Det's reconsider the task of classifying vsequences. Suppose that a DNA sequence is in a particular family if it contains 3 or more "G" bases, e.g.

AGGTAACG

GATAGGGATA

belong to the family, but:

TATACCAGATTA

GATTACAG'ATTACA

do not.

3 One could try using a CNN, but maybe we don't know upfront to be maximum length of a DNA sequence. That's problematic, because we need the input layer to be an upper bound on any sequence length

"A"
$$X_1 \rightarrow$$
"G" $X_2 \rightarrow$

$$\vdots \qquad \vdots \qquad \vdots \qquad \vdots$$

$$\|T\| X_N \rightarrow$$

3) Alternatively, we could try to mimic the process of identifying positive sequences programmatically: this looks like lythm, but let's count from def f(X: string)

Q = [False, False]

for x in X:

if x == "G" and not Q[1]:

Q[1] = True

elif x == "G" and not Q[2]:

Q[2] = True

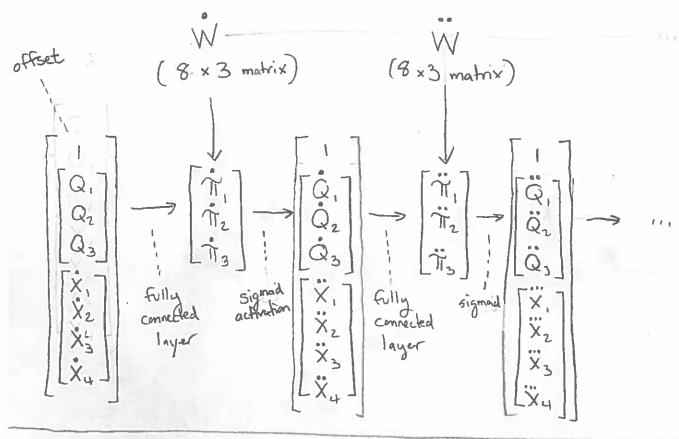
elif x == "G" and not Q[3]:

O[3] = True

(4) We could try encoding this as a neural network, in which rather than giving the entire input sequence as input to the first layer, we give the sequence one character at a time to each layer.

First, let's represent an input sequence AGGTG as one-hot vectors

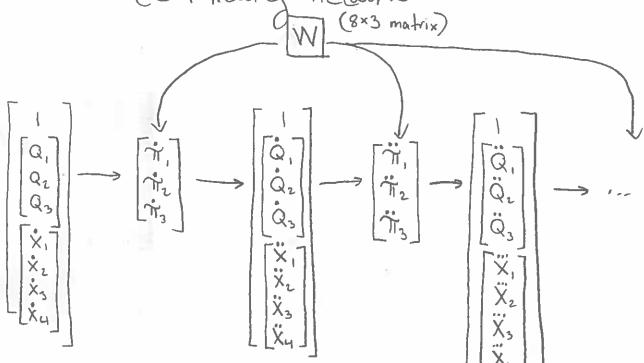
5) The neural network representation of our Python function could look as follows:



But just as, in a for-loop, the logic doesn't change from iteration to iteration, there's no need to change our weight matrix (which encodes the logic) from iteration to iteration.

If we share these parameters between all layers, we obtain the following network:

(8×3 matrix)



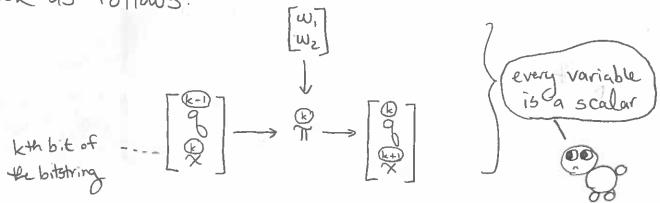
This is called a recurrent neural network (RNN).

3) Observe that you can specify an RNN by showing how a single layer looks:

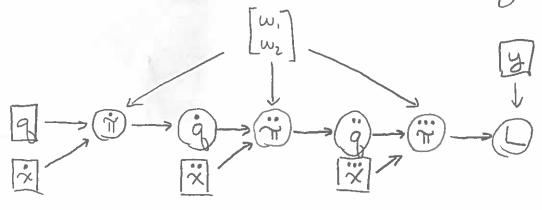
Where
$$R = W^T \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$
, $R = a(R)$

1) Although we had weight sharing in CNNs, his is the first time we've encountered weight sharing between layers, so it's worth a look at how gradients are computed.

Consider an RNN for bitstrings, where the state vectors Q each have size I for simplicity, we won't use an offset. Thus, the RNN layers look as follows:

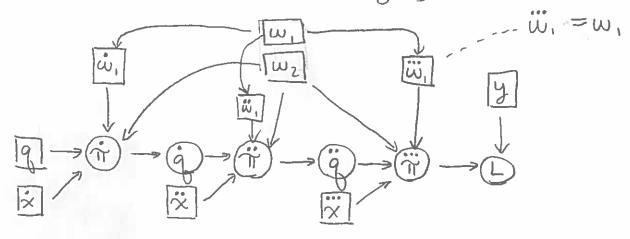


10) Suppose we run this RNN on a bitstring of length 3:



I) Exercise: Compute
$$\frac{\partial L}{\partial w}$$
 for datum $(x,y) = ("101", 15)$

It's more straightforward to apply the Chain Rule if we create copies of w, for each layer, i.e.



12 Now, we can use ziv, iv, ii, z as a separating set between w, and it:

$$\frac{\partial L}{\partial w} = \frac{\partial L}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial w} + \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial \tilde{w}} + \frac{\partial \tilde{w}}{\partial \tilde{w}} + \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial \tilde{w}} + \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial \tilde{w}}{\partial \tilde{w}} + \frac{\partial \tilde{w}}{\partial \tilde{w}} \frac{\partial$$

(13) The remaining derivatives can be computed efficiently through backpropagation:

$$\frac{\partial \vec{r}}{\partial \vec{w}} = 9$$

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where:

$$\frac{\partial \ddot{\pi}}{\partial \ddot{\pi}} = \frac{\partial \ddot{\pi}}{\partial \ddot{q}} \frac{\partial \ddot{q}}{\partial \ddot{\pi}} = \ddot{w}_{1} \cdot a'(\ddot{\pi}) = w_{1} \cdot a'(\ddot{\pi})$$

$$\frac{\partial \ddot{\pi}}{\partial \ddot{\pi}} = \frac{\partial \ddot{\pi}}{\partial \dot{q}} \cdot \frac{\partial \dot{q}}{\partial \dot{\pi}}$$

$$= \frac{\partial \ddot{\pi}}{\partial \ddot{\pi}} \cdot \frac{\partial \ddot{\pi}}{\partial \dot{q}} \cdot \frac{\partial \dot{q}}{\partial \dot{\pi}} = (w_{1} \cdot a'(\ddot{\pi})) \ddot{w}_{1} \cdot a'(\ddot{\pi}) = w_{1}^{2} \cdot a'(\ddot{\pi}) a'(\ddot{\pi})$$

$$= \frac{\partial \ddot{\pi}}{\partial \ddot{\pi}} \cdot \frac{\partial \ddot{\pi}}{\partial \dot{q}} \cdot \frac{\partial \dot{q}}{\partial \dot{\pi}} = (w_{1} \cdot a'(\ddot{\pi})) \ddot{w}_{1} \cdot a'(\ddot{\pi}) = w_{1}^{2} \cdot a'(\ddot{\pi}) a'(\ddot{\pi})$$

(4) So then:

$$\frac{\partial L}{\partial w_{i}} = -2(y-\ddot{n})\left(\ddot{g} + \dot{g} \cdot w_{i} \cdot a'(\ddot{n}) + g \cdot w_{i}^{2} \cdot a'(\ddot{n}) \cdot a'(\ddot{n})\right)$$

15) Doing the forward pass on the specific data, we get:

$$\boxed{0} \rightarrow \boxed{1} \rightarrow \boxed{1} \rightarrow \boxed{4}$$

$$\boxed{0} \rightarrow \boxed{1} \rightarrow \boxed{4}$$

$$\boxed{0} \rightarrow \boxed{1} \rightarrow \boxed{4}$$

To So our partial derivative evaluates to:

$$\frac{\partial L}{\partial w_{1}} = -2(15-17)(4+1.4.1+0.4^{2}.1.1)$$

$$= -2(-2)(8)$$