"
log_file = "cellular.log"
```

17.1 Meta Data

The logfile stores meta data about a given run including the time and date of the run, the number of MPI tasks, dimensionality, compiler flags and other information about the run. The snippet below is an example from a logfile showing the basic setup and compilation information:

Number of MPI tasks: 2
MPI version: 1

MPI subversion: 2
Dimensionality: 2
Max Number of Blocks/Proc: 1000
Number x zones: 8
Number y zones: 8

```
Number z zones:
                                       1
Setup stamp:
              Wed Apr 19 13:49:36 2006
              Wed Apr 19 16:35:57 2006
Build stamp:
System info:
Linux zingiber.uchicago.edu 2.6.12-1.1376_FC3smp #1 SMP Fri Aug 26 23:50:33 EDT
Version:
                 Flash-X 3.0.
Build directory: /home/kantypas/Flash-X3/trunk/Sod
Setup syntax:
/home/kantypas/Flash-X3/trunk/bin/setup.py Sod -2d -auto -unit=I0/I0Main/hdf5/parallel/PM
                   -objdir=Sod
f compiler flags:
/usr/local/pgi6/bin/pgf90 -I/usr/local/mpich-pg/include -c -r8 -i4 -fast -g
                   -DMAXBLOCKS=1000 -DNXB=8 -DNYB=8 -DNZB=1 -DN_DIM=2
c compiler flags:
/usr/local/pgi6/bin/pgcc -I/usr/local/hdf5-pg/include -I/usr/local/mpich-pg/include
                   -c -O2 -DMAXBLOCKS=1000 -DNXB=8 -DNYB=8 -DNZB=1 -DN_DIM=2
```

17.2 Runtime Parameters, Physical Constants, and Multispecies Data

The logfile also records which units were included in a simulation, the runtime parameters, physical constants, and any species and their properties from the Multispecies unit. The FLASH-X logfile keeps track of whether a runtime parameter is a default value or whether its value has been redefined in the flash.parThe [CHANGED] symbol will occur next to a runtime parameter if its value has been redefined in the flash.par. Note that the runtime parameters are output in alphabetical order within the Fortran datatype – so integer parameters are shown first, then real, then string, then Boolean. The snippet below shows the this portion of the logfile; omitted sections are indicated with "...".

```
Flash-X Units used:
  Driver
  Driver/DriverMain
  Driver/DriverMain/TimeDep
  Grid/GridMain
  Grid/GridMain/paramesh
  Grid/GridMain/paramesh/paramesh4
  Multispecies
  Particles
  PhysicalConstants
  PhysicalConstants/PhysicalConstantsMain
  RuntimeParameters
  RuntimeParameters/RuntimeParametersMain
  physics/utilities/solvers/LinearAlgebra
______
RuntimeParameters:
______
                             2 [CHANGED]
algebra
bndpriorityone
                             1
```

```
bndprioritythree
                                       3
. . .
cfl
                                              0.800E+00
checkpointfileintervaltime =
                                              0.100E-08 [CHANGED]
                                              0.100E+00
derefine_cutoff_1
                                              0.200E+00
derefine_cutoff_2
                                              0.200E+00
                                              0.128E+02 [CHANGED]
zmax
                                              0.000E+00
                            =
zmin
basenm
                            = cellular_
                                                             [CHANGED]
                           = dens_ie
eosmode
eosmodeinit
                           = dens_ie
                            = cartesian
geometry
                                                             [CHANGED]
log_file
                           = cellular.log
output_directory
pc_unitsbase
                           = CGS
plot_grid_var_1
                            = none
plot_grid_var_10
                            = none
plot_grid_var_11
                            = none
plot_grid_var_12
                            = none
plot_grid_var_2
                            = none
yr_boundary_type
                            = periodic
zl_boundary_type
                            = periodic
zr_boundary_type
                            = periodic
bytepack
                            = F
chkguardcells
converttoconsvdformeshcalls = F
converttoconsvdinmeshinterp = F
                               T [CHANGED]
useburn
                               F
useburntable
```

Known units of measurement:

	Unit	CGS Value	Base Unit	
1	cm	1.0000	cm	
2	s	1.0000	S	
3	K	1.0000	K	
4	g	1.0000	g	
5	esu	1.0000	esu	
6	m	100.00	cm	
7	km	0.10000E+06	cm	
8	pc	0.30857E+19	cm	

Known physical constants:

	Constant Name	Constant Value	cm	s	g	K	esu
1	Newton	0.66726E-07	3.00	-2.00	-1.00	0.00	0.00
2	speed of light	0.29979E+11	1.00	-1.00	0.00	0.00	0.00

. . .

```
15 Euler 0.57722 0.00 0.00 0.00 0.00 0.00
```

Multifluid database contents:

Initially defined values of species:

Name	Index	Total	Positive Neutral	Negative	bind Ener Gamma
ar36	12	3.60E+01	1.80E+01 -9.99E+02	-9.99E+02	3.07E+02 -9.99E+02
c12	13	1.20E+01	6.00E+00 -9.99E+02	-9.99E+02	9.22E+01 -9.99E+02
ca40	14	4.00E+01	2.00E+01 -9.99E+02	-9.99E+02	3.42E+02 -9.99E+02
ti44	24	4.40E+01	2.20E+01 -9.99E+02	-9.99E+02	3.75E+02 -9.99E+02
=====		=========			

17.3 Accessor Functions and Timestep Data

Other units within Flash-X may make calls to write information, or stamp, the logfile. For example, the Driver unit calls the API routine [[api reference]] after each timestep. The Grid unit calls [[api reference]] whenever refinement occurs in an adaptive grid simulation. If there is an error that is caught in the code the API routine [[api reference]] stamps the logfile before aborting the code. Any unit can stamp the logfile with one of two routines [[api reference]] which includes a data and time stamp along with a logfile message, or [[api reference]] which simply writes a string to the logfile.

The routine [[api reference]] is overloaded so the user must use the interface file Logfile_interface.F90 in the calling routine. The next snippit shows logfile output during the evolution loop of a Flash-X run.

```
[ 04-19-2006 16:40.43 ] [Simulation_init]: initializing Sod problem
[GRID amr_refine_derefine]
                                     initiating refinement
[GRID amr_refine_derefine] min blks 0
                                       max blks 1
                                                    tot blks 1
[GRID amr_refine_derefine] min leaf blks 0
                                           max leaf blks 1
                                                             tot leaf blks 1
[GRID amr_refine_derefine]
                                     refinement complete
[ 04-19-2006 16:40.43 ] [GRID gr_expandDomain]: create level=2
[GRID amr_refine_derefine]
                                     initiating refinement
[GRID amr_refine_derefine] min blks 250
                                         max blks 251
                                                        tot blks 501
[GRID amr_refine_derefine] min leaf blks 188
                                             max leaf blks 188
                                                                  tot leaf blks 376
[GRID amr_refine_derefine]
                                     refinement complete
[ 04-19-2006 16:40.44 ] [GRID gr_expandDomain]: create level=7
[ 04-19-2006 16:40.44 ] [GRID gr_expandDomain]: create level=7
[ 04-19-2006
            16:40.44 ] [GRID gr_expandDomain]: create level=7
[ 04-19-2006 16:40.44 ] [IO_writeCheckpoint] open: type=checkpoint name=sod_hdf5_chk_0000
[ 04-19-2006 16:40.44 ] [io_writeData]: wrote
                                                501
                                                             blocks
[ 04-19-2006 16:40.44 ] [IO_writeCheckpoint] close: type=checkpoint name=sod_hdf5_chk_0000
[ 04-19-2006 16:40.44 ] [IO writePlotfile] open: type=plotfile name=sod_hdf5_plt_cnt_0000
[ 04-19-2006 16:40.44 ] [io_writeData]: wrote
                                                501
                                                             blocks
[ 04-19-2006 16:40.44 ] [IO_writePlotfile] close: type=plotfile name=sod_hdf5_plt_cnt_0000
[ 04-19-2006 16:40.44 ] [Driver_evolveFlash]: Entering evolution loop
[ 04-19-2006 16:40.44 ] step: n=1 t=0.000000E+00 dt=1.000000E-10
[ 04-19-2006 16:41.06 ] [io_writeData]: wrote
                                                501
[ 04-19-2006 16:41.06 ] [IO_writePlotfile] close: type=plotfile name=sod_hdf5_plt_cnt_0002
[ 04-19-2006 16:41.06 ] [Driver_evolveFlash]: Exiting evolution loop
______
```

17.4 Performance Data

Finally, the logfile records performance data for the simulation. The Timers unit (see ??) is responsible for storing, collecting and interpreting the performance data. The Timers unit calls the API routine [[api reference]] to format the performance data and write it to the logfile. The snippet below shows the performance data section of a logfile.

perf_summary: code performance summary

beginning: 04-19-2006 16:40.43

ending: 04-19-2006 16:41.06

seconds in monitoring period: 23.188

number of subintervals: 21

number of evolved zones: 16064

zones per second: 692.758

zones per second : 692.758

accounting unit	time sec	num calls	secs avg	time pct
initialization	1.012	1	1.012	4.366
guardcell internal	0.155	17	0.009	0.669
writeCheckpoint	0.085	1	0.085	0.365
writePlotfile	0.061	1	0.061	0.264
evolution	22.176	1	22.176	95.633
hydro	18.214	40	0.455	78.549
guardcell internal	2.603	80	0.033	11.227
sourceTerms	0.000	40	0.000	0.002
particles	0.000	40	0.000	0.001
Grid_updateRefinement	1.238	20	0.062	5.340
tree	1.126	10	0.113	4.856
guardcell tree	0.338	10	0.034	1.459
guardcell internal	0.338	10	0.034	1.458
markRefineDerefine	0.339	10	0.034	1.460
guardcell internal	0.053	10	0.005	0.230
amr_refine_derefine	0.003	10	0.000	0.011
updateData	0.002	10	0.000	0.009
guardcell	0.337	10	0.034	1.453
guardcell internal	0.337	10	0.034	1.452
eos	0.111	10	0.011	0.481
update particle refinemen	0.000	10	0.000	0.000
io	2.668	20	0.133	11.507
writeCheckpoint	0.201	2	0.101	0.868
writePlotfile	0.079	2	0.039	0.340
diagnostics	0.040	20	0.002	0.173

[04-19-2006 16:41.06] LOGFILE_END: Flash-X run complete.

17.5 Example Usage

An example program using the Logfile unit might appear as follows:

program testLogfile

use Logfile_interface, ONLY: Logfile_init, Logfile_stamp, Logfile_open, Logfile_close use Driver_interface, ONLY: Driver_initParallel

```
use RuntimeParameters_interface, ONLY: RuntimeParameters_init
use PhysicalConstants_interface, ONLY: PhysicalConstants_init
implicit none
integer :: i
integer :: log_lun
integer :: myPE, numProcs
logical :: restart, localWrite
call Driver_initParallel(myPE, numProcs) !will initialize MPI
call RuntimeParameters_init(myPE, restart) ! Logfile_init needs runtime parameters
call PhysicalConstants_init(myPE) ! PhysicalConstants information adds to logfile
call Logfile_init(myPE, numProcs) ! will end with Logfile_create(myPE, numProcs)
call Logfile_stamp (myPE, "beginning log file test...", "[programtestLogfile]")
localWrite=.true.
call Logfile_open(log_lun,localWrite) !! open the local logfile
do i = 1, 10
  write (log_lun,*) 'i = ', i
enddo
call Logfile_stamp (myPE, "finished logfile test", "[program testLogfile]")
call Logfile_close(myPE, log_lun)
```

end program testLogfile

Timer and Profiler Units

18.1 Timers

18.1.1 MPINative

Flash-X includes an interface to a set of stopwatch-like timing routines for monitoring performance. The interface is defined in the monitors/Timers unit, and an implementation that uses the timing functionality provided by MPI is provided in monitors/Timers/TimersMain/MPINative. Future implementations might use the PAPI framework to track hardware counter details.

The performance routines start or stop a timer at the beginning or end of a section of code to be monitored, and accumulate performance information in dynamically assigned accounting segments. The code also has an interface to write the timing summary to the Flash-X logfile. These routines are not recommended for timing very short segments of code due to the overhead in accounting.

There are two ways of using the Timers routines in your code. One mode is to simply pass timer names as strings to the start and stop routines. In this first way, a timer with the given name will be created if it doesn't exist, or otherwise reference the one already in existence. The second mode of using the timers references them not by name but by an integer key. This technique offers potentially faster access if a timer is to be started and stopped many times (although still not recommended because of the overhead). The integer key is obtained by calling with a string name [[api reference]] which will only create the timer if it doesn't exist and will return the integer key. This key can then be passed to the start and stop routines.

The typical usage pattern for the timers is implemented in the default Driver implementation. This pattern is: call [[api reference]] once at the beginning of a run, call [[api reference]] and [[api reference]] around sections of code, and call [[api reference]] at the end of the run to report the timing summary at the end of the logfile. However, it is possible to call [[api reference]] in the middle of a run to reset all timing information. This could be done along with writing the summary once per-timestep to report code times on a per-timestep basis, which might be relevant, for instance, for certain non-fixed operation count solvers. Since [[api reference]] does not reset the integer key mappings, it is safe to obtain a key through [[api reference]] once in a saved variable, and continue to use it after calling [[api reference]].

Two runtime parameters control the Timer unit and are described below.

Table 18.1: Timer Unit runtime parameters.

Parameter Ty	pe Default value	Description
eachProcWritesSummar	, LOGICAL TRUE	Should each process write its summary to its own file? If true, each process will write its summary to a file named timer_summary_ <pre>process id></pre>

Table 18.1: Timers parameters (continued).

Parameter	Type	Default	value	Description
writeStatSummary	I	LOGICAL	TRUE	Should timers write the max/min/avg values
				for timers to the logfile?

monitors/Timers/TimersMain/MPINative writes two summaries to the logfile: the first gives the timer execution of the master processor, and the second gives the statistics of max, min, and avg times for timers on all processors. The secondary max, min, and avg times will not be written if some process executed timers differently than another. For example, this anomaly happens if not all processors contain at least one block. In this case, the Hydro timers only execute on the processors that possess blocks. See ?? for an example of this type of output. The max, min, and avg summary can be disabled by setting the runtime parameter [[rpi reference]] to false. In addition, each process can write its summary to its own file, set the runtime parameter [[rpi reference]] to false.

18.1.2 Tau

In Flash-X3.1 we add an alternative Timers implementation which is designed to be used with the Tau framework (http://acts.nersc.gov/tau/). Here, we use Tau API calls to time the Flash-X labeled code sections (marked by Timers_start and Timers_stop). After running the simulation, the Tau profile contains timing information for both Flash-X labeled code sections and all individual subroutines / functions. This is useful because fine grained subroutine / function level data can be overwhelming in a huge code like Flash-X. Also, the callpaths are preserved, meaning we can see how long is spent in individual subroutines / functions when they are called from within a particular Flash-X labeled code section. Another reason to use the Tau version is that the MPINative version (See ??) is implemented using recursion, and so incurs significant overhead for fine grain measurements.

To use this implementation we must compile the Flash-X source code with the Tau compiler wrapper scripts. These are set as the default compilers automatically whenever we specify the -tau option (see ??) to the setup script. In addition to the -tau option we must specify --with-unit=monitors/Timers/Timers-Main/Tau as this Timers implementation is not the default.

18.2 Profiler

In addition to an interface for simple timers, Flash-X includes a generic interface for third-party profiling or tracing libraries. This interface is defined in the monitors/Profiler unit.

In FLASH-X we created an interface to the IBM profiling libraries libmpihpm.a and libmpihpm.smp.a and also to HPCToolkit http://hpctoolkit.org/ (Rice University). We make use of this interface to profile Flash-X evolution only, i.e. not initialization. To use this style of profiling add -unit=monitors/-Profiler/ProfilerMain/hpctoolkit to your setup line and also set the Flash-X runtime parameter profileEvolutionOnly = .true.

For the IBM profiling library (mpihpm) you need to add LIB_MPIHPM and LIB_MPIHPM_SMP macros to your Makefile.h to link Flash-X to the profiling libraries. The actual macro used in the link line depends on whether you setup Flash-X with multithreading support (LIB_MPIHPM for MPI-only Flash-X and LIB_MPIHPM_SMP for multithreaded Flash-X). Example values from sites/miralac1/Makefile.h follow

```
LIB_MPI =
HPM_COUNTERS = /bgsys/drivers/ppcfloor/bgpm/lib/libbgpm.a
LIB_MPIHPM = -L/soft/perftools/hpctw -lmpihpm $(HPM_COUNTERS) $(LIB_MPI)
LIB_MPIHPM_SMP = -L/soft/perftools/hpctw -lmpihpm_smp $(HPM_COUNTERS) $(LIB_MPI)
```

For HPCToolkit you need to set the environmental variable HPCRUN_DELAY_SAMPLING=1 at job launch to enable selective profiling (see the HPCToolkit user guide).

Part VII Tools

VisIt

The developers of Flash-X also highly recommend VisIt, a free parallel interactive visualization package provided by Lawrence Livermore National Laboratory (see https://wci.llnl.gov/codes/visit/). VisIt runs on Unix and PC platforms, and can handle small desktop-size datasets as well as very large parallel datasets in the terascale range. VisIt provides a native reader to import Flash-X2.5 and FLASH-X. Version 1.10 and higher natively support FLASH-X. For VisIt versions 1.8 or less, FLASH-X support can be obtained by installing a tarball patch available at http://flash.uchicago.edu/site/flashcode/user_support/visit/. Full instructions are also available at that site.

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Serial Flash-X Output Comparison Utility (sfocu)

Sfocu (Serial Flash Output Comparison Utility) is mainly used as part of an automated testing suite called flashTest and was introduced in Flash-X version 2.0 as a replacement for focu.

Sfocu is a serial utility which examines two Flash-X checkpoint files and decides whether or not they are "equal" to ensure that any changes made to Flash-X do not adversely affect subsequent simulation output. By "equal", we mean that

- The leaf-block structure matches each leaf block must have the same position and size in both datasets.
- The data arrays in the leaf blocks (dens, pres...) are identical.
- The number of particles are the same, and all floating point particle attributes are identical.

Thus, sfocu ignores information such as the particular numbering of the blocks and particles, the timestamp, the build information, and so on.

Sfocu can read HDF5 and PnetCDF Flash-X checkpoint files. Although sfocu is a serial program, it is able to do comparisons on the output of large parallel simulations. Sfocu has been used on irix, linux, AIX and OSF1.

20.1 Building sfocu

The process is entirely manual, although Makefiles for certain machines have been provided. There are a few compile-time options which you set via the following preprocessor definitions in the Makefile (in the CDEFINES macro):

NO_HDF5 build without HDF5 support

NO_NCDF build without PnetCDF support

NEED_MPI certain parallel versions of HDF5 and all versions of PnetCDF need to be linked with the MPI library. This adds the necessary MPI_Init and MPI_Finalize calls to sfocu. There is no advantage to running sfocu on more than one processor; it will only give you multiple copies of the same report.

20.2 Using sfocu

The basic and most common usage is to run the command sfocu <file1> <file2>. The option -t <dist> allows a distance tolerance in comparing bounding boxes of blocks in two different files to determine which are the same (which have data to compare to one another). You might need to widen your terminal to view the output, since it can be over 80 columns. Sample output follows:

```
A: 2006-04-25/sod_2d_45deg_4lev_ncmpi_chk_0001
A: 2000-04-25/80d_2d_4006g_410V_ncmpi_cnkc_0001
Min Error: inf(2|a-b| / max(|a+b|, 1e-99) )
Max Error: sup(2|a-b| / max(|a+b|, 1e-99) )
Abs Error: sup|a-b| / max(sup|a|, sup|b|, 1e-99)
Block shapes for both files are: [8,8,1]
Mag-error tolerance: ie-12
Total leaf blocks compared: 541 (all other blocks
```

Total leaf blocks compared: 541 (all other blocks are ignored)

	Bad Blocks				Max Error		П		Abs Error	
	! !	İ	П	Error	I A	l B	П	Error	l A	l B
dens		0		1.098e-11				4.661e-12		0.424
eint	502	0	11 :	1.1e-11	1.78	1.78	П	1.956e-11	1.78	1.78
ener	502	0	11 8	8.847e-12	2.21	2.21	П	1.956e-11	2.21	1 2.21
gamc	10	0	11 (0	1 0	I 0	П	0	l 0	I 0
game	10	1 0	11 0	0	1 0	I 0	П	0	l 0	I 0
pres	502	1 0	11:3	1.838e-14	0.302	0.302	П	1.221e-14	0.982	0.982
temp	502	1 0	11:3	1.1e-11	8.56e-09	8.56e-09	П	9.41e-20	8.56e-09	8.56e-09
velx	516	1 0	11.8	5.985	5.62e-17	-1.13e-16	П	2.887e-14	0.657	0.657
vely	516	1 0	11.2	2	l 1e-89	-4.27e-73	П	1.814e-14	0.102	0.102
velz	1 0	1 0	11.0)	0	1 0	П	0	I 0	1 0
	1.0	1.0	11.0	0	1 0	1 0	П	0	I 0	I 0
 Iar	+ +	+ +	11		A	+	++- 		В	+
 Var	+ +	+ +	11		+A	+	++- 		В	+
Var	Bad Blocks	+	11	Sum	A +	+	++- 	Sum	B Max	+ + Min +
Var	Bad Blocks	+		Sum 1.36e+04	A +	+		Sum 1.36e+04	B Max 1	+
Var	Bad Blocks 	Mag Error Mag Error 4.661e-12 6.678e-12		Sum 1.36e+04 7.3e+04	A +	+	++- 	Sum 1.36e+04 7.3e+04	B Max 1 2.93	Min
Var dens eint ener	Bad Blocks 	Mag Error 		Sum 1.36e+04 7.3e+04 8.43e+04	A +	+	++- 	Sum 1.36e+04 7.3e+04 8.43e+04	B Max 1 1 1 2.93 1 3.34	Min 0.125 1.61 2
Var dens eint ener gamc	Bad Blocks 	Mag Error 		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04	A +	+	++- 	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04	B Max 1 1 2.93 3.34 1.4	Min
Var dens eint ener gamc game	Bad Blocks 	Mag Error 		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04	A +	+	++-	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04	B Max 1 1 1 2.93 1 3.34 1 1.4 1 1.4	Min 0.125 1.61 2 1.4 1.4
Var dens eint ener gamc game pres	Bad Blocks 	Mag Error 		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04	A Max 1 1 2.93 1 3.34 1 1.4 1 1 1 1 1	Min 0.125 1.61 2 1.4 1.4	***	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04	B Max 1 2.93 3.34 1.4 1.4 1	Min 0.125 1.61 2 1.4 1.4
Var dens eint ener game game pres temp	Bad Blocks	Mag Error 		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 1.13e+04 0.000351	A	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-09	++-	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04 0.000351	B Max 1 1 2.93 3.34 1.4 1.4 1 1 1.41e-08	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-08
Var dens eint ener game pres temp	Bad Blocks	Mag Error 4.661e-12 6.678e-12 5.858e-12 0 0 1.221e-14 6.678e-12 3.45e-14		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04 0.000351 1.79e+04	A	Min Min 0.125 1.61 2 1.4 1.4 1.4 0.1 7.75e-09 -6.09e-06	***	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04 0.000351 1.79e+04	B Max 1 2 2 93 3 3 4 1 4 1 1 4 1 1 1 4 1 1	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-05 -6.09e-06
Var dens eint ener gamc game pres temp velx	Bad Blocks	Mag Error 4.661e-12 6.678e-12 5.858e-12 0 1.221e-14 6.678e-12 3.45e-14 2.166e-14		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 1.13e+04 0.000351 1.79e+04 1.79e+04	A Max 1 2.93 3.34 1.4 1.4 1 1 1.41e-08 0.837 0.838	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-09 -6.09e-06 -1.96e-06	***	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 1.13e+04 0.000351 1.79e+04 1.79e+04	B Max 1 2.93 3.34 1.4 1 1 1.4 1 1 1.41e-08 0.837 0.838	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-08 -6.09e-06 -1.96e-06
Var dens eint ener game pres temp	Bad Blocks	Mag Error 4.661e-12 6.678e-12 5.858e-12 0 0 1.221e-14 6.678e-12 3.45e-14		Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 1.13e+04 0.000351 1.79e+04 1.79e+04 0	A Max 1 1 2.93 3.34 1.4 1 1 1 1.41e-08 0.837 0.838 0	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-09 -6.09e-06 -1.96e-06	***	Sum 1.36e+04 7.3e+04 8.43e+04 4.85e+04 4.85e+04 1.13e+04 0.000351 1.79e+04 0.79e+04	B Max 1 2.93 3.34 1.4 1.4 1 1.41e-08 0.837 0.838 0	Min 0.125 1.61 2 1.4 1.4 0.1 7.75e-05 -6.09e-06

"Bad Blocks" is the number of leaf blocks where the data was found to differ between datasets. Four different error measures (min/max/abs/mag) are defined in the output above. In addition, the last six columns report the sum, maximum and minimum of the variables in the two files. Note that the sum is physically meaningless, since it is not volume-weighted. Finally, the last line permits other programs to parse the sfocu output easily: when the files are identical, the line will instead read SUCCESS.

It is possible for sfocu to miss machine-precision variations in the data on certain machines because of compiler or library issues, although this has only been observed on one platform, where the compiler produced code that ignored IEEE rules until the right flag was found.

Drift

21.1 Introduction

Drift is a debugging tool added to Flash-X to help catch programming mistakes that occur while refactoring code in a way that *should not* change numerical behavior. Historically, simulation checkpoints have been used to verify that results obtained after a code modification have not affected the numerics. But if changes are observed, then the best a developer can do to narrow the bug hunting search space is to look at pairs of checkpoint files from the two different code bases sequentially. The first pair to compare unequal will tell you that somewhere between that checkpoint and its immediate predecessor something in the code changed the numerics. Therefor, the search space can only be narrowed to the limit allow by the checkpointing interval, which in Flash-X, without clever calls to IO sprinkled about, is at best once per time cycle.

Drift aims to refine that granularity considerably by allowing comparisons to be made upon every modification to a block's contents. To achieve this, drift intercepts calls to <code>Grid_releaseBlkPtr</code>, and inserts into them a step to checksum each of the variables stored on the block. Any checksums that do not match with respect to the last checksums recorded for that block are logged to a text file along with the source file and line number. The developer can then compare two drift logs generated by the different runs using <code>diff</code> to find the first log entry that generates unequal checksums, thus telling the developer which call to <code>Grid_releaseBlkPtr</code> first witnessed divergent values.

The following are example excerpts from two drift logs. Notice the checksum value has changed for variable dens on block 18. This should clue the developer in that the cause of divergent behavior lies somewhere between Eos_wrapped.F90:249 and hy_ppm_sweep.F90:533.

```
inst=2036
                                                       inst=2036
step=1
                                                       step=1
src=Eos_wrapped.F90:249
                                                       src=Eos_wrapped.F90:249
b1k=57
                                                       b1k=57
 dens E8366F6E49DD1B44
                                                        dens E8366F6E49DD1B44
 eint 89D635E5F46E4CE4
                                                        eint 89D635E5F46E4CE4
 ener C6ED4F02E60C9E8F
                                                        ener C6ED4F02E60C9E8F
 pres 6434628E2D2E24E1
                                                        pres 6434628E2D2E24E1
 temp DB675D5AFF7D48B8
                                                        temp DB675D5AFF7D48B8
 velx 42546C82E30F08B3
                                                        velx 42546C82E30F08B3
inst=2100
                                                       inst=2100
step=1
                                                       step=1
src=hy_ppm_sweep.F90:533
                                                       src=hy_ppm_sweep.F90:533
b1k=18
                                                       h1k=18
 dens A462F49FFC3112DE
                                                        dens 5E52D67C5E93FFF1
 eint 9CD79B2E504C7C7E
                                                        eint 9CD79B2E504C7C7E
 ener 4A3E03520C3536B9
                                                        ener 4A3E03520C3536B9
 velx 8193E8C2691A0725
                                                        velx 8193E8C2691A0725
                                                        vely 86C5305CB7DE275E
 vely 86C5305CB7DE275E
```

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21.2 Enabling drift

In Flash-X, drift is disabled by default. Enabling drift is done by hand editing the Simulation.h file generated by the setup process. The directive line #define DRIFT_ENABLE 0 should be changed to #define DRIFT_ENABLE 1. Once this has been changed, a recompilation will be necessary by executing make.

With drift enabled, the Flash-X executable will generate log files in the same directory it is executed in. These files will be named drift.<rank>.log, one for each MPI process.

The following runtime parameters are read by drift to control its behavior:

Parameter	Default	Description
drift_trunc_mantissa	2	The number of least significant mantissa bits to zero
		out before hashing a floating point value. This can be
		used to stop numerical noise from altering checksum
		values.
drift_verbose_inst	0	The instance index at which drift should start logging
		checksums per call to Grid_releaseBlkPtr. Before
		this instance is hit, only user calls to Driver_driftUnk
		will generate log data. A value of zero means never log
		checksums per block. Instance counting is described
		below.
drift_tuples	.false.	A boolean switch indicating if drift should write logs in
		the more human readable "non-tuples" format or the
		machine friendly "tuples" format that can be read in
		by the driftDee script found in the tools/ directory.
		Generally the "non-tuples" format is a better choice
		to use with tools such as diff.

21.3 Typical workflow

Drift has two levels of output verbosity, let us refer to them as verbose and not verbose. When in non-verbose mode, drift will only generate output when directly told to do so through the <code>Driver_driftUnk</code> API call. This call tells drift to generate a checksum for each <code>unk</code> variable over all blocks in the domain and then log those checksums that have changed since the last call to <code>Driver_driftUnk</code>. Verbose mode also generates this information and additionally includes the per-block checksums for every call to <code>Grid_releaseBlkPtr</code>. Verbose mode can generate <code>a lot</code> of log data and so should only be activated when the simulation nears the point at which divergence originates. This is the reason for the <code>drift_verbose_inst</code> runtime parameter.

Drift internally maintains an "instance" counter that is incremented with every intercepted call to Grid_releaseBlkPtr. This is drift's way of enumerating the program states. When comparing two drift logs, if the first checksum discrepancy occurs at instance number 1349 (arbitrary), then it is clear that somewhere between the 1348'th and 1349'th call to Grid_releaseBlkPtr a divergent event occurred.

The suggested workflow once drift is enabled is to first run both simulations with verbose mode off (dirft_verbse_inst=0). The main Driver_evolveFlash implementations have calls to Driver_driftUnk between all calls to Flash-X unit advancement routines. So the default behavior of drift will generate multiple unk-wide checksums for each variable per timestep. These two drift logs should be compared to find the first entry with a mismatched checksum. Each entry generated by Driver_driftUnk will contain an instance range like in the following:

step=1 from=Driver_evolveFlash.F90:276 unks inst=1234 to 2345 dens 9CF3C169A5BB129C eint 9573173C3B51CD12 ener 028A5D0DED1BC399

The line "unks inst=1349 to 2345" informs us these checksums were generated sometime after the 2345'th call to Grid_releaseBlkPtr. Assume this entry is the first such entry to not match checksums with its counterpart. Then we know that somewhere between instance 1234 and 2345 divergence began. So we set drift_verbose_inst = 1234 in the runtime parameters file of each simulation and then run them both again. Now drift will run up to instance 1234 as before, only printing at calls to Driver_driftUnk, but starting with instance 1234 each call to Grid_releaseBlkPtr will induce a per block checksum to be logged as well. Now these two drift files can be compared to find the first difference, and hopefully get you on your way to hunting down the cause of the bug.

21.4 Caveats and Annoyances

The machinery drift uses to intercept calls to <code>Grid_releaseBlkPtr</code> is lacking in sophistication, and as such can put some unwanted constraints on the code base. The technique used is to declare a preprocessor <code>#define</code> in <code>Simulation.h</code> to expand occurrences of <code>Grid_releaseBlkPtr</code> to something larger that includes <code>__FILE__</code> and <code>__LINE__</code>. This is how drift is able to correlate calls to <code>Grid_releaseBlkPtr</code> with the originating line of source code. Unfortunately this technique places a very specific restriction on the code once drift is enabled. The trouble comes from the types of source lines that may refer to a subroutine without calling it. The primary offender being use statements with <code>only</code> clauses listing the module members to import into scope. Because macro expansion is dumb with respect to context, it will expand occurrences of <code>Grid_releaseBlkPtr</code> in these use statements, turning them into syntactic rubbish. The remedy for this issue is to make sure the line <code>#include "Simulation.h"</code> comes after all statements involving <code>Grid_releaseBlkPtr</code> but not calling it, and before all statements that are calls to <code>Grid_releaseBlkPtr</code>. In practice this is quite easy. With only one subroutine per file, there will only be one line like:

```
use Grid\_interface, only: ..., Grid\_releaseBlkPtr, ...
```

and it will come before all calls to Grid_releaseBlkPtr, so just move the #include "Simulation.h" after the use statements. The following is an example:

If such a solution is not possible because no separation between all use and call statements exists, then there are two remaining courses of action to get the source file to compile. One, hide these calls to Grid_releaseBlkPtr from drift by forceably disabling the macro expansion. To do so, just add the line #undef Grid_releaseBlkPtr after #include "Simulation.h". The second option is to carry out the macro expansion by hand. This also requires disabling the macro with the undef just mentioned, but then also rewriting each call to Grid_releaseBlkPtr just as the preprocessor would. Please consult Simulation.h to see the text that gets substituted in for Grid_releaseBlkPtr.