

# StereoVision

**Paulo Dias**





- Introduction - Stereopsis
- Camera models and Camera calibration
- Stereo Vision
  - Frontal parallel arrangement
  - Epipolar geometry
  - Essential and Fundamental Matrix
  - Image rectification
  - Template Matching
  - Stereo Matching



What is stereo?

Where is it coming from?

Where can you see it or use it?



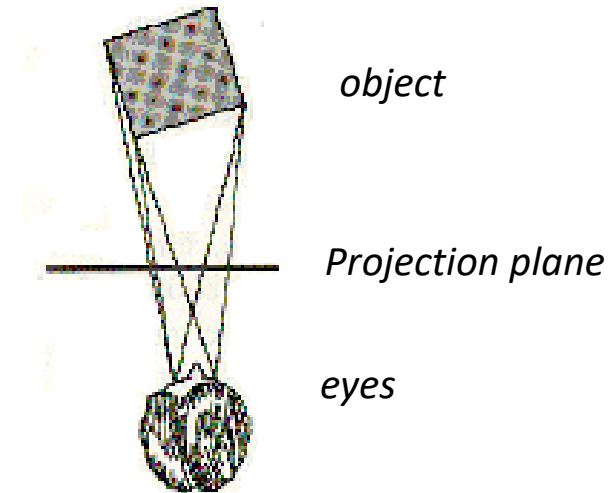
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- Many of the **perceptual cues** we use to visualize 3D structure are **available** in **2D projections**
- Such cues include:
  - occlusion (one object partially covering another)
  - perspective (point of view)
  - familiar size (we know the real-world sizes of many objects)
  - atmospheric haze (objects further away look more washed out)
- **Four cues are missing** from single 2D views:
  - stereo parallax - seeing a different image with each eye
  - movement parallax - seeing different images when we move the head
  - Accommodation - the eyes' lenses focus on the object of interest
  - Convergence - both eyes converge on the object of interest

Stereo = "solid" or "**three-dimensional**"  
opsis = appearance or **sight**

Also: "binocular vision",  
"binocular depth perception"  
"stereoscopic depth perception"



- Stereopsis is the impression of **depth** that is perceived when a scene is viewed with **both eyes** by someone with normal binocular vision
- Binocular disparity is due to the **different position** of our two **eyes**



- Depth perception in stereo is based on stereopsis:
  - when the brain registers and fuses two images
  - **Image parallax** means that the two eyes register different images (horizontal shift)
  - The amount of shift depends on the “inter-pupillary distance” (IPD) (varies for each person in the range of 53-73 mm)
  - Works in the **near field** (to a few meters from the eye)

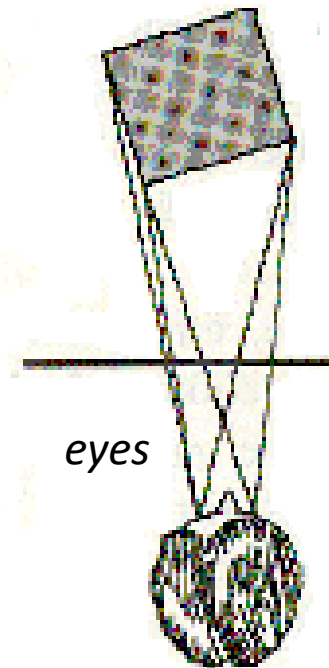


*object*

(Hearn and Baker, 2002)



*Right eye image    Left eye image*



*eyes*

*Projection  
plane*



# Stereopsis: implications for Graphic devices



- Present two images of the same scene
  - Two images can be presented
    - at the **same time** on two displays
- HMD**
- **time-sequenced** on one display
    - active** glasses
  - **spatially-sequenced** on one display
    - auto-stereoscopic** displays



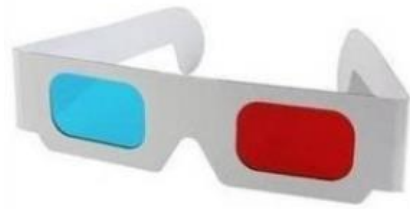
Left eye, right eye images  
(Burdea and Coiffet., 2003)



# Common ways to produce 3D sensation



- Anaglyphs: two colored images and color coded glasses (red/cyan(green))



- Two images with different light polarization and polarizing glasses
  - Linear and circular



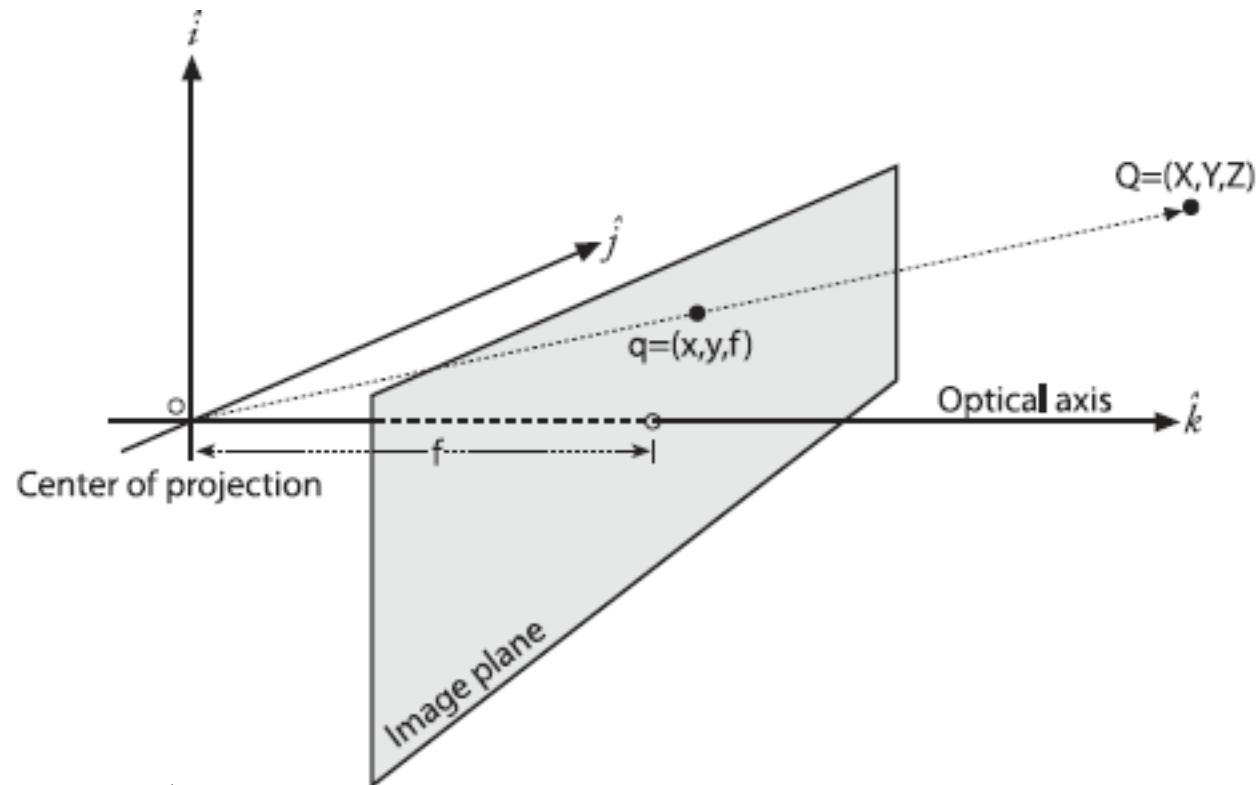
- Double frame-rate displays combined with LCD shutter glasses
- Autostereoscopic displays
  - Parallax barrier and lenticular lens
- Head Mounted Displays (HMDs)
- and “exotic displays”





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- pinhole camera model



- We get

$$x = f \frac{X}{Z}$$

$$y = f \frac{Y}{Z}$$



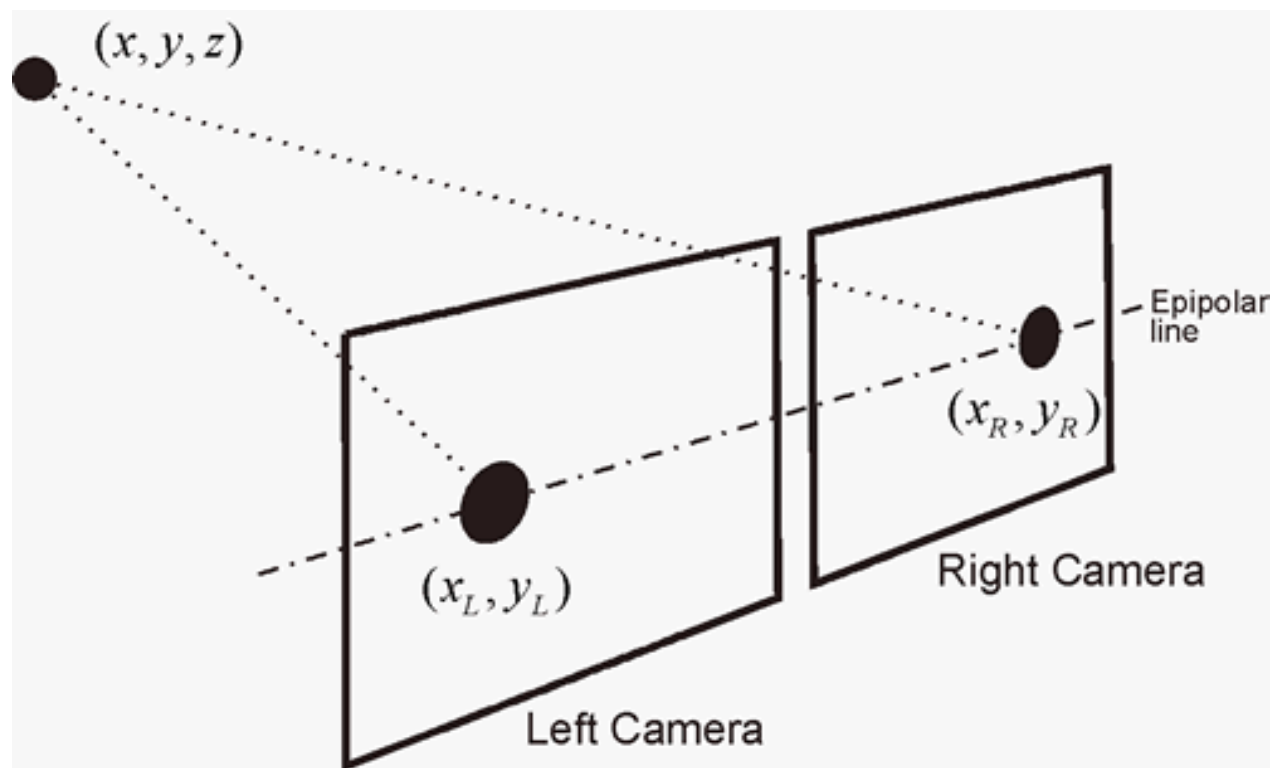
- OpenCV Camera model:
  - 4 intrinsic parameters:
    - Focal distance:  $f_x, f_y$
    - Optical centre:  $c_x, c_y$
  - 5 distortion parameters
    - Lens distortion:  $k_1, k_2, k_3, p_1, p_2$
  - 6 extrinsic parameters:
    - Rotation:  $r_x, r_y, r_z$
    - Translation:  $t_x, t_y, t_z$

Total: **15 parameters**
- Other models: Tsai, Heikkila, Zhang



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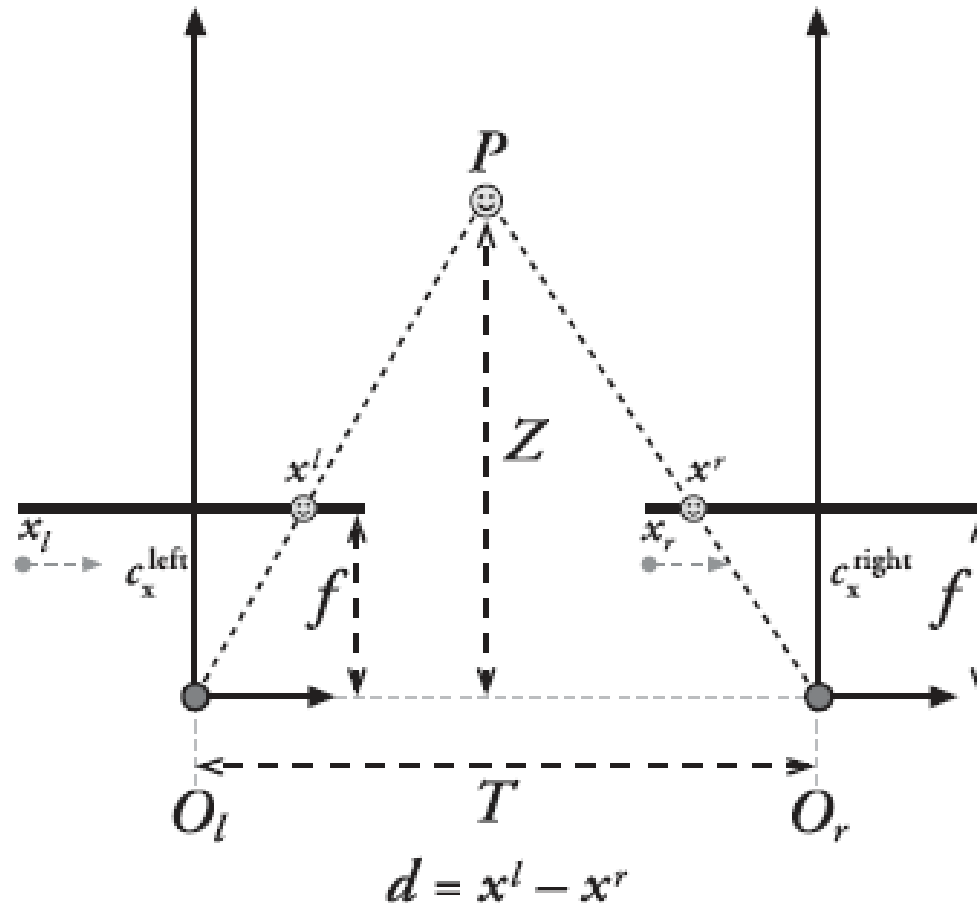
- Capability to define **depth from 2 images**
- Possible by computing **correspondences** between two images



# Frontal parallel arrangement

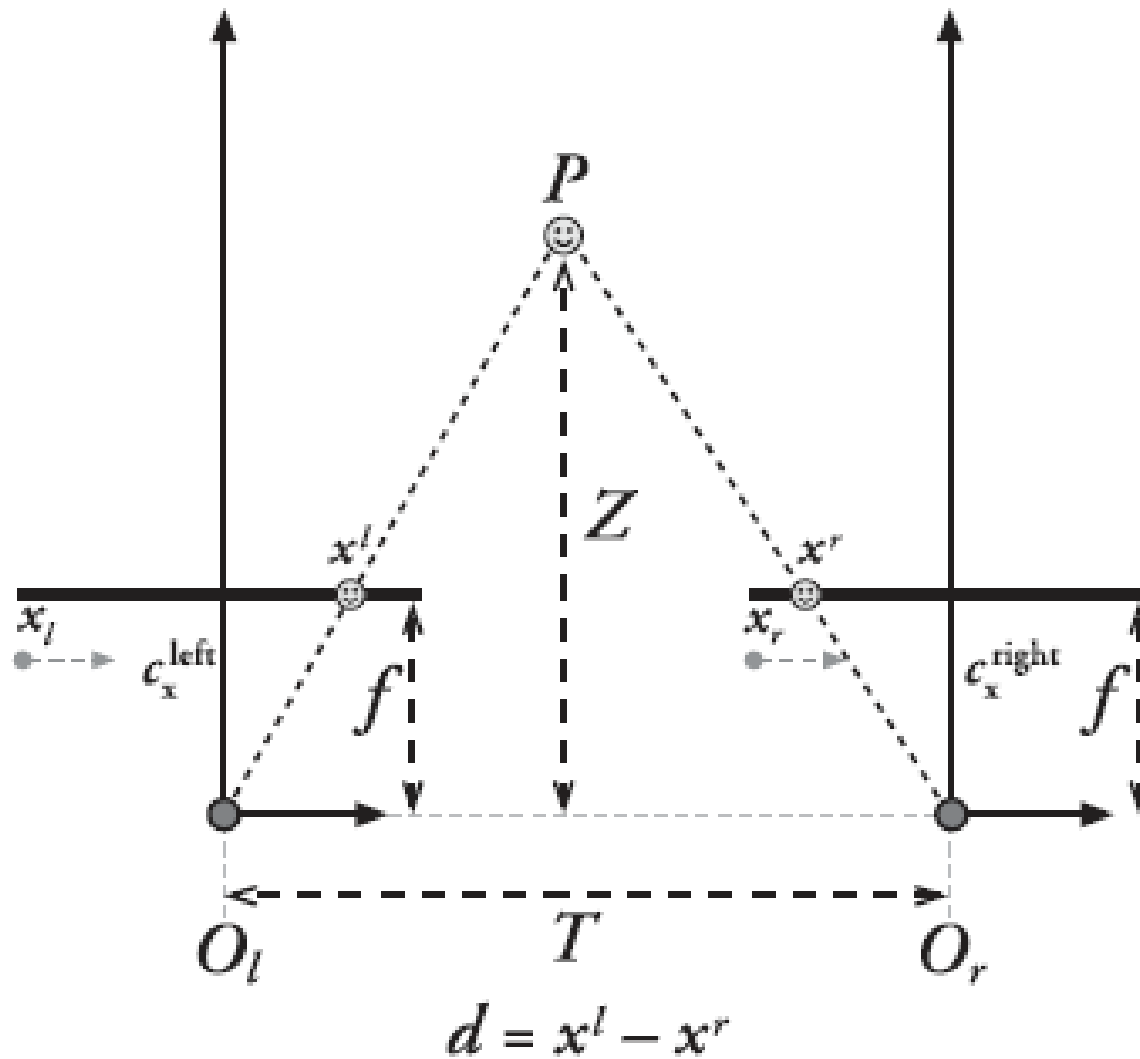


- Two perfectly aligned, coplanar cameras with same focal distance:





# Frontal parallel arrangement



- $Z=?$



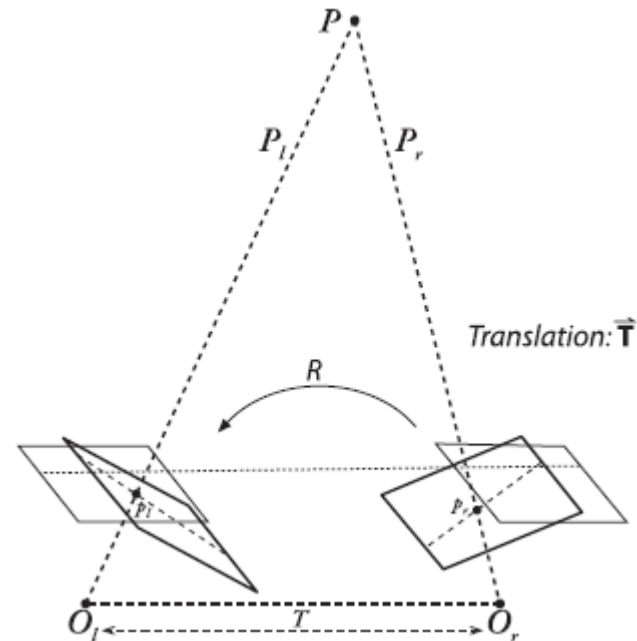
- $\frac{T}{Z} = \frac{T-(x^l-x^r)}{(Z-f)}$  then  $Z = \frac{T(Z-f)}{T-(x^l-x^r)}$ ,
- $TZ - Z(x^l - x^r) = TZ - fT$
- So :  $Z = \frac{fT}{d}$

=> Stereo system have good depth resolution for **close objects** since depth is inversely proportional to disparity.

# Frontal parallel arrangement



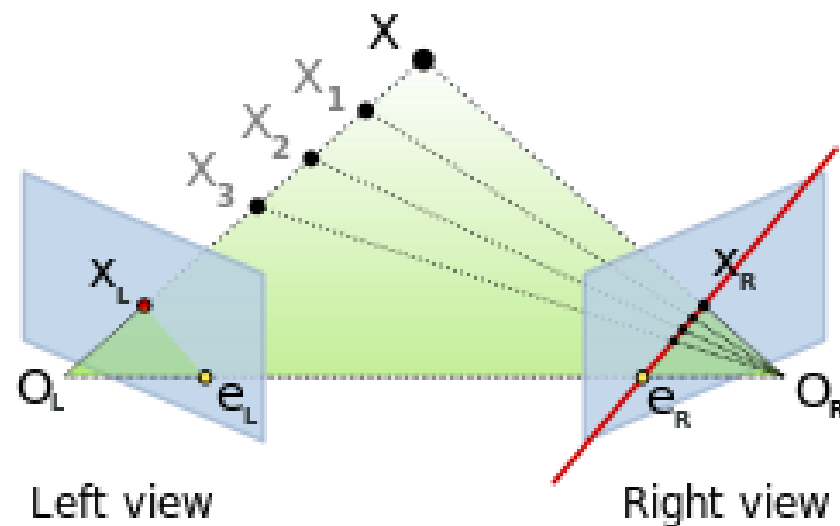
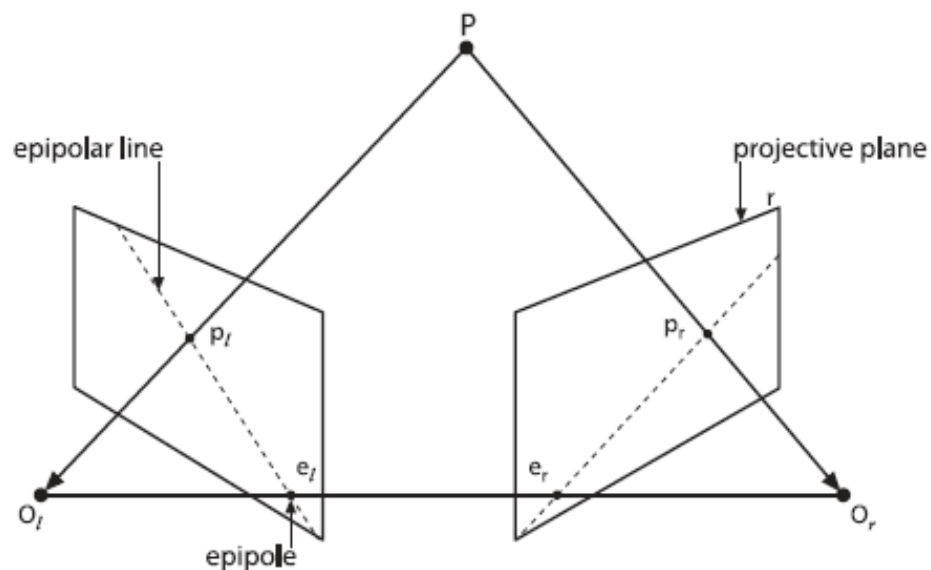
- Easy to relate correspondence to depth in frontal parallel arrangement
- Problem: how to map **real configuration** to frontal **parallel arrangement**.





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- An epipole is a **projection of the optical centre** of a camera on the other image plane



- <http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.html>



- What is it useful for?:
    - Given a point in an image, its corresponding point in the other image lies on the corresponding epipolar line
    - Order is preserved (given 2 points A e B in a given order in one images, order will be the same in the other image)
- =>Epipolar geometry transform a **2D search** (in image) into a **1D search (along epipolar lines)** saving resources and avoiding errors.



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- Epipolar Geometry is defined by:
  - Information about relative position between the cameras (rotation and translation) [extrinsic] – **Essential Matrix** (E)
  - Intrinsic parameters of the cameras (focal length, lens distortion, optical centre, etc...) – **Fundamental Matrix** (F)





- Matrix that **maps a 3D point** in one image with its **corresponding 3D point** on the other image considering translation and rotation between cameras:
- $p_l^T E p_r = 0$
- $p_l$  and  $p_r$  are in camera 3D coordinate system



- Matrix that **maps a pixel** in one image with its **corresponding pixel** on the other image considering rotation, translation and intrinsic parameters of the cameras:
- $u_l^T F u_r = 0$
- $u_l$  e  $u_r$  are in image 2D coordinate system



- Fundamental and Essential matrices represent the **transformation between the stereo pair images**. Fundamental matrix operates in image coordinates (pixels) and Essential matrix operates in physical coordinates.
- Possible to evaluate with 8 point correspondences (eight point algorithm: <http://www.cs.unc.edu/~marc/tutorial/node54.html>)



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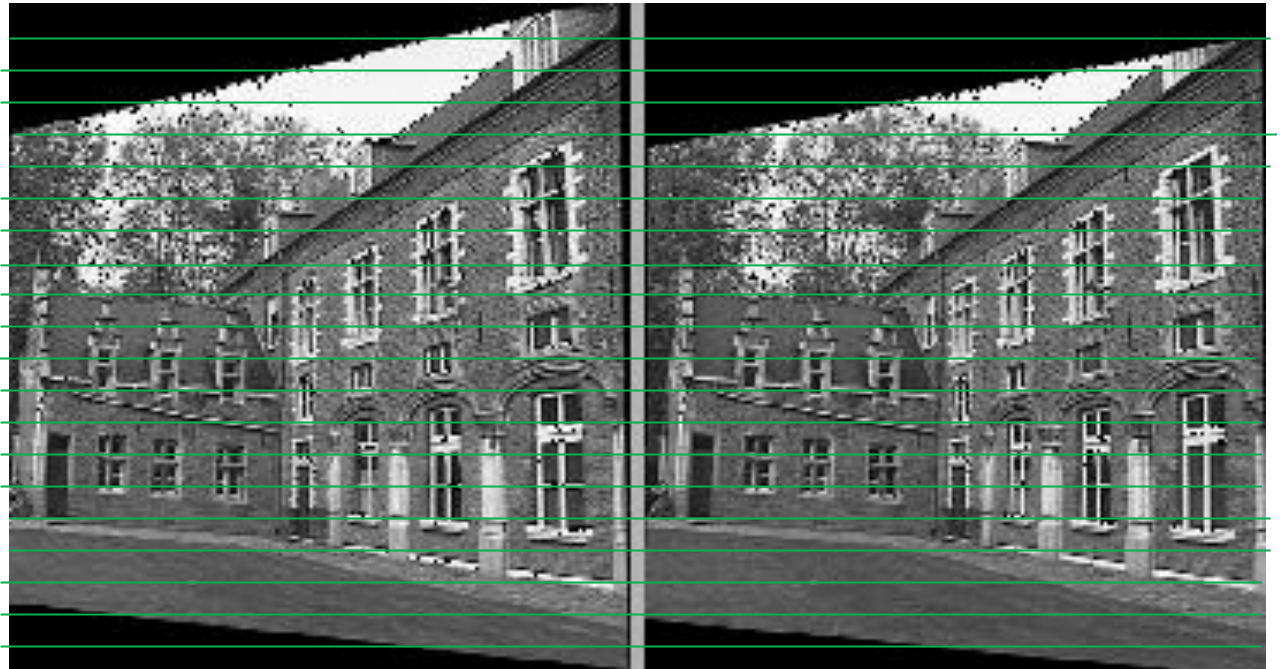


- Given the fundamental matrix, it is possible to **rectify an image by aligning epipolar lines** in rows on the two rectified images getting a **frontal parallel arrangement**.

Original images

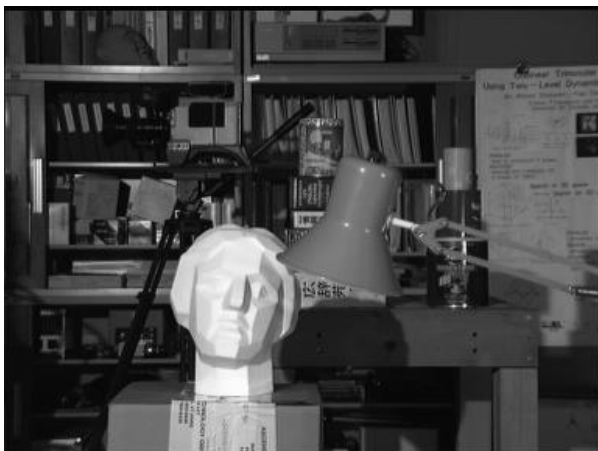


Rectified images



From Visual 3D Modeling from Images (<http://www.cs.unc.edu/~marc/tutorial/>)

- In rectified images, **disparity** is simply **difference** between pixel coordinates  $x_l$  and  $x_r$ .



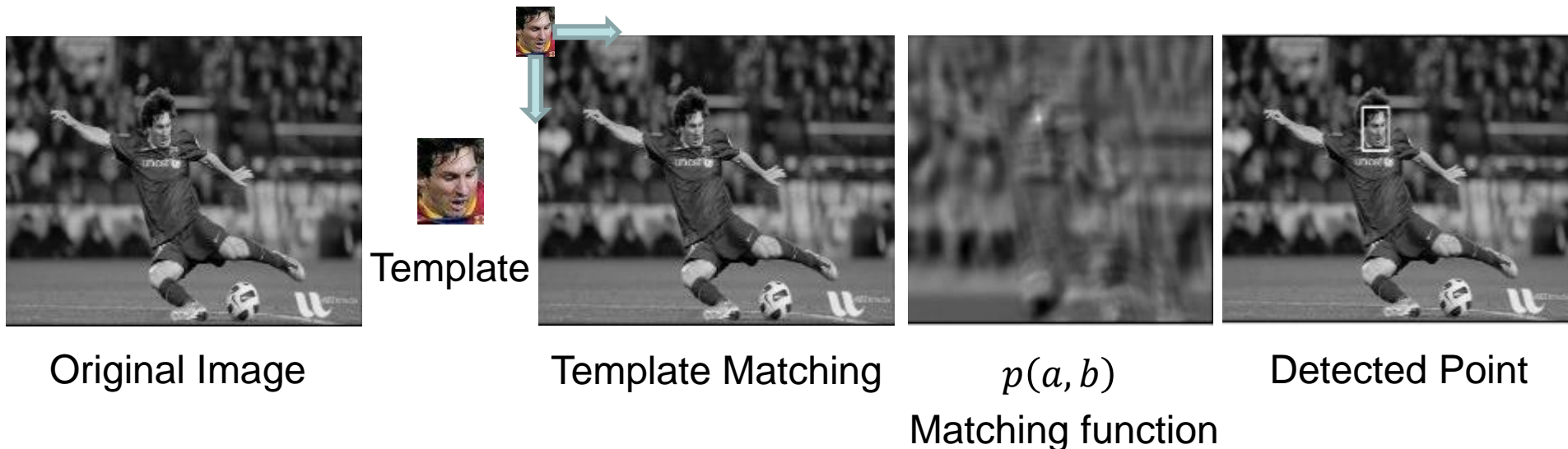
Tsukuba head and lamp stereo dataset



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- Template matching is moved to all positions  $(u, v)$  in image and computes  $p(a, b)$  to evaluate how well template matches image in that position

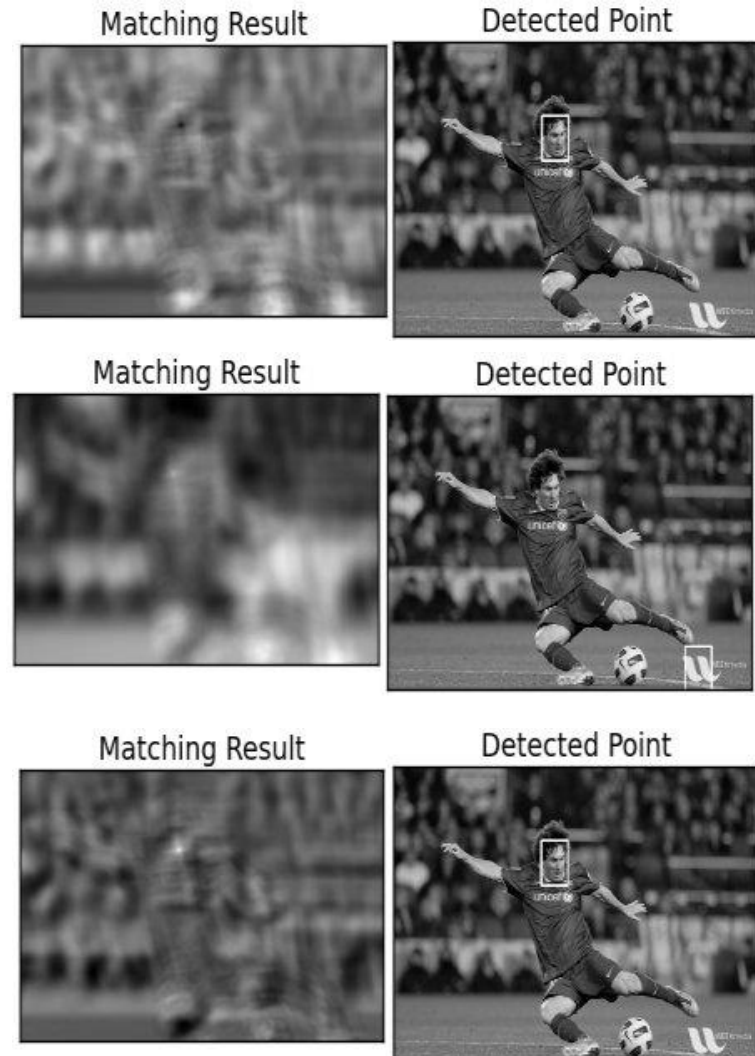


- Object is on image at position where occurs  $\max(p(a, b))$  if  $\max(p(a, b)) > \text{threshold}$

- Several possible functions to compare template and image  $p(a, b)$ :

- Square difference matching
- Correlation matching
- Correlation coefficient matching

– ...



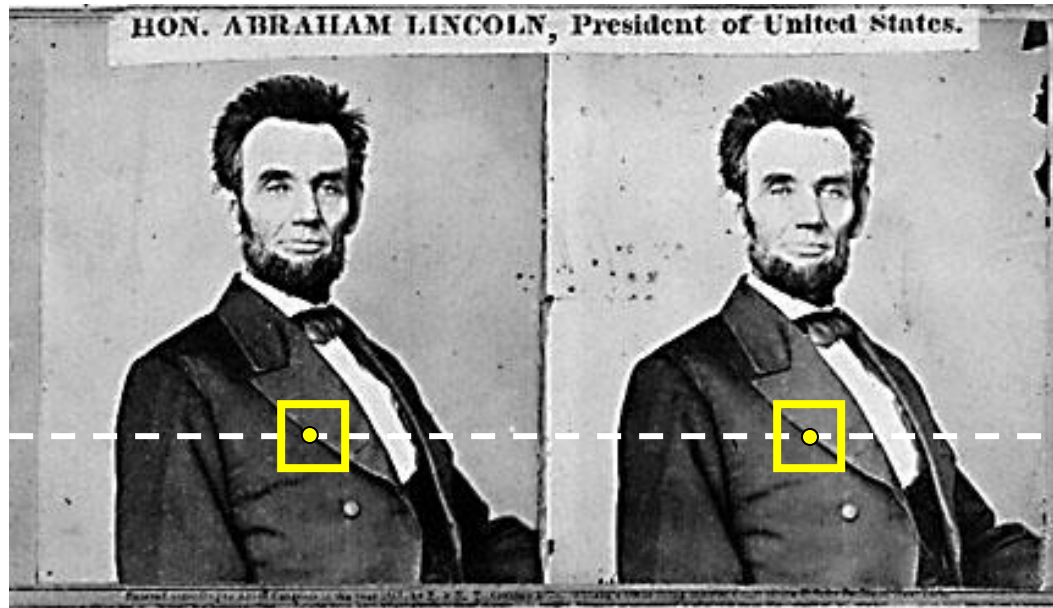


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- Match Pixels in Conjugate Epipolar Lines
  - This is a tough problem
  - Numerous approaches
    - A good survey and evaluation:  
<http://vision.middlebury.edu/stereo/>

# Basic stereo algorithm

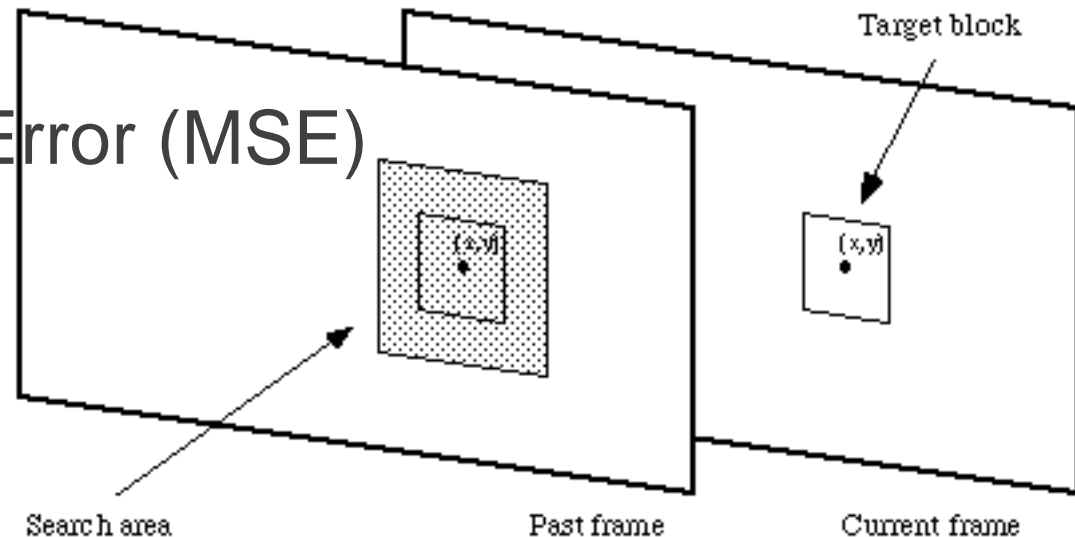


For each epipolar line

For each pixel in the left image

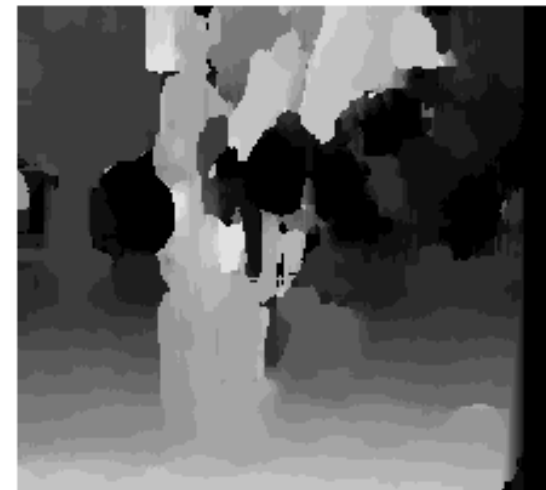
- compare with every pixel on same epipolar line in right image
- pick pixel with minimum match cost

- Block Matching:
  - Divides an image into macroblocks and compare each with a corresponding block and its neighbours in a another image
- Several Metrics
  - Mean difference or Mean Absolute Difference (MAD)
  - Mean Squared Error (MSE)
  - ...





$W = 3$



$W = 20$

## Effect of window size

- Smaller window
- Larger window

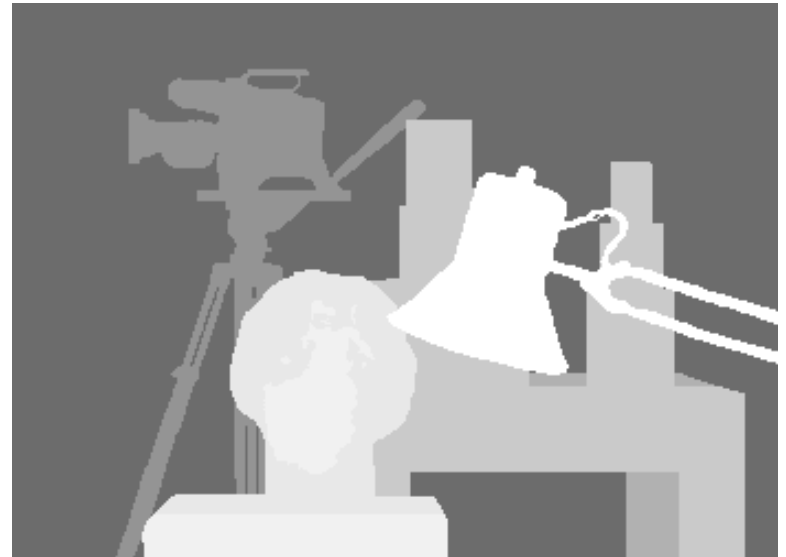
## Better results with *adaptive window*

- T. Kanade and M. Okutomi, [A Stereo Matching Algorithm with an Adaptive Window: Theory and Experiment](#), Proc. International Conference on Robotics and Automation, 1991.
- D. Scharstein and R. Szeliski. [Stereo matching with nonlinear diffusion](#). International Journal of Computer Vision, 28(2):155-174, July 1998

- Data from University of Tsukuba
- Similar results on other images with ground truth



Scene



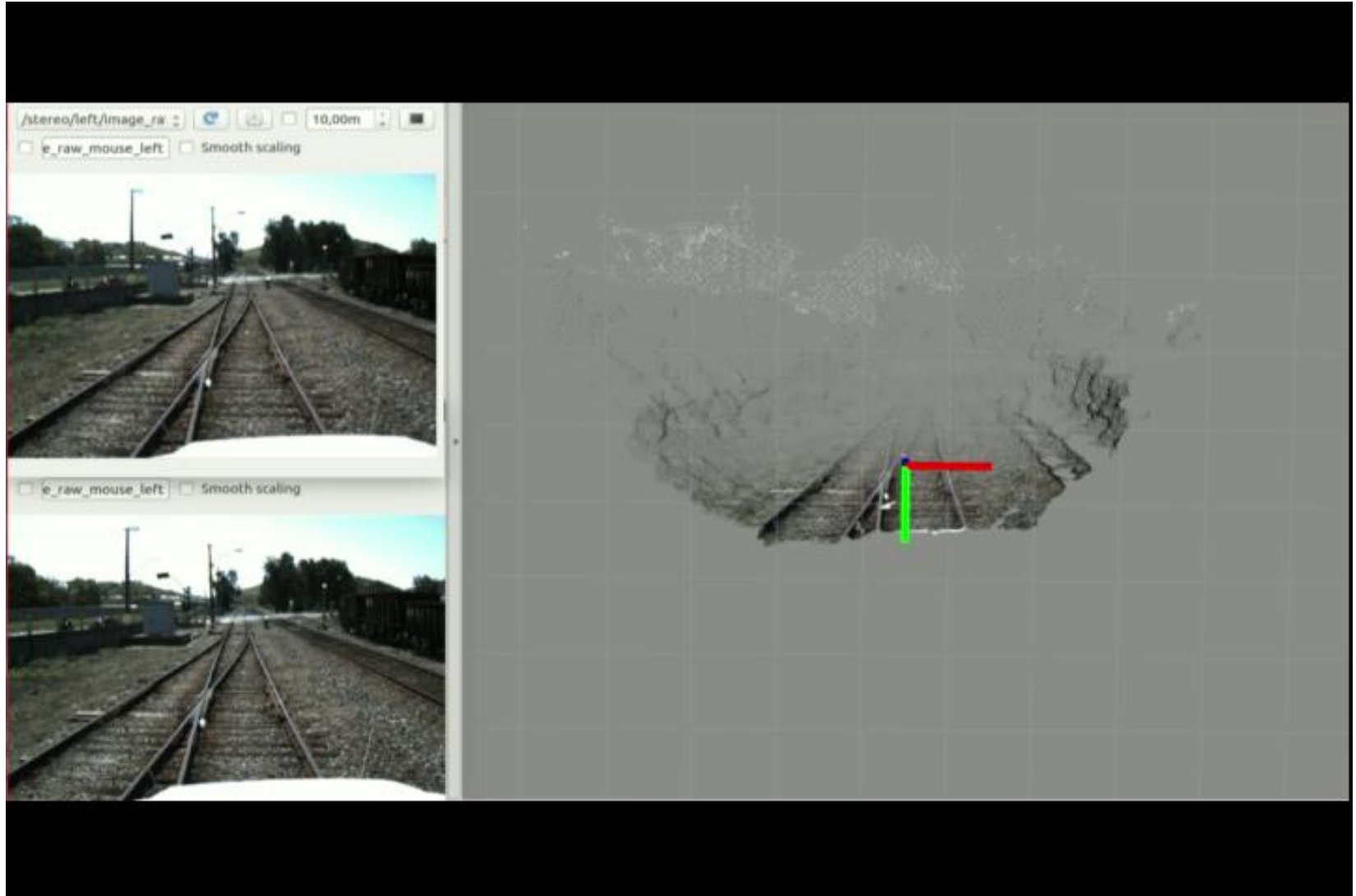
Ground truth



- Sistemas Embarcados de Vistoria (SEV)
  - Stereo vision system with two AVT Mako cameras
  - baseline is around 0.1 meters
  - horizontally aligned.



- Stereo Vision and SLAM





- **Errors** in stereo system comes from
  - Camera calibration errors
  - Poor image resolution
  - Occlusions
  - Violations of brightness constancy (specular reflections)
  - Large motions
  - Low-contrast image regions



- Stereo vision **steps**
  - Calibrate cameras
  - Rectify images
  - Compute disparity
  - Estimate depth



- `cvFindChessboardCorners`: detect chessboard corner in stereo images
- `cvStereoCalibrate`: calibrates stereo rig
- `cvStereoRectify`: computes rotations that make both camera planes the same.
- `cvInitUndistortRectifyMap` and `cvRemap`: use to compute undistortion map and rectified images
- Stereo correspondence (ex: `cvFindStereoCorrespondenceBM`): computes the disparity map.
- `cvReprojectImageTo3D`: disparity map to 3D with calibrated cameras



# OPENCV STEREO VISION DEMO



- Gary Bradski and Adrian Kaehler. *Learning OpenCV: Computer Vision with the OpenCV Library*. O'Reilly, Cambridge, MA, 2008.
- Olivier Faugeras Three-dimensional computer vision: a geometric viewpoint. MIT Press Cambridge, MA, USA ©1993
- Szeliski, R. (2010).. *Computer Vision: Algorithms and Applications*, Springer
- Quang-Tuan Luong. "[Learning Epipolar Geometry](#)". Retrieved 2007-03-04.