COMSM1201 : Data Structures & Algorithms

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- Let's look at some toy examples to begin with.

```c
1   #include <stdio.h>
2   #include <string.h>
3
4   #define SWAP(A,B) {char temp; temp=A;A=B;B=temp;}
5
6   void strrev(char* s, int n);
7
8   int main(void)
9   {
10      char str[] = "Hello World!";
11      strrev(str, strlen(str));
12      printf("%s\n", str);
13      return 0;
14  }
15
16  /* Iterative Inplace String Reverse */
17  void strrev(char* s, int n)
18  {
19      for(int i=0, j=n-1; i<j; i++, j--){
20          SWAP(s[i], s[j]);
21      }
22  }
```

Execution :

```
!dlroW  olleH
```

Recursion for *strrev()*

```c
#include <stdio.h>
#include <string.h>

#define SWAP(A,B) {char temp; temp=A;A=B;B=temp;}

void strrev(char* s, int start, int end);

int main(void)
{
    char str[] = "Hello World!";
    strrev(str, 0, strlen(str)-1);
    printf("%s\n", str);
    return 0;
}

/* Recursive : Inplace String Reverse */
void strrev(char* s, int start, int end)
{
    if(start >= end){
        return;
    }
    SWAP(s[start], s[end]);
    strrev(s, start+1, end-1);
}
```

Execution :

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- We need to change the function prototype.

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24  }
```

- We need to change the function prototype.
- This allows us to track both the start and the end of the string.

Execution :

!dlroW olleH

The Fibonacci Sequence

A well known example of a recursive
function is the Fibonacci sequence.
The first term is 1, the second term
is 1 and each successive term is
defined to be the sum of the two
previous terms, i.e. :

fib(1) is 1
fib(2) is 1
fib(n) is fib(n-1)+fib(n-2)

1,1,2,3,5,8,13,21, ...

Iterative & Recursive Fibonacci

```c
1    #include <stdio.h>
2
3    #define MAXFIB 24
4
5    int fibonacci(int n);
6
7    int main(void)
8    {
9
10       for(int i=1; i<=MAXFIB; i++){
11           printf("%d = %d\n", i, fibonacci(i));
12       }
13
14       return 0;
15
16   }
17
18   int fibonacci(int n)
19   {
20       if(n <= 2){
21           return 1;
22       }
23       int a = 1;
24       int b = 1;
25       int next;
26       for(int i=3; i<=n; i++){
27           next = a + b;
28           a = b;
29           b = next;
30       }
31       return b;
32   }
```

Iterative & Recursive Fibonacci

```c
#include <stdio.h>

#define MAXFIB 24

int fibonacci(int n);

int main(void)
{

    for(int i=1; i<=MAXFIB; i++){
        printf("%d = %d\n", i, fibonacci(i));
    }

    return 0;

}

int fibonacci(int n)
{
    if(n <= 2){
        return 1;
    }
    int a = 1;
    int b = 1;
    int next;
    for(int i=3; i<=n; i++){
        next = a + b;
        a = b;
        b = next;
    }
    return b;
}
```

Execution :

```
1  = 1
2  = 1
3  = 2
4  = 3
5  = 5
6  = 8
7  = 13
8  = 21
9  = 34
10 = 55
11 = 89
12 = 144
13 = 233
14 = 377
15 = 610
16 = 987
17 = 1597
18 = 2584
19 = 4181
20 = 6765
21 = 10946
22 = 17711
23 = 28657
24 = 46368
```

Iterative & Recursive Fibonacci

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10      for(int i=1; i<=MAXFIB; i++){
11          printf("%d = %d\n", i, fibonacci(i));
12      }
13
14      return 0;
15
16  }
17
18  int fibonacci(int n)
19  {
20      if(n == 1) return 1;
21      if(n == 2) return 1;
22      return( fibonacci(n-1)+fibonacci(n-2));
23  }
```

Iterative & Recursive Fibonacci

```c
#include <stdio.h>

#define MAXFIB 24

int fibonacci(int n);

int main(void)
{

    for(int i=1; i<=MAXFIB; i++){
        printf("%d = %d\n", i, fibonacci(i));
    }

    return 0;

}

int fibonacci(int n)
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    if(n == 1) return 1;
    if(n == 2) return 1;
    return( fibonacci(n-1)+fibonacci(n-2));
}
```

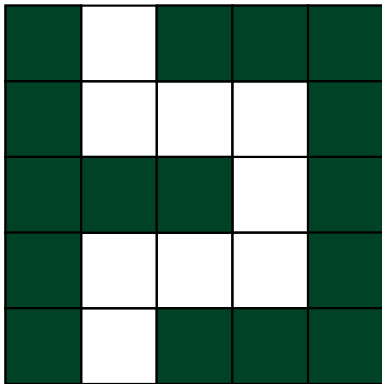It's interesting to see how run-time increases as the length of the sequence is raised.
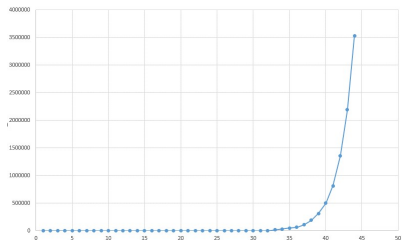
Maze Escape

The correct route through a maze can be obtained via recursive, rather than iterative, methods.
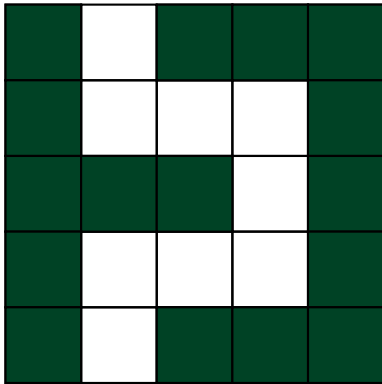
Maze Escape

The correct route through a maze can be obtained via recursive, rather than iterative, methods.


```
bool explore(int x, int y, char mz[YS][XS])
{
  if  mz[y][x] is exit return true;

  Mark mz[y][x] so we don't return here

  if we can go up :
    if(explore(x, y+1, mz)) return true

  if we can go right :
    if(explore(x+1, y, mz)) return true

  Do left & down in a similar manner

  return false; // Failed to find route
}
```

Permuting

- Here we consider the ways to permute a string (or more generally an array)

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- Permutations are all possible ways of rearranging the positions of the characters.

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  CBA
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Execution :

ABC
ACB
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CAB

```c
1   // From e.g.  http://www.geeksforgeeks.org
2   #include <stdio.h>
3   #include <string.h>
4
5   #define SWAP(A,B) {char temp = *A; *A = *B; *B = temp;}
6
7   void permute(char* a, int s, int e);
8
9   int main()
10  {
11      char str[] = "ABC";
12      int n = strlen(str);
13      permute(str, 0, n-1);
14      return 0;
15  }
16
17  void permute(char* a, int s, int e)
18  {
19      if (s == e){
20        printf("%s\n", a);
21        return;
22      }
23      for (int i = s; i <= e; i++){
24        SWAP((a+s), (a+i)); // Bring one char to the front
25        permute(a, s+1, e);
26        SWAP((a+s), (a+i)); // Backtrack
27      }
28  }
```

Self-test : Power

- Raising a number to a power $n = 2^5$ is the same as multiple multiplications $n = 2*2*2*2*2$.

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- Or, thinking recursively, n = 2 * (2^4).

```
1   /* Try to write power(a,b) to computer a^b
2      without using any maths functions other than
3      multiplication :
4      Try (1) iterative then (2) recursive
5      (3) Trick that for n%2==0, x^n = x^(n/2)*x^(n/2)
6
7   */
8
9   #include <stdio.h>
10
11  int power(unsigned int a, unsigned int b);
12
13  int main(void)
14  {
15
16      int x = 2;
17      int y = 16;
18
19      printf("%d^%d = %d\n", x, y, power(x,y));
20
21  }
22
23  int power(unsigned int a, unsigned int b)
24  {
25  }
```

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- The need to search an array for a particular value is a common problem.

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- The simplest method for searching is called the sequential search.
- Simply move through the array from beginning to end, stopping when you have found the value you require.

```c
1    #include <stdio.h>
2    #include <string.h>
3    #include <assert.h>
4
5    #define NOTFOUND -1
6    #define NUMPEOPLE 6
7    typedef struct person{
8          char* name; int age;
9    } person;
10
11   int findAge(const char* name, const person* p, int n);
12
13   int main(void)
14   {
15       person ppl[NUMPEOPLE] = { {"Ackerby", 21}, {"Bloggs", 25},
16                   {"Chumley", 26}, {"Dalton",   25},
17                   {"Eggson", 22}, {"Fulton",  41} };
18
19       assert(findAge("Eggson",   ppl, NUMPEOPLE)==22);
20       assert(findAge("Campbell", ppl, NUMPEOPLE)==NOTFOUND);
21       return 0;
22   }
23
24   int findAge(const char* name, const person* p, int n)
25   {
26       for(int j=0; j<n; j++){
27           if(strcmp(name, p[j].name) == 0){
28               return p[j].age;
29           }
30       }
31       return NOTFOUND;
32   }
```

Sequential Search

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```
1   #include <stdio.h>
2   #include <string.h>
3   #include <assert.h>
4
5   #define NOTFOUND -1
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7   typedef struct person{
8           char* name; int age;
9   } person;
10
11  int findAge(const char* name, const person* p, int n);
12
13  int main(void)
14  {
15      person ppl[NUMPEOPLE] = { {"Ackerby", 21}, {"Bloggs", 25},
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18
19      assert(findAge("Eggson",   ppl, NUMPEOPLE)==22);
20      assert(findAge("Campbell", ppl, NUMPEOPLE)==NOTFOUND);
21      return 0;
22  }
23
24  int findAge(const char* name, const person* p, int n)
25  {
26      for(int j=0; j<n; j++){
27          int m = strcmp(name, p[j].name);
28          if(m == 0) // Braces!
29              return p[j].age;
30          if(m < 0)
31              return NOTFOUND;
32      }
33      return NOTFOUND;
34  }
```

Binary Search for *101*
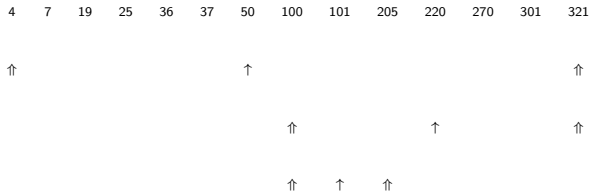
- Searching small lists doesn't require much computation time.

| 4 | 7 | 19 | 25 | 36 | 37 | 50 | 100 | 101 | 205 | 220 | 270 | 301 | 321 |

⇑   ↑   ⇑

               ⇑   ↑   ⇑

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Binary Search for *101*

- Searching small lists doesn't require much computation time.
- However, as lists get longer (e.g. phone directories), sequential searching becomes extremely inefficient.

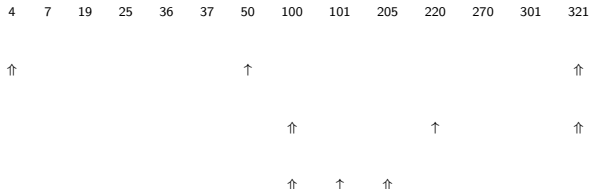| 4	7	19	25	36	37	50	100	101	205	220	270	301	321

⇑   ↑   ⇑

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Binary Search for *101*

- Searching small lists doesn't require much computation time.
- However, as lists get longer (e.g. phone directories), sequential searching becomes extremely inefficient.
- A binary search consists of examining the middle element of the array to see if it has the desired value. If not, then half the array may be discarded for the next search.

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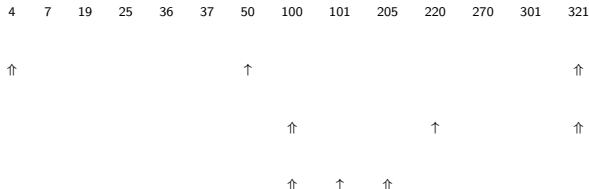
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⇑						↑							⇑
					⇑			↑					⇑
				⇑	↑	⇑							

```c
#include <stdio.h>
#include <stdlib.h>
#include <assert.h>
#include <time.h>
#define NMBRS 1000000

int bin_it(int k, const int* a, int l, int r);

int main(void)
{
    int a[NMBRS];
    srand(time(NULL));

    // Put even numbers into array
    for(int i=0; i<NMBRS; i++){
        a[i] = 2*i;
    }

    // Do many searches for a random number
    for(int i=0; i<10*NMBRS; i++){
        int n = rand()%NMBRS;
        if((n%2) == 0){
            assert(bin_it(n, a, 0, NMBRS-1) == n/2);
        }
        else{ // No odd numbers in this list
            assert(bin_it(n, a, 0, NMBRS-1) < 0);
        }
    }
    return 0;
}
```

Iterative v. Recursion Binary Search

```
int bin_it(int k, const int* a, int l, int r)
{
    while(l <= r){
        int m = (l+r)/2;
        if(k == a[m]){
            return m;
        }
        else{
            if (k > a[m]){
                l = m + 1;
            }
            else{
                r = m - 1;
            }
        }
    }
    return -1;
}
```

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```
int bin_it(int k, const int* a, int l, int r)
{
    while(l <= r){
        int m = (l+r)/2;
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            return m;
        }
        else{
            if (k > a[m]){
                l = m + 1;
            }
            else{
                r = m - 1;
            }
        }
    }
    return -1;
}
```

```
int bin_rec(int k, const int* a, int l, int r)
{
    if(l > r) return -1;
    int m = (l+r)/2;
    if(k == a[m]){
        return m;
    }
    else{
        if (k > a[m]){
            return bin_rec(k, a, m+1, r);
        }
        else{
            return bin_rec(k, a, l, m-1);
        }
    }
}
```

Interpolation Search

- When we look for a word in a dictionary, we don't start in the middle. We make an educated guess as to where to start based on the 1st letter of the word being searched for.

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- This idea led to the interpolation search.
- In binary searching, we simply used the middle of an ordered list as a best guess as to where to begin the search.
- Now we use an interpolation involving the key, the start of the list and the end.

$$i = (k - l[0])/(l[n-1] - l[0]) * n$$

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- when searching for '15' :

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- Now we use an interpolation involving the key, the start of the list and the end.

$$i = (k - l[0])/(l[n-1] - l[0]) * n$$

- when searching for '15' :

0	4	5	9	10	12	15	20

⇑

```c
int interp(int k, const int* a, int l, int r)
{

    int m;
    double md;

    while(l <= r){
        md = ((double)(k-a[l])/
              (double)(a[r]-a[l])*
              (double)(r-l)
              )
              +(double)(l);
        m = 0.5 + md;
        if((m > r) || (m < l)){
            return -1;
        }
        if(k == a[m])
            return m;
        else{
            if (k > a[m]){
                l = m + 1;
            }
            else{
                r = m- 1;
            }
        }
    }
}
```

Algorithmic Complexity

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1   #include <stdio.h>
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- We'll discuss the dream of a **O(1)** search later in "Hashing".

Binary vs. Interpolation Timing

```c
1   #include <stdio.h>
2   #include <stdlib.h>
3   #include <assert.h>
4   #include <time.h>
5
6   int bin_it(int k, const int *a, int l, int r);
7   int bin_rec(int k, const int *a, int l, int r);
8   int interp(int k, const int *a, int l, int r);
9   int* parse_args(int argc, char* argv[], int* n, int* srch);
10
11  int main(int argc, char* argv[])
12  {
13
14      int i, n, srch;
15      int* a;
16      int (*p[3])(int k, const int*a, int l, int r) =
17          {bin_it, bin_rec, interp};
18
19      a = parse_args(argc, argv, &n, &srch);
20
21      srand(time(NULL));
22      for(i=0; i<n; i++){
23          a[i] = 2*i;
24      }
25      for(i=0; i<5000000; i++){
26          assert((*p[srch])(a[rand()%n], a, 0, n-1) >= 0);
27      }
28
29      free(a);
30      return 0;
31
32  }
```

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Execution :

```
Binary Search : Iterative
n =     100000 = 0.57
n =     800000 = 0.84
n =    6400000 = 2.20
n =   51200000 = 3.87
Binary Search : Recursive
n =     100000 = 1.23
n =     800000 = 1.79
n =    6400000 = 3.20
n =   51200000 = 4.85
Interpolation
n =     100000 = 0.20
n =     800000 = 0.28
n =    6400000 = 0.50
n =   51200000 = 0.70
```

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- To create linked data representations we use pointers to connect separate blocks of storage together. If a given block contains a pointer to a second block, we can follow this pointer there.
- By following pointers one after another, we can travel right along the structure.

```c
#include <stdio.h>
#include <stdlib.h>
#include "general.h"

typedef struct data{
    int i;
    struct data* next;
} Data;

Data* allocateData(int i);
void printList(Data* l);

int main(void)
{
    int i;
    Data* start, *current;
    start = current = NULL;
    printf("Enter the first number: ");
    if(scanf("%i", &i) == 1){
        start = current = allocateData(i);
    }
    else{
        on_error("Couldn't read an int");
    }

    printf("Enter more numbers: ");
    while(scanf("%i", &i) == 1){
        current->next = allocateData(i);
        current = current->next;
    }
    printList(start);
    // Should Free List
    return 0;
}
```

```
Data* allocateData(int i)
{
    Data* p;
    p = (Data*) ncalloc(1, sizeof(Data));
    p->i = i;
    // Not really required
    p->next = NULL;
    return p;
}

void printList(Data* l)
{
    printf("\n");
    do{
        printf("Number : %i\n", l->i);
        l = l->next;
    }while(l != NULL);
    printf("END\n");
}
```

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void printList(Data* l)
{
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    do{
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        l = l->next;
    }while(l != NULL);
    printf("END\n");
}
```

Searching and Recursive printing:

```c
Data* inList(Data* n, int i)
{
    do{
        if(n->i==i){
            return n;
        }
        n = n->next;
    }while(n != NULL);
    return NULL;
}

void printList_r(Data* l)
{
    // Recursive Base-Case
    if(l == NULL) return;

    printf("Number: %i\n", l->i);
    printList_r(l->next);
}
```

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- The user of the ADT doesn't need to understand how the data is being stored (e.g. array vs. linked lists etc.)

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- Some collections allow duplicate elements and others do not (e.g. Sets).
- Some are ordered (for faster searching) and others unordered.
- Our Collection will be unsorted and will allow duplicates.

```c
1   #include "../General/general.h"
2
3   typedef int colltype;
4
5   typedef struct coll coll;
6
7   #include <stdio.h>
8   #include <stdlib.h>
9   #include <assert.h>
10
11  // Create an empty coll
12  coll* coll_init(void);
13  // Add element onto top
14  void coll_add(coll* c, colltype i);
15  // Take element out
16  bool coll_remove(coll* c, colltype d);
17  // Does this exist ?
18  bool coll_isin(coll* c, colltype i);
19  // Return size of coll
20  int coll_size(coll* c);
21  // Clears all space used
22  bool coll_free(coll* c);
```

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Fixed/specific.h:

```
1    #pragma once
2
3    #define COLLTYPE "Fixed"
4
5    #define FIXEDSIZE 5000
6    struct coll {
7        // Underlying array
8        colltype a[FIXEDSIZE];
9        int size;
10   };
```

Collection ADT using a Fixed-size Array

Fixed/fixed.c:

```c
1   #include "../coll.h"
2   #include "specific.h"
3
4   coll* coll_init(void)
5   {
6       coll* c = (coll*) ncalloc(1, sizeof(coll));
7       c->size = 0;
8       return c;
9   }
10
11  int coll_size(coll* c)
12  {
13      if(c==NULL){
14          return 0;
15      }
16      return c->size;
17  }
18
19  bool coll_isin(coll* c, colltype d)
20  {
21      for(int i=0; i<coll_size(c); i++){
22          if(c->a[i] == d){
23              return true;
24          }
25      }
26      return false;
27  }
```

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23               return true;
24           }
25       }
26       return false;
27   }
```

```
void coll_add(coll* c, colltype d)
{
    if(c){
        if(c->size >= FIXEDSIZE){
            on_error("Collection overflow");
        }
        c->a[c->size] = d;
        c->size = c->size + 1;
    }
}

bool coll_remove(coll* c, colltype d)
{
    for(int i=0; i<coll_size(c); i++){
        if(c->a[i] == d){
            // Shuffle end of array left one
            for(int j=i; j<coll_size(c); j++){
                c->a[j] = c->a[j+1];
            }
            c->size = c->size - 1;
            return true;
        }
    }
    return false;
}

bool coll_free(coll* c)
{
    free(c);
    return true;
}
```

Collection ADT via an Array (Realloc)

Realloc/specific.h:

```
1   #pragma once
2
3   #define COLLTYPE "Realloc"
4
5   #define FIXEDSIZE 16
6   #define SCALEFACTOR 2
7   struct coll {
8       // Underlying array
9       colltype* a;
10      int size;
11      int capacity;
12  };
```

Collection ADT via an Array (Realloc)

Realloc/specific.h:

```
1    #pragma once
2
3    #define COLLTYPE "Realloc"
4
5    #define FIXEDSIZE 16
6    #define SCALEFACTOR 2
7    struct coll {
8        // Underlying array
9        colltype* a;
10       int size;
11       int capacity;
12   };
```

Realloc/realloc.c:

```
1    #include "../coll.h"
2    #include "specific.h"
3
4    coll* coll_init(void)
5    {
6        coll* c = (coll*) ncalloc(1, sizeof(coll));
7        c->a = (colltype*) ncalloc(FIXEDSIZE, sizeof(colltype));
8        c->size = 0;
9        c->capacity= FIXEDSIZE;
10       return c;
11   }
12
13   void coll_add(coll* c, colltype d)
14   {
15       if(c){
16           if(c->size >= c->capacity){
17               c->a = (colltype*) nremalloc(c->a,
18                       sizeof(colltype)*c->capacity*SCALEFACTOR);
19               c->capacity = c->capacity*SCALEFACTOR;
20           }
21           c->a[c->size] = d;
22           c->size = c->size + 1;
23       }
```

Linked/specific.h:

```
1    #pragma once
2
3    #define COLLTYPE "Linked"
4
5    struct dataframe {
6        colltype i;
7        struct dataframe* next;
8    };
9    typedef struct dataframe dataframe;
10
11   struct coll {
12       // Underlying array
13       dataframe* start;
14       int size;
15   };
```

Collection ADT via a Linked List

Linked/specific.h:

```
1   #pragma once
2
3   #define COLLTYPE "Linked"
4
5   struct dataframe {
6       colltype i;
7       struct dataframe* next;
8   };
9   typedef struct dataframe dataframe;
10
11  struct coll {
12      // Underlying array
13      dataframe* start;
14      int size;
15  };
```

Linked/linked.c:

```
#include "../coll.h"
#include "specific.h"

coll* coll_init(void)
{
    coll* c = (coll*) ncalloc(1, sizeof(coll));
    return c;
}

int coll_size(coll* c)
{
    if(c==NULL){
        return 0;
    }
    return c->size;
}

bool coll_isin(coll* c, colltype d)
{
    if(c == NULL || c->start==NULL){
        return false;
    }
    dataframe* f = c->start;
    do{
        if(f->i == d){
            return true;
        }
        f = f->next;
    }while(f != NULL);
    return false;
}
```

Collection ADT via a Linked List II

```c
void coll_add(coll* c, colltype d)
{
    if(c){
        dataframe* f = ncalloc(1, sizeof(dataframe));
        f->i = d;
        f->next = c->start;
        c->start = f;
        c->size = c->size + 1;
    }

}

bool coll_free(coll* c)
{
    if(c){
        dataframe* tmp;
        dataframe* p = c->start;
        while(p!=NULL){
            tmp = p->next;
            free(p);
            p = tmp;
        }
        free(c);
    }
    return true;
}
```

```c
void coll_add ( coll* c , colltype d)
{
    if(c){
        dataframe* f = ncalloc(1, sizeof(dataframe));
        f->i = d;
        f->next = c->start;
        c->start = f;
        c->size = c->size + 1;
    }

}

bool coll_free ( coll* c)
{
    if(c){
        dataframe* tmp;
        dataframe* p = c->start;
        while(p!=NULL){
            tmp = p->next;
            free(p);
            p = tmp;
        }
        free(c);
    }
    return true;
}
```

```c
bool coll_remove ( coll* c , colltype d)
{
    dataframe* f1 , *f2;
    if((c==NULL) || (c->start==NULL)){
        return false;
    }

    // If Front
    if(c->start->i == d){
        f1 = c->start->next;
        free(c->start);
        c->start = f1;
        c->size = c->size - 1;
        return true;
    }

    f1 = c->start;
    f2 = c->start->next;
    do{
        if(f2->i == d){
            f1->next = f2->next;
            free(f2);
            c->size = c->size - 1;
            return true;
        }
        f1 = f2;
        f2 = f1->next;
    }while(f2 != NULL);
    return false;
}
```

Collection Summary

- Any code using the ADT can be compiled
  against any of the implementations,
  e.g. the test (testcoll.c) code.

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- Any code using the ADT can be compiled against any of the implementations, e.g. the test (testcoll.c) code.
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    - Fixed Array : Simple to implement - can't avoid the problems of it being a fixed-size. Deletion expensive.

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  - Fixed Array : Simple to implement - can't avoid the problems of it being a fixed-size. Deletion expensive.
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  - Linked : Slightly fiddly implementation - fast to delete an element.

Task	Fixed Array	Realloc Array	Linked List
Insert new element	O(1) at end *if space*	O(1) at end *but realloc()*	O(1) at front
Search for an element	O(n) *brute force*	O(n) *brute force*	O(n) *brute force*
Search + delete	O(n) + O(n) *move left*	O(n) + O(n) *move left*	O(n) + O(1) *delete 'free'*

- If we had ordered our ADT (ie. the elements were sorted), then the searches could be via a binary / interpolation search, leading to O(log n) or O(log log n) search times.

ADTs Making Coding Simpler

That Linked List code from the previous
Chapter again:

ADTs Making Coding Simpler

That Linked List code from the previous
Chapter again:

```c
1   #include "coll.h"
2   #include "Fixed/specific.h"
3
4   int main(void)
5   {
6       coll* c;
7       int i;
8
9       printf("Please type some numbers :");
10      c = coll_init();
11      while(scanf("%i", &i) == 1){
12          coll_add(c, i);
13      }
14      // Do print etc.
15      coll_free(c);
16      return 0;
17  }
```
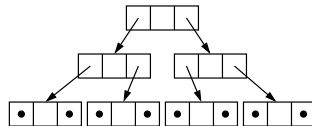
Table of Contents

ADTs

At the highest level of abstraction, ADTs that
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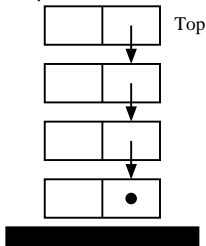- Stacks
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- Sets
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Binary Trees:

Unidirectional Graph:
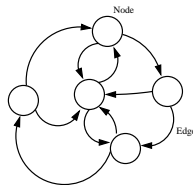
Stacks

The push-down stack:
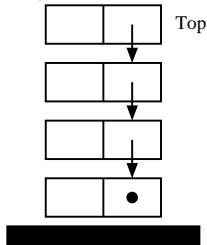
Stacks

The push-down stack:

LIFO (Last in, First out):
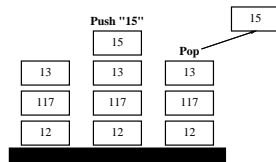
- Operations include push and pop.

Stacks

The push-down stack:
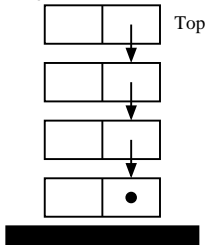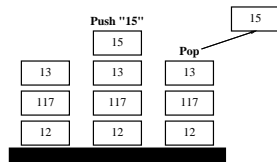
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- Operations include push and pop.
- In the C run-time system, function calls are implemented using stacks.
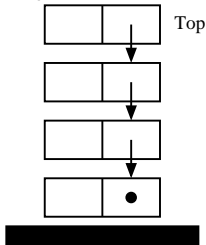
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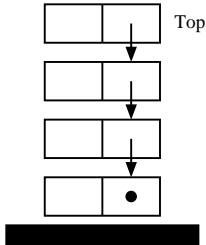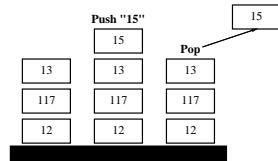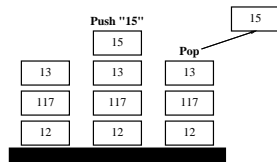

LIFO (Last in, First out):

- Operations include push and pop.
- In the C run-time system, function calls are implemented using stacks.
- Most recursive algorithms can be re-written using stacks instead.

Stacks

The push-down stack:

LIFO (Last in, First out):

- Operations include push and pop.
- In the C run-time system, function calls are implemented using stacks.
- Most recursive algorithms can be re-written using stacks instead.
- But, once again, we are faced with the question : How best to implement such a data type ?

ADT:Stacks Arrays (Realloc) I

stack.h:

```c
1    #pragma once
2
3    #include "../General/general.h"
4
5    typedef int stacktype;
6
7    typedef struct stack stack;
8
9    #include <stdio.h>
10   #include <stdlib.h>
11   #include <assert.h>
12   #include <string.h>
13
14   /* Create an empty stack */
15   stack* stack_init(void);
16   /* Add element to top */
17   void stack_push(stack* s, stacktype i);
18   /* Take element from top */
19   bool stack_pop(stack* s, stacktype* d);
20   /* Clears all space used */
21   bool stack_free(stack* s);
22
23   /* Optional? */
24
25   /* Copy top element into d (but don't pop it) */
26   bool stack_peek(stack*s,  stacktype* d);
27   /* Make a string version - keep .dot in mind */
28   void stack_tostring(stack*, char* str);
```

stack.h:

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1   #pragma once
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3   #include "../General/general.h"
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14  /* Create an empty stack */
15  stack* stack_init(void);
16  /* Add element to top */
17  void stack_push(stack* s, stacktype i);
18  /* Take element from top */
19  bool stack_pop(stack* s, stacktype* d);
20  /* Clears all space used */
21  bool stack_free(stack* s);
22
23  /* Optional? */
24
25  /* Copy top element into d (but don't pop it) */
26  bool stack_peek(stack*s,  stacktype* d);
27  /* Make a string version - keep .dot in mind */
28  void stack_tostring(stack*, char* str);
```

Realloc/specific.h:

```
1   #pragma once
2
3   #define FORMATSTR "%i"
4   #define ELEMSIZE 20
5
6   #define STACKTYPE "Realloc"
7
8   #define FIXEDSIZE 16
9   #define SCALEFACTOR 2
10
11  struct stack {
12      /* Underlying array */
13      stacktype* a;
14      int size;
15      int capacity;
16  };
```

ADT:Stacks Arrays (Realloc) II

Realloc/realloc.c

```c
1   #include "../stack.h"
2   #include "specific.h"
3
4   #define DOTFILE 5000
5
6   stack* stack_init(void)
7   {
8       stack *s = (stack*) ncalloc(1, sizeof(stack));
9       /* Some implementations would allow you to pass
10          a hint about the initial size of the stack */
11      s->a = (stacktype*) ncalloc(FIXEDSIZE, sizeof(stacktype));
12      s->size = 0;
13      s->capacity= FIXEDSIZE;
14      return s;
15  }
16
17  void stack_push(stack* s, stacktype d)
18  {
19      if(s==NULL){
20          return;
21      }
22      if(s->size >= s->capacity){
23          s->a = (stacktype*) nremalloc(s->a,
24                  sizeof(stacktype)*s->capacity*SCALEFACTOR);
25          s->capacity = s->capacity*SCALEFACTOR;
26      }
27      s->a[s->size] = d;
28      s->size = s->size + 1;
29  }
```

Realloc/realloc.c

```c
#include "../stack.h"
#include "specific.h"

#define DOTFILE 5000

stack* stack_init(void)
{
    stack *s = (stack*) ncalloc(1, sizeof(stack));
    /* Some implementations would allow you to pass
       a hint about the initial size of the stack */
    s->a = (stacktype*) ncalloc(FIXEDSIZE, sizeof(stacktype));
    s->size = 0;
    s->capacity= FIXEDSIZE;
    return s;
}

void stack_push(stack* s, stacktype d)
{
    if(s==NULL){
        return;
    }
    if(s->size >= s->capacity){
        s->a = (stacktype*) nremalloc(s->a,
                sizeof(stacktype)*s->capacity*SCALEFACTOR);
        s->capacity = s->capacity*SCALEFACTOR;
    }
    s->a[s->size] = d;
    s->size = s->size + 1;
}
```

```c
bool stack_pop(stack* s, stacktype* d)
{
    if((s == NULL) || (s->size < 1)){
        return false;
    }
    s->size = s->size - 1;
    *d = s->a[s->size];
    return true;
}

bool stack_peek(stack* s, stacktype* d)
{
    if((s==NULL) || (s->size <= 0)){
        /* Stack is Empty */
        return false;
    }
    *d = s->a[s->size-1];
    return true;
}
```

ADT:Stacks Arrays (Realloc) III

Realloc/realloc.c

```
1    void stack_tostring(stack* s, char* str)
2    {
3        char tmp[ELEMSIZE];
4        str[0] = '\0';
5        if((s==NULL) || (s->size <1)){
6            return;
7        }
8        for(int i=s->size-1; i>=0; i--){
9            sprintf(tmp, FORMATSTR, s->a[i]);
10           strcat(str, tmp);
11           strcat(str, "|");
12       }
13       str[strlen(str)-1] = '\0';
14   }
15
16   bool stack_free(stack* s)
17   {
18       if(s==NULL){
19           return true;
20       }
21       free(s->a);
22       free(s);
23       return true;
24   }
```

ADT:Stacks Arrays (Realloc) III

Realloc/realloc.c

```c
1    void stack_tostring(stack* s, char* str)
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3        char tmp[ELEMSIZE];
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6            return;
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9            sprintf(tmp, FORMATSTR, s->a[i]);
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12       }
13       str[strlen(str)-1] = '\0';
14   }
15
16   bool stack_free(stack* s)
17   {
18       if(s==NULL){
19           return true;
20       }
21       free(s->a);
22       free(s);
23       return true;
24   }
```

- We need a thorough testing program teststack.c

Realloc/realloc.c

```
1   void stack_tostring(stack* s, char* str)
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3       char tmp[ELEMSIZE];
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6           return;
7       }
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17  {
18      if(s==NULL){
19          return true;
20      }
21      free(s->a);
22      free(s);
23      return true;
24  }
```

- We need a thorough testing program teststack.c
- See also revstr.c : a version of the string reverse code (for which we already seen an iterative (in-place) and a recursive solution).

Linked/specific.h

```
1    #pragma once
2
3    #define FORMATSTR "%i"
4    #define ELEMSIZE 20
5    #define STACKTYPE "Linked"
6
7    struct dataframe {
8        stacktype i;
9        struct dataframe* next;
10   };
11   typedef struct dataframe dataframe;
12
13   struct stack {
14       /* Underlying array */
15       dataframe* start;
16       int size;
17   };
```

Linked/specific.h

```
1    #pragma once
2
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12
13   struct stack {
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15       dataframe* start;
16       int size;
17   };
```

Linked/linked.c

```
1    #include "../stack.h"
2    #include "specific.h"
3
4    #define DOTFILE 5000
5
6    stack* stack_init(void)
7    {
8        stack* s = (stack*) ncalloc(1, sizeof(stack));
9        return s;
10   }
11
12   void stack_push(stack* s, stacktype d)
13   {
14       if(s){
15           dataframe* f = ncalloc(1, sizeof(dataframe));
16           f->i = d;
17           f->next = s->start;
18           s->start = f;
19           s->size = s->size + 1;
20       }
21   }
```

```
1    bool stack_pop(stack* s, stacktype* d)
2    {
3        if((s==NULL) || (s->start==NULL)){
4            return false;
5        }
6
7        dataframe* f = s->start->next;
8        *d = s->start->i;
9        free(s->start);
10       s->start = f;
11       s->size = s->size - 1;
12       return true;
13   }
14
15   bool stack_peek(stack* s, stacktype* d)
16   {
17       if((s==NULL) || (s->start==NULL)){
18           return false;
19       }
20       *d = s->start->i;
21       return true;
22   }
```

ADT:Stacks Linked II

```
1    bool stack_pop(stack* s, stacktype* d)
2    {
3        if((s==NULL) || (s->start==NULL)){
4            return false;
5        }
6
7        dataframe* f = s->start->next;
8        *d = s->start->i;
9        free(s->start);
10       s->start = f;
11       s->size = s->size - 1;
12       return true;
13   }
14
15   bool stack_peek(stack* s, stacktype* d)
16   {
17       if((s==NULL) || (s->start==NULL)){
18           return false;
19       }
20       *d = s->start->i;
21       return true;
22   }
```

```
1    void stack_tostring(stack* s, char* str)
2    {
3        char tmp[ELEMSIZE];
4        str[0] = '\0';
5        if((s==NULL) || (s->size <1)){
6            return;
7        }
8        dataframe* p = s->start;
9        while(p){
10           sprintf(tmp, FORMATSTR, p->i);
11           strcat(str, tmp);
12           strcat(str, "|");
13           p = p->next;
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15       str[strlen(str)-1] = '\0';
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19   {
20       if(s){
21           dataframe* p = s->start;
22           while(p!=NULL){
23               dataframe* tmp = p->next;
24               free(p);
25               p = tmp;
26           }
27           free(s);
28       }
29       return true;
30   }
```
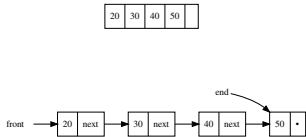
Table of Contents

ADTs : Queues

FIFO (First in, First out):

- Intuitively more "useful" than a stack.

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- Operations include enqueue, dequeue and size.

queue.h

```c
1   #pragma once
2
3   #include "../General/general.h"
4
5   typedef int queuetype;
6
7   typedef struct queue queue;
8
9   #include <stdio.h>
10  #include <stdlib.h>
11  #include <string.h>
12  #include <assert.h>
13
14  /* Create an empty queue */
15  queue* queue_init(void);
16  /* Add element on end */
17  void queue_enqueue(queue* q, queuetype v);
18  /* Take element off front */
19  bool queue_dequeue(queue* q, queuetype* d);
20  /* Return size of queue */
21  int queue_size(queue* q);
22  /* Clears all space used */
23  bool queue_free(queue* q);
24
25  /* Helps with visualisation & testing */
26  void queue_tostring(queue* q, char* str);
```

ADTs : Queues (Fixed) I
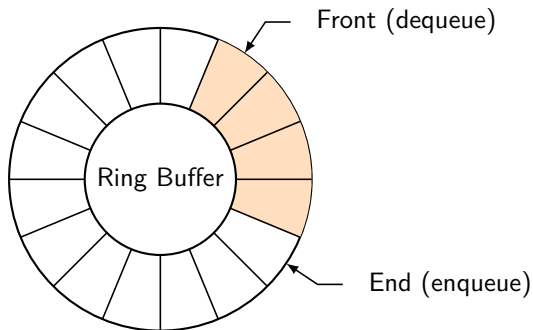
specific.h

```
1    #pragma once
2
3    #define FORMATSTR "%d"
4    #define ELEMSIZE 20
5
6    #define QUEUETYPE "Fixed"
7
8    #define BOUNDED 5000
9
10   struct queue {
11       /* Underlying array */
12       queuetype a[BOUNDED];
13       int front;
14       int end;
15   };
16
17   #define DOTFILE 5000
```

specific.h

```
1   #pragma once
2
3   #define FORMATSTR "%d"
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16
17  #define DOTFILE 5000
```


Front (dequeue)

Ring Buffer

End (enqueue)

fixed.c

```
1   #include "../queue.h"
2   #include "specific.h"
3
4   void _inc(queuetype* p);
5
6   queue* queue_init(void)
7   {
8       queue* q = (queue*) ncalloc(1, sizeof(queue));
9       return q;
10  }
11
12
13  void queue_enqueue(queue* q, queuetype d)
14  {
15      if(q){
16          q->a[q->end] = d;
17          _inc(&q->end);
18          if(q->end == q->front){
19              on_error("Queue too large");
20          }
21      }
22  }
```

fixed.c

```
1   #include "../queue.h"
2   #include "specific.h"
3
4   void _inc(queuetype* p);
5
6   queue* queue_init(void)
7   {
8       queue* q = (queue*) ncalloc(1, sizeof(queue));
9       return q;
10  }
11
12
13  void queue_enqueue(queue* q, queuetype d)
14  {
15      if(q){
16          q->a[q->end] = d;
17          _inc(&q->end);
18          if(q->end == q->front){
19              on_error("Queue too large");
20          }
21      }
22  }
```

```
1   bool queue_dequeue(queue* q, queuetype* d)
2   {
3       if((q==NULL) || (q->front==q->end)){
4           return false;
5       }
6       *d = q->a[q->front];
7       _inc(&q->front);
8       return true;
9   }
10
11  void queue_tostring(queue* q, char* str)
12  {
13      char tmp[ELEMSIZE];
14      str[0] = '\0';
15      if((q==NULL) || (queue_size(q)==0)){
16          return;
17      }
18      for(int i=q->front; i != q->end;){
19          sprintf(tmp, FORMATSTR, q->a[i]);
20          strcat(str, tmp);
21          strcat(str, "|");
22          _inc(&i);
23      }
24      str[strlen(str)-1] = '\0';
25  }
```

```
1    int queue_size(queue* q)
2    {
3        if(q==NULL){
4            return 0;
5        }
6        if(q->end >= q->front){
7            return q->end-q->front;
8        }
9        return q->end + BOUNDED - q->front;
10   }
11
12   bool queue_free(queue* q)
13   {
14       free(q);
15       return true;
16   }
17
18   void _inc(queuetype* p)
19   {
20       *p = (*p + 1) % BOUNDED;
21   }
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1    int queue_size(queue* q)
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- We need a thorough testing program

```
1   int queue_size(queue* q)
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8       }
9       return q->end + BOUNDED - q->front;
10  }
11
12  bool queue_free(queue* q)
13  {
14      free(q);
15      return true;
16  }
17
18  void _inc(queuetype* p)
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```

- We need a thorough testing program
- We'll see queues again for traversing trees

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1   int queue_size(queue* q)
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3       if(q==NULL){
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9       return q->end + BOUNDED - q->front;
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11
12  bool queue_free(queue* q)
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```

- We need a thorough testing program
- We'll see queues again for traversing trees
- Simulating a (slow) printer

specific.h

```
1   #pragma once
2
3   #define FORMATSTR "%d"
4   #define ELEMSIZE 20
5
6   #define QUEUETYPE "Linked"
7
8   struct dataframe {
9       queuetype i;
10      struct dataframe* next;
11  };
12  typedef struct dataframe dataframe;
13
14  struct queue {
15      /* Underlying array */
16      dataframe* front;
17      dataframe* end;
18      int size;
19  };
```

specific.h

```c
1   #pragma once
2
3   #define FORMATSTR "%d"
4   #define ELEMSIZE 20
5
6   #define QUEUETYPE "Linked"
7
8   struct dataframe {
9       queuetype i;
10      struct dataframe* next;
11  };
12  typedef struct dataframe dataframe;
13
14  struct queue {
15      /* Underlying array */
16      dataframe* front;
17      dataframe* end;
18      int size;
19  };
```

linked.c

```c
1   #include "../queue.h"
2   #include "specific.h"
3
4   queue* queue_init(void)
5   {
6       queue* q = (queue*) ncalloc(1, sizeof(queue));
7       return q;
8   }
9
10  void queue_enqueue(queue* q, queuetype d)
11  {
12      dataframe* f;
13      if(q==NULL){
14          return;
15      }
16
17      /* Copy the data */
18      f = ncalloc(1, sizeof(dataframe));
19      f->i = d;
20
21      /* 1st one */
22      if(q->front == NULL){
23          q->front = f;
24          q->end = f;
25          q->size = q->size + 1;
26          return;
27      }
28      /* Not 1st */
29      q->end->next = f;
30      q->end = f;
31      q->size = q->size + 1;
32  }
```

ADTs : Queues (Linked) II

```c
1    bool queue_dequeue( queue* q, queuetype* d)
2    {
3        dataframe* f;
4        if((q==NULL) || (q->front==NULL) || (q->end==NULL)){
5            return false;
6        }
7        f = q->front->next;
8        *d = q->front->i;
9        free(q->front);
10       q->front = f;
11       q->size = q->size - 1;
12       return true;
13   }
14
15   bool queue_free( queue* q)
16   {
17       if(q){
18           dataframe* tmp;
19           dataframe* p = q->front;
20           while(p!=NULL){
21               tmp = p->next;
22               free(p);
23               p = tmp;
24           }
25           free(q);
26       }
27       return true;
28   }
```

ADTs : Queues (Linked) II

```
1   bool queue_dequeue(queue* q, queuetype* d)
2   {
3       dataframe* f;
4       if((q==NULL) || (q->front==NULL) || (q->end==NULL)){
5           return false;
6       }
7       f = q->front->next;
8       *d = q->front->i;
9       free(q->front);
10      q->front = f;
11      q->size = q->size - 1;
12      return true;
13  }
14
15  bool queue_free(queue* q)
16  {
17      if(q){
18          dataframe* tmp;
19          dataframe* p = q->front;
20          while(p!=NULL){
21              tmp = p->next;
22              free(p);
23              p = tmp;
24          }
25          free(q);
26      }
27      return true;
28  }
```

```
1   void queue_tostring(queue* q, char* str)
2   {
3       dataframe *p;
4       char tmp[ELEMSIZE];
5       str[0] = '\0';
6       if((q==NULL) || (q->front == NULL)){
7           return;
8       }
9       p = q->front;
10      while(p){
11          sprintf(tmp, FORMATSTR, p->i);
12          strcat(str, tmp);
13          strcat(str, "|");
14          p = p->next;
15      }
16      str[strlen(str)-1] = '\0';
17  }
18
19  int queue_size(queue* q)
20  {
21      if((q==NULL) || (q->front==NULL)){
22
23          return 0;
24      }
25      return q->size;
26  }
```

Detour : Graphviz

- There exists a nice package, called Graphviz:

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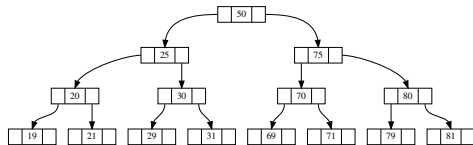
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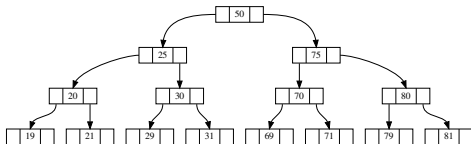- Game Trees
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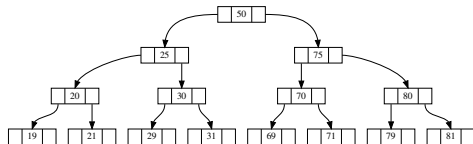- Game Trees
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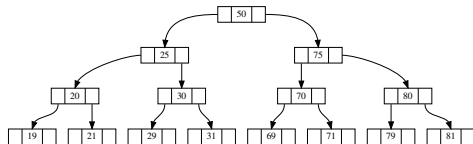- Trees drawn upside-down !

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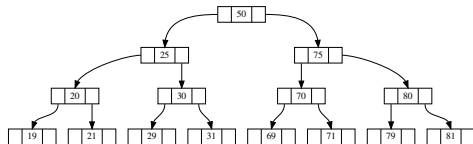- Game Trees
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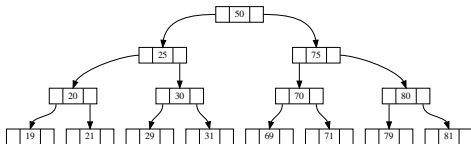
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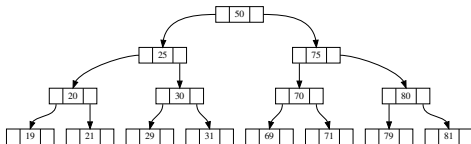- A node with no children is a leaf

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- Most trees need to be created dynamically
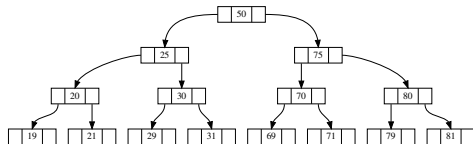
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- In a tree, there is only one path from the root to any child
- A node with no children is a leaf
- Most trees need to be created dynamically
- Empty subtrees are set to NULL

Binary Search Trees

In a binary search tree the left-hand tree of a parent contains all keys less than the parent node, and the right-hand side all the keys greater than the parent node.
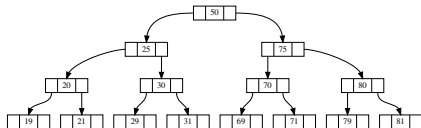
Binary Search Trees

In a binary search tree the left-hand tree of a parent contains all keys less than the parent node, and the right-hand side all the keys greater than the parent node.

bst.h

```
1    #include "../General/general.h"
2    #include "../Queue/queue.h"
3
4    #include <stdio.h>
5    #include <stdlib.h>
6    #include <assert.h>
7
8    bst* bst_init(void);
9
10   /* Insert 1 item into the tree */
11   bool bst_insert(bst* b, treetype d);
12
13   /* Return number of nodes in tree */
14   int bst_size(bst* b);
15
16   /* Whether the data d is stored in the tree */
17   bool bst_isin(bst* b, treetype d);
18
19   /* Bulk insert n items from an array a into an initialised tree */
20   bool bst_insertarray(bst* b, treetype* a, int n);
21
22   /* Clear all memory associated with tree, & set pointer to NULL */
23   bool bst_free(bst* b);
24
25   /* Optional ? */
26
27   char* bst_preorder(bst* b);
28   void bst_printlevel(bst* b);
29   /* Create string with tree as ((head)(left)(right)) */
30   char* bst_printlisp(bst* b);
31   /* Use Graphviz via a .dot file */
32   void bst_todot(bst* b, char* dotname);
```

Binary Search Trees : Linked I

specific.h

```c
1    #include <string.h>
2
3    typedef int treetype;
4    #define FORMATSTR "%i"
5    #define ELEMSIZE 20
6    #define BSTTYPE "Linked"
7
8    struct dataframe {
9        treetype d;
10       struct dataframe* left;
11       struct dataframe* right;
12   };
13   typedef struct dataframe dataframe;
14
15   struct bst {
16       dataframe* top;
17       /* Data element size, in bytes */
18   };
19   typedef struct bst bst;
```

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13 typedef struct dataframe dataframe;
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15 struct bst {
16     dataframe* top;
17     /* Data element size, in bytes */
18 };
19 typedef struct bst bst;
```

```c
/* Based on geekforgeeks.org */
dataframe* _insert(dataframe* t, treetype d)
{
    dataframe* f;
    /* If the tree is empty, return a new frame */
    if (t == NULL){
        f = ncalloc(sizeof(dataframe), 1);
        f->d = d;
        return f;
    }
    /* Otherwise, recurs down the tree */
    if (d < t->d){
        t->left = _insert(t->left, d);
    }
    else if(d > t->d){
        t->right = _insert(t->right, d);
    }
    /* return the (unchanged) dataframe pointer */
    return t;
}
```

Binary Search Trees : Linked II

```
bool _isin(dataframe* t, treetype d)
{
    if(t==NULL){
        return false;
    }
    if(t->d == d){
        return true;
    }
    if(d < t->d){
        return _isin(t->left, d);
    }
    else{
        return _isin(t->right, d);
    }
    return false;
}
```

```c
bool _isin(dataframe* t, treetype d)
{
    if(t==NULL){
        return false;
    }
    if(t->d == d){
        return true;
    }
    if(d < t->d){
        return _isin(t->left, d);
    }
    else{
        return _isin(t->right, d);
    }
    return false;
}
```

```c
char* _printlisp(dataframe* t)
{
    char tmp[ELEMSIZE];
    char *s1, *s2, *p;

    if(t==NULL){
        /*  \0 string */
        p = ncalloc(1,1);
        return p;
    }
    sprintf(tmp, FORMATSTR, t->d);
    s1 = _printlisp(t->left);
    s2 = _printlisp(t->right);
    p = ncalloc(strlen(s1)+strlen(s2)+strlen(tmp)+
        strlen("()() "), 1);
    sprintf(p, "%s(%s)(%s)", tmp, s1, s2);
    free(s1);
    free(s2);
    return p;
}
```

Binary Trees using Arrays ?

- Don't rush to assume a linked data structure must be used to implement trees.

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- You could use 1 cell of an array for the first node, the next two cells for its children, the next 4 cells for their children and so on.

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- You could use 1 cell of an array for the first node, the next two cells for its children, the next 4 cells for their children and so on.
- You need to mark which cells are in use & which aren't ...

Counting from cell 1, for a tree with n nodes:

To find	Use	Iff
The root	$A[1]$	A is nonempty
The left child of $A[i]$	$A[2i]$	$2i \leq n$
The parent of $A[i]$	$A[i/2]$	$i > 1$
Is $A[i]$ a leaf ?	True	$2i > n$

Binary Search Trees : Realloc

specific.h

```
1    #include <stdbool.h>
2
3    typedef int treetype;
4    #define FORMATSTR "%i"
5    #define ELEMSIZE 20
6    #define BSTTYPE "Realloc"
7
8    // Probably (2^n) -1
9    #define INITSIZE 31
10   #define SCALEFACTOR 2
11
12   struct dataframe {
13       treetype d;
14       bool isvalid;
15   };
16   typedef struct dataframe dataframe;
17
18   struct bst {
19       dataframe* a;
20       int capacity;
21   };
22   typedef struct bst bst;
```

Binary Search Trees : Realloc

specific.h

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1   #include <stdbool.h>
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3   typedef int treetype;
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7
8   // Probably (2^n) -1
9   #define INITSIZE 31
10  #define SCALEFACTOR 2
11
12  struct dataframe {
13      treetype d;
14      bool isvalid;
15  };
16  typedef struct dataframe dataframe;
17
18  struct bst {
19      dataframe* a;
20      int capacity;
21  };
22  typedef struct bst bst;
```

Using a queue for Level-Order traversal:

```
void bst_printlevel(bst* b)
{
    treetype n;
    if((b==NULL) || (! _isvalid(b, 0))){
        return;
    }
    /* Make a queue of cell indices */
    queue* q = queue_init();
    queue_enqueue(q, 0);
    while(queue_dequeue(q, &n) && _isvalid(b, (int)n)){
        printf(FORMATSTR, b->a[n].d);
        putchar(' ');
        queue_enqueue(q, _leftchild((int)n));
        queue_enqueue(q, _rightchild((int)n));
    }
}
```

Binary Search Trees : Complexity

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- In this case, complexity becomes $O(n)$.
- The tree search performs best when well balanced trees are formed.
- Large body of literature about creating & re-balancing trees - Red-Black trees, Tries, 2-3 trees, AVL trees etc.

Binary Trees : Huffman Compression I

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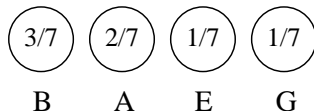
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- To encode the string "BABBAGE":

$$\left(3/7\right) \left(2/7\right) \left(1/7\right) \left(1/7\right)$$
$$\quad B \qquad A \qquad E \qquad G$$

- Keep a list of characters, ordered by their frequency
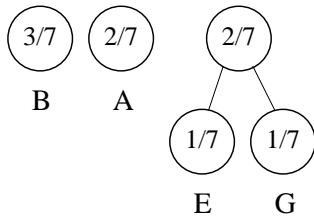
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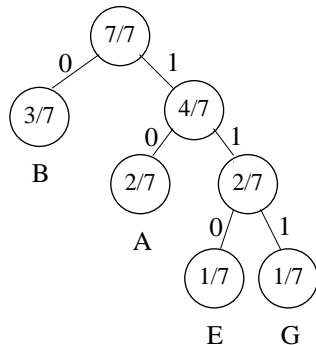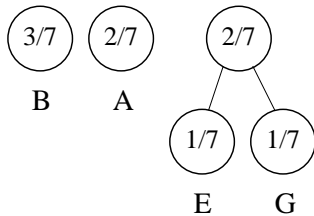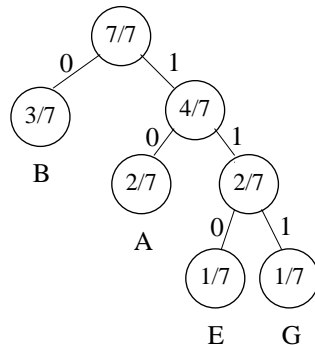 sub-tree, and re-order (sort) the nodes :

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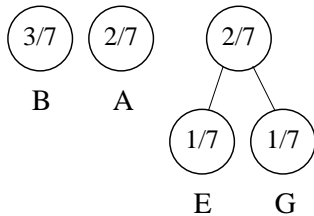# Binary Trees : Huffman Compression II

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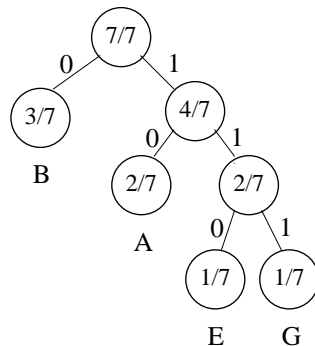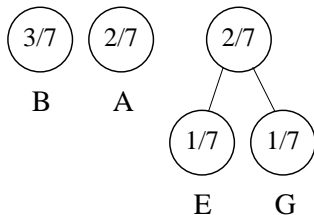
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Table of Contents

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- A black-box into which we insert a key (e.g. NI number) and out pops an array index.
- As an example lets use an array of size 11 to store some airport codes, e.g. PHL, DCA, FRA.

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	1
	2
	3
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	5
GCM	6
	7
ORY	8
	9
	10

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- However, inserting "HKG" causes a collision.

	0
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	2
	3
PHL	4
	5
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	7
ORY	8
	9
	10

?

HKG

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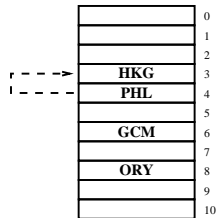
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- The function is chosen so that two keys which collide at the same address will have different probe decrements, e.g. :

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- Although "PHL" and "HKG" share the same primary hash value of $h(K) = 4$, they have different probe decrements:
$p("PHL") = 4$
$p("HKG") = 3$

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- If the size of our array, M, was even and the probe decrement was chosen to be 2, then only half of the locations could be probed.

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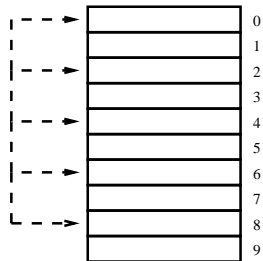
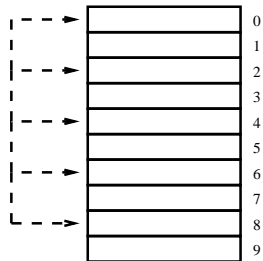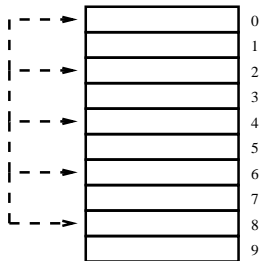## ADTs : Primes and Chaining

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- Often we choose our table size to be a prime number and our probe decrement to be a number in the range $1 \ldots M - 1$.

Open-addressing is not the only method of collision reduction. Another common one is separate chaining.

```c
1    #include <stdio.h>
2
3    int hash(unsigned int sz, char *s);
4
5    int main(void)
6    {
7
8        char str[] = "Hello World!";
9        // Hash modulus 7919
10       printf("%d\n", hash(7919, str));
11       return 0;
12
13   }
14
15   /*
16   Modified Bernstein hashing
17   5381 & 33 are magic numbers required by the algorithm
18   */
19   int hash(unsigned int sz, char *s)
20   {
21       unsigned long hash = 5381;
22       int c;
23       while((c = (*s++))){
24           hash = 33 * hash ^ c;
25       }
26       return (int)(hash%sz);
27   }
```

Execution :

5479

ADTs : A Practical Hash Function

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Execution :

5479

Has similarities to the implementation of `rand()` :

```c
#include <stdio.h>

int rand_r(unsigned int* seed);

int main(void)
{
    unsigned int seed = 0;
    printf("%d\n", rand_r(&seed));
    return 0;
}

/* This algorithm is mentioned in the ISO C standard,
   here extended for 32 bits. */
int rand_r(unsigned int* seed)
{
    unsigned int next = *seed;
    int result;

    next *= 1103515245;
    next += 12345;
    result = (unsigned int) (next / 65536) % 2048;

    next *= 1103515245;
    next += 12345;
    result <<= 10;
```

Execution :

1012484

ADTs : Cuckoo Hashing

- We have two tables, each with their **own** hash function.

```
Empty: copied farandoles into table 0(4)
Empty: copied bronzine into table 0(12)
Empty: copied auscultatory into table 0(5)
Empty: copied bifer into table 0(13)
Empty: copied steepgrass into table 0(6)
Empty: copied prevised into table 0(7)
Empty: copied oomph into table 0(8)
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Empty: copied bronzine into table 1(5)
ranseur, so cuckooed out empodium from table 0(5)
Empty: copied empodium into table 1(4)
Empty: copied megalodon into table 0(11)
geosynchronous, so cuckooed out megalodon from table 0(11)
Empty: copied megalodon into table 1(14)
Empty: copied osmeteria into table 0(14)
Table getting full -> rehashed old sz =16
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Empty: copied auscultatory into table 0(5)
Empty: copied bifer into table 0(13)
Empty: copied steepgrass into table 0(6)
Empty: copied prevised into table 0(7)
Empty: copied oomph into table 0(8)
empodium, so cuckooed out auscultatory from table 0(5)
Empty: copied auscultatory into table 1(10)
interquarreled, so cuckooed out bronzine from table 0(12)
Empty: copied bronzine into table 1(5)
ranseur, so cuckooed out empodium from table 0(5)
Empty: copied empodium into table 1(4)
Empty: copied megalodon into table 0(11)
geosynchronous, so cuckooed out megalodon from table 0(11)
Empty: copied megalodon into table 1(14)
Empty: copied osmeteria into table 0(14)
Table getting full -> rehashed old sz =16
```

ADTs : Cuckoo Hashing

- We have two tables, each with their **own** hash function.
- We only need to check two cells when searching.
- On collision, the existing item is 'cuckooed' out of it's cell into the other table.

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Table of Contents

ADTs : Graphs

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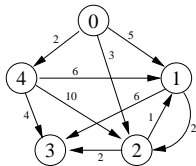
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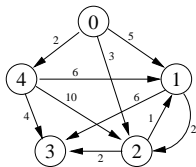
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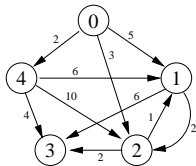
`graph.h` (partial)

```c
#include <limits.h>
#define INF (INT_MAX)

/* Initialise an empty graph */
graph* graph_init(void);

/* Add new vertex */
int graph_addVert(graph* g, char* label);

/* Add new edge between two Vertices */
bool graph_addEdge(graph* g,  int from,
                   int to, edge weight);

/* Returns NO_VERT if not already a vert
   else 0 ... (size-1)              */
int graph_getVertNum(graph* g, char* label);

/* Returns label of vertex v */
char* graph_getLabel(graph* g, int v);

/* Returns edge weight - if none = INF */
edge graph_getEdgeWeight(graph* g, int from, int to);

/* Number of verts */
int graph_numVerts(graph* b);

/* Output edge weights e.g. "0->1 200 2->1 100" */
void graph_tostring(graph* g, char* str);

/* Clear all memory associated with graph */
bool graph_free(graph* g);
```

Graph ADT : 2D Realloc I

The graph type could be implemented in a large number of different ways.

- As two sets, one for vertices, one for edges. We haven't looked at an implentation for sets, but one could use lists.

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	0	1	2	3	4
0	0	5	3	∞	2
1	∞	0	2	6	∞
2	∞	1	0	2	∞
3	∞	∞	∞	0	∞
4	∞	6	10	4	0

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3	∞	∞	∞	0	∞
4	∞	6	10	4	0

specific.h

```
1    #define GRAPHTYPE "Realloc"
2
3    #define INITSIZE 8
4    #define SCALEFACTOR 2
5
6    #define TMPSTR 1000
7
8    #define NO_VERT -1
9
10   typedef unsigned int edge;
11
12   struct graph {
13       edge** adjMat;
14       char** labels;
15       /* Actual number of verts */
16       int size;
17       /* Max verts before realloc() */
18       int capacity;
19   };
20   typedef struct graph graph;
```

2D Realloc II

```
graph* graph_init(void)
{
    graph* g = (graph*) ncalloc(sizeof(graph), 1);
    int h = INITSIZE;
    int w = h;
    g->capacity = h;
    g->adjMat = (edge**) n2dcalloc(h, w, sizeof(edge));
    g->labels = (char**) n2dcalloc(h, MAXLABEL+1, sizeof(char));
    for(int j=0; j<h; j++){
        for(int i=0; i<w; i++){
            /* It's not clear if weight[j][j] should be 0 or INF */
            g->adjMat[j][i] = INF;
        }
    }
    return g;
}

edge graph_getEdgeWeight(graph* g, int from, int to)
{
    if((g==NULL) || (from >= g->size) || (to >= g->size)){
        return INF;
    }
    return g->adjMat[from][to];
}


int graph_numVerts(graph* g)
{
    if(g==NULL){
        return 0;
    }
    return g->size;
}
```

2D Realloc II

```c
graph* graph_init(void)
{
    graph* g = (graph*) ncalloc(sizeof(graph), 1);
    int h = INITSIZE;
    int w = h;
    g->capacity = h;
    g->adjMat = (edge**) n2dcalloc(h, w, sizeof(edge));
    g->labels = (char**) n2dcalloc(h, MAXLABEL+1, sizeof(char));
    for(int j=0; j<h; j++){
        for(int i=0; i<w; i++){
            /* It's not clear if weight[j][j] should be 0 or INF */
            g->adjMat[j][i] = INF;
        }
    }
    return g;
}

edge graph_getEdgeWeight(graph* g, int from, int to)
{
    if((g==NULL) || (from >= g->size) || (to >= g->size)){
        return INF;
    }
    return g->adjMat[from][to];
}


int graph_numVerts(graph* g)
{
    if(g==NULL){
        return 0;
    }
    return g->size;
}
```

```c
int graph_addVert(graph* g, char* label)
{
    if(g==NULL){
        return NO_VERT;
    }
    if(graph_getVertNum(g, label) != NO_VERT){
        return NO_VERT;
    }
    /* Resize */
    if(g->size >= g->capacity){
        g->adjMat = (edge**) n2drecalloc((void**)g->adjMat,
                        g->capacity, g->capacity*SCALEFACTOR,
                        g->capacity, g->capacity*SCALEFACTOR,
                        sizeof(edge));
        g->labels = (char**) n2drecalloc((void**)g->labels,
                        g->capacity, g->capacity*SCALEFACTOR,
                        MAXLABEL+1, MAXLABEL+1, 1);
        for(int j=0; j<g->capacity*SCALEFACTOR; j++){
            for(int i=0; i<g->capacity*SCALEFACTOR; i++){
                if((i>=g->capacity)||(j>=g->capacity)){
                    g->adjMat[j][i] = INF;
                }
            }
        }
        g->capacity = g->capacity*SCALEFACTOR;
    }
    strcpy(g->labels[g->size], label);
    g->size = g->size + 1;
    return g->size-1;
}
```
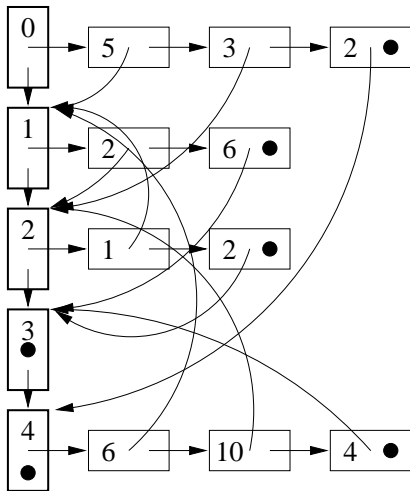
Graph ADT - Linked

specific.h

```
1    #define GRAPHTYPE "Linked"
2
3    #define INITSIZE 8
4    #define SCALEFACTOR 2
5
6    #define TMPSTR 1000
7
8    #define NO_VERT -1
9
10   typedef unsigned int edge;
11
12   struct vertex {
13       char* label;
14       struct vertex* nextv;
15       void* firste;
16       int num;
17   };
18   typedef struct vertex vertex;
19
20   struct edge {
21       edge weight;
22       vertex* v;
23       struct edge* nexte;
24   };
25   typedef struct edge edgel;
26
27   struct graph {
28       vertex* firstv;
29       vertex* endv;
30       int size;
31   };
32   typedef struct graph graph;
```

Linked II

```c
graph* graph_init(void)
{
    graph* g = (graph*) ncalloc(1, sizeof(graph));
    return g;
}

edge graph_getEdgeWeight(graph* g, int from, int to)
{
    if((g==NULL) || (from >= g->size) || (to >= g->size)){
        return INF;
    }
    vertex* v = g->firstv;
    for(int i=0; i<from; i++){
        v = v->nextv;
    }
    if((v==NULL) || (v->num != from)){
        return INF;
    }
    edgel* e = v->firste;
    while(e != NULL){
        if(e->v->num == to){
            return e->weight;
        }
        e = e->nexte;
    }
    return INF;
}
```
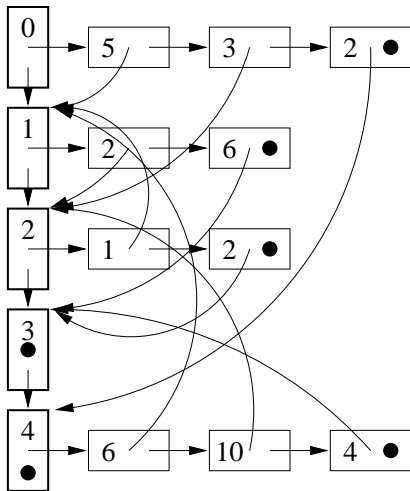
Linked II

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graph* graph_init(void)
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    graph* g = (graph*) ncalloc(1, sizeof(graph));
    return g;
}

edge graph_getEdgeWeight(graph* g, int from, int to)
{
    if((g==NULL) || (from >= g->size) || (to >= g->size)){
        return INF;
    }
    vertex* v = g->firstv;
    for(int i=0; i<from; i++){
        v = v->nextv;
    }
    if((v==NULL) || (v->num != from)){
        return INF;
    }
    edgel* e = v->firste;
    while(e != NULL){
        if(e->v->num == to){
            return e->weight;
        }
        e = e->nexte;
    }
    return INF;
}
```

```c
bool graph_addEdge(graph* g, int from, int to, edge w)
{
    if((g==NULL) || (g->size == 0)){
        return false;
    }
    if((from >= g->size) || (to >= g->size)){
        return false;
    }
    vertex* f = g->firstv;
    for(int i=0; i<from; i++){
        f = f->nextv;
    }
    vertex* t = g->firstv;
    for(int i=0; i<to; i++){
        t = t->nextv;
    }
    return _addEdge(f, t, w);
}
```

Table of Contents

Algorithms : Sorting

```c
#define NUMS 6

void bubble_sort(int b[], int s);

int main(void)
{
    int a[] = {3, 4, 1, 2, 9, 0};
    bubble_sort(a, NUMS);
    for(int i=0; i<NUMS; i++){
        printf("%i ", a[i]);
    }
    printf("\n");
    return 0;
}

void bubble_sort(int b[], int s)
{
    bool changes;
    do{
        changes = false;
        for(int i=0; i<s-1; i++){
            if(b[i] > b[i+1]){
                SWAP(b[i], b[i+1]);
                changes = true;
            }
        }
    }while(changes);
}
```

Execution :

0 1 2 3 4 9

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- Bubblesort has complexity $O(n^2)$, therefore very inefficient.

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- If an algorithm uses comparison keys to decide the correct order then the theoretical lower bound on complexity is $O(n \log n)$. From wiki:

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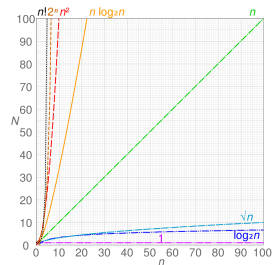
Algorithms : Merge Sort

- Transposition (Bubblesort)

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- Merge sort is divide-and-conquer in that you divide the array into two halves, mergesort each half and then merge the two halves into order.

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- Merge sort is divide-and-conquer in that you divide the array into two halves, mergesort each half and then merge the two halves into order.

```c
#include <stdio.h>
#include <stdlib.h>
#include <string.h>

void mergesort(int *src, int *spare, int l, int r);
void merge(int *src, int *spare, int l, int m, int r);

#define NUM 5000

int main(void)
{
    int a[NUM];
    int spare[NUM];

    for(int i=0; i<NUM; i++){
        a[i] = rand()%100;
    }

    mergesort(a, spare, 0, NUM-1);

    for(int i=0; i<NUM; i++){
        printf("%4d => %d\n", i, a[i]);
    }

    return 0;
}
```

Merge Sort II

```c
void mergesort(int *src, int *spare, int l, int r)
{
    int m = (l+r)/2;
    if(l != r){
        mergesort(src, spare, l, m);
        mergesort(src, spare, m+1, r);
        merge(src, spare, l, m, r);
    }
}

void merge(int *src, int *spare, int l, int m, int r)
{
    int s1 = l;
    int s2 = m+1;
    int d = l;

    do{
        if(src[s1] < src[s2]){
            spare[d++] = src[s1++];
        }
        else{
            spare[d++] = src[s2++];
        }
    }while((s1 <= m) && (s2 <= r));

    if(s1 > m){
        memcpy(&spare[d], &src[s2], sizeof(spare[0])*(r-s2+1));
    }
    else{
        memcpy(&spare[d], &src[s1], sizeof(spare[0])*(m-s1+1));
    }
    memcpy(&src[l], &spare[l], (r-l+1)*sizeof(spare[0]));
}
```

Merge Sort II

```c
void mergesort(int *src, int *spare, int l, int r)
{
    int m = (l+r)/2;
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        mergesort(src, spare, l, m);
        mergesort(src, spare, m+1, r);
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    }
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void merge(int *src, int *spare, int l, int m, int r)
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    int s1 = l;
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    int d = l;

    do{
        if(src[s1] < src[s2]){
            spare[d++] = src[s1++];
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        }
    }while((s1 <= m) && (s2 <= r));

    if(s1 > m){
        memcpy(&spare[d], &src[s2], sizeof(spare[0])*(r-s2+1));
    }
    else{
        memcpy(&spare[d], &src[s1], sizeof(spare[0])*(m-s1+1));
    }
    memcpy(&src[l], &spare[l], (r-l+1)*sizeof(spare[0]));
}
```

- Quicksort is also divide-and-conquer.

Merge Sort II

```c
void mergesort(int *src, int *spare, int l, int r)
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    int m = (l+r)/2;
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    }
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    do{
        if(src[s1] < src[s2]){
            spare[d++] = src[s1++];
        }
        else{
            spare[d++] = src[s2++];
        }
    }while((s1 <= m) && (s2 <= r));

    if(s1 > m){
        memcpy(&spare[d], &src[s2], sizeof(spare[0])*(r-s2+1));
    }
    else{
        memcpy(&spare[d], &src[s1], sizeof(spare[0])*(m-s1+1));
    }
    memcpy(&src[l], &spare[l], (r-l+1)*sizeof(spare[0]));
}
```

- Quicksort is also divide-and-conquer.
- Choose some value in the array as the *pivot* key.

Merge Sort II

```
void mergesort(int *src, int *spare, int l, int r)
{
    int m = (l+r)/2;
    if(l != r){
        mergesort(src, spare, l, m);
        mergesort(src, spare, m+1, r);
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}

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    int d = l;

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            spare[d++] = src[s1++];
        }
        else{
            spare[d++] = src[s2++];
        }
    }while((s1 <= m) && (s2 <= r));

    if(s1 > m){
        memcpy(&spare[d], &src[s2], sizeof(spare[0])*(r-s2+1));
    }
    else{
        memcpy(&spare[d], &src[s1], sizeof(spare[0])*(m-s1+1));
    }
    memcpy(&src[l], &spare[l], (r-l+1)*sizeof(spare[0]));
}
```

- Quicksort is also divide-and-conquer.
- Choose some value in the array as the *pivot* key.
- This key is used to divide the array into two partitions. The left partition contains keys $\leq$ pivot key, the right partition contains keys $>$ pivot.

Merge Sort II

```c
void mergesort(int *src, int *spare, int l, int r)
{
    int m = (l+r)/2;
    if(l != r){
        mergesort(src, spare, l, m);
        mergesort(src, spare, m+1, r);
        merge(src, spare, l, m, r);
    }
}

void merge(int *src, int *spare, int l, int m, int r)
{
    int s1 = l;
    int s2 = m+1;
    int d = l;

    do{
        if(src[s1] < src[s2]){
            spare[d++] = src[s1++];
        }
        else{
            spare[d++] = src[s2++];
        }
    }while((s1 <= m) && (s2 <= r));

    if(s1 > m){
        memcpy(&spare[d], &src[s2], sizeof(spare[0])*(r-s2+1));
    }
    else{
        memcpy(&spare[d], &src[s1], sizeof(spare[0])*(m-s1+1));
    }
    memcpy(&src[l], &spare[l], (r-l+1)*sizeof(spare[0]));
}
```

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- Choose some value in the array as the *pivot* key.
- This key is used to divide the array into two partitions. The left partition contains keys $\leq$ pivot key, the right partition contains keys $>$ pivot.
- Once again, the sort is then applied recursively.

Algorithms : Quicksort

```c
#include <stdio.h>
#include <stdlib.h>
#include <math.h>

int partition(int *a, int l, int r);
void quicksort(int *a, int l, int r);

#define NUM 100000

int main(void)
{
    int a[NUM];

    for(int i=0; i<NUM; i++){
        a[i] = rand()%100;
    }
    quicksort(a, 0, NUM-1);

    return 0;
}

void quicksort(int *a, int l, int r)
{
    int pivpoint = partition(a, l, r);
    if(l < pivpoint){
        quicksort(a, l, pivpoint-1);
    }
    if(r > pivpoint){
        quicksort(a, pivpoint+1, r);
    }
}
```

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3   #include <math.h>
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5   int partition(int *a, int l, int r);
6   void quicksort(int *a, int l, int r);
7
8   #define NUM 100000
9
10  int main(void)
11  {
12      int a[NUM];
13
14      for(int i=0; i<NUM; i++){
15          a[i] = rand()%100;
16      }
17      quicksort(a, 0, NUM-1);
18
19      return 0;
20  }
21
22  void quicksort(int *a, int l, int r)
23  {
24      int pivpoint = partition(a, l, r);
25      if(l < pivpoint){
26          quicksort(a, l, pivpoint-1);
27      }
28      if(r > pivpoint){
29          quicksort(a, pivpoint+1, r);
30      }
31  }
```

```
int partition(int *a, int l, int r)
{
    int piv = a[l];
    while(l<r){
        /* Right -> Left Scan */
        while(piv < a[r] && l<r) r--;
        if(r!=l){
            a[l] = a[r];
            l++;
        }
        /* Left -> Right Scan */
        while(piv > a[l] && l<r) l++;
        if(r!=l){
            a[r] = a[l];
            r--;
        }
    }
    a[r] = piv;
    return r;
}
```

qsort()

- Theoretically both methods have a complexity $O(n \log n)$

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```c
#include <stdio.h>
#include <stdlib.h>

int intcompare(const void *a, const void *b);

int main(void)
{
    int a[10];

    for(int i=0; i<10; i++){
        a[i] = 9 - i;
    }

    qsort(a, 10, sizeof(int), intcompare);

    for (int i=0; i<10; i++){
        printf(" %d",a[i]);
    }
    printf("\n");
    return 0;

}


int intcompare(const void *a, const void *b)
{
    const int *ia = (const int *)a;
    const int *ib = (const int *)b;
    return *ia - *ib;
}
```

Algorithms : The Radix Sort

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459 254 472 534 649 239 432 654 477

0
1
2 472 432
3
4 254 534 654
5
6
7 477
8
9 459 649 239

Read out the new list:
472 432 254 534 654 477 459 649 239

Radix Sort II

472 432 254 534 654 477 459 649 239

0
1
2
3 432 534 239
4 649
5 254 654 459
6
7 472 477
8
9

432 534 239 649 254 654 459 472 477

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Radix Sort Discussion

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- $O(n)$ simply means that the number of operations can be bounded by $k.n$, for some constant k.
- With the radix sort, k is often very large.
- For many lists this may be less efficient than more traditional $O(n \log n)$ algorithms.

Algorithm : Rabin-Karp String Searching

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  Master String : AAAAAAAAAAAAH
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- Recall that to compute a hash function on a word we did something like:

$$h("NEILL") =$$

$$(13 \times 26^4 + 4 \times 26^3 + 8 \times 26^2 + 11 \times 26 + 11)\%P$$

where P is a big prime number.

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  where P is a big prime number.

- This can be expanded by Horner's method to:

$$(((((((13 \times 26) + 4) \times 26) + 8) \times 26) + 11) \times 26 + 11)\%P$$

Rabin-Karp II

- For a large search string, overflow can occur. We therefore move the *mod* operation inside the brackets:

$$(((((13 \times 26) + 4)\%P \times 26) + 8)\%P \times 26) + 11)\%P \times 26 + 11)\%P$$

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```c
1   #include <string.h>
2   #include <assert.h>
3
4   #define Q 33554393
5   #define D 26
6   #define index(C) (C-'A')
7
8   int rk(char *p, char *a);
9
10  int main(void)
11  {
12      assert(rk("STING",
13          "A STRING EXAMPLE CONSISTING OF ...")==22);
14      return 0;
15  }
16
17  int rk(char *p, char *a)
18  {
19      int i, dM = 1, h1=0, h2=0;
20      int m = strlen(p);
21      int n = strlen(a);
22      for(i=1; i<m; i++) dM = (D*dM)%Q;
23      for(i=0; i<m; i++){
24          h1 = (h1*D+index(p[i]))%Q;
25          h2 = (h2*D+index(a[i]))%Q;
26      }
27      // h1 = search string hash, h2 = master string hash
28      for(i=0; h1!=h2; i++){
29          h2 = (h2+D*Q-index(a[i])*dM) % Q;
30          h2 = (h2*D+index(a[i+m])) % Q;
31          if(i>n-m) return n;
32      }
33      return i;
34  }
```

Algorithm : Boyer-Moore String Searching

The Boyer-Moore algorithm uses (in part) an
array flagging which characters form part of
the search string and an array telling us how
far to slide right if that character appears in
the master and causes a mismatch.

Execution :

```
A STRING SEARCHING EXAMPLE CONSISTING OF ...
      |     |
STING       |
      STING
           STING
```

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- Since R doesn't appear in the search string, we can take 5 steps to the left.

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- Since R doesn't appear in the search string, we can take 5 steps to the left.
- The next comparison is between the G and the S. We can slide the search string right until it matches the S in the master.

Boyer-Moore II

Execution :

```
A STRING SEARCHING EXAMPLE CONSISTING OF ...
            |    |    |    |    |
          STING  |    |    |    |
              STING   |    |    |
                    STING   |    |
                          STING  |
                                STING
```

- Now the C doesn't appear in the master and once again we can slide a full 5 places to the right.

Boyer-Moore II

Execution :

```
A STRING SEARCHING EXAMPLE CONSISTING OF ...
              |    |    |     |     |
           STING   |    |     |     |
                 STING  |     |     |
                      STING   |     |
                           STING    |
                                  STING
```

- Now the C doesn't appear in the master and once again we can slide a full 5 places to the right.
- After 3 more full slides right we arrive at the T in CONSISTING.

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```
A STRING SEARCHING EXAMPLE CONSISTING OF ...
              |    |    |     |     |
          STING    |    |     |     |
               STING    |     |     |
                    STING     |     |
                         STING      |
                               STING
```

- Now the C doesn't appear in the master and once again we can slide a full 5 places to the right.
- After 3 more full slides right we arrive at the T in CONSISTING.
- We align the T's, and have found our match using 7 compares (plus 5 to verify the match).

Algorithms : TSP on Graphs

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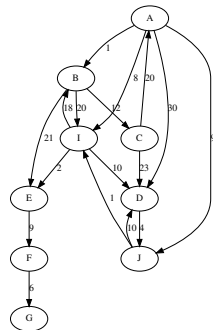
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- A -> B -> C -> D -> J -> I -> E -> F -> G

```
edge graph_salesman(graph* g, int from, char* str)
{
    bool* unvis;
    int curr, ncurr, nvs;
    edge cst, bcst, e;

    nvs = graph_numVerts(g);
    if((g==NULL) || (from >= nvs) || (str==NULL)){
        return INF;
    }
    unvis = (bool*)ncalloc(nvs, sizeof(bool));
    for(int v=0; v<nvs; v++){
        unvis[v] = true;
    }
    curr = from;
    bcst = 0;
    strcpy(str, graph_getLabel(g, from));
    do{
        unvis[curr] = false;
        cst = INF;
        ncurr = NO_VERT;
        /* Look at neighbours of curr */
```

TSP II

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    }
    unvis = (bool*)ncalloc(nvs, sizeof(bool));
    for(int v=0; v<nvs; v++){
        unvis[v] = true;
    }
    curr = from;
    bcst = 0;
    strcpy(str, graph_getLabel(g, from));
    do{
        unvis[curr] = false;
        cst = INF;
        ncurr = NO_VERT;
        /* Look at neighbours of curr */
```

```c
        for(int v=0; v<nvs; v++){
            e = graph_getEdgeWeight(g, curr, v);
            if((v!=curr) && unvis[v] && (e!=INF)){
                if(e < cst){
                    cst = e;
                    ncurr = v;
                }
            }
        }
        /* Add in cost to go to closest */
        if(cst < INF){
            bcst += cst;
            curr = ncurr;
            strcat(str, " ");
            strcat(str, graph_getLabel(g, ncurr));
        }
    }while((cst < INF) && (curr != NO_VERT));
    free(unvis);
    return bcst;
}
```

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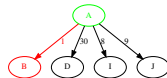
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