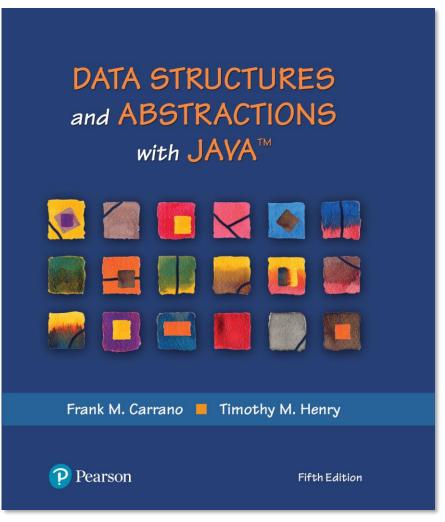
Data Structures and Abstractions with JavaTM

5th Edition



Chapter 9

Recursion

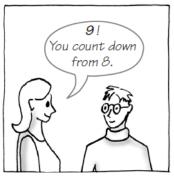
What Is Recursion?

- Consider hiring a contractor to build
 - He hires a subcontractor for a portion of the job
 - That subcontractor hires a sub-subcontractor to do a smaller portion of job
- The last sub-sub- ... subcontractor finishes
 - Each one finishes and reports "done" up the line



Example: The Countdown















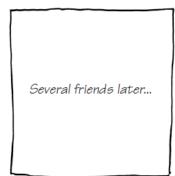




FIGURE 9-1 Counting down from 10



Example: The Countdown

```
/** Counts down from a given positive integer.
    @param integer An integer > 0.
*/
public static void countDown(int integer)
{
    System.out.println(integer);
    if (integer > 1)
        countDown(integer - 1);
} // end countDown
```

Recursive Java method to do countDown.



Definition

- Recursion is a problem-solving process
 - Breaks a problem into identical but smaller problems.
- A method that calls itself is a recursive method.
 - The invocation is a recursive call or recursive invocation.



Design Guidelines

- Method must be given an input value
- Method definition must contain logic that involves this input, leads to different cases
- One or more cases should provide solution that does not require recursion
 - Else infinite recursion
- One or more cases must include a recursive invocation



Programming Tip

- Iterative method contains a loop
- Recursive method calls itself
- Some recursive methods contain a loop and call themselves
 - If the recursive method with loop uses while, make sure you did not mean to use an if statement



Tracing a Recursive Method

countDown(3)

Display 3
Call countDown(2)

countDown(2)

Display 2
Call countDown(1)

countDown(1)

Display 1

FIGURE 9-2 The effect of the method call countDown (3)



Tracing a Recursive Method

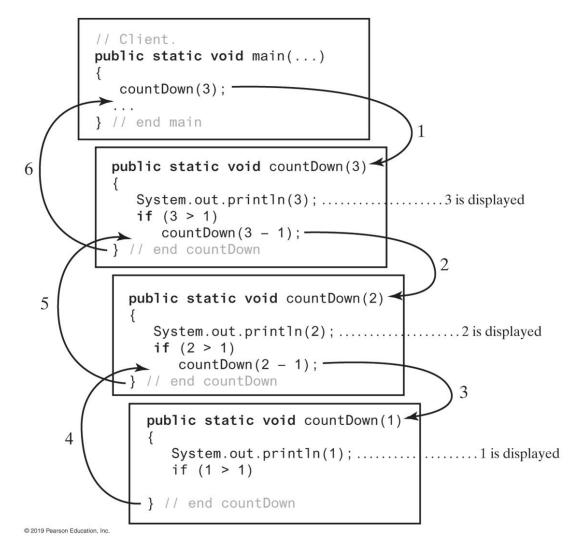


FIGURE 9-3 Tracing the execution of countDown (3)



Stack of Activation Records

- Each call to a method generates an activation record
- Recursive method uses more memory than an iterative method
 - Each recursive call generates an activation record
- If recursive call generates too many activation records, could cause stack overflow



Stack of Activation Records

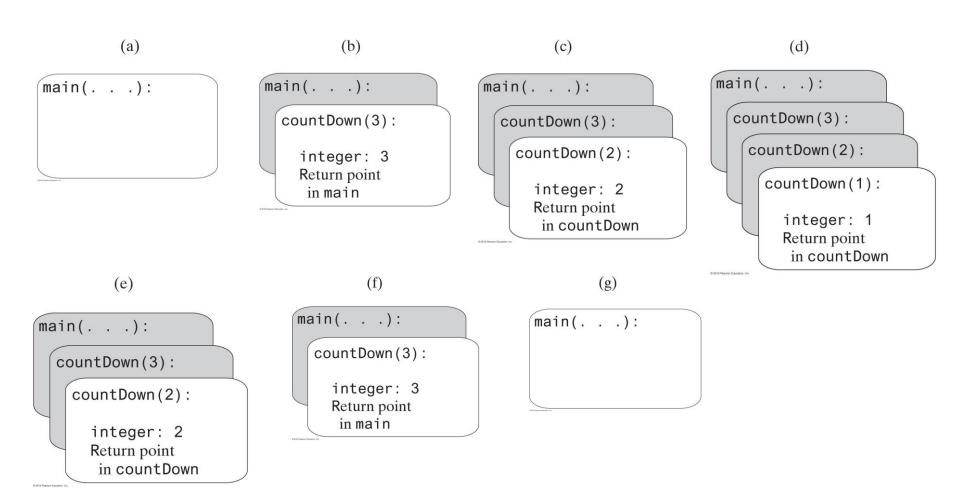


FIGURE 9-4 The stack of activation records during the execution of the call countDown (3)



Recursive Methods That Return a Value

Recursive method to calculate





FIGURE 9-5 Tracing the execution of sumOf(3)

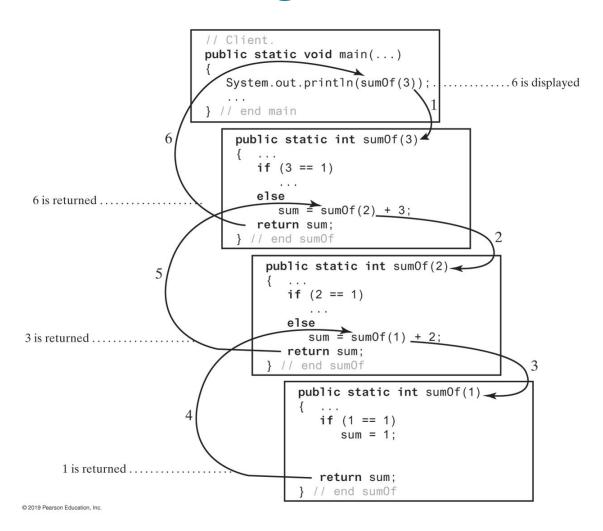


FIGURE 9-5 Tracing the execution of sumOf (3)



Given definition of a recursive method to display array.



```
public static void displayArray(int array[], int first, int last)
{
    System.out.print(array[first] + " ");
    if (first < last)
        displayArray(array, first + 1, last);
} // end displayArray</pre>
```

Starting with array [first]



```
public static void displayArray(int array[], int first, int last)
{
   if (first <= last)
   {
      displayArray(array, first, last - 1);
      System.out.print(array[last] + " ");
   } // end displayArray</pre>
```

Starting with array [last]



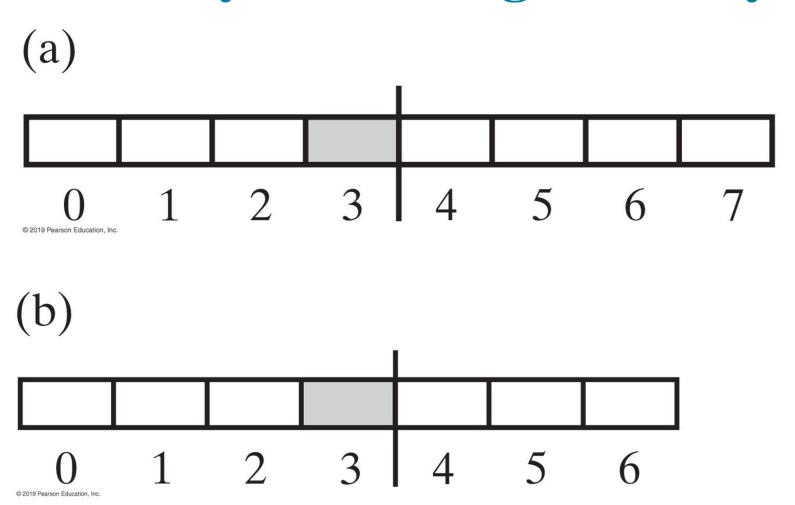


FIGURE 9-6 Two arrays with their middle elements within their left halves



```
public static void displayArray(int array[], int first, int last)
{
   if (first == last)
       System.out.print(array[first] + " ");
   else
   {
      int mid = (first + (last - first) / 2;
      displayArray(array, first, mid);
      displayArray(array, mid + 1, last);
   } // end if
} // end displayArray
```

Processing array from middle.



Displaying a Bag

```
public void display()
{
    displayArray(0, numberOfEntries - 1);
} // end display

private void displayArray(int first, int last)
{
    System.out.println(bag[first]);
    if (first < last)
        displayArray(first + 1, last);
} // end displayArray</pre>
```

Recursive method that is part of an implementation of an ADT often is private.



Recursively Processing a Linked Chain

```
public void display()
{
    displayChain(firstNode);
} // end display

private void displayChain(Node nodeOne)
{
    if (nodeOne != null)
    {
        System.out.println(nodeOne.getData()); // Display data in first node displayChain(nodeOne.getNextNode()); // Display rest of chain
    } // end displayChain
```

Display data in first node and recursively display data in rest of chain.



Recursively Processing a Linked Chain

```
public void displayBackward()
 displayChainBackward(firstNode);
} // end displayBackward
private void displayChainBackward(Node nodeOne)
 if (nodeOne != null)
   displayChainBackward(nodeOne.getNextNode());
   System.out.println(nodeOne.getData());
 } // end if
} // end displayChainBackward
```

Displaying a chain backwards. Traversing chain of linked nodes in reverse order easier when done recursively.



Time Efficiency of Recursive Methods

```
public static void countDown(int n)
{
    System.out.println(n);
    if (n > 1)
        countDown(n - 1);
} // end countDown
```

Using proof by induction, we conclude method is O(n).



Time Efficiency of Computing x^n

$$x^n = (x^{n/2})^2$$
 when n is even and positive $x^n = x (x^{(n-1)/2})^2$ when n is odd and positive $x^0 = 1$

Efficiency of algorithm is $O(\log n)$



Tail Recursion

- When the last action performed by a recursive method is a recursive call.
- In a tail-recursive method, the last action is a recursive call
- This call performs a repetition that can be done by using iteration.
- Converting a tail-recursive method to an iterative one is usually a straightforward process.

```
public static void countDown(int n)
{
    System.out.println(n);
    if (n > 1)
        countDown(n - 1);
} // end countDown
```



Using a Stack Instead of Recursion

Converting a recursive method to an iterative one

```
public static void countDown(int integer)
{
   if (integer >= 1)
   {
      System.out.println(integer);
      countDown(integer - 1);
   } // end if
} // end countDown
```

An iterative version

```
public static void countDown(int integer)
{
   while (integer >= 1)
   {
      System.out.println(integer);
      integer = integer - 1;
   } // end while
} // end countDown
```



Using a Stack Instead of Recursion

An iterative displayArray to maintain its own stack

```
public void displayArray(int first, int last)
 boolean done = false;
 StackInterface<Record> programStack = new LinkedStack<>();
 programStack.push(new Record(first, last));
 while (!done && !programStack.isEmpty())
   Record topRecord = programStack.pop();
   first = topRecord.first;
   last = topRecord.last;
   if (first == last)
     System.out.println(array[first] + " ");
   else
     int mid = first + (last - first) / 2;
     // Note the order of the records pushed onto the stack
     programStack.push(new Record(mid + 1, last));
     programStack.push(new Record(first, mid));
   } // end if
 } // end while
} // end displayArray
```



End

Chapter 9

