

## HW15: Backpropagation

Complete the following page from the "Neural Networks and Backpropagation" lecture notes:

### NEURAL NETWORKS AND BACKPROPAGATION

⑫ In summary (for our 3-layer example):

$$\frac{\partial \pi}{\partial \pi_j} = a'(\pi_j) \sum_{h=1}^2 \ddot{w}_{hj} \frac{\partial \pi}{\partial \pi_h}$$

and for the general case:

$$\frac{\partial \pi^{(M)}}{\partial \pi^{(M)}} = \boxed{\phantom{0}} \quad \leftarrow \text{base case}$$

$$\frac{\partial \pi^{(M)}}{\partial \pi_j^{(M)}} = \boxed{\phantom{0}} \quad \leftarrow \text{recursive step}$$

⑬ Putting it all together, we have cobbled together a strategy for computing every partial derivative  $\frac{\partial L}{\partial w_{ij}^{(M)}}$ :

BACKPROPAGATION:

(a) for  $m$  in range( $\boxed{\phantom{0}}$ ) and  $j$  in range( $\boxed{\phantom{0}}$ )  
compute  $\frac{\partial \pi^{(M)}}{\partial \pi_j^{(M)}} = \boxed{\phantom{0}}$

(b)  $\frac{\partial L}{\partial w_{ij}^{(M)}} = \boxed{\phantom{0}} \cdot \frac{\partial \pi^{(M)}}{\partial \pi_j^{(M)}}$

Because we compute the partial derivatives  $\frac{\partial \pi^{(M)}}{\partial \pi_j^{(M)}}$  starting from the final layer  $M$  and moving back, we call it backpropagation.