



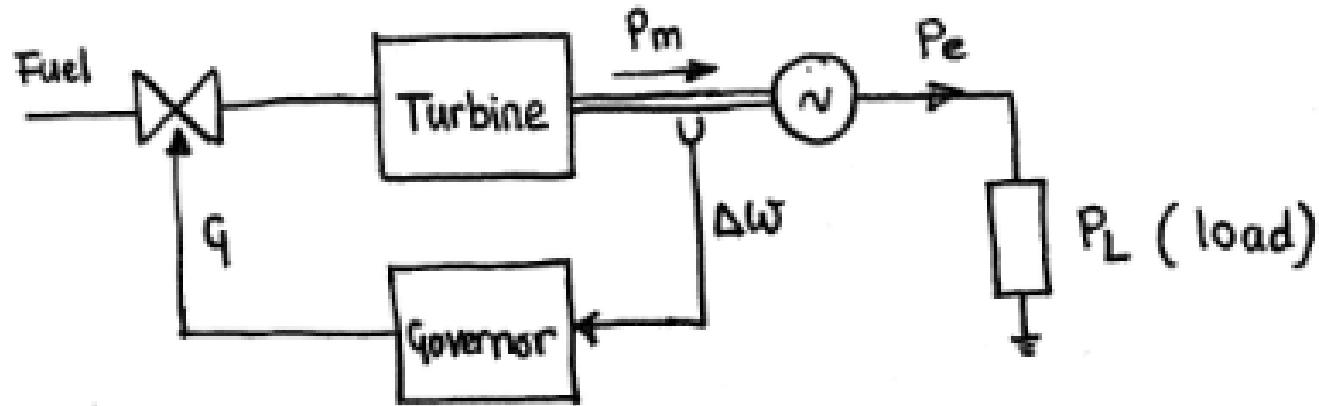
THE UNIVERSITY  
*of*ADELAIDE

Course:  
ELEC ENG 3110 Electric Power Systems  
ELEC ENG 7074 Power Systems PG  
(Semester 2, 2021)

Power and Frequency Control (Part 2)

Lecturer and coordinator: David Vowles  
[david.vowles@adelaide.edu.au](mailto:david.vowles@adelaide.edu.au)

## Example – Isolated Generator Supplying a Load – No Governor



Change in load  $\Rightarrow$  near instant change in generator electrical torque / power  
 $\Rightarrow$  mismatch between mechanical & electrical torque  
 $\Rightarrow$  speed variations according to rotor equations of motion

## Example – Isolated Generator Supplying a Load – No Governor

Power system loads comprise many types of devices

- Resistive loads - lighting + heating
  - insensitive to frequency variation
- Motor loads
  - pumps, fans, compressors, etc
  - electrical power consumption is frequency dependent.

$$\Delta P_L = \underline{\Delta P_{L_0}} + \underline{D_L \Delta \omega}$$

Total load change ( $= \Delta P_e$ )

Frequency insensitive load change

Frequency / speed sensitive load change

$D_L \rightarrow$  load damping constant

$$\frac{\Delta P_L (\text{pu})}{\Delta \omega (\text{pu})}$$

Typically between 1.0 to 2.0 per-unit.

## Example – Isolated Generator Supplying a Load – No Governor

Isolated mining site

$3 \times 120 \text{ MVA}$  generators  $\rightarrow S_b = 360 \text{ MVA}$

200 MW load

$H = 3.5 \text{ pu}$  for each unit on 120 MVA

$D_L = 1.0 \text{ pu}$

Determine the frequency response to the connection of a 9MW load, assuming no speed-governing

For the three units

$$H = 3.5 \times \left( \frac{120}{360} \right) \times 3 = 3.5 \text{ pu on } 360 \text{ MVA}$$

$$D_L = 1.0 \times \left( \frac{200 + 9}{360} \right) = 0.5806 \text{ pu on } 360 \text{ MVA}$$

*Include load that is connected*

## Example – Isolated Generator Supplying a Load – No Governor

In generator rotor equation of motion  
assume generator damping constant  $D=0$

$$\frac{d\Delta W}{dt} = \frac{1}{2H} (\Delta P_m - \Delta P_e)$$

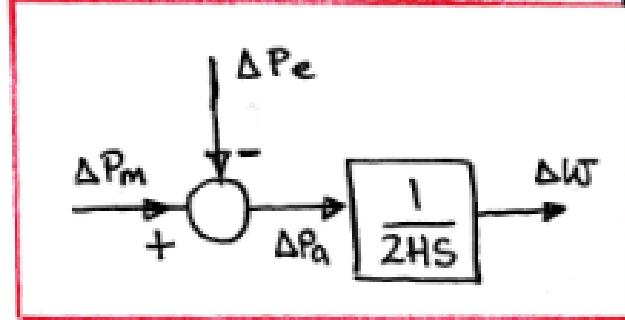
Take Laplace Transform  $\rightarrow \frac{d}{dt} \rightarrow s$

$$s \Delta W = \frac{1}{2H} (\Delta P_m - \Delta P_e)$$

$$\Delta W = \frac{1}{2HS} (\Delta P_m - \Delta P_e)$$

$\underbrace{\Delta P_a}_{\text{accelerating power}}$

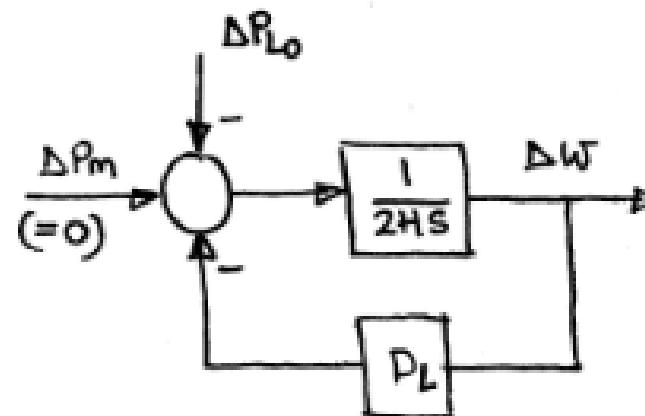
Block diagram of acceleration Eqn.



$$\Delta P_e = \Delta P_{L_0} + D_L \Delta W$$

$$\Delta W = \frac{1}{2HS} (\Delta P_m - \Delta P_{L_0} - D_L \Delta W)$$

$$\Delta W = \frac{1}{2HS + D_L} (\Delta P_m - \Delta P_{L_0})$$



## Example – Isolated Generator Supplying a Load – No Governor

Since  $\Delta P_M = 0$  (no governing action)

$$\Delta W = -\frac{1}{2H(s + \frac{D_L}{2H})} \cdot \Delta P_{L_0}$$

$$\delta P_{L_0} = \frac{q}{360} = 0.025 \text{ pu on } 360 \text{ MVA}$$

$$\frac{1}{s} \xrightarrow{\text{d}} \frac{1}{s}$$

$$\Delta W = -\frac{1}{2H(s + \frac{D_L}{2H})} \cdot \frac{\Delta P_{L_0}(s)}{s}$$

### Partial Fraction Expansion

$$\underbrace{\Delta W}_{\text{PRODUCT FORM}} = -\frac{1}{2H(s + \frac{D_L}{2H})} \cdot \frac{\Delta P_{L_0}}{s} = \underbrace{\frac{A}{(s + \frac{D_L}{2H})}}_{\text{SUM FORM}} + \underbrace{\frac{B}{s}}$$

- Use Heaviside cover-up method to determine residues.  
(OK for distinct poles)

- To determine A cover-up  $(s + \frac{D_L}{2H})$  in the product and substitute  $s = -\frac{D_L}{2H}$  elsewhere  $\Rightarrow$

$$A = \frac{\Delta P_{L_0}}{D_L}$$

- To determine B cover-up s in the product and substitute  $s = 0$  elsewhere  $\Rightarrow$

$$B = \frac{-\Delta P_{L_0}}{D_L}$$

- $\Delta W = \frac{\Delta P_{L_0}}{D_L} \left( \frac{1}{s + \frac{D_L}{2H}} - \frac{1}{s} \right)$

## Example – Isolated Generator Supplying a Load – No Governor

$$\Delta W(s) = -\left(\frac{\delta P_{L0}}{D_L}\right)\left(\frac{1}{s} - \frac{1}{s + \left(\frac{D_L}{2H}\right)}\right) \xrightarrow{\mathcal{L}^{-1}} \Delta W(t) = -\left(\frac{\delta P_{L0}}{D_L}\right)\left(1 - e^{-\left(t \times \frac{D_L}{2H}\right)}\right)$$

Define  $T = \frac{2H}{D_L} = \frac{2 \times 3.5}{0.5806} = 12.057 \text{ s}$  Time Constant

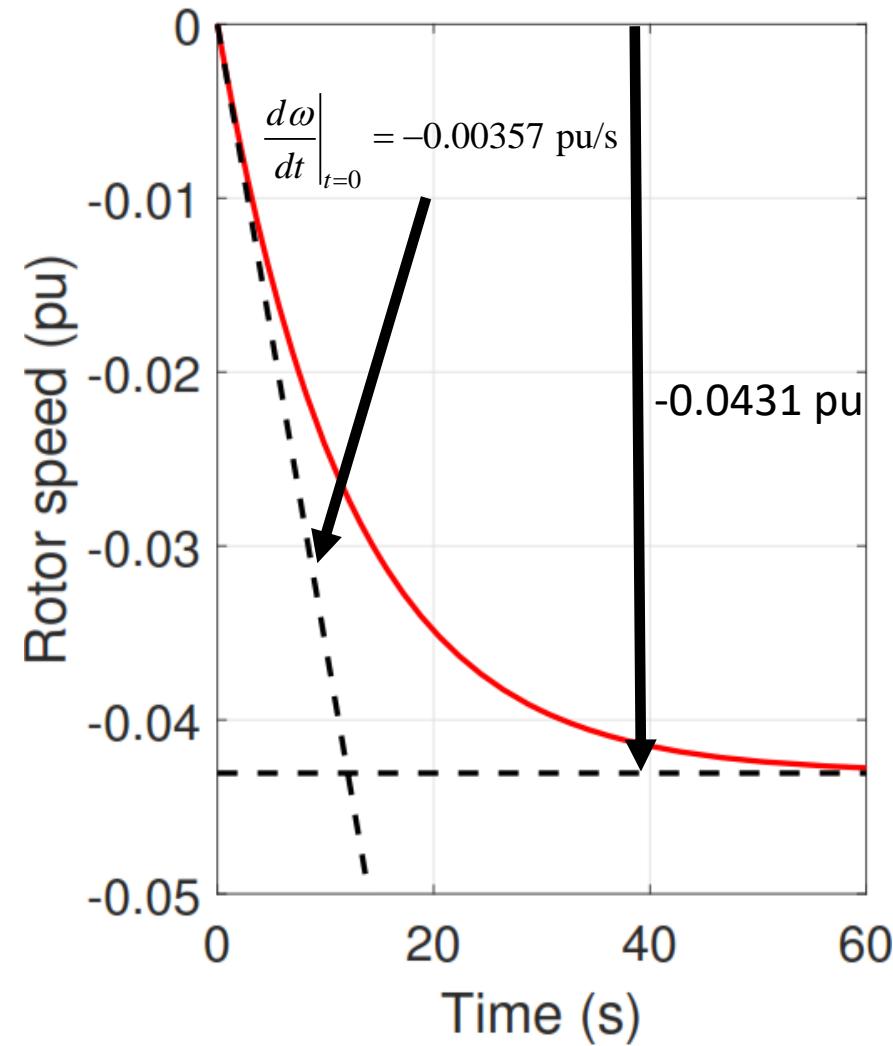
$$\delta w = -\left(\frac{\delta P_{L0}}{D_L}\right) = -\left(\frac{0.025}{0.5806}\right) = -0.0431 \text{ pu}$$
 Speed change

$$\Delta w(t) = \delta w \left(1 - e^{-\left(t/T\right)}\right) = -0.0431 \left(1 - e^{-t/12.057}\right)$$

$$\frac{d \Delta w}{dt} = \frac{\delta w}{T} \cdot e^{-\left(t/T\right)}$$

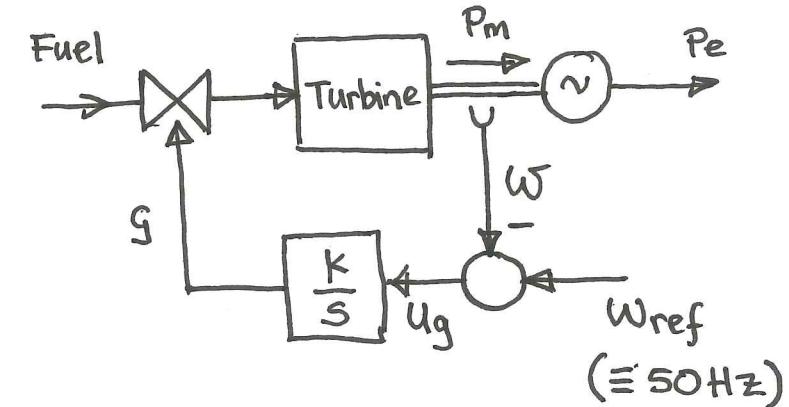
$$\text{At } t=0, \frac{d \Delta w}{dt} \Big|_{t=0} = \frac{\delta w}{T} = -\left(\frac{\delta P_{L0}}{2H}\right) = -\frac{0.025}{7} = -0.00357 \text{ pu/s}$$

Initial Rate  
of change of  
rotor-speed



## Constant Speed Governor

- \* Isochronous Governor
- \* Adjusts fuel flow by adjusting valve position ( $g$ ) to restore rotor-speed (i.e. frequency) to setpoint ( $\omega_{ref}$ )
- \* Speed-error  $u_g = \omega_{ref} - \omega$  amplified and integrated to produce control signal  $g$  that actuates fuel supply valve.
- \* Due to integral action  $g$  will reach a new steady-state after a disturbance when  $u_g = 0$  ( $\omega = \omega_{ref} \equiv 50\text{Hz}$ )



$$g = \frac{K}{s} \cdot u_g$$

$$\Rightarrow s g = K u_g \xrightarrow{\text{d}^{-1}} \frac{dg}{dt} = K u_g$$

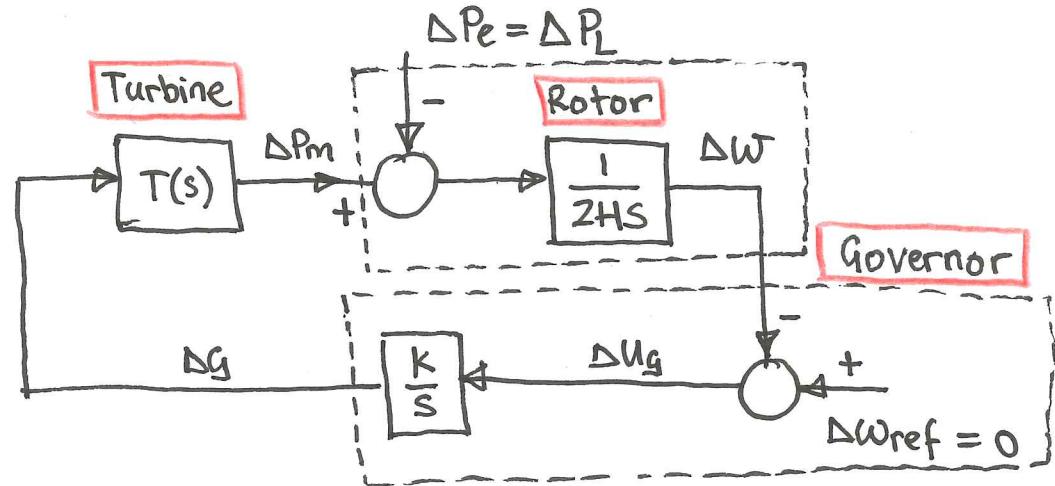
Steady-state  $\Rightarrow \frac{dg}{dt} = 0$

$$\Rightarrow u_g = 0$$

## Constant Speed Governor

### Illustrative dynamic model

- \* Model represents perturbations from initial steady-state operating Condition -  $P_{M_0}, P_e_0 = P_{L_0}$ ,  $\omega_0 = \omega_{ref} = 1.0$  pu (synchronous speed)
- \* The turbine is represented by a general transfer-function  $T(s)$
- \* For simplicity the frequency-dependence of loads is neglected
- \* The transfer-function from  $\Delta P_L$  (perturbation in load) to the rotor-speed ( $\Delta \omega$ ) is derived



Treat  $\Delta P_L$  as input,  $\Delta \omega_{ref} = 0$

$$\Delta P_m(s) = - T(s) \cdot \left( \frac{K}{s} \right) \Delta \omega(s)$$

$$\Delta \omega(s) = \frac{(\Delta P_m(s) - \Delta P_L(s))}{2Hs}$$

$$2Hs \Delta \omega(s) = - T(s) \frac{K}{s} \Delta \omega(s) - \Delta P_L(s)$$

$$\frac{\Delta \omega(s)}{\Delta P_L(s)} = \frac{-1}{2Hs + T(s) \cdot \left( \frac{K}{s} \right)}$$

$$= \frac{-s}{2Hs^2 + K \cdot T(s)}$$

## Constant Speed Governor

### Illustrative dynamic model - Example

Suppose a step-change in load is applied

$$\text{i.e. } \Delta P_L(s) = \frac{\delta P_L}{s}$$

$$\begin{aligned} \text{Then } \Delta \omega(s) &= \frac{-s}{2Hs^2 + KT(s)} \cdot \frac{\delta P_L}{s} \\ &= \frac{-\delta P_L}{2Hs^2 + KT(s)} \end{aligned}$$

Assuming that the poles of  $\Delta \omega(s)$  are negative (i.e. system is stable) then by the final value theorem :

$$\begin{aligned} \lim_{t \rightarrow \infty} \Delta \omega(t) &= \lim_{s \rightarrow 0} s \Delta \omega(s) \\ &= \lim_{s \rightarrow 0} \frac{-\delta P_L s}{2Hs^2 + KT(s)} \\ &= 0 \end{aligned}$$

This confirms the earlier point that following a disturbance to a generator with an isochronous governor the rotor will reach a new steady-state when  $\Delta \omega = 0$  (i.e.  $\omega = \omega_{ref}$ )

The final value of  $\Delta P_m$  is expected to be  $\Delta P_m = \delta P_L$

- Explain why

## Constant Speed Governor

### Illustrative dynamic model - Example

Derive the transfer-function for the turbine-governor-generator model in which the turbine transfer-function is

$$T(s) = \underbrace{\left( \frac{1+sT_A}{1+sT_B} \right)}_{\text{Governor Phase compensation}} \underbrace{\frac{1}{(1+sT_T)}}_{\text{Turbine characteristic}}$$

$$\begin{aligned} \frac{\Delta w(s)}{\Delta P_L(s)} &= \frac{-s}{2Hs^2 + \underline{KT(s)}} \\ &= \frac{-s}{2Hs^2 + \boxed{\frac{K(1+sT_A)}{(1+sT_B)(1+sT_T)}}} \end{aligned}$$

$$\frac{\Delta w(s)}{\Delta P_L(s)} = \frac{-s(1+sT_B)(1+sT_T)/K}{\left(\frac{2H}{K}\right)s^2(1+sT_B)(1+sT_T) + 1}$$

Example parameters:

$$H = 3.5 \text{ pu.s}, T_T = 0.5s, K = 0.2 \text{ pu.s}$$

$$T_A = 10s, T_B = 1s$$

Calculate and plot the time-response of the rotor-speed ( $\Delta w(t)$ ) and mechanical power ( $\Delta P_m(t)$ ) perturbations due to a 5% step increase in the load (i.e.  $\Delta P_L(t) = 0.05 \underline{u(t)}$ )

unit-step

## Constant Speed Governor

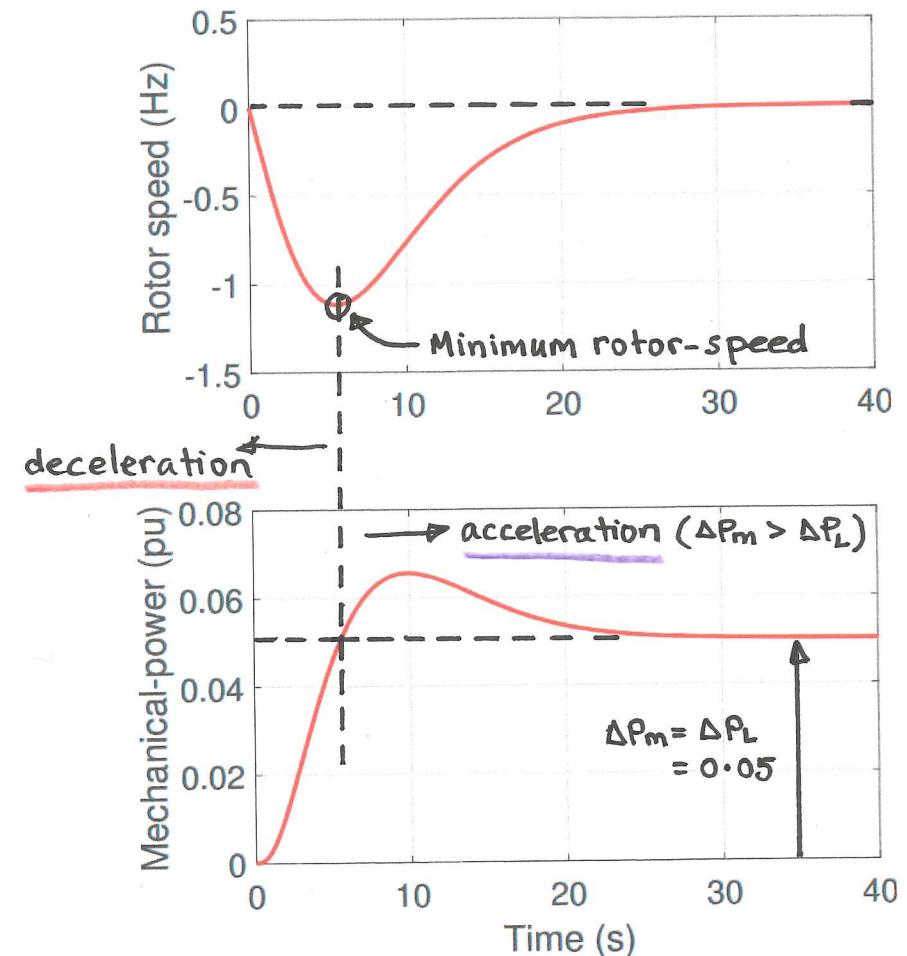
### Example time-response

- \* Following step-increase in load  
the generator rotor decelerates

$$\frac{d\Delta w}{dt} = \frac{1}{2H} (\Delta P_m - \Delta P_e) < 0$$

$\Rightarrow \Delta w$  decreases

- \* Governor, in response to  $\Delta w < 0$   
begins to open valve to increase  
fuel flow  $\Rightarrow$  begin to increase  $\Delta P_m$
- \* At  $t = 5.48$  s  $\Delta P_m = \Delta P_e = \Delta P_L = 0.05$  pu  
 $\Rightarrow$  minimum frequency (rotor-speed)
- \* For  $t > 5.48$  s,  $\Delta P_m > \Delta P_L \Rightarrow$  acceleration  
 $\Rightarrow$  rotor-speed begins to increase
- \* Due to integral control speed returns  
to synchronous speed (i.e.  $\Delta w = 0$ ).

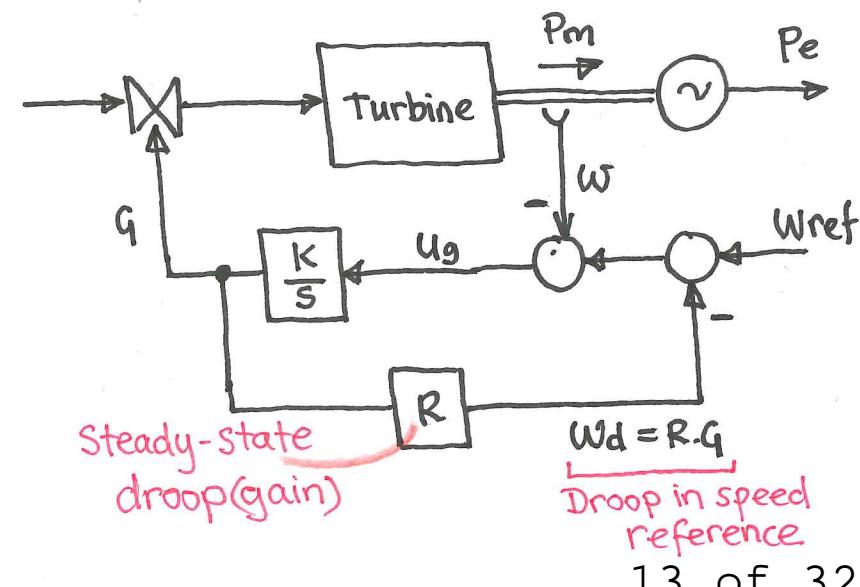


## Governors With steady-state droop characteristic

- \* Two or more generators operating in parallel cannot use isochronous governors
  - multiple units attempting to reduce their measurement of the speed-error signal to zero
  - small differences in measurement and/or setpoint between units results in sustained ramping of mechanical power of the interconnected generators
  - controllers 'fight' for control of common system frequency (i.e. common rotor synchronous speed)

Solution - introduce steady-state droop characteristic so that interconnected machines 'share' the load.

The speed reference of the governor is reduced in proportion to the control valve opening



## Governors with steady-state droop

- \* Suppose the generating unit is operating with steady-state gate position and power output of  $g_0$  and  $P_{m_0} = P_e_0$ , respectively and that the machine is spinning at synchronous speed -  $\omega_0 = 1 \text{ pu}$ .
- \* Suppose now that the rotor-speed is changed by  $\Delta\omega$ .
- \* What is the associated change in gate position?
- \*  $U_g = (w_{ref} - R(g_0 + \Delta g)) - (\omega_0 + \Delta\omega)$
- \* The final value of  $U_g = 0 \Rightarrow$ 
$$\begin{aligned}\omega_0 + \Delta\omega &= w_{ref} - R(g_0 + \Delta g) \\ &= \underbrace{(w_{ref} - R \cdot g_0)}_{\omega_0} - R \Delta g\end{aligned}$$
- \*  $\Delta\omega = -R \Delta g$
- \*  $\Delta g = -\frac{\Delta\omega}{R}$
- \* Thus, the value of  $R$  (droop) determines the steady-state relationship between rotor-speed and turbine valve position.
- \* Since, under steady-state conditions the valve position  $g_0$  is related to the turbine power  $P_{m_0}$  and for small perturbations
$$\Delta P_m = K_t \cdot \Delta g$$
it follows that
$$\Delta P_m = -\left(\frac{K_t}{R}\right) \cdot \Delta\omega$$

## Governors with steady-state droop characteristic

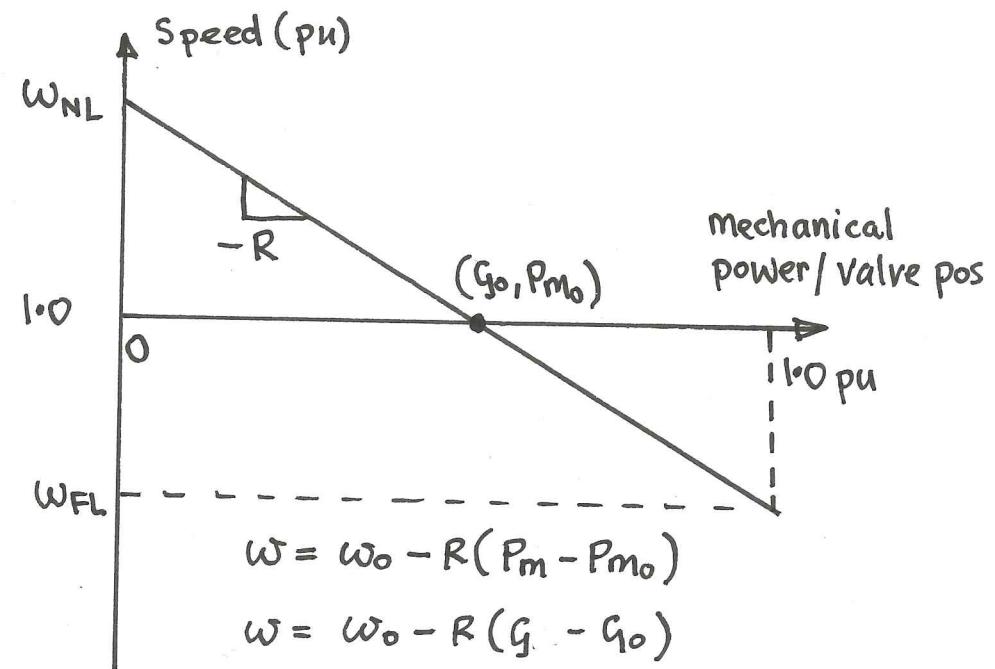
- \* In the ideal case - which is well approximated in modern governors - the perturbation relationships above extend over the full range of valve opening / power output

- \* For the ideal case :

$$g = g_o + \Delta g = g_o - \left( \frac{w - w_o}{R} \right)$$

- \* With appropriate choice of base values  $K_t = 1$  and

$$P_m = P_{m_o} - \left( \frac{w - w_o}{R} \right)$$



### Governor steady-state characteristic

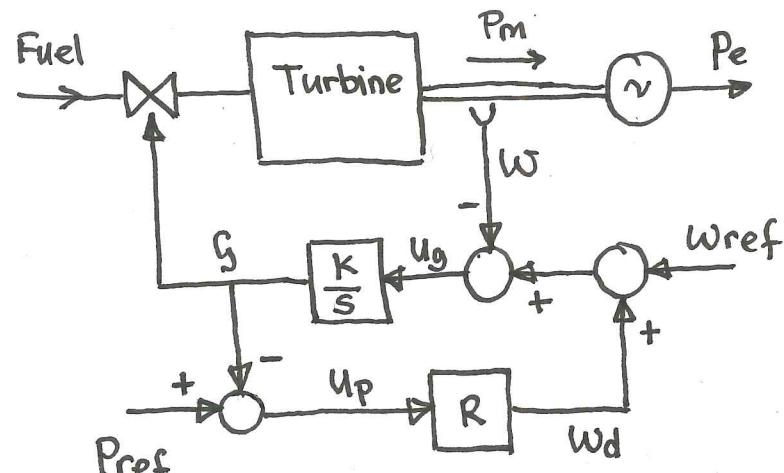
$$R = \frac{\text{p.u. decrease in speed}}{\text{p.u. increase in turbine power output}}$$

$R \rightarrow$  Droop

## Governors with steady-state droop characteristic

Control of power output →

Load reference



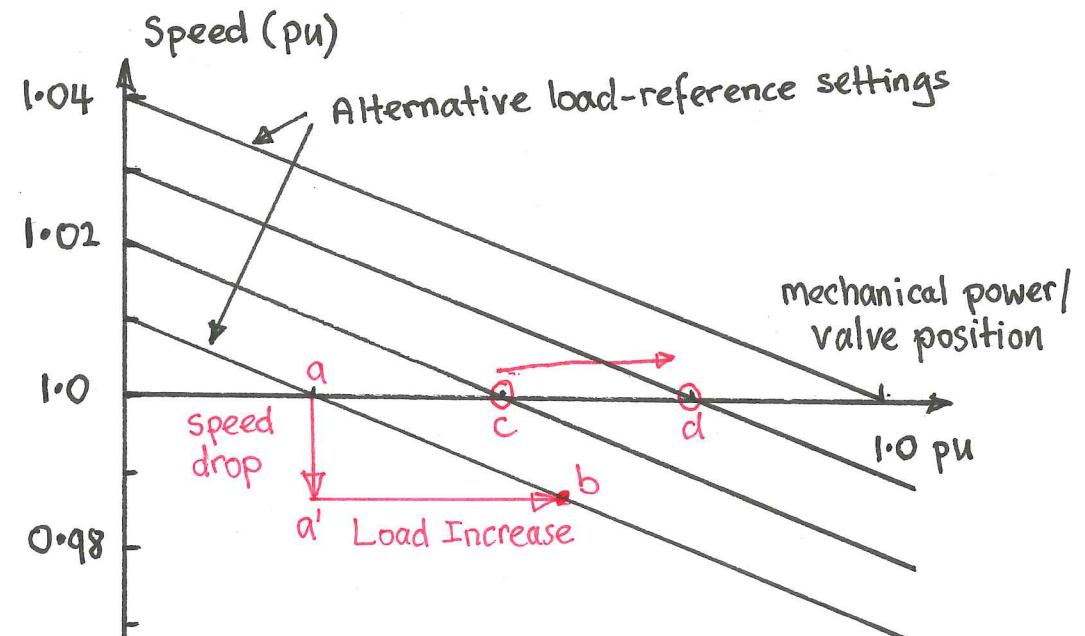
(Load - reference)

\* Under steady-state conditions

$$w = w_{ref} = 1 \text{ pu} \quad (\text{synchronous speed})$$

$$* u_g = 0 = (w_{ref} + w_d - w) = w_d$$

$$* u_p = 0 \Rightarrow \underline{g_0 = P_{ref}}$$



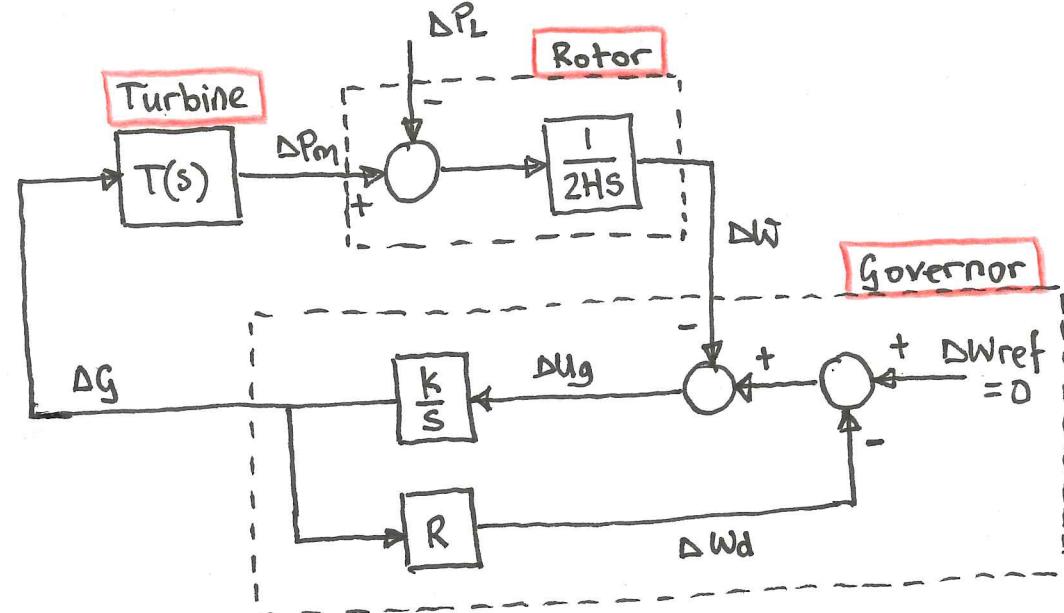
c → d Load increase, constant speed - Load reference

a → a' → b Load increase  $\Rightarrow$  speed drop  $\Rightarrow$  increase in turbine output (a → b)

## Governors with steady-state droop characteristic

### Illustrative dynamic model

- \* Model represents perturbations from initial steady-state operating condition -  $P_{M_0}, P_{e_0} = P_{L_0}, W_0 = W_{ref} = 1.0$
- \* Turbine represented by general TF  $T(s)$  - assumed to be proper.
- \* Neglect frequency-dependence of loads
- \* Derive TF from  $\Delta P_L$  (load-perturbation) to rotor-speed ( $\Delta W$ )
- \* Assume that the steady-state gain of  $T(s)$  is unity (i.e.  $\Delta P_m = \Delta Q$  in steady-state)



$$\Delta U_g = -(\Delta W + R \Delta G)$$

$$\Delta Q = \frac{K}{S} \Delta U_g = -\frac{K}{S} (\Delta W + R \Delta G)$$

$$\Delta Q = \frac{-(1/R)}{1+ST_g} \Delta W , \quad T_g = \frac{1}{KR}$$

$$\Delta P_m = T(s) \cdot \Delta Q = -\frac{(1/R)}{1+ST_g} \cdot T(s) \cdot \Delta W$$

## Governors with steady-state droop characteristic

### Illustrative dynamic model - continued

$$\Delta\omega = \frac{\Delta P_m - \Delta P_L}{2Hs}$$

$$2Hs \Delta\omega = \frac{-(1/R)}{1+sT_g} \cdot T(s) \cdot \Delta\omega - \Delta P_L$$

$$[2Hs(1+sT_g) + (1/R) \cdot T(s)] \Delta\omega = -(1+sT_g) \Delta P_L$$

$$\frac{\Delta\omega}{\Delta P_L} = \frac{-(1+sT_g)}{2HT_g s^2 + 2Hs + (1/R)T(s)}$$

Find the final steady-state rotor-speed deviation following a step-change in load

$$\Delta P_L(s) = \frac{\delta P_L}{s}$$

$$\therefore \Delta\omega = \frac{-(1+sT_g)}{2HT_g s^2 + 2Hs + (1/R)T(s)} \cdot \frac{\delta P_L}{s}$$

By the final value theorem (assuming the system is stable)

$$\Delta\omega(t \rightarrow \infty) = \lim_{s \rightarrow 0} s \Delta\omega(s)$$

$$= \lim_{s \rightarrow 0} \frac{-(1+sT_g) \delta P_L}{2HT_g s^2 + 2Hs + (1/R)T(s)}$$

$$= -R \cdot \delta P_L$$

$$\text{i.e. } \delta\omega = -R \delta P_L$$

Confirming our earlier steady-state analysis.

## Illustrative dynamic model

Derive the transfer-function for the turbine-governor-generator model in which the turbine TF is

$$T(s) = \frac{1}{1+sT_t}$$

$$\begin{aligned}\frac{\Delta W}{\Delta P_L} &= \frac{-(1+sT_g)}{2HT_g s^2 + 2HS + \frac{1}{R}T(s)} \\ &= \frac{-(1+sT_g)(1+sT_t)/R}{2HRT_g s^2(1+sT_t) + 2HRS(1+sT_t) + 1} \\ &= \frac{-(1/R)(1+s(T_g+T_t)+s^2 T_g T_t)}{(2HRT_g T_t)s^3 + 2HR(T_g+T_t)s^2 + (2HR)s + 1}\end{aligned}$$

Example parameters -

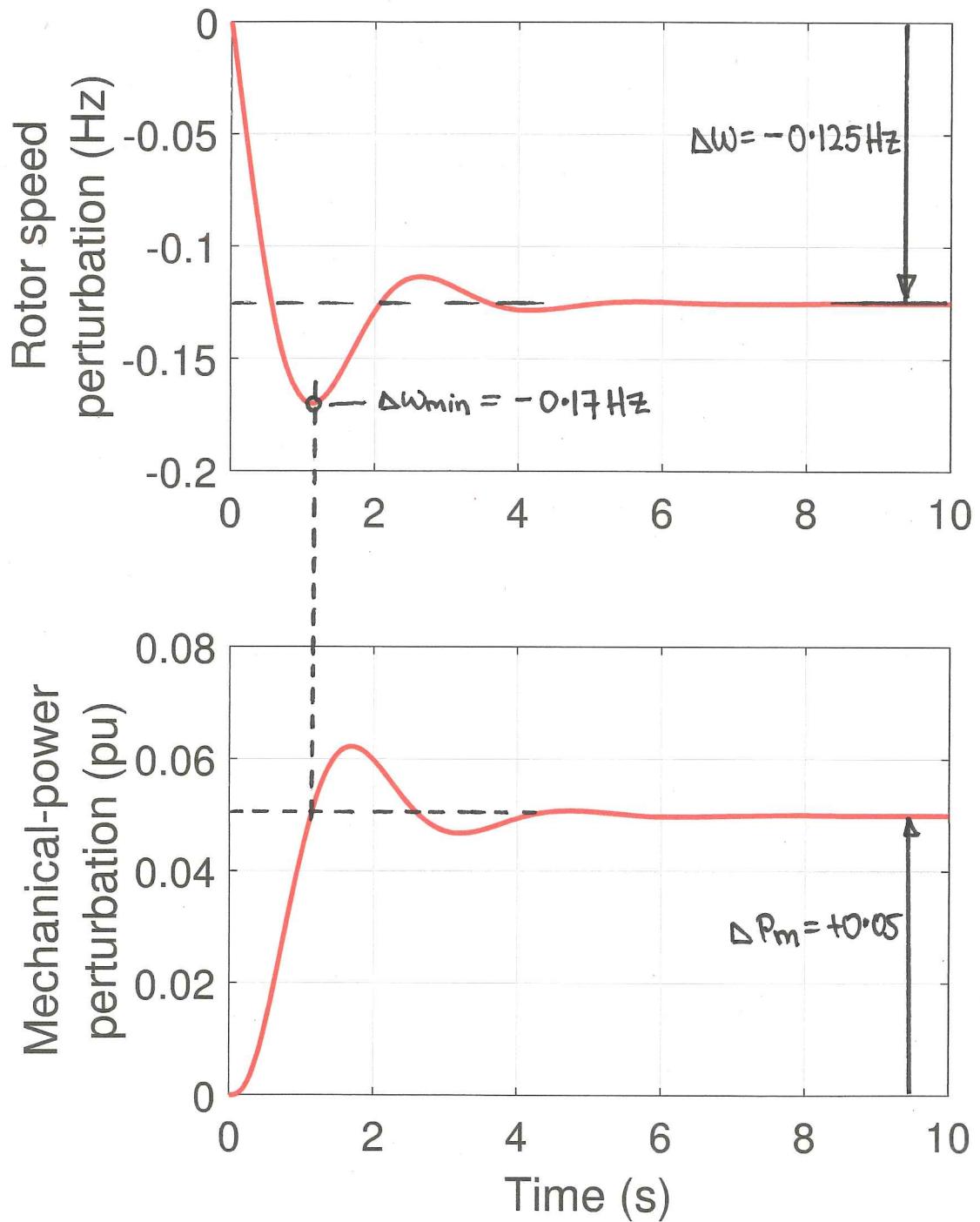
Representative of steam turbine without reheat

$$H = 5.0 \text{ pu.s}, \quad T_t = 0.3s, \quad R = 0.05 \text{ pu}$$

$$T_g = 0.2 \text{ s}$$

Calculate and plot the time-response of the rotor-speed ( $\Delta W$ ) and mechanical power ( $\Delta P_m$ ) perturbations due to a 5% step increase in the load -  $\Delta P_L = 0.05 u(t)$

↑  
Unit step.

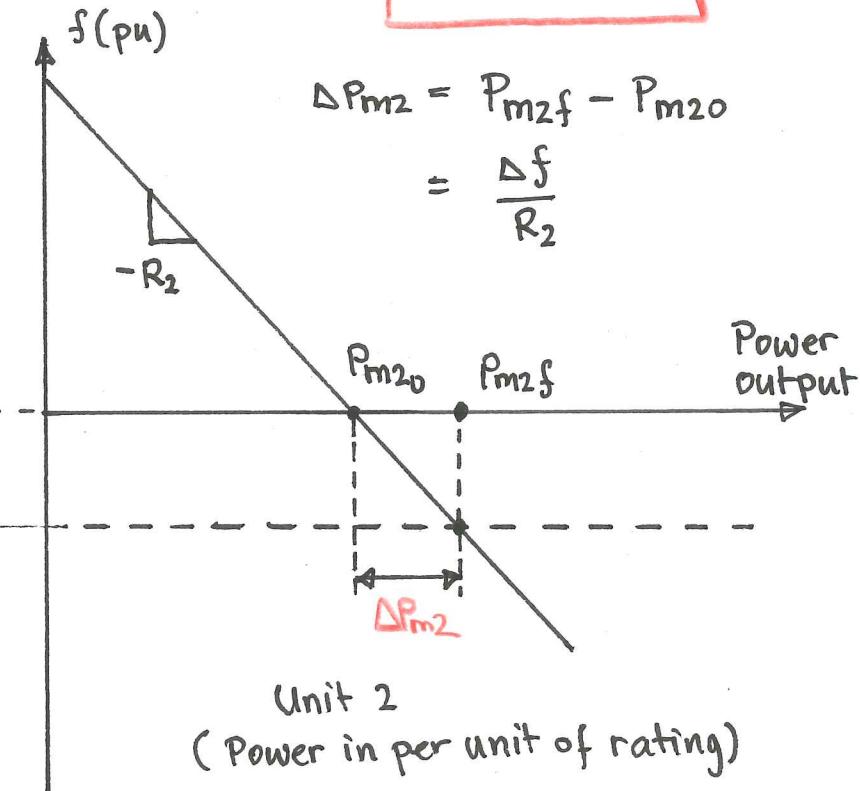
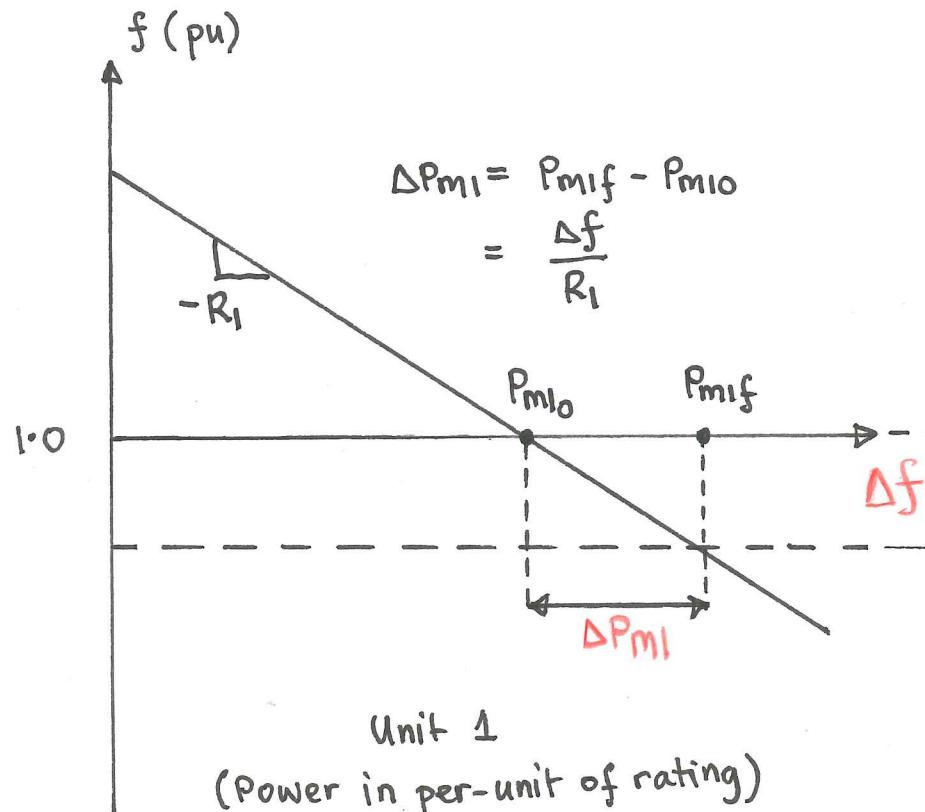


## Parallel Operation of Synchronous Generators - Load Sharing

Consider two units with steady-state governor characteristics as shown below.

- \* Initial steady-state operation @ synchronous speed and outputs  $P_{m10}$  and  $P_{m20}$ .
- \* The load picked up by each generator depends on their respective droop characteristics

$$\frac{\Delta P_{m1}}{\Delta P_{m2}} = \frac{R_2}{R_1}$$



## Parallel Operation of Synchronous Generators

- \* From previous slide, the amount of load picked up by generators following a frequency change depends on their respective droop characteristics

$$\frac{\Delta P_{m1}}{\Delta P_{m2}} = \frac{R_2}{R_1}$$

- \* If the droop settings of the units are approximately equal (in per-unit of rating) then the units will share the required change in power output in proportion to their respective ratings - which is most desirable

Example : Two prime-movers supply an isolated 50Hz. Their ratings are 100 MW and 300 MW respectively and their initial outputs are 50 MW and 250MW respectively. The governor droop settings are 4% (i.e.  $R = 0.04 \text{ pu}$ ) on turbine rating.

what is the system frequency and what are the generator outputs following a 12MW load increase.

$$\begin{aligned}\Delta P_L &= \Delta P_{m1} + \Delta P_{m2} = 12 \text{ MW} \\ &= -\frac{\Delta w}{R_1} - \frac{\Delta w}{R_2} = 12 \text{ MW}\end{aligned}$$

$$R_1 = \frac{0.04}{100} \text{ pu/MW}, R_2 = \frac{0.04}{300} \text{ pu/MW}$$

## Parallel Operation of Synchronous Generators

$$-\Delta W \left( \frac{1}{R_1} + \frac{1}{R_2} \right) = 12 \text{ MW}$$

$$\Delta P_{m1} = 3 \text{ MW}$$

$$\Delta P_{m2} = 9 \text{ MW}$$

$$\Delta W = \frac{-12}{\frac{1}{R_1} + \frac{1}{R_2}}$$

$$= \frac{-12 * 0.04}{100 + 300}$$

$$= \frac{-12 * 0.04}{400}$$

$$= -1.2 \times 10^{-3} \text{ pu}$$

$$= -0.06 \text{ pu}$$

$$\Delta P_{m1} = \frac{1.2 \times 10^{-3}}{R_1} = \frac{1.2 \times 10^{-3}}{0.04} = 0.03 \text{ pu on } 100 \text{ MW}$$

$$\Delta P_{m2} = \frac{1.2 \times 10^{-3}}{R_2} = \frac{1.2 \times 10^{-3}}{0.04} = 0.03 \text{ pu on } 300 \text{ MW}$$

The increase in load is shared between the two generators in proportion to their respective ratings. This is a consequence of their governor droop settings being the same (on unit rating)

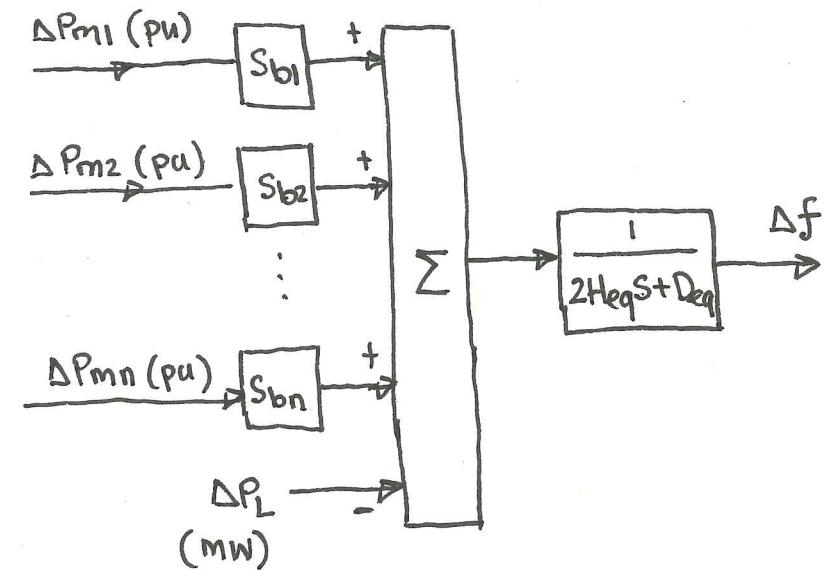
## System Frequency Regulation

- \* Interested in combined performance of all generators in the system.
- \* Neglect intermachine oscillations and transmission system behaviour
- \* Assume that all generators respond coherently - i.e. rotor-speeds of all machines are assumed to be equal and also equal to the system frequency.
- \* Composite generator with inertia constant

$$H_{eq} = \sum_{i=1}^n (H_i * S_{bi}) \text{ MW.s}$$

- \* Composite load damping constant

$$D_{eq} = \frac{\Delta P_L \text{ (MW)}}{\Delta f \text{ (pu)}}$$



Composite system model for analysis of load-frequency controls

## System Frequency Regulation

\* Composite power/frequency characteristic of the system depends on combined effect of all generator speed-droop settings.

\* The steady-state frequency deviation following a load change is derived as follows:

$$\begin{aligned}\Delta P_L &= \sum_{i=1}^n \Delta P_{mi} - D_{eq} \Delta f \\ &= -\Delta f \left[ \underbrace{\sum_{i=1}^n \left( \frac{S_{bi}}{R_i} \right)}_{1/R_{eq}} + D_{eq} \right]\end{aligned}$$

$$\therefore \Delta f = \frac{-\Delta P_L}{1/R_{eq} + D_{eq}}$$

\*  $S_{bi}$  is the MVA base of the  $i^{th}$  generator, and is the base on which the droop  $R_i$  and inertia constant  $H_i$  are specified.

\* The load damping characteristic is expressed as

$$D_{eq} = \frac{\Delta P_L \text{ (mw)}}{\Delta f \text{ (pu)}}$$

in the equation for  $\Delta f$

However, the load-frequency sensitivity is given as

$$D_L = \frac{\% \text{ change in load}}{\% \text{ change in frequency}}$$

$\therefore D_{eq} = D_L * P_L$  where  $P_L$  is the total system load (5000 MVA) after any load change.

## System Frequency Regulation

$$\Delta f = \frac{-\Delta P_L}{\frac{1}{R_{eq}} + D_{eq}} = -\frac{\Delta P_L}{k_{eq}}$$

$k_{eq} = \frac{1}{R_{eq}} + D_{eq}$  is the (frequency)

stiffness of the system. The higher  $R_{eq}$ , the lower is the frequency change for a given load change.

### Example

Total system load 2000 MW at 50 Hz. The load increases by 1% for every 1% increase in frequency. Find the steady-state frequency deviation when 100 MW is suddenly connected.

(1) Assume all synchronous generation (2500 MW) is governing and that the droop settings are identical and equal to 4% on unit rating.

$$1/R_{eq} = \frac{2500}{0.04} \text{ MW/pu.}$$

$$D_{eq} = 1.0 \times 200 \text{ MW/pu}$$

$$k_{eq} = \frac{1}{R_{eq}} + D_{eq}$$

$$= \frac{2500}{0.04} + 200 = 64,600$$

$$\Delta f = -\frac{\Delta P_L}{k_{eq}} \text{ pu}$$

$$= -\frac{100}{64,600} \text{ pu}$$

$$= -1.548 \times 10^{-3} \text{ pu}$$

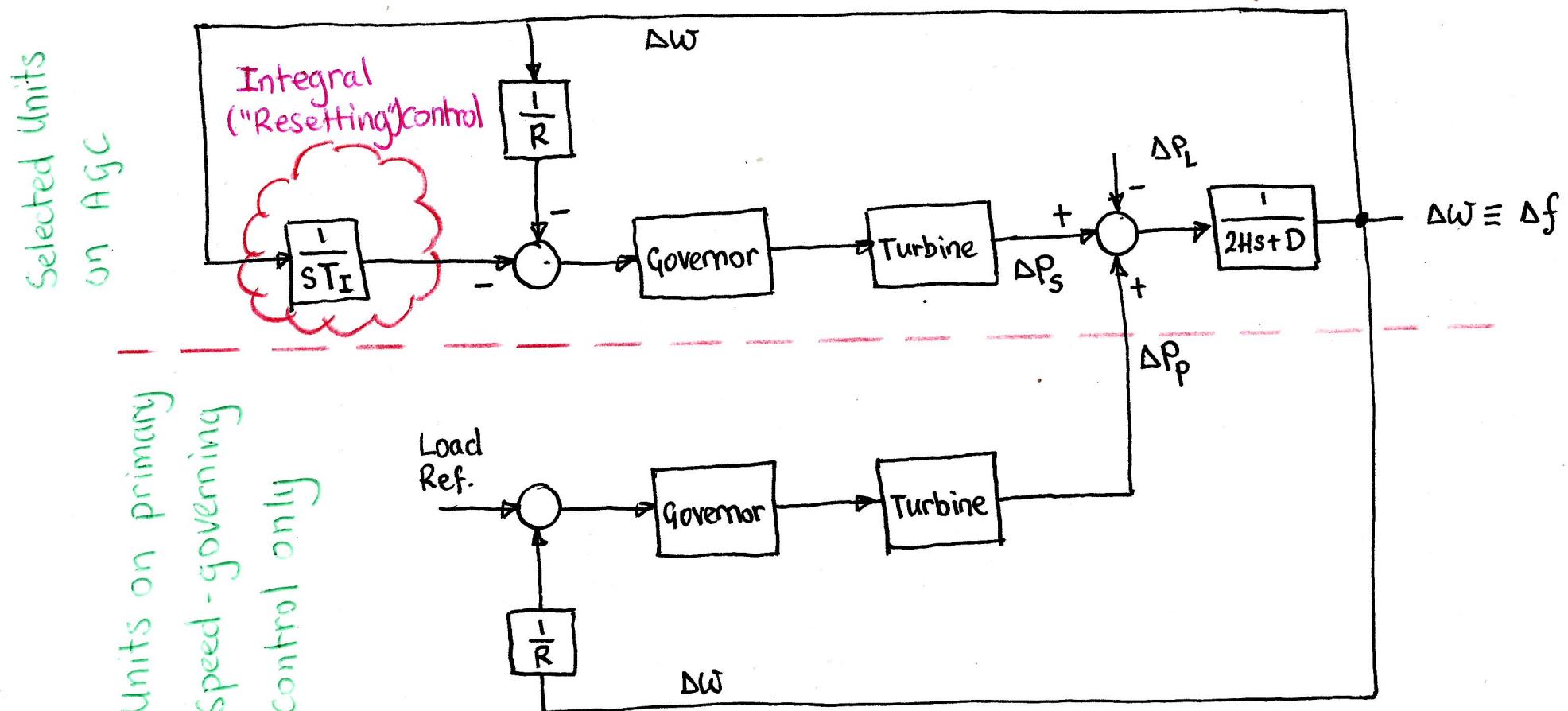
$$\Delta f = -0.0774 \text{ Hz} \quad 26 \text{ of } 32$$

## Primary, Secondary & Tertiary Frequency Controls

- \* Governor action — "primary control"
  - Due to droop characteristic there is a steady-state deviation in frequency
  - All generating units enabled for speed governing will contribute (more-or-less equally in proportion to unit rating) to the overall change in generation.
    - Irrespective of the location of change in load that causes the governing units to change output
    - Interconnector Power flows changed

## Primary, Secondary & Tertiary Frequency Controls

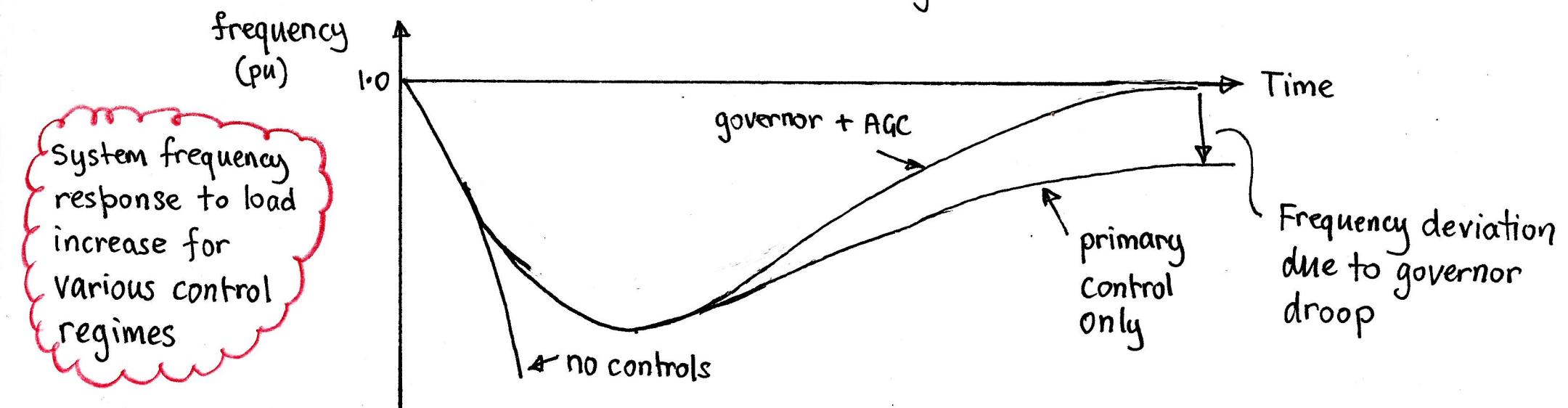
- \* Automatic Generation Control (AGC) - "Secondary Control".
  - Restoration of system frequency to nominal (e.g. 50 Hz)
  - requires supplementary control  $\Rightarrow$  AGC



## Primary, Secondary & Tertiary Frequency Controls

### \* AGC (continued)

- Selected units under AGC
  - Load set-points of AGC units automatically adjusted in response to frequency error
  - AGC is integral (i.e. reset) control
    - ▷ Frequency error ( $-\Delta\omega$ ) reduced to zero in steady-state.



## Primary, Secondary & Tertiary Frequency Controls

- \* Security constrained market disp - "Tertiary Control"
  - Centralized control system that determines change in generator outputs required to meet trend change in load
    - ▢ Generation dispatch determined in response to bids (\$/MWh) from generators to
      - \* achieve least cost
      - \* subject to security constraints.
    - ▢ Dispatch orders sent to generators
      - \* respond by adjusting load reference set-points in a ramp-like fashion over the dispatch interval ( $\sim 5\text{ min}$ )

## Primary, Secondary & Tertiary Frequency Control

- \* Primary, Secondary & Tertiary controls act in concert and merge roughly into the following time frame

Excitation controls  
& rotor dynamics                    0 - 5 seconds

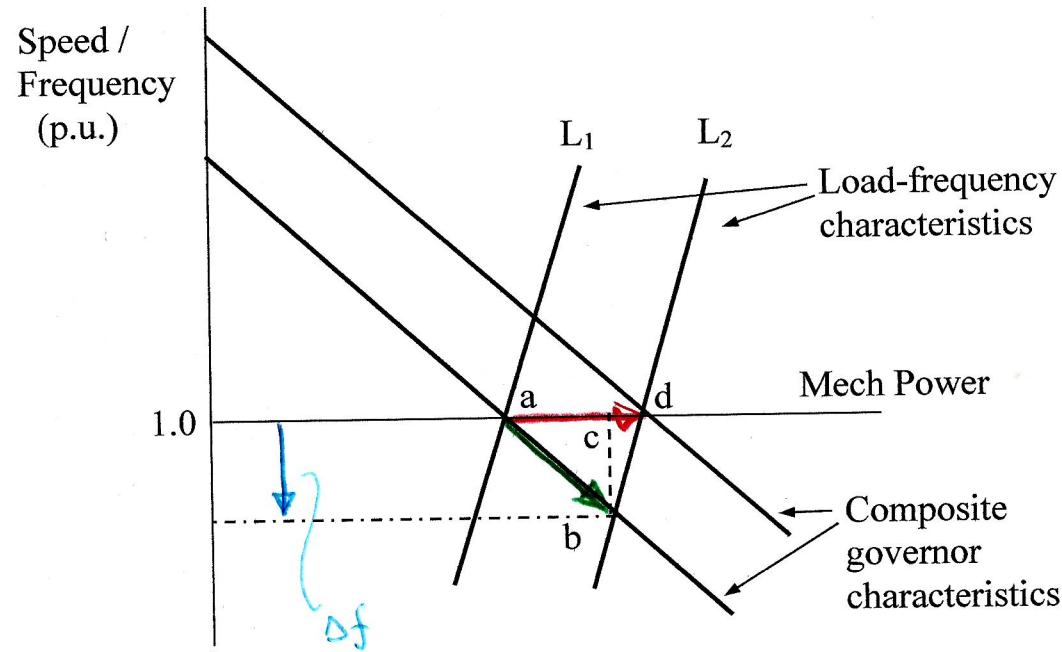
Governor action &  
AGC                                    ~2 s to ~3 min

Market Dispatch &  
boiler controls of  
steam turbines                        2 min to 5+ minutes  
(Dispatch cycle: 5 min)

## Primary, Secondary & Tertiary Frequency Controls

Summary of control actions

→ Consider a load increase  $\underline{a} \rightarrow \underline{d}$  at 50 Hz



\* Security constrained market dispatch

- Load set-points of most cost-effective units increased to meet trend increase in load

- AGC units reduce their outputs in response.

Market Dispatch

AGC action

\* Accommodated by fall in frequency until a steady-state condition is reached at  $\underline{b}$  due to governors

- Due to load-frequency characteristic actual load increase ( $\underline{a} \rightarrow \underline{c}$ ) less than load increase at 50 Hz.
- Mechanical power increase equivalent to  $\underline{a} \rightarrow \underline{c}$

\* Units on AGC receive orders to increase their load reference inputs.

- Units with governors only return from  $\underline{b} \rightarrow \underline{a}$
- AGC units take up load increase  $\underline{a} \rightarrow \underline{d}$