# Supervised us unsupervised

The supervised learner doesn't know much



The unsupervised learner knows what it is doing



# Supervised learning tasks with networks

#### Node classification

- Given a network (e.g. friendship network) and some labels (e.g. political party). Can we predict the labels of a node from the labels of their neighbours?

#### Graph classification

- Given many networks (e.g. ego-networks, brain networks) and outcomes (e.g. political party, mental disorders). Can we predict the outcomes from the topology of the network?

#### Link prediction

- Given a network (e.g. friendship network) and optionally some metadata (e.g. political party). Can we predict which links we are missing (or will be created)?



Does this link exist?



Does this link exist?

#### Many tasks

#### 1. Model Validation

- Observe part of the adjacency matrix (fit model)
- Predict held out entries (cross validation)



Does this link exist?

- 1. Model Validation
- 2. De-noising / network reconstruction
- Real-world data are noisy / contain errors



Does this link exist?

- 1. Model Validation
- 2. De-noising / network reconstruction
- 3. Predict missing links
- Observed edges are assumed correct
- Predict which unobserved edges exist



Does this link exist?

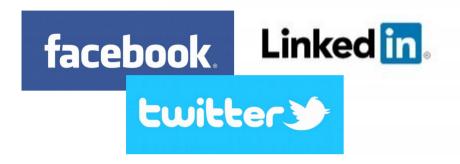
- 1. Model Validation
- 2. De-noising / network reconstruction
- 3. Predict missing links
- 4. Predict future links
- Observe the adjacency matrix at time (t)
- Predict edges in time (t+1)



Does this link exist?

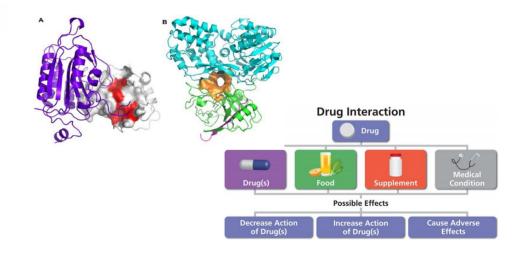
- 1. Model Validation
- 2. De-noising / network reconstruction
- 3. Predict missing links
- 4. Predict future links

### Applications



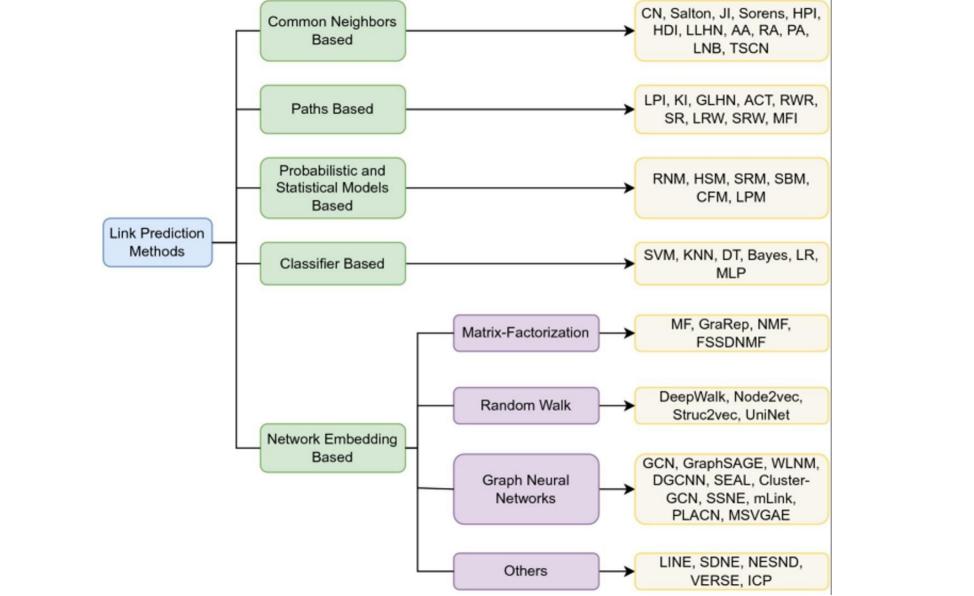
Suggesting social and professional connections

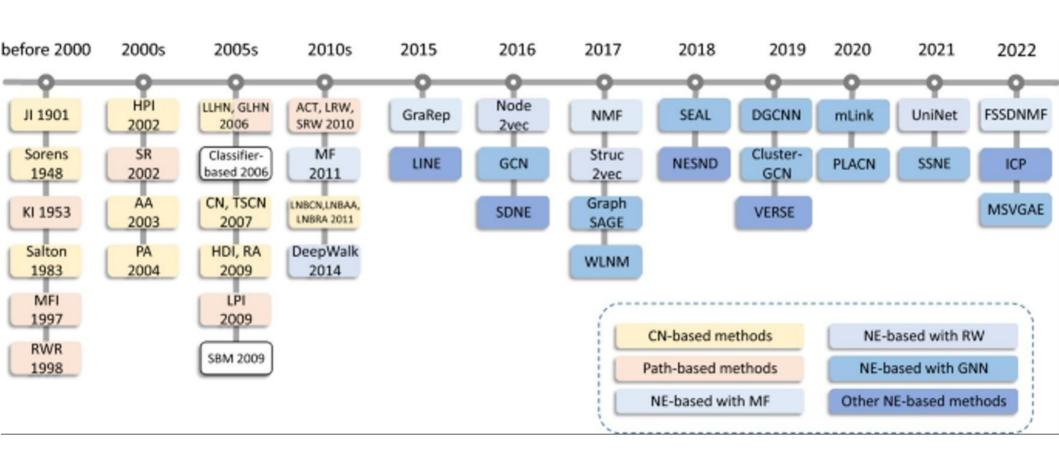
Predicting biological interactions





Recommending products and services



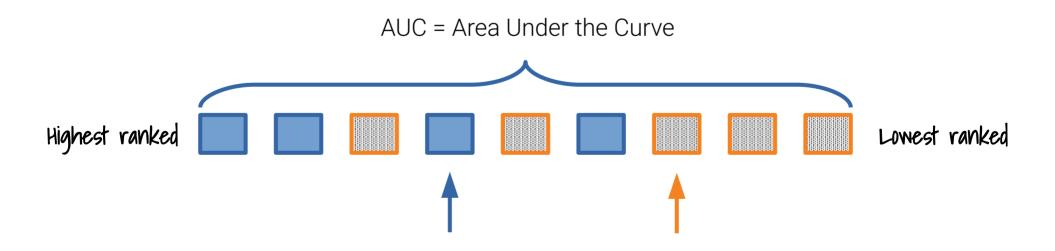


Link Prediction on Complex Networks: An Experimental Survey; Wu, Song, Ge, and Ge (2022)

# Predicting missing links

Goal: Rank all non-edges according to how likely they are to exist

Assessed using measures such as AUC



#### Local heuristics

Based on similarity of node connections

$$\Gamma(x) \leftarrow \text{neighbours of } x$$
 $k_x \leftarrow \text{degree of } x$ 

#### Similar neighbours

Common neighbours

$$s_{xy}^{\text{CN}} = |\Gamma(x) \cap \Gamma(y)|,$$

$$\Gamma(x) \leftarrow \text{neighbours of } x$$

#### Similar neighbours

Jaccard similarity

$$s_{xy}^{\text{Jaccard}} = \frac{|\Gamma(x) \cap \Gamma(y)|}{|\Gamma(x) \cup \Gamma(y)|}$$

$$\Gamma(x) \leftarrow \text{neighbours of } x$$

#### Similar neighbours

Cosine similarity

$$s_{xy}^{\text{Salton}} = \frac{|\Gamma(x) \cap \Gamma(y)|}{\sqrt{k_x \times k_y}}$$

$$k_x \leftarrow \text{degree of x}$$

$$\Gamma(x) \leftarrow \text{neighbours of x}$$

 $\Gamma(y)$ CN

**BCD** ABC 2 **ABC ABC** 

BC

 $\Gamma(x)$ 

**ABC** 

**ABC** 

CD CDE

Common Neighbours ignores degrees

Jaccard and Cosine provide similar rankings

Jaccard 0.66

0.5

0.33

0.25

0.2









Cosine

0.81

0.66

0.57



 $\Gamma(y)$ 

DE

DEFGH

 $\Gamma(x)$ 

**ABCDEF** 

**ABCDEF** 

Jaccard and Cosine do not always provide the same ranking!

CN

Jaccard

Cosine

Jaccard is biased towards nodes with similar degree

 $\Gamma(y)$ 

DE

DEFGH

 $\Gamma(x)$ 

**ABCDEF** 

**ABCDEF** 

Jaccard and Cosine do not always provide the same ranking!

Jaccard

0.38

0.33

CN

3

2

Cosine

0.55

0.58

Jaccard is biased towards nodes with similar degree

#### Other local heuristics

Adamic-Adar

Resource Allocation

$$s_{xy}^{AA} = \sum_{z \in \Gamma(x) \cap \Gamma(y)} \frac{1}{\log k_z}$$
  $s_{xy}^{RA} = \sum_{z \in \Gamma(x) \cap \Gamma(y)} \frac{1}{k_z}$ 

#### Other local heuristics

Adamic-Adar

Resource Allocation

$$s_{xy}^{AA} = \sum_{z \in \Gamma(x) \cap \Gamma(y)} \frac{1}{\log k_z} \qquad s_{xy}^{RA} = \sum_{z \in \Gamma(x) \cap \Gamma(y)} \frac{1}{k_z}$$

Preferential Attachment

$$s_{xy}^{\text{PA}} = k_x \times k_y$$

#### Other approaches

Global heuristics: Similar to local heuristics, but considering longer path lengths

Model based: Assign probability (or "likelihood") of edge existence

#### **SBM**