



PRACTICA 1

CINEMATICA DE ROBOTS



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CODIGO:

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syms theta1
syms theta2
syms theta3
syms d1
syms d2
T1=[cos(theta1),-sin(theta1),0,0;0,0,-1,0;sin(theta1),cos(theta1),0,0;0,0,0,1]
syms L1
T2=[cos(theta2),-sin(theta2),0,0;0,0,1,d1;sin(theta2),cos(theta2),0,0;0,0,0,1]
syms L2
T3=[cos(theta3),-sin(theta3),0,L2;sin(theta3),cos(theta3),0,0;0,0,1,d2;0,0,0,1]
syms ans
ans =T1*T2*T3

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$$\begin{aligned}
 T_1^0 &= \begin{pmatrix} \cos(\theta_1) & -\sin(\theta_1) & 0 & 0 \\ 0 & 0 & -1 & 0 \\ \sin(\theta_1) & \cos(\theta_1) & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \\
 T_2^1 &= \begin{pmatrix} \cos(\theta_2) & -\sin(\theta_2) & 0 & L_1 \\ \sin(\theta_2) & \cos(\theta_2) & 0 & 0 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{pmatrix} \\
 T_3^2 &= \begin{pmatrix} \cos(\theta_3) & -\sin(\theta_3) & 0 & L_2 \\ \sin(\theta_3) & \cos(\theta_3) & 0 & 0 \\ 0 & 0 & 1 & d_2 \\ 0 & 0 & 0 & 1 \end{pmatrix} \\
 T_3^0 &= \begin{pmatrix} \sigma_1 & -\cos(\theta_3) \sigma_3 - \sin(\theta_3) \sigma_2 & 0 & L_2 \sigma_2 + L_1 \cos(\theta_1) \\ 0 & 0 & -1 & -d_1 - d_2 \\ \cos(\theta_3) \sigma_3 + \sin(\theta_3) \sigma_2 & \sigma_1 & 0 & L_2 \sigma_3 + L_1 \sin(\theta_1) \\ 0 & 0 & 0 & 1 \end{pmatrix}
 \end{aligned}$$

where

$$\sigma_1 = \cos(\theta_3) \sigma_2 - \sin(\theta_3) \sigma_3$$

$$\sigma_2 = \cos(\theta_1) \cos(\theta_2) - \sin(\theta_1) \sin(\theta_2)$$

$$\sigma_3 = \cos(\theta_1) \sin(\theta_2) + \cos(\theta_2) \sin(\theta_1)$$

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Flavio A.

Practica #1

	a_{i-1}	α_{i-1}	d_i	θ_i
1	0	90°	0	θ_1
2	L_1	0	d_1	θ_2
3				

$$T_1^0 = \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ \sin \theta_1 & \cos \theta_1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_2^1 = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 & 0 & L_1 \\ \sin \theta_2 & \cos \theta_2 & 0 & 0 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_3^2 = \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & L_2 \\ \sin \theta_3 & \cos \theta_3 & 0 & d_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$T_3^0 = T_1^0 \cdot T_2^1 \cdot T_3^2$$

$$= \begin{bmatrix} \cos \theta_3 \cdot (\cos \theta_1 \cdot \cos \theta_2 - \sin \theta_1 \cdot \sin \theta_2) - \sin \theta_3 \cdot (\cos \theta_1 \cdot \sin \theta_2 + \sin \theta_1 \cdot \cos \theta_2) & \cos \theta_3 \cdot (\cos \theta_1 \cdot \sin \theta_2 + \sin \theta_1 \cdot \cos \theta_2) + \sin \theta_3 \cdot (\cos \theta_1 \cdot \cos \theta_2 - \sin \theta_1 \cdot \sin \theta_2) & \cos \theta_3 \cdot (-\sin \theta_1) - \sin \theta_3 \cdot (\cos \theta_1) & L_1 \cdot \cos \theta_3 \cdot \cos \theta_2 + L_2 \cdot \cos \theta_3 \cdot \sin \theta_2 + d_1 \cdot \cos \theta_3 \\ \sin \theta_3 \cdot (\cos \theta_1 \cdot \cos \theta_2 - \sin \theta_1 \cdot \sin \theta_2) + \cos \theta_3 \cdot (\cos \theta_1 \cdot \sin \theta_2 + \sin \theta_1 \cdot \cos \theta_2) & \sin \theta_3 \cdot (\cos \theta_1 \cdot \sin \theta_2 + \sin \theta_1 \cdot \cos \theta_2) - \cos \theta_3 \cdot (\cos \theta_1 \cdot \cos \theta_2 - \sin \theta_1 \cdot \sin \theta_2) & \sin \theta_3 \cdot (-\sin \theta_1) + \cos \theta_3 \cdot (\cos \theta_1) & L_1 \cdot \sin \theta_3 \cdot \cos \theta_2 + L_2 \cdot \sin \theta_3 \cdot \sin \theta_2 + d_1 \cdot \sin \theta_3 \\ 0 & 0 & -\sin \theta_1 \cos \theta_3 - \cos \theta_1 \sin \theta_3 & -L_1 \sin \theta_1 \cos \theta_3 - L_2 \sin \theta_1 \sin \theta_3 - d_1 \sin \theta_1 \\ 0 & 0 & \cos \theta_1 \cos \theta_3 - \sin \theta_1 \sin \theta_3 & L_1 \cos \theta_1 \cos \theta_3 + L_2 \cos \theta_1 \sin \theta_3 + d_1 \cos \theta_1 \end{bmatrix}$$