

PROGRAMMING IN PYTHON I

Recursion, Generators and Modules



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RECURSION



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- We know how to multiply, so we can solve this subtask immediately and we assume that the rest (x^{y-1}) is taken care of by our function.
- We let our function repeat this process, i.e., splitting into subtask and rest until we reach a state where the rest can also be solved immediately: x^y with $y = 1$ is $x^1 = x$. This is called a **base case** or **recursion anchor**.

Recursive Power Function

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    if y == 1: # base case  
        return x  
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- End of recursion reached: evaluate “backwards” until the initial power(2, 4) call: $2*2*2*2 = 16$
- Always implement the end of a recursion, otherwise, this will result in an endless recursion

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- There can be **multiple recursive calls** in the same function, either in different branches or even subsequent calls
- There can be **multiple ends** of a recursion (multiple base cases)
- Especially useful if the problem is already defined in a “recursive” way, e.g.:
 - Traversing through a tree-like data structure
 - Processing (potentially arbitrarily) nested data structures
 - Problems that can be solved with the “divide and conquer” principle (e.g., merge sort)

GENERATOR FUNCTIONS



Generator Functions (1)

- Writing **yield** within a function instead of **return** will make the function a so-called **generator function** that returns a generator iterator object

```
def generate_str_numbers(n):  
    for i in range(n):  
        yield str(i)
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- The code of a generator function is actually only executed when an element is requested, e.g., via a for loop:

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gen = generate_str_numbers(3)  # No execution  
for str_number in gen:        # Code is executed  
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- After reaching a **yield**, the specified value is returned and the **execution is suspended** until the **next element** is requested and the function is **resumed again**

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    while True:  
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- Elements of generators can also be accessed using the function `next(...)`:

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my_rnd_generator = infinite()  
for _ in range(3):  
    rnd = next(my_rnd_generator)  
    print(rnd)
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- If there are no more elements and you still call `next(...)`, this will result in an error (`StopIteration`)

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- In Python, we can do this by putting the function into a separate file (**module**)
- Naming convention for modules: lowercase letters + underscores (if needed)
- We can then load (**import**) this function definition from the file into our code file
- There are many modules with lots of functionalities available
 - You will write your own modules
 - We will learn about some important modules

Example for Importing a Module (1)

- Consider the file `my_module.py` in the same directory where your code is¹

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Example for Importing a Module (1)

- Consider the file `my_module.py` in the same directory where your code is¹
- Assume that the file contains a function `add`
- There are now several ways to import from this module:

```
import my_module # Can use everything within  
my_module.add(...)
```

```
import my_module as mm # Same but renamed  
mm.add(...)
```

```
from my_module import add # Can only use add  
add(...) # No module specification needed
```

```
from my_module import add as my_add  
my_add(...) # Same but renamed
```

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²They need not be empty, e.g., some initialization

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- Consider the same file `my_module.py` but in a package called `mypackage`

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- Python files can also be put into **packages** for better structuring your project
- Naming convention for packages: lowercase letters (underscores are discouraged)
- Packages are directories/folders that contain an empty `__init__.py` file²
- Consider the same file `my_module.py` but in a package called `mypackage`
- Again, there are several ways to import from this module (see next slide)

²They need not be empty, e.g., some initialization

Example for Importing a Module (3)

```
import mypackage.my_module  
mypackage.my_module.add(...)
```

```
import mypackage.my_module as mm  
mm.add(...)
```

```
from mypackage import my_module  
my_module.add(...)
```

```
from mypackage import my_module as mm  
mm.add(...)
```

```
from mypackage.my_module import add  
add(...)
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```
from mypackage.my_module import add as my_add  
my_add(...)
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- If you want this code only to be executed when running the module as a script (as your main starting code, e.g., via `python my_module.py`) and not when you import the module, you have to create this conditional check:

```
if __name__ == "__main__":  
    # Code that is only executed when run as a  
    script
```